A visualization of a gravitational well, showing a bright, glowing ring of light in the upper left and a similar ring in the lower right, set against a dark, starry background. The rings represent the paths of objects in a gravitational field, with the center being a point of infinite density.

# No peaks without valleys

## An investigation of the stable mass transfer channel in light of the NS-BH mass gap

NBIA Copenhagen - Lieke van Son

And others i.a.: Selma de Mink, Charlie Conroy, Mathieu Renzo, Tom Callister, Will Farr, Katie Breivik, Manos Zapartas, Stephen Justham



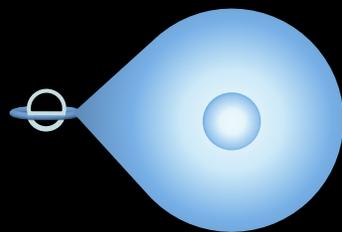
UNIVERSITY OF AMSTERDAM



Image credit: Ligo/Virgo/Kagra

CENTER FOR **ASTROPHYSICS**

HARVARD & SMITHSONIAN



The stable mass transfer channel leads to a  
minimum primary mass

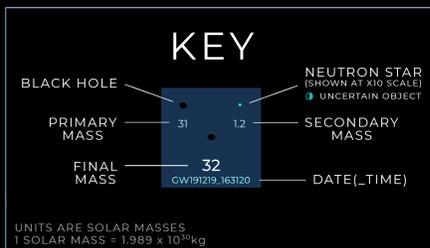
this can cause a “NS-BH mass gap” in the GW  
inferred mass distribution

# Nov 2021:

# GRAVITATIONAL WAVE MERGER DETECTIONS

SINCE 2015

# GWTC-3

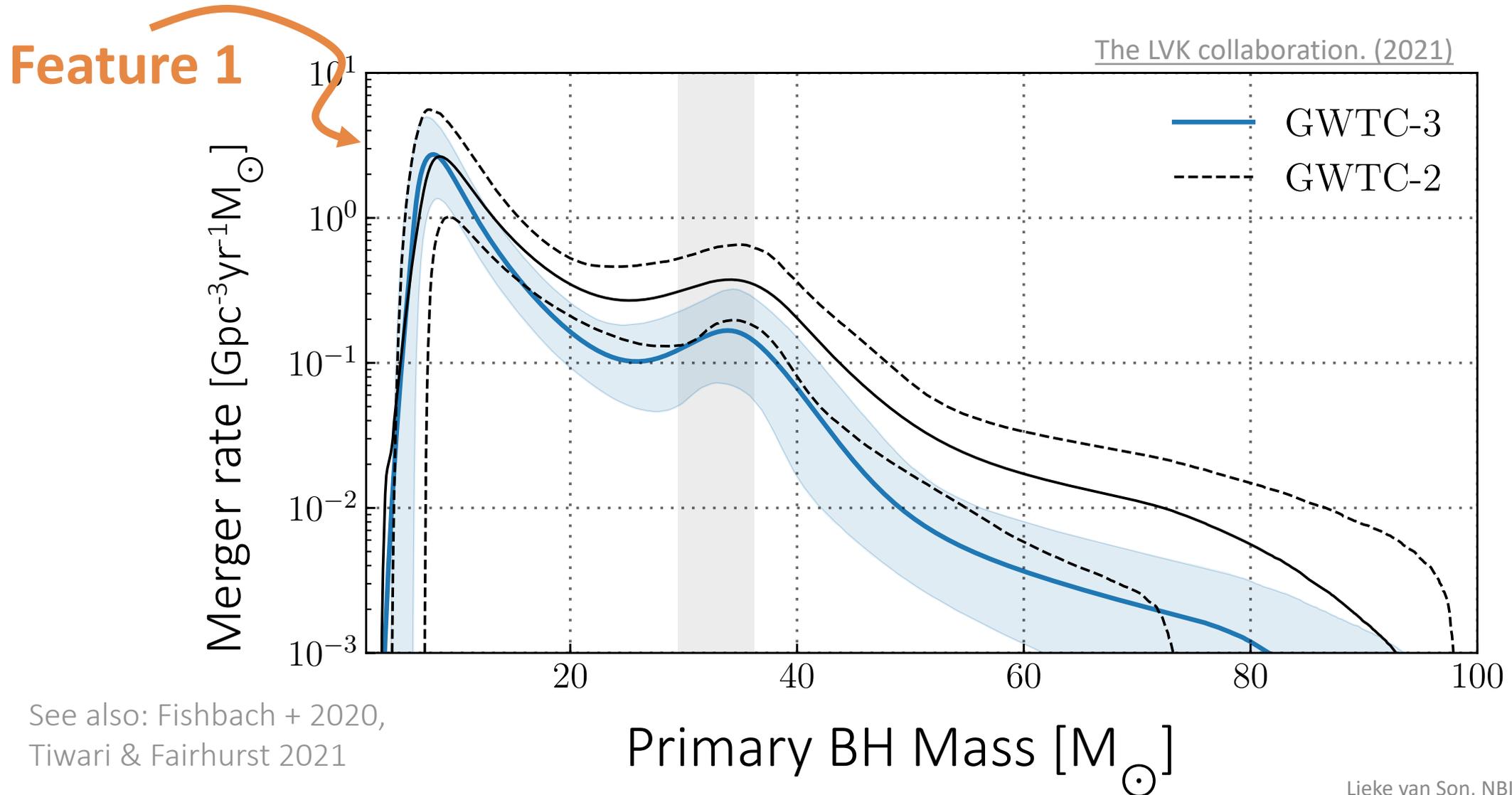


Note that the mass estimates shown here do not include uncertainties, which is why the final mass is sometimes larger than the sum of the primary and secondary masses. In actuality, the final mass is smaller than the primary plus the secondary mass.

The events listed here pass one of two thresholds for detection. They either have a probability of being astrophysical of at least 50%, or they pass a false alarm rate threshold of less than 1 per 3 years.



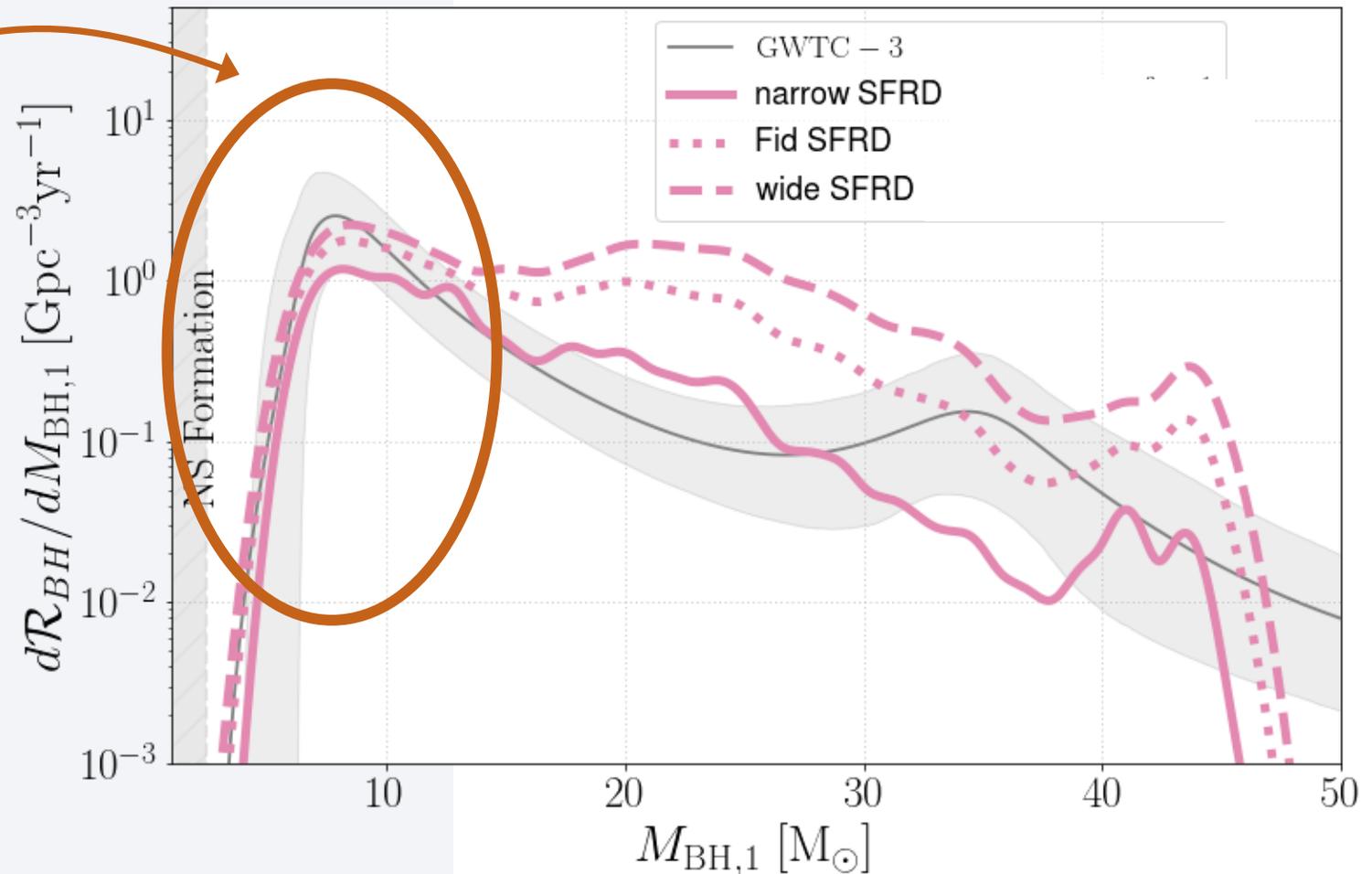
# There are features in the mass distribution!



See also: Fishbach + 2020,  
Tiwari & Fairhurst 2021

# The low mass end is a great place to start

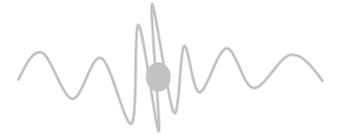
less bothered by  
metallicity dependent  
star formation uncertainty



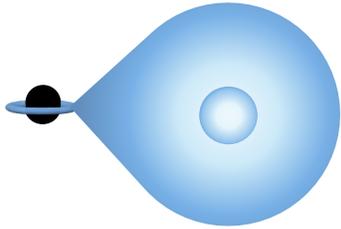
# Many different channels have been proposed...

Only few are expected to have the overall peak occur at low mass!

*Primordial BHs?*



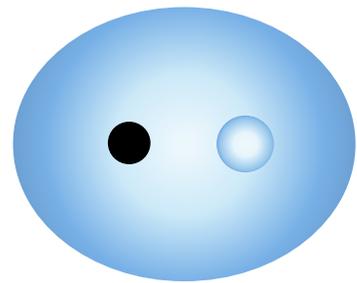
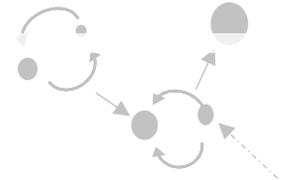
ii) Stable mass transfer



iv) Triple systems

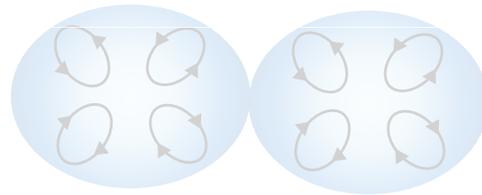


vi) Dynamical formation in massive star clusters



i) Classical  
(Common Envelope)

iii) Chemically Homogeneous

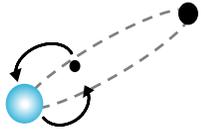


v) In gas disk of Active Galactic Nuclei

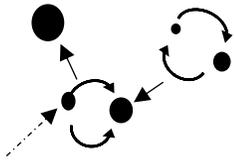


vii) Kozai resonance with SMBH

# ... most are not expected to dominate at low masses!



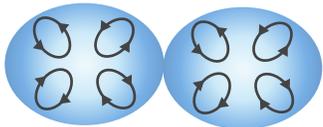
**Hierarchical mergers of NS are not efficient (neither in clusters nor triples)**  
e.g. Samsing & Hotokezaka (2021), Lu et al. (2021), Hamers et al. (2021)



**Globular clusters miss the low mass peak**  
e.g. Hong et al. 2018; Rodriguez et al. 2019; Antonini & Gieles 2020

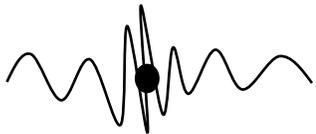
**Young open clusters: light BHs are easily ejected and don't contribute**

e.g. Portegies Zwart & McMillan 2000; Ziosi et al. 2014; Bouffanais et al. 2019; Santoliquido et al. 2021; Fragione & Banerjee 2021



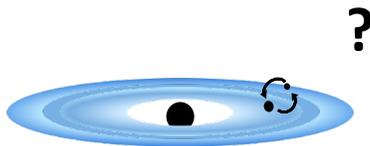
**CHE leads to  $\sim 30 + 30 M_{\odot}$**

e.g. de Mink et al. 2009; Song et al. 2013, 2016; Mandel & de Mink 2016; Marchant et al. 2016; Riley et al. 2021)



**Population III binaries peak at  $\sim 20 M_{\odot}$**

e.g. Marigo et al. 2001; Belczynski et al. 2004; Kinugawa et al. 2014; Inayoshi et al. 2017)



**AGN disks: rates are highly uncertain, but gas could lead to 10M BH?**

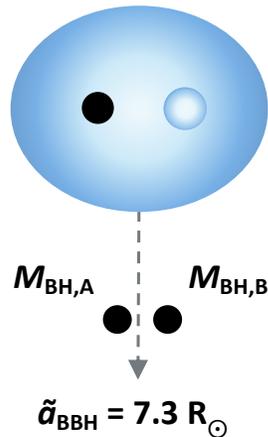
e.g. Baruteau et al. 2011; Bellovary et al. 2016; Leigh et al. 2018; Yang et al. 2019; Secunda et al. 2019; McKernan et al. 2020; Cantiello et al. 2021

# Isolated binary formation can be roughly split in two

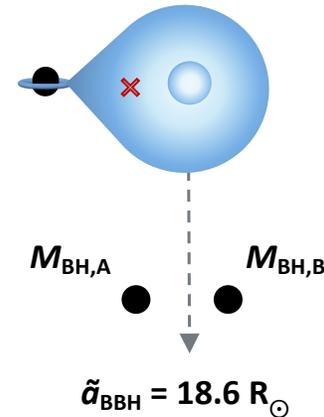
## Common envelope channel: at least one common envelope

e.g. Belczynski et al. (2007); Postnov & Yungelson (2014); Belczynski et al. 2016a; Eldridge & Maund (2016); Lipunov et al. (2017); Vigna-Gomez et al. (2018)

