

Quo vadis Cosmology?

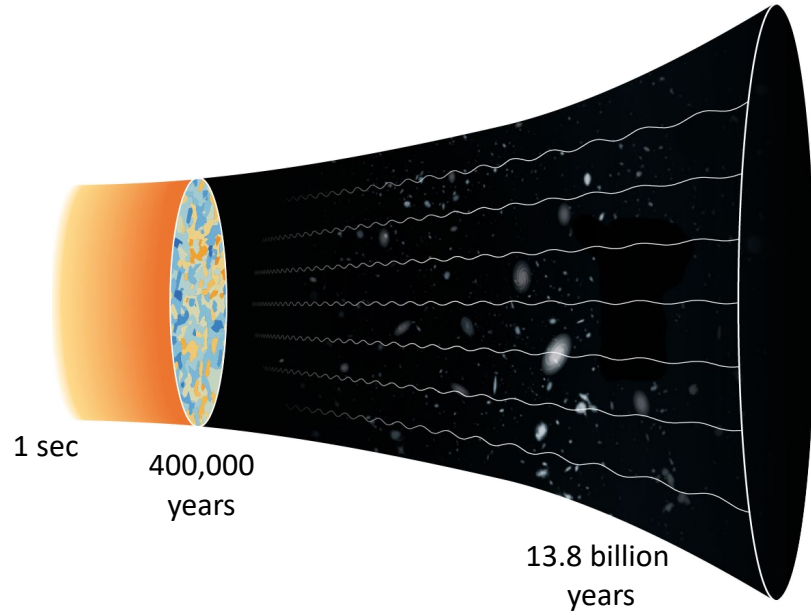
Paul Steinhardt (Princeton)
Anna Ijjas (NYU)

Copenhagen
August 19, 2022

The Road to Precision Cosmology

Michael Turner, Ann. Rev. Nucl. Part. Sci. (2022)

The past 50 years has seen cosmology go from a field known for the errors being in the exponents to precision science . . . with the Λ CDM paradigm as its crowning achievement.

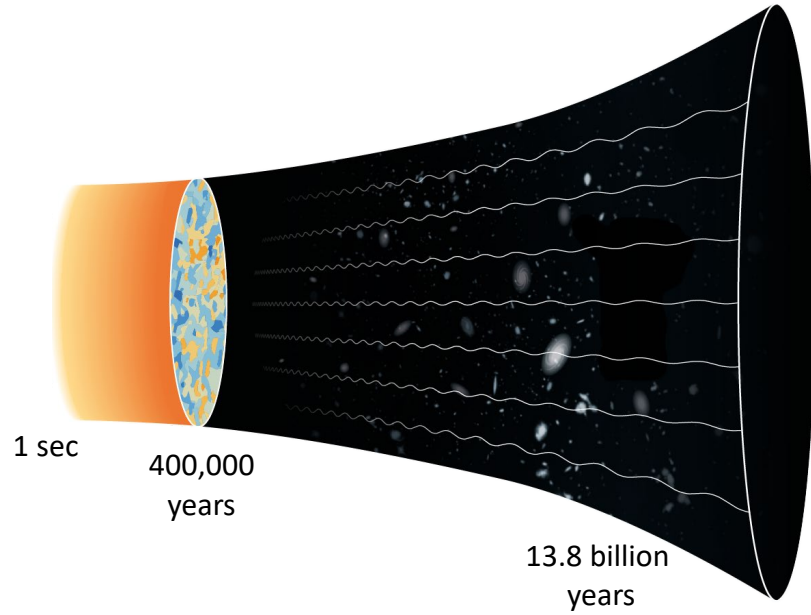


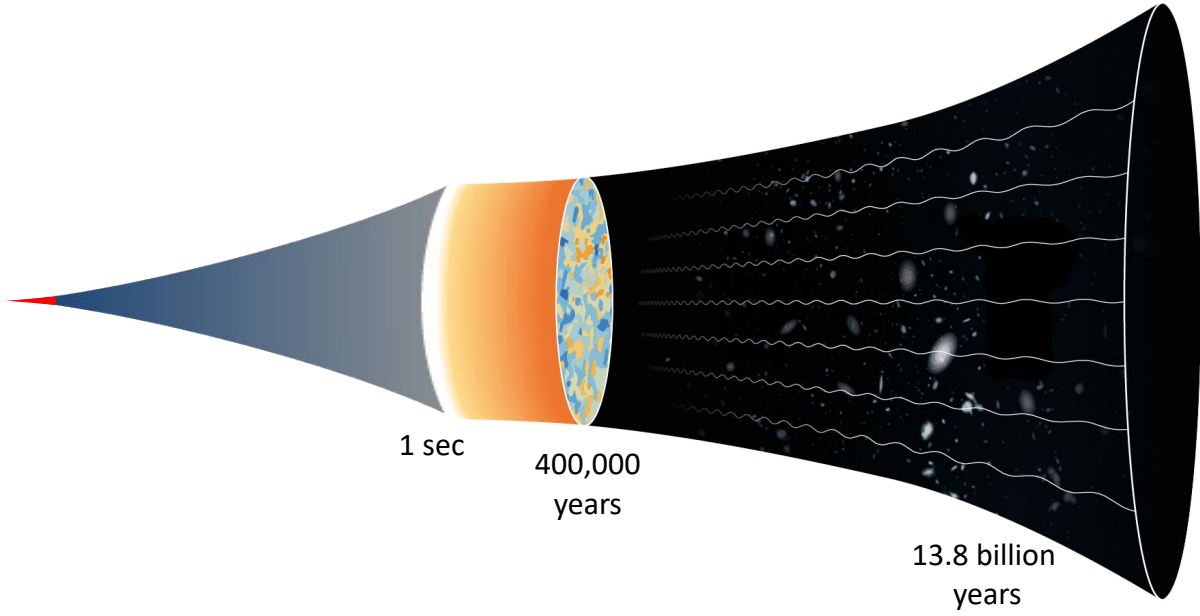
The Road to Precision Cosmology

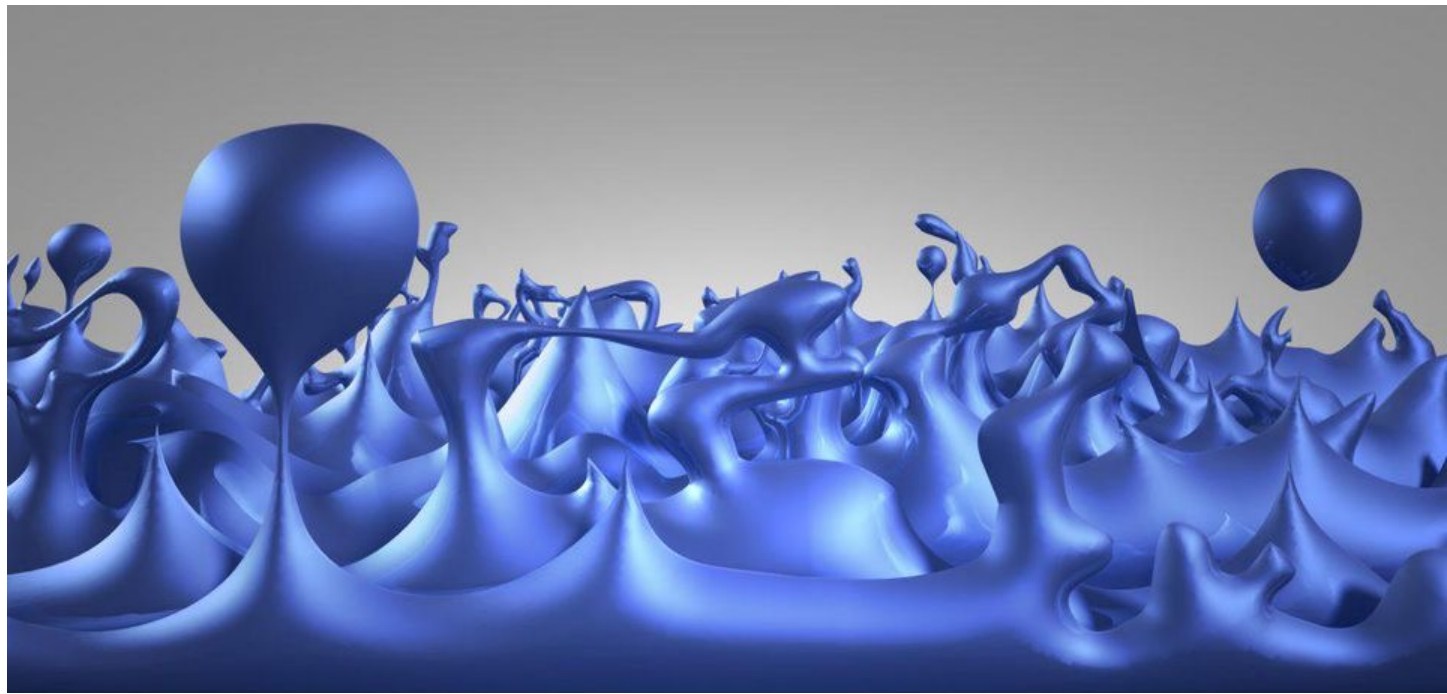
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Kuhnian shift

We could be on the wrong track . . . the modern equivalent of Ptolemy's epicycles.







