

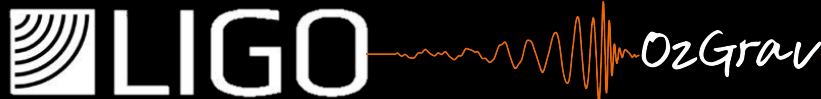
ALL BINARY BLACK HOLES MAY FORM DYNAMICALLY: THE ECCENTRIC PERSPECTIVE



Isobel Romero-Shaw

Paul Lasky
Eric Thrane

NBIA Workshop on Black Hole Dynamics
31.05.22

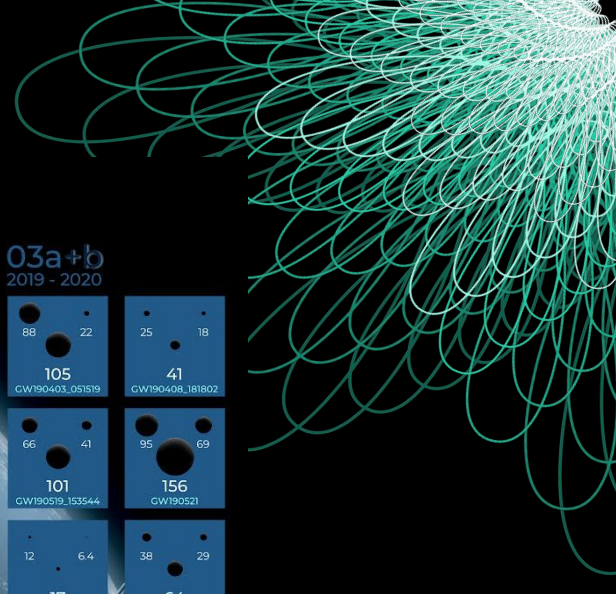


OzGrav



MONASH
University

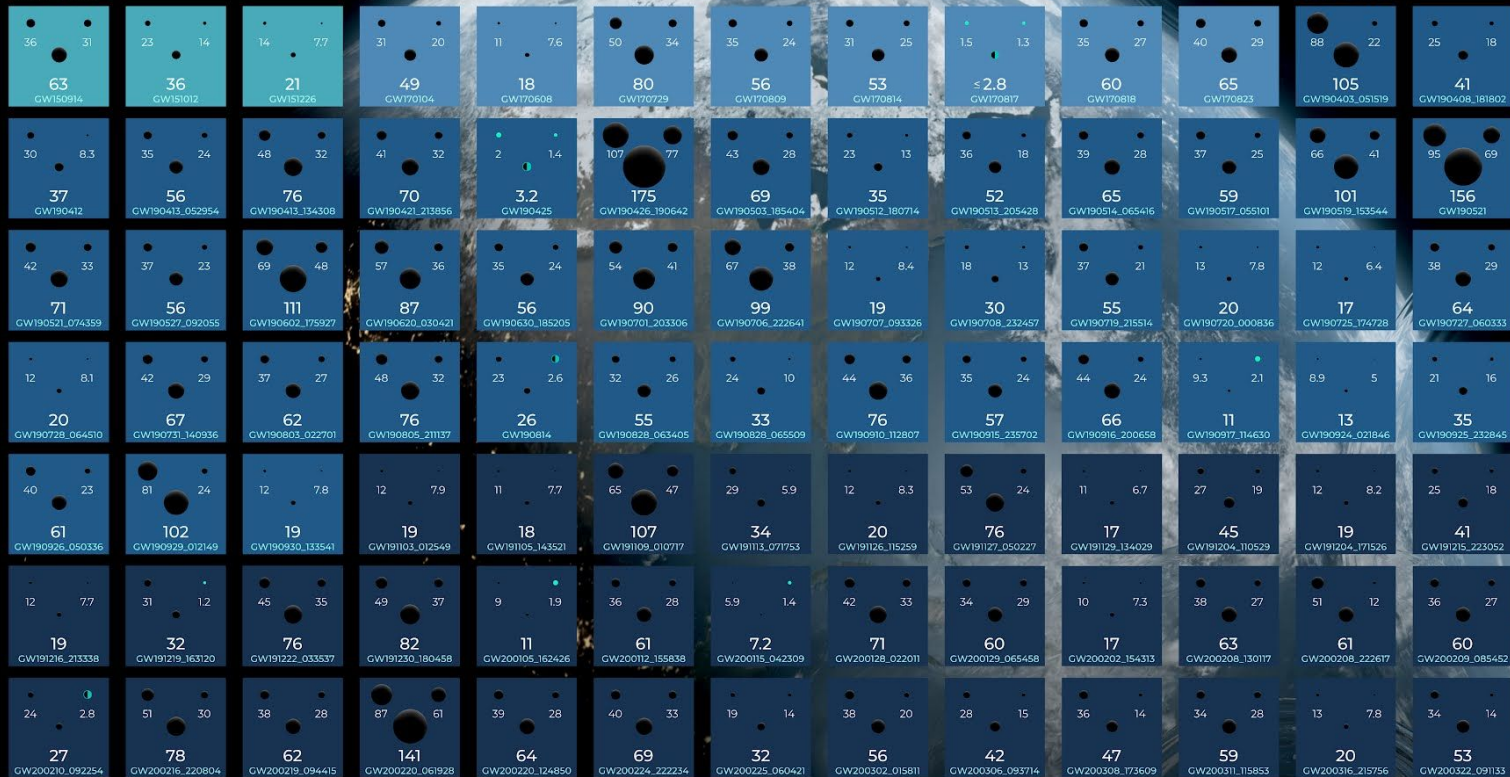
GRAVITATIONAL WAVES DETECTED: 2015-2020



OBSERVING RUN 01
2015 - 2016

02
2016 - 2017

03a+b
2019 - 2020



KEY

- BLACK HOLE
- NEUTRON STAR (SHOWN AT THE SCALE) & UNCERTAIN OBJECT
- PRIMARY MASS
- SECONDARY MASS
- FINAL MASS
- DATE [TIME]

