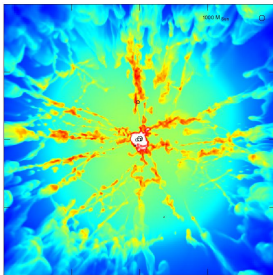
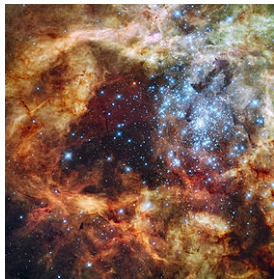


# Multiple stellar populations in globular clusters from winds of massive stars



Richard Wunsch

Zooming in on Star Formation, Nafplio, 13th June 2019

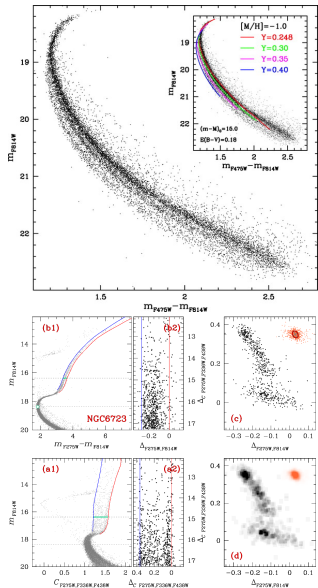


In collaboration with:

J. Palouš, G. Tenorio-Tagle, S. Silich, D. Szécsi, S. Martínez González,  
S. Ehlerová, C. Muñoz-Tuñón, S. Walch, D. Kománek

# Multiple stellar populations in GCs

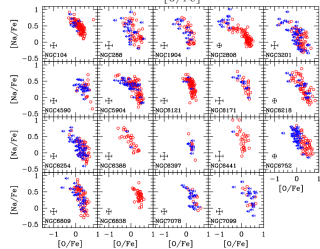
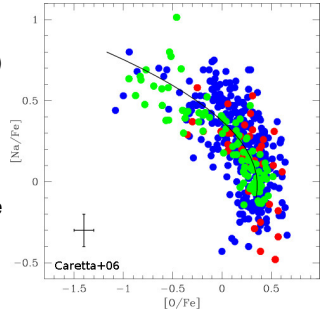
- **photometric evidence:**
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- **spectroscopic evidence:**
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- **correspond. between both (Milone+15)**
- **constant Fe (and other heavier elements):**
  - (exceptions:  $\omega$  Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- **universal for GCs:**
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- **variable pop. fraction:**
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$



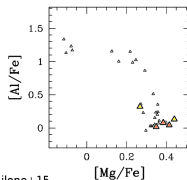
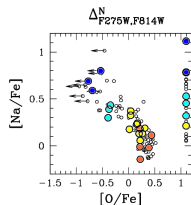
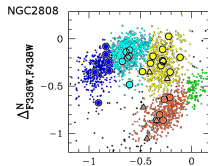


# Multiple stellar populations in GCs

- photometric evidence:
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- spectroscopic evidence:
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- correspond. between both (Milone+15)
- constant Fe (and other heavier elements):
  - (exceptions:  $\omega$ Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- universal for GCs:
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- variable pop. fraction:
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$



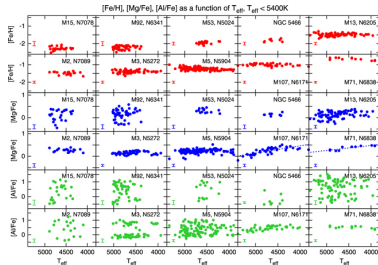
- **photometric evidence:**
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- **spectroscopic evidence:**
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- **correspond. between both (Milone+15)**
- **constant Fe** (and other heavier elements):
  - (exceptions:  $\omega$ Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- **universal for GCs:**
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- **variable pop. fraction:**
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$



Milone+15

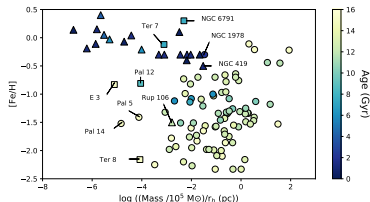
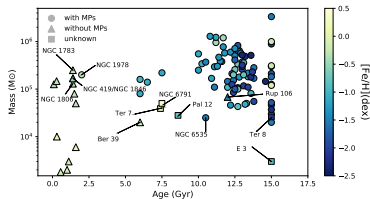
# Multiple stellar populations in GCs