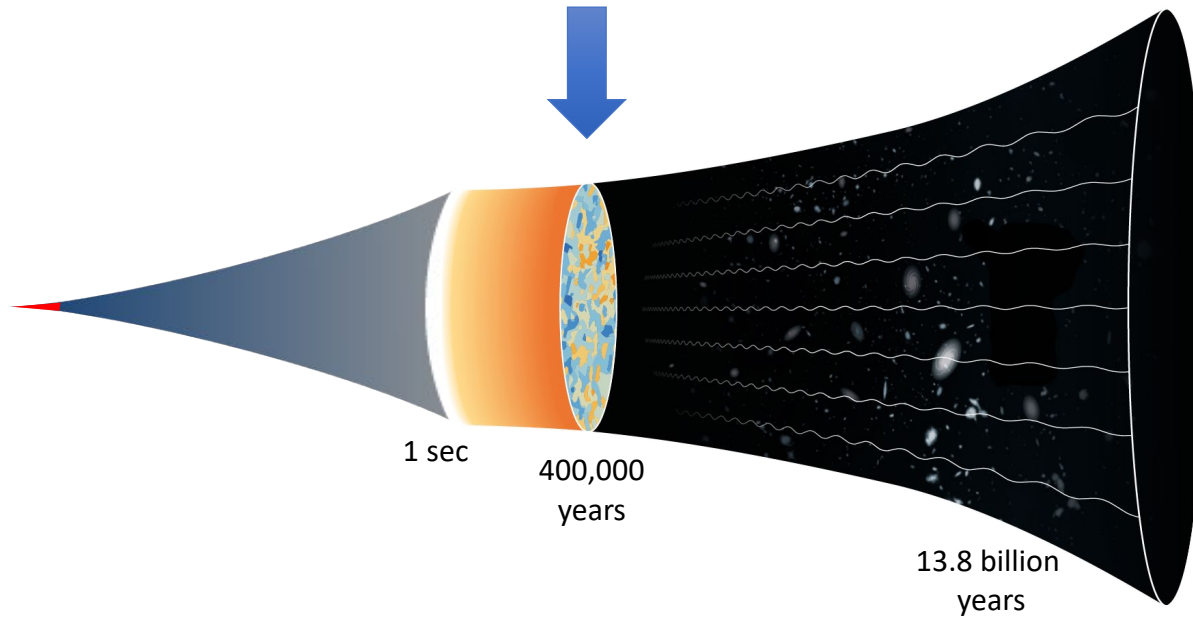
the big bang has always been a sketchy idea

mathematical singularity

quantum foam, emergent spacetime, tunneling from nothing, ...

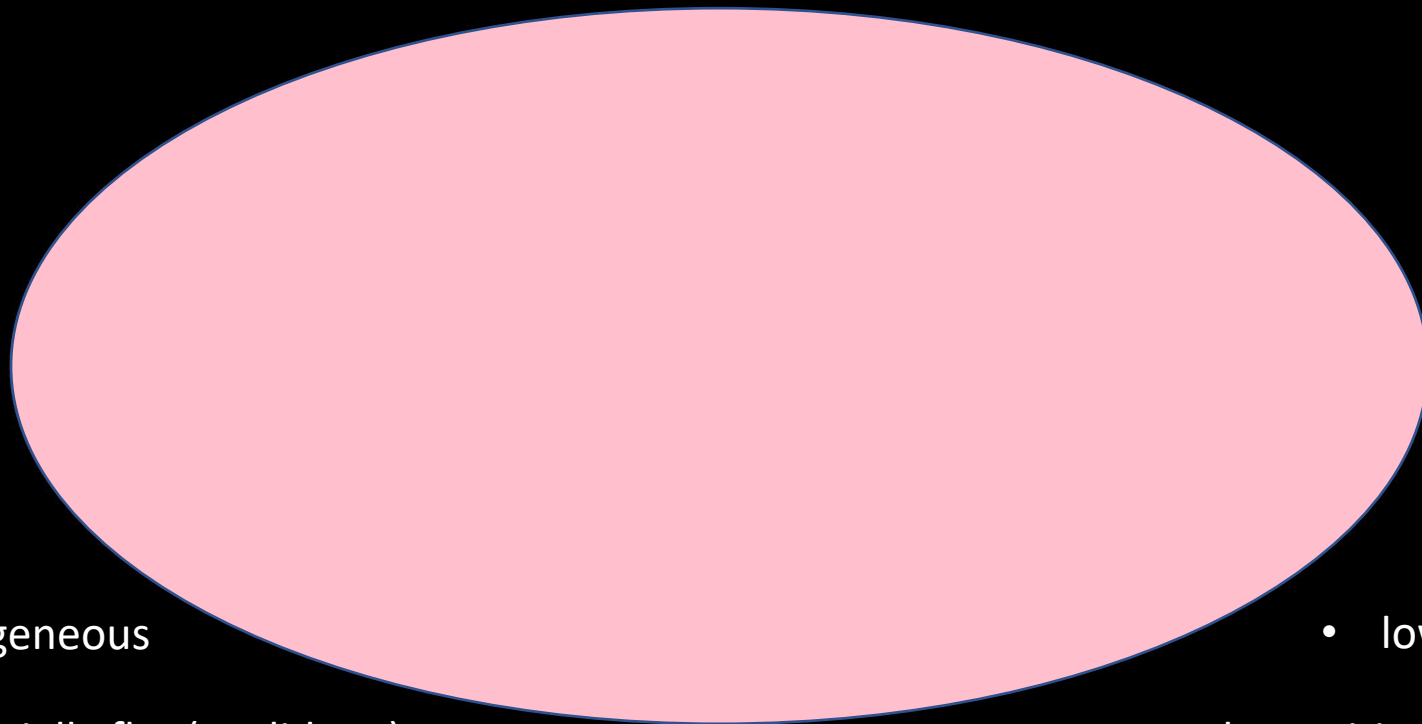
no accepted theory

cosmic microwave background radiation



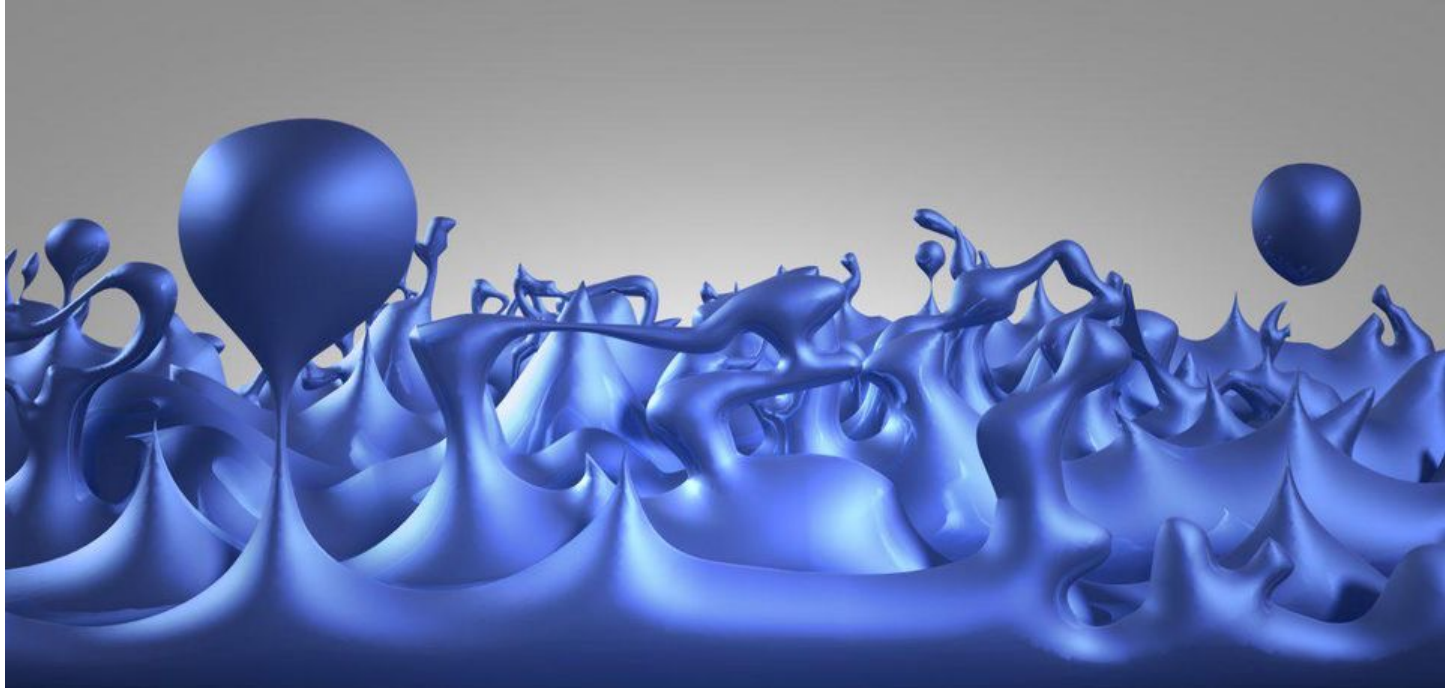
*a big bang followed by expansion may not be able to explain
the salient observable features of our universe*