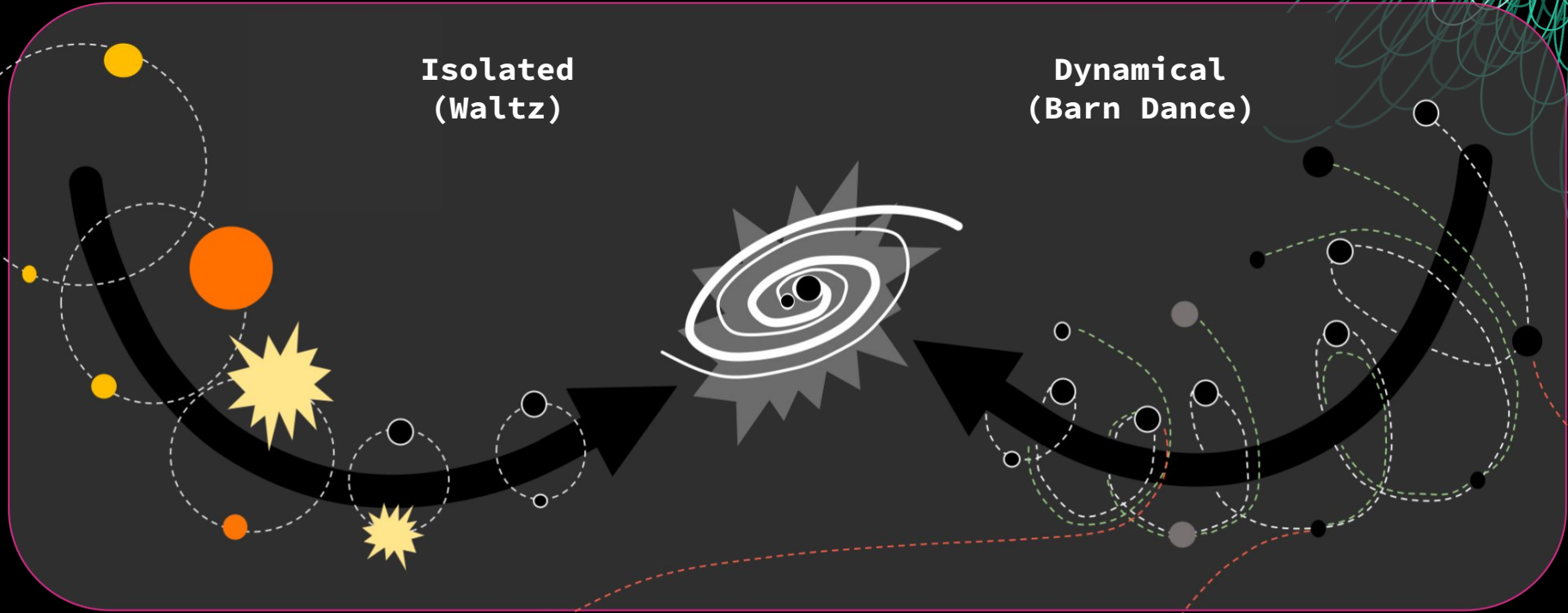
UNITS ARE SOLAR MASSES.
1 SOLAR MASS = 1.989 x 10³⁰ kg



FORMATION CHANNELS

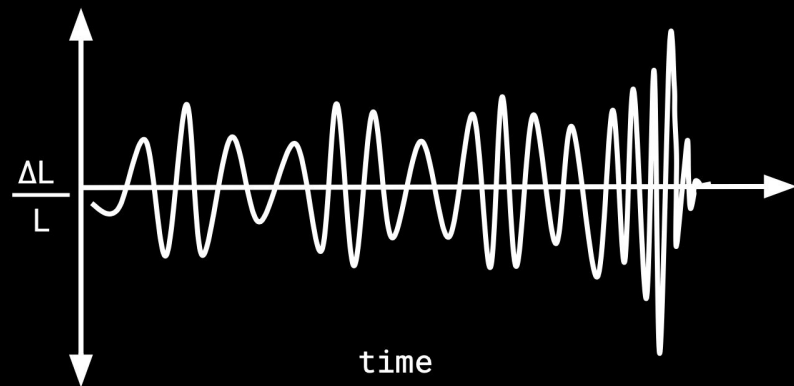
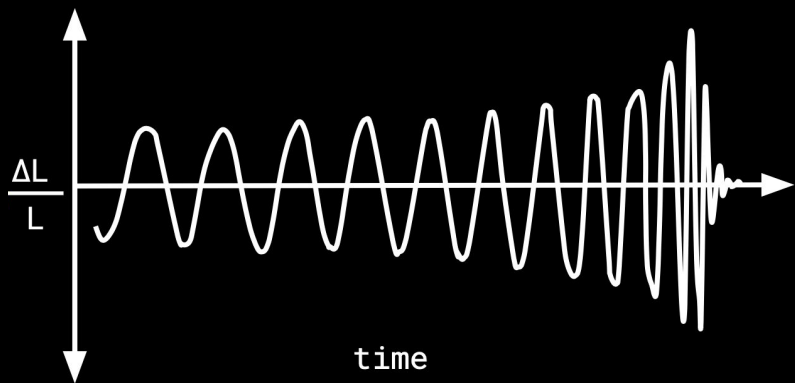
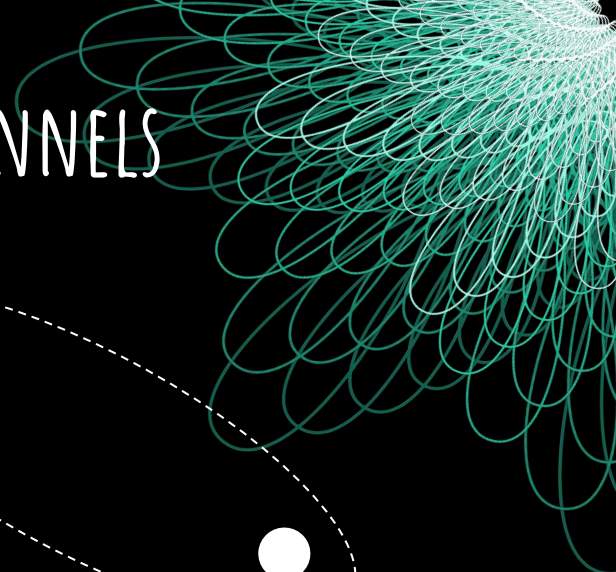
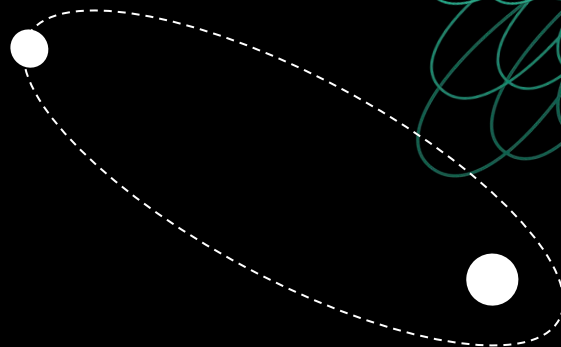
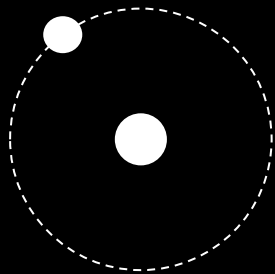
**Isolated
(Waltz)**