- photometric evidence:
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- spectroscopic evidence:
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- correspond. between both (Milone+15)
- constant Fe (and other heavier elements):
  - (exceptions:  $\omega$ Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- universal for GCs:
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- variable pop. fraction:
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$



Mészáros+15

- photometric evidence:
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- spectroscopic evidence:
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- correspond. between both (Milone+15)
- constant Fe (and other heavier elements):
  - (exceptions:  $\omega$ Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- universal for GCs:
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- variable pop. fraction:
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$

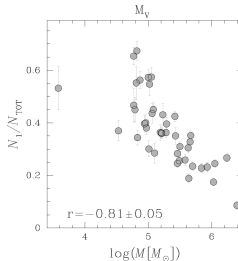
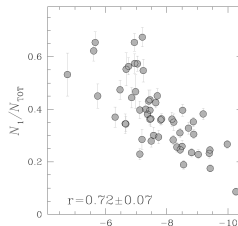


Bastian&Lardo18

(see review in ARA&A)

# Multiple stellar populations in GCs

- photometric evidence:
  - split main-sequence (also RGB, SGB, EHB, TO)
  - (Bedin+04, Piotto+07, Milone11,12,13,15, ...)
- spectroscopic evidence:
  - anticor. among pairs of light elements
  - (e.g. Na-O, Mg-Al, ...) Carreta+06,09 → signature of hot H burning (massive stars, AGB, SMS)
  - (e.g. Gratton+04, Charbonnel+05)
- correspond. between both (Milone+15)
- constant Fe (and other heavier elements):
  - (exceptions:  $\omega$ Cen, ... → anomalous GC)
  - no SN enrichment; origin from one cloud
- universal for GCs:
  - determined: M, [Fe/H], M/R?, age (2Gyr?)
- variable pop. fraction:
  - $N_1/N_{\text{tot}} = f(M, \dots)$ , but  $N_1/N_{\text{tot}} \neq (R_G, \dots)$



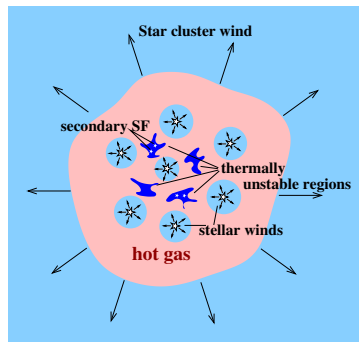
Milone+17

- self-enrichment scenario: 2G stars are formed out of winds of 1G stars  
→ **mass budget problems**: how to (i) produce enough enriched mass, and (ii) capture it?
- young massive clusters have winds  
stellar winds → collisions → shocked wind → outflow
- thermal instability, rapid cooling  
if the cluster is massive and compact enough
- dense warm/cold clumps are formed  
cluster gravity ⇒ clumps fall to the centre;  
accumulation ⇒ self-shielding against EUV radiation
- 2nd generation (2G) stars formed  
enriched by products of massive stars chem. evolution

## Basic parameters:

- $L_{SC}, \dot{M}_{SC} \leftarrow M_{1G}$ , stellar evolution tracks
- $R_{SC}$  + eventually radial profile ( $R_c, \beta$ )

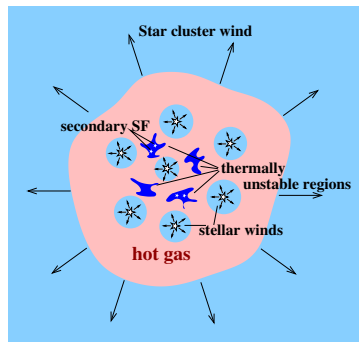
- self-enrichment scenario: 2G stars are formed out of winds of 1G stars  
→ **mass budget problems**: how to (i) produce enough enriched mass, and (ii) capture it?
- young massive clusters have winds  
stellar winds → collisions → shocked wind → outflow
- thermal instability, rapid cooling  
if the cluster is massive and compact enough
- dense warm/cold clumps are formed  
cluster gravity ⇒ clumps fall to the centre;  
accumulation ⇒ self-shielding against EUV radiation
- 2nd generation (2G) stars formed  
enriched by products of massive stars chem. evolution