## Common envelope channel

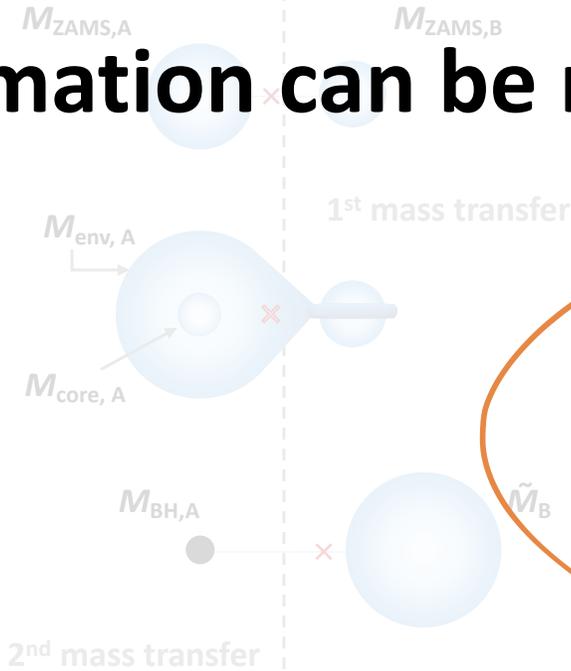


## Stable mass transfer channel

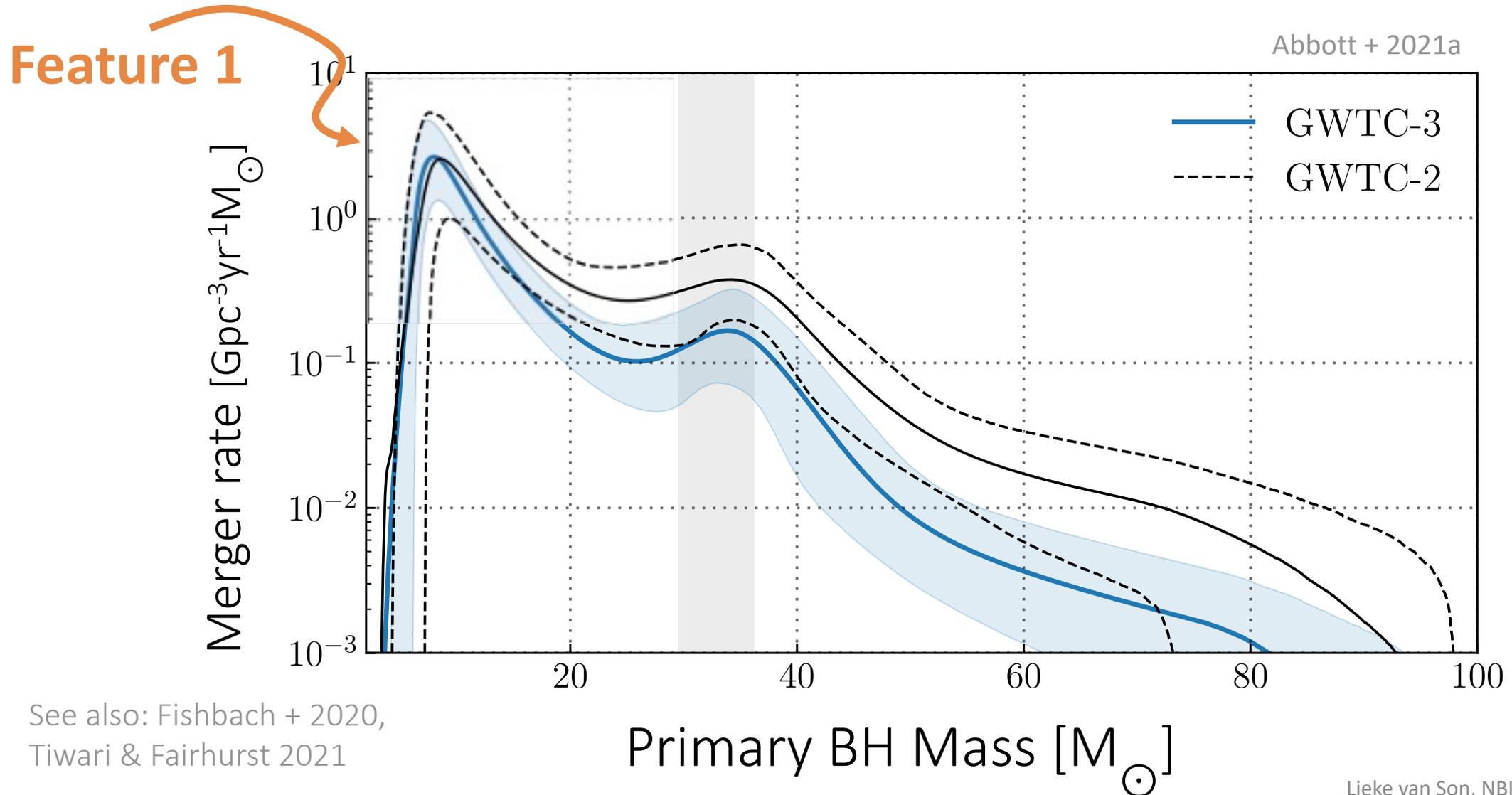


## Stable RLOF channel:

Experiences *only* stable mass transfer  
van den Heuvel et al. (2017); Inayoshi et al. (2017); Neijssel et al. (2019); Bavera et al. (2021); Marchant et al. (2021); Gallegos-Garcia et al. (2021)



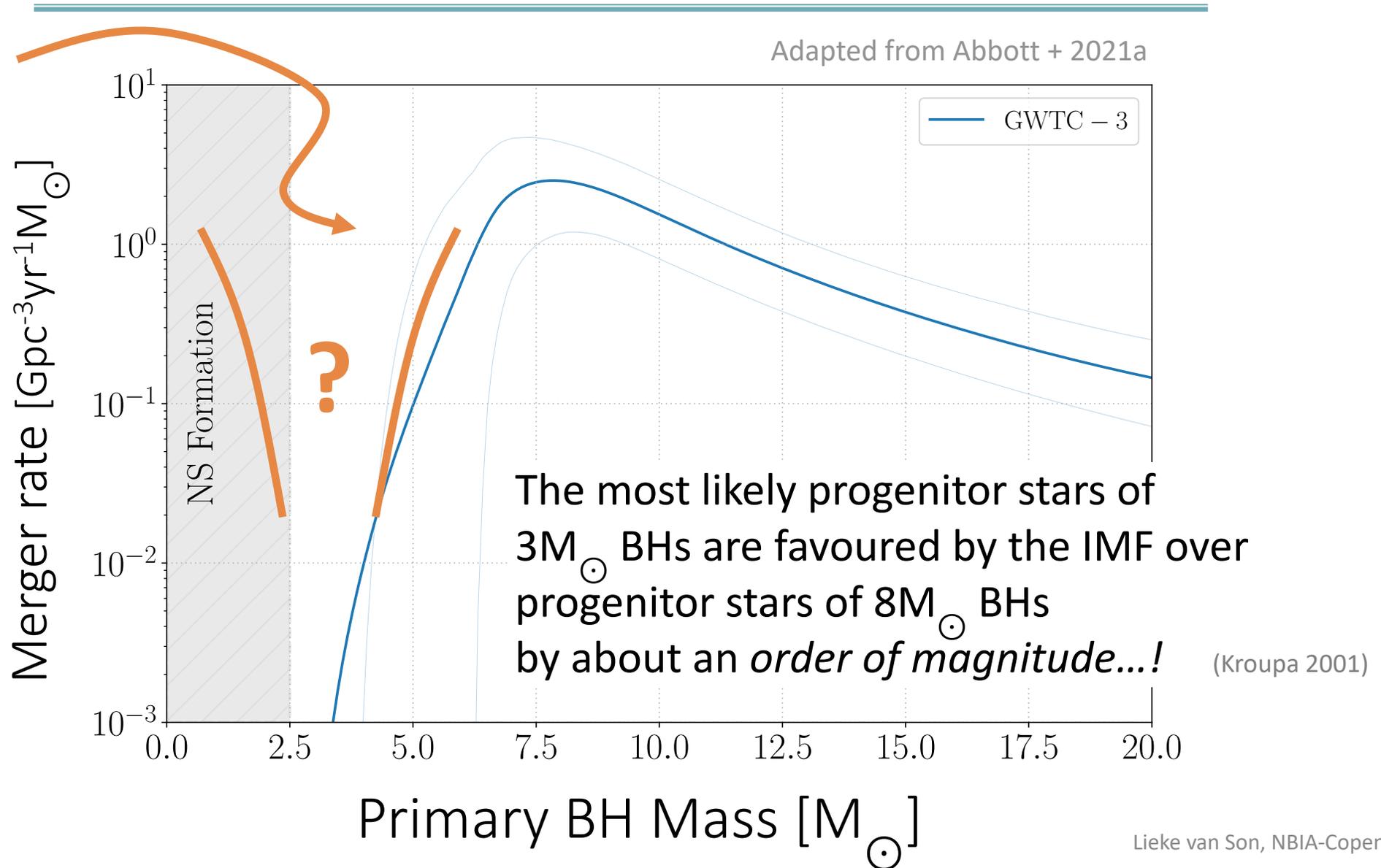
# There are features in the mass distribution!



See also: Fishbach + 2020,  
Tiwari & Fairhurst 2021

# There are features in the mass distribution!

Feature 1



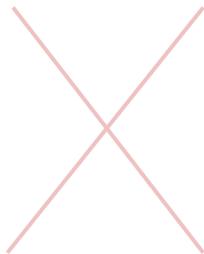
# Where are the BH's with 3-6 $M_{\odot}$ ?

(There appears to be an underabundance of 3-6 $M_{\odot}$  BHs: Fishbach + 2020, Abbott et al. 2021b, Farah + 2021, Ye & Fishbach 2021 )

We don't see them



Observational bias  
against detecting  
such systems?



(Fishbach + 2017)

A: They don't exist



You cannot form *any*  
BHs with masses 3-6  
solar mass  
("NS-BH mass gap")

e.g. Fryer & Kalogera 2001, Fryer+ 2012,  
Belczynski+2012, Fryer+2022, Olejak+2022

Lieke van Son, NBIA-Copenhagen 2022

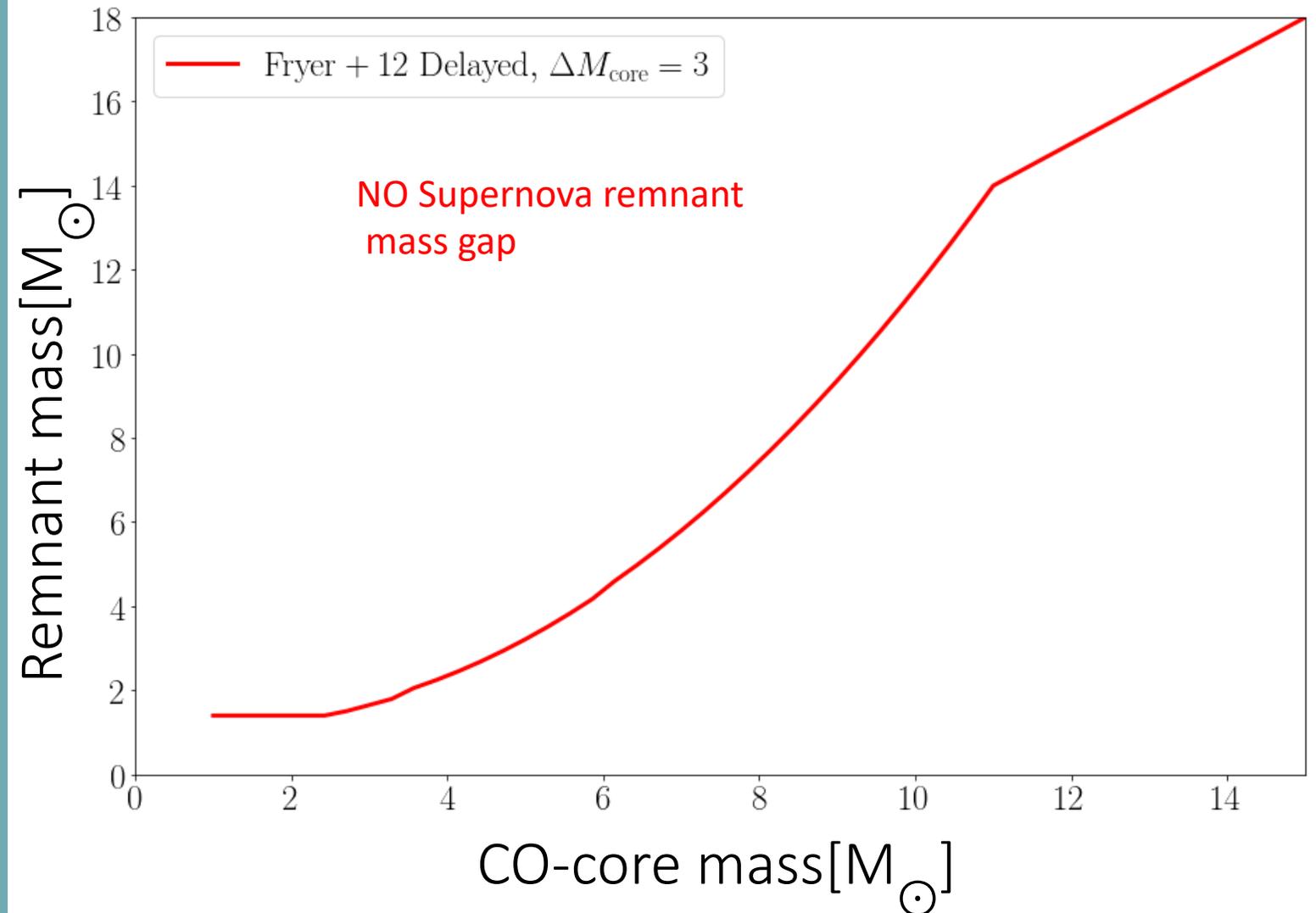
B: They don't merge

# A: They don't exist?

Supernova remnant mass function can be smooth...

SN physics: Fryer & Kalogera 2001,  
Fryer + 2012, Belczynski + 2012, Fryer + 2022,  
Olejak + 2022

Adapted from Fryer + 2012



# A: They don't exist?

...or discontinuous

SN physics: Fryer & Kalogera 2001,  
Fryer + 2012, Belczynski + 2012, Fryer + 2022,  
Olejak + 2022

Discontinuous remnant mass  
distribution based on X-ray  
observations (= **NS-BH gap**)

Bailyn et al. 1998, Özel + 2010, Farr + 2011,  
Kreidberg + 2012

Claims against a gap:

