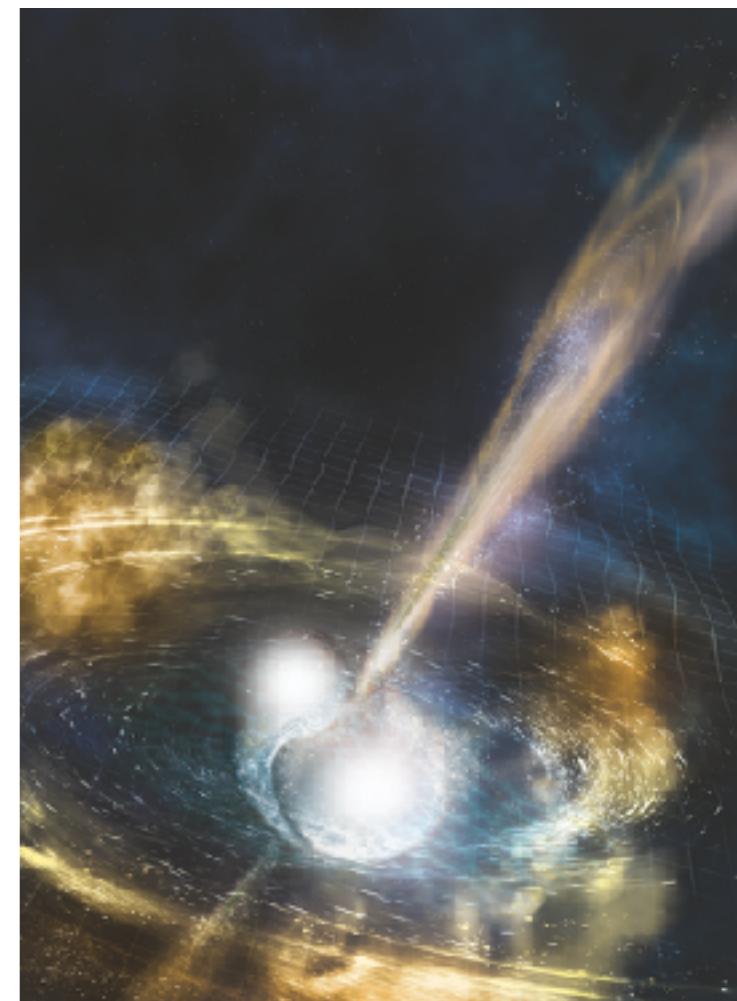
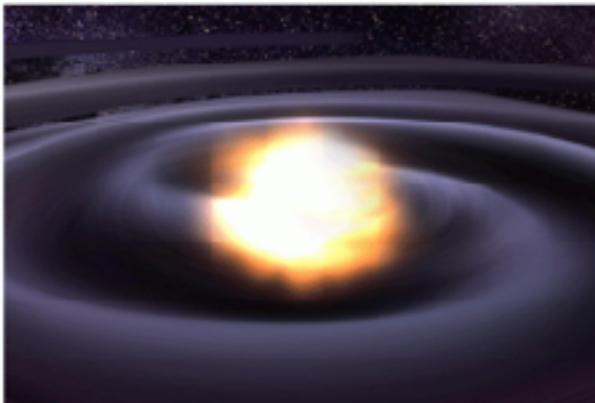
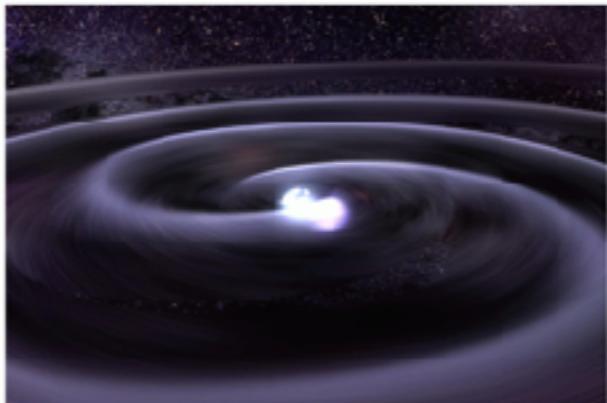
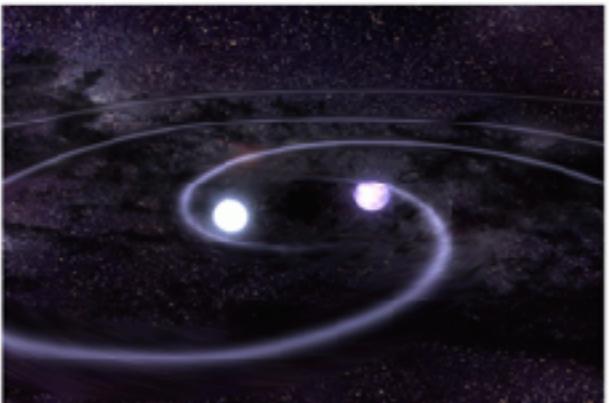


Astrophysical GW sources cont:

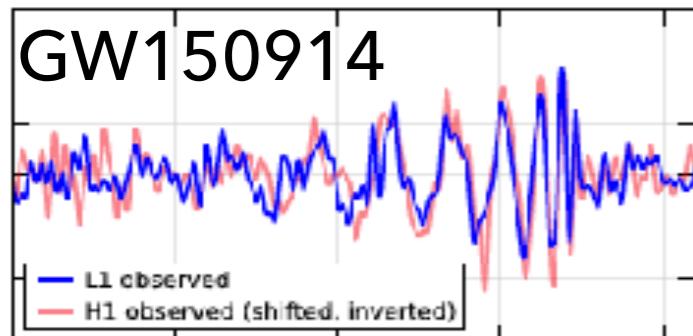
1. GW signatures of non-black-hole objects

2. Multi-messenger observations of GW170817

3. Outlook

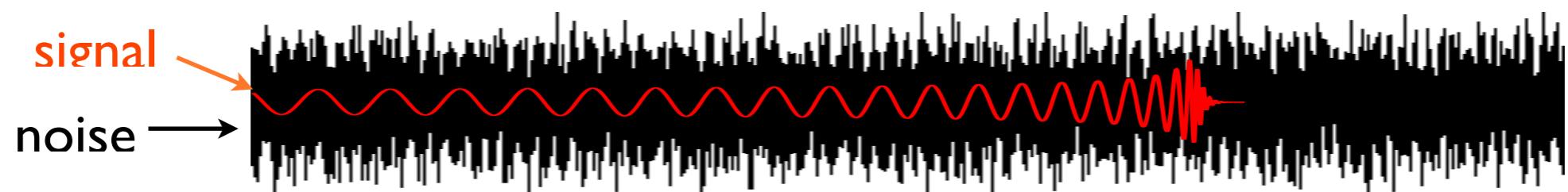


Last time: GWs from binary black holes



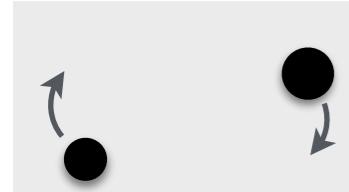
Data and tutorials available at: <https://losc.ligo.org/>

Weak signals (e.g. GW151226) buried in the noise:



- ▶ **Detection:** cross-correlate data with **template bank**
- ▶ **Extracting information** (e.g. source parameters): Bayesian analysis (MCMC), need **accurate** templates
 - ▶ phase evolution to better than 1 rad over entire signal

Last time: Effective One-Body (EOB) templates

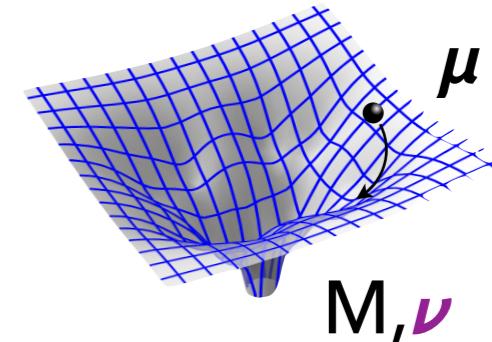


$$H_{\text{EOB}} = M \sqrt{1 + 2\nu \left(\frac{H_{\text{eff}}}{\mu} - 1 \right)}$$

$$\frac{dP_i}{dt} = \{P_i, H^{\text{EOB}}\} + \mathcal{F}_{\text{rr}}$$

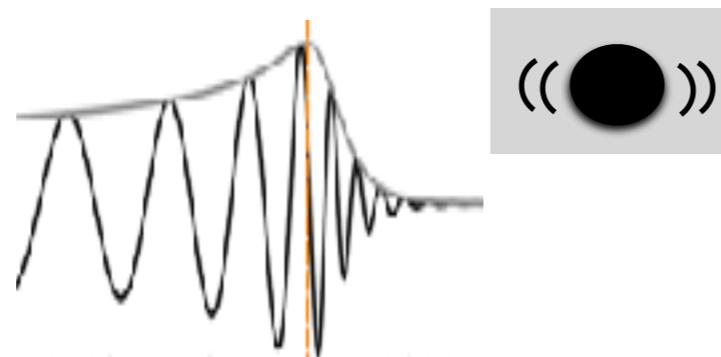
+

Effective description



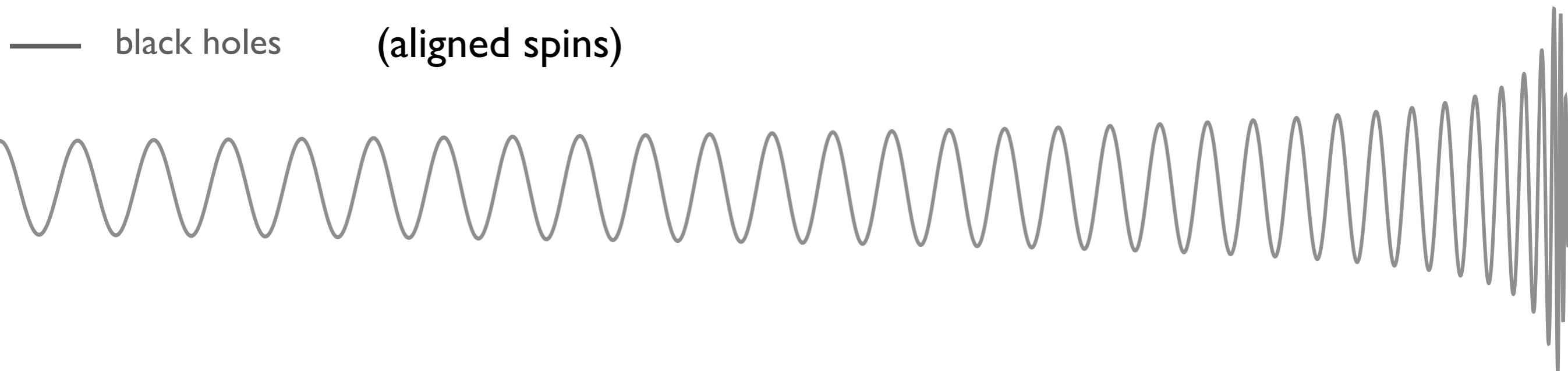
$$\nu = \mu/M \in [0, 1/4]$$

Merger & Ringdown



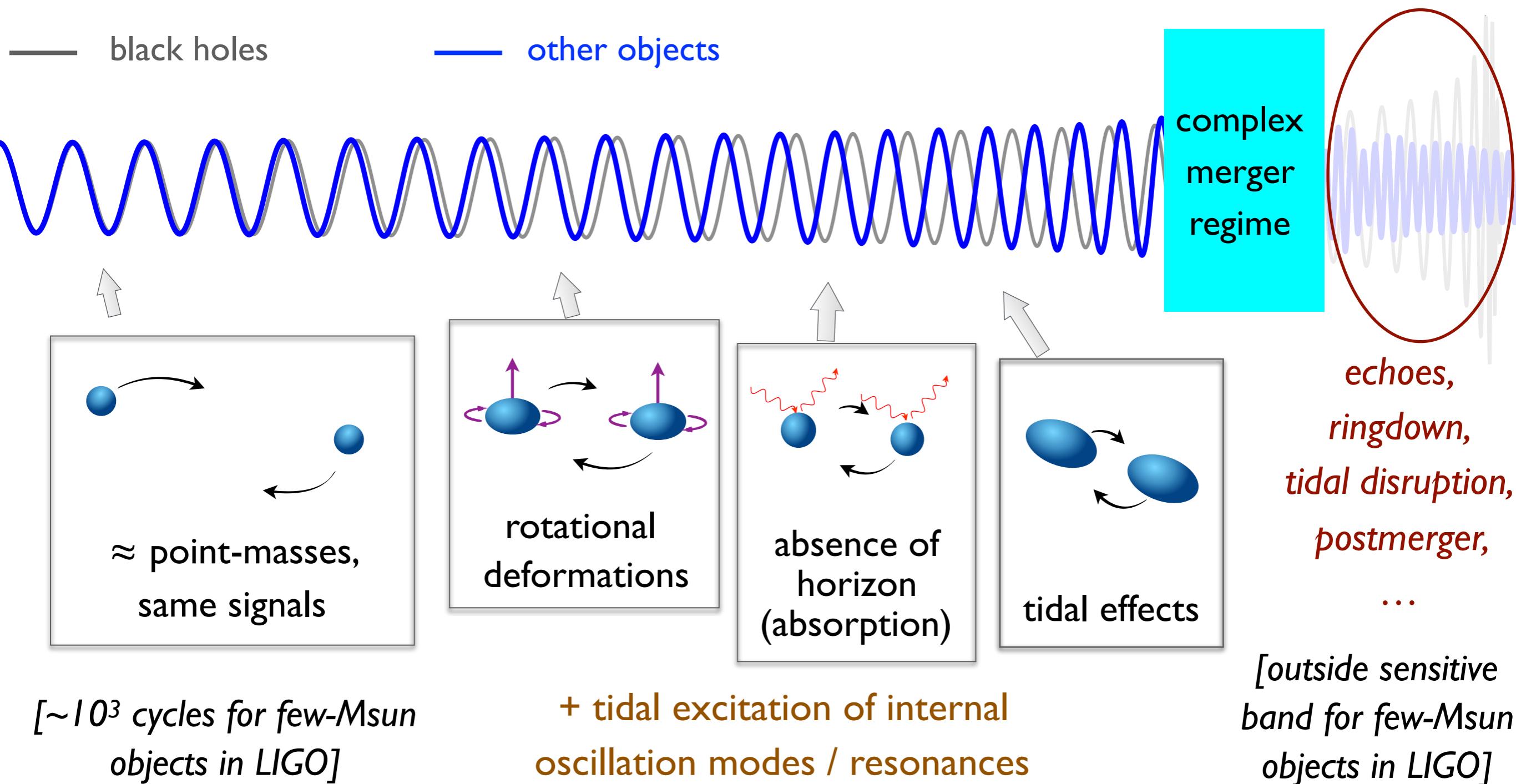
Uncalibrated EOB re-summation of PN information also used in alternative
“Phenom” template models for frequency-domain GW signals

Imprints of objects' internal structure on GWs



What changes for non-black hole objects (comparable masses)?

