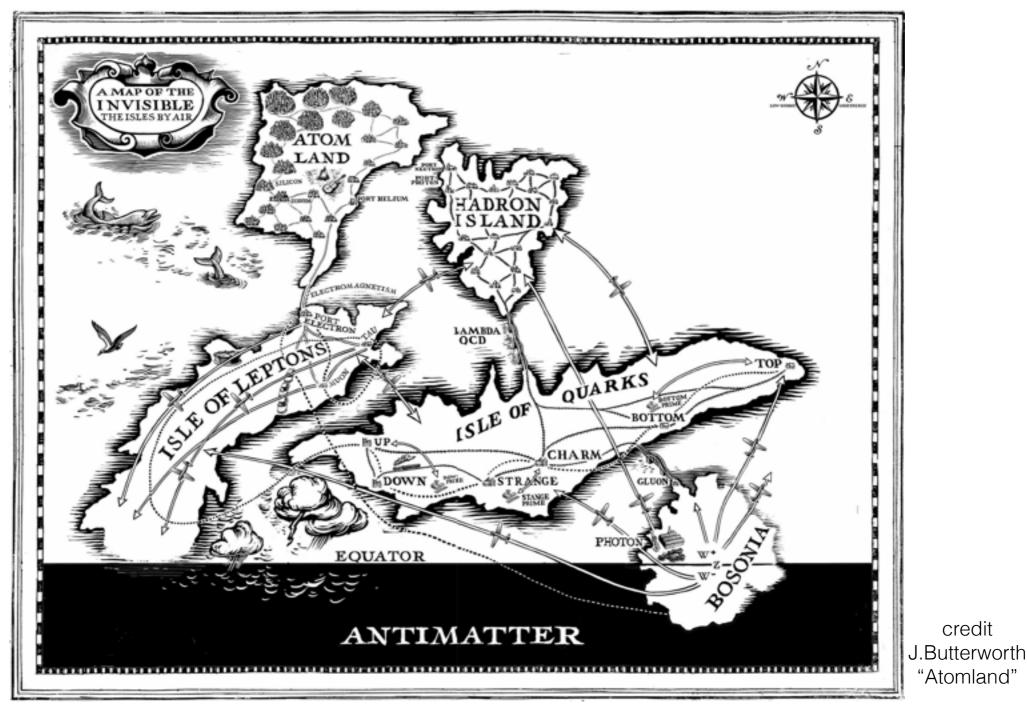
Topics in Experimental Particle Physics S. Xella

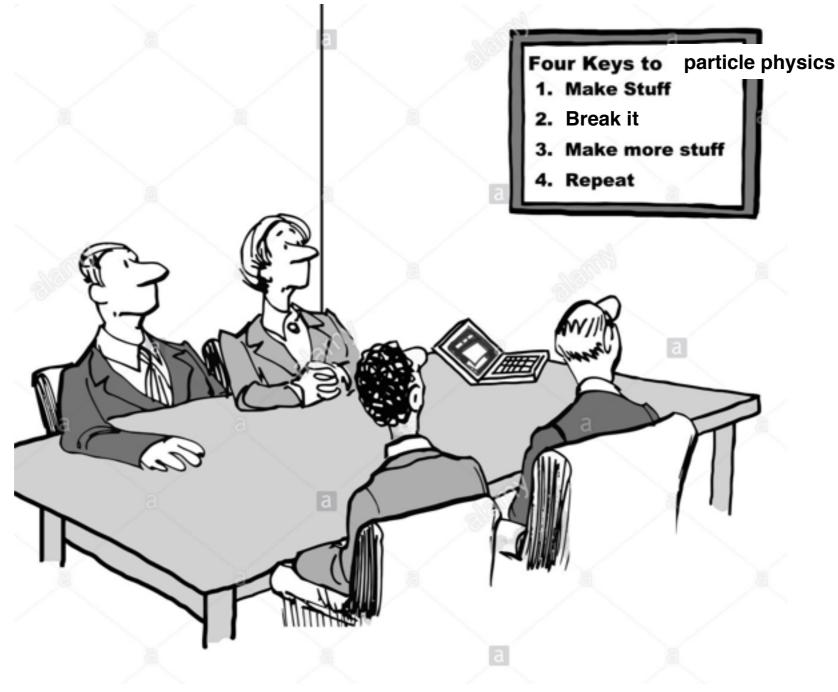


Content

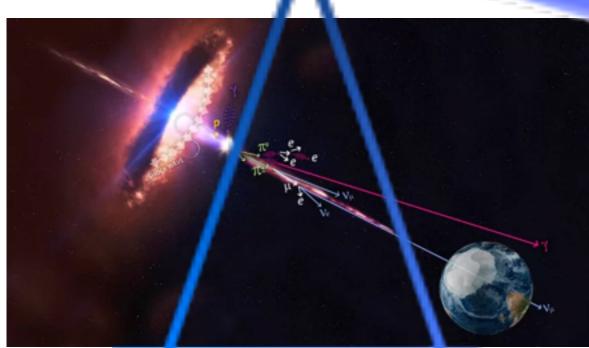
Focus of these lectures is accelerator-based particle physics.

- Lecture 1: Colliders. Focus: LHC. One experiment in details : ATLAS : detector+trigger+reconstruction of collisions.
- Lecture 2: What have we learnt about the Higgs boson so far.
- Lecture 3: New physics beyond the Standard Model: what can the LHC collider tell us (DM, neutrinos, matter-antimatter asymmetry).
- Lecture 4: Possible future accelerator-based research at CERN: FCC, SHiP, Mathusla, FASER. What can they tell us?

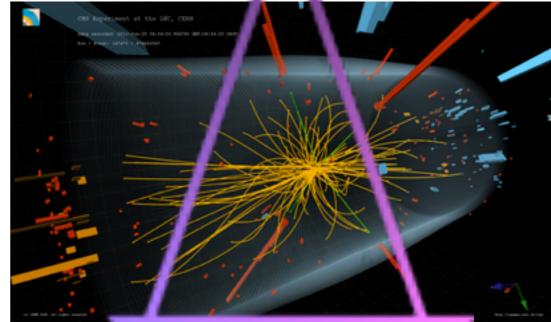
Why do we need accelerators?

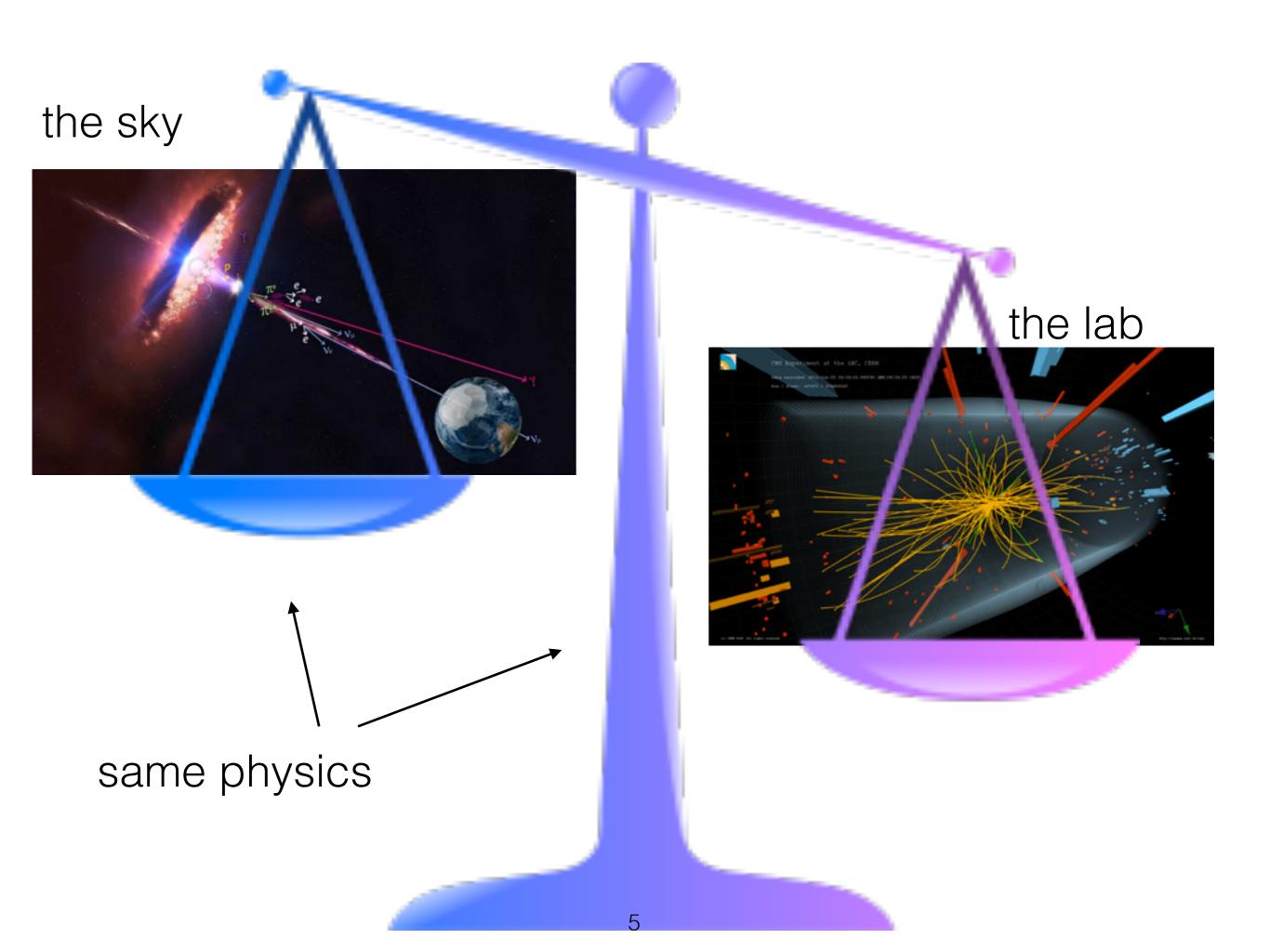






the lab





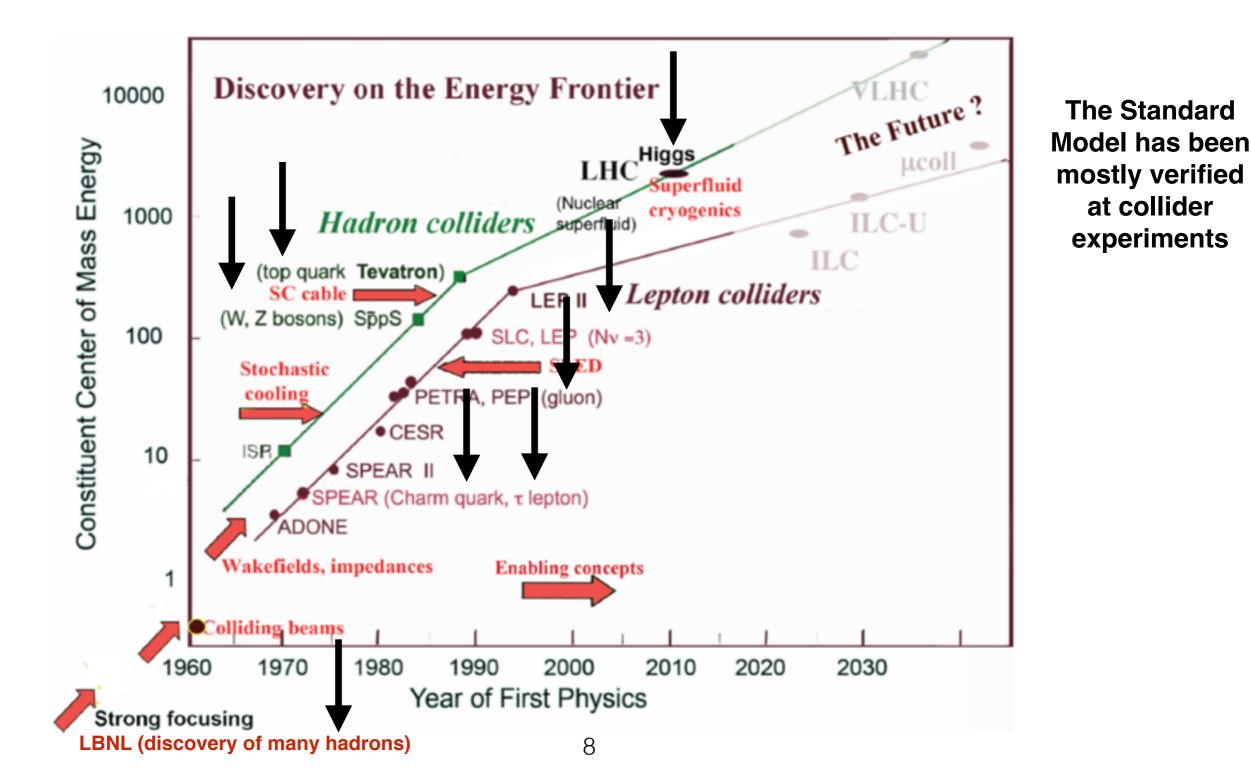
Why do we need accelerators

- **Precision tests of** particle physics **theory** are best carried out at accelerator facilities.
 - one can reproduce the outcome of an experiment over and over in the lab and verify definitely that only one interpretation (= theory) is correct.
- **Discoveries of new particle phenomena** are very trustworthy outputs of accelerator experiments : hadrons, J/psi, top quark, Higgs boson, CP violation in quarks processes,
- hints from theory or from previous observations are usefull in the first usecase (test of theory) : choice of energy and type and luminosity best suited for testing. For the second case (discovery), simply try to reach a new frontier in energy or intensity (& be lucky?) is a worthwhile approach.

Accelerators are not enough

- Neutrino or dark matter particle properties: questions not addressable with accelerators only. Need to exploit cosmic/atmospheric, nuclear reactors sources, etc... too.
- In general, the current big questions in particle physics are really big ! They need different simultaneous experimental approaches, to find answers. Theory is also of little guidance at the moment.