**Dynamical
(Barn Dance)**



DISTINGUISHING FEATURES OF FORMATION CHANNELS

- Mass, Spin, **Eccentricity**

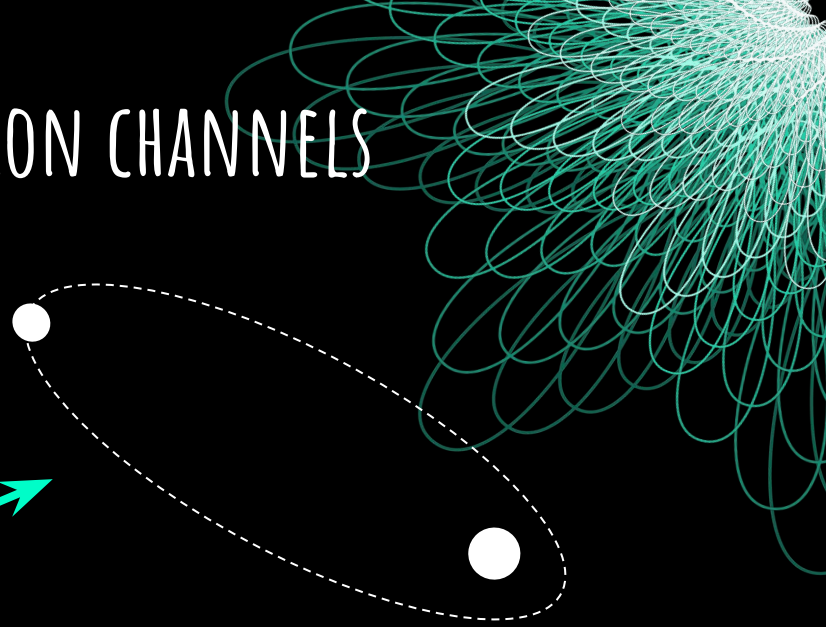
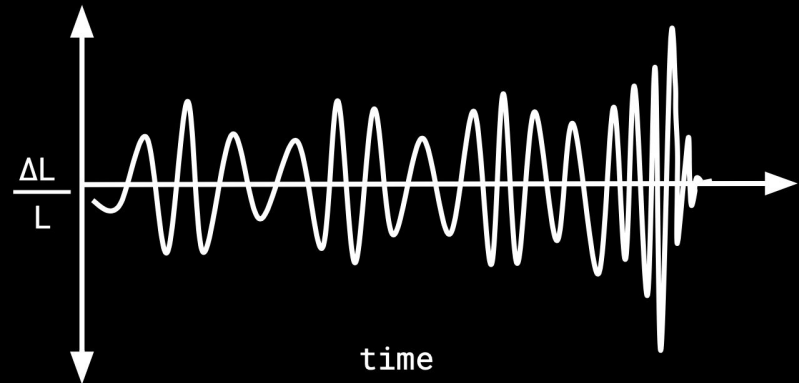
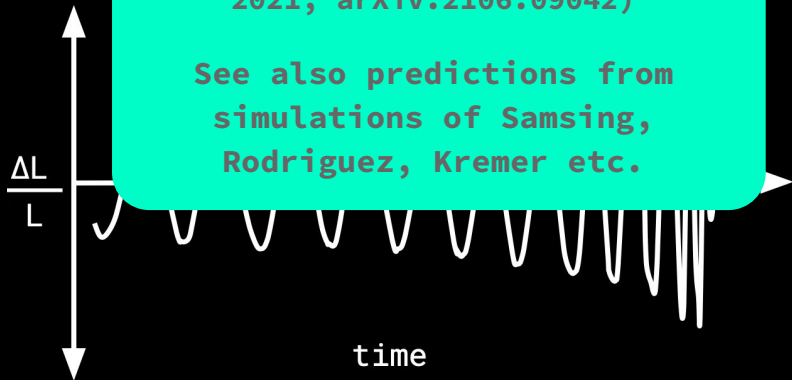


DISTINGUISHING FEATURES OF FORMATION CHANNELS

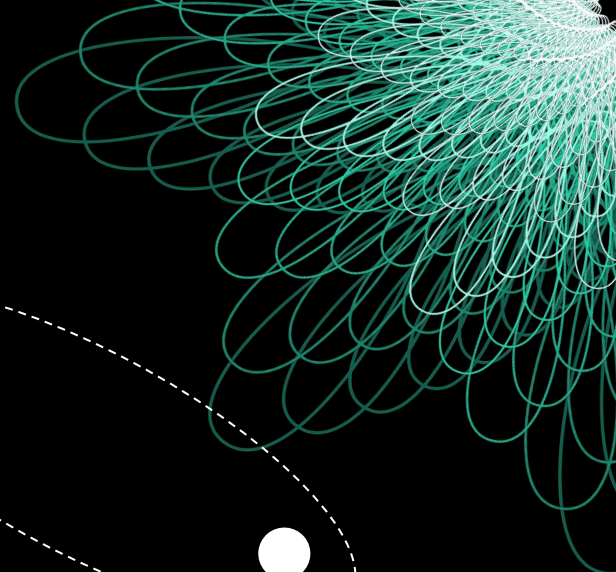
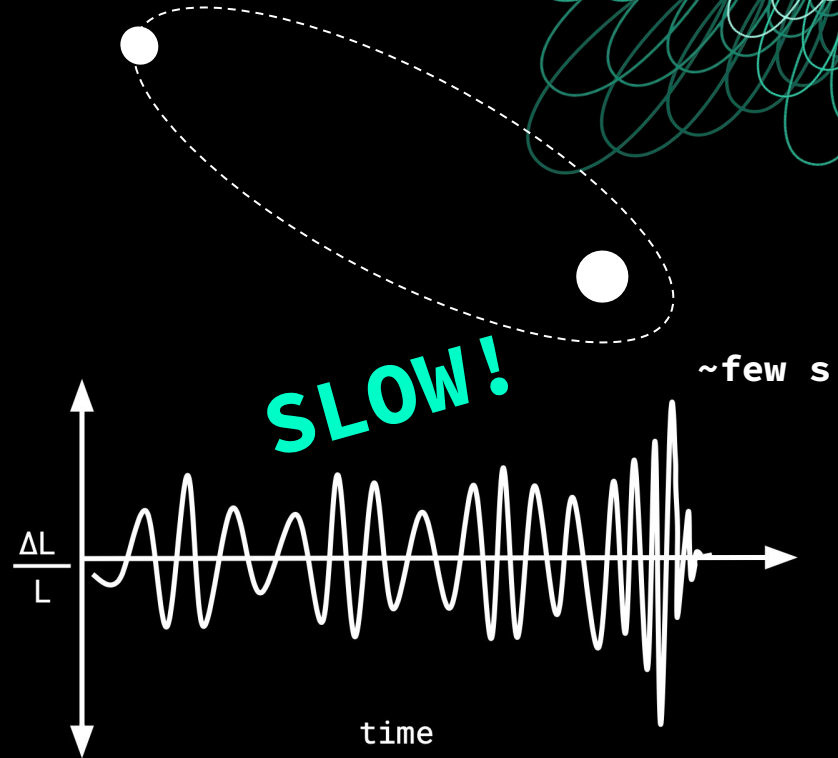
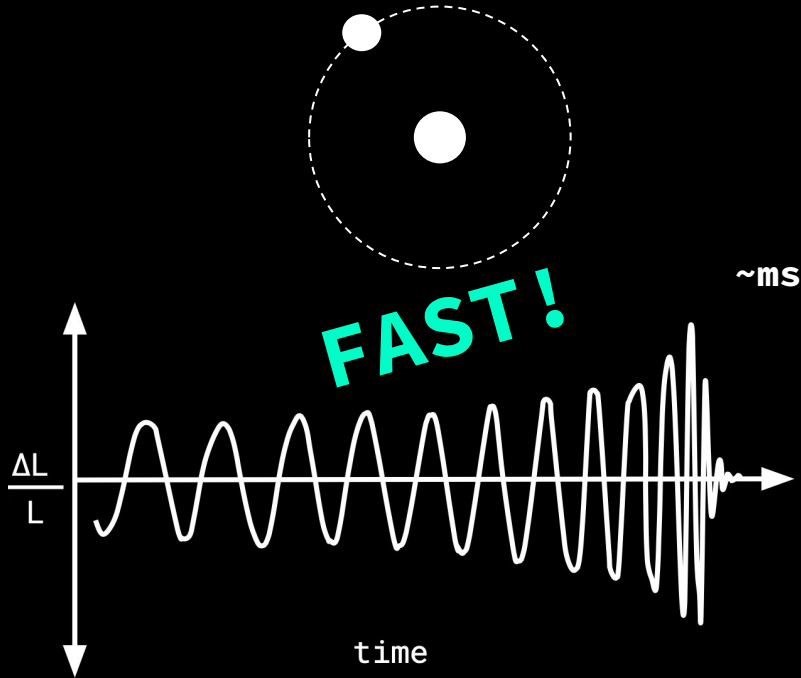
- Mass, Spin, **Eccentricity**