Imprints of objects' internal structure on GWs



Tidal effects in nonspinning binaries

- ▶ Are there new, non-tidal interactions in GR that impact the early inspiral?
[Wilson+ 1995 ``Instabilities in Close Neutron Star Binaries'' & 4 follow-up papers;
Sociological account: Kennefick 2000 ``Star crushing: theoretical practice & the theoretician's regress'']
- ▶ Rigorous analysis: [Flanagan 1998: ``GR coupling between orbital motion & internal degrees of freedom for inspiraling binary neutron stars'']



Dimensionless parameters characterizing the system:

$$\epsilon = \frac{M}{R}$$

Internal gravity

$$\alpha = \frac{R}{D}$$

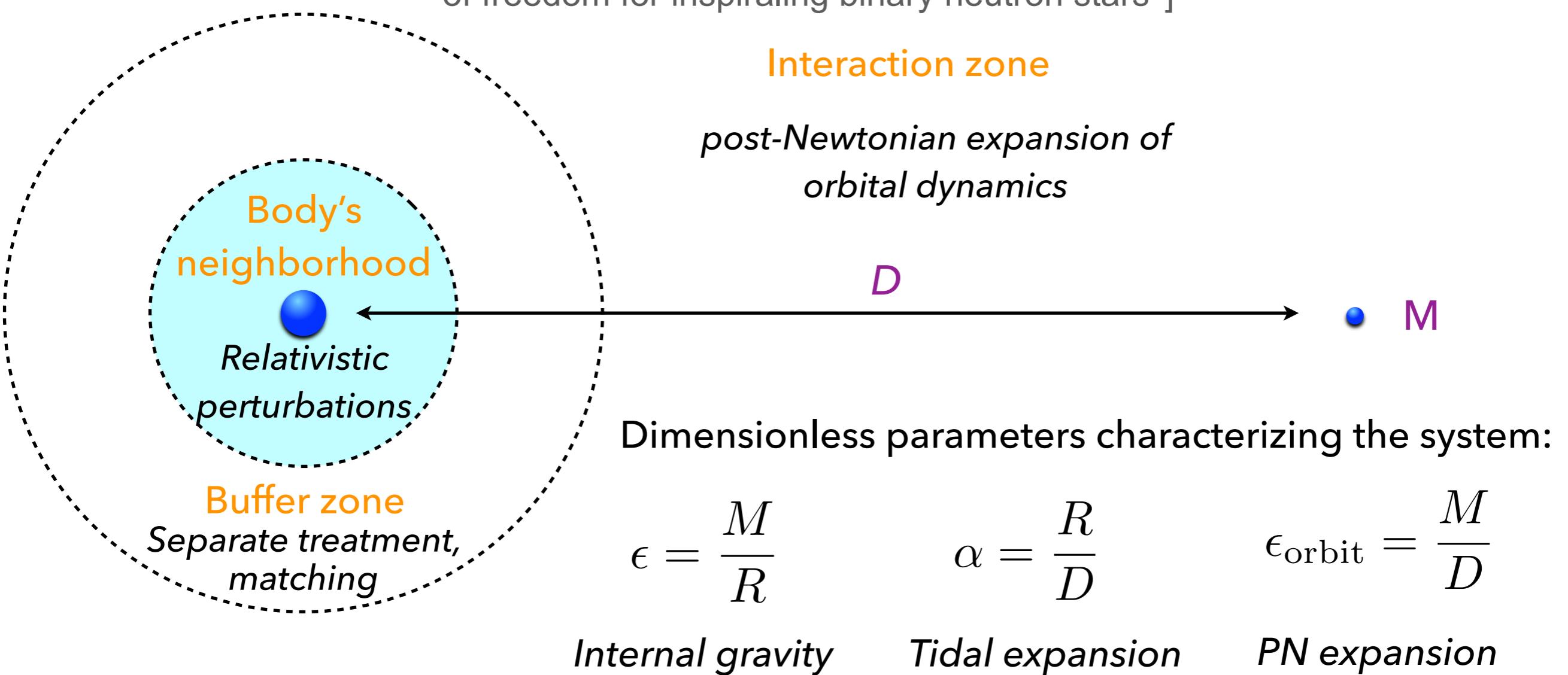
Tidal expansion

$$\epsilon_{\text{orbit}} = \frac{M}{D}$$

PN expansion

Tidal effects in nonspinning binaries

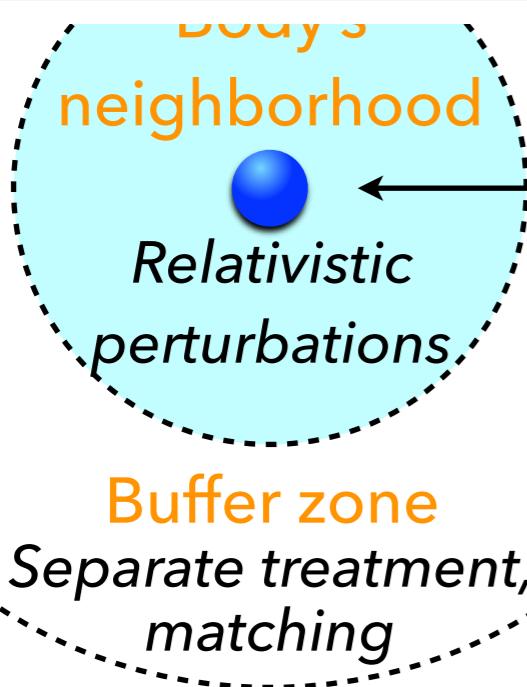
- ▶ Are there new, non-tidal interactions in GR that impact the early inspiral?
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Tidal effects in nonspinning binaries

► Matched asymptotic expansions (for $D \gg R$, to all orders in ϵ):

- There are **NO** GR non-tidal interactions [Flanagan 1998]
- **Body-dependence** of the equations of **motion** starts at $O(\alpha^5)$
- Tidal **deformation** of compact objects starts at $O(\alpha^3)$



Dimensionless parameters characterizing the system:

$$\epsilon = \frac{M}{R}$$

$$\alpha = \frac{R}{D}$$

$$\epsilon_{\text{orbit}} = \frac{M}{D}$$

Internal gravity

Tidal expansion

PN expansion

Tidal effects (nonspinning objects, leading order)

- Isolated object in equilibrium

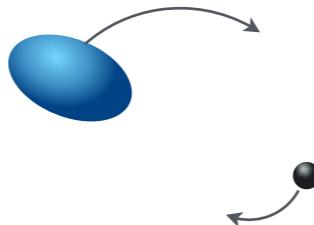


- In a binary: tidal field due to curvature produced by distant companion

$$\mathcal{E}_{ij} = R_{titj}$$

in object's rest frame

- linear response: object deforms



- Limit where variations in tidal field are much faster than object's internal timescales:

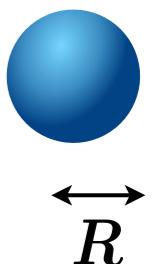
induced quadrupole

$$Q_{ij} = -\lambda \mathcal{E}_{ij}$$

tidal deformability parameter

$$\lambda = \frac{2}{3} k_2 R^5$$

dimensionless Love
number



Tidal deformability parameter

- Convert tensors to spherical harmonic decomposition, sufficient to consider $(l,m)=(2,0)$

$$Q = -\lambda \epsilon$$

- quantities defined by the asymptotic metric (buffer zone)
e.g. in the object's local rest frame:

$$\frac{(1 + g_{tt})}{2} = -\frac{m}{r} - \frac{3 Q Y_{20}(\theta, \phi)}{2 r^3} + \dots$$
$$+ \frac{1}{2} \epsilon r^2 Y_{20}(\theta, \phi) + \dots$$

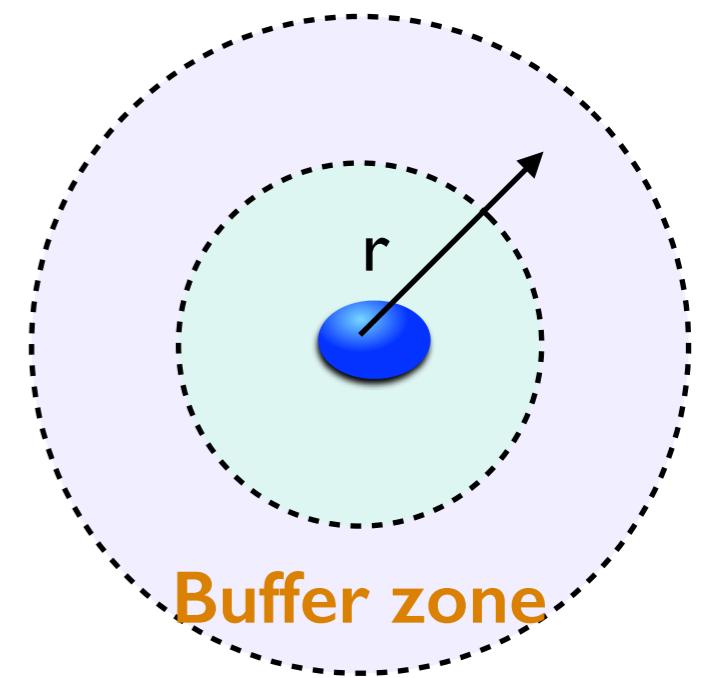
- Determined from Einstein's equations: linear static perturbations to equilibrium

[Hinderer 2008]

- $\lambda=0$ for a nonspinning BH

[e.g. Kol & Smolkin 2011]

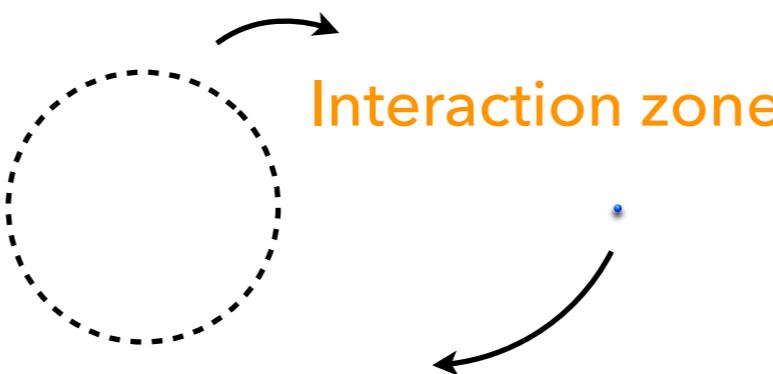
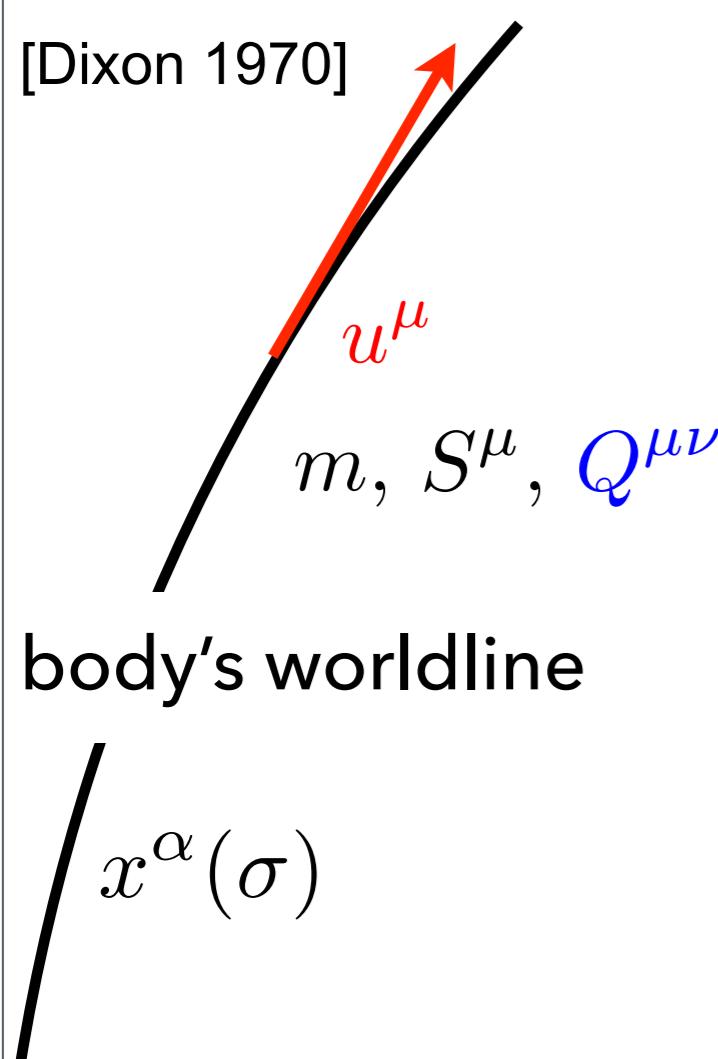
Similar method for higher multipoles [Damour, Nagar 2009, Binnington, Poisson 2009]



