# $H+j$ production at NLO QCD 

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## , <br> 11III The Niels Bohr 111011 International Academy CARISBERG FOUNDATION

## Introductions

## Theoretical Particle Physics and Cosmology at NBI

## Gravity

Gravitational waves
Black holes
Limits of gravity
Holography/Quantum gravity


Astroparticle and Cosmology
Neutrino physics Icecube observatory Transient events High-energy astrophysics Astrophysical jets


Cosmic microwave background Primordial gravitational waves


Particle Physics and Condensed-matter Modern methods of amplitudes Particle physics phenomenology Defect conformal field theory Strongly coupled matter Holographic principle Thermalization Integrability


## Introductions

## High-energy theory and phenomenology at NBI

## Oleg Ruchayskiy, Inar Timiryasov,Kevin Urquía <br> Blegdamsvej 17, building M

-The group is working on physics beyond the Standard Model with feebly interacting particles
-Theoretical developments (what are they good for) and experimental searches (how to find them at CERN and beyond)


## Introductions

## Theoretical Particle Physics and Cosmology at NBI

Permanent members:<br>Poul Henrik Damgaard (NBIA director)<br>Irene Tamborra<br>Niels A. Obers<br>Charlotte F. Kristjansen<br>Vitor Cardoso (new!)<br>Pavel Naselsky<br>Konstantin Zarembo<br>Troels Harmark<br>Emil Bjerrum-Bohr<br>Markus Ahlers (tenure track)

Longterm non-permanent:
Michael Trott
Matthias Wilhelm
Jacob Bourjaily
Mauricio Bustamante
Andrés Luna Godoy
Christian Vergu
Matt von Hippel

Postdocs: 10
PHD students: 10
MSC students: 15-20
Emeritus professors: 9

Higgs plus jet production at the LHC.

Leading order QCD is one-loop


NLO/two-loop is not yet completely known with full mass dependence...

## Introduction

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## NLO/two-loop is not yet completely known with full mass dependence...

Three processes in one:

$$
\begin{array}{ll}
p p \rightarrow H j & \text { is important in its own right } \\
H \rightarrow 3 j & \text { Higgs decay } \\
p p \rightarrow H & \text { Real radiation at next order }
\end{array}
$$

## Previous work on NLO QCD $H+j$ production

| Exact LO results: | R. K. Ellis, I. Hinchliffe, M. Soldate, JJ van der Bij. (1988) <br> U. Baur and E. W. N. Glover. (1990) |
| :---: | :---: |
| HEFT results: | R. Boughezal, F. Caola, K. Melnikov, F. Petriello, M. Schulze. (2013) arXiv:1302.6216 <br> X. Chen, T. Gehrmann, E. W. N. Glover, M. Jaquier. (2015) arXiv:1408.5325 <br> R. Boughezal, F. Caola, K. Melnikov, F. Petriello, M. Schulze. (2015) arXiv:1504.07922 <br> R. Boughezal, C. Focke, W. Giele, X. Liu, F. Petriello. (2015) arXiv:1505.03893 |
| Various other limits and expansions: | R. Harlander, T. Neumann, K. Ozeren, M. Wiesemann. (2012) arXiv:1206.0157 <br> T. Neumann and M. Wiesemann. (2014) arXiv:1408.6836 <br> T. Neumann and C. Williams. (2017) arXiv:1609.00367 <br> R. Mueller and D. Öztürk. (2016) arXiv:1512.08570 <br> K. Melnikov, L. Tancredi, C. Wever. (2016) arXiv:1610.03747 <br> K. Melnikov, L. Tancredi, C. Wever. (2017) arXiv:1702.00426 <br> J. Lindert, K. Melnikov, L. Tancredi, C. Wever. (2017) arXiv:1703.03886 <br> K. Kudashkin, K. Melnikov, C. Wever. (2017) arXiv:1712.06549 <br> J. Lindert, K. Kudashkin, K. Melnikov, C. Wever. (2018) arXiv:1801.08226 |
| Numerical results: | S. Jones, M. Kerner, G. Luisoni. (2018) arXiv:1802.00349 <br> M. Czakon, R. Harlander, J. Klappert, M. Niggetiedt. (2021) arXiv:2105.04436 |
| Feynman integrals: | R. Bonciani, V. Del Duca, HF, J. Henn, F. Moriello, V. Smirnov. (2016) arXiv:1609.06685 <br> R. Bonciani, V. Del Duca, HF, J. Henn, et. al. (2020) arXiv:1907.13156 <br> HF, M. Hidding, L. Maestri, F. Moriello, G. Salvatori. (2020) arXiv:1911.06308 |

## Integrals

The biggest challenge is the evaluation of the Feynman Integrals. $\mathcal{O}\left(10^{5}\right)$ integrals $\rightarrow \mathcal{O}\left(10^{2}\right)$ "master integrals" (independent basis) The integrals must be sorted into "integral families"

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I_{a_{1}, \ldots, a_{9}}^{f}=\iint \frac{\mathrm{d}^{d} k_{1}}{i \pi^{d / 2}} \frac{\mathrm{~d}^{d} k_{2}}{i \pi^{d / 2}} \frac{P_{f, 8}^{-a_{8}} P_{f, 9}^{-a_{9}}}{P_{f, 1}^{a_{1}} P_{f, 2}^{a_{2}} P_{f, 3}^{a_{3}} P_{f, 4}^{a_{4}} P_{f, 5}^{a_{5}} P_{f, 6}^{a_{6}} P_{f, 7}^{a_{7}}}
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There are eight such integral families:




Integrals


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Bonciani, Del Duca, HF, Henn, Moriello, Smirnov JHEP, vol. 12(2016), p. 096 [arXiv:1609.06685]


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JHEP, vol. 06(2020), p. 093 [arXiv:1911.06308]

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Three different "complexity classes":

1) Result given in terms of polylogarithms such as $\operatorname{Li}_{n}(x)=\int_{0}^{x} \frac{\mathrm{~d} y}{y} \mathrm{Li}_{n-1}(y)$.
2) Result looks polylogarithmic but no closed expression can be found.
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All cases present in family A


## Results

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What we actually do, is solve the diff-eqs numerically.
We use the Frobenius method: sequential series expansions near critical points Moriello [2020], Hidding [2020]
This can be done to arbitrary precision, also close to branch points.

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Plots for the final NLO cross section will be published this year!

## Perspectives

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Main project: Intersection Theory and Feynman Integrals

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\left.J_{i}=\int_{\mathcal{C}} u \phi_{i}=\left\langle\phi_{i}\right| \mathcal{C}\right] \quad I=\sum_{i} c_{i} J_{i} \Leftrightarrow c_{i}=\left\langle\phi_{I} \mid \phi_{i}\right\rangle
$$

$\left\langle\phi_{I} \mid \phi_{i}\right\rangle$ is the intersection number - a pairing between differential forms
We can extract the coefficients with a direct projection!
Mastrolia, Mizera [2019]; HF, Gasparotto, Laporta, Mandal, Mastrolia, Mattiazzi, Mizera [2019,19,21]

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Thank you for inviting me, and thank you for listening!