Expect ~4% of mergers from GCs to be observed with eccentricity > 0.05 at 10 Hz (Zevin, RS, Kremer, Thrane & Lasky 2021, arXiv:2106.09042)

See also predictions from simulations of Samsing, Rodriguez, Kremer etc.



PROBLEM: ECCENTRIC WAVEFORMS ARE SLOW



POSSIBLE SOLUTIONS

- **Likelihood reweighting**

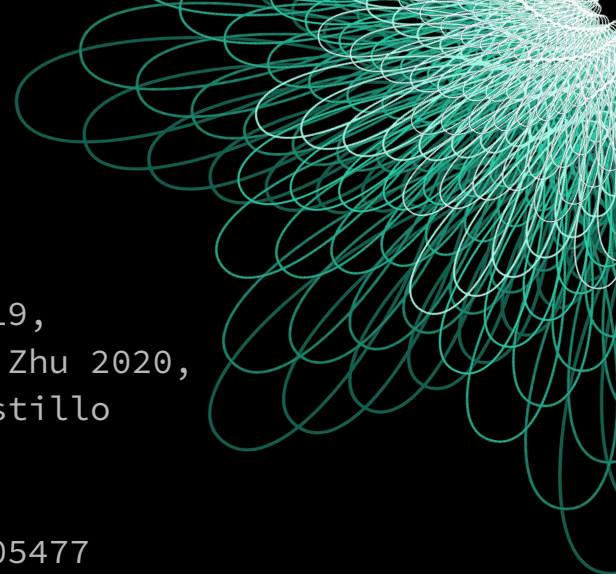
- **SEOBNRE**; as demonstrated by RS, Lasky & Thrane 2019, arXiv:1909.05466, RS, Farrow, Stevenson, Thrane & Zhu 2020, arXiv:2001.06492, RS, Lasky, Thrane & Calderon Bustillo 2020, arXiv:2009.04771, RS, Lasky & Thrane 2021, arXiv:2108.01284
- See also Payne, Talbot & Thrane 2019, arXiv:1905.05477

- **Use faster inspiral-only waveform**

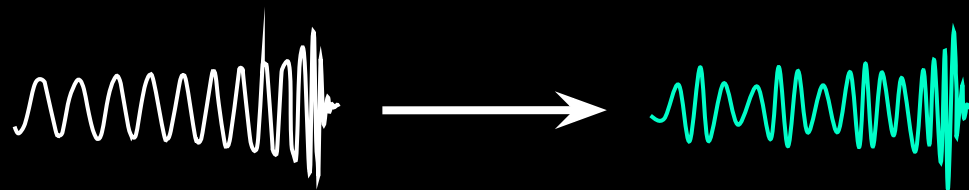
- **TaylorF2Ecc**; as demonstrated by Lower, Lasky & Thrane 2019, arXiv:1806.05350; Lenon et al. 2020, arXiv:2005.14146

- **Adjust error threshold of ODE solver within code**

- **TEOBResumSe**; as demonstrated by O'Shea & Kumar 2021, arXiv:2107.07981

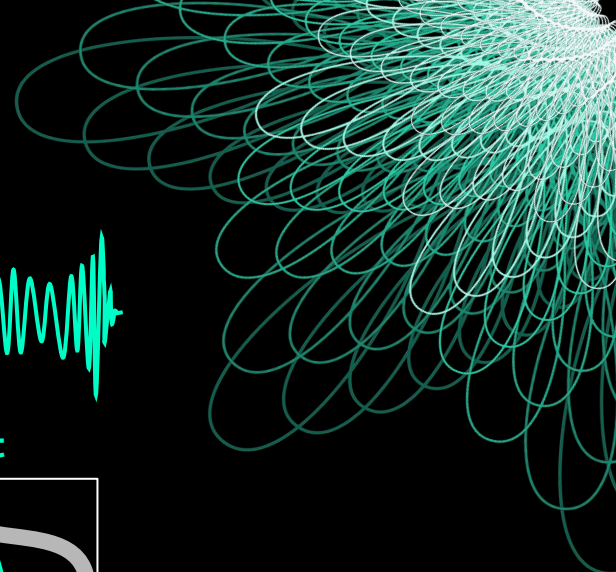
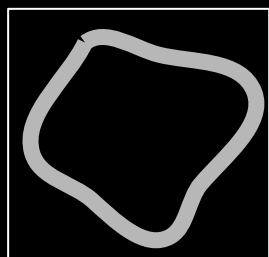


SOLUTION: LIKELIHOOD REWEIGHTING



Proposal

Target



marginalised over eccentricity



$$P(\theta|d) = \frac{L(d|\theta) \pi(\theta)}{Z(d)} \longrightarrow P(\theta|d)_e = \frac{L(d|\theta)_e}{L(d|\theta)} P(\theta|d)$$

then reconstruct eccentricity distribution from marginal 1D likelihood (ask me for the bonus slide!)