Tidal effects on the dynamics in the interaction zone

World-line-skeleton
for extended bodies

[Dixon 1970]



Two-body dynamics described by an effective action:

$$S = S_{\text{pp}} + \int d\sigma [L_{\text{tidal}} + L_{\text{internal}}]$$

point-mass
contribution

$$L_{\text{tidal}} = -\frac{z}{2} \mathcal{E}_{\mu\nu} Q^{\mu\nu}$$

$$z = \sqrt{-u_\mu u^\mu}$$

dynamics of
quadrupole

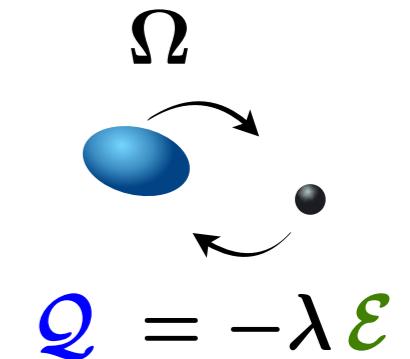
$$Q^{\mu\nu}$$

[Goldberger 2010
Steinhoff+2016]

Influence on the GWs

- ▶ Energy goes into deforming the NS

$$\textcolor{brown}{E} \sim E_{\text{orbit}} + \frac{1}{4} \mathcal{Q} \mathcal{E}$$



- ▶ moving tidal bulges contribute to gravitational radiation

$$\dot{E}_{\text{GW}} \sim \left[\frac{d^3}{dt^3} (Q_{\text{orbit}} + \mathbf{Q}) \right]^2$$

$$M = m_1 + m_2$$

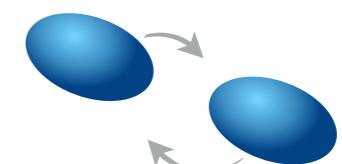
- ▶ approx. GW phase:

$$\frac{d\phi_{\text{GW}}}{dt} = 2\Omega, \quad \frac{d\Omega}{dt} = \frac{\dot{E}_{\text{GW}}}{d\textcolor{brown}{E}/d\Omega}$$

$$\Delta\phi_{\text{GW}}^{\text{tidal}} \sim \lambda \frac{(M\Omega)^{10/3}}{M^5}$$

- ▶ for two extended objects, tidal analogue of the chirp mass is:

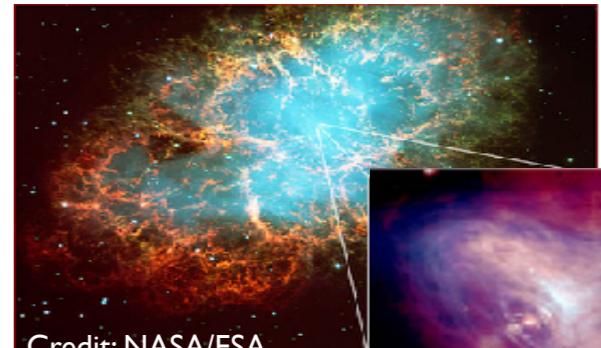
$$\tilde{\Lambda} = \frac{1}{26} \left[\left(1 + 12 \frac{m_2}{m_1} \right) \lambda_1 + \left(1 + 12 \frac{m_1}{m_2} \right) \lambda_2 \right]$$



Neutron stars (NSs)

- ▶ **densest** stable material **objects** known in the universe
- ▶ **1939**: theoretical description [Oppenheimer & Volkoff]
- ▶ **thousands observed to date**

debris from a supernova
explosion in 1054



Crab Pulsar
(NS rotating at 30 rev/sec)



crushed to neutron-star
compactness



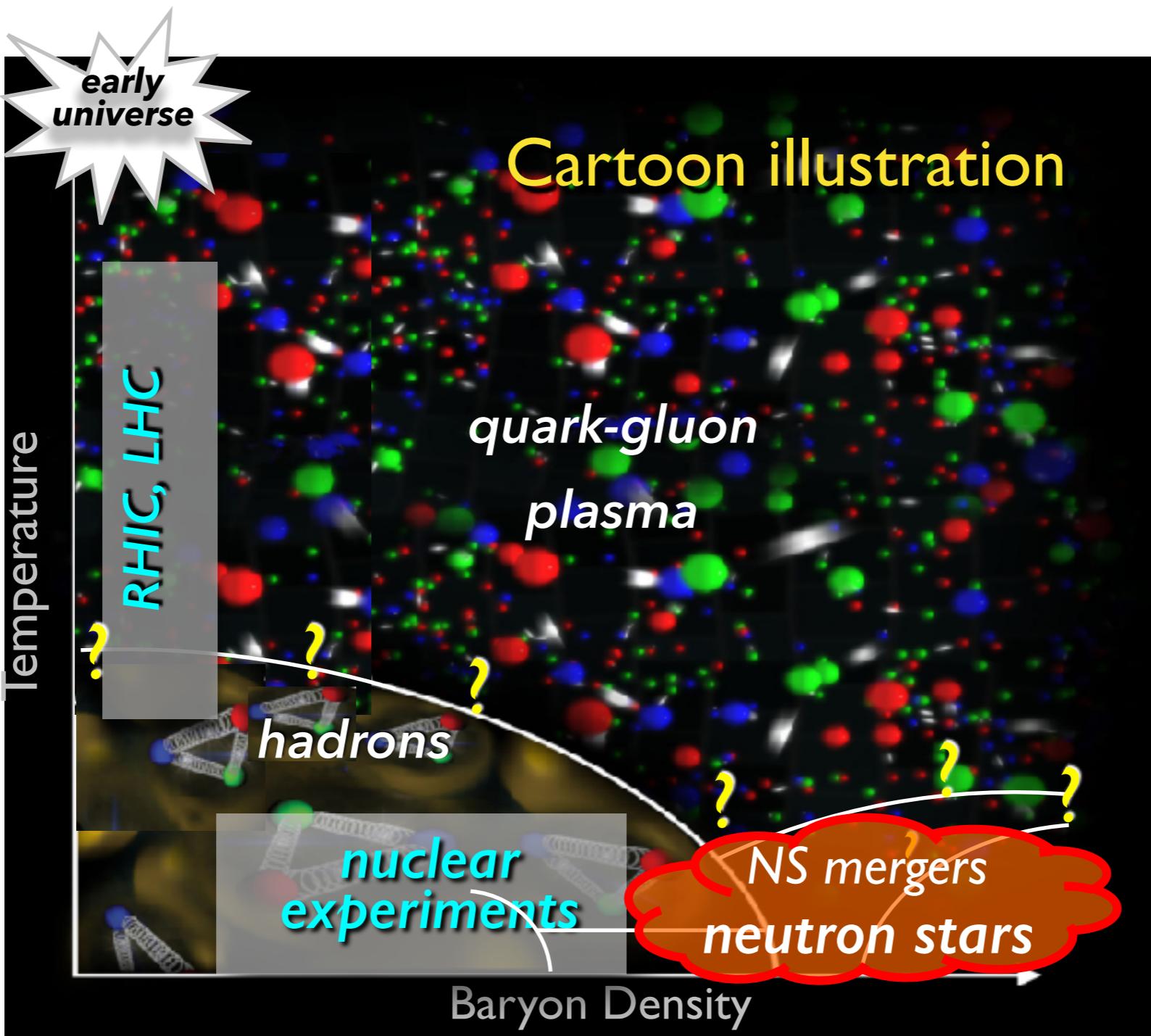
crushed



Black hole

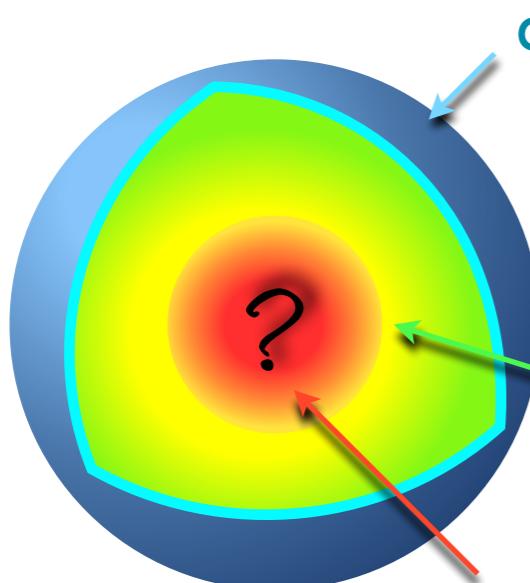
What is the nature of matter in such extreme conditions?

Phases of QCD



Credit: F. Linde

Conjectured Neutron Star (NS) structure



crust ~ km
neutron rich ions,
free neutrons

outer core
uniform liquid

deep core
 $\sim 2-10x$ nuclear density
exotic states of matter?
deconfined quarks?
signatures of new physics?

[iron ~ 10 g/cm³]

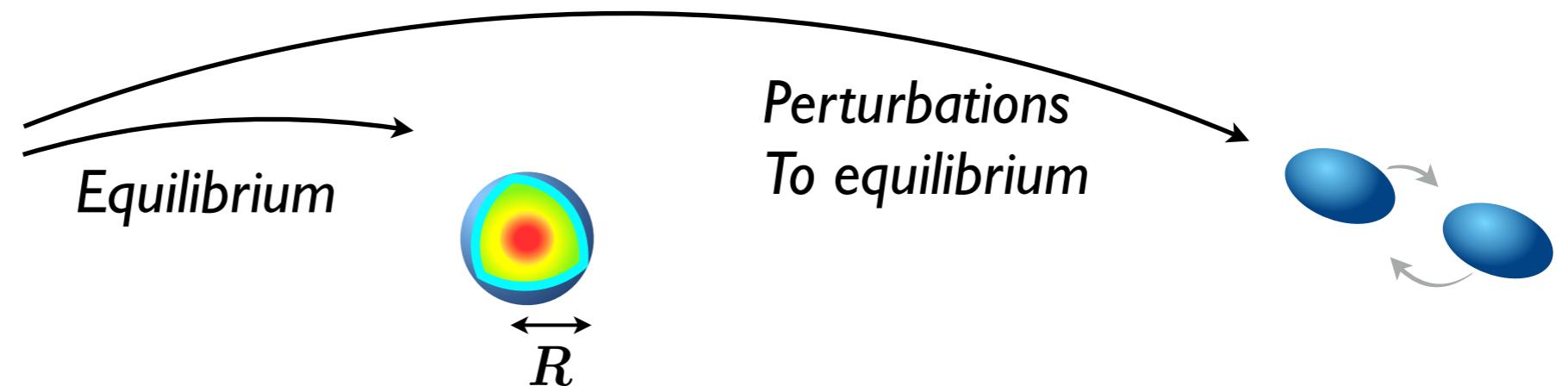
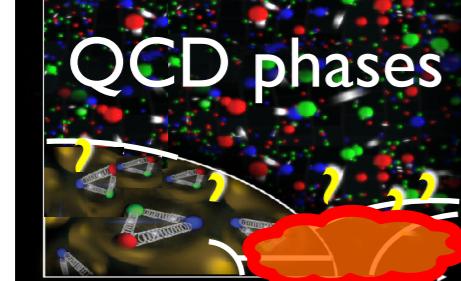
$\sim 10^6$ g/cm³ inverse β -decay