## Basic parameters:

- $L_{SC}, \dot{M}_{SC} \leftarrow M_{1G}$ , stellar evolution tracks
- $R_{SC}$  + eventually radial profile ( $R_c, \beta$ )

- self-enrichment scenario: 2G stars are formed out of winds of 1G stars  
→ **mass budget problems**: how to (i) produce enough enriched mass, and (ii) capture it?
- young massive clusters have winds  
stellar winds → collisions → shocked wind → outflow
- thermal instability, rapid cooling  
if the cluster is massive and compact enough
- dense warm/cold clumps are formed  
cluster gravity ⇒ clumps fall to the centre;  
accumulation ⇒ self-shielding against EUV radiation
- 2nd generation (2G) stars formed  
enriched by products of massive stars chem. evolution

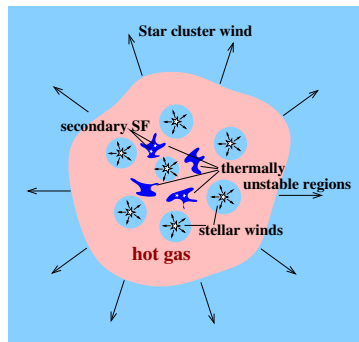


## Basic parameters:

- $L_{SC}, \dot{M}_{SC} \leftarrow M_{1G}$ , stellar evolution tracks
- $R_{SC}$  + eventually radial profile ( $R_c, \beta$ )



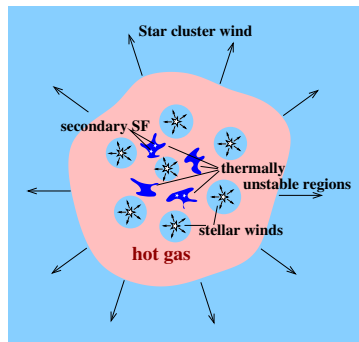
- self-enrichment scenario: 2G stars are formed out of winds of 1G stars  
→ **mass budget problems**: how to (i) produce enough enriched mass, and (ii) capture it?
- young massive clusters have winds  
stellar winds → collisions → shocked wind → outflow
- thermal instability, rapid cooling  
if the cluster is massive and compact enough
- dense warm/cold clumps are formed  
cluster gravity ⇒ clumps fall to the centre;  
accumulation ⇒ self-shielding against EUV radiation
- 2nd generation (2G) stars formed  
enriched by products of massive stars chem. evolution



## Basic parameters:

- $L_{SC}, \dot{M}_{SC} \leftarrow M_{1G}$ , stellar evolution tracks
- $R_{SC}$  + eventually radial profile ( $R_c, \beta$ )

- self-enrichment scenario: 2G stars are formed out of winds of 1G stars  
→ **mass budget problems**: how to (i) produce enough enriched mass, and (ii) capture it?
- young massive clusters have winds  
stellar winds → collisions → shocked wind → outflow
- thermal instability, rapid cooling  
if the cluster is massive and compact enough
- dense warm/cold clumps are formed  
cluster gravity ⇒ clumps fall to the centre;  
accumulation ⇒ self-shielding against EUV radiation
- 2nd generation (2G) stars formed  
enriched by products of massive stars chem. evolution



## Basic parameters:

- $L_{SC}, \dot{M}_{SC} \leftarrow M_{1G}$ , stellar evolution tracks
- $R_{SC}$  + eventually radial profile ( $R_c, \beta$ )

## Semi-analytic model:

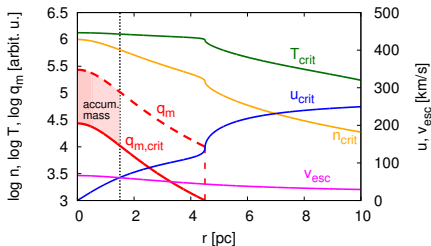
(Chevalier&Clegg+85, Silich+04, Wünsch+17)

$$\frac{1}{r^2} \frac{d}{dr} (\rho u r^2) = q_m$$

$$\rho u \frac{du}{dr} = -\frac{dP}{dr} - q_m u - \nabla \Phi$$

$$\frac{1}{r^2} \frac{d}{dr} \left[ \rho u r^2 \left( \frac{u^2}{2} + \frac{\gamma}{\gamma-1} \frac{P}{\rho} \right) \right] = q_e - Q$$