Discoveries by colliders



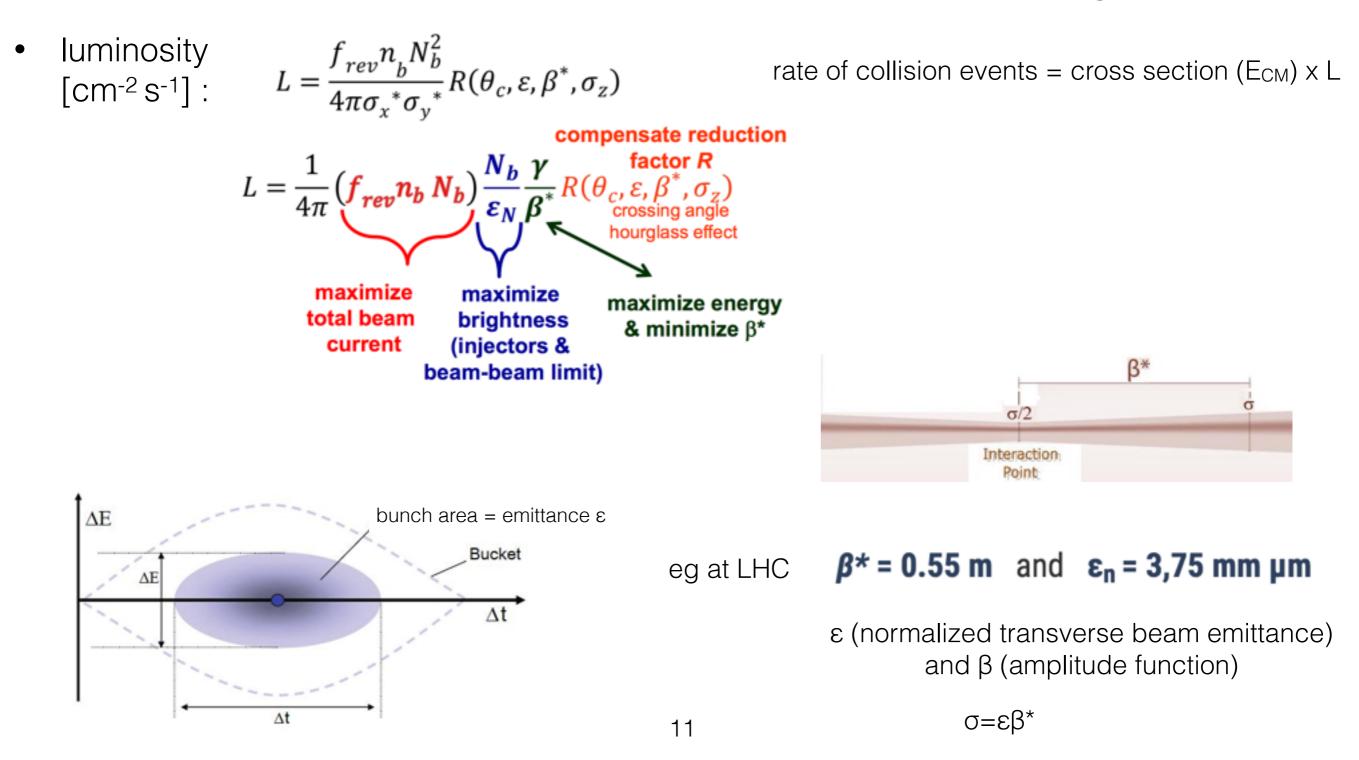
key parameters

accelerator types

key parameters of an accelerator: setup and energy

- setup: beam on target or collider? collider best :
 - E_{CM} (b-on-target)= $\sqrt{(mE)}$
 - E_{CM} (collider) = 2 E
- energy : circular collider vs linear collider.
 - circular: limited by the bending power of the magnets (dipoles). For a given fixed radius (eg LHC, re-using LEP tunnel), energy is limited by the maximum magnetic field achievable. Super-conducting coils, large currents (10 kAmps -> ~ 8 Tesla at LHC) is best method achievable so far.
 - linear : limited by the size mainly. much longer instrumented beampipe needed to achieve same energy as in circular collider. eg @ LHC accelerating units 5MV/m x 0.5 m x 8 units, 16 MeV per turn in LHC to bring 450 GeV-> 7 TeV in 10.000 turns per sec and 20 min

key parameters of an accelerator: luminosity



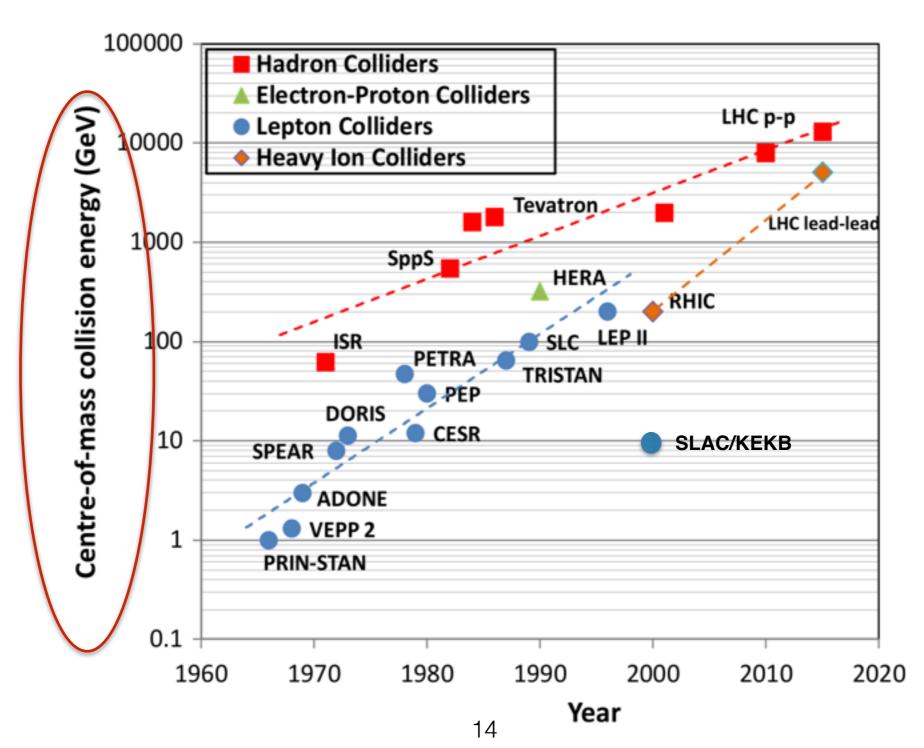
Which type of colliders is usefull to build

- high energy means probing early times of Universe life, means studying something new and likely discovering something interesting, so hadron colliders are best
 - harder to achieve high E with light particles, eg electron beams, in circular collider due to synchrotron radiation energy loss : P~ E⁴/m⁴. Easier with heavier particles, eg protons. electron beam fill needs to be topped up continously, while proton beam fill can be stable for hours.
 - p-antip Tevatron first (~1 TeV), then p-p LHC (~10 TeV), then maybe p-p FCC later (~100 TeV)

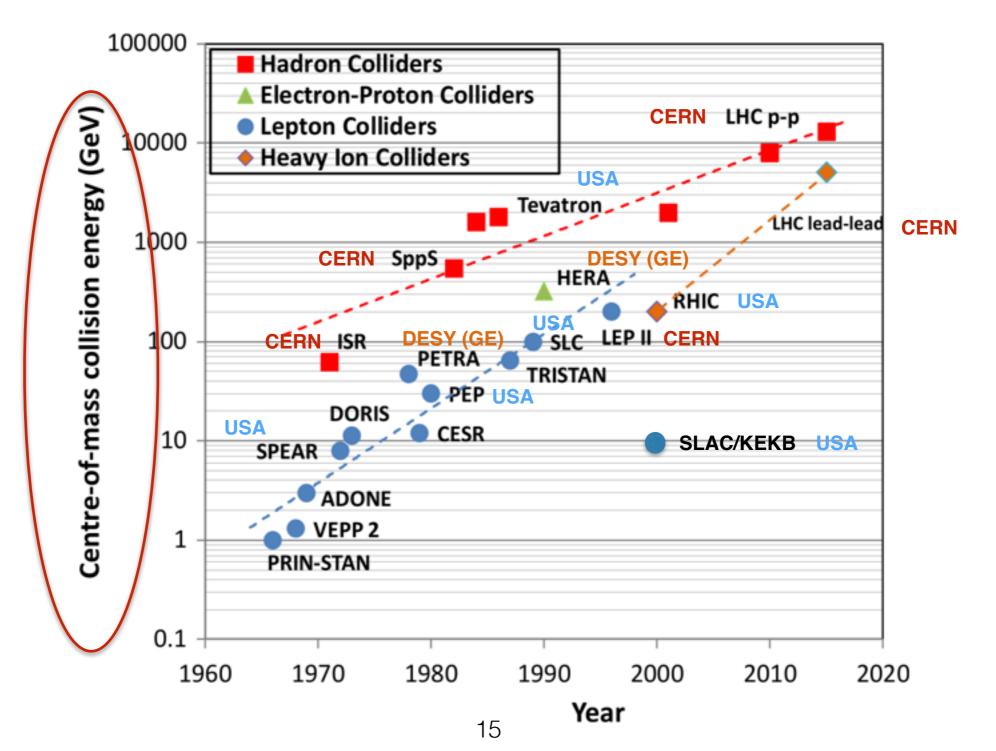
Which type of colliders is usefull to build

- hadron collisions' debris are more difficult to reconstruct precisely than lepton collisions' ones.
 - in hadron colliders, collisions happen between partons in the proton, whose energy and direction is unknown. in lepton colliders one has very good control of these two parameters and can use them to further constraint the output products (energy, momentum conservation rules can be applied)
- typically you would alternate these two types, to achieve the most precise understanding of particle physics processes at a given energy regime
 - e+e- LEP and then p-p LHC, p-p LHC and then maybe e+e- ILC, etc....

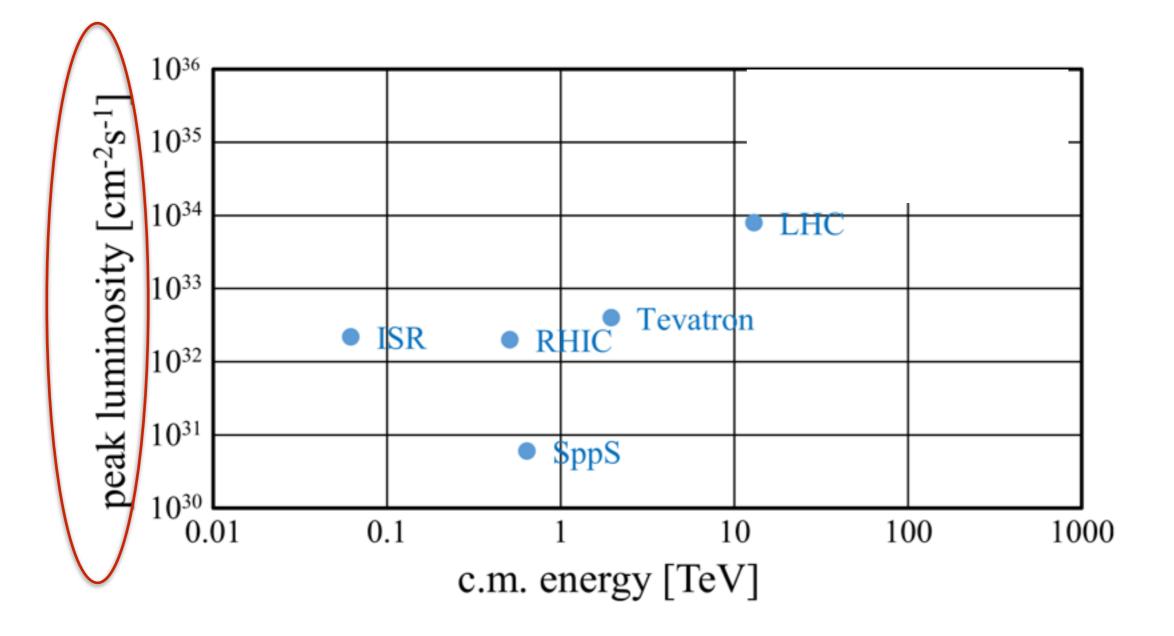
Which type of colliders have been built so far



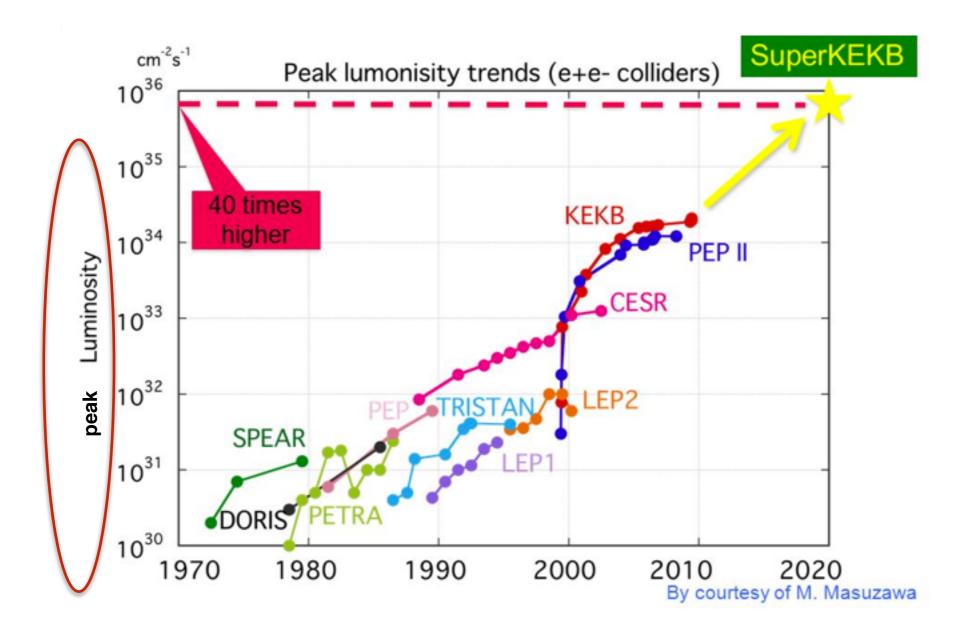
Which type of colliders have been built so far



Which type of colliders have been built so far : hadron colliders



Which type of colliders have been built so far : e+e- colliders



CERN Accelerator Complex

Large Hadron Collider (LHC) Lake Geneva

Geneva

Airport

CERN LAB 2 (France)

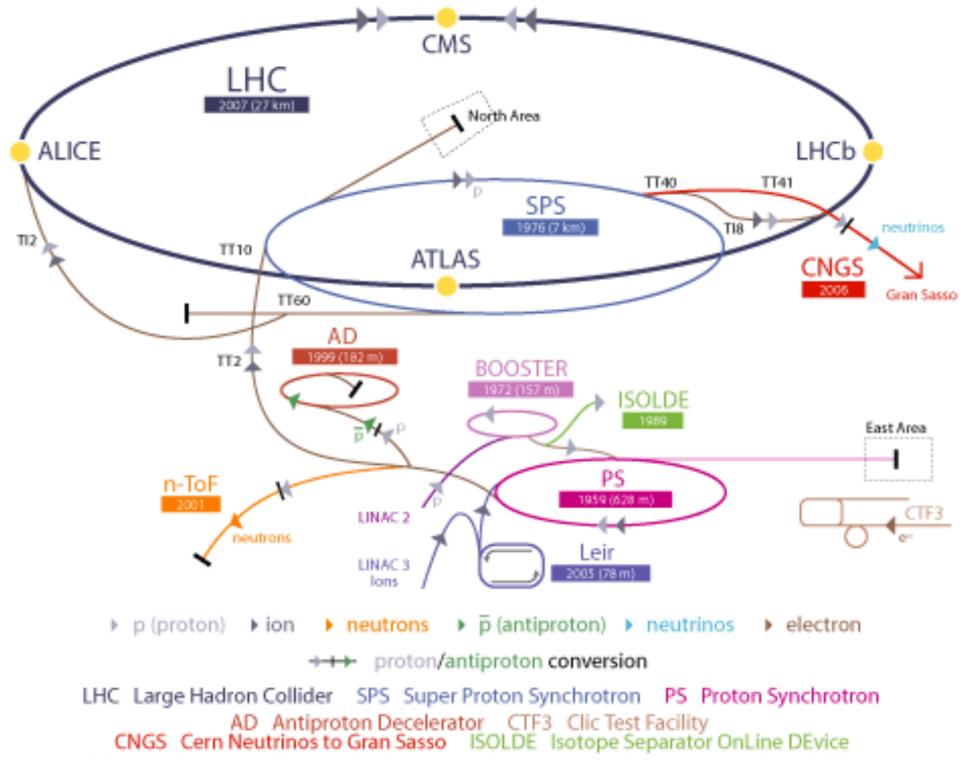
Super Proton Synchrotron

27km long 150m underground

CERN LAB 1 (Switzerland)

Proton Synchrotron (PS)