the salient features of our universe

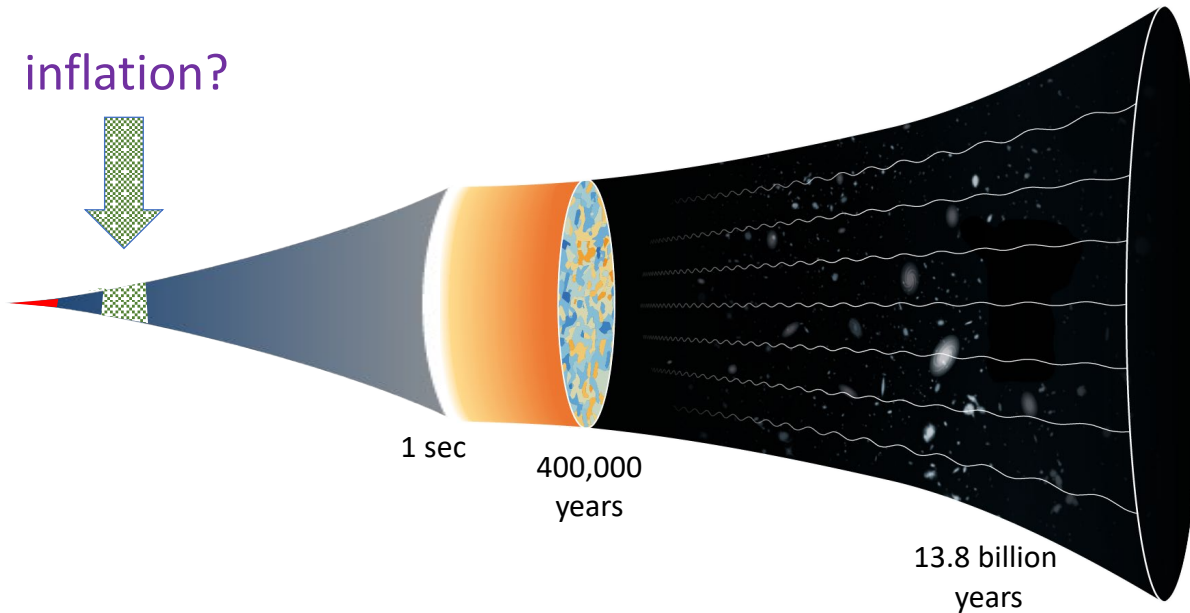


- homogeneous
- spatially flat (Euclidean)
- well-described by classical physics
- low entropy
- strangely partitioned entropy

a big bang is exactly the opposite



inhomogeneous, curvy, high entropy, and inherently quantum



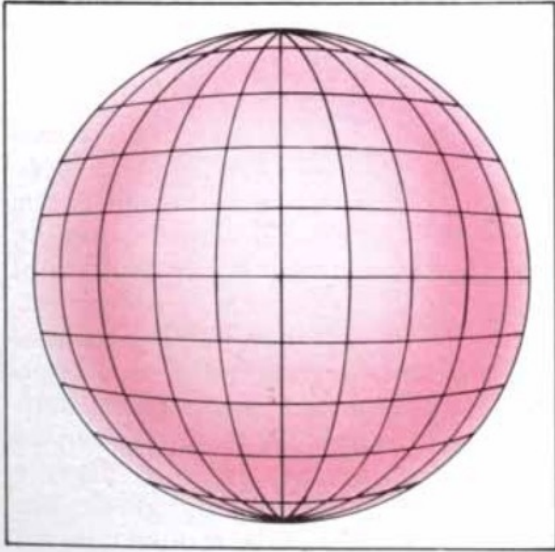
does this band-aid do the job?
and are there other options?

Does the band-aid do the job?

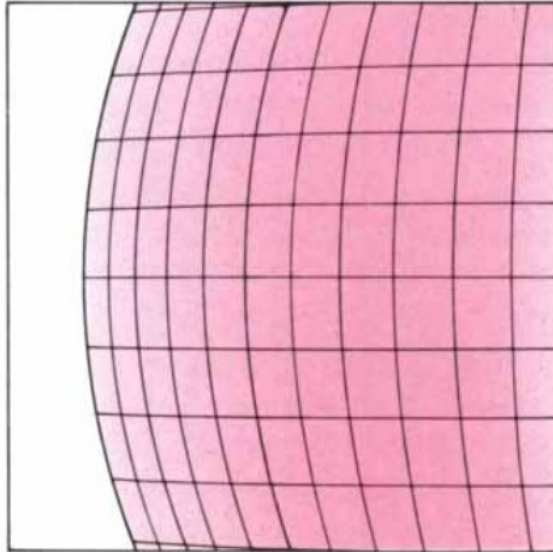
1. **“Entropy” Problem:** Inflation requires ultra-low entropy to start (but big bang produces ultra-high entropy)
2. **Initial “ $\dot{\phi}$ ” Problem:** Inflation requires ultra-low “ $\dot{\phi}$ ” (but “ $\dot{\phi}$ ” is ultra-high at the Planck density)
3. **Initial “ ϕ ” Problem:** Inflation requires “ ϕ ” to lie within a narrow, bounded range of the potential over a Hubble radius or more to start
4. **Singularity Problem:** Inflation does not avoid it
5. **Classical EofM Problem:** Inflation requires a transition from quantum- to classical-dominated evolution
6. **Multiverse Problem:** Quantum runaway \rightarrow eternal inflation \rightarrow multiverse \rightarrow no predictions
7. **Bunch-Davies Problem:** Smoothing not enough \rightarrow after smoothing need enough time to relax to B-D vacuum
8. **B-mode Problem:** Simplest textbook models predict B-modes \gg current limits
9. **Amplitude Problem:** Inflation does not predict the density fluctuation amplitude (it’s set by hand)
10. **Dark energy Problem:** Dark energy was not predicted and is not explained (plays no essential role)
11. **TCC Problem:** May not be embeddable in a consistent theory of quantum gravity
12. **Field range Problem:** Inflaton ranges over superPlanckian values resulting in loss of perturbative control

How to solve the Flatness Problem

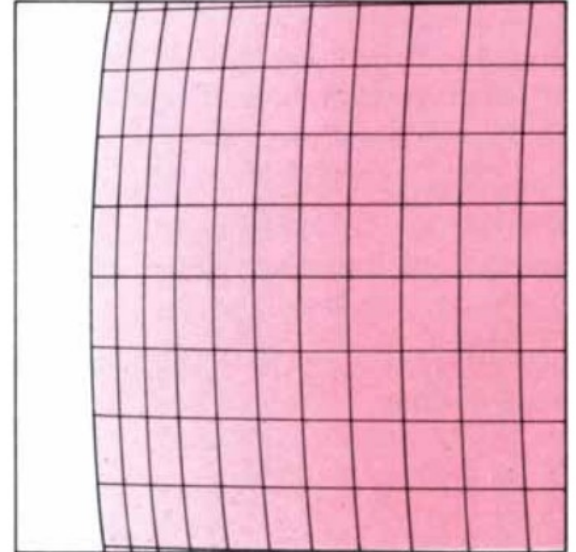
1



2



3



SOLUTION OF THE FLATNESS PROBLEM is illustrated by this sequence of perspective drawings of an inflating sphere.