Casares et al. 2017; Wyrzykowski & Mandel 2020

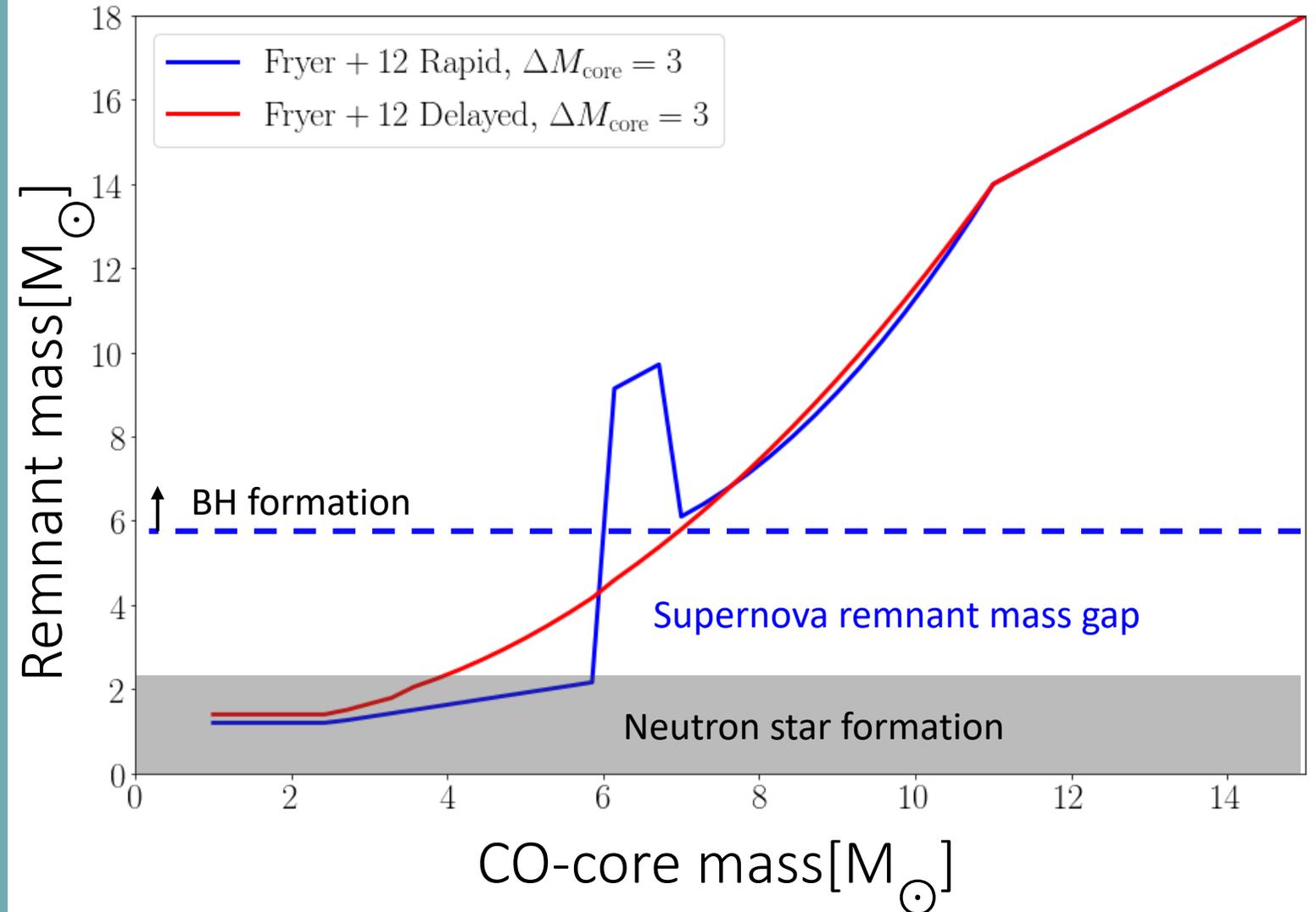
**2MASS J0521** (RV): Thompson et al. 2019,

Unicorn & Giraffe: Jayasinghe et al. 2021, 2022

**GW190814** (GW): LVK 2020. **OB110462**

(microlensing): Sahu+ 2022, Lam + 2022

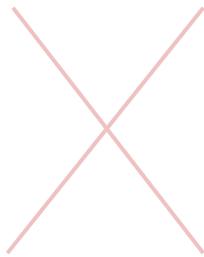
Adapted from Fryer + 2012



# Where are the BH's with 3-6 $M_{\odot}$ ?

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You cannot form *any*  
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solar mass  
("NS-BH mass gap")



e.g. Fryer & Kalogera 2001, Fryer+ 2012,  
Belczynski+2012, Fryer+2022, Olejak+2022

B: They don't merge

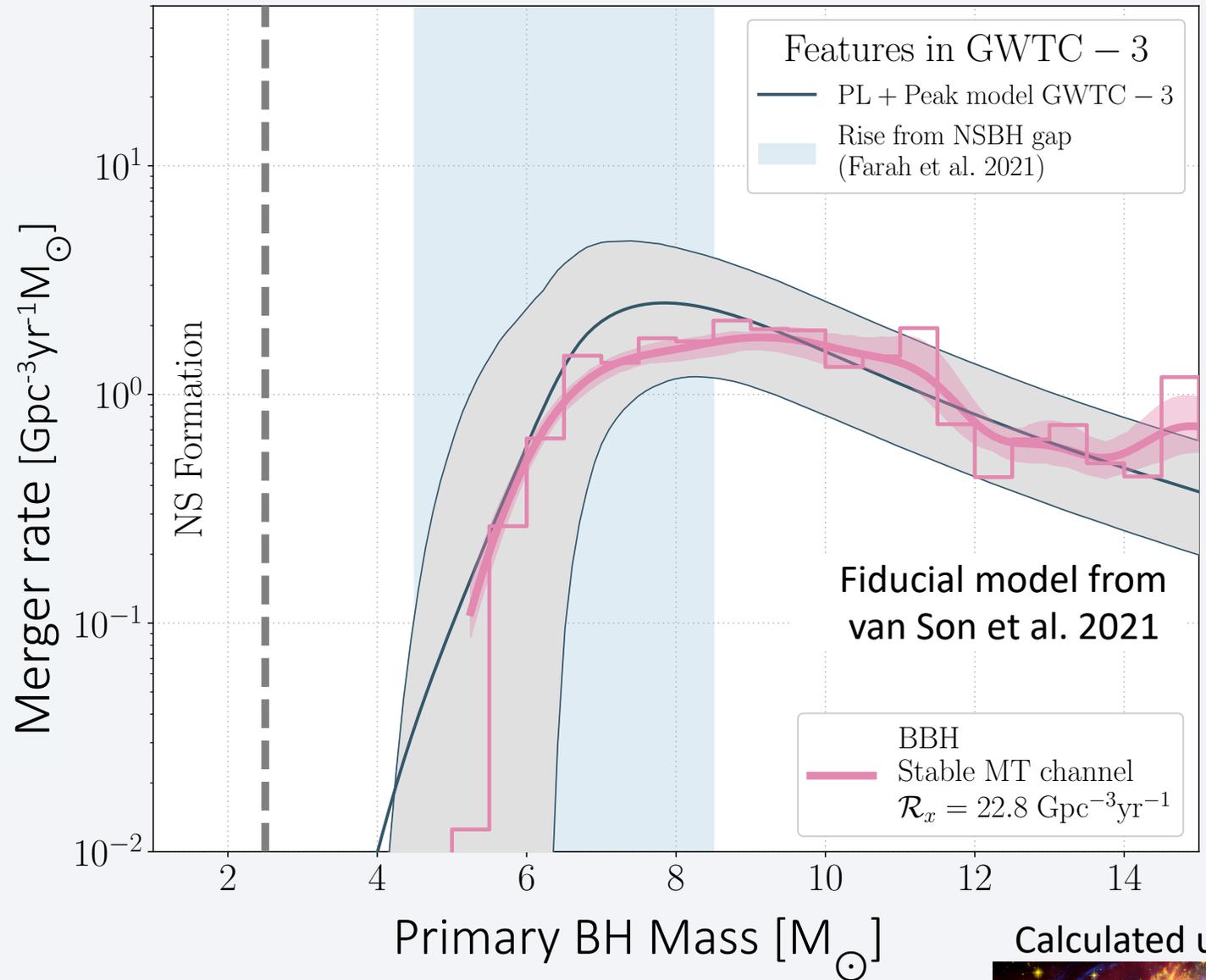
Evolutionary bias  
against merging  
double compact  
objects

Van Son et al. in prep

# What does the stable channel predict?

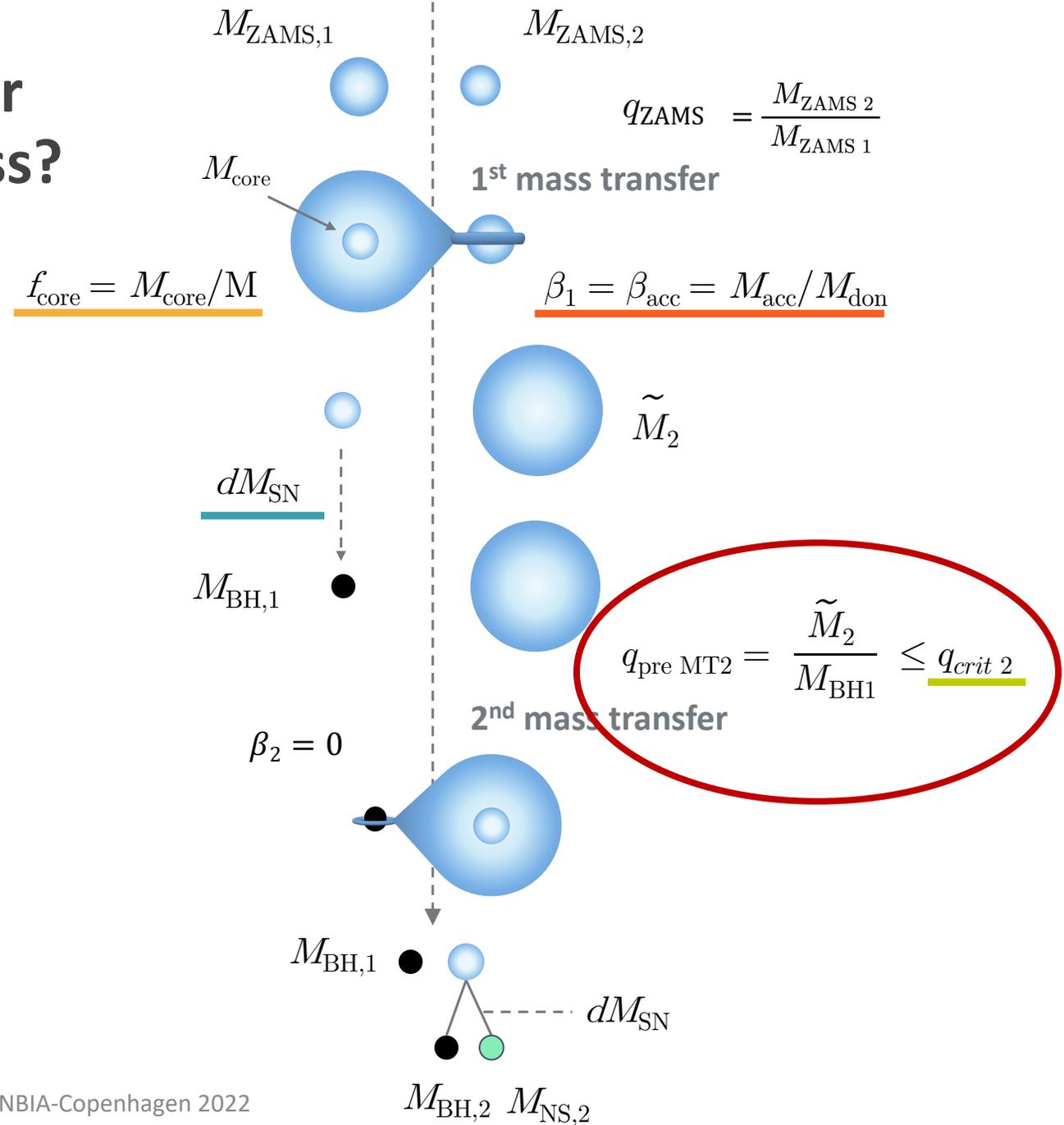
The fiducial stable channel matches the *rate* and *shape* at low mass

→ Why?



# Why does the stable mass transfer channel drop below a certain mass?

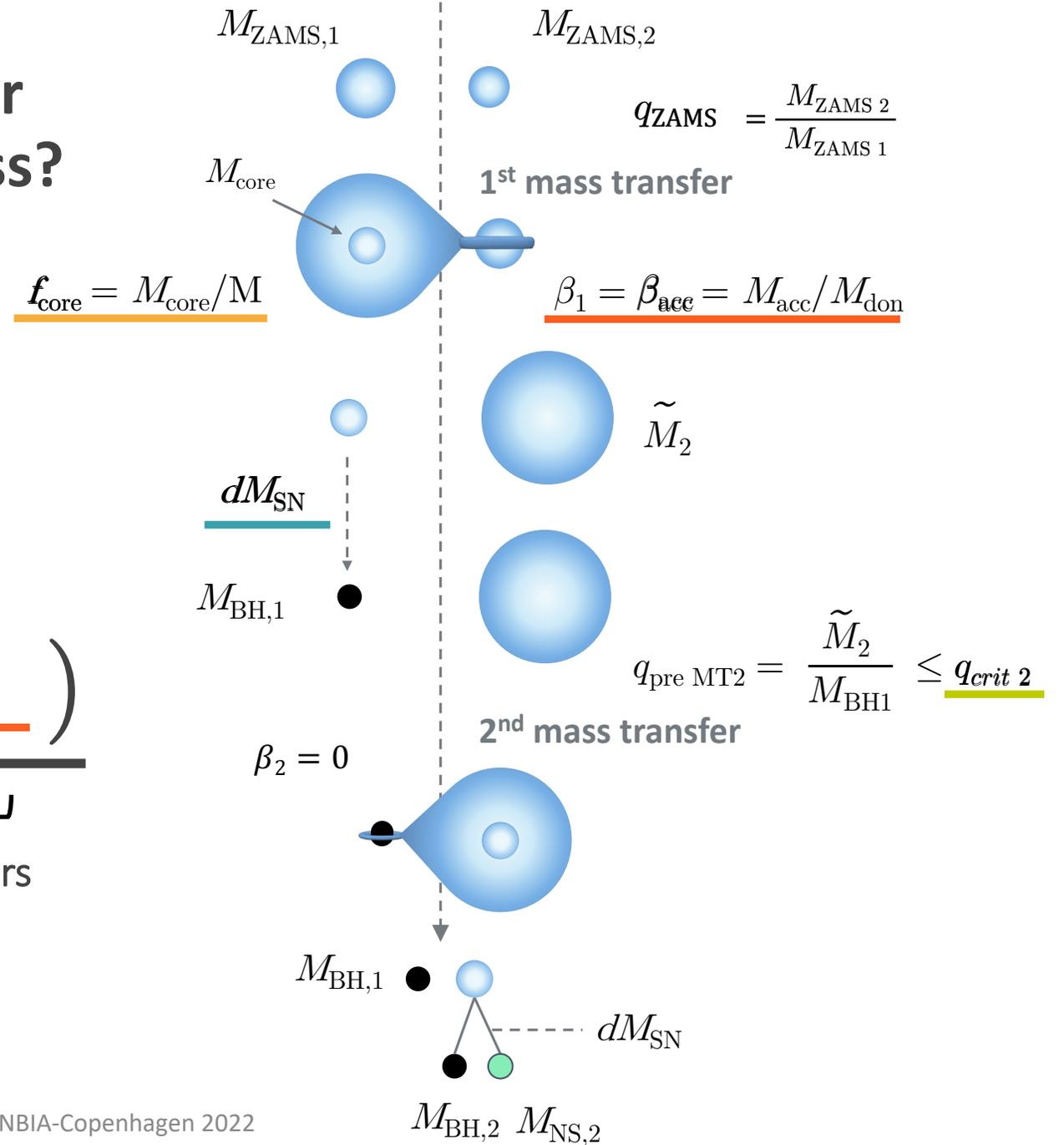
Requiring mass transfer stability imposes a minimum on the mass!