CERN Accelerator Complex



LEIR Low Energy Ion Ring LINAC LINear ACcelerator n-ToF Neutrons Time Of Flight

LHC: fun facts

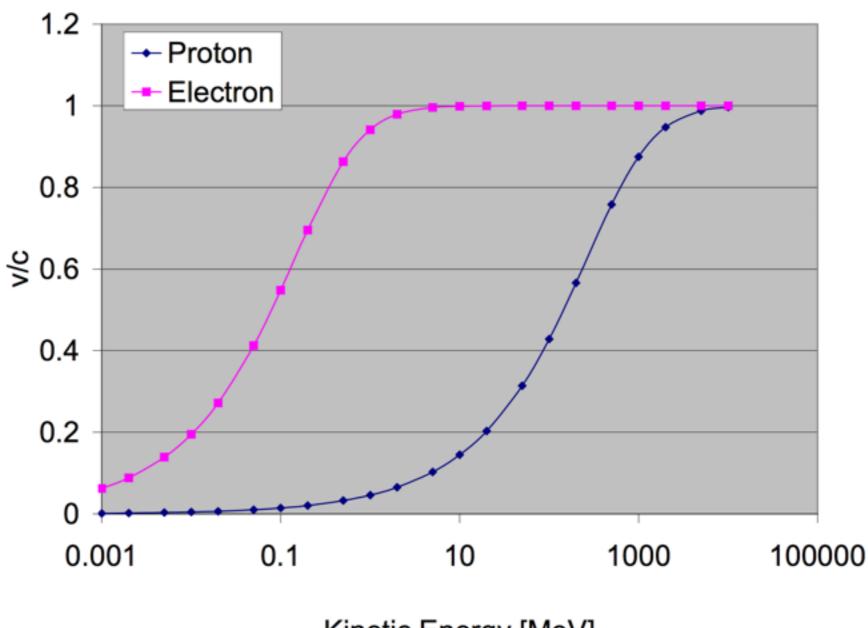
- The space within the LHC beam pipe is one of the emptiest spaces in the Solar System. In fact, it is an ultra-high vacuum and is as empty as outer space. This is to ensure that the protons do not collide with molecules of gas. The internal pressure is 10⁻¹³ atmosphere, which is 10 times less than the pressure on the Moon during the day! As the beam pipes are cooled to extremely low temperatures, the gases condense and adhere to the walls of the beam pipe by adsorption. Two weeks are needed to reach 10⁻¹³ atmosphere.
- In the cryomagnets, insulation vacuum is maintained by cryogenic pumping of 9000 cubic metres of gas. Like pumping down a cathedral.
- Only two nanograms of hydrogen are accelarated each day, which means it would take almost a year for the LHC to accelerate 1 gram of hydrogen.
- The beams throw off billions of stray particles that will heat up anything they hit, and they pass within about a centimeter of thousands of superconducting magnets that have to be kept colder than the vacuum of outer space. If stray particles damage the magnets, the collider could be forced to shut down for weeks, months, or more
- When two beams of protons collide, they will generate temperatures more than 100,000 times hotter than the heart of the sun, concentrated within a miniscule space.

LHC: fun facts

- The LHC can be called the world's largest fridge, because the thousands of magnets within the accelerator are pre-cooled to -193.2°C (80 K) using 10,080 tons of liquid nitrogen, after which they are filled with more than 60 tons of liquid helium to further cool them down to -271.3°C (1.9 K).
- When this amazing machine operates in full power, trillions of protons race around the circumference of the tunnel 11,245 times a second, at a speed that is 99.999991% of the speed of light, which is equivalent to 671,000,000 mph!
- The cost of building the LHC was estimated around USD 4.1 billion. Not only this, it
 has a running budget of approximately USD 1 billion per year, which makes it one
 of the most expensive scientific instruments ever built. Still, it costs less than what
 US spends in a few weeks of military operations in Middle East.

CERN accelerator complex

- to achieve stable beams at 13 TeV in the LHC, it is necessary to have a set of accelerators bringing the particles slowly up from 0 to the nominal energy.
- the pre-existing accelerators needed only minor modifications to achieve nominal LHC beams energy.
- no single machine to achieve the same. CERN is a unique place in the world for this.



Kinetic Energy [MeV]

This has important implications for the type of acceleration scheme that is appropriate for protons, wrt electrons. Electrons at the source already are relativistic. Protons are not.

PS, SPS and LHC require different components functionality for accelerating and keeping in orbit

The Synchrotron (circular collider)

 The bending field changes with particle beam energy to maintain a constant radius:

$$\frac{1}{\rho[m]} = 0.3 \frac{B[T]}{\beta E[GeV]} = 0.3 \frac{B[T]}{cp[GeV]}$$

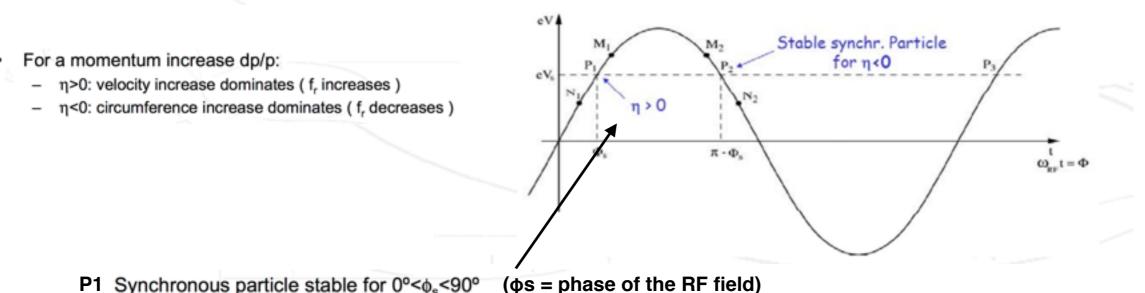
- So B ramps in proportion to the momentum. The revolution frequency also changes with momentum.
- The synchronicity condition, including the relativistic mass, is:

$$\omega = \frac{qB}{m\gamma}$$

- For an electron synchrotron, the injected beam is already relativistic at source,
 so only the magnetic field changes with beam energy.
- For a proton synchrotron, the injected beam is not yet relativistic at source, so the RF accelerating frequency and the magnetic field both ramp with energy.

acceleration

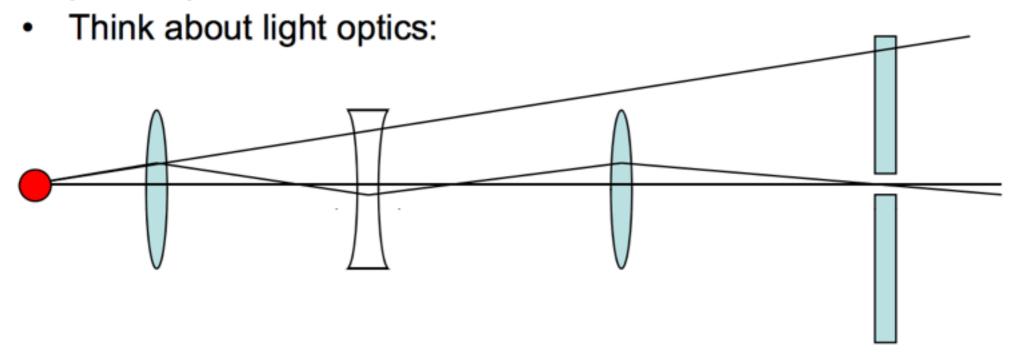
- Summary: to ramp up the energy in a synchrotron
 - Simply ramp up the magnetic field (bending units) while RF increases (E increases)
 - With the (automatic) RF frequency modulation the synchronous particle will stay on the reference orbit (keep right E)
 - Due to the phase-stability, the particles in the phase-space vicinity of the synchronous particle will be captured by the RF and will also be accelerated at the same rate, undergoing synchrotron oscillations (stay close to the desired energy)



- A particle N₁ arriving early with φ=φ_s-δ will get a lower energy kick, and arrive relatively later next pass
- A particle M₁ arriving late with φ=φ_s+δ will get a higher energy k₂ck, and arrive relatively earlier next pass

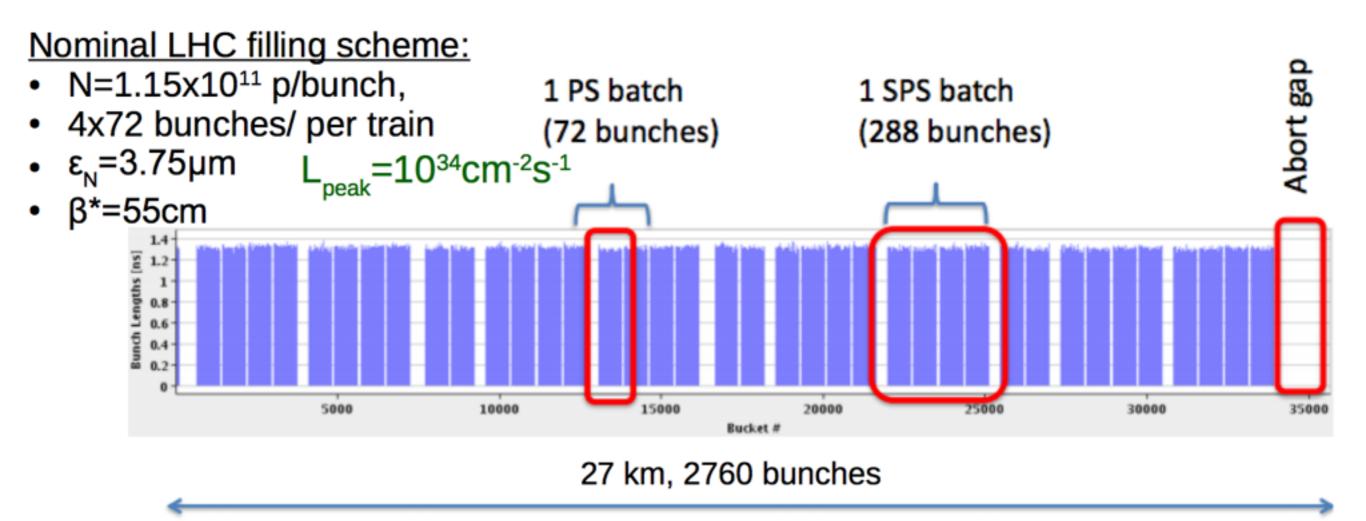
Particle Beam Focusing

 Suppose two particles start the acceleration process. One has exactly the correct energy, position and angle, so that it is properly accelerated. The accompanying particle has slightly different starting parameters. We need some way of ensuring that nonperfect particles are also accelerated.



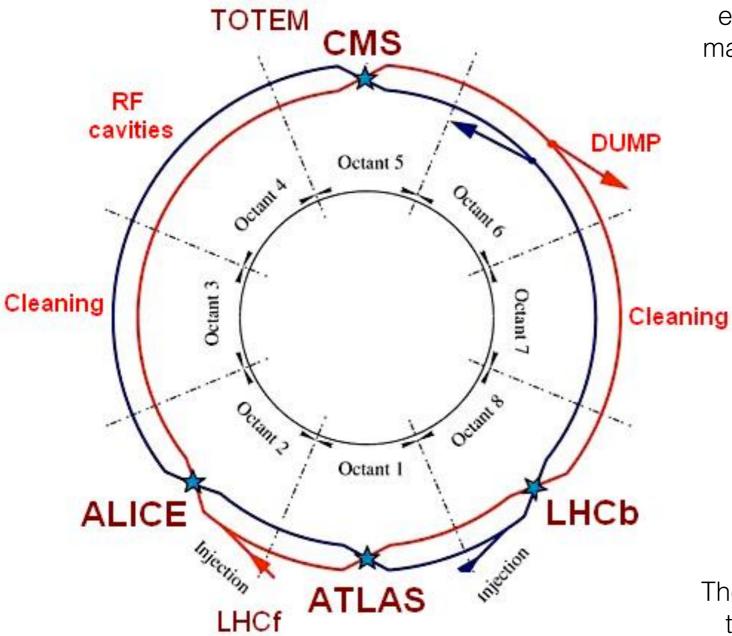
- This concept was first applied to particle accelerators by Courant, Livingston, and Snyder.
- It is known as "Strong Focusing" or "Alternating Gradient Focusing".
- "Optical" magnetic elements provide focusing

LHC filling scheme



LHC

eight arcs (~3 km long) and eight straight 'insertions' (~ 0.5 m long).



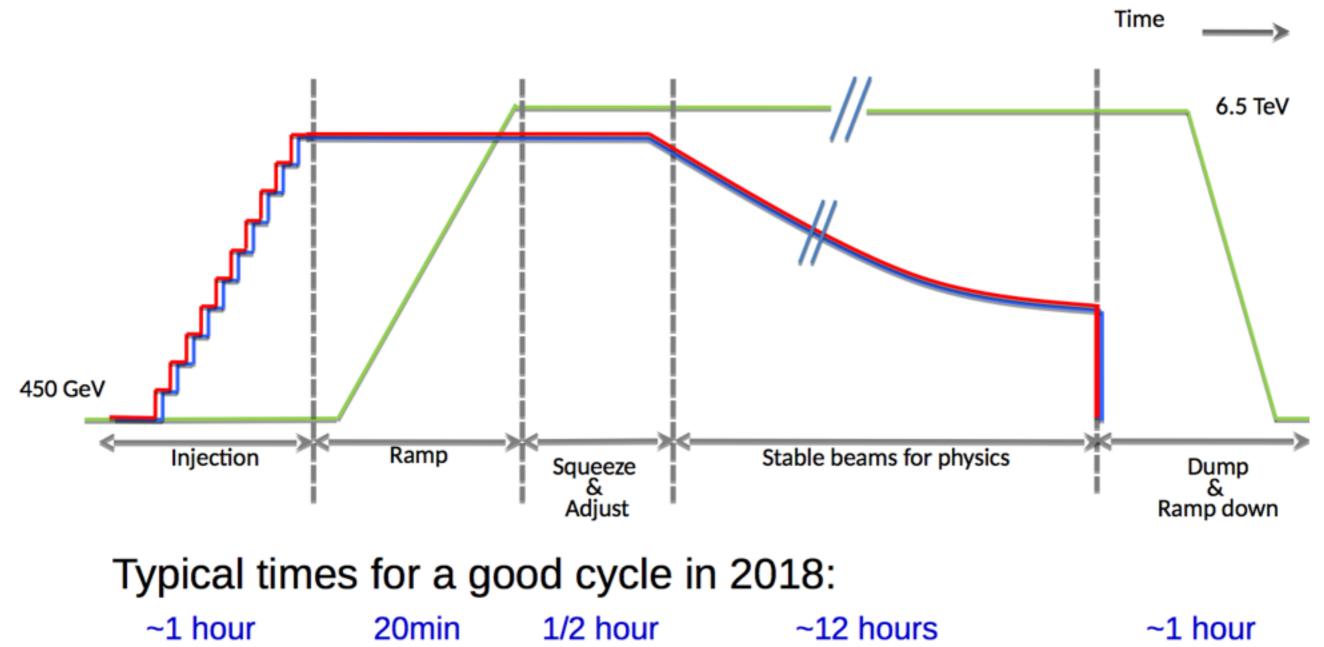
The arcs contain the dipole 'bending' magnets, with 154 in each arc. Each arc contains 23 arc cells, and each arc cell has a FODO structure (main dipole magnets + quadrupole magnets + other multipoles magnets), 106.9 m long.



The exact layout of the straight section depends on the specific use of the insertion: physics (beam collisions within an experiment), injection, beam dumping or beam cleaning.