The problem with this explanation is:

It's wrong...

... and it misleads you into believing that **expansion is essential to flatten** the universe ...

... when the truth is just the opposite!

Some Definitions:

$a(t)$ (the 'scale factor')

= the factor by which the universe has expanded or contracted

$H(t)$ (the 'Hubble parameter')

= the rate of expansion ($\equiv \dot{a}/a$)

ε (the 'equation of state')

= $\frac{3}{2} \left(1 + \frac{\textit{pressure}}{\textit{energy density}} \right)$ for the dominant form of energy

where $\varepsilon = 3/2$ corresponds to zero pressure

“Hubble radius”
~ how far you can see

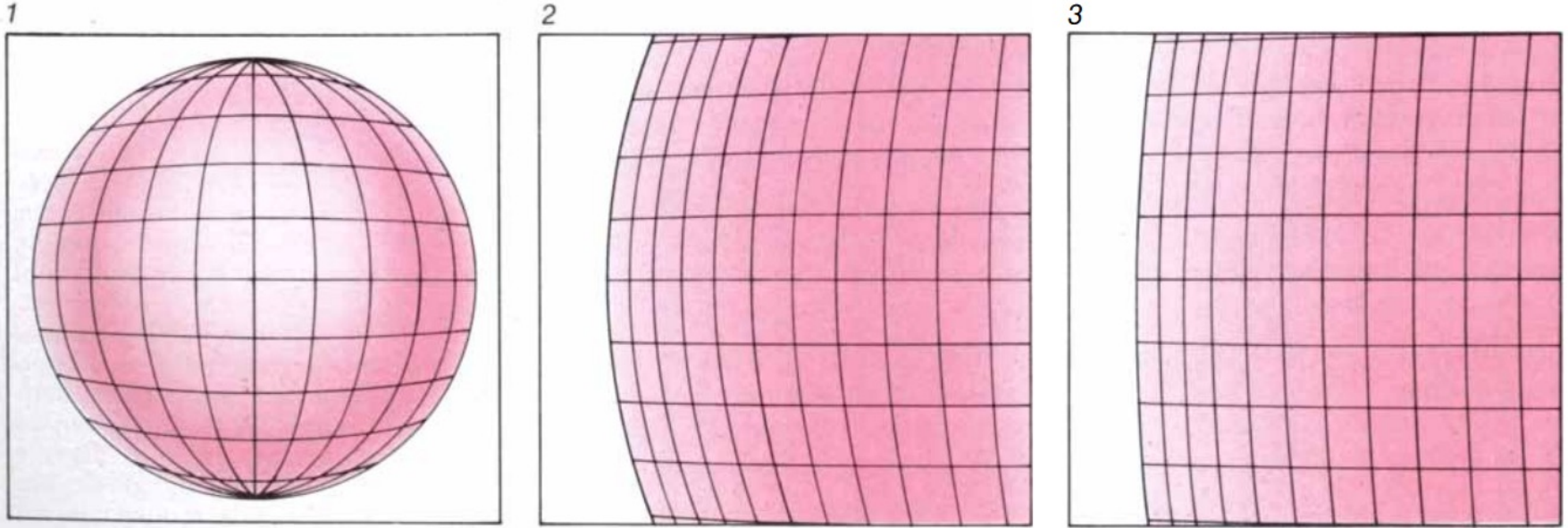
Pressure/energy density

$$\frac{c |H(t)|^{-1}}{c |H(t_0)|^{-1}} \sim \left(\frac{a(t)}{a(t_0)} \right)^\varepsilon$$

geometry

$$c |H|^{-1} \sim a^\varepsilon$$

How to solve the Flatness Problem

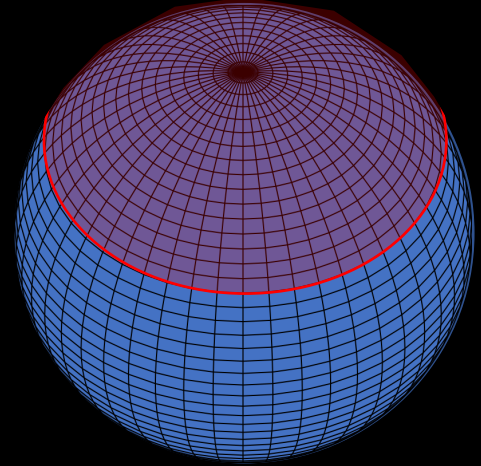
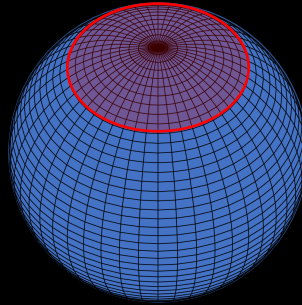
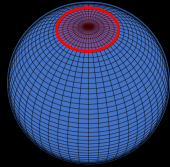


SOLUTION OF THE FLATNESS PROBLEM is illustrated by this sequence of perspective drawings of an inflating sphere.

$$c |H|^{-1} \sim a^\varepsilon$$

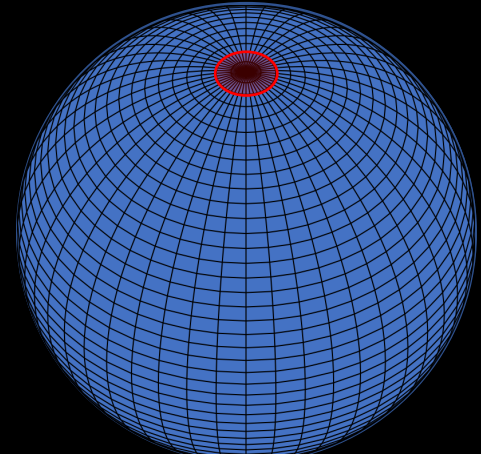
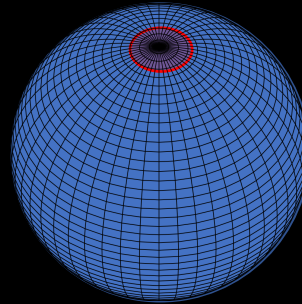
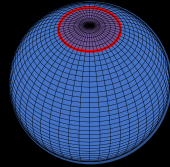
Cosmological Flatness = "Apparent Flatness"

expanding
 $\varepsilon > 1$



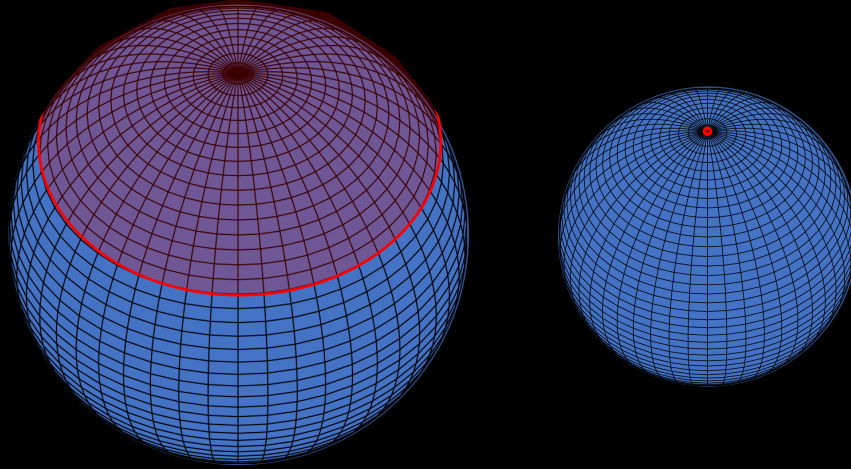
$$c |H|^{-1} \sim a^\varepsilon$$

inflating
 $\varepsilon < 1$



Cosmological Flatness = “Apparent Flatness”