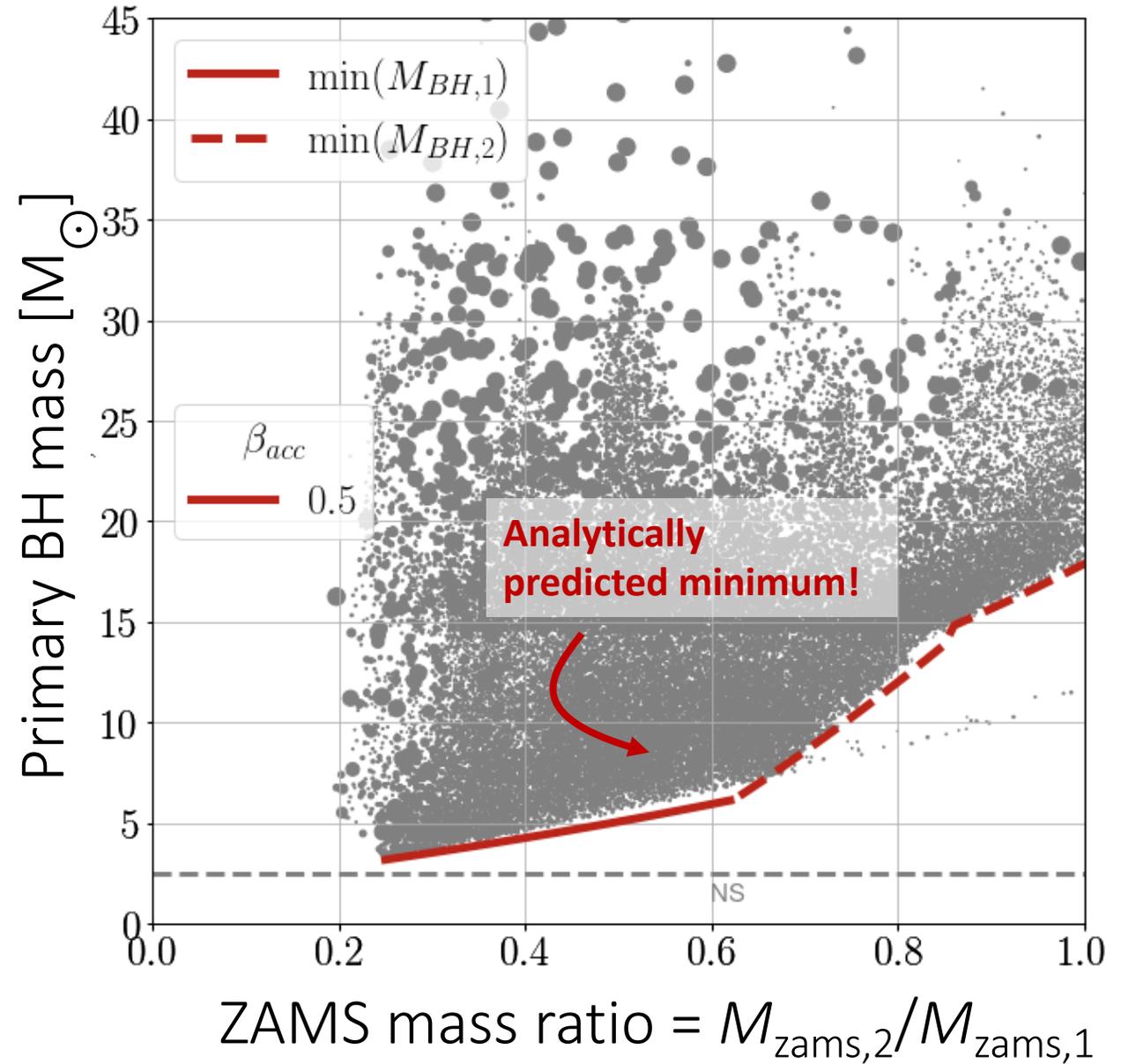
# Why does the stable mass transfer channel drop below a certain mass?

$$M_{\text{BH}} > f(\underbrace{\hspace{10em}}_{\text{Initial distribution variable}} \underbrace{\hspace{10em}}_{\text{Physics parameters}})$$

van Son et al. (in prep)



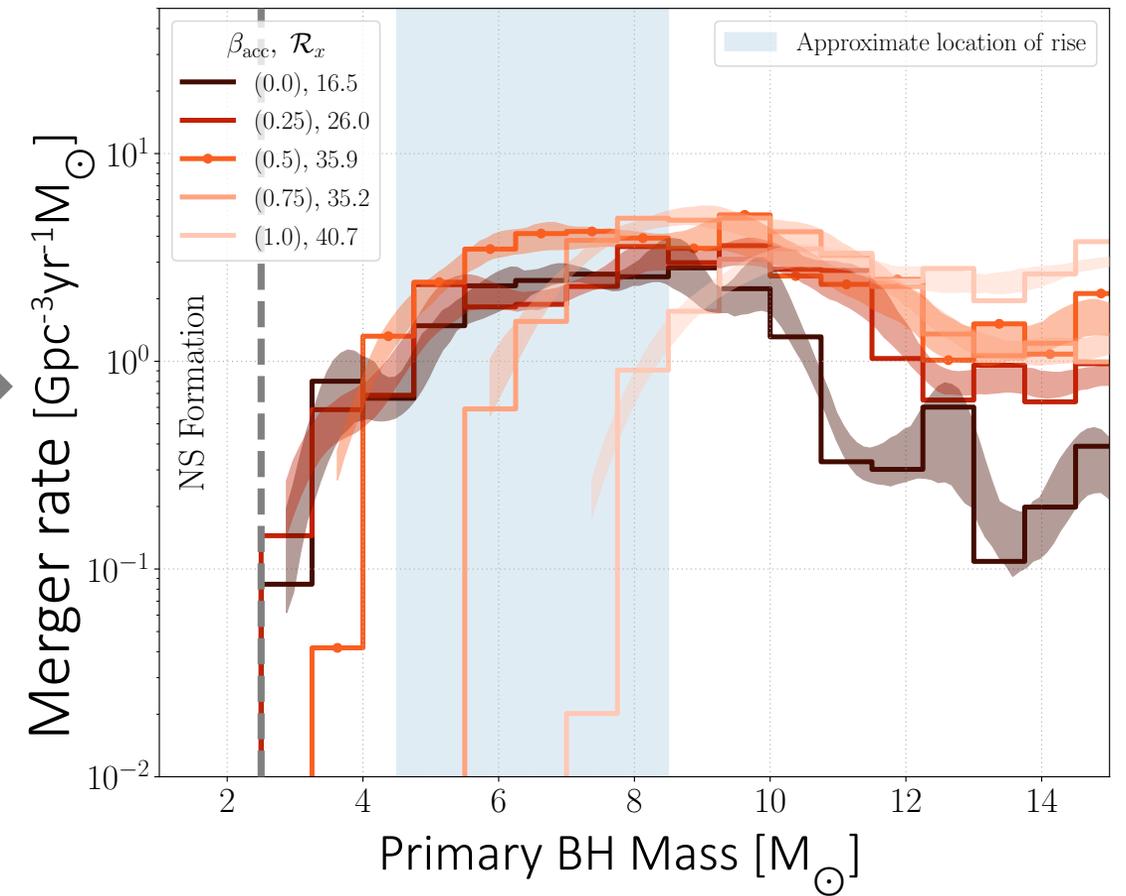
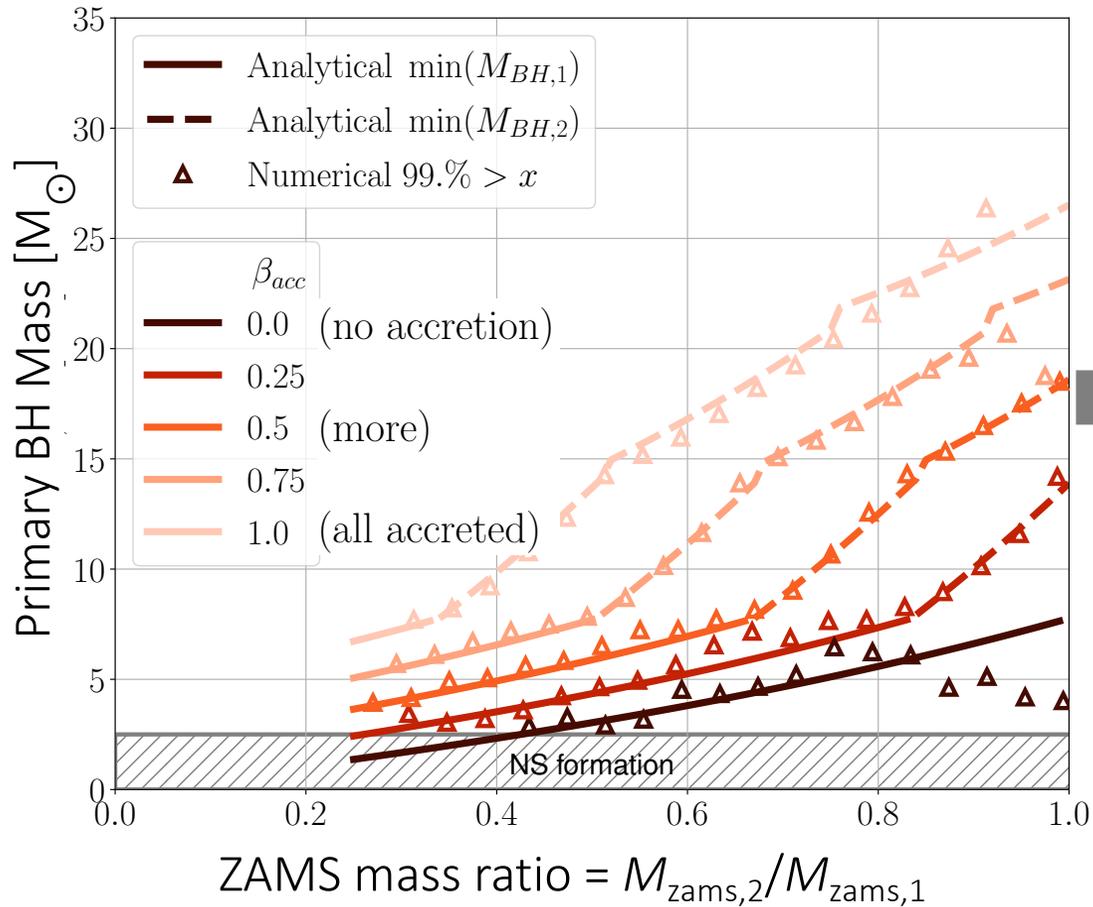
We can predict  
the minimum  
BH mass  
analytically ....!



**This creates a dearth of low mass BHs without the need for a gap in the remnant mass distribution..!**

**Variations in mass accreted**

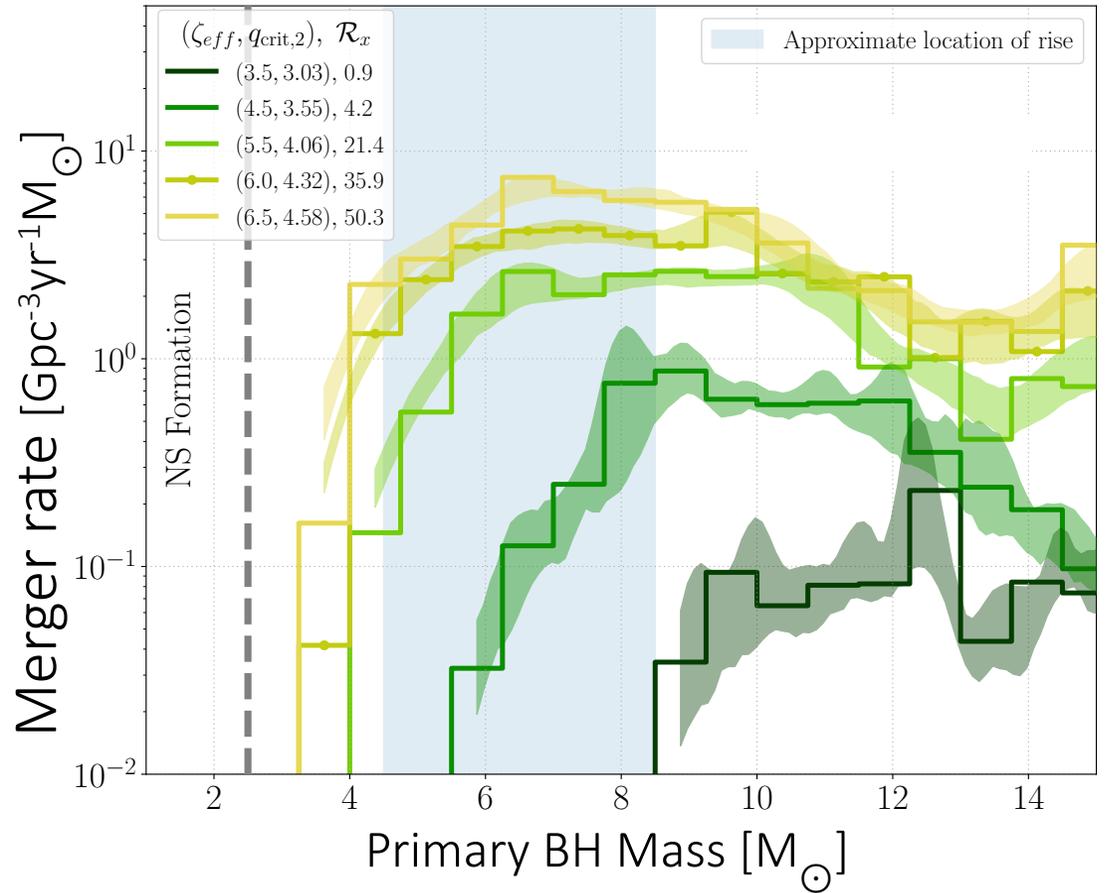
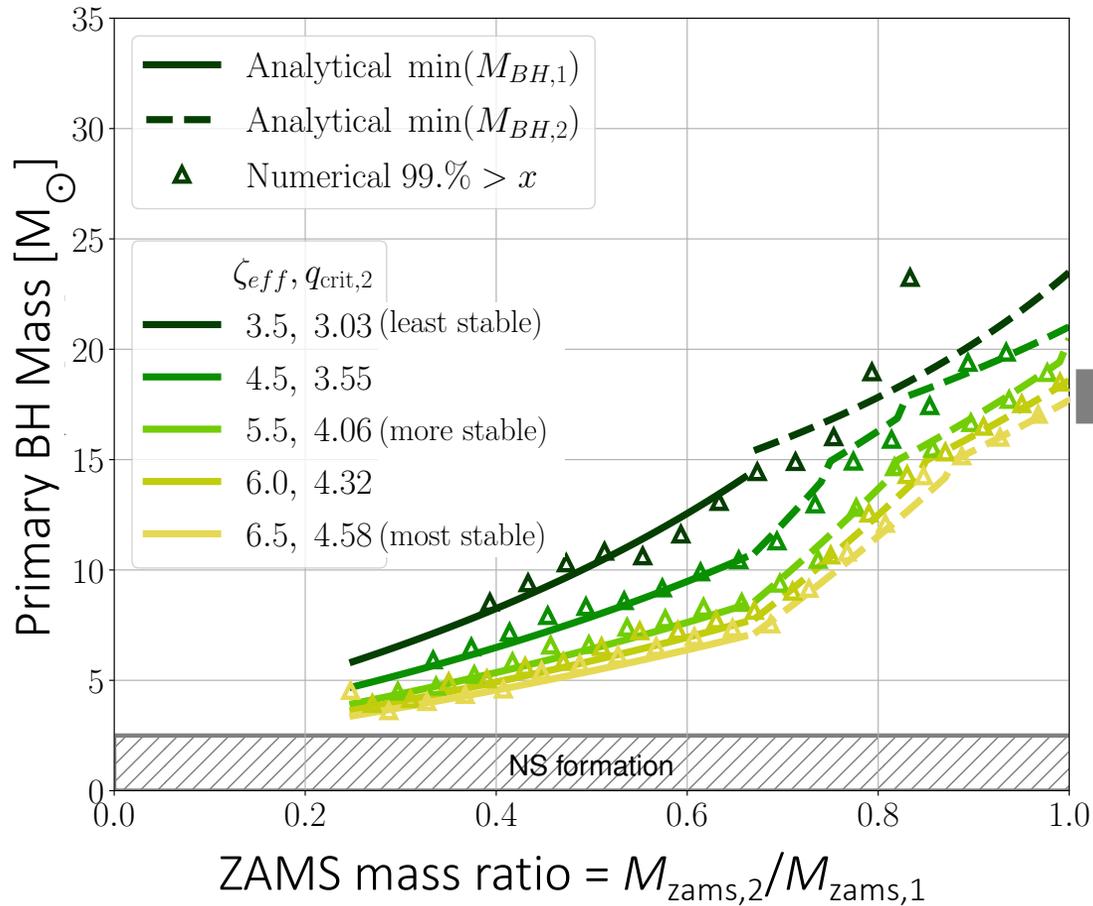
van Son et al. (in prep)