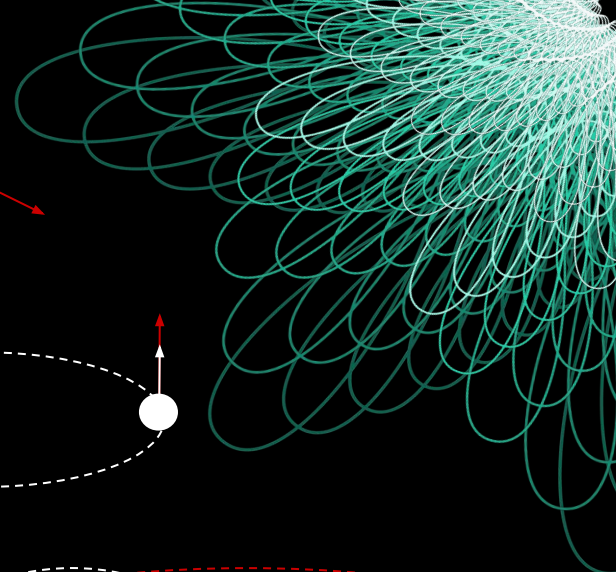
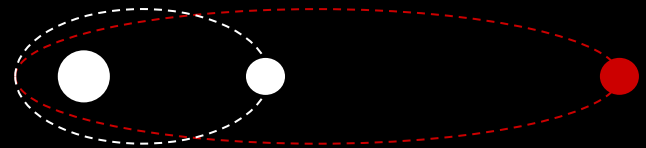
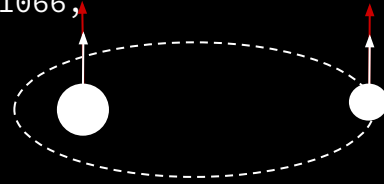
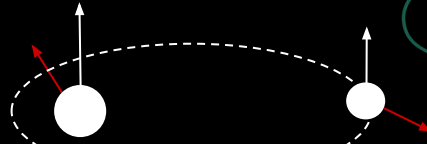
Ashton et al. 2019,
arXiv:1811.02042

RS et al. 2020c,
arXiv:2006.00714



CAVEATS

- **Spin-precession or eccentricity?**
 - Can be confused for each other
 - See Calderón-Bustillo et al. 2020, arXiv:2009:01066, Romero-Shaw et al. 2020b, arXiv:2009.04771
- **Aligned spin magnitude capped at 0.6**
- **Eccentricity magnitude capped at 0.2 (10 Hz)**
- **Initial argument of periapsis is fixed**
 - Don't think this affects results significantly - see Teagan Clarke's upcoming work
- **“Eccentricity” has no consistent definition between simulations / models**
 - Measurements not directly comparable to model predictions / measurements using other models
 - See Alan Knee's upcoming work



BLIND SPOTS

- **We neglect events that may contain neutron stars**
 - Leaves us with 82 **confident** BBH
- **We neglect events that wind up undersampled**
 - Leaves us with 62 **well-sampled** confident BBH

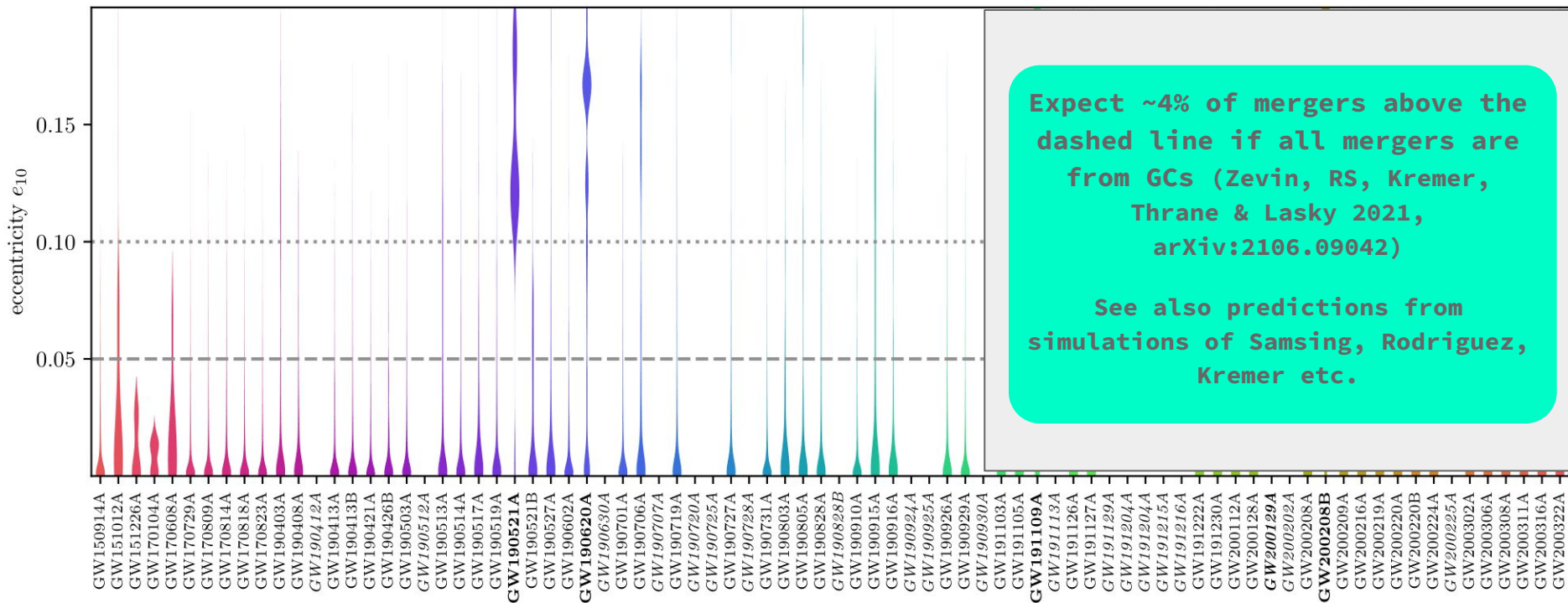
$$w_i = \frac{L(d|\theta_i)e}{L(d|\theta_i)}$$

$$n_{\text{eff}} = \frac{\text{sum}(w_i) ** 2}{\text{sum}(w_i ** 2)}$$

WARNING: Next slide has white background!