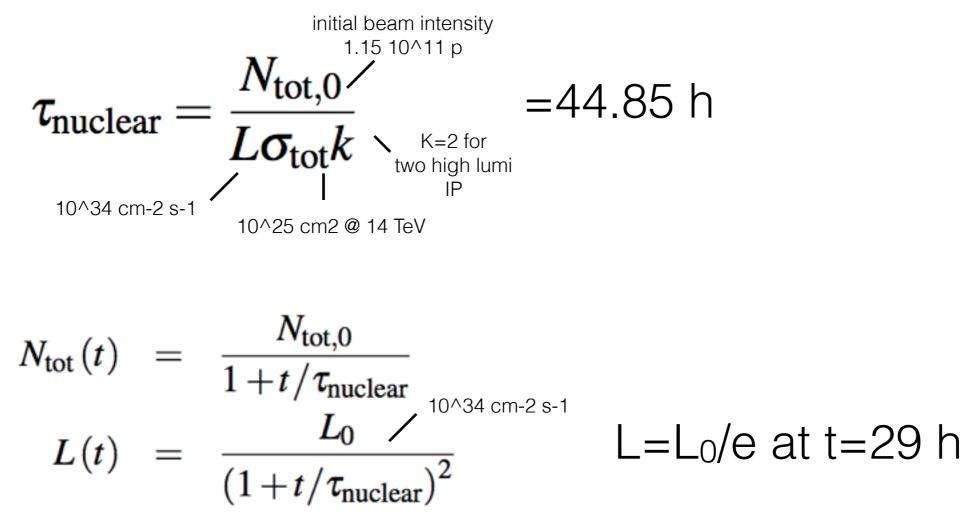
LHC Operational Cycle

- = Field in main magnets
- = Beam 1 intensity (current)
- Beam 2 intensity (current)



LHC limitations

- lifetime limitation :
 - beam loss from collisions is main loss



LHC limitations

- lifetime limitation :
 - the scattering of particles on residual gas
 - IBS scattering

$$\frac{1}{\tau_L} = \frac{1}{\tau_{\text{IBS}}} + \frac{1}{\tau_{\text{rest gas}}} + \frac{1}{\tau_{\text{nuclear},1/e}}$$
$$\tau_L = 14.9 \ h.$$

RF cavities : acceleration



A particle exactly synchronised with the RF frequency is called synchronous particle. All the other particles in the accelerator will oscillate longitudinally around the synchronous particles under the influence of the RF system. This means that instead of being spread uniformly around the circumference of the accelerator the particles get "clumped" around the synchronous particle in a BUNCH. This bunch is contained in an RF bucket.

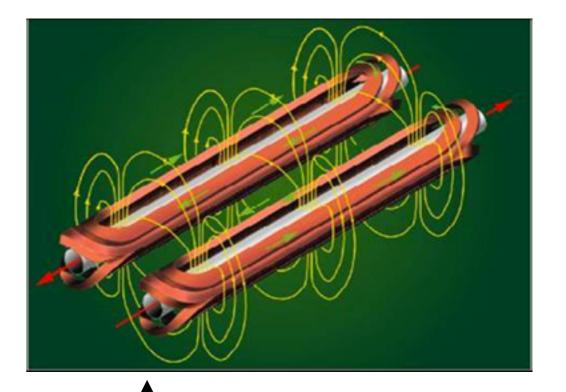
 $h = f_{RF}/f_{rev} = (400 \cdot 10^{6} \text{ Hz})/(c/26659 \text{ m}) = 35640$ RF buckets (points where synchronous particle sees a accelerating voltage)

Superconducting cavities with small energy losses (synchrotron radiation) and large stored energy : they keep particles bunched and they give power during acceleration

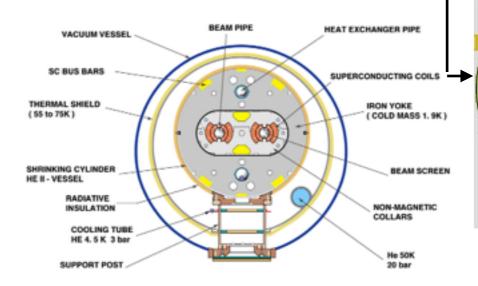
Dipole magnets: bending

The dipolar magnetic field is created for superconductive currents which circulate on each side of the pipe by where the protons travel. The wiring is arranged in individual double layers around each tube

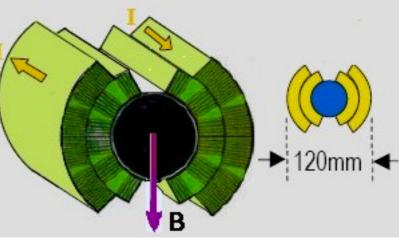
160 superconducting cables, 6500 superconducting filaments of Niobium-titanium



the total superconducting length in the 1232 dipoles (2 tubes per dipole): 1,38·10¹² m = 10 times the distance Earth-Sun

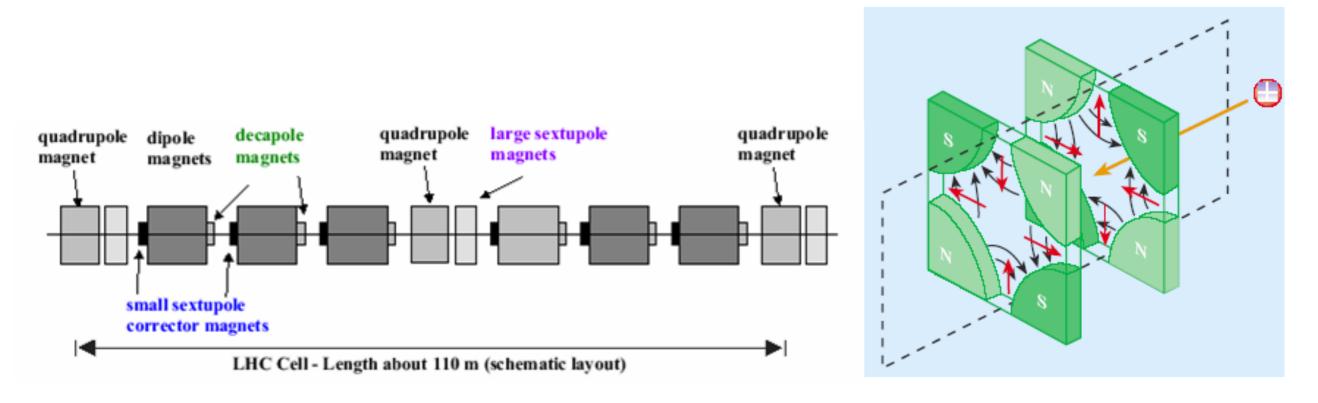


CROSS SECTION OF LHC DIPOLE



temperature 1.9 Kelvin

Quadrupole magnets: focusing



858 quadrupole magnets in the LHC

2808 bunches per beam and a very high intensity $(1.15 \times 10^{11} \text{ protons per bunch})$; this requires 9300

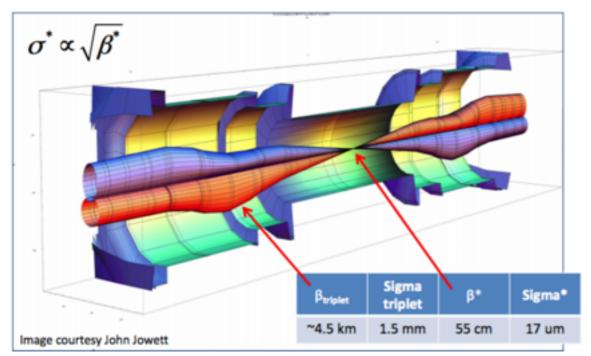
superconducting magnets of different types http://lhc-machine-outreach.web.cern.ch/lhc-machine-outreach/ components/magnets/types_of_magnets.htm

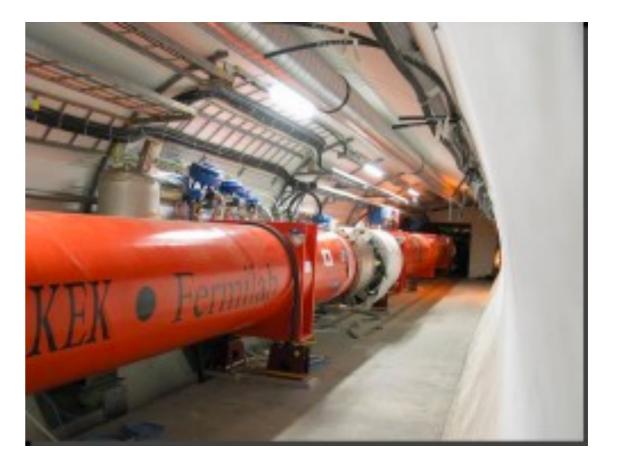
Triplet magnets near IP: collisions

35

"inner triplet", final focusing, superconducting magnets in the LHC. Their job is to focus the particle beams into the four areas where particles will collide. The size of bunches passes from 0,2 mm to 16 micrometers at the Interaction Points (IP):

at IP (ATLAS, CMS) 16 μm
in the triplets ~1.6 mm
in the arcs ~0.2 mm



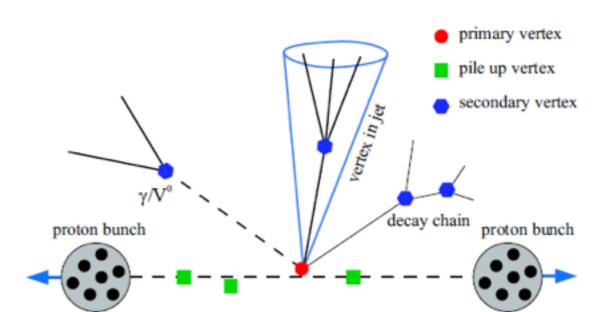


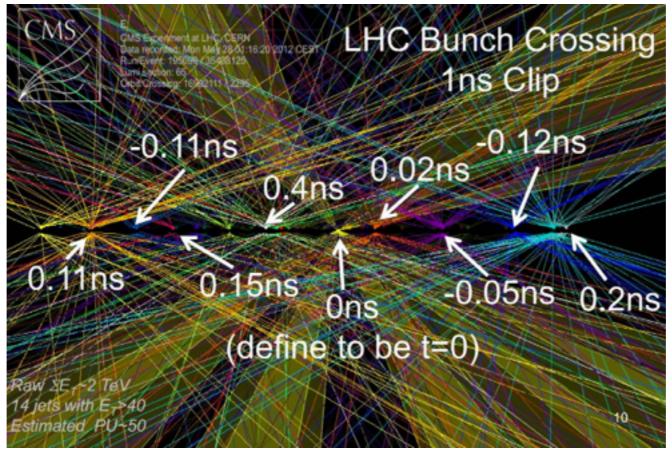
Pile-up

bunch collision rate
= #bunches/beam x revolution frequency

#events per bunch crossing
= cross section x luminosity / bunch collision rate

nominal #events per bunch crossing in the detector = 8.5×10^{-26} cm² 10^{34} cm⁻²s⁻¹ / (32 × 10⁶ s⁻¹) = 27