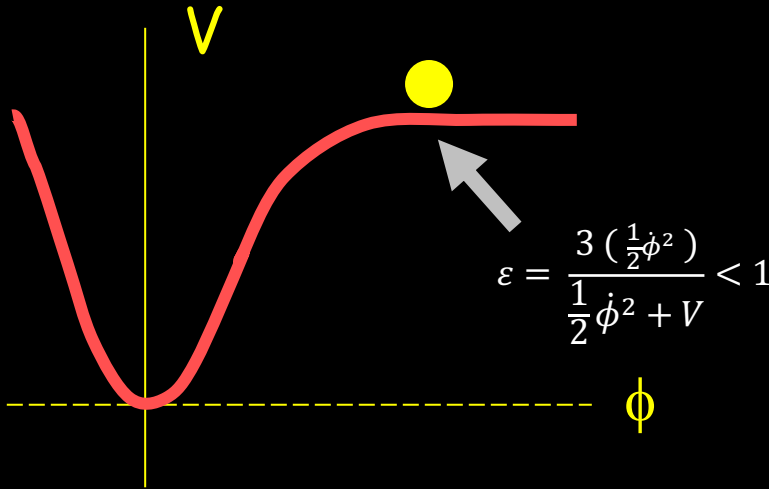
slow contraction
pressure $\gg 0$
 $\varepsilon \gg 1$



$$c |H|^{-1} \sim a^\varepsilon$$

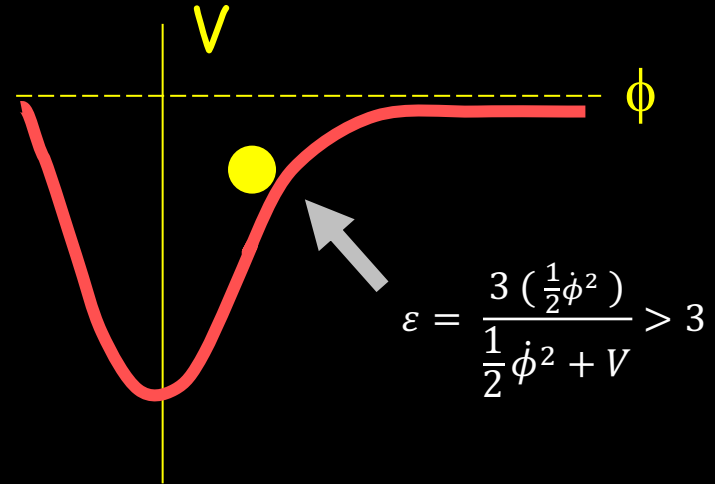
$$S = \int d^4 x \left[\frac{1}{2} R - \frac{1}{2} (\partial_\mu \phi)^2 - V(\phi) + \dots \right]$$

$$\ddot{\phi} + 3 H \dot{\phi} + V'(\phi) = 0$$



Inflation (accelerated expansion)

$$a(t) \sim |t|^{1/\varepsilon} \text{ as } t \rightarrow \infty$$

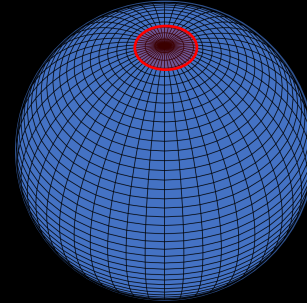
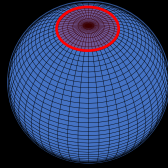


slow contraction ★

$$a(t) \sim |t|^{1/\varepsilon} \text{ as } t \rightarrow 0$$

slow contraction is much faster than inflation!

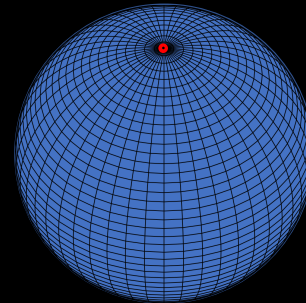
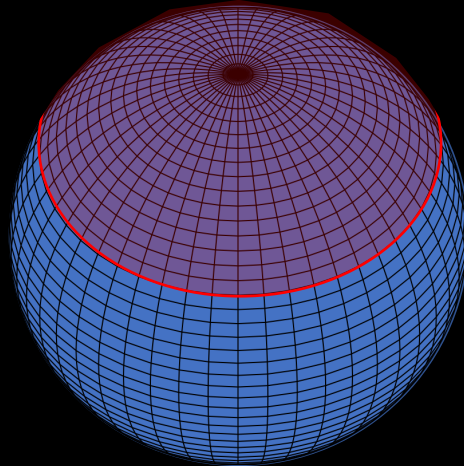
inflating
 $\epsilon < 1$



cap/surface area
reduced by 2^2

$$c |H|^{-1} \sim a^\epsilon$$

slow contraction
pressure $\gg 0$
 $\epsilon \gg 1$



cap/surface area
reduced by 2^{100}

How to solve the Homogeneity & Isotropy Problems

The problem with this explanation is . . .

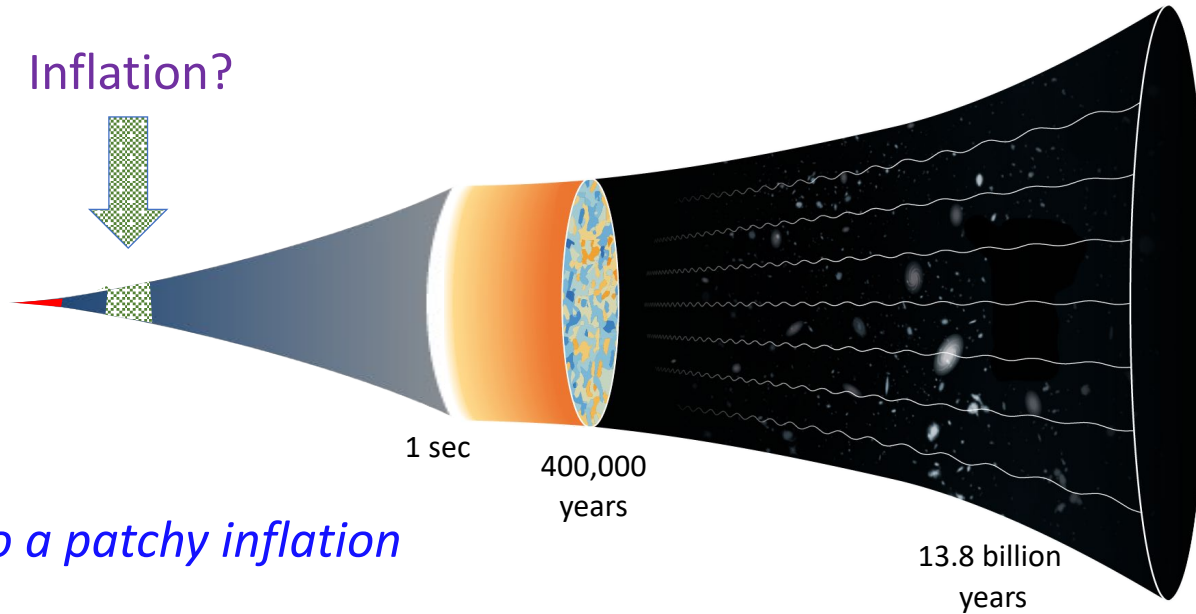
It's wrong. . .

. . . and it misleads you into believing that **expansion is essential to smooth** the universe . . .

. . . when the truth is just the opposite!