$\sim 10^{11}$ g/cm³ neutron drip

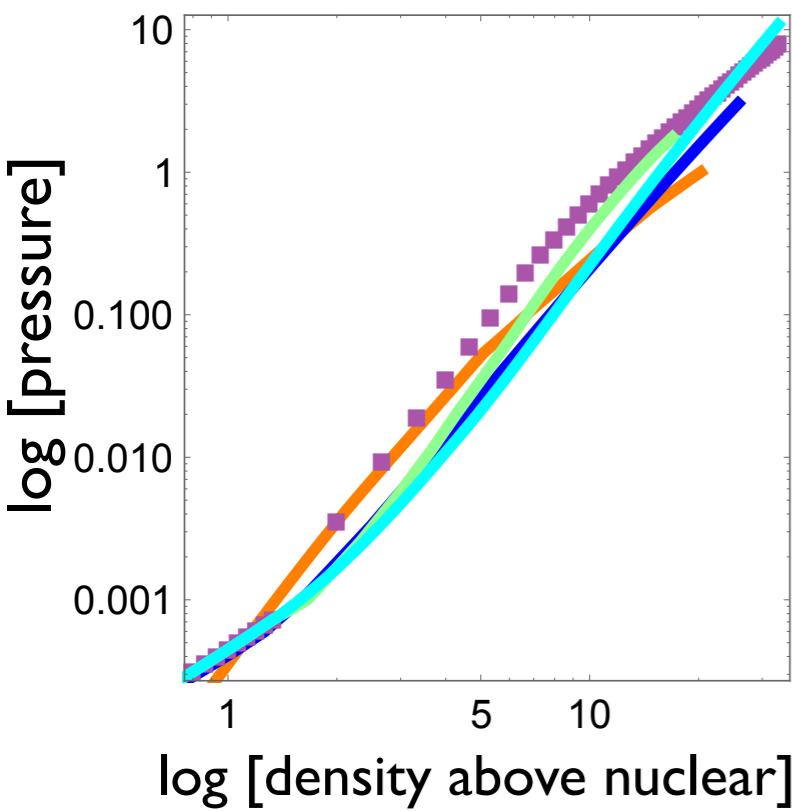
$\sim 10^{15}$ g/cm³

- ▶ many theoretical difficulties
- ▶ far extrapolations from known physics

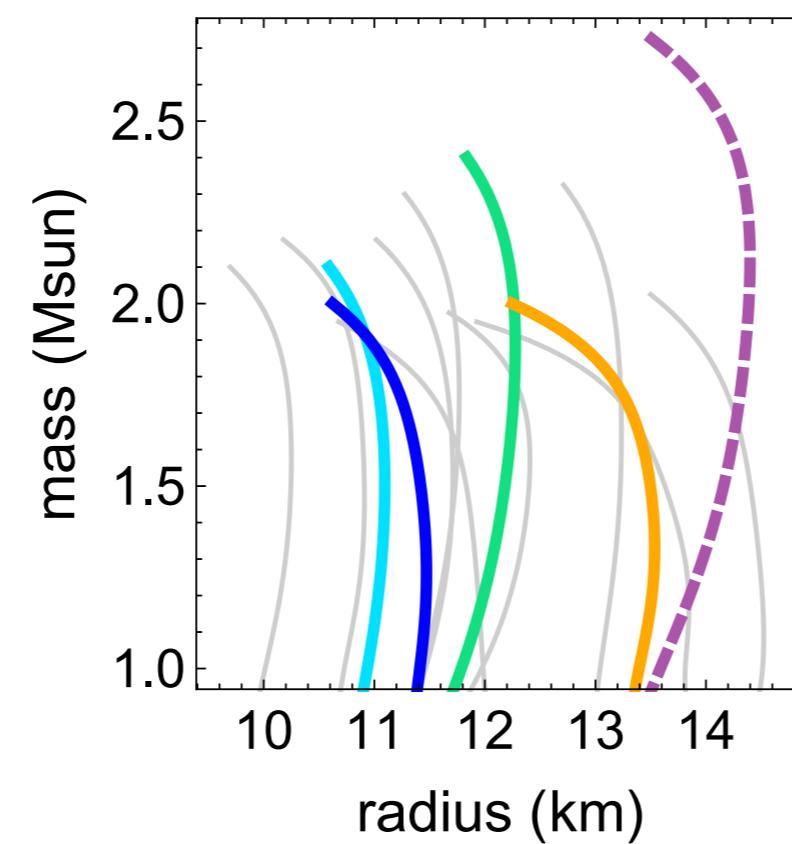
Properties of NS matter reflected in global observables



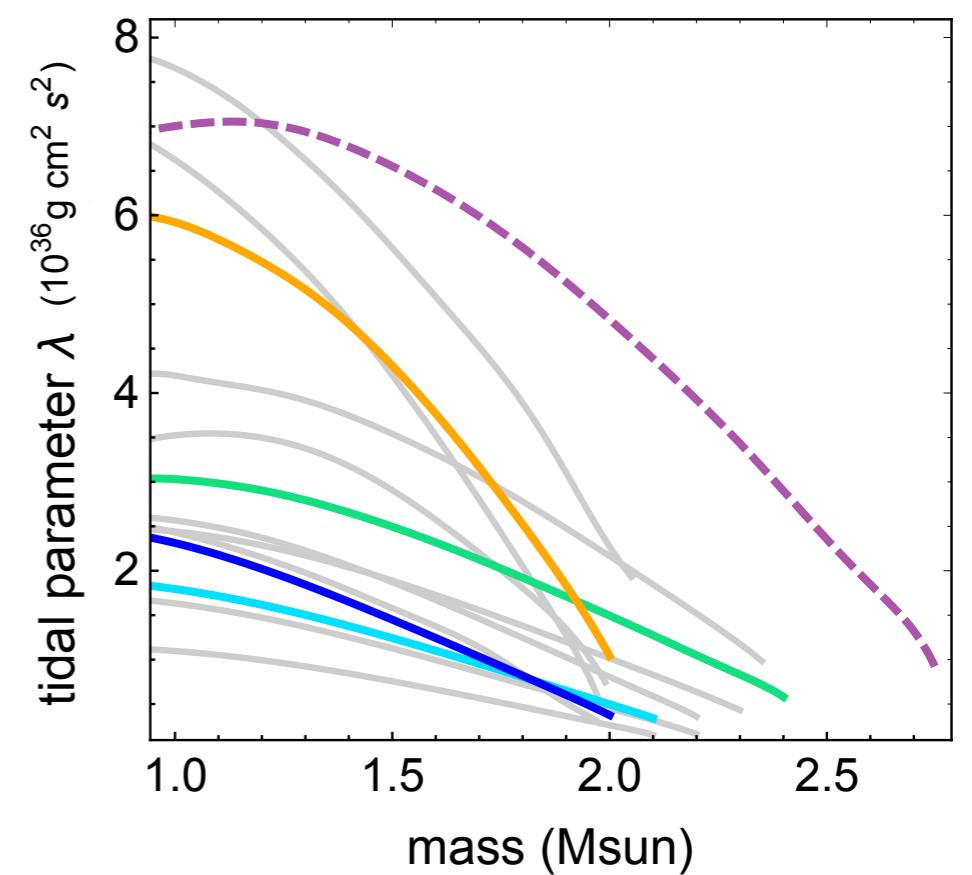
NS matter models
(equations of state)



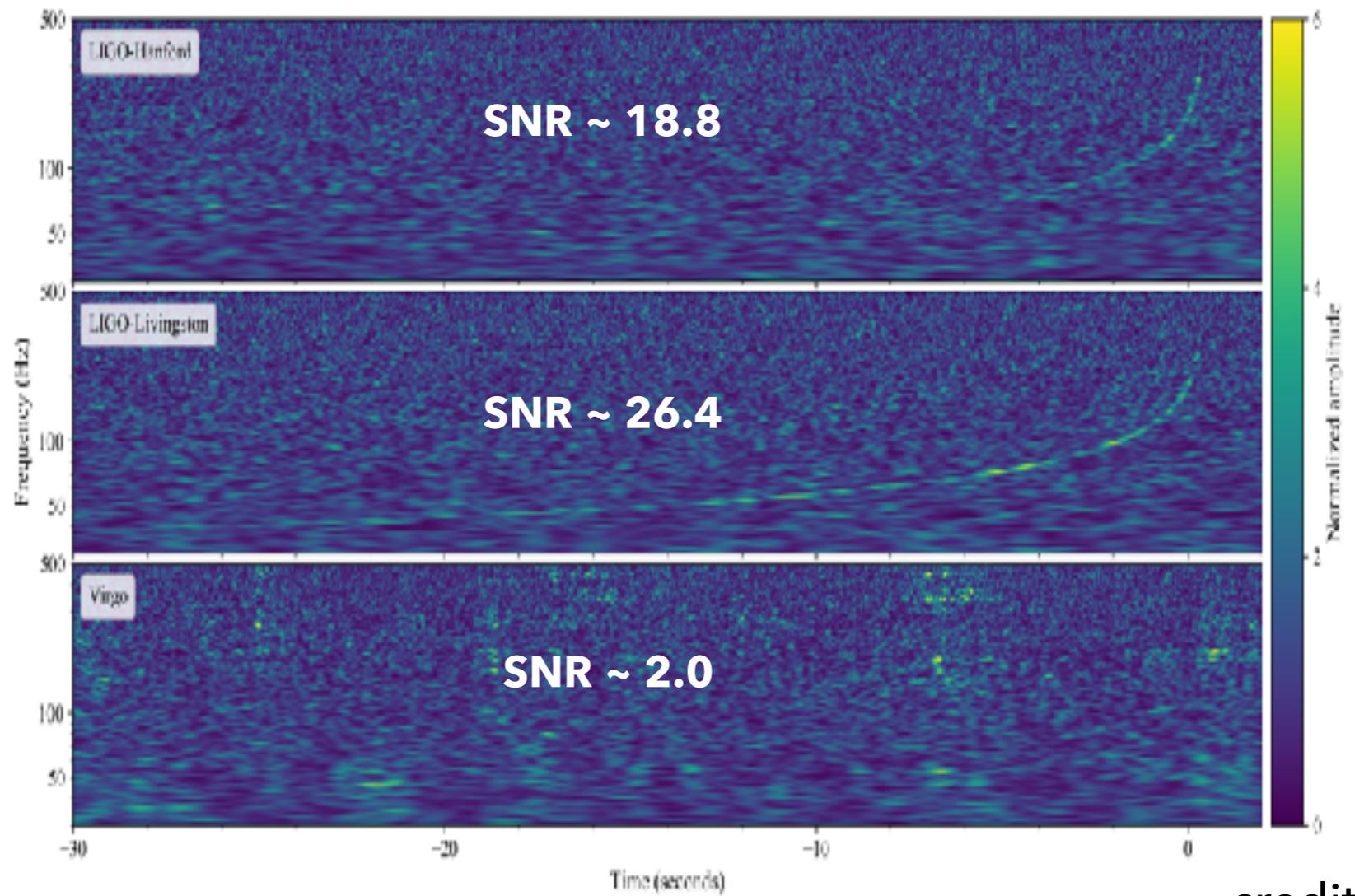
Mass vs. radius



tidal deformability λ vs. mass



Aug. 17, 2017: binary neutron star merger GW170817



credit:LVC

Distance: ~40 Mpc

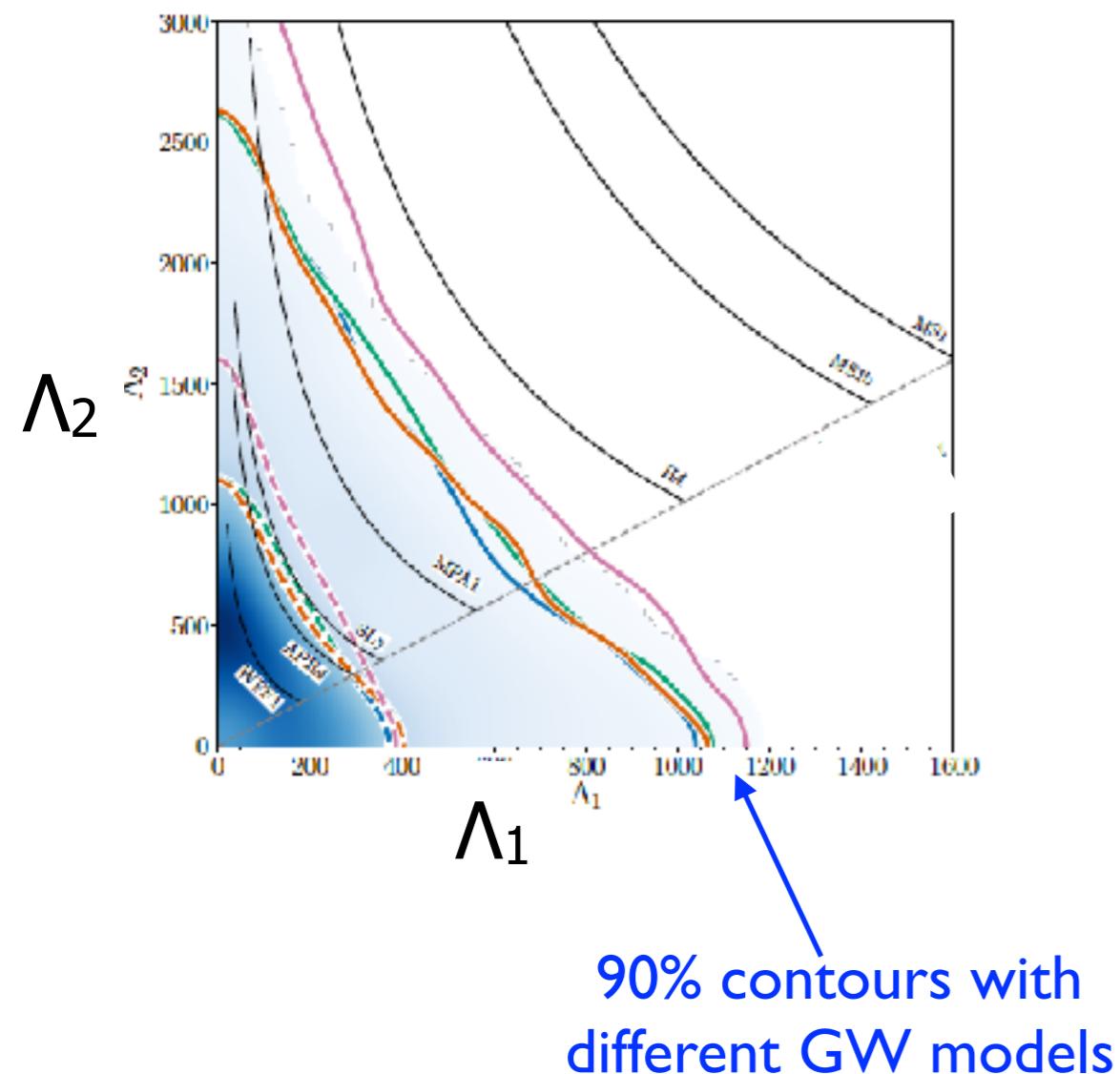
Total mass: ~ 2.74 Msun

Loudest, closest, richest in science

Longest: ~100 s (c.f. <2 s for GW151226)