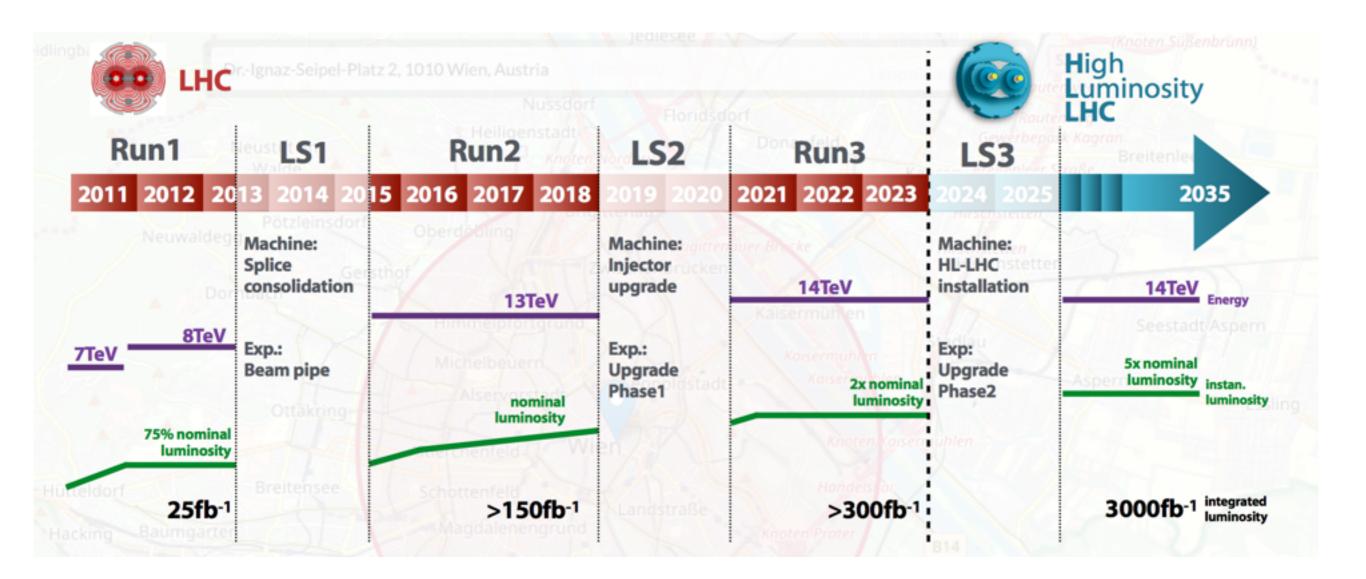




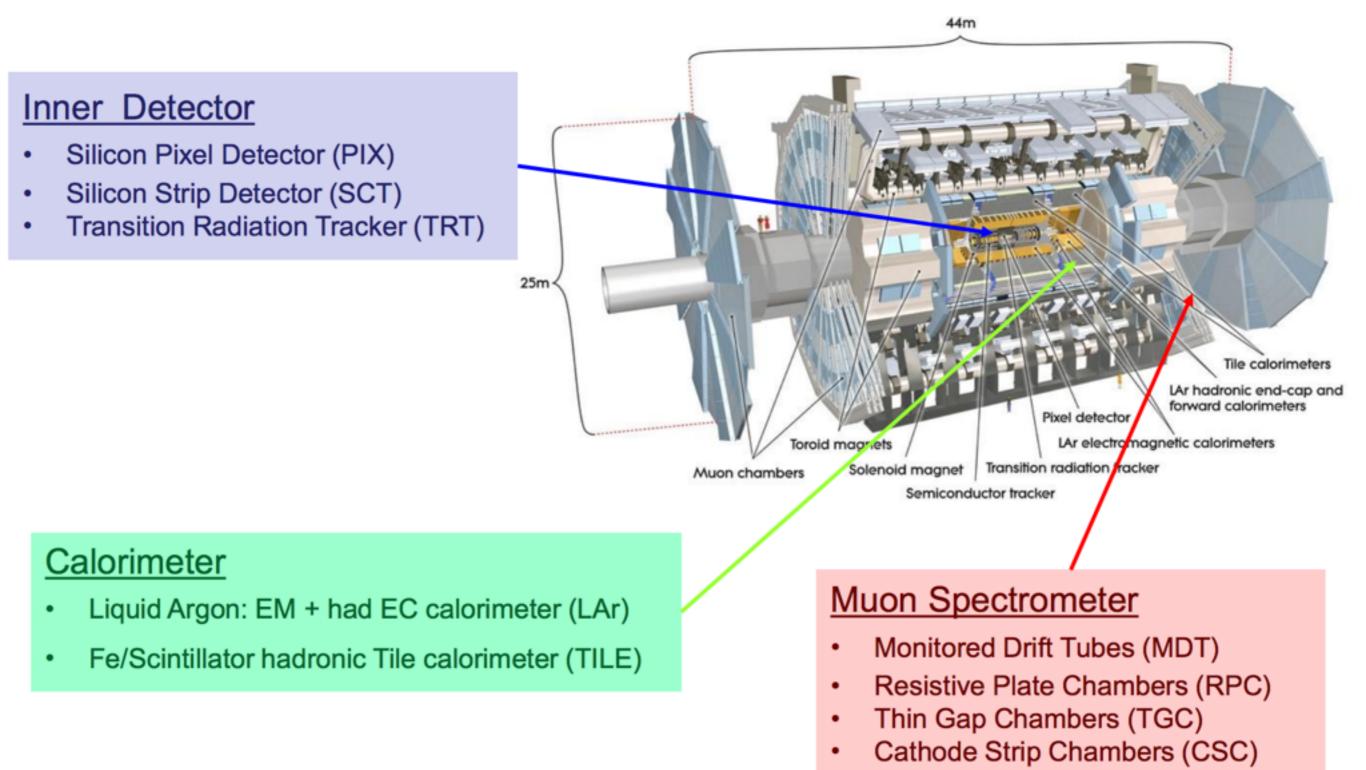
LHC Parameters Achieved in 2018

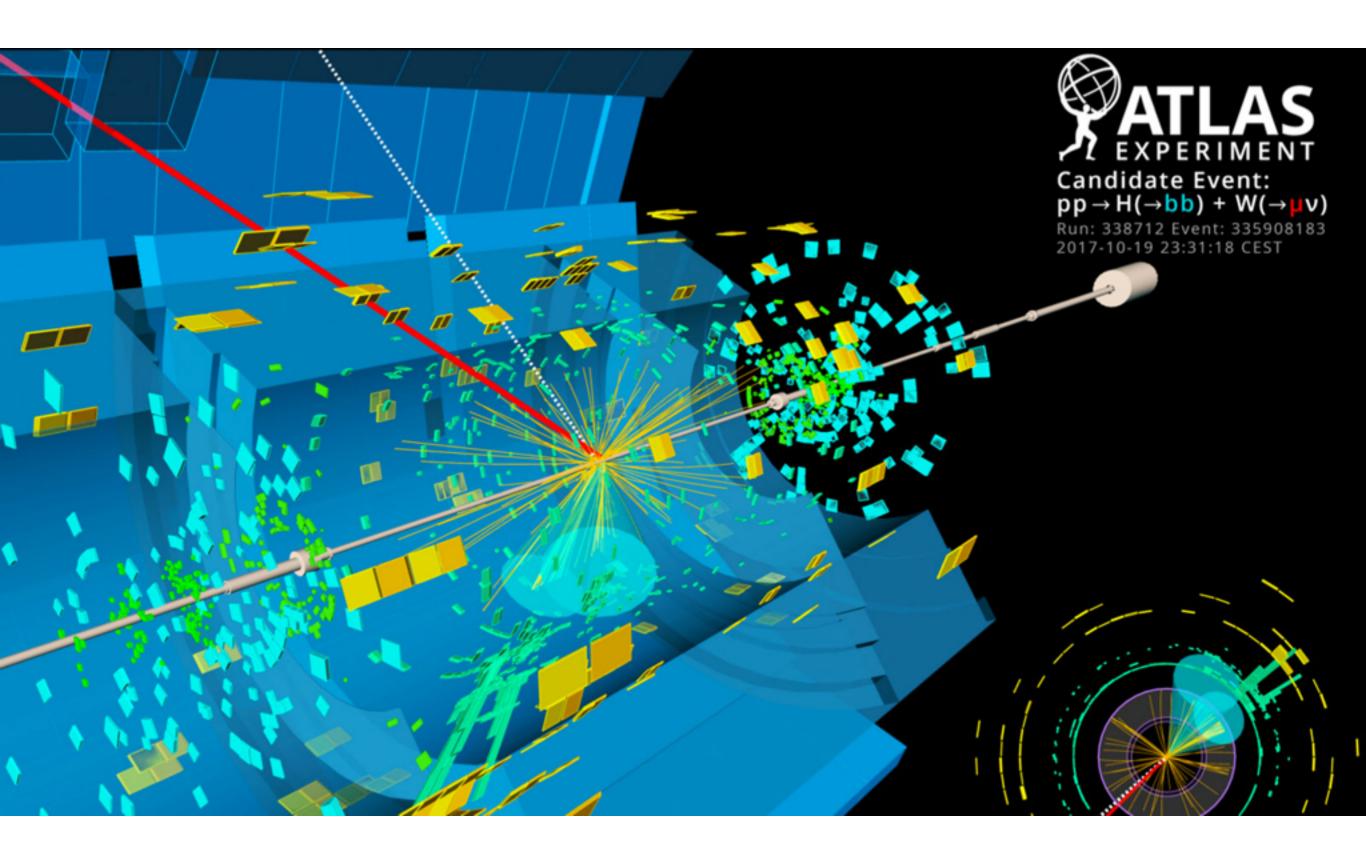
Parameter	2018	Design
Energy [TeV]	6.5	7.0
No. of bunches	2556	2808
Max. stored energy per beam (MJ)	312	362
β* [cm]	<mark>30→25</mark>	55
p/bunch (typical value) [10 ¹¹]	1.1	1.15
Typical normalized emittance [µm]	~1.8	3.75
Peak luminosity [10 ³⁴ cm ⁻² s ⁻¹]	2,1	1.0

LHC timeline



ATLAS





LHC event rate

The probability of one particular proton in a bunch coming from the left hitting a particular proton in a bunch coming from the right depends roughly on the rate of proton size (d^2 with $d\sim1$ fm) and the cross-sectional size of the bunch (σ^2 , with σ =16 microns) in the interaction point.

Then:

```
Probability \approx (d_{proton})^2/(\sigma^2) \Rightarrow Probability \approx (10^{-15})^2/(16 \cdot 10^{-6})^2 \approx 4 \cdot 10^{-21}
```

But with **1,15·10**¹¹ **protons/bunch** a good number of interactions will be possible every crossing.

Now, the number of interactions will be:

Probability x N² (with N = number of protons per bunch)

So, $(4 \cdot 10^{-21}) \times (1, 15 \cdot 10^{11})^2 \Rightarrow \sim 50$ interactions every crossing

But just a fraction of these interactions (~50 %) are inelastic scatterings that give rise to particles at sufficient high angles with respect to the beam axis.

Therefore, there are about 20 "effective" collisions every crossing.

With 11245 crosses per second we get:

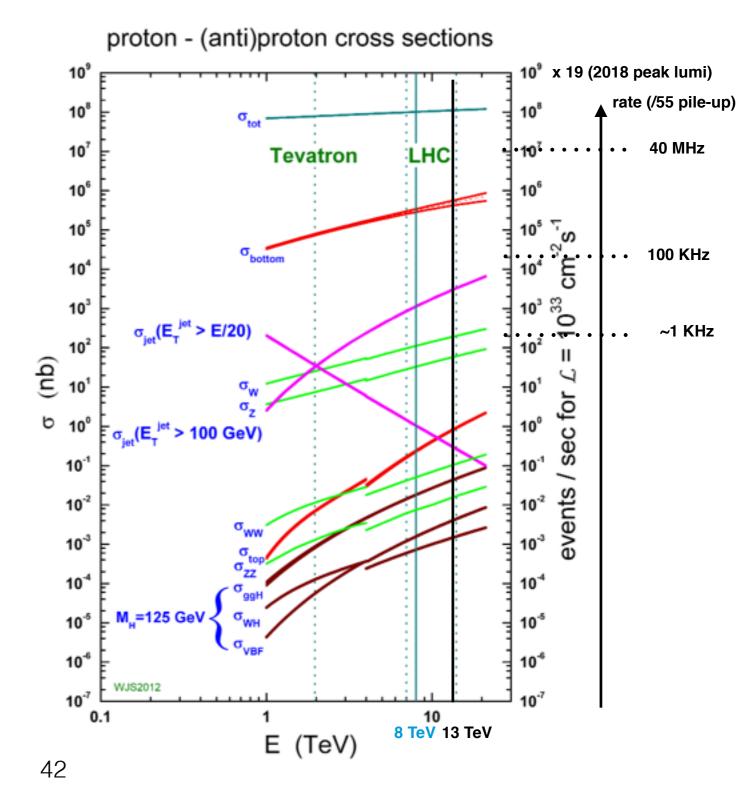
11245 x 2808 = 31,6 millions crosses , the "average crossing rate".

 $(31,6\cdot10^6 \text{crosses/s}) \times (20 \text{ collisions/cross}) \Rightarrow 600 \text{ millions collision/s}$

If we consider 3550 bunches: 11245 x 3550 = 40 millions crosses ⇒ 40 MHz

Why do we need a trigger?

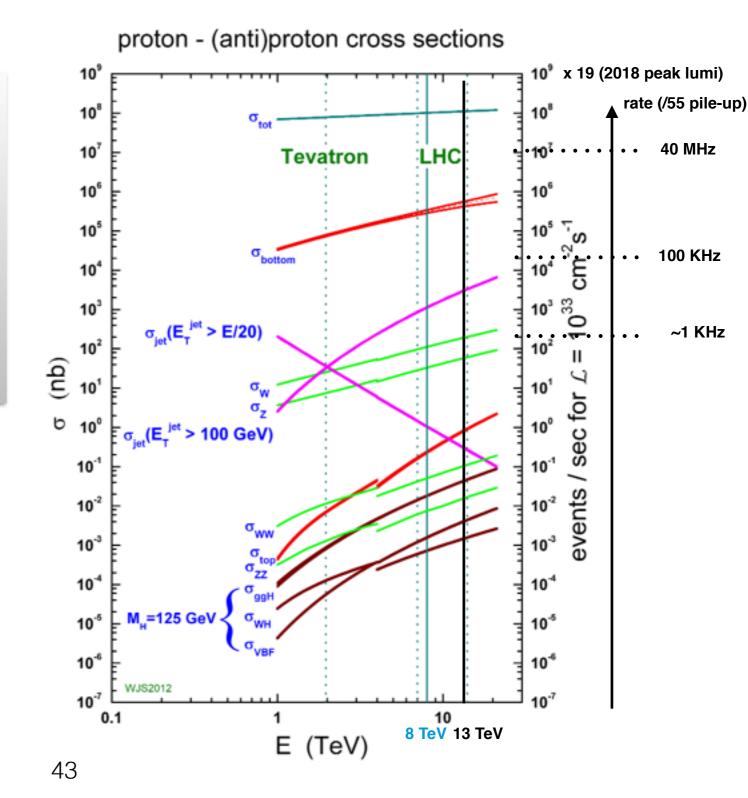
- 40 MHz bunch crossing rate (1 BC every 25 ns when LHC is full). ATLAS sees "bunches of collisions" (eg in 2018 ~ 55 proton-proton scatterings at start of a run)
- 1.3 MBytes ~ size of one event at start of a run in 2018
- 52 TBytes/sec
- Even if one could build a very costly and complex system to assemble, reconstruct and store to disk basic data objects for every event, why would we do that?

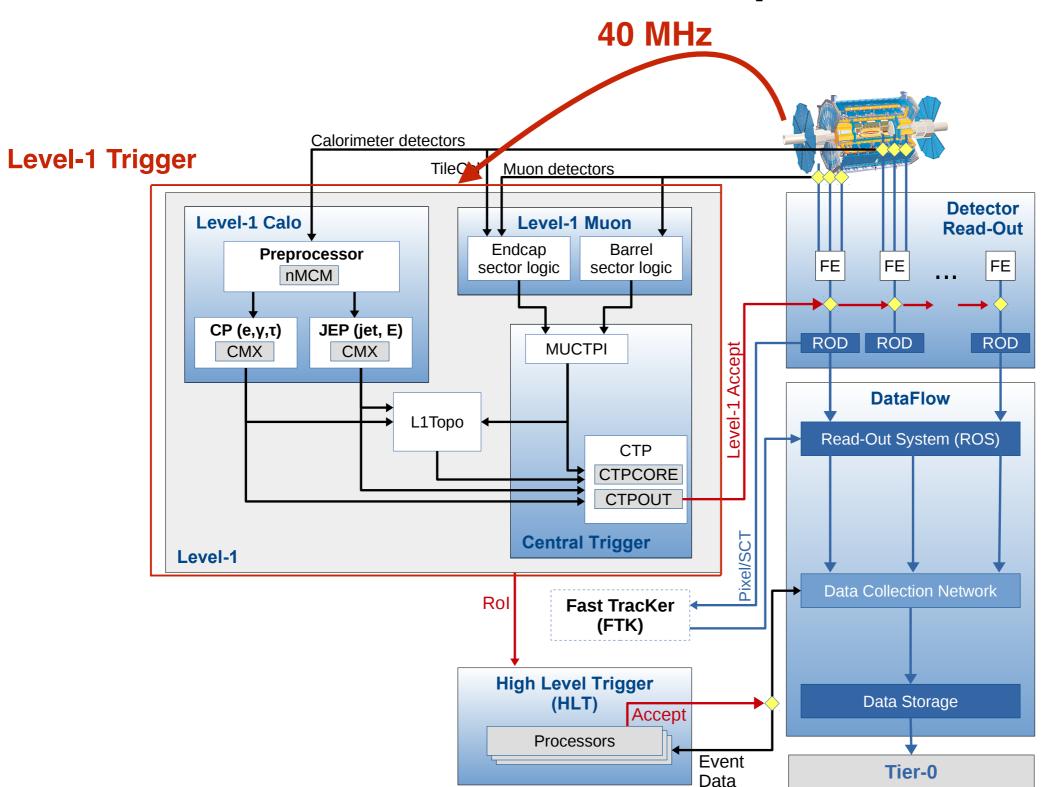


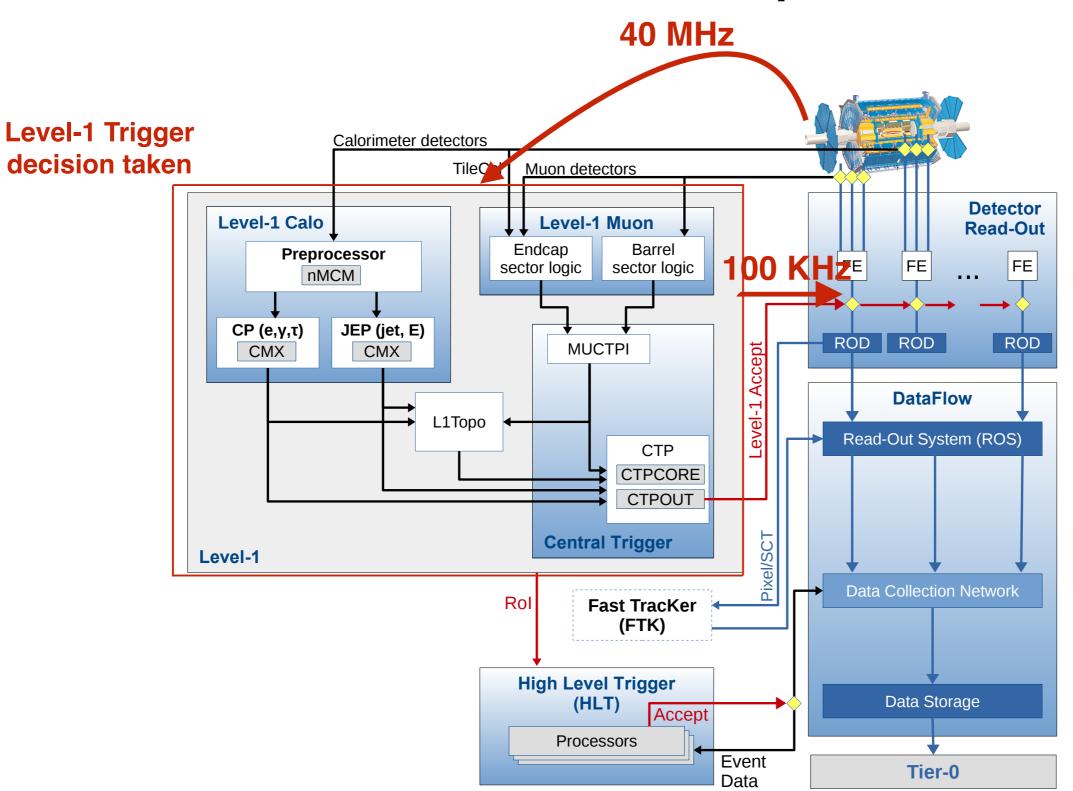
Why do we need a trigger?