How to solve the Smoothness Problem

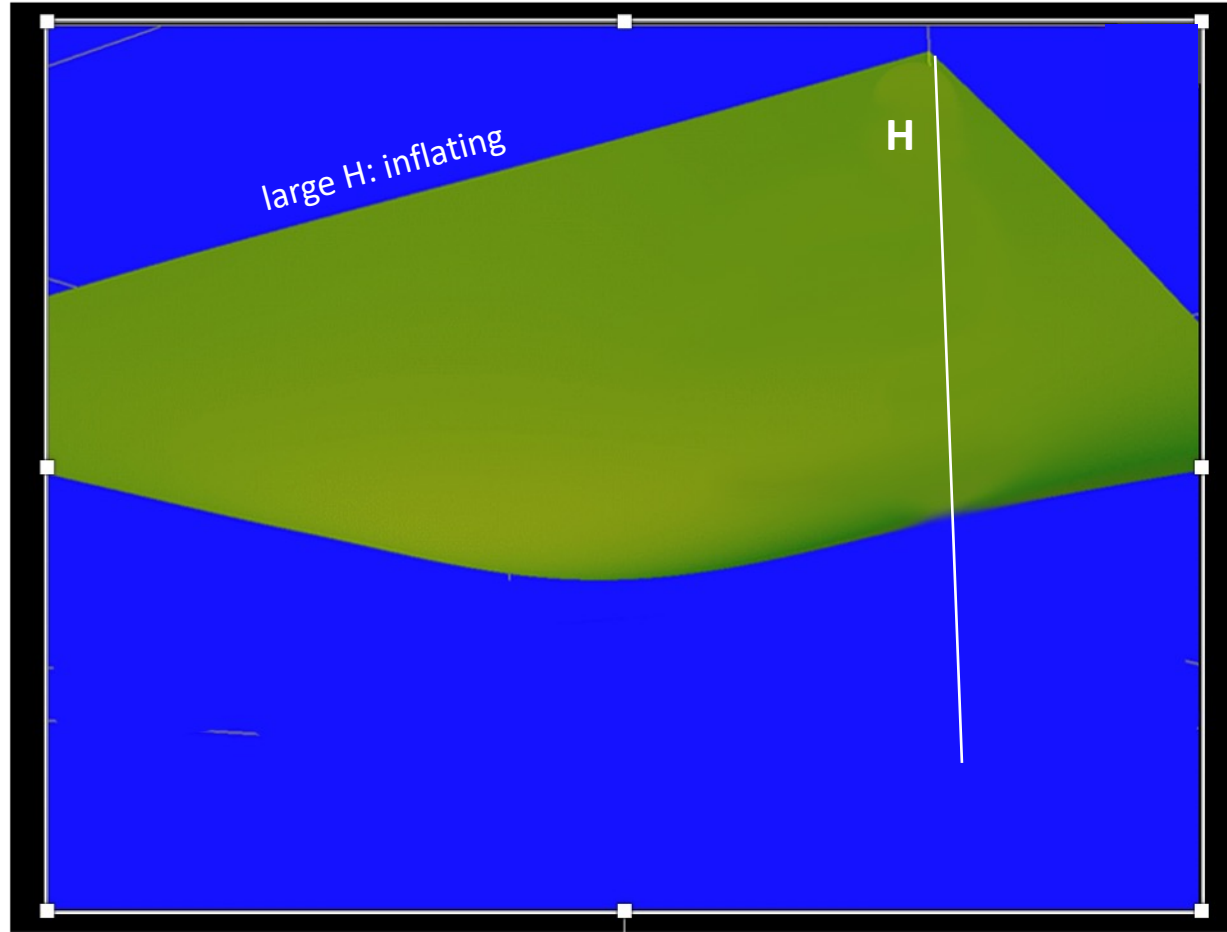
Inflation requires a nearly smooth spacetime to get started



Which leads to a patchy inflation

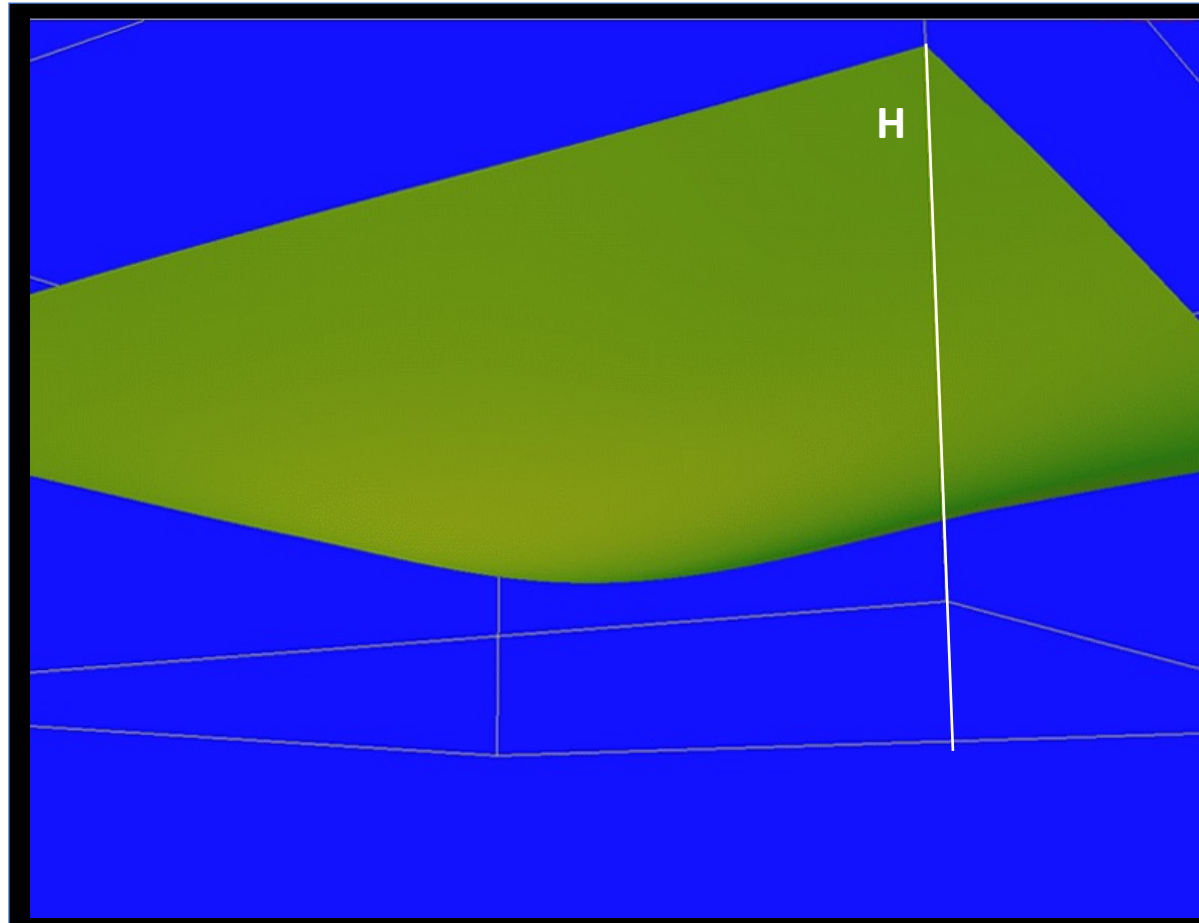
where “bad inflation is more likely than good inflation”

"QUANTUM PHYSICS" ADDED



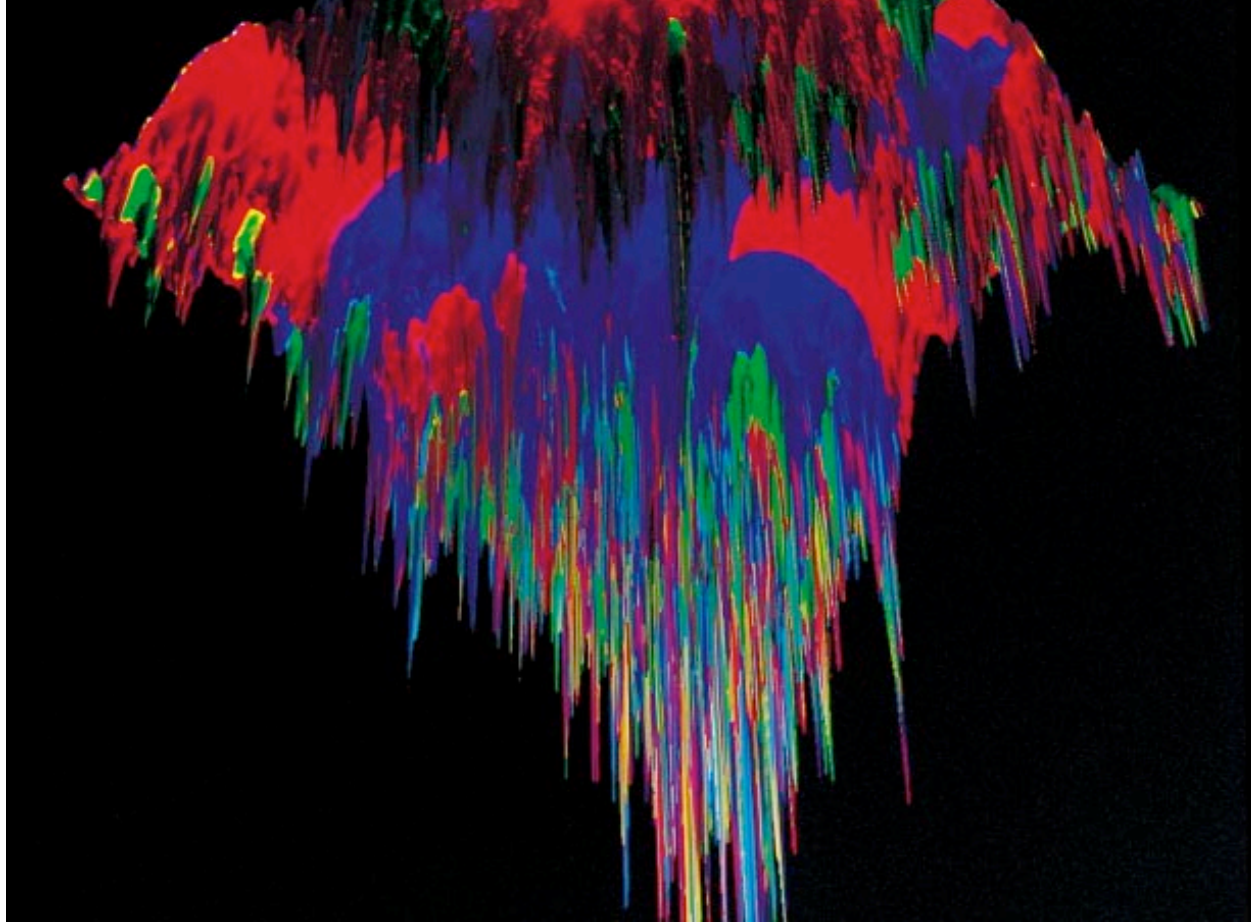
a simple
litmus test

“QUANTUM PHYSICS” ADDED



quantum
runaway!