RESULTS: GWTC-1 AND GWTC-2

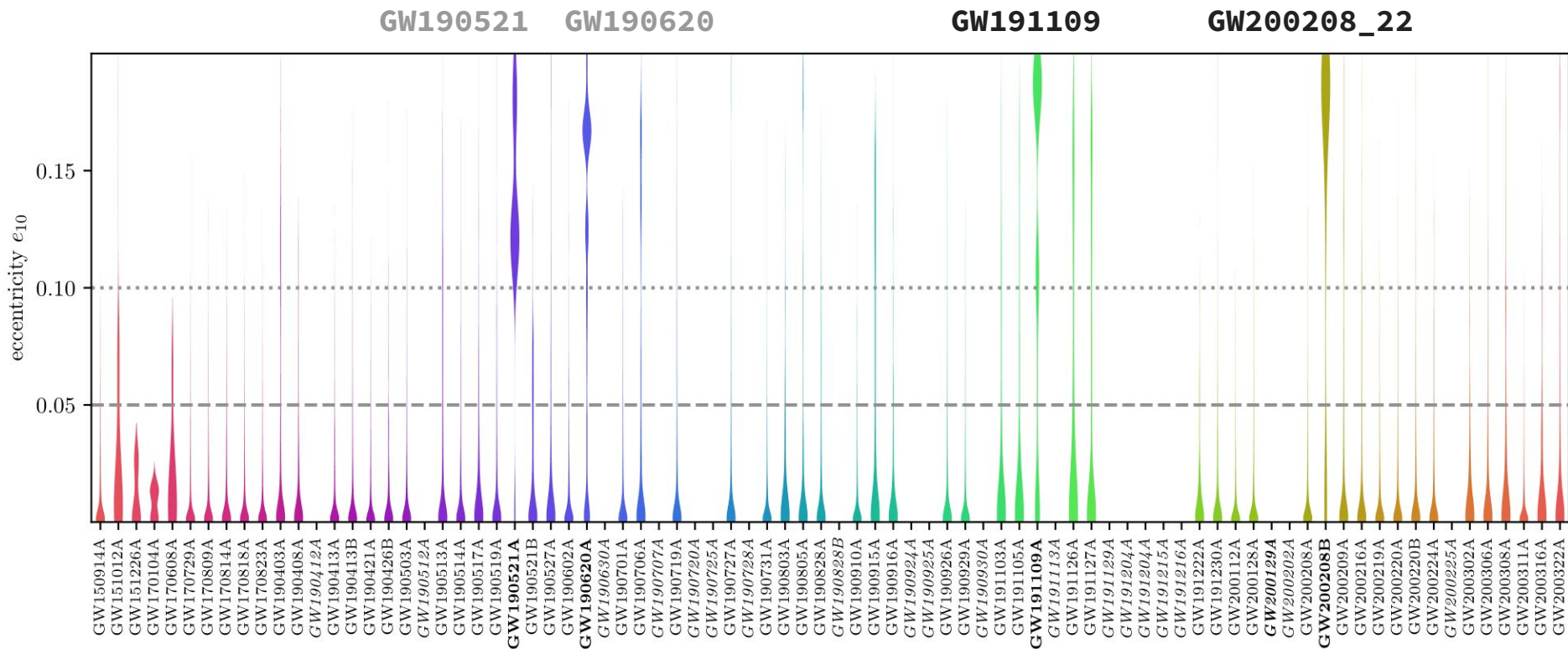
GW190521 GW190620



RS, Lasky & Thrane 2019, 2021

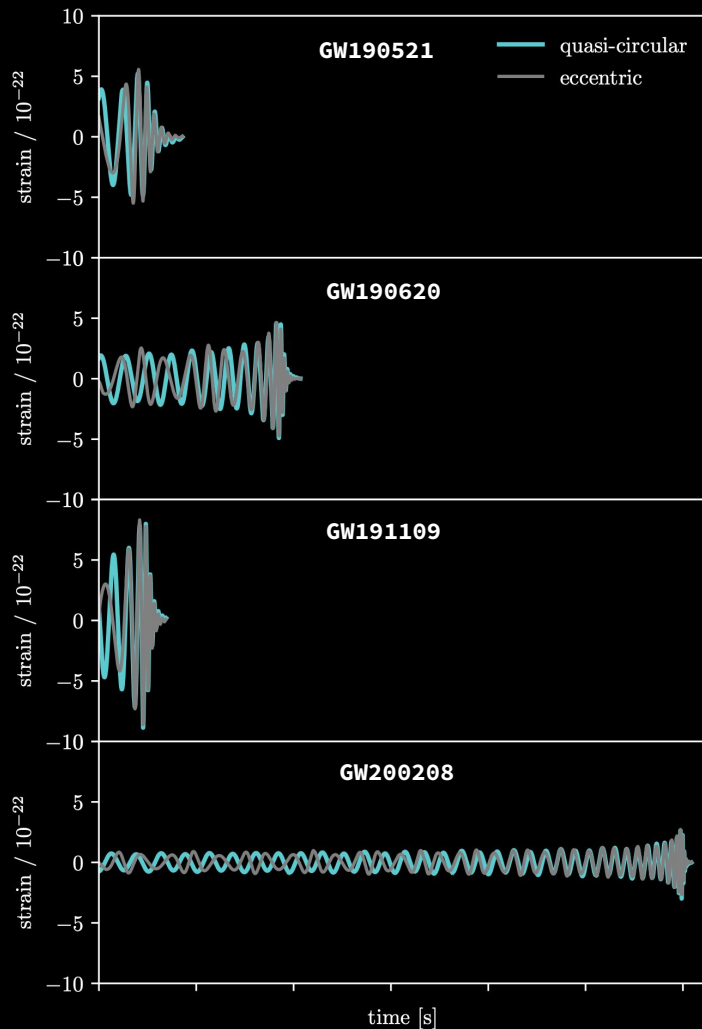
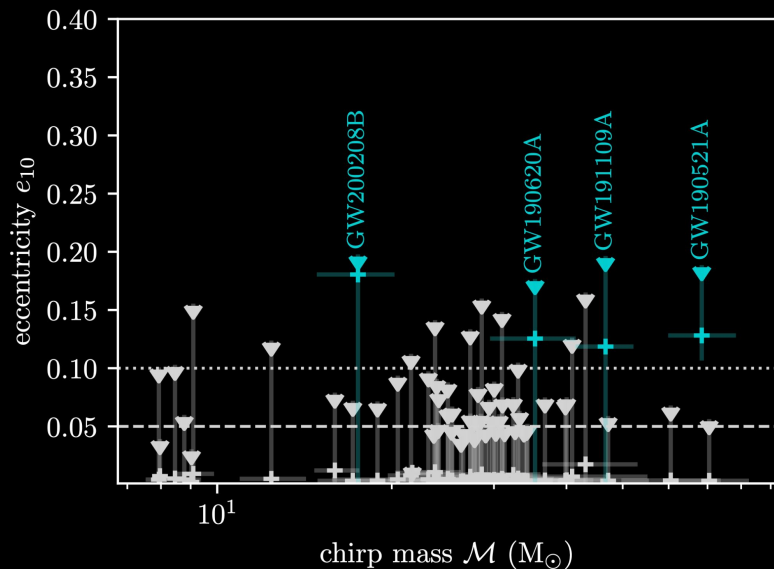
See also RS, Lasky, Thrane & Calderon-Bustillo 2020