$$q_m, q_e \propto (1 + (r/R_c)^2)^{-\beta} \text{ for } r < R_{SC}$$



## Mass accumulation:

$$M_{\text{acc}}(t) = \int_{t_{\text{bs}}}^t \int_0^{R_{\text{esc}}} [q_m(r, t') - q_{m,\text{crit}}(r, t')] dr dt'$$

rate of the clump formation is given by  $q_m - q_{m,\text{crit}}$

only clumps formed with  $v < v_{\text{esc}}$  accumulate

## RHD simulations:

(Wünsch+17):

- AMR code Flash,  $512^3$  (finest) (Fryxell+00)
- opt. thin cooling (Schure+09)
- fixed stellar gravity, self-gravity → tree code (Wünsch+18)
- ionising radiation → TreeRay (Wünsch, in prep.)

Semi-analytic model:

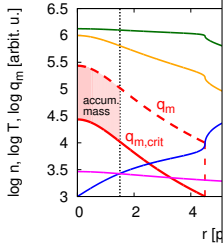
(Chevalier&Clegg+85, S

$$\frac{1}{r^2} \frac{d}{dr} (\rho U)$$

$$\rho U \frac{du}{dr} = - \frac{dP}{dr}$$

$$\frac{1}{r^2} \frac{d}{dr} \left[ \rho u r^2 \left( \frac{u^2}{2} + \right. \right.$$

$$q_m, q_e \propto (1 + (r/h$$



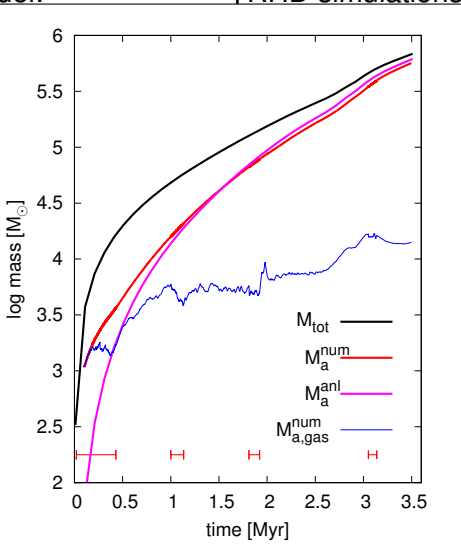
Mass accumulation:

$$M_{\text{acc}}(t) = \int_{t_{\text{bs}}}^t \int_0^{R_{\text{esc}}} [q_m$$

rate of the clump formation is g

only clumps formed with  $v < v_{\text{esc}}$  accumulate

, RHD simulations:



2<sup>3</sup> (finest)

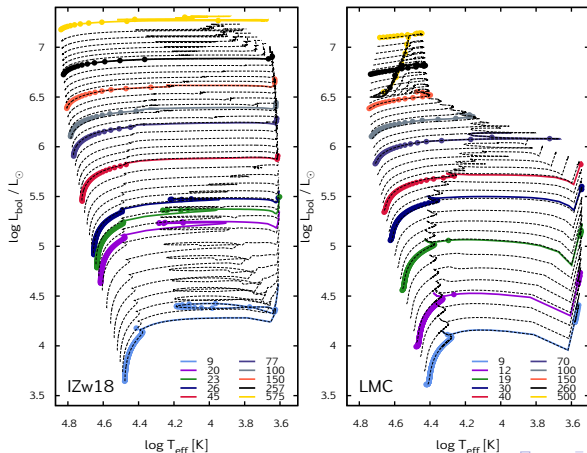
(Gure+09)  
self-gravity  
(Sh+18)

(in prep.)