“QUANTUM PHYSICS” VIEW



smoothness
flatness
are not
the generic
outcome

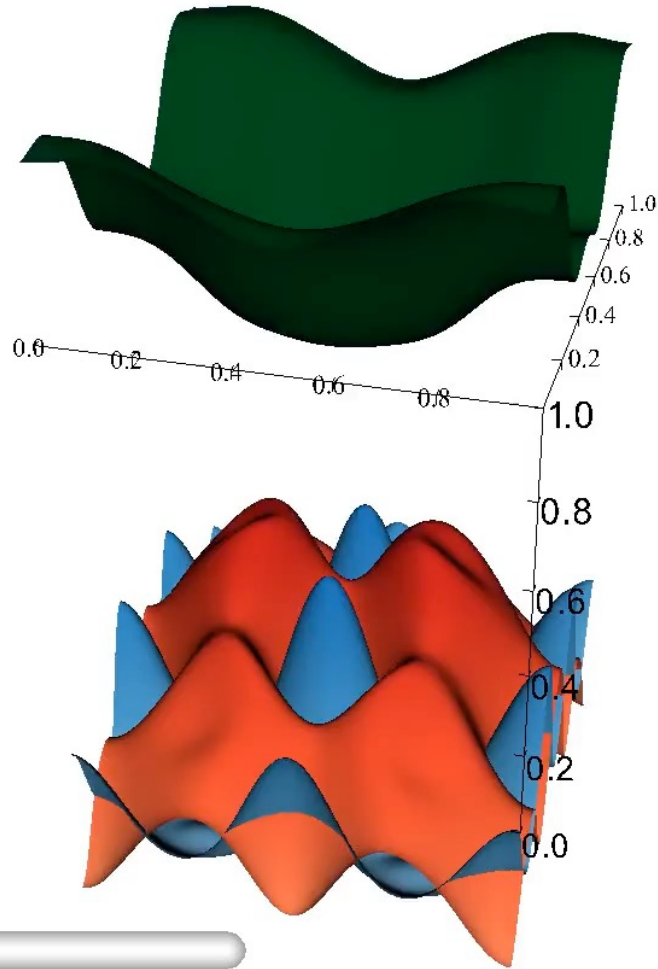
Anna Ijjas,

Numerical Relativity as a New Tool
for Fundamental Cosmology,
Physics 4, 301 (2022)

Ω_ϕ

Ω_k

Ω_s

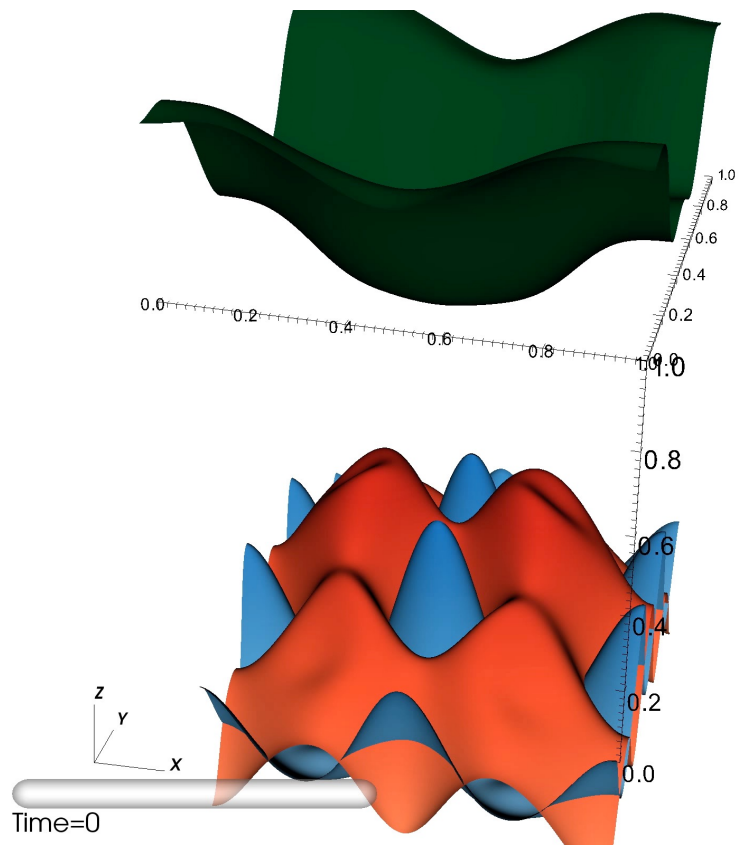


Time=0

what about
smoothing by
slow contraction

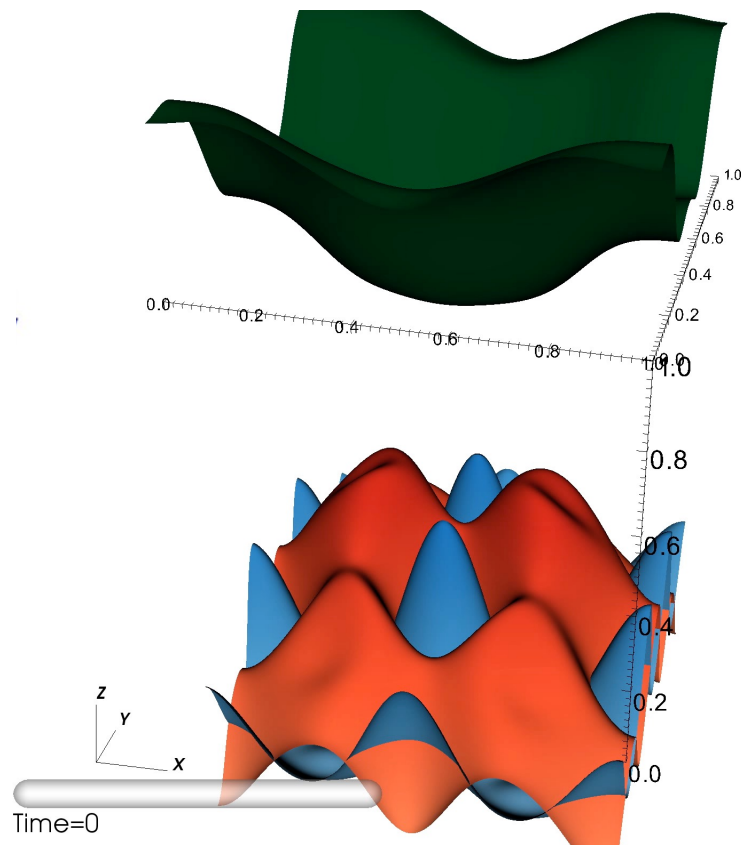
begins far
from
slow contraction
conditions

fast contraction ($\varepsilon < 3$)



Ω_ϕ
 Ω_k
 Ω_s

slow contraction ($\varepsilon > 3$)



universal smoother !!