**This creates a dearth of low mass BHs without the need for a gap in the remnant mass distribution..!**

**Variations in mass transfer stability**

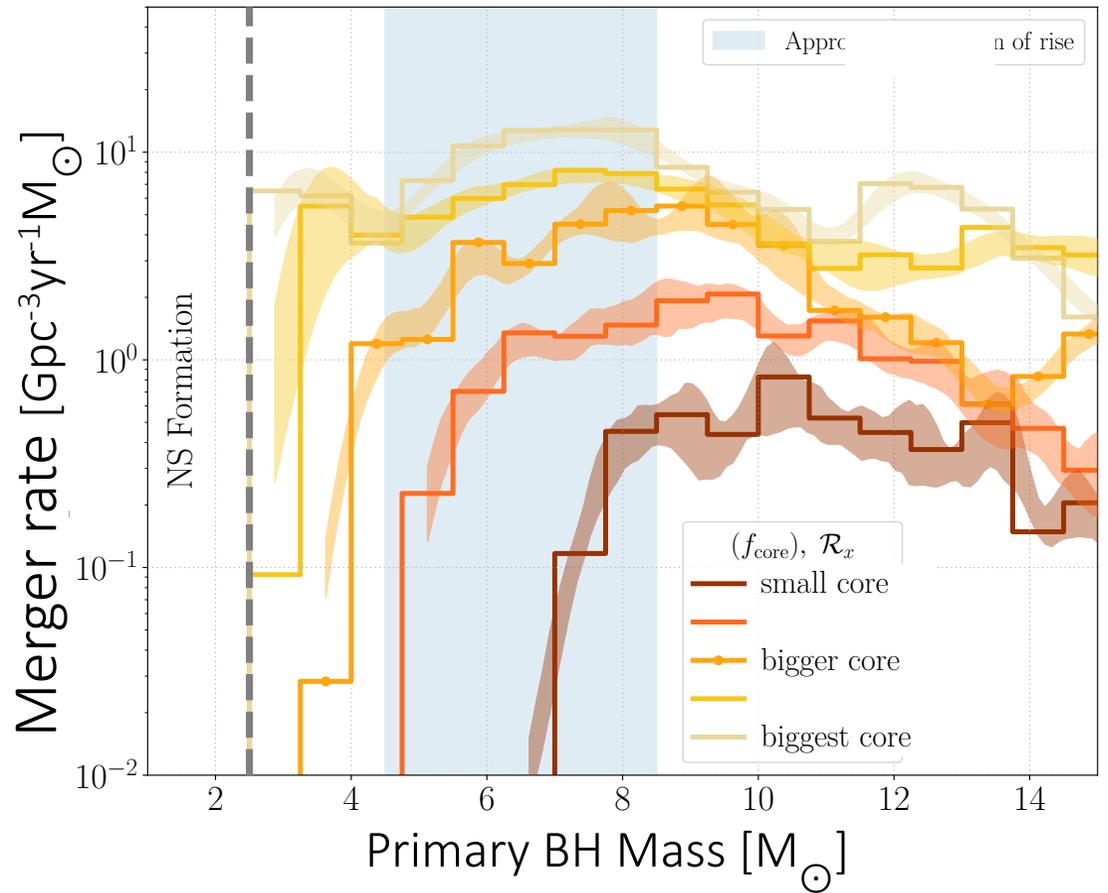
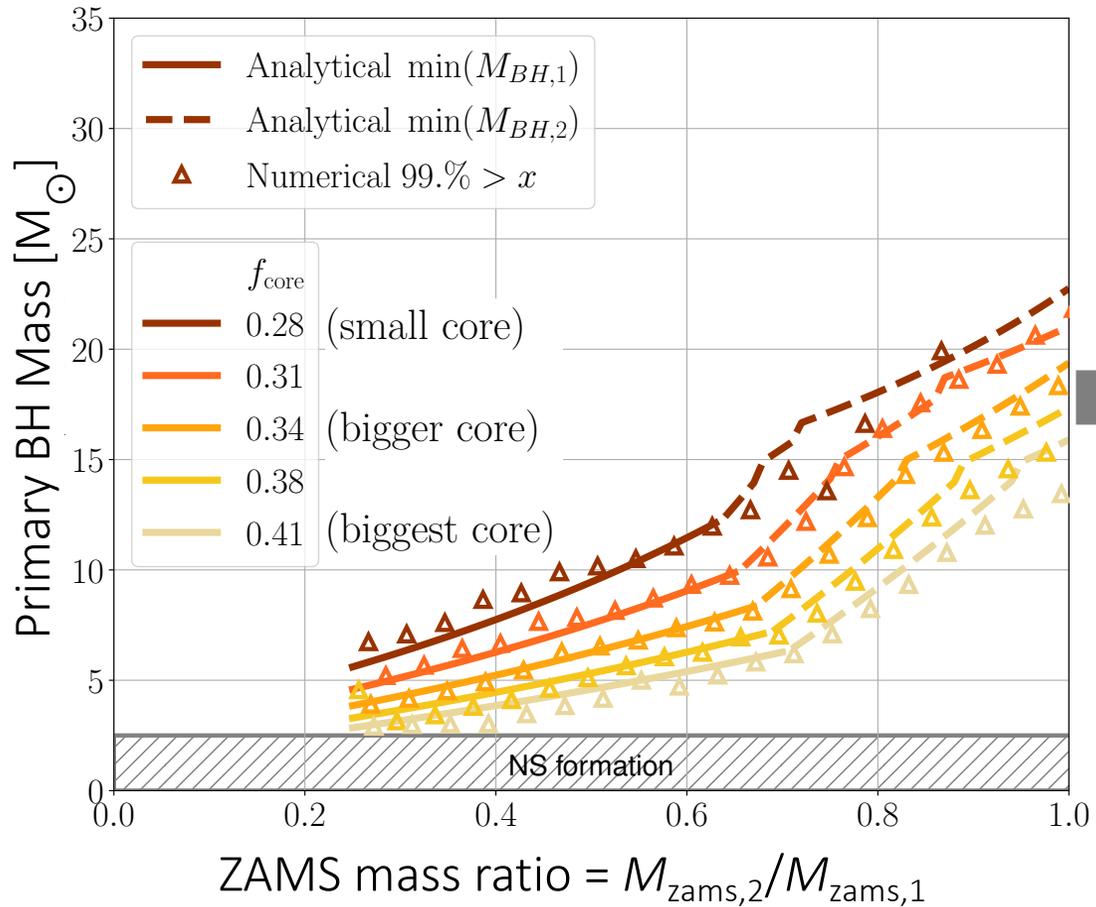
van Son et al. (in prep)



**This creates a dearth of low mass BHs without the need for a gap in the remnant mass distribution..!**

**Variations in core mass fraction**

van Son et al. (in prep)



# Implications

A GW-observed dearth of BHs below  $\sim 6 M_{\odot}$   
could be caused by:

A) The supernova engine (BHs with 3-6  $M_{\odot}$  don't *exist*)

Detections of BHs with masses between 3-8  $M_{\odot}$  through e.g. Gaia  
(e.g. Janssens et al. 2022)

B) Binary evolution physics (BHs with 3-6  $M_{\odot}$  don't merge)

The stable mass transfer channel naturally produces such a death  
(van Son et al. in prep)

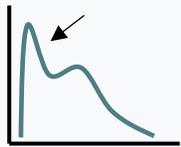
# Discussion:

**The stable mass transfer channel is bad at making the lowest mass BHs**

Is the channel you work on bad at something?

# Main takeaways

---

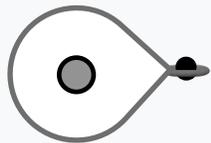


The **low mass end of the BH hole mass distribution** is a great place to start constraining physics/formation channels



## **No peaks without valleys:**

The dearth of BHs between  $3-5 M_{\odot}$  and the peak at  $\sim 9 M_{\odot}$  should be jointly investigated



The **stable mass transfer channel** to BBHs imposes a **minimum mass** that could **dismiss the need for a gap** in the remnant mass distribution

**Extra slides**

# recent work that manages to get a peak at $9 M_{\odot}$ in the mass distribution adopt a gap.

(e.g. Belczynski et al. 2016a; Giacobbo & Mapelli 2018; Giacobbo et al. 2018; Wiktorowicz et al. 2019; Belczynski et al. 2020. )

## More and more claims against a gap:

Casares et al. 2017; Wyrzykowski & Mandel 2020

2MASS J0521 (RV): Thompson et al. 2019,

Unicorn & Giraffe: Jayasinghe et al. 2021, 2022

GW190814 (GW): LVK 2020. OB110462 (microlensing): Sahu+ 2022, Lam + 2022

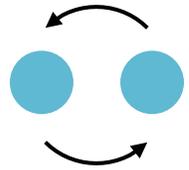
## No peaks without valleys:

The dearth of BHs between  $3-5 M_{\odot}$  and the peak at  $\sim 9 M_{\odot}$  should be jointly investigated



# The things we hope to do..

Understanding these features can teach us about:



→ Constrain formation

**We need unique and falsifiable predictions!!**

...ive stars

...ect distance measurement ('dark sirens')

Formation channels: e.g. ; Wong et al. '21, Zevin et al. '21, Mapelli et al. '22

Progenitor physics: e.g. Farmer et al. '19;'20, **van Son et al. 2020**, Bavera et al. '21,

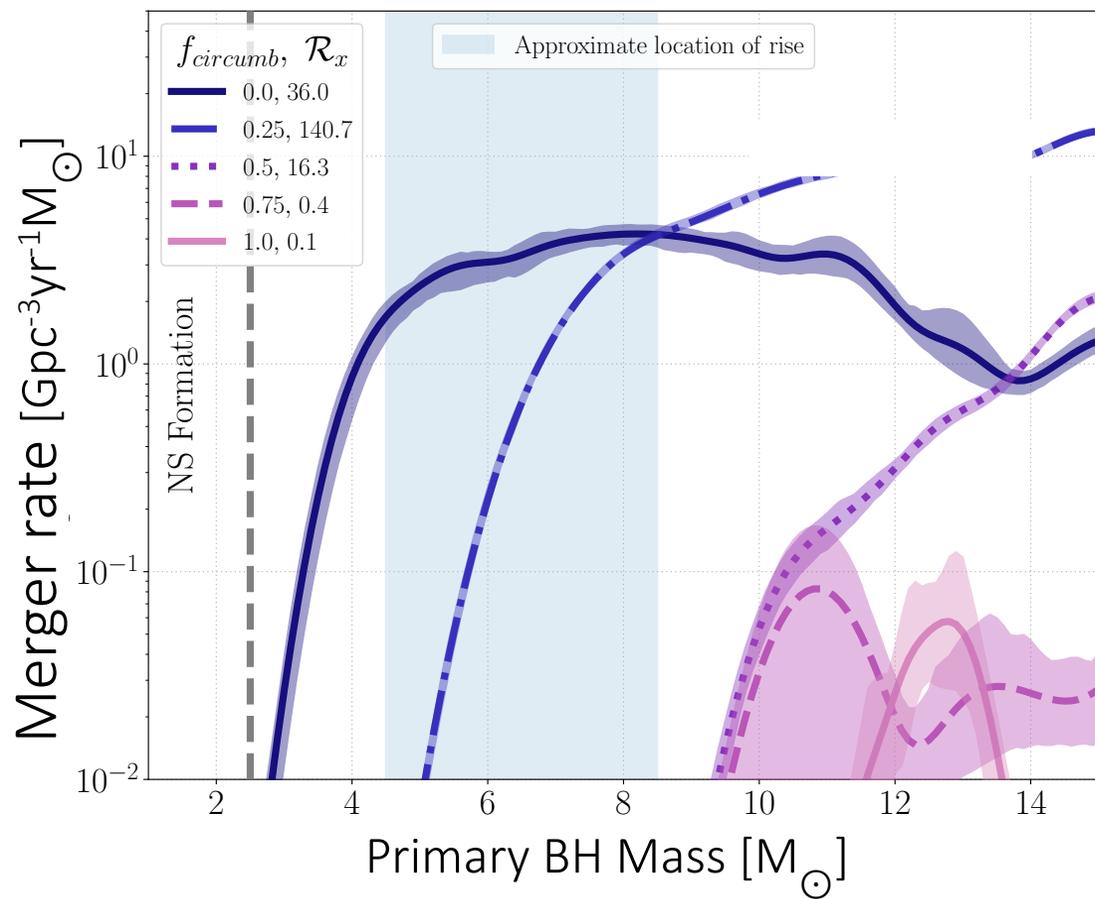
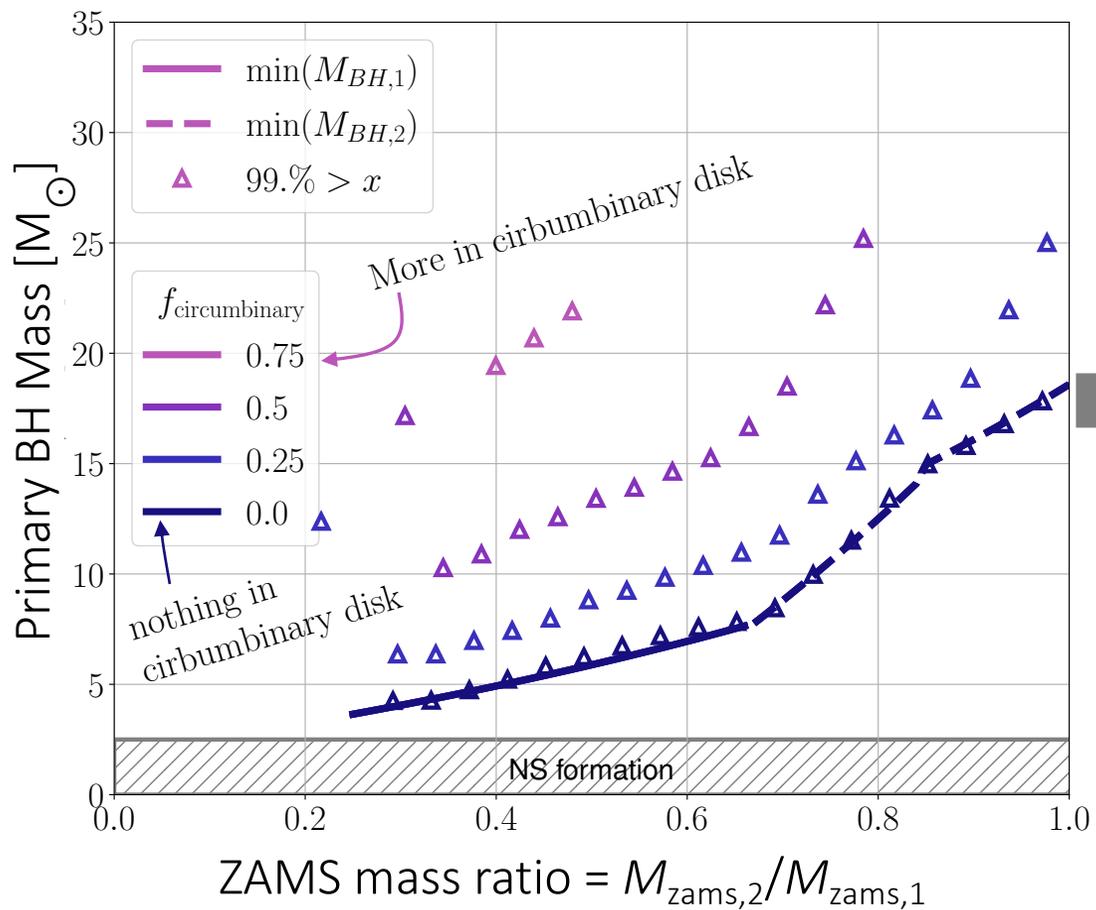
Cosmology: e.g. Holz & Hughes '05, Chen et al. '18, Ye & fishbach'21, Abbott et al. 21, María Ezquiaga & Holz '22, Mukherjee et al. '22

SF: e.g., Vitale et al. '19, Ken et al. '21, **van Son et al. 2021**.