RESULTS: GWTC-3



FOUR (POSSIBLY) ECCENTRIC EVENTS IN GWTC-3

- Panel width spans 0.35 seconds and shows median posterior waveforms



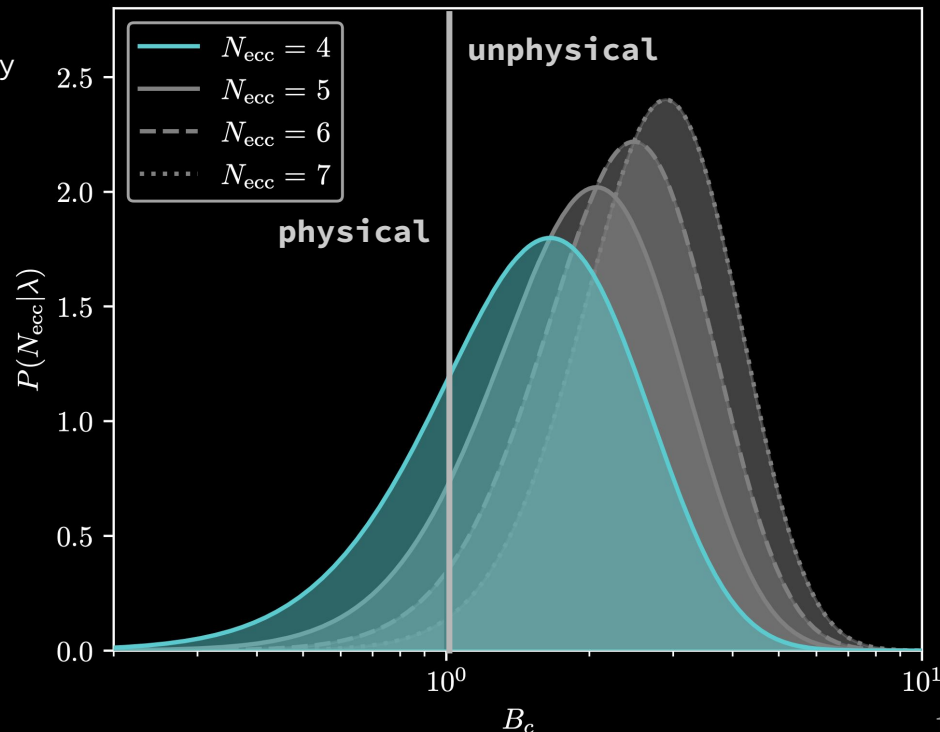
POPULATION IMPLICATIONS

- Branching fraction

- See Zevin, RS, Kremer, Thrane & Lasky 2021, arXiv:2106.09042
- Consistent with 100% ($B_c=1$) of population formed in GCs
- ...but also consistent with other dynamical channels contributing eccentric mergers

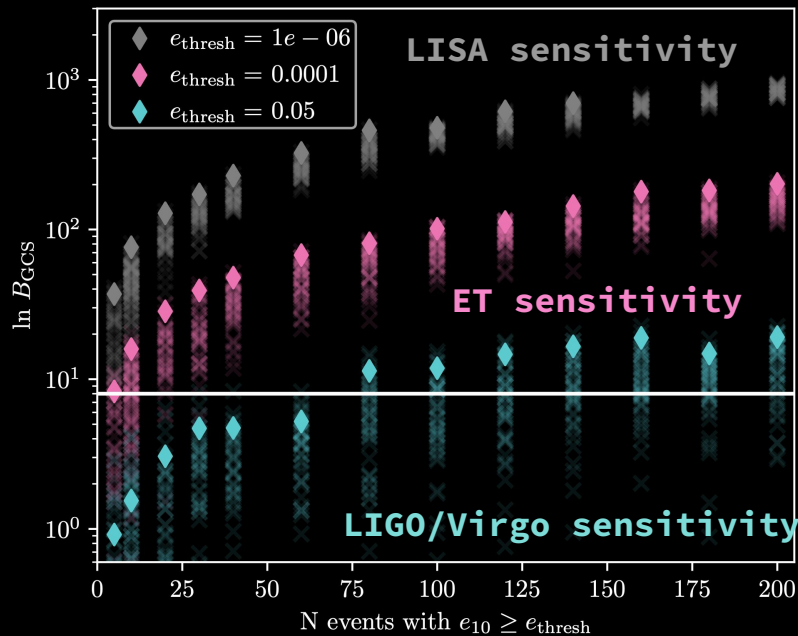
$$p(N_{\text{ecc}}|\lambda) = e^{-\lambda} \lambda^{N_{\text{ecc}}} / N_{\text{ecc}}!$$

$$\lambda \equiv \xi_{\text{ecc}} \beta_c N_{\text{obs}}$$



WHEN WILL WE KNOW WHERE ECCENTRIC BBH FORM?

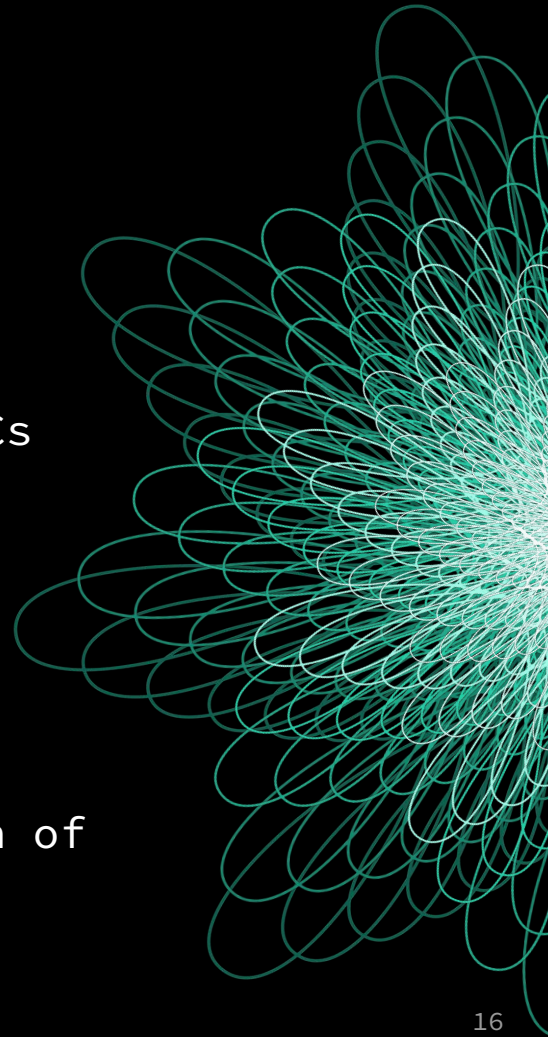
- Simulate eccentricity measurements of dynamically-formed binaries
- Compare hypotheses: GCs or AGN?
- If all form in GCs, can distinguish from AGN after ~80 detectably-eccentric LIGO-Virgo observations



RS, Lasky & Thrane 2022, in prep.