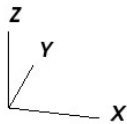
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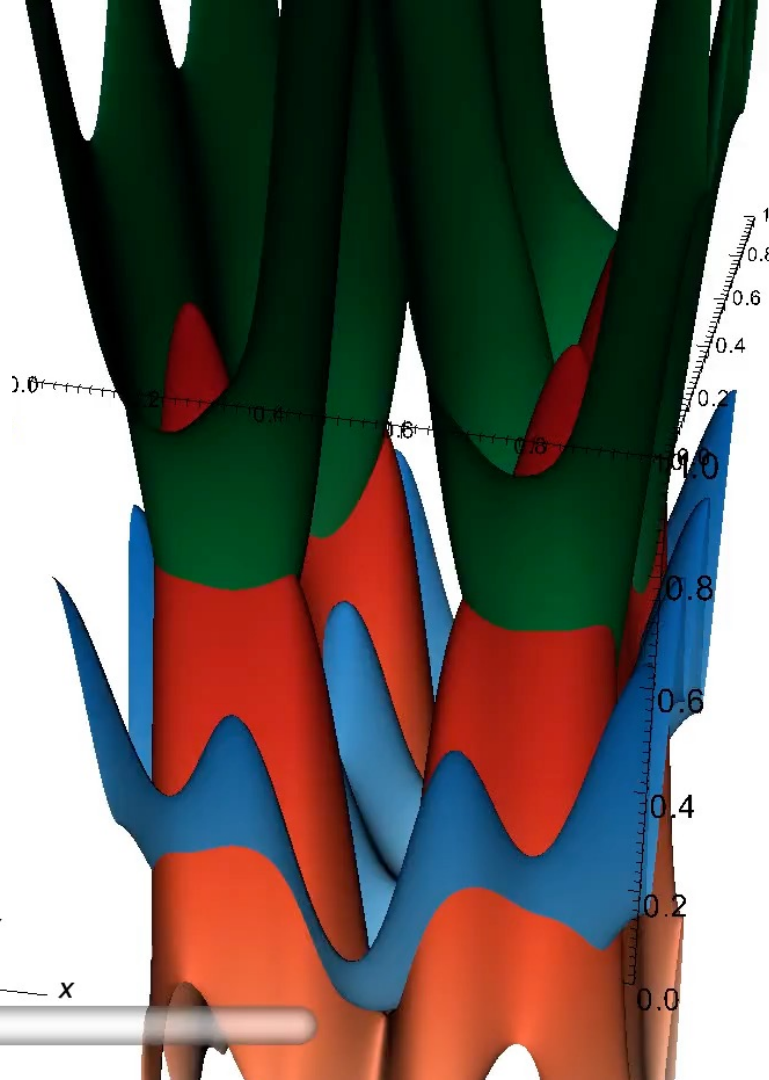
Ω_ϕ

Ω_k

Ω_s



Time=0

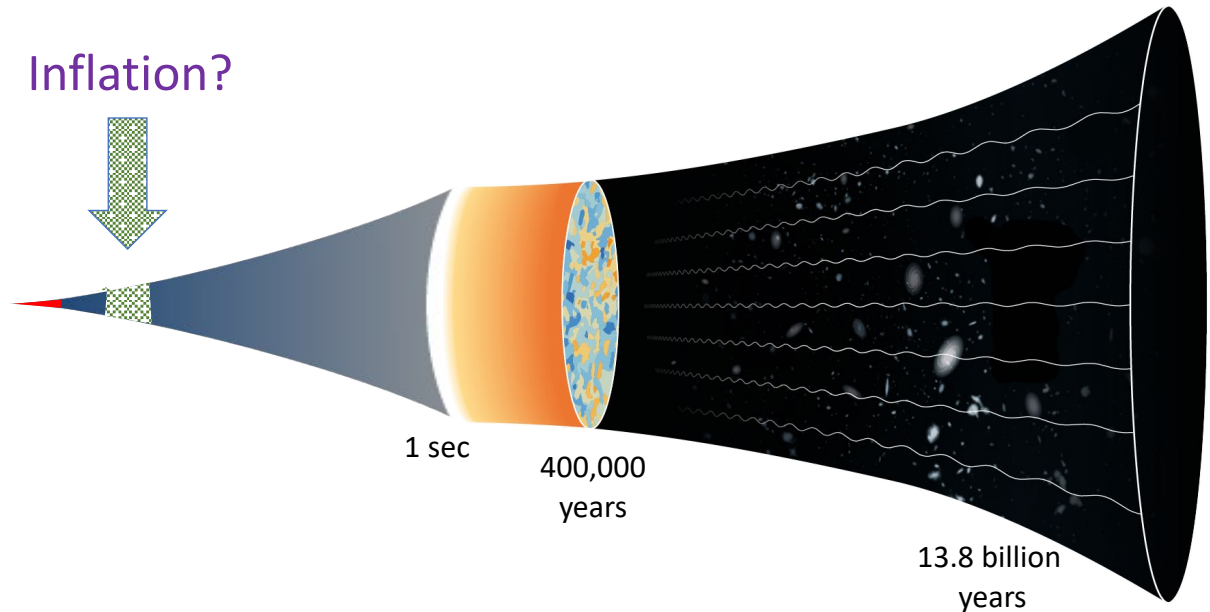


What about
smoothing by
slow contraction

begins far
from
slow contraction
conditions

How to solve the Big Bang “Entropy” Problem

any theory with a big bang/quantum gravity-dominated phase is susceptible to having an “entropy” problem



A universe that begins with a bang and expands forever...

... has an entropy problem

(and inflation cannot resolve it)

... has a smoothness problem

(and inflation cannot resolve it)

... has a flatness problem

(and inflation cannot resolve it)

Quo vadis Cosmology?

A universe with a bounce can avoid all of these problems

slow contraction

robustly and rapidly resolves
smoothness & flatness probs
w/no multiverse

"reheating"

explains
strange partition
of entropy

big bang

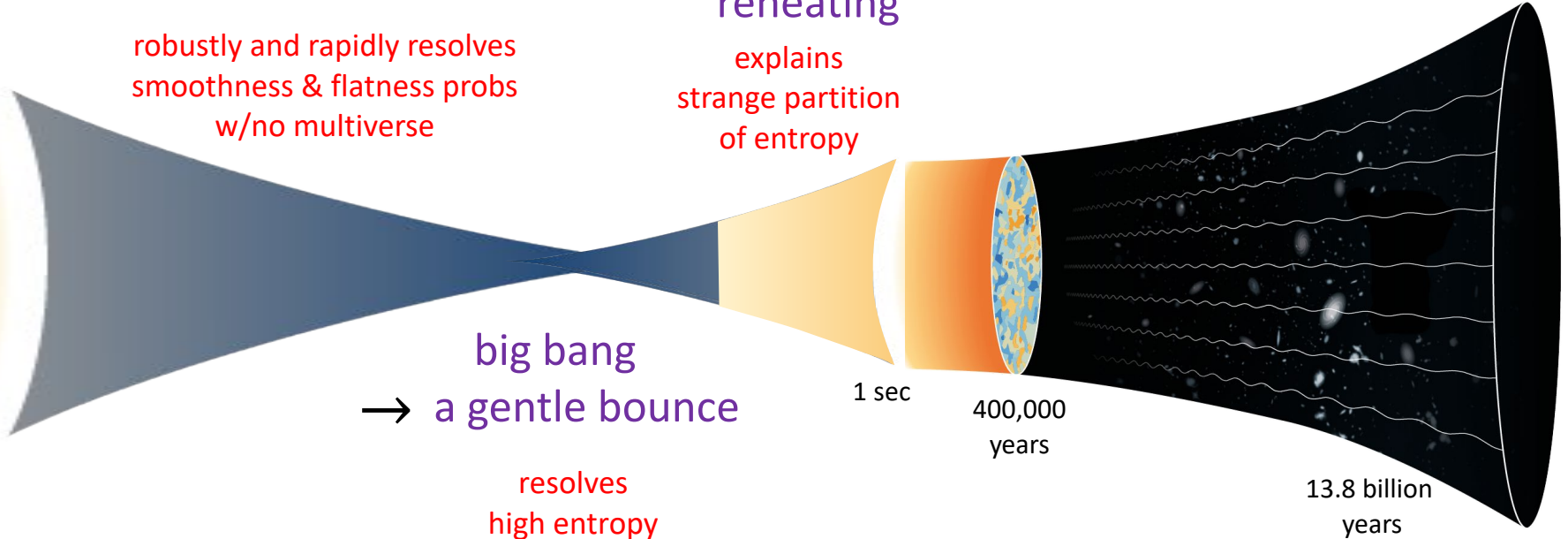
→ a gentle bounce

resolves
high entropy
w/no quantum->classical
transition

1 sec

400,000
years

13.8 billion
years



OBSERVATIONS

- homogeneity
- flatness
- entropy
- no detectable B-mode polarization
- dark energy is time-varying
- acceleration era will come to an end

The Atacama Desert: Site of the forthcoming Simons Observatory