**This creates a low mass dearth without the need for a gap in the remnant mass distribution..!**

**Variations in mass angular momentum loss**

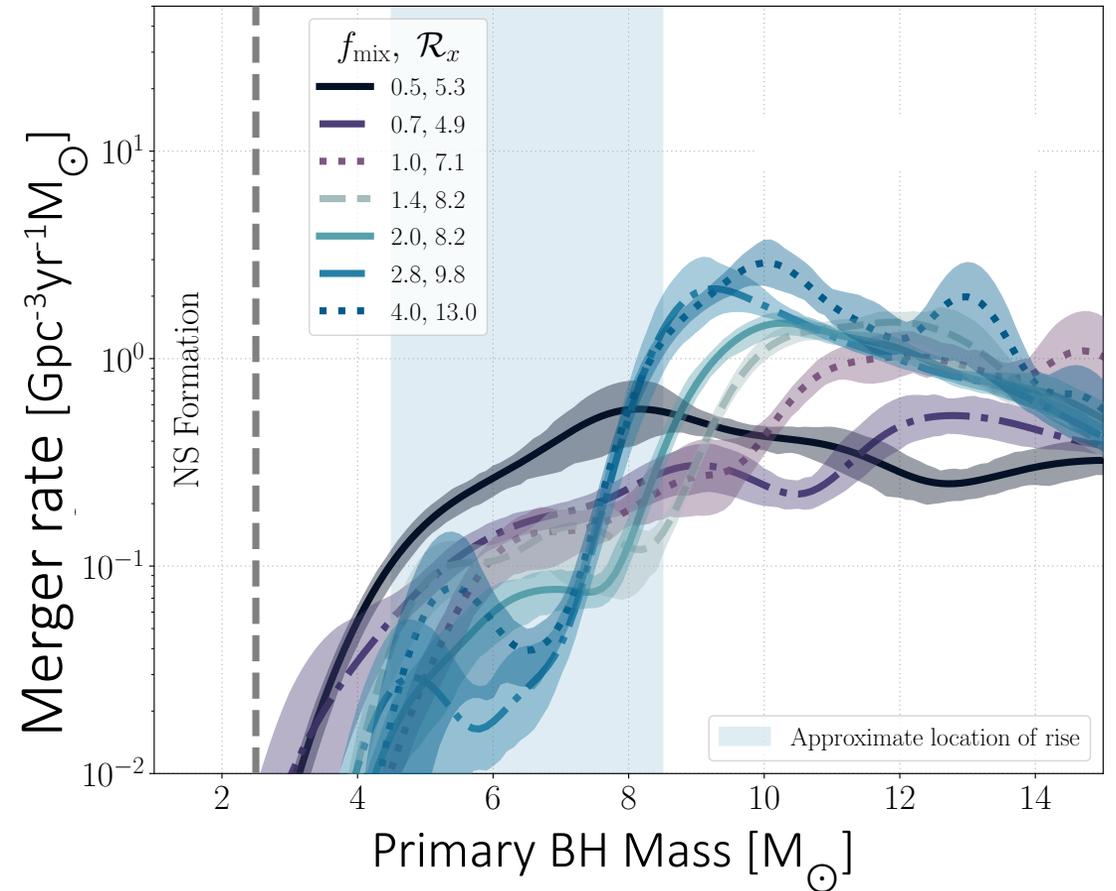
van Son et al. (in prep)



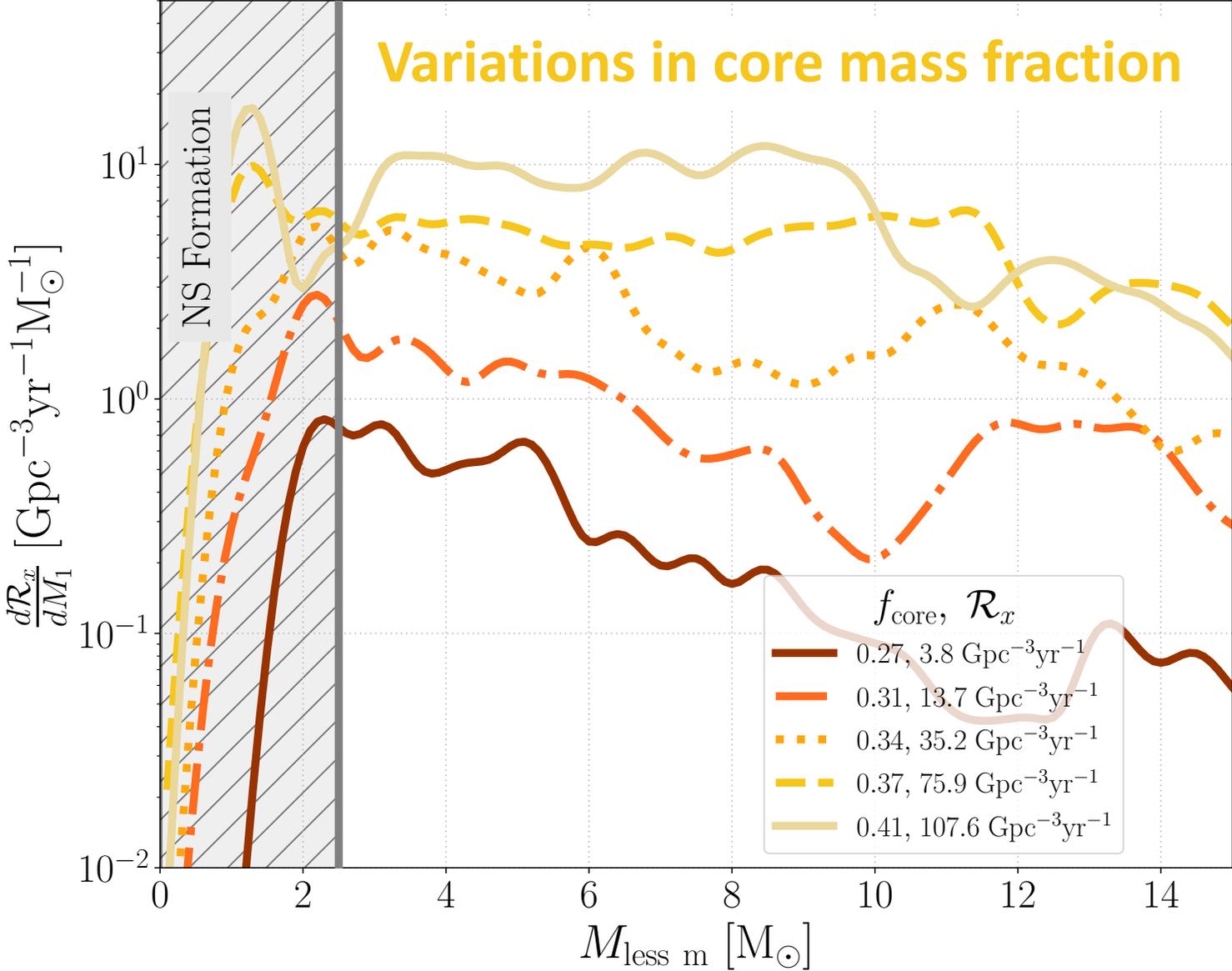
This creates a low mass dearth without the need for a gap in the remnant mass distribution..!

## Variations in the supernova remnant mass function

van Son et al. (in prep)