Measurements of tidal deformability for GW170817

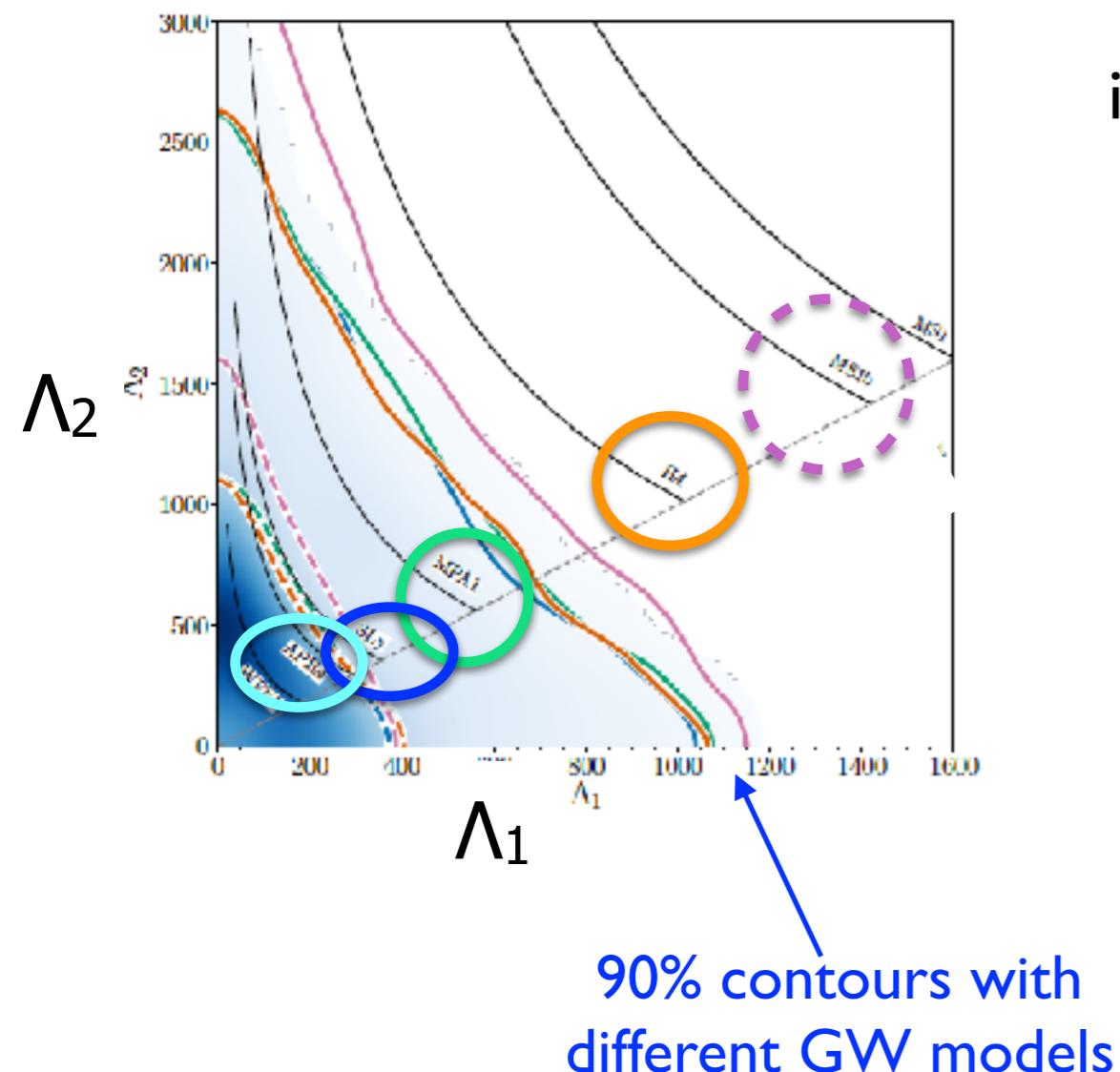
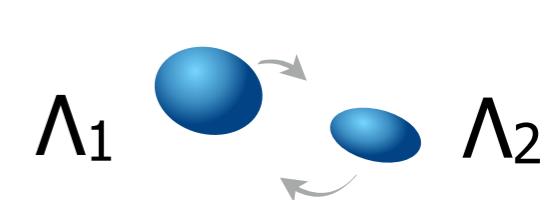
- Results for dimensionless tidal deformability $\Lambda = \frac{\lambda}{m_{\text{NS}}^5}$ allowing for high spins:



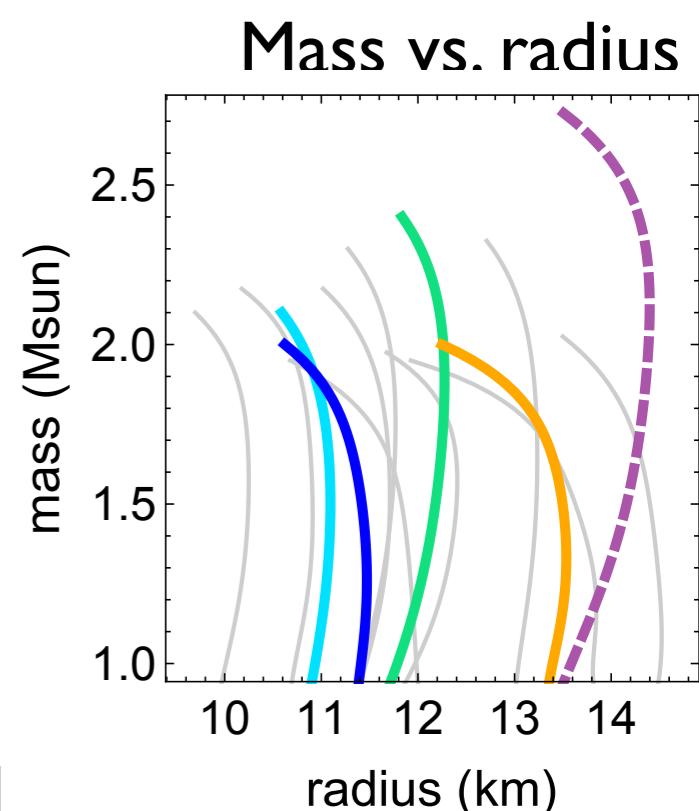
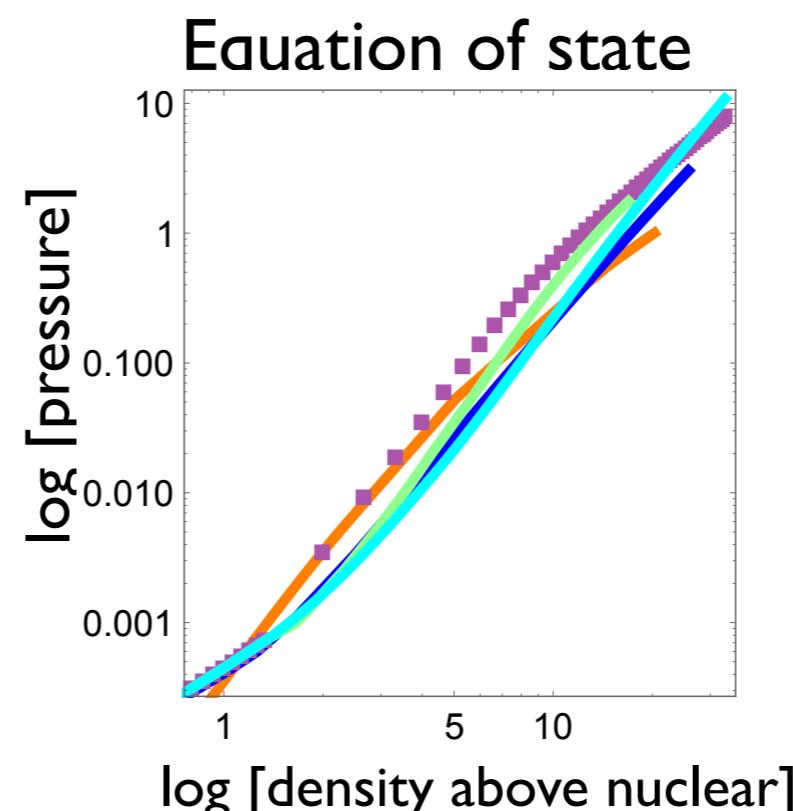
LVC arXiv:1805.11579

Measurements of tidal deformability for GW170817

- ▶ Results for dimensionless tidal deformability $\Lambda = \frac{\lambda}{m_{\text{NS}}^5}$ allowing for high spins:

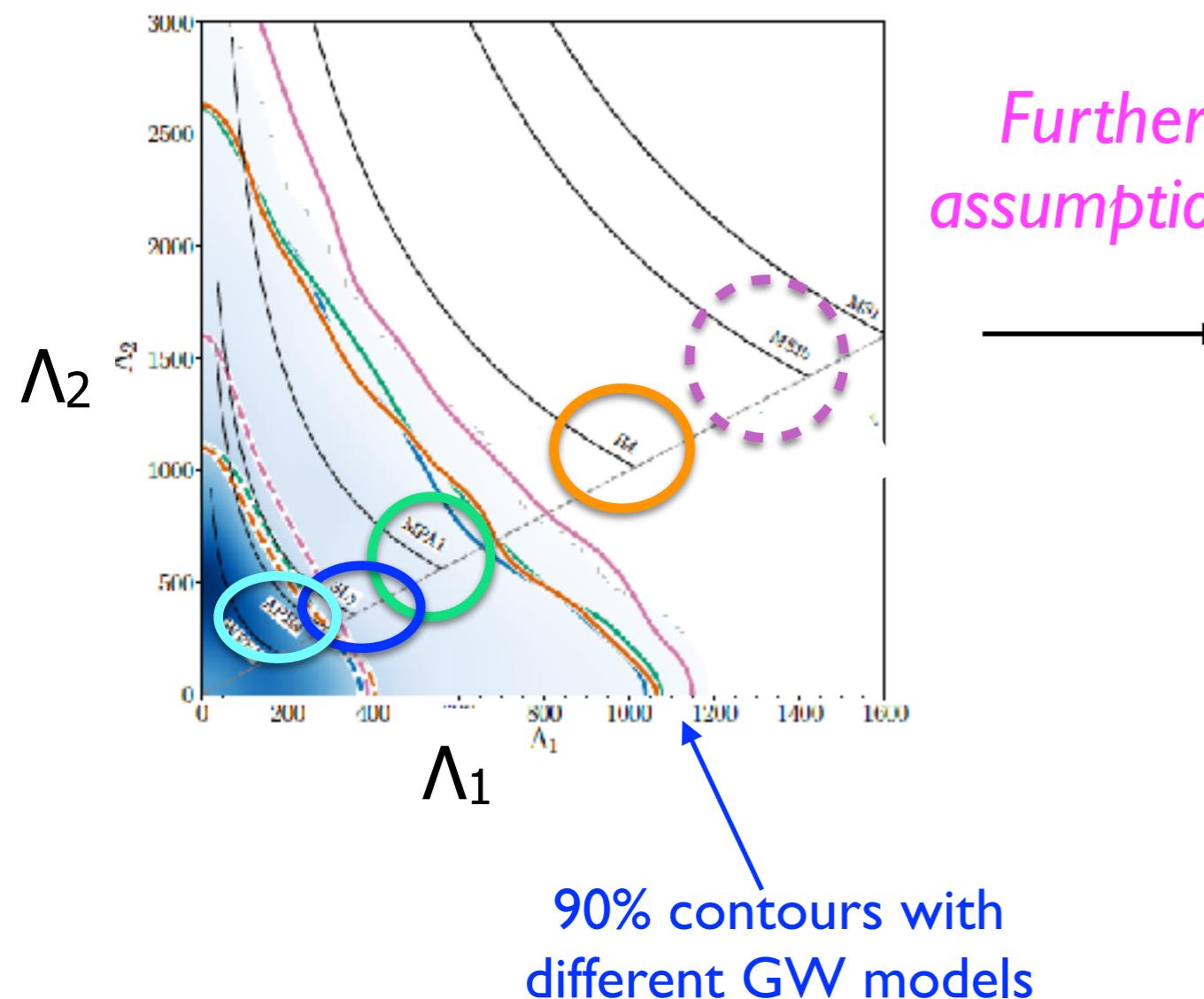
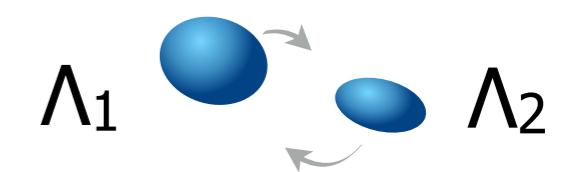


if two NSs:

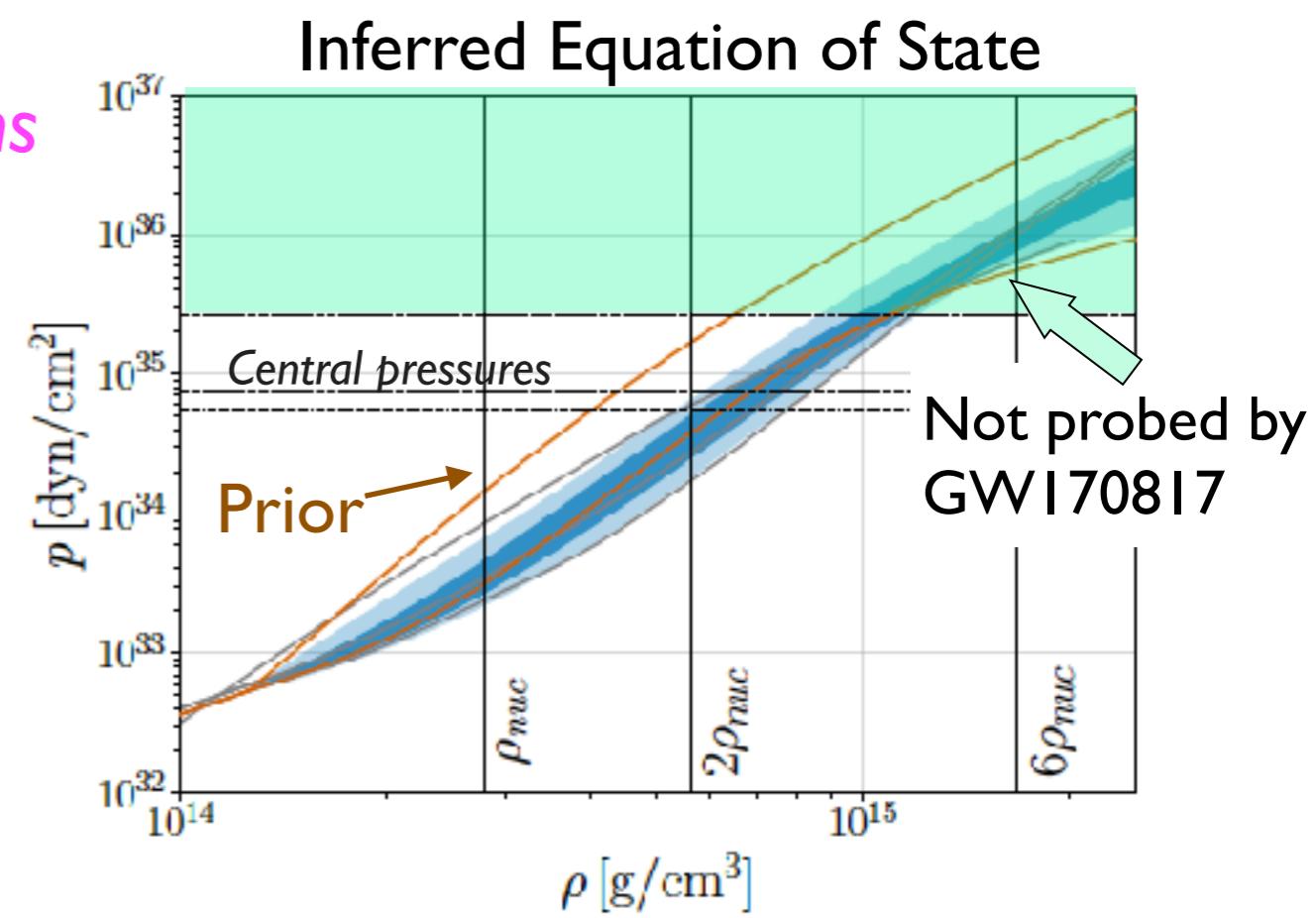


Measurements of tidal deformability for GW170817

- ▶ Results for dimensionless tidal deformability $\Lambda = \frac{\lambda}{m_{\text{NS}}^5}$ allowing for high spins:



*Further
assumptions*

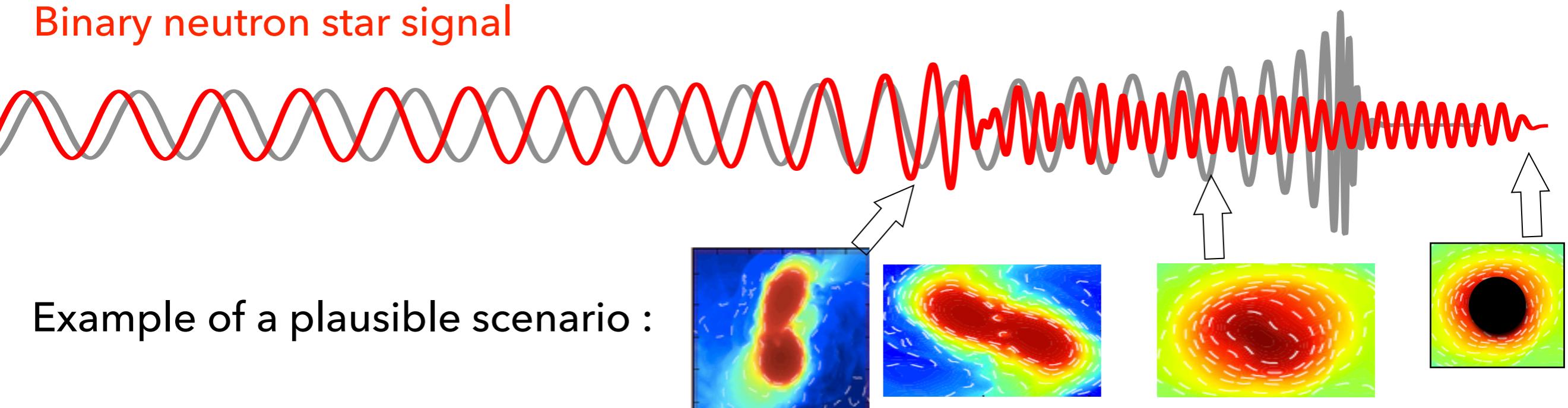


90% contours with
different GW models

What happened post-inspiral? If a NS-NS system

NR data: T. Dietrich

Binary neutron star signal



Example of a plausible scenario :

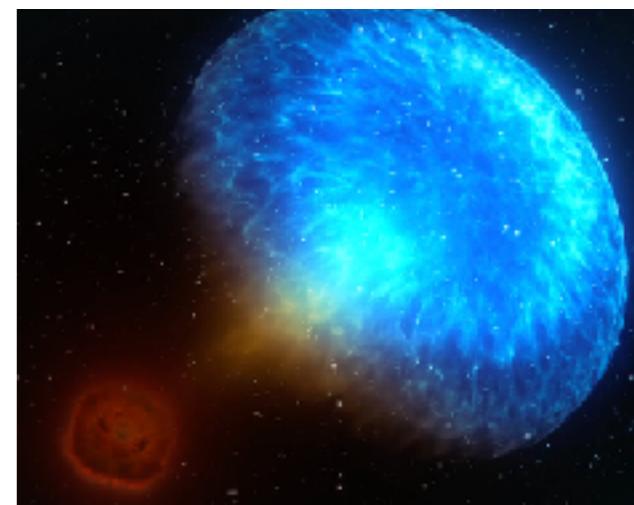
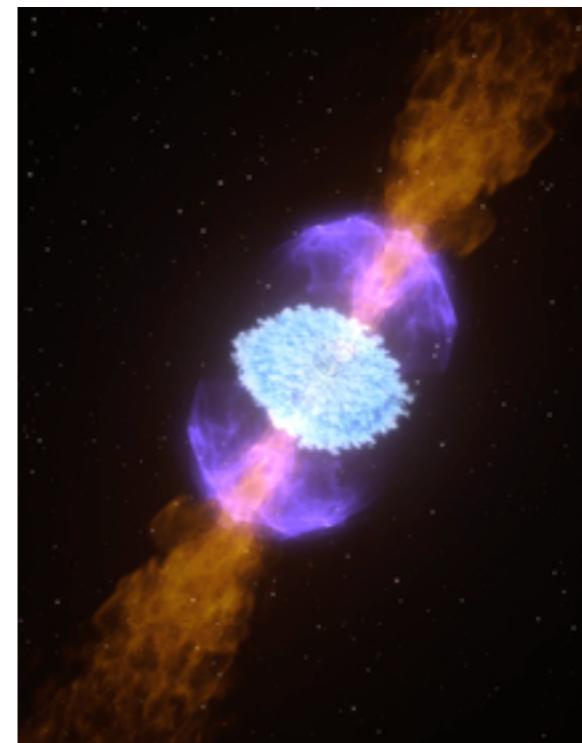
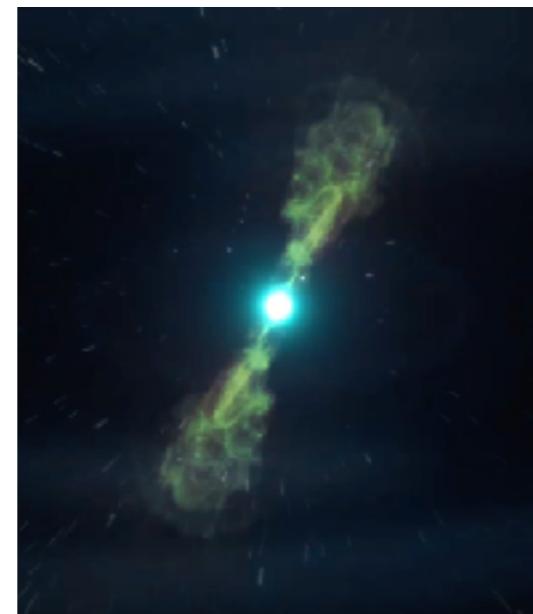
Couldn't tell anything about their fate from GWs

.... but lots of information from spectacular electromagnetic counterparts
at all wavelengths

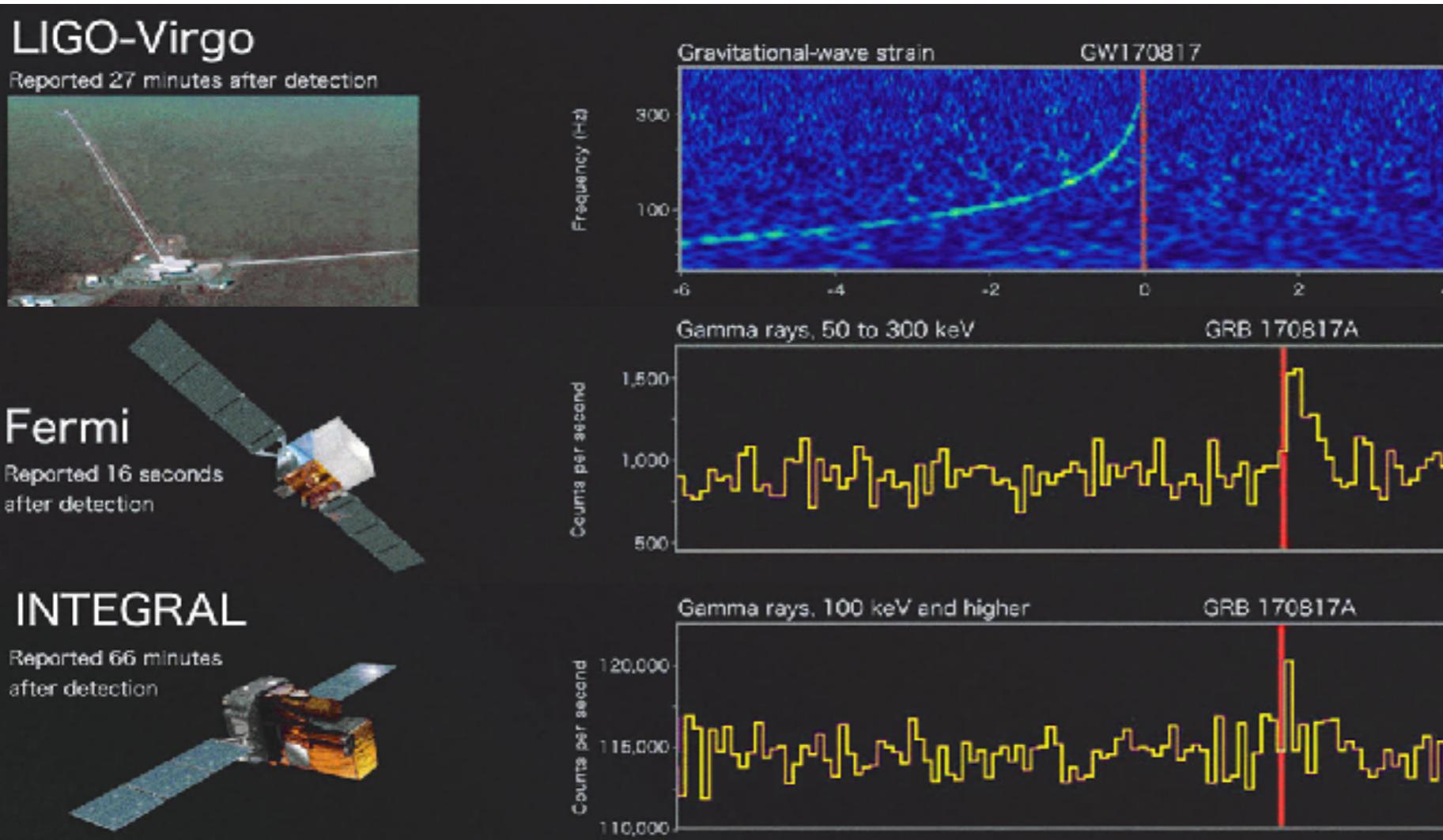
Relativistic outflows of neutron-rich material