- tracks by D. Szécsi (Bonn stellar evol. code)

→ Szécsi & Wunsch (2019)

- $M_{\max} = 500 M_{\odot}$ ,  $Z = 0.02 Z_{\odot}$  (IZw18) vs.  $Z = 0.4 Z_{\odot}$  (LMC)



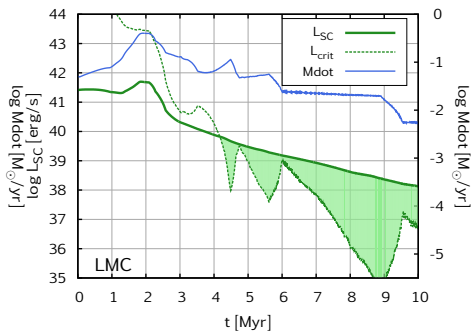
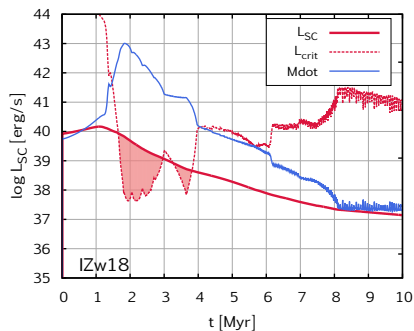
# RSG wind + hot star wind $\rightarrow$ cluster wind?



- convergence of the cluster consisting of hot stars to the smooth wind solution tested by [Cantó+00](#), [Raga+01](#),...
- however, does it work also for hot stars mixed with RSGs?
- mass and momentum inserted into a sphere with  $r = 4$  cells

- cluster with  $M = 10^6 M_{\odot}$  2.4 Myr includes:
  - 150 RSGs  $\rightarrow$  represented with 150 sources
  - $\sim 7000$  massive MS stars  $\rightarrow$  represented with 150 sources
  - $\Rightarrow$  marginally unstable (left)
- cluster with  $M = 10^7 M_{\odot}$  2.4 Myr includes:
  - $10\times$  more RSGs and hot stars  $\rightarrow$  represented by  $2 \times 150$  sources
  - $\Rightarrow$  fully thermally unstable (right)

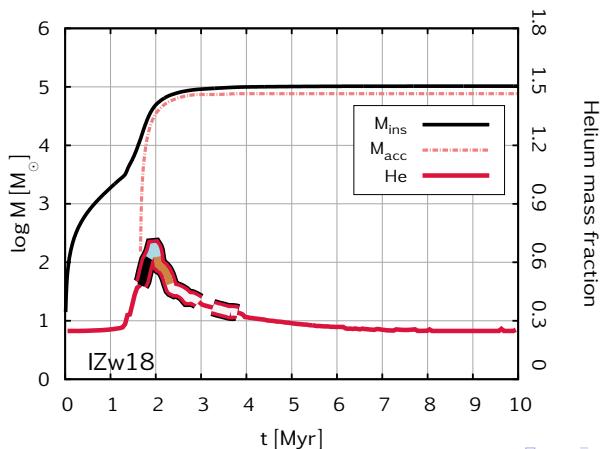
- period of instability:  $L_{SC} > L_{crit} \rightarrow$  mass accumulation
- low Z: 1.8 – 3.8 Myr (before SNe)
- high Z: 4.2 – 10 Myr (during SNe)



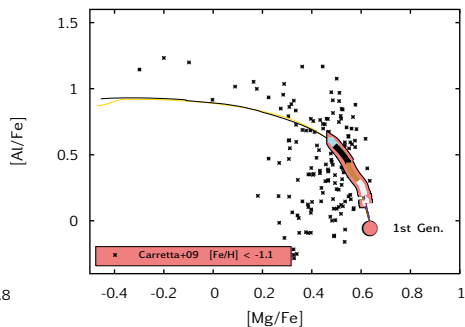
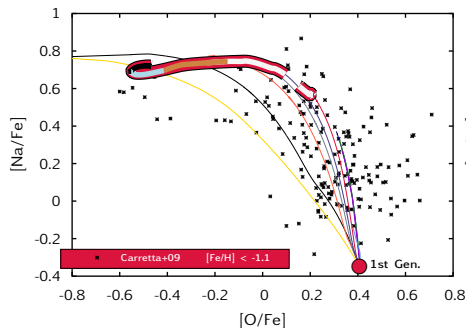


# Accumulated mass (for $M_{1G} = 10^7 M_{\odot}$ )

- inserted  $M_{\text{ins}} = 10^5 M_{\odot}$ , accumulated  $M_{\text{acc}} = 8 \times 10^4 M_{\odot}$  (80%)
- C+N+O constant  $\Rightarrow$  no He burning products (good!)
- He mass fraction in accum. mass: 0.7 (max), 0.52 (mean)