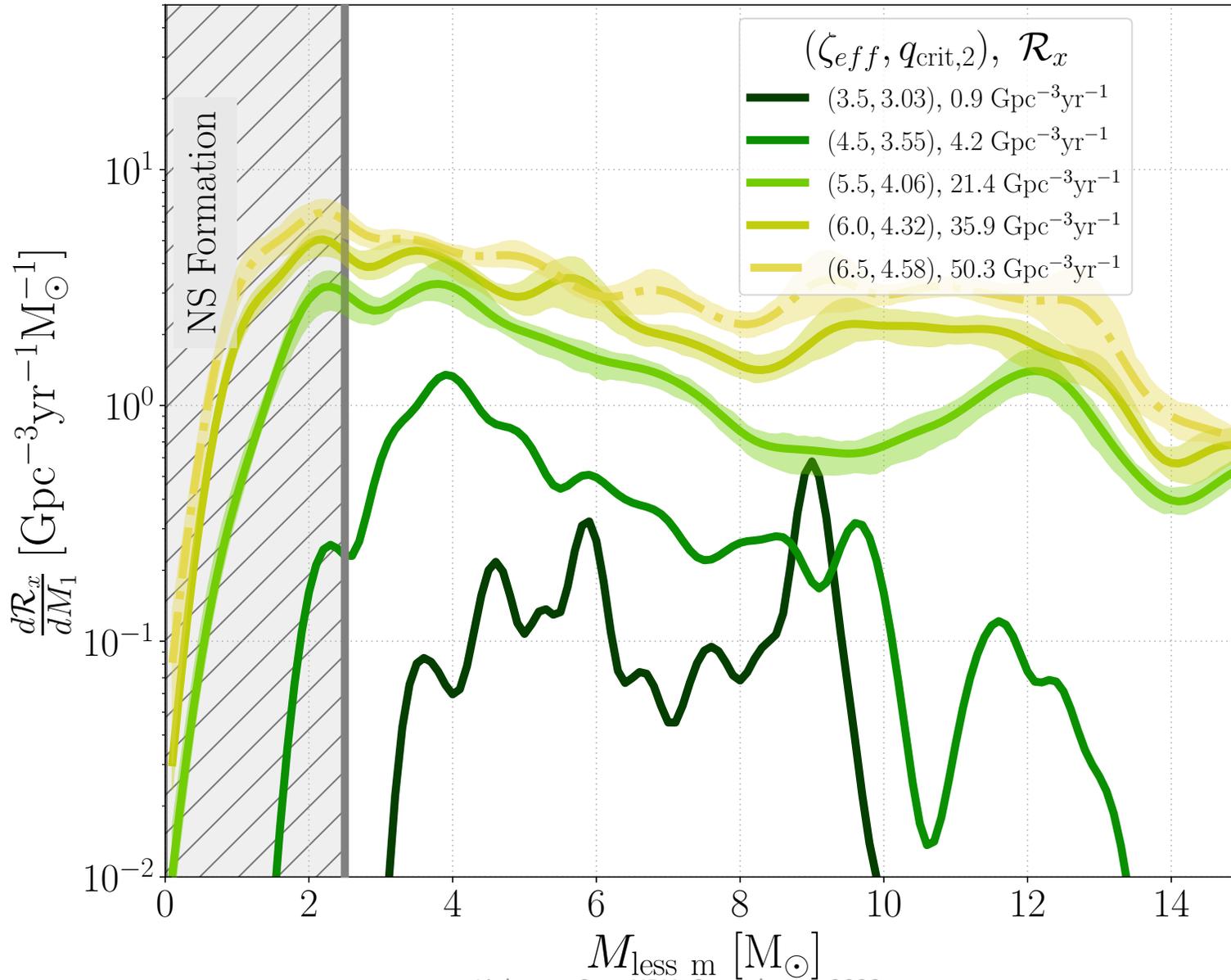


# Less massive component dist

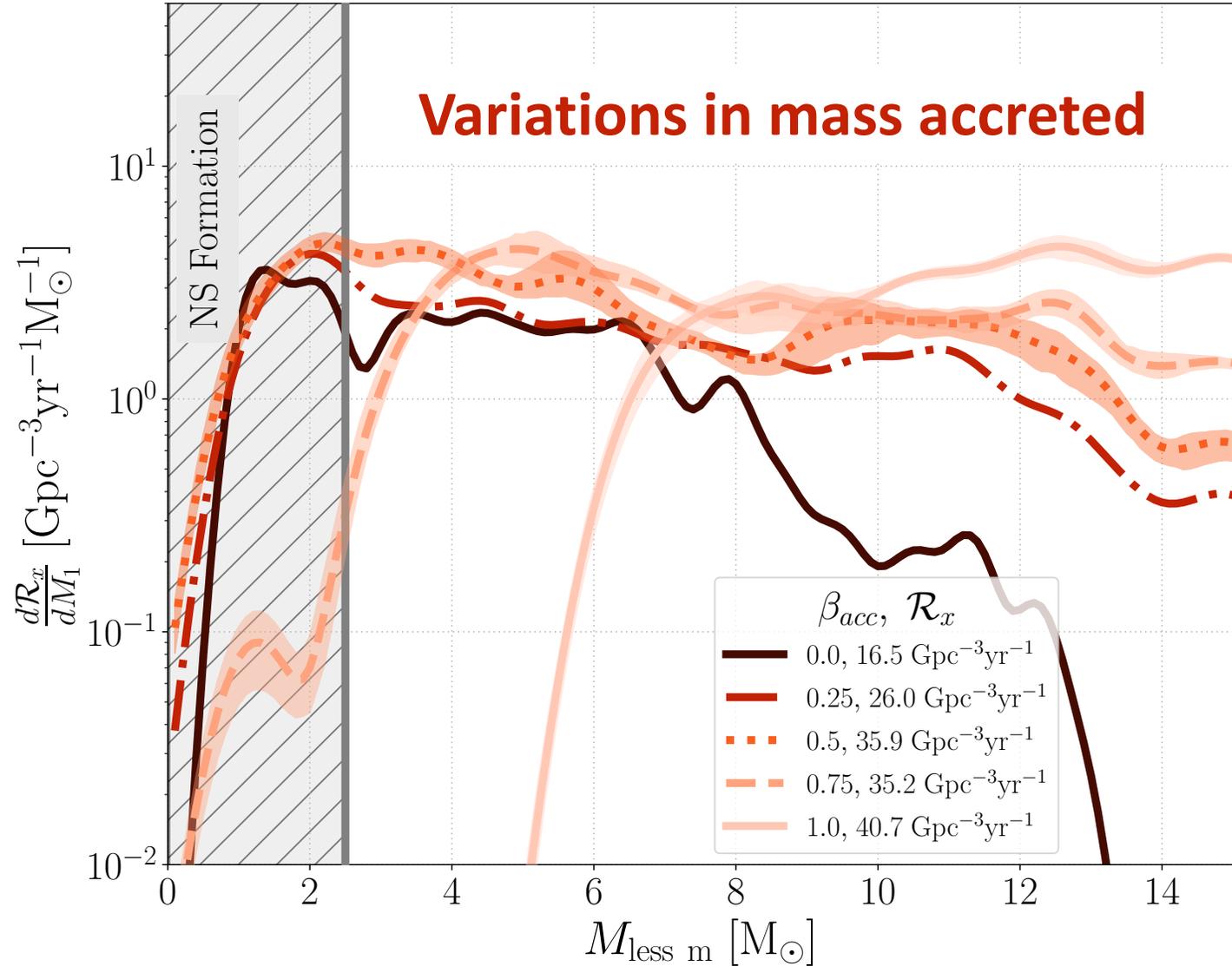


# Less massive component dist

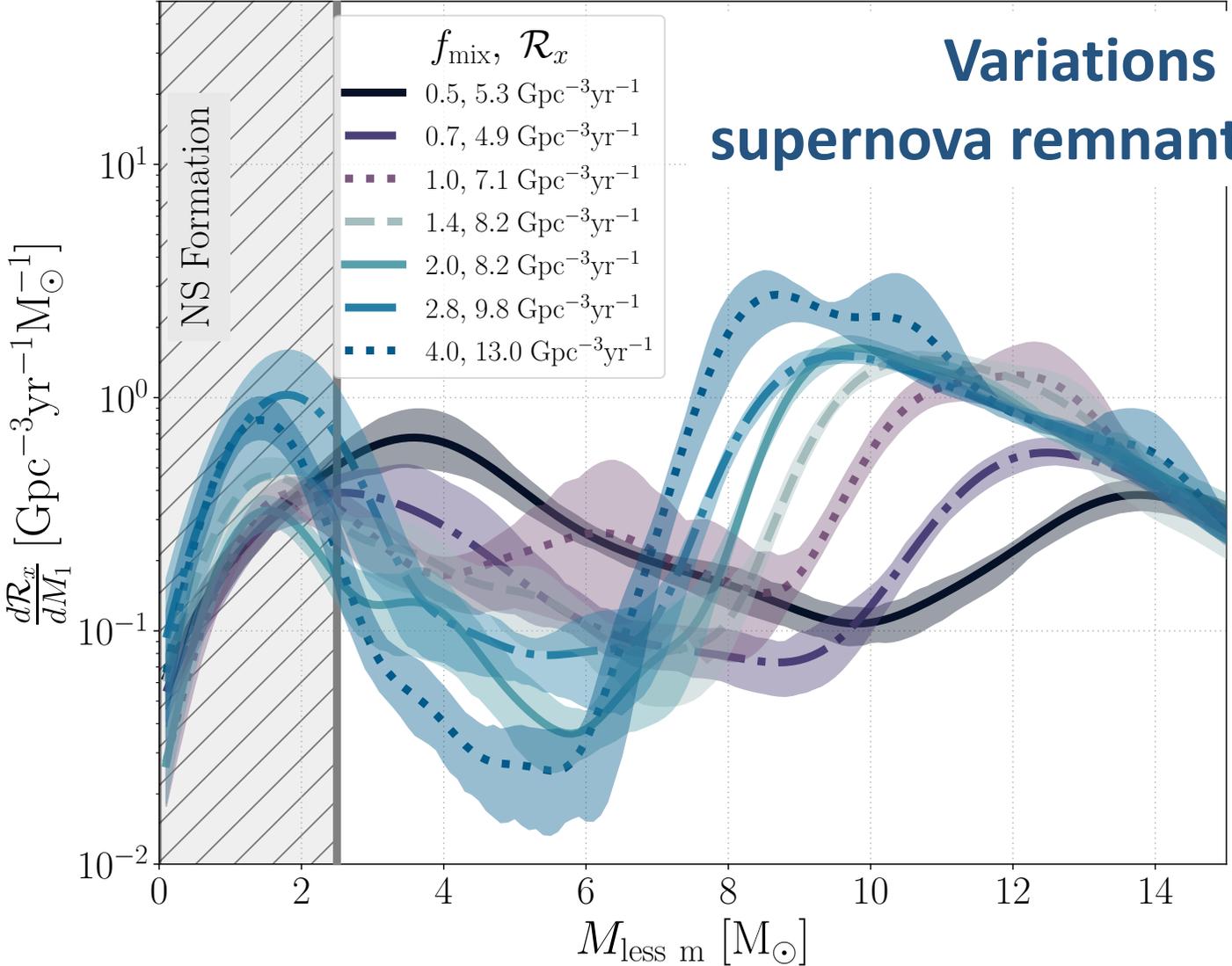
# Variations in mass transfer stability



# Less massive component dist

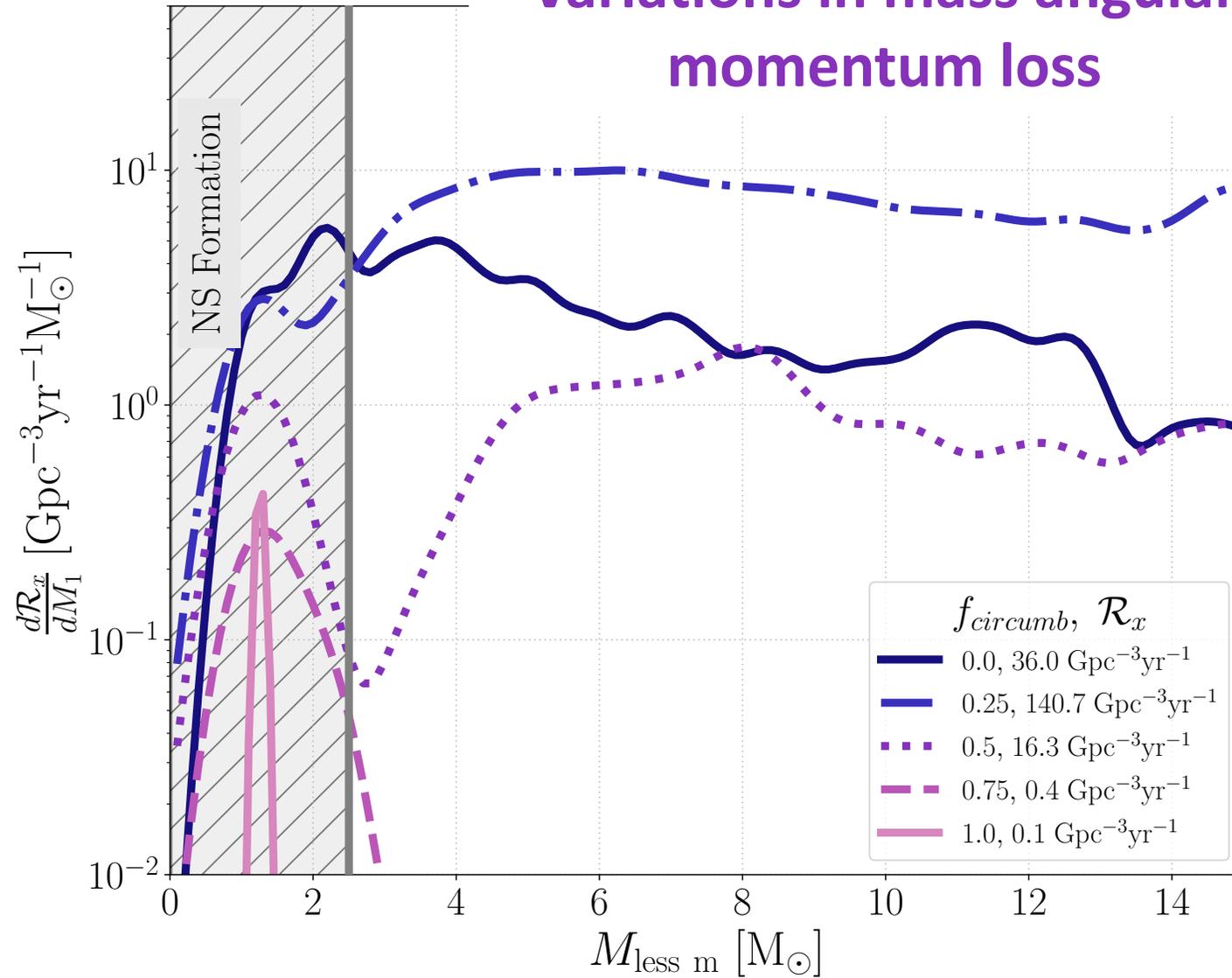


# Less massive component dist

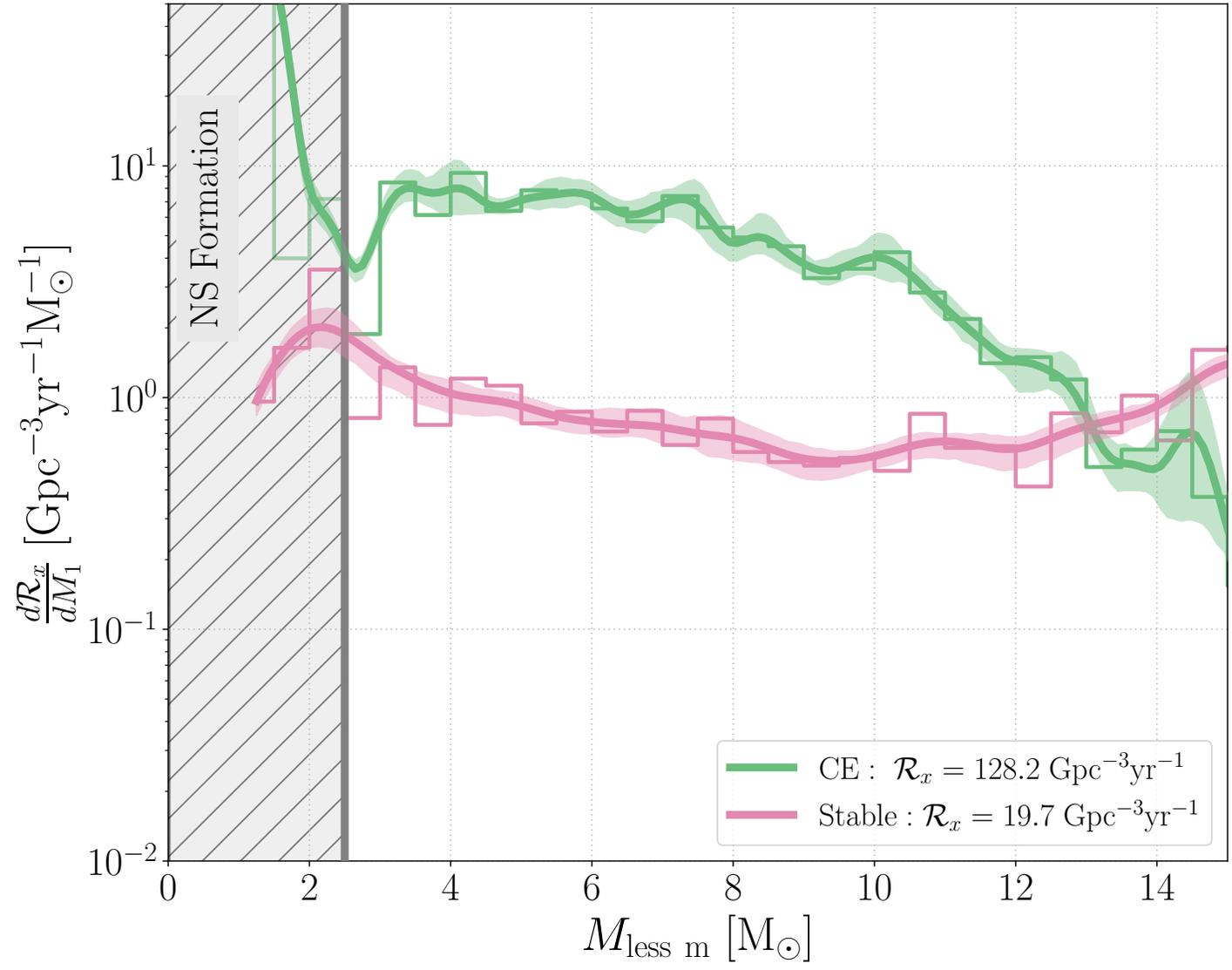


# Less massive component dist

## Variations in mass angular momentum loss



# Less massive component dist



# Evidence against a gap appears to be accumulating:

## Surveys

(OGLE-III): Wyrzykowski & Mandel 2020,  
(NGC 3201): Giesers et al. 2019;

## BH with gap masses

- 2MASS J0521 (RV): Thompson et al. 2019,
- Unicorn & Giraffe: Jayasinghe et al. 2021, 2022
- HD96670 Gomez & Grindlay 2021;
- (HR 6819): Rivinius et al. 2020
- GW190814 (GW): LVK 2020.
- GW190917 (GW): LVK 2020.
- OB110462 (microlensing): Sahu+ 2022, Lam + 2022

... yet recent work that manages  
to get a peak in the mass  
distribution all adopt a gap.

(e.g. Belczynski et al. 2016a; Giacobbo & Mapelli 2018;  
Giacobbo et al. 2018; Wiktorowicz et al. 2019; Belczynski  
et al. 2020. )

Please let me know if you  
know of an exception!



Evolutionary models: Pols 1998 Hurley+2000	Metallicity flat in log distributed $0.0001 < Z < 0.03$	accretion rate $< 10 \text{ tKH}$ accretor (Hurley 2000)
Kroupa IMF (Kroupa 2002)	SN prescription Fryer delayed (Fryer+2012)	Isotropic reemission of lost mass (Soberman et al. 1997)
flat distribution of mass ratios (Kouwenhoven+2005)	Remnant masses (Fryer+2012 and Farmer+ 2019)	CE $\alpha \lambda$ prescription (Webbink 1984, de Kool 1990; Xu & Li 2010a,b)
Öpik distribution of initial separations (i.e. flat in log, Opik 1924)	Stellar winds: Vink et al (2001), Nieuwenhuijzen & de Jager (1990) Kudritzki & Reimers (1978), Vassiliadis & Woods Hamann & Koesterke (1998) + Vink & de Koter 2005,	Adaptive importance sampling (Broekgaarden et al. 2019)  LBV 'eruptions': Hurley et al. (2000)

Team COMPAS, Riley et al. (2021); Stevenson et al. 2017; Vigna-Gomez et al. 2018; Neijssel et al. (2019); Broekgaarden et al. (2019)

<https://compas.science/>

# Implications/discussion points

- The stable channel is bad at:
  - making low mass BHs
  - making NSNS and WDWD

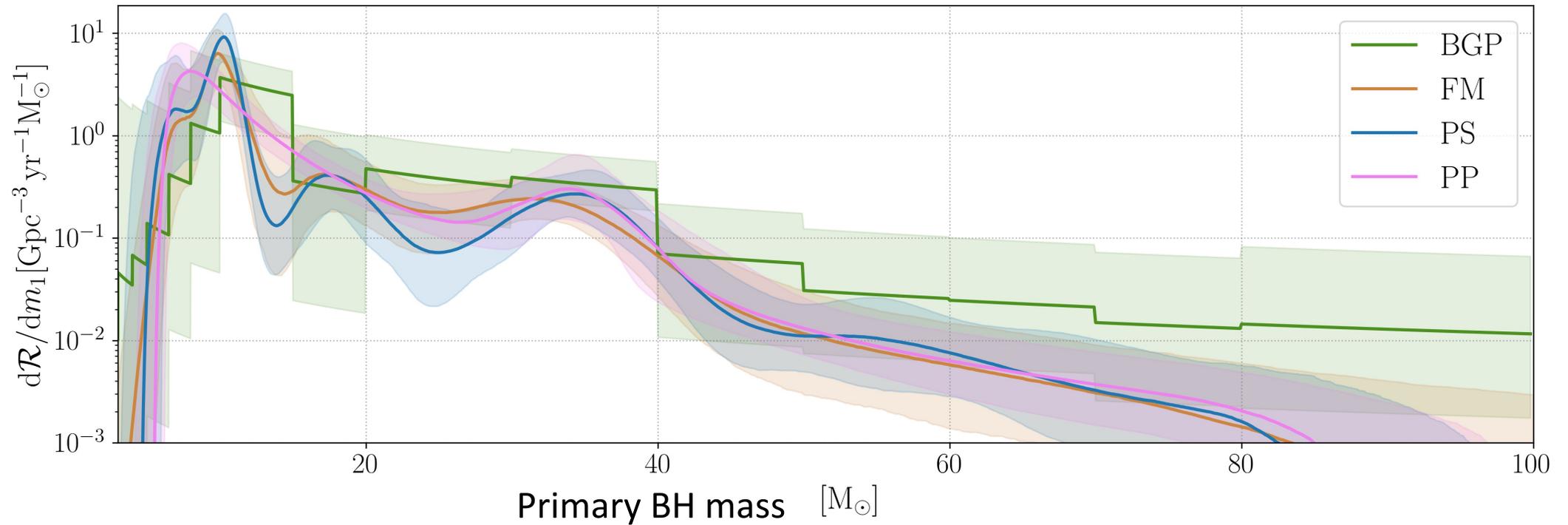


Could look like a NS-BH gap!
- What about X-Ray Binaries?