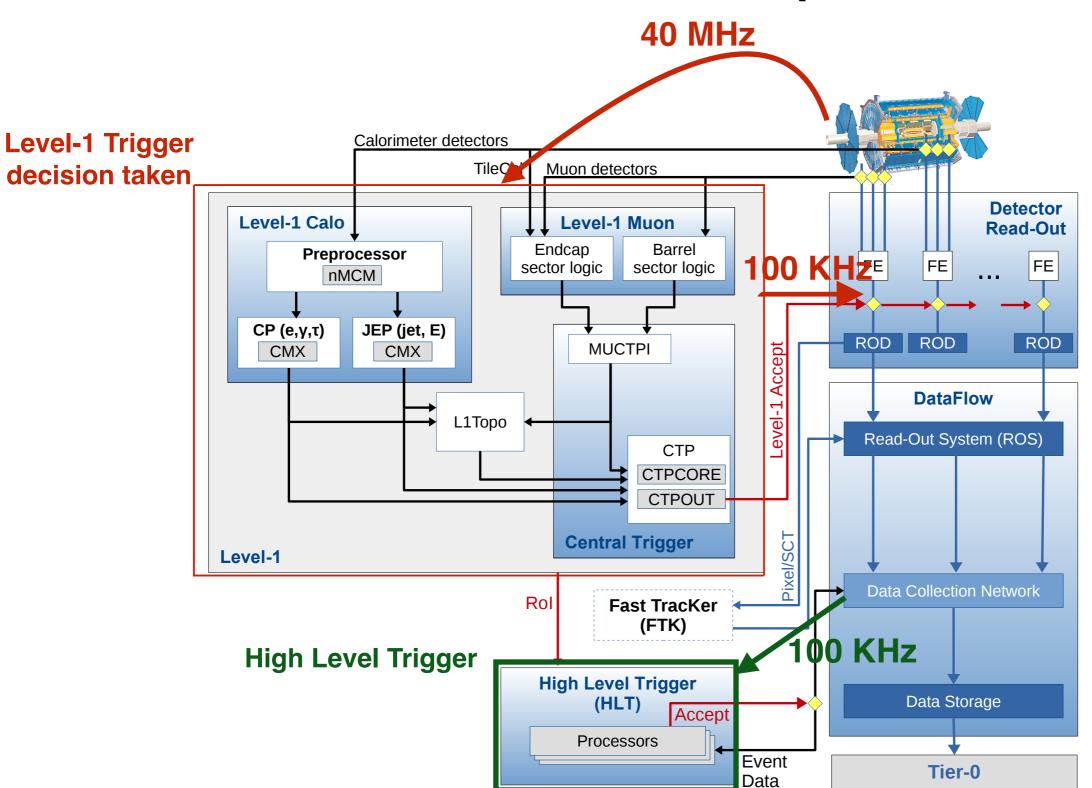
pre-LHC unobserved new physics phenomena (Higgs, SUSY, exotica,....) or processes poorly measured (Z,W top cross sections) lie in the lower part of this plot. No need to save all data!

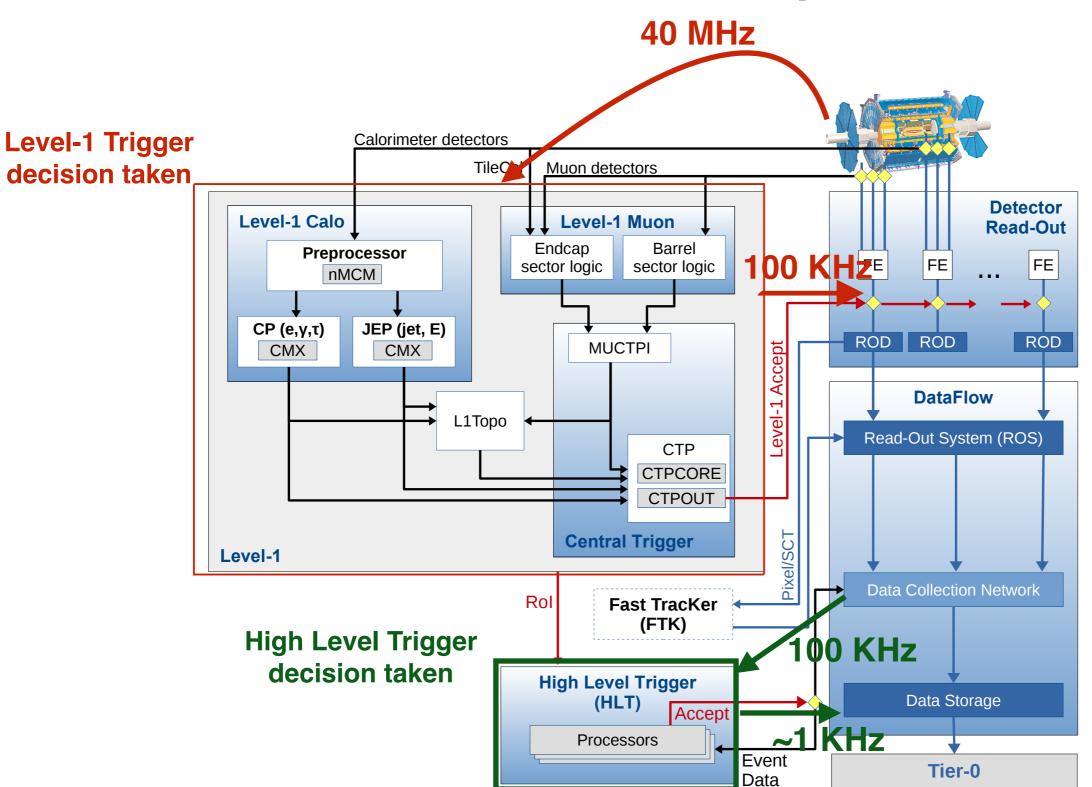
The goal of the trigger system is to run real-time analysis of the data and decide what to keep and what to throw away.



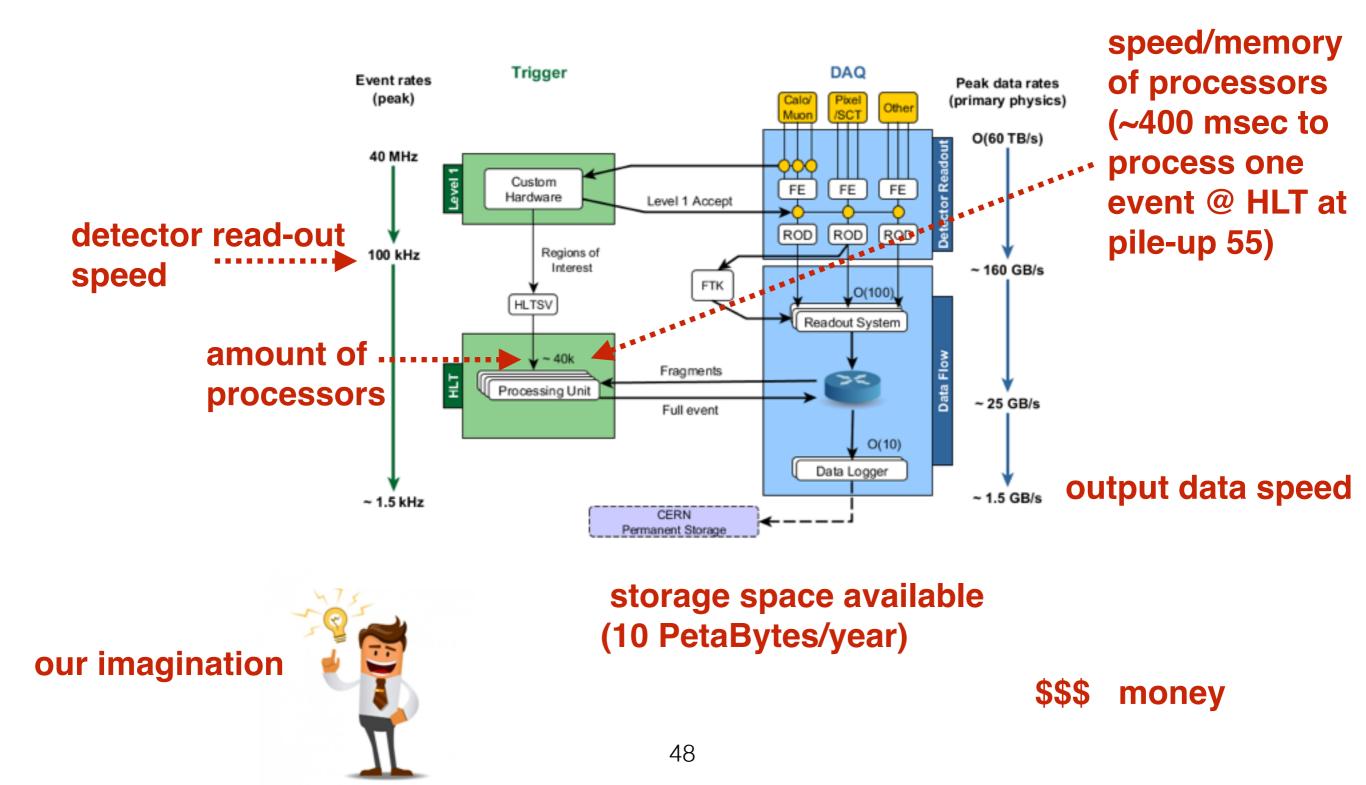








Constraints on the trigger



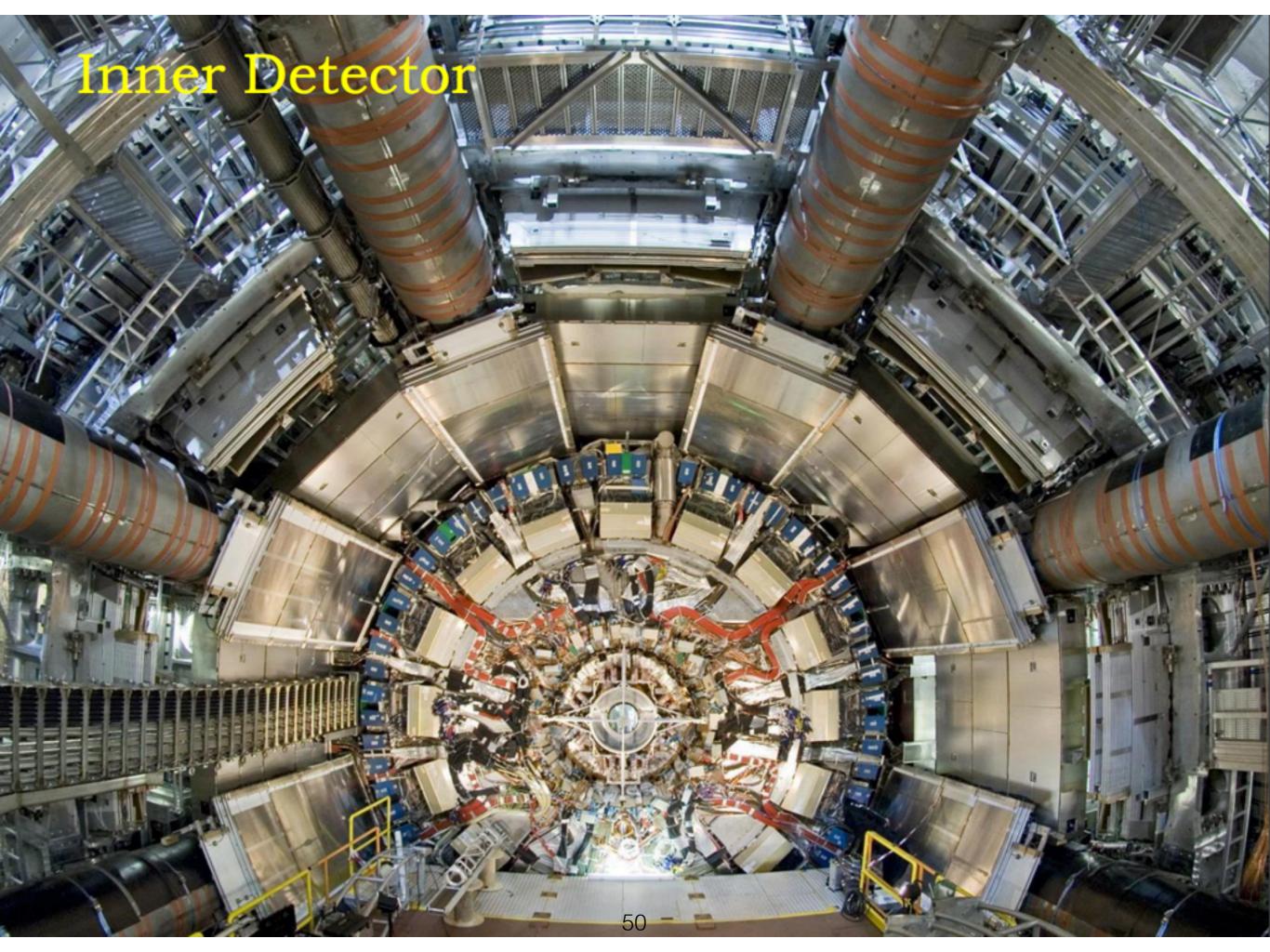
Which triggers do we run? Main physics stream