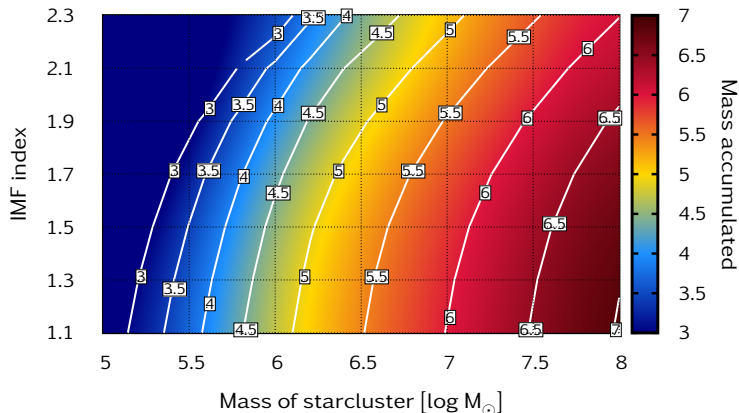


- Na-O: range reproduced well
- Mg-Al: predicted range smaller  
(some stars have correct chem. composition, however, their mass is not accumulated)



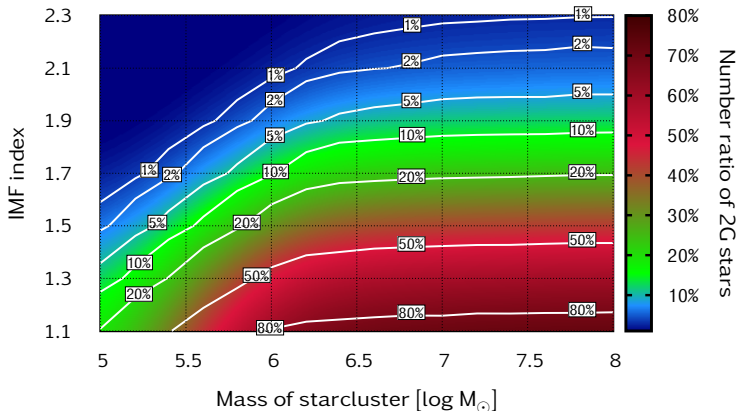
Varied parameters:

- first generation mass:  $M_{1G}$
- IMF high-mass slope:  $\alpha$  (Salpeter = 2.35)



# Param space: population ratio $N_2/N_{\text{tot}}$

- 2G stars form with standard IMF (not only low mass stars)
- only stars between  $0.08$  and  $0.8 M_{\odot}$  considered for  $N_1$  and  $N_2$
- no dynamical mass loss of the first generation assumed