**Shocks, collision with interstellar medium,
and nuclear reactions : wide range of
electromagnetic signals (+neutrinos)**



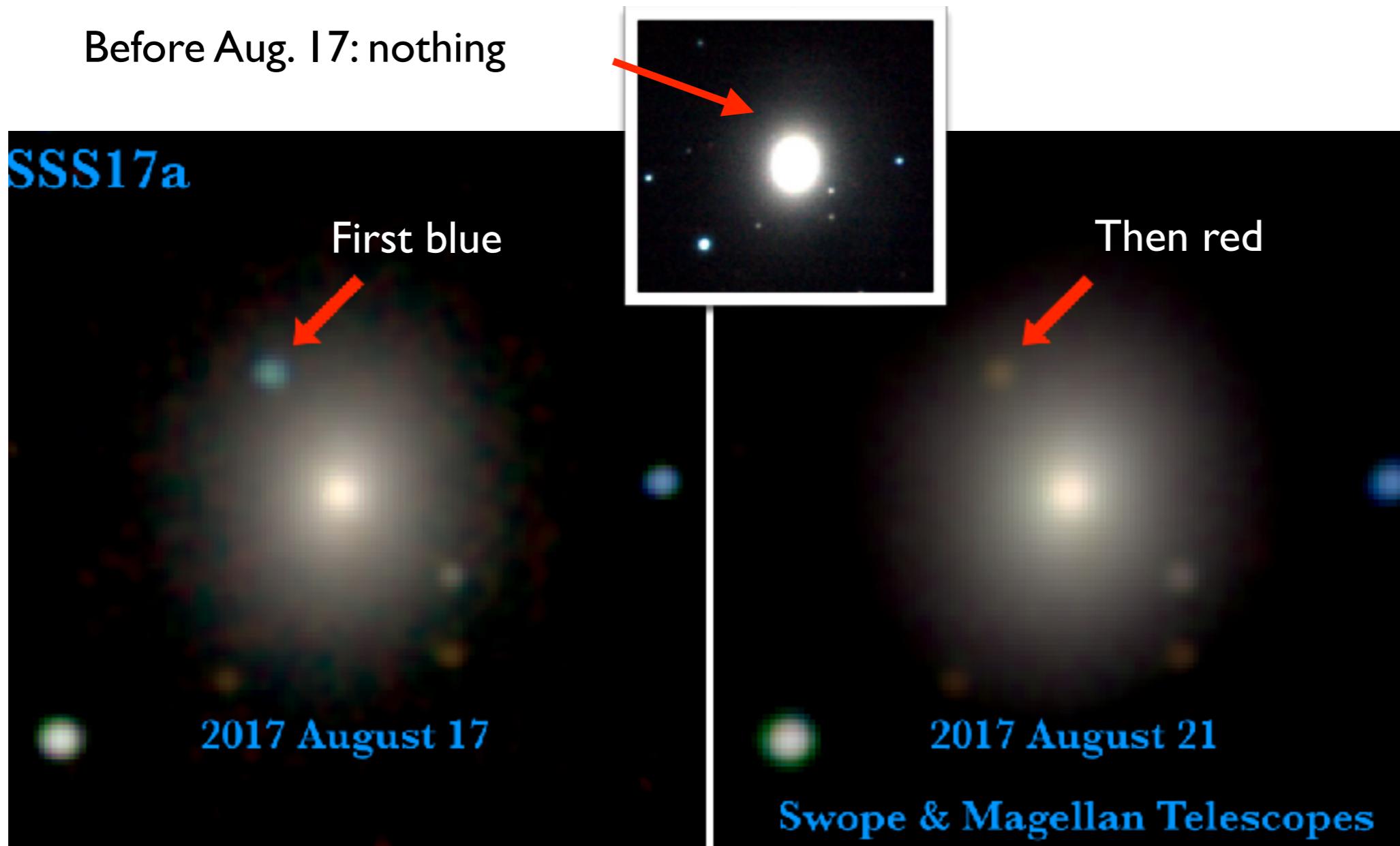
Multimessenger observations of GW170817



1.7 s after signal in LIGO ended:
Short gamma-ray burst

- ▶ Observed arrival times (travel over 130 million light years):
 - ▶ test speed of gravity, Lorentz invariance, and equivalence principle

Optical observations



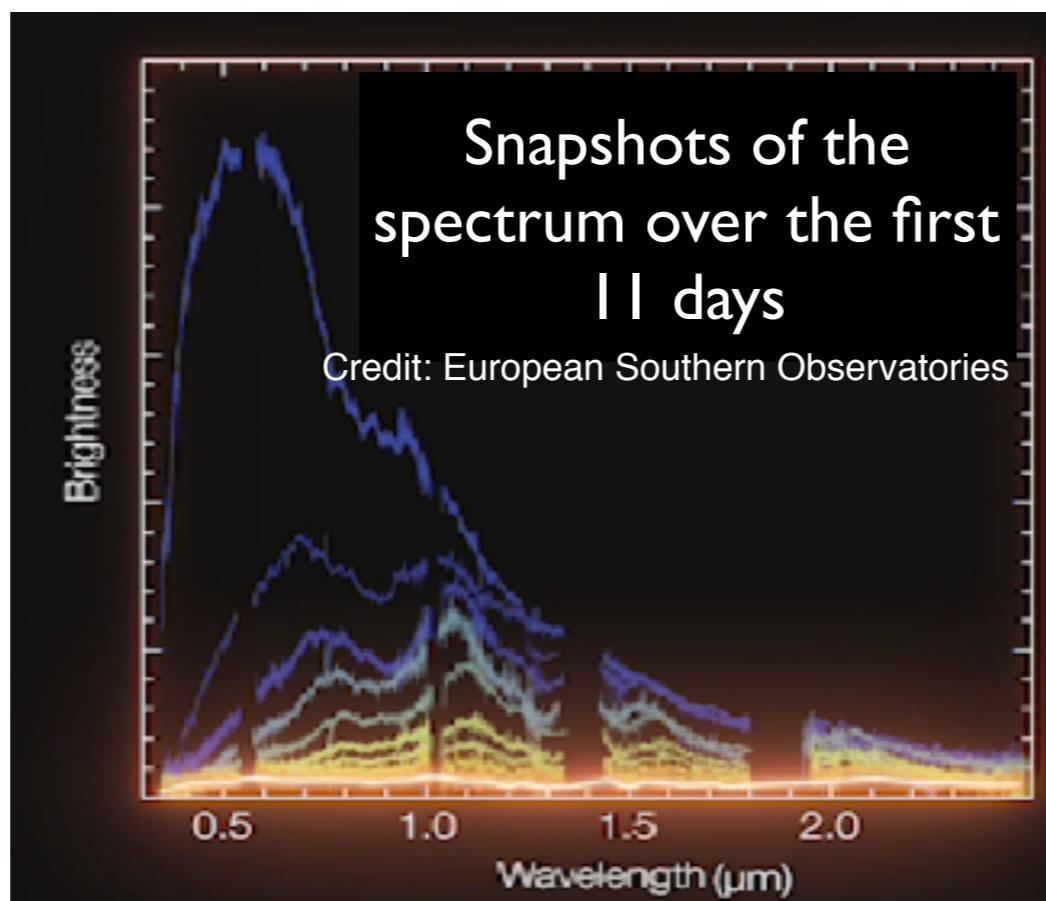
Credit: NASA

EM counterpart



Credit: NASA

- Numerous multiwavelength EM observations
- Focus on UVOIR:



Credit: ESO

Kilonova
characteristic of r-process
nucleosynthesis

Production site of heavy elements

Periodic Table of the Elements

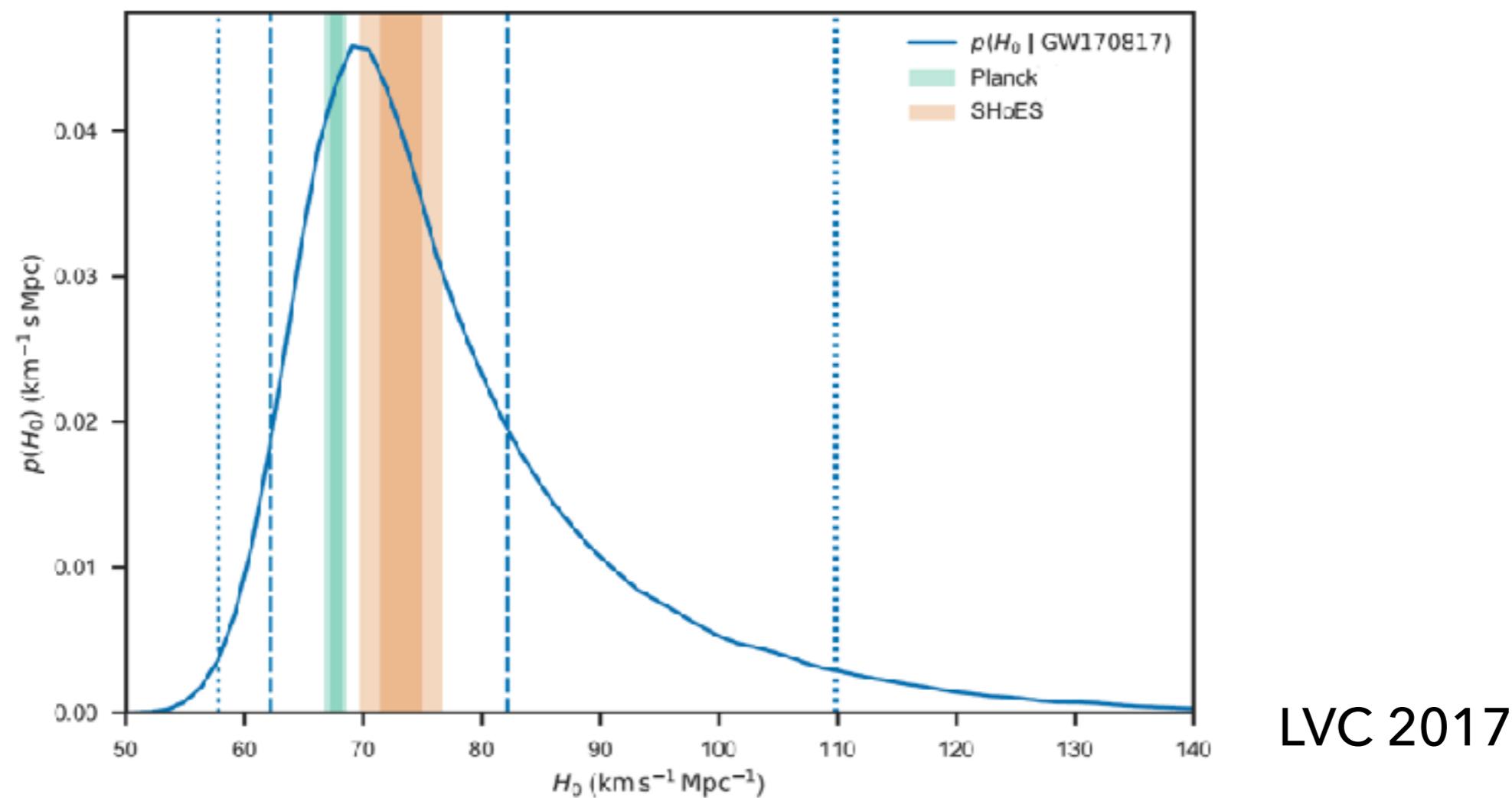
[Credit: Caltech LIGO labs]

1 H															2 He		
3 Li	4 Be																
11 Na	12 Mg																
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra																
57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu			
89 Ac	90 Th	91 Pa	92 U														