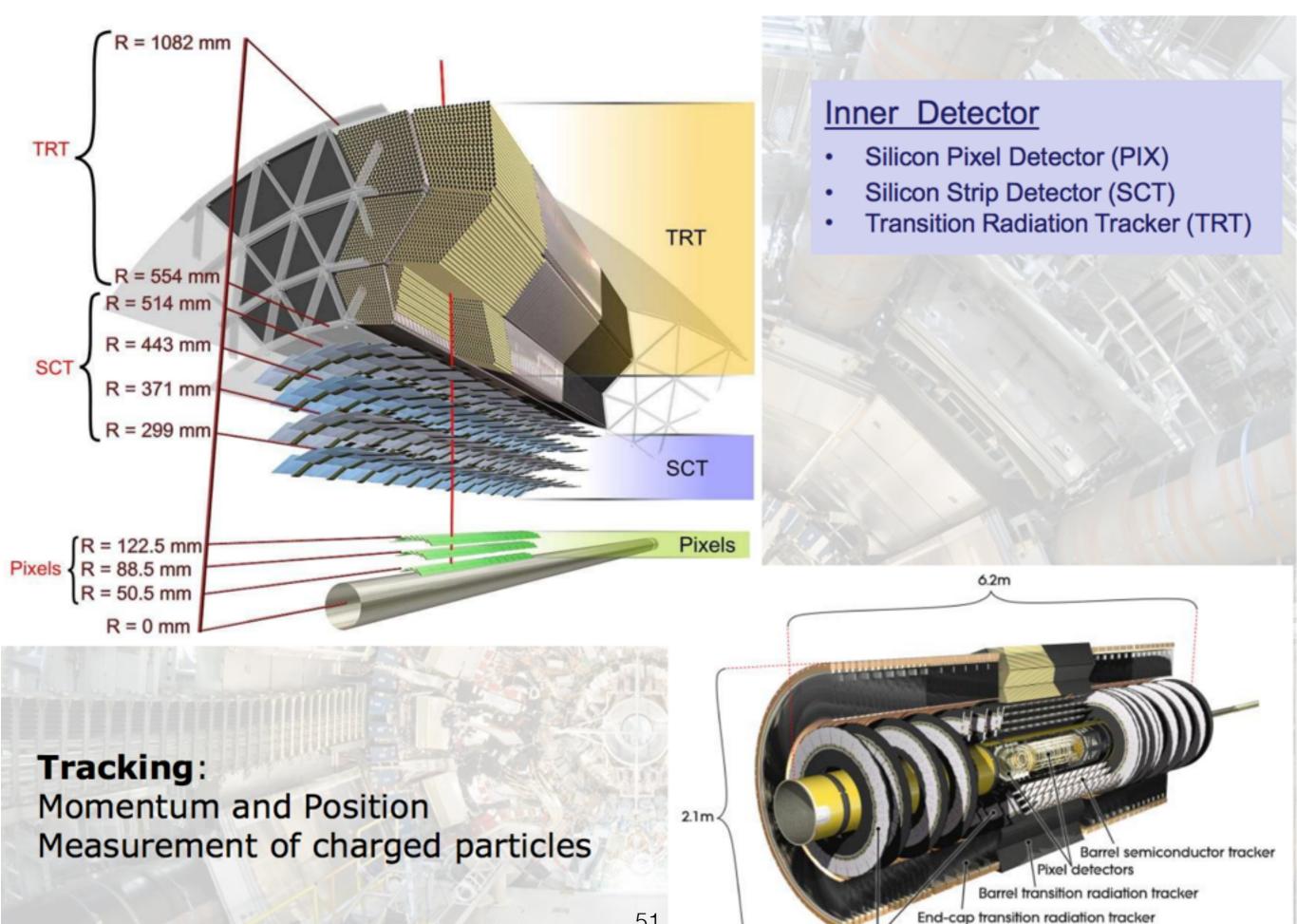
Trigger		Trigger Sele	Level-1 Peak	HLT Peak	
	Typical offline selection	Level-1 (GeV)	HLT (GeV)	Rate (kHz) $L = 1.7 \times 10^{-10}$	Rate (Hz) 34 cm ⁻² s ⁻¹
	Single isolated μ , $p_T > 27$ GeV	20	26 (i)	16	187
	Single isolated tight $e, p_T > 27 \text{ GeV}$	22 (i)	26 (i)	26	178
Single leptons	Single μ , $p_T > 52 \text{ GeV}$	20	50	16	65
	Single $e, p_T > 61 \text{ GeV}$	22 (i)	60	26	17
	Single τ , $p_T > 170 \text{ GeV}$	100	160	1.2	49
	Two μ 's, each $p_T > 15 \text{ GeV}$	2×10	2×14	2.0	30
	Two μ 's, $p_{\rm T} > 23, 9 {\rm GeV}$	20	22, 8	16	42
	Two very loose e 's, each $p_T > 18 \text{ GeV}$	2 × 15 (i)	2×17	1.6	11
Two leptons	One e & one μ , $p_T > 8$, 25 GeV	20 (µ)	7, 24	16	5
Two reptons	One <i>e</i> & one μ , $p_T > 18$, 15 GeV	15, 10	17, 14	2.0	4
	One e & one μ , $p_T > 27, 9$ GeV	22 (e, i)	26, 8	26	2
	Two τ 's, $p_T > 40, 30 \text{ GeV}$	20 (i), 12 (i) (+jets, topo)	35, 25	5.1	59
	One τ & one isolated μ , $p_T > 30$, 15 GeV	12 (i), 10 (+jets)	25, 14 (i)	2.1	9
	One τ & one isolated $e, p_T > 30, 18 \text{ GeV}$	12 (i), 15 (i) (+jets)	25, 17 (i)	3.9	16
	Three loose e 's, $p_T > 25$, 13, 13 GeV	20, 2 × 10	24, 2 × 12	1.2	< 0.1
	Three μ 's, each $p_T > 7 \text{ GeV}$	3×6	3×6	0.2	8
Three leptons	Three μ 's, $p_T > 21, 2 \times 5$ GeV	20	20, 2 × 4	16	8
	Two μ 's & one loose $e, p_T > 2 \times 11, 13 \text{ GeV}$	$2 \times 10 (\mu's)$	2 × 10, 12	2.0	0.3
	Two loose e's & one μ , $p_T > 2 \times 13$, 11 GeV	2×8, 10	2 × 12, 10	1.6	0.2
One photon	One loose γ , $p_T > 145$ GeV	22 (i)	140	26	46
	Two loose γ 's, $p_T > 55$, 55 GeV	2×20	50, 50	2.4	6
Two photons	Two medium γ 's, $p_T > 40$, 30 GeV	2×20	35, 25	2.4	18
-	Two tight γ 's, $p_T > 25, 25 \text{ GeV}$	2 × 15 (i)	2 × 20 (i)	2.4	15
Single jet	Jet $(R = 0.4)$, $p_T > 435$ GeV	100	420	3.4	33
Single Jet	Jet ($R = 1.0$), $p_T > 480 \text{ GeV}$	100	460	3.4	24
E ^{miss}	$E_{\rm T}^{\rm miss} > 200 {\rm GeV}$	50	110	4.4	100
	Four jets, each $p_T > 125 \text{ GeV}$	3 × 50	4×115	0.5	16
Multi-jets	Five jets, each $p_T > 95$ GeV	4 × 15	5 × 85	4.9	10
	Six jets, each $p_T > 80$ GeV	4 × 15	6×70	4.9	4
	Six jets, each $p_T > 60$ GeV, $ \eta < 2.0$	4 × 15	6×55 , $ \eta < 2.4$	4.9	15
b-jets	One $b \ (\epsilon = 40\%), p_T > 235 \text{ GeV}$	100	225	3.4	15
	Two b's ($\epsilon = 60\%$), $p_T > 185, 70 \text{ GeV}$	100	175, 60	3.4	12
	One b ($\epsilon = 40\%$) & three jets, each $p_T > 85$ GeV	4 × 15	4×75	4.9	15
	Two b's ($\epsilon = 70\%$) & one jet, $p_T > 65, 65, 160 \text{ GeV}$	2 × 30, 85	2 × 55, 150	2.7	15
	Two b's ($\epsilon = 60\%$) & two jets, each $p_T > 45$ GeV	4 × 15	4 × 35	4.9	13

not easy to come up with the "perfect" list

every year we review this carefully

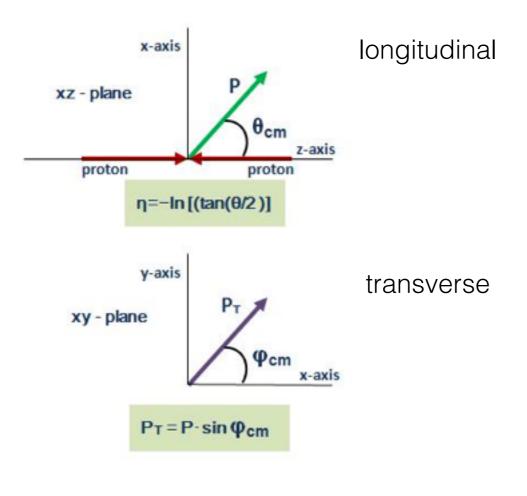
this is the first place where physics reach of ATLAS gets limited

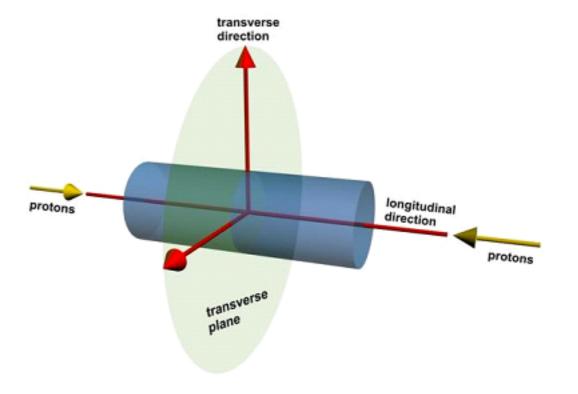


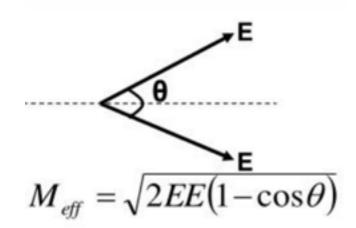


End-cap semiconductor tracker

ATLAS: particle kinematic







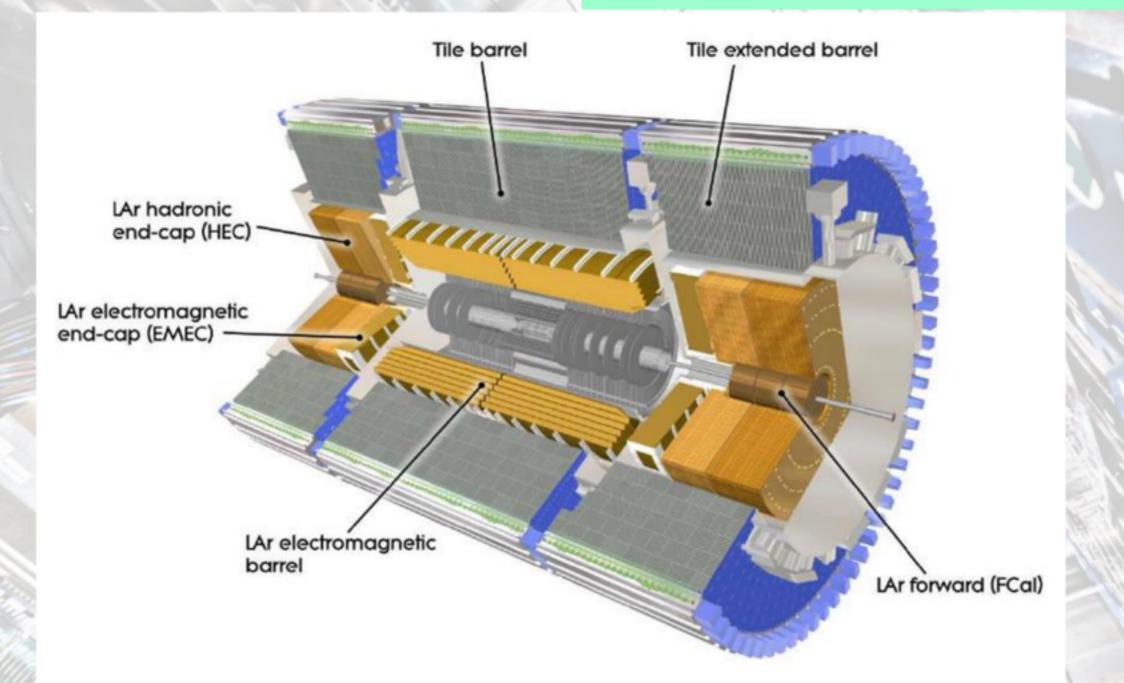


Calorimeter

Calorimeter

ALL X MA

- Liquid Argon: EM + had EC calorimeter (LAr)
- Fe/Scintillator hadronic Tile calorimeter (TILE)

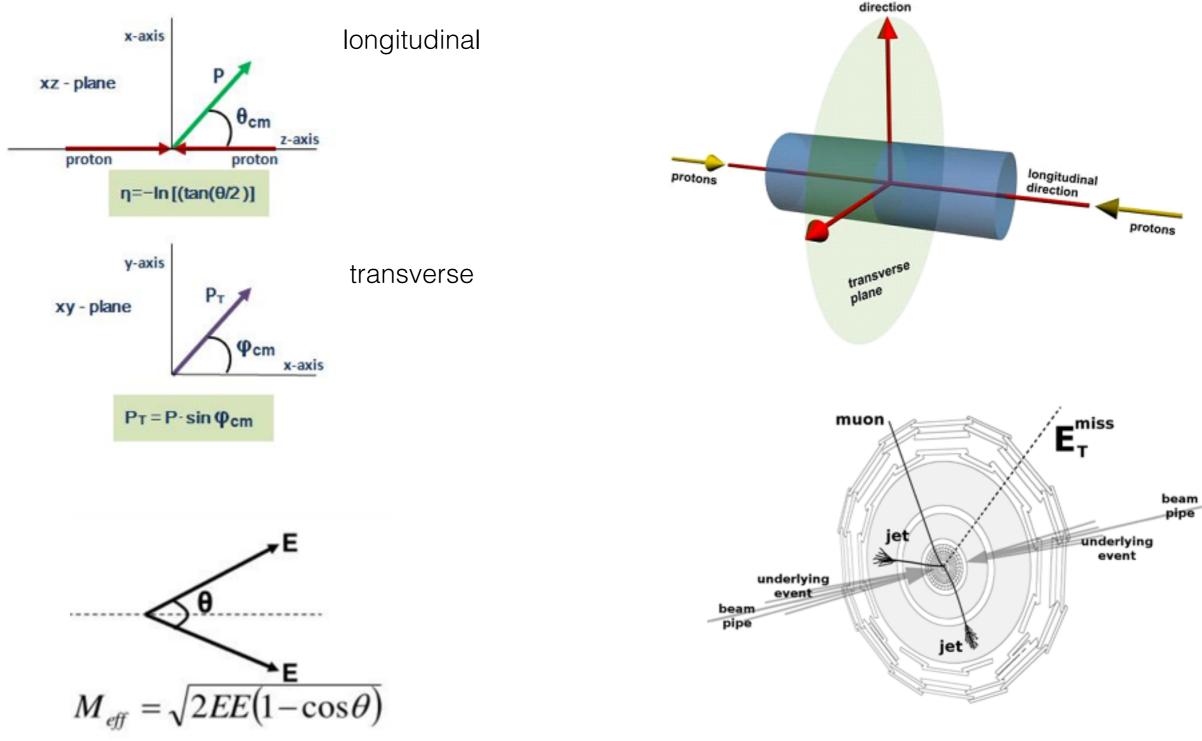


54

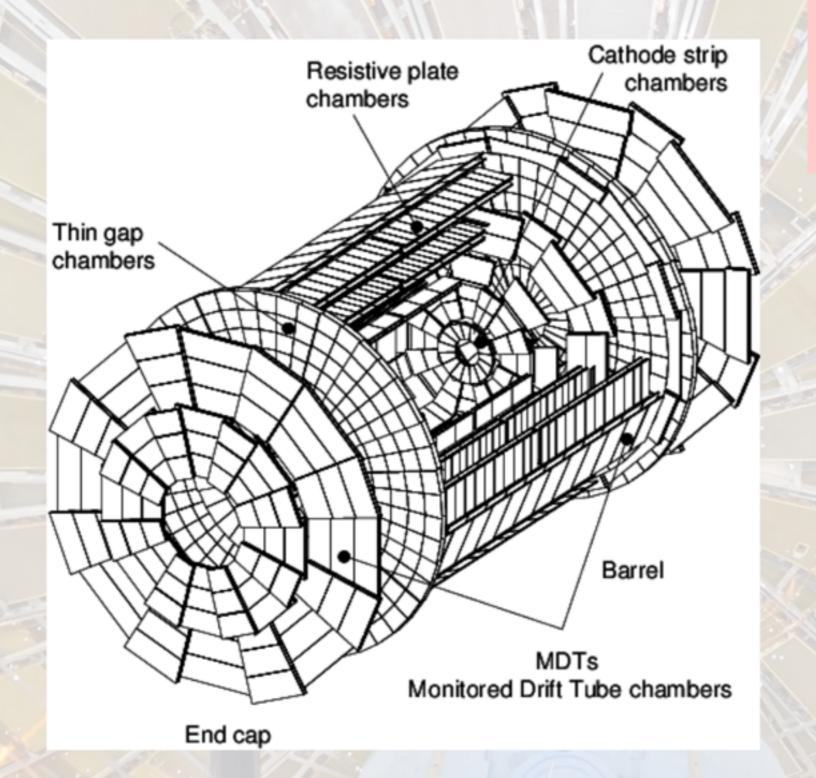
Energy Measurement, Trigger Input

ATLAS: particle kinematic

transverse





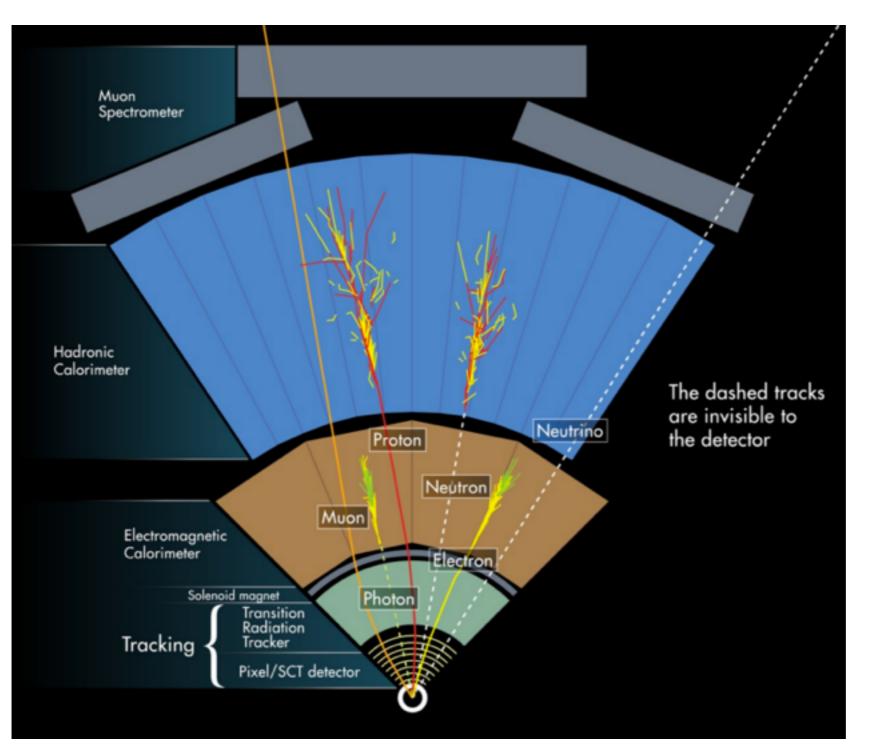


Muon Spectrometer

- Monitored Drift Tubes (MDT)
- Resistive Plate Chambers (RPC)
- Thin Gap Chambers (TGC)
- Cathode Strip Chambers (CSC)