What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**

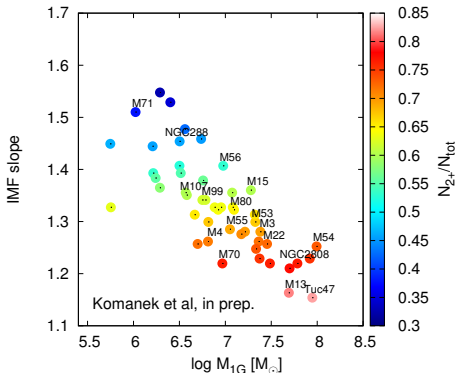
# Predicted IMF slope for Galactic GC

What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**



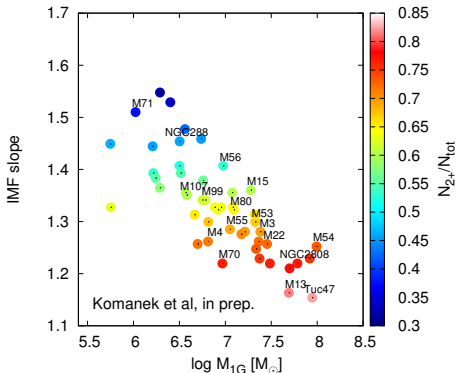
# Predicted IMF slope for Galactic GC

What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**



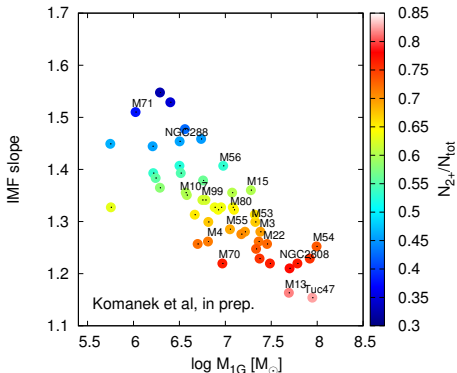
# Predicted IMF slope for Galactic GC

What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**





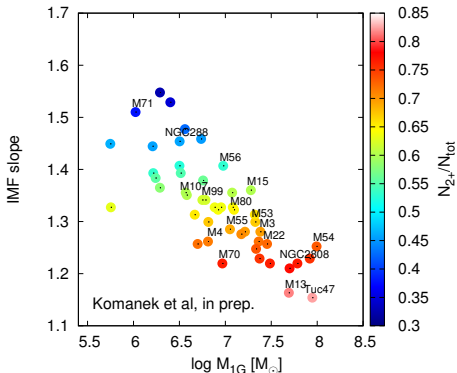
# Predicted IMF slope for Galactic GC

What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**



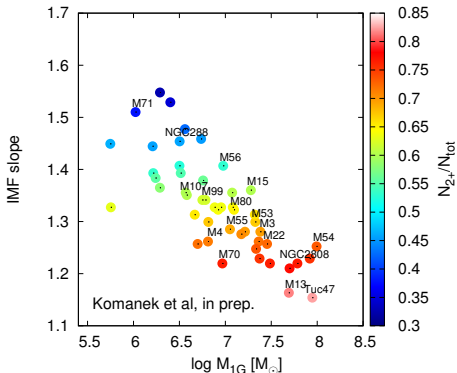
# Predicted IMF slope for Galactic GC

What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$

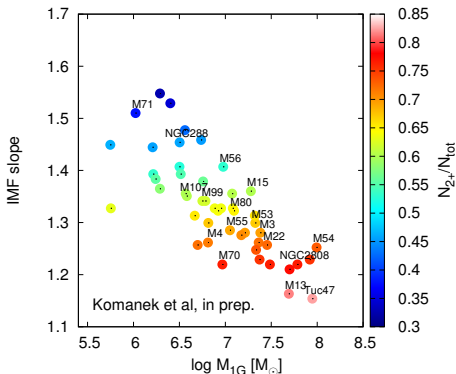


What IMF slope is needed to get the observed population ratios?

- $N_{2+}/N_{tot}$  for MW GC (Milone+17)
- $M_{GC}$  and  $R_{GC}$  (Baumgardt&Hilker18)
- stellar evolution:
  - $M_{GC} \rightarrow M_{1G}$  ( $\leftarrow$  IMF slope)
  - $R_{GC} \rightarrow R_{1G}$  ( $\leftarrow M_{1G}/M_{GC}$ , virial th.)
- for each GC, find IMF slope so that:

$$\left. \frac{N_{2+}}{N_{tot}} \right|_{\text{pred}} = \left. \frac{N_{2+}}{N_{tot}} \right|_{\text{obs}}$$

- IMF shallower for higher mass clusters (with higher  $N_{2+}$ ):
  - shallow IMF  $\rightarrow$  more massive stars  $\rightarrow$  more enriched mass
  - shallow IMF  $\rightarrow$  more massive cluster capture winds more efficiently
- **caveats: no dynamical mass loss, const  $Z_{1G} = 0.02Z_{\odot}$**



- Rapidly cooling shocked stellar winds + low Z stellar evolution models
- almost all massive stars winds (including fast ones) can be captured
  - 2G stars predicted to form in the cluster centre
  - chemical composition of the accumulated mass:
    - C+N+O = const, Na-O anticorrelation → OK
    - He mass fraction, Mg-AL anticorrelation → not so well
  - mass budget:
    - observed population ratios can be obtained with IMF slope  $\sim 1.1 - 1.6$ ; (Salpeter = 2.35)
    - with reasonable assumption about 2G IMF
    - dynamical mass lost of 1G can make this slope closer to the standard IMF
  - more massive clusters (with higher fraction of enriched population) need shallower IMF to form

# Thank you!