SUMMARY

- Potentially (at least) 4 eccentric events in GWTC-3
- Consistent with 100% of mergers forming in GCs
- May imply other dynamical channels required
- Need ~80 eccentric events to distinguish dominant dynamical channel with LIGO/Virgo
- Further reading: How can we use a population of GC mergers to infer how GCs form?
 - See Romero-Shaw, Kremer, Lasky, Thrane & Samsing 2021 arXiv:011.14541



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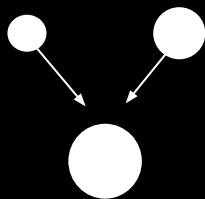
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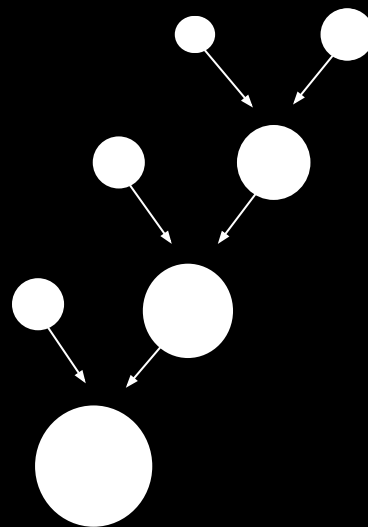


DISTINGUISHING FEATURES OF FORMATION CHANNELS

- **Mass**, Spin, Eccentricity



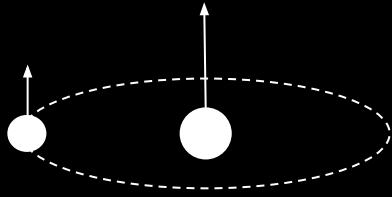
component masses $\approx 60 M_{\odot}$



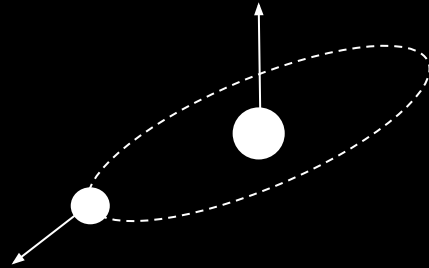
component masses \sim any

DISTINGUISHING FEATURES OF FORMATION CHANNELS

- Mass, **Spin**, Eccentricity



spins approximately aligned

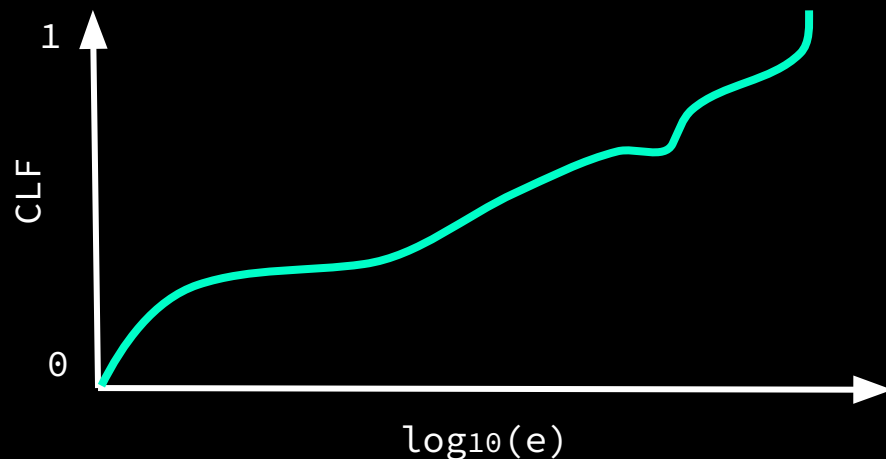


spins likely misaligned

RECONSTRUCTING ECCENTRICITY DISTRIBUTION

For each sample i with parameters θ_i :

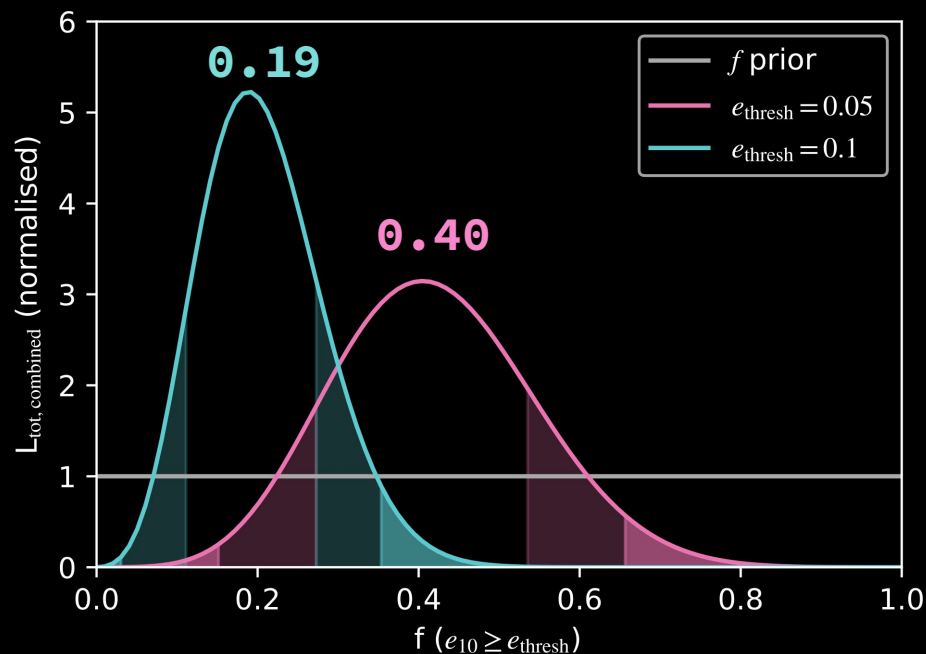
- Calculate $L(d|e)_i$ over log-uniform grid of e
- Draw random sample from cumulative $L(d|e)_i$ grid



POPULATION IMPLICATIONS

- Fraction of population with support for eccentricity above some threshold
- 1-, 2- and 3-sigma intervals shown
- Exclude $f = 0$ at greater than 2-sigma

$$\mathcal{L}(d|f) = \prod_k \left(f \int_{e_{\text{thresh}}}^{e_{\text{max}}} de \pi(e) \mathcal{L}(d_k|e) + (1-f) \int_{e_{\text{min}}}^{e_{\text{thresh}}} de \pi(e) \mathcal{L}(d_k|e) \right)$$



WHEN WILL WE KNOW WHERE ECCENTRIC BBH FORM?

- Approximate each event posterior as a delta function
- Model population from GCs, compare against AGN hypothesis