Momentum and Position Measurement of Muons, Trigger

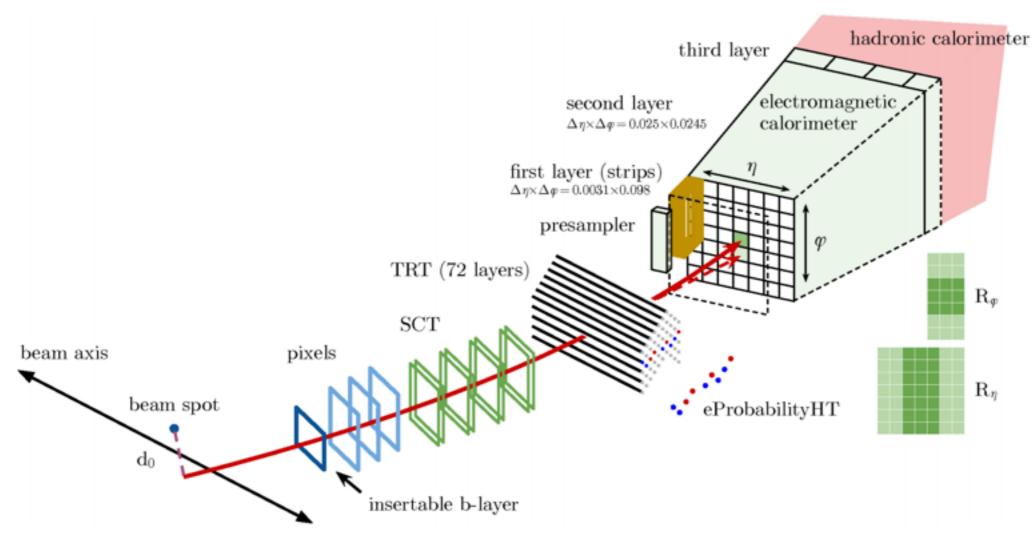
ATLAS: particle identification



electron, photon and muon (and a.p.) are the "easiest" to see

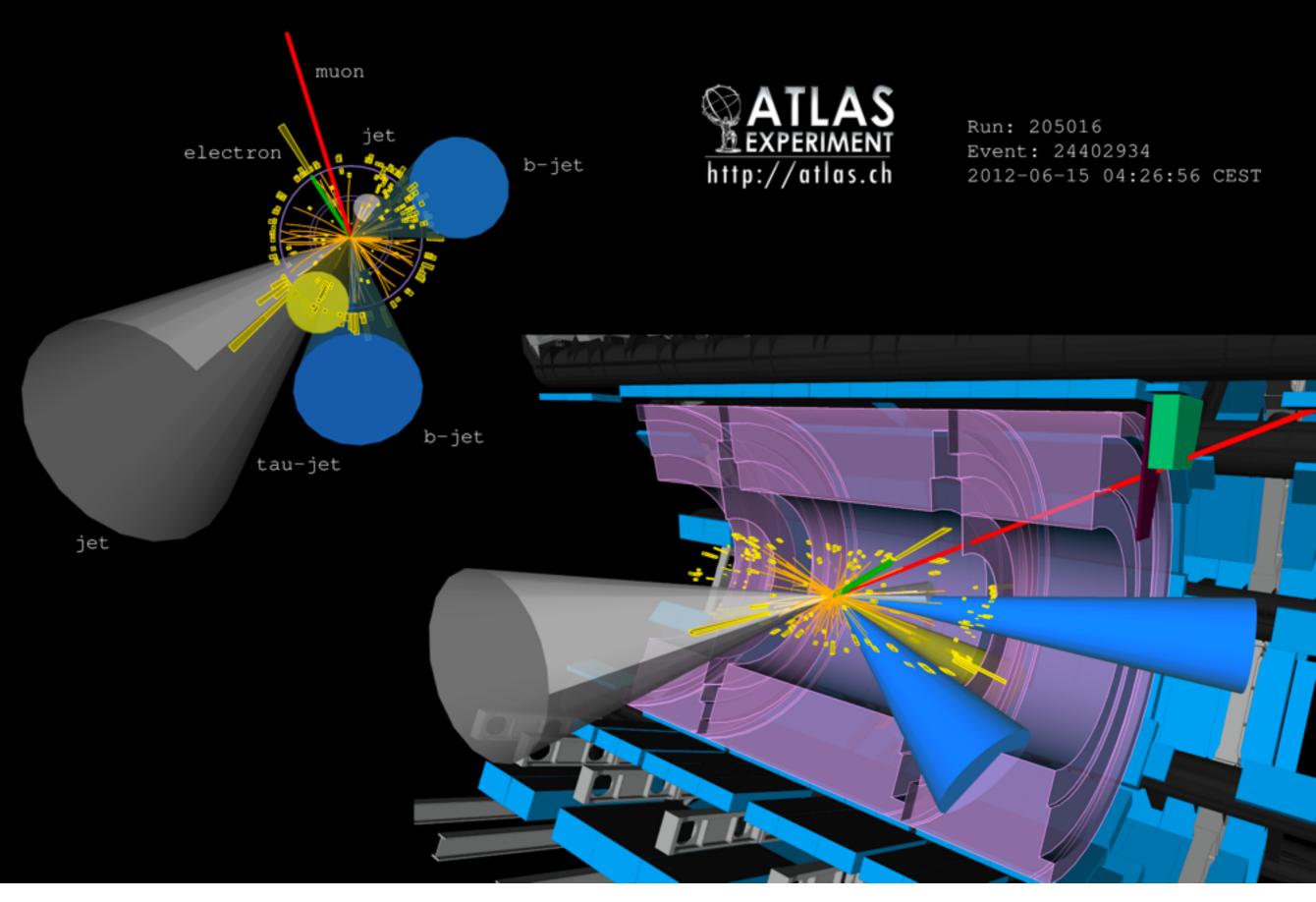
in p-p collisions the majority of the output products are jets with hadrons

to find a b-quark, a c-quark, a hadronic decay of a tau lepton, is a much harder job. Typically, multi-variate methods (Boosted Decision trees, Neural Network, etc) are used.



electron reconstruction and identification

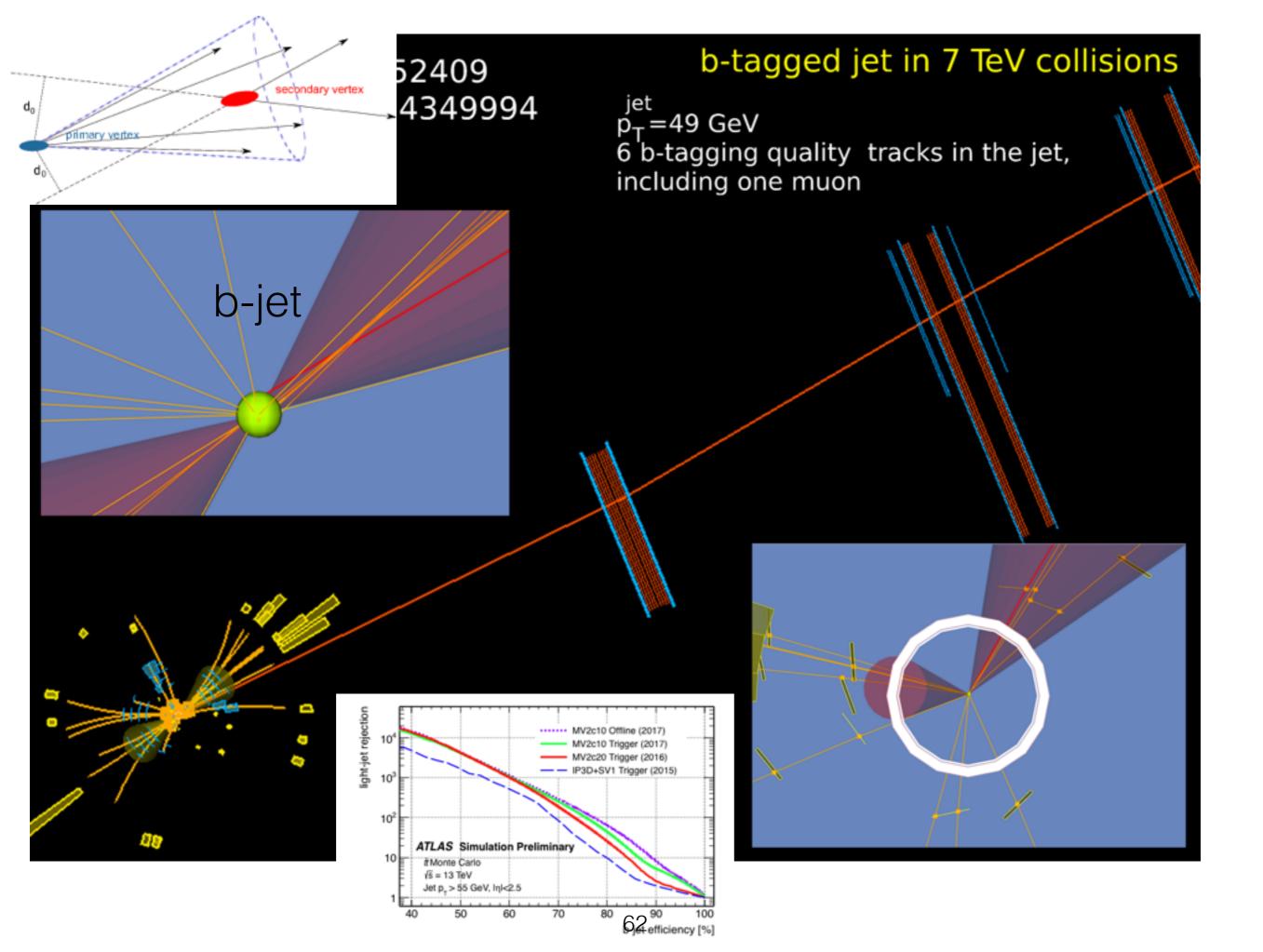
Cuts optimized	$E_T > 20 \text{ TeV}$							
	Efficiency (%)	Jet rejection						
	$Z \rightarrow ee$							
Loose	94.30 ± 0.03	1066 ± 4						
Medium	89.97 ± 0.03	6821 ± 69						
Tight	71.52 ± 0.03	$(1.38 \pm 0.06)10^5$						





Run: 280464 Event: 478442529 2015-09-27 22:09:07 CEST

di-jet event



ATLAS: event identification

very often, the characteristics of the whole event are used to discriminate against background

because backgrounds are very high and everything helps

because one needs data-driven methods (eg ABCD method) for background estimates, since MC simulations are unreliable or with too poor statistics. Additional requests on the event, as well as on single volgects, can be inverted to create control regions or regions rich in background to be estimated.

-> very hard to do a general search at the LHC and be sensitive.

 $f \Delta t$ Higgs or for new physics, analyses are typically exclusive if one wants to minimize Δt rors.

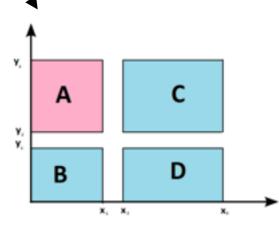


Fig. 1. – The ABCD method. The x and y axis are two uncorrelated variables. The region A is dominated by the signal (for instance, large $E_{\rm T}^{\rm miss}$ and low isolation or small impact parameter (d_0) significance), while all other regions are dominated by backgrounds, which are characterized e.g. by non-isolated leptons or leptons with large d_0 significance, or events with small $E_{\rm T}^{\rm miss}$).

Variable		VBF		Boosted				
	TepTep	$\eta_{ep}\eta_{had}$	7had7had	$\eta_{ep}\eta_{ep}$	7lep7had	7had 7had		
$m_{\tau\tau}^{MMC}$	•	•	•	•	•	•		
$\Delta R(\tau_1, \tau_2)$	•	•	•		•	•		
$\Delta \eta(j_1, j_2)$	•	•	•					
m_{j_1, j_2}	•	•	•					
$\eta_{i_1} \times \eta_{i_2}$		•	•					
p_{T}^{Total}		•	•					
Sum p_T					•	•		
$p_{T}^{\tau_{1}}/p_{T}^{\tau_{2}}$					•	•		
$E_T^{miss}\phi$ centrality		•	•	•	•	•		
m_{ℓ,ℓ,j_1}				•				
m_{ℓ_1,ℓ_2}				•				
$\Delta \phi(\ell_1, \ell_2)$				•				
Sphericity				•				
$p_T^{\ell_1}$				•				
$p_T^{j_1}$				•				
$E_{T}^{miss}/p_{T}^{\ell_{2}}$				•				
m_{T}		•			•			
$min(\Delta \eta_{\ell_1 \ell_2, jets})$	•							
$C_{\eta_1,\eta_2}(\eta_{\ell_1}) \cdot C_{\eta_1,\eta_2}(\eta_{\ell_2})$	•							
$C_{\eta_1,\eta_2}(\eta_\ell)$		•						
$C_{\eta_1,\eta_2}(\eta_{j_3})$	•							
$C_{\eta_1,\eta_2}(\eta_{r_1})$			•					
$C_{n_1,n_2}(\eta_{n_2})$			•					

able 5	Discr	imina	ting	variables	used in	the t	raining	of the	BD	Γ for	each	chann	el and	category	
$\sqrt{s} =$	8 TeV.	The	more	complex	variab	les ar	e descr	ibed is	1 the	text.	The	filled	circles	indicate	
hich va	riables	are w	sed in	each cas	se.										

L.Evans "The Large Hadron Collider: A Marvel of Technology" - Google Books <u>http://cdsweb.cern.ch/record/1017689/files/ab-note-2007-014.pdf</u> <u>https://www.lhc-closer.es/taking_a_closer_look_at_lhc</u> <u>http://uspas.fnal.gov/materials/09VU/Lecture1a.pdf</u> L. Evans, LHC machine, <u>http://iopscience.iop.org/article/10.1088/1748-0221/3/08/S08001/pdf</u>

https://indico.cern.ch/event/22574/contributions/475143/attachments/371243/516589/ IntroductionToAccelerators.pdf