Yellow: Formed by Merging Neutron Stars

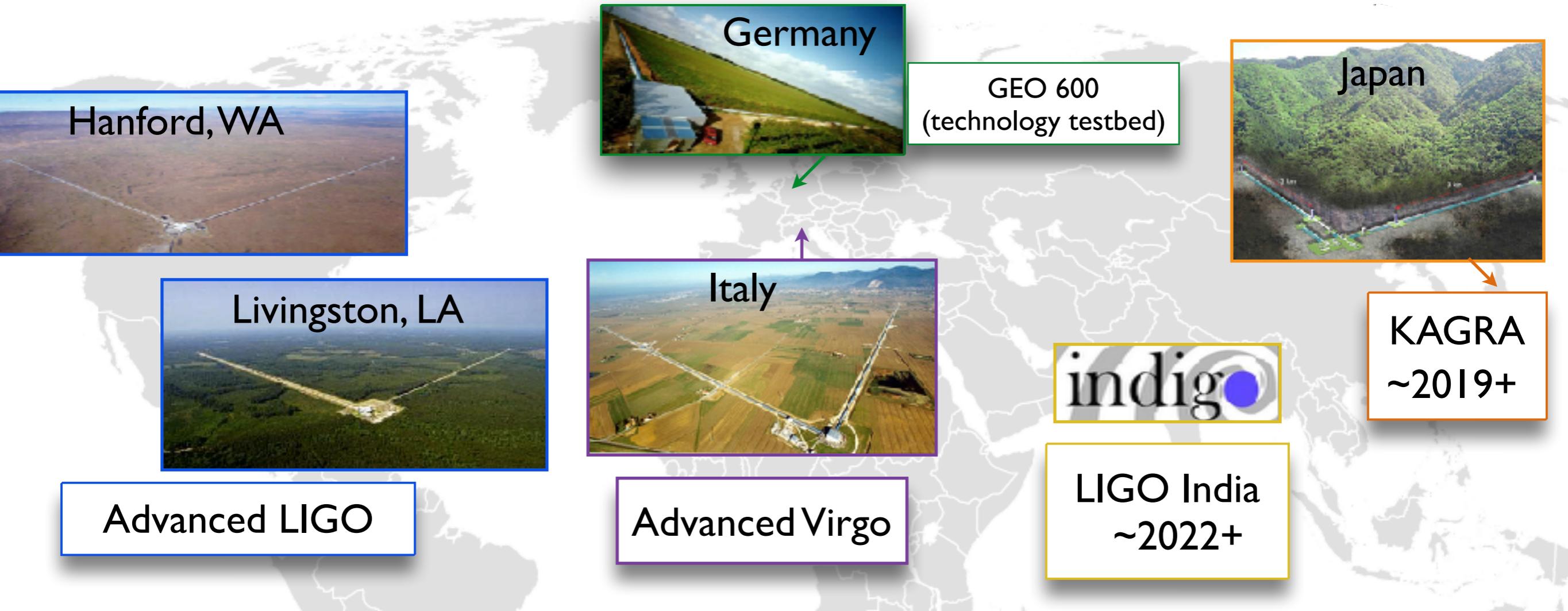
More combined GW & EM science

- ▶ Source localized to NGC 4993 (Elliptical galaxy ~130 million light years away)
- ▶ From GWs: luminosity distance to source
- ▶ Combine to infer Hubble constant:



Outlook

Upcoming worldwide network of GW detectors



Future upgrades, new detectors (?) e.g. Einstein Telescope, Cosmic Explorer

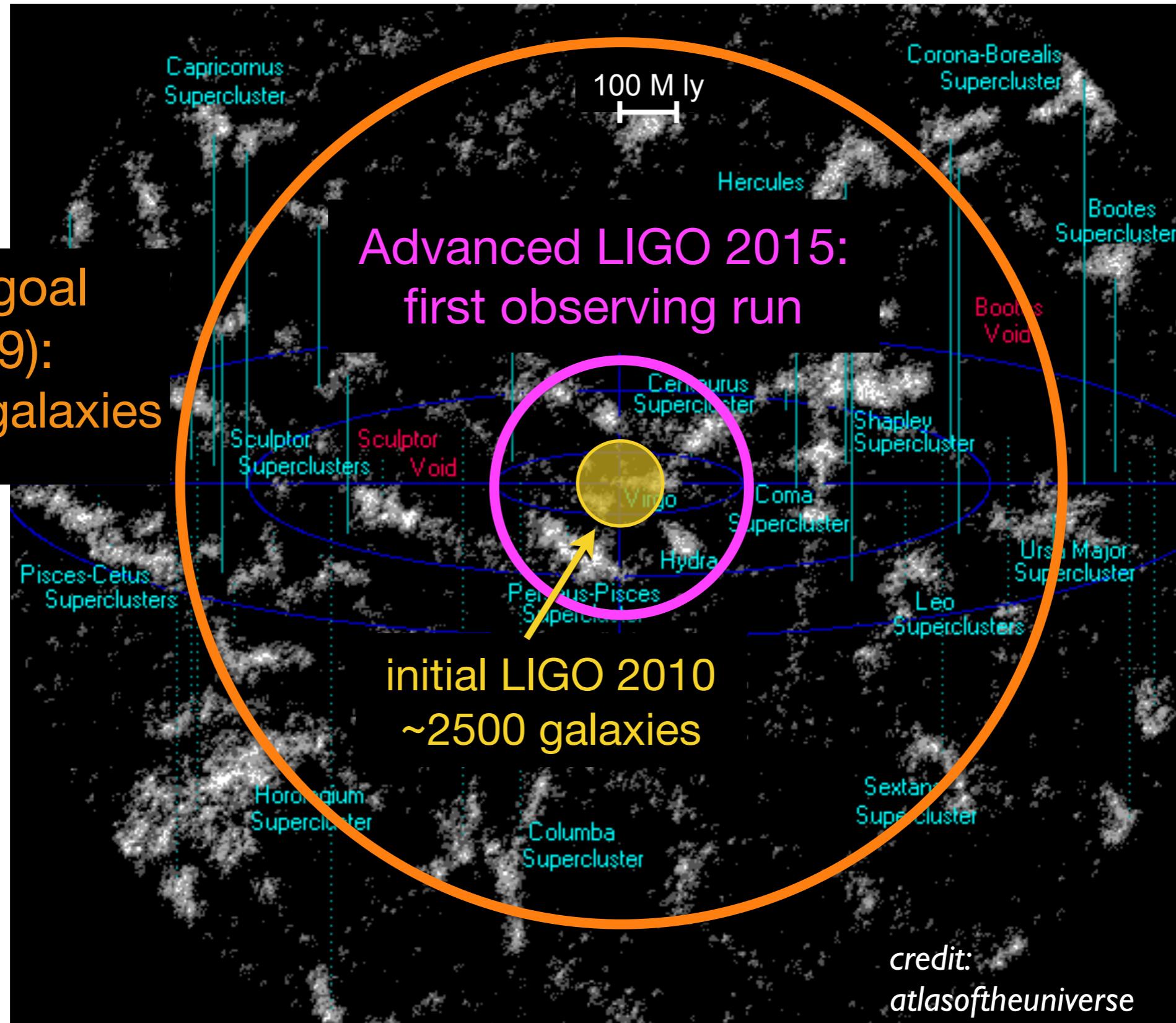
- preparatory studies (experimental, site selection, ...) underway,
- international team currently preparing 3G science case document



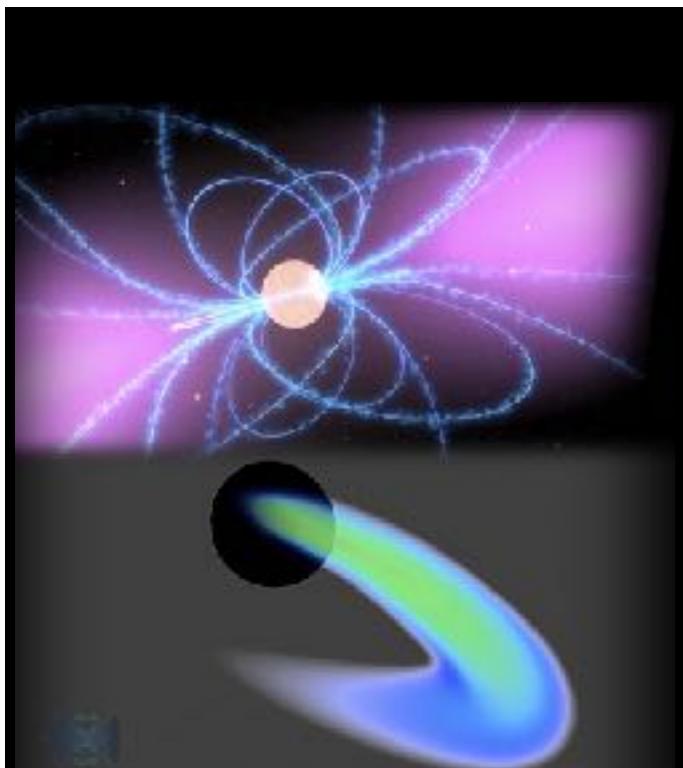
Pulsar timing arrays: GWs in nanoHertz window



Visible volume of the universe (for binary neutron stars)



Other sources for ground-based detectors: a few examples



Binaries:

- inspirals of **neutron stars** into BHs

Continuous, nearly monochromatic signals

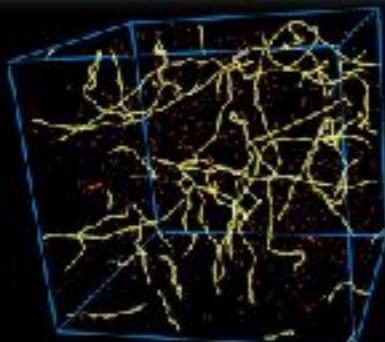
- single **neutron stars**
 - Distortions (mountains, accretion)
 - wobbles
 - unstable modes

Burst signals:

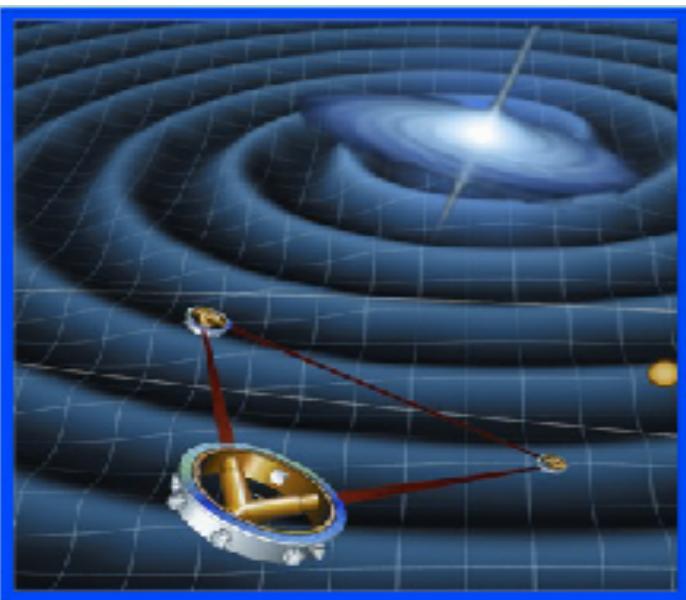
- supernovae [$h \sim 10^{-20}$ if at $D = 10\text{kpc}$]

Stochastic background:

- cosmic strings, early universe physics

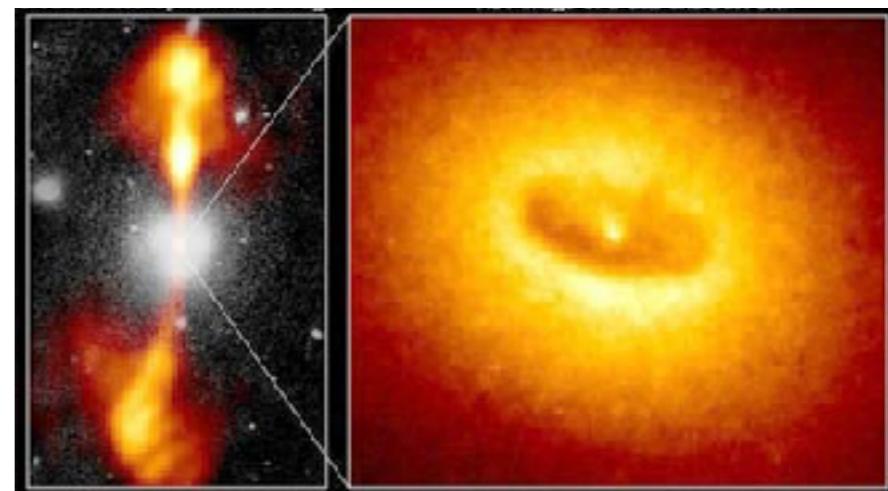
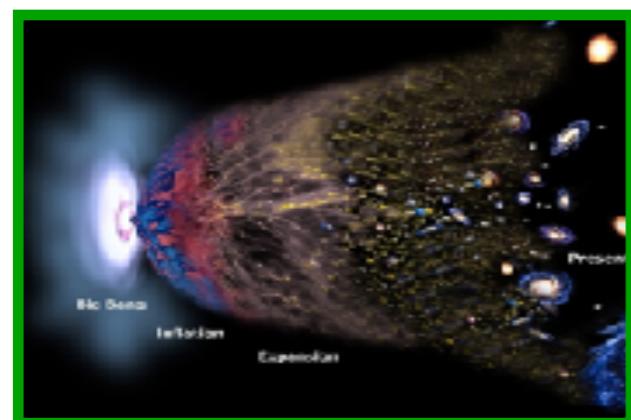


Next step: LISA (lower frequency window than LIGO)



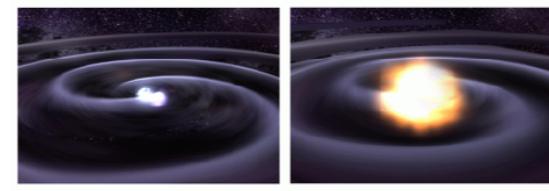
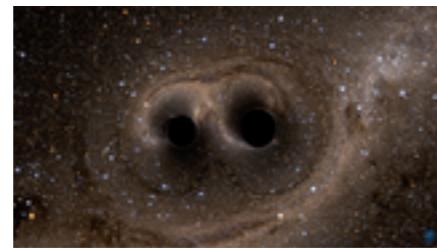
ESA-led mission, scheduled launch date in 2034:
new era of discoveries: mHz GW window

- formation, growth history of massive black holes
- stellar populations and dynamics in galactic nuclei
- exquisitely accurate tests of General Relativity and black holes
- cosmology
- multimessenger studies



Outlook

- gravitational waves now available as a channel of information about the universe
- even more science gains with joint electromagnetic/neutrino observations
- Much remains to be studied, further developments needed, progress underway



Expect a wealth of new insights in the coming years - decades