Different XRB represent different evolutionary states!

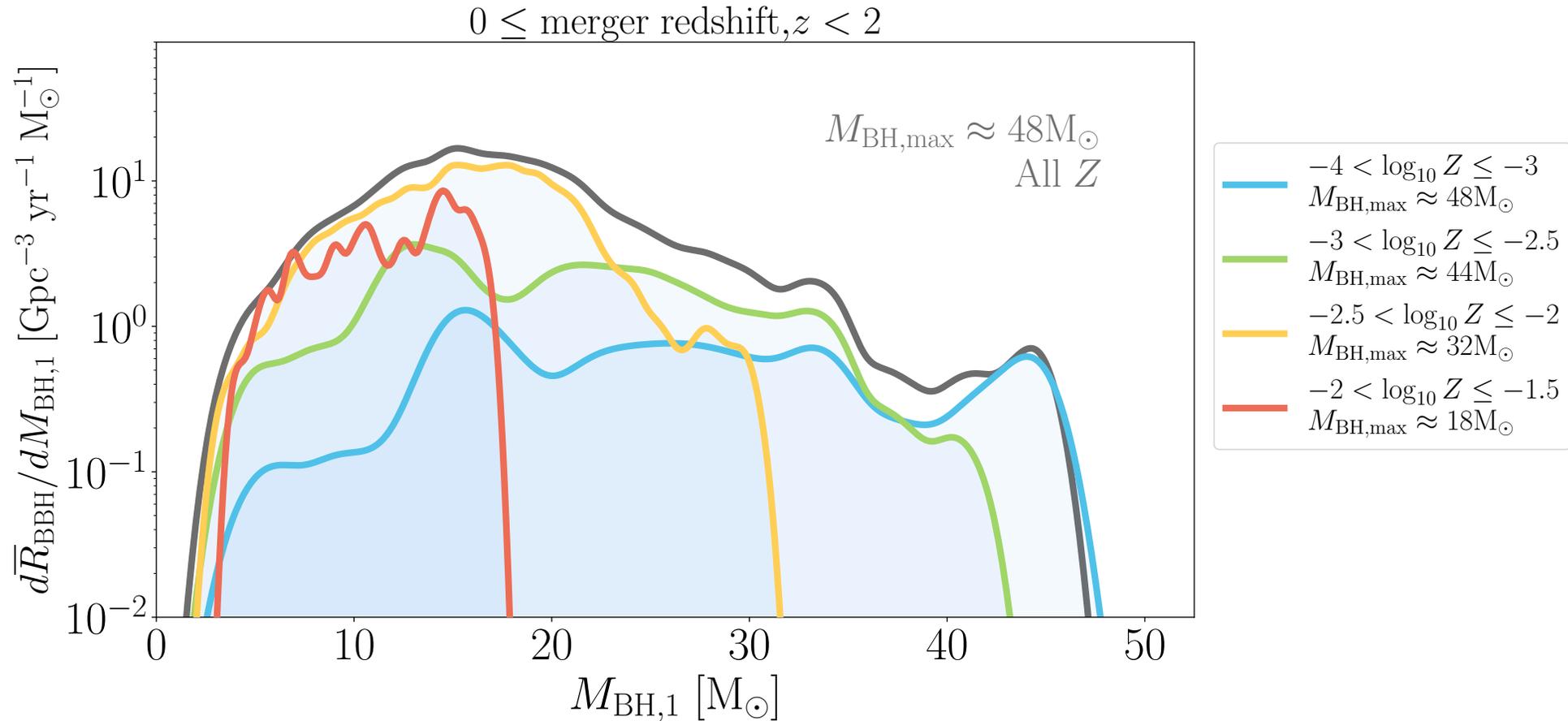
  - In principle this mechanism should apply to post MT XRB (SS433)
  - ‘missing WR X-ray binaries’ (van Beveren et al. 1982; Lommen et al. 2005; van den Heuvel et al. 2017)

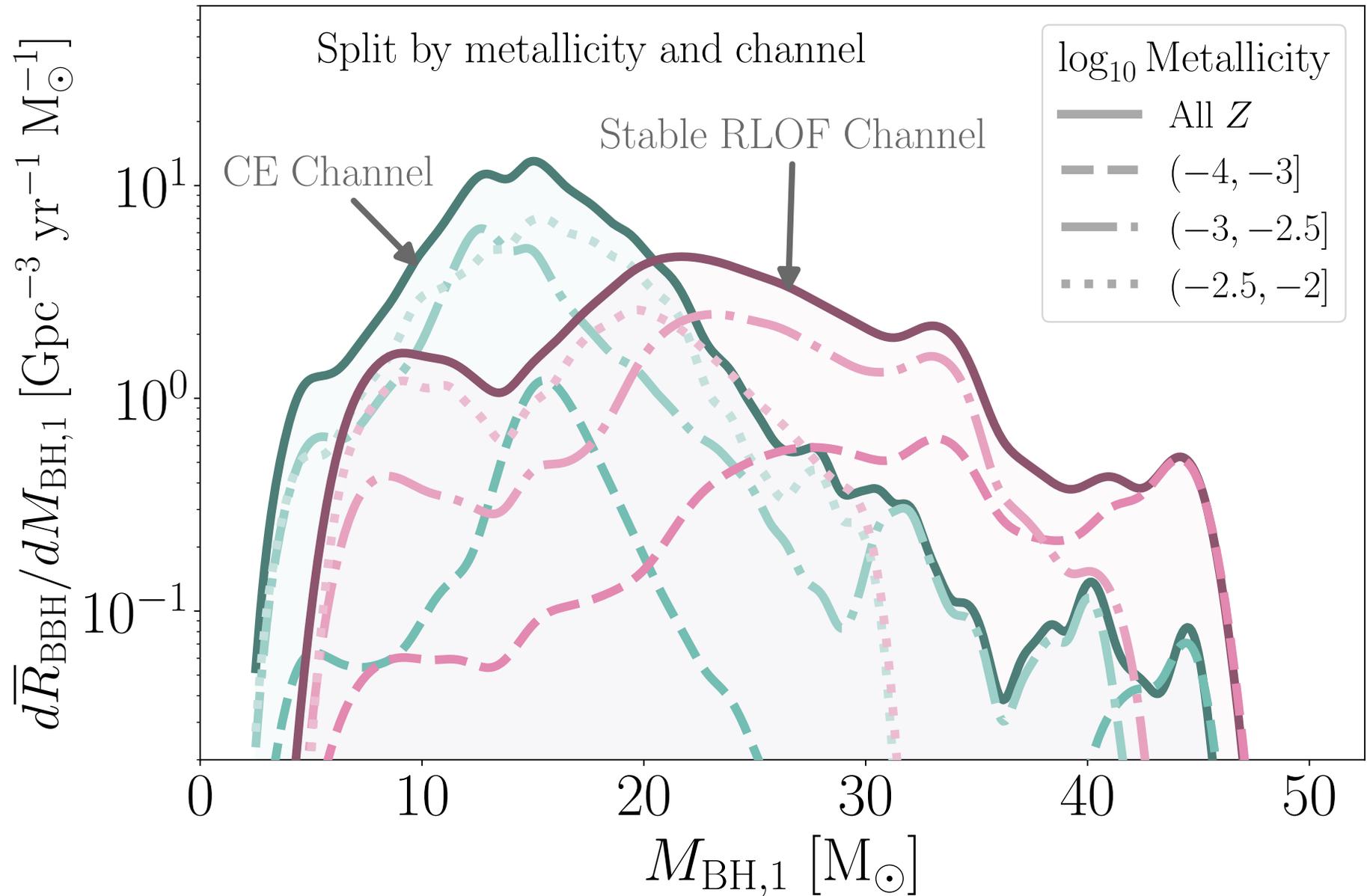
# BBH mass distribution

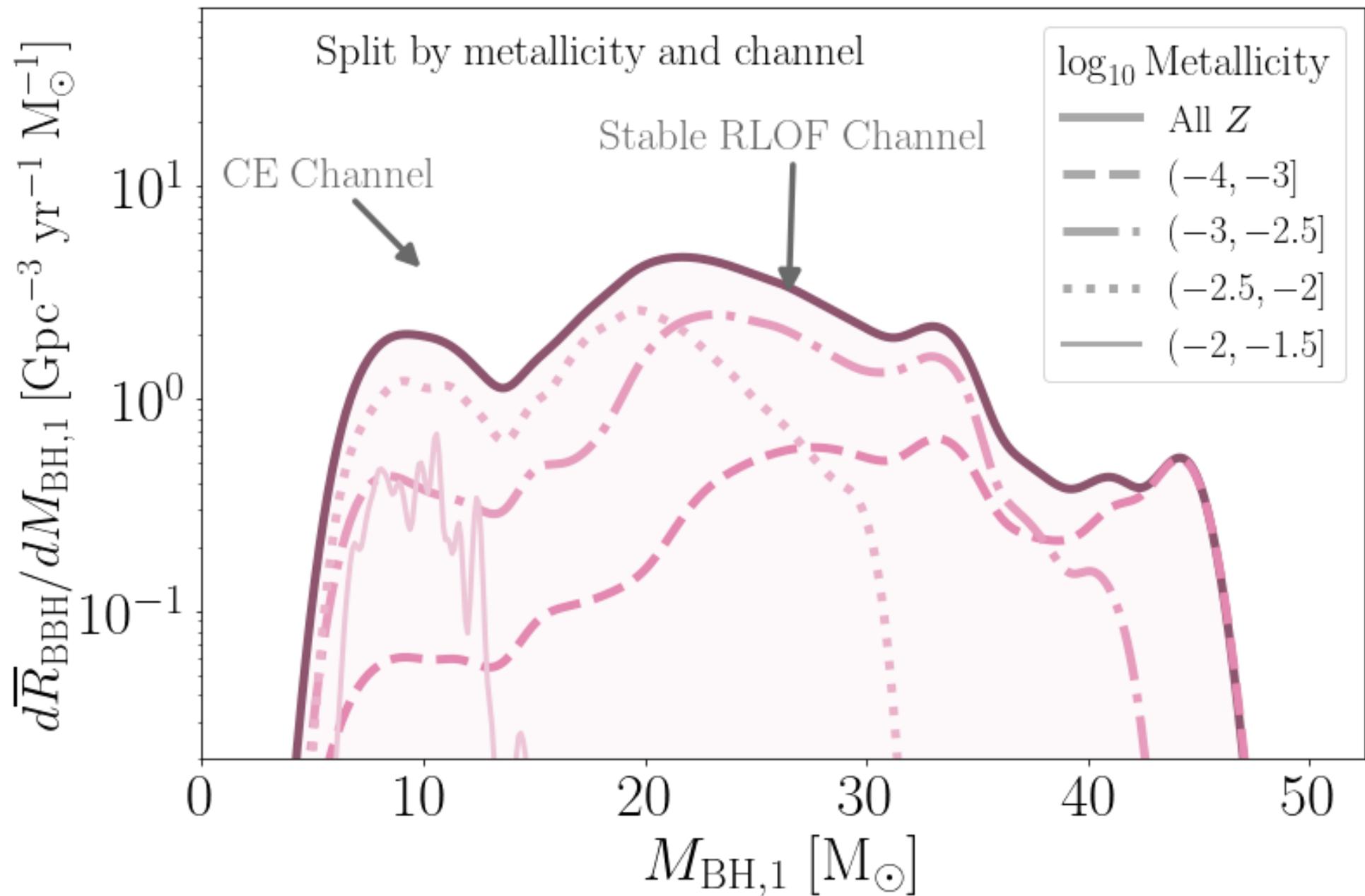


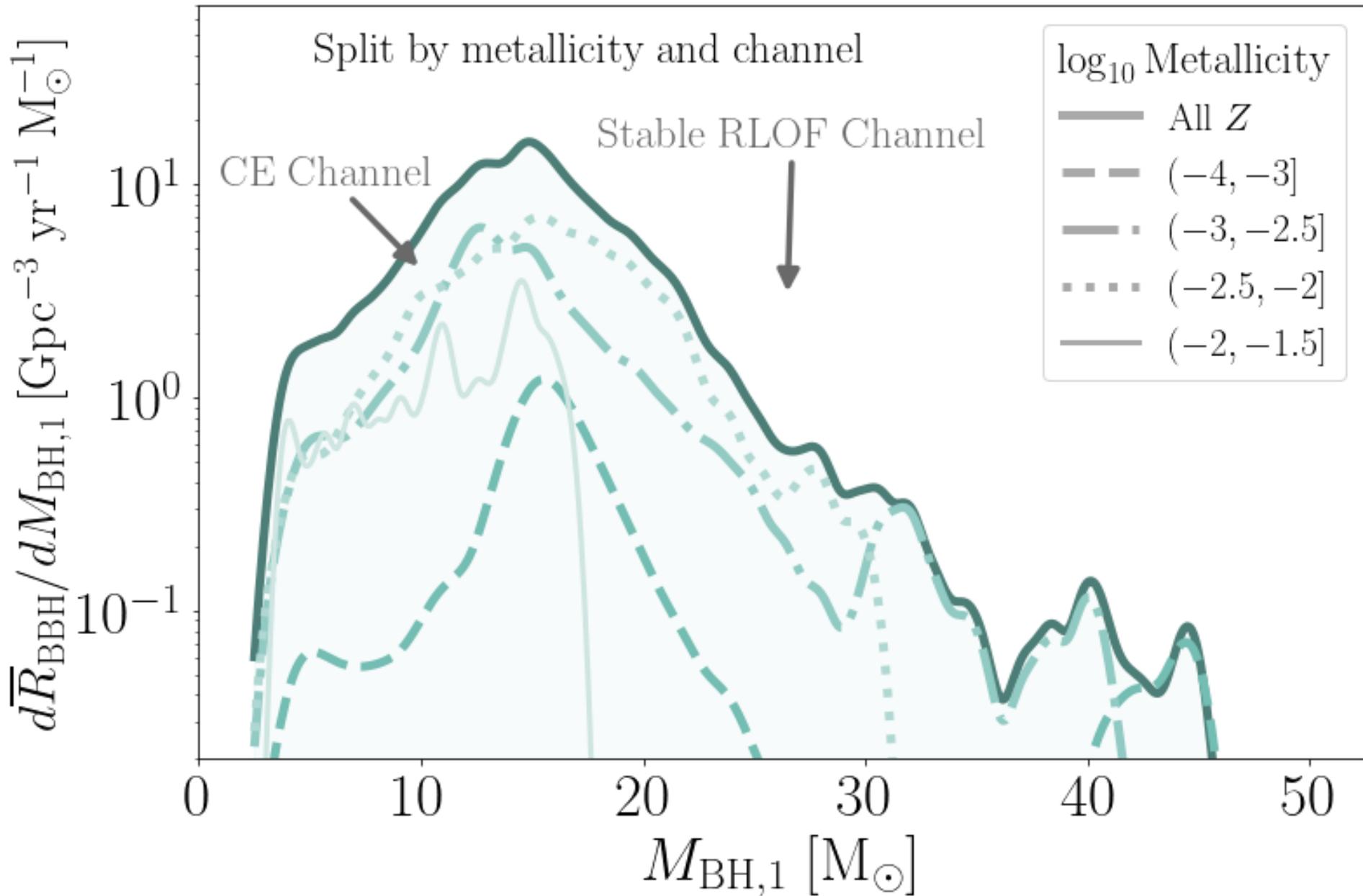
The LVK collaboration, Abbott et al. (2021)

# Metallicity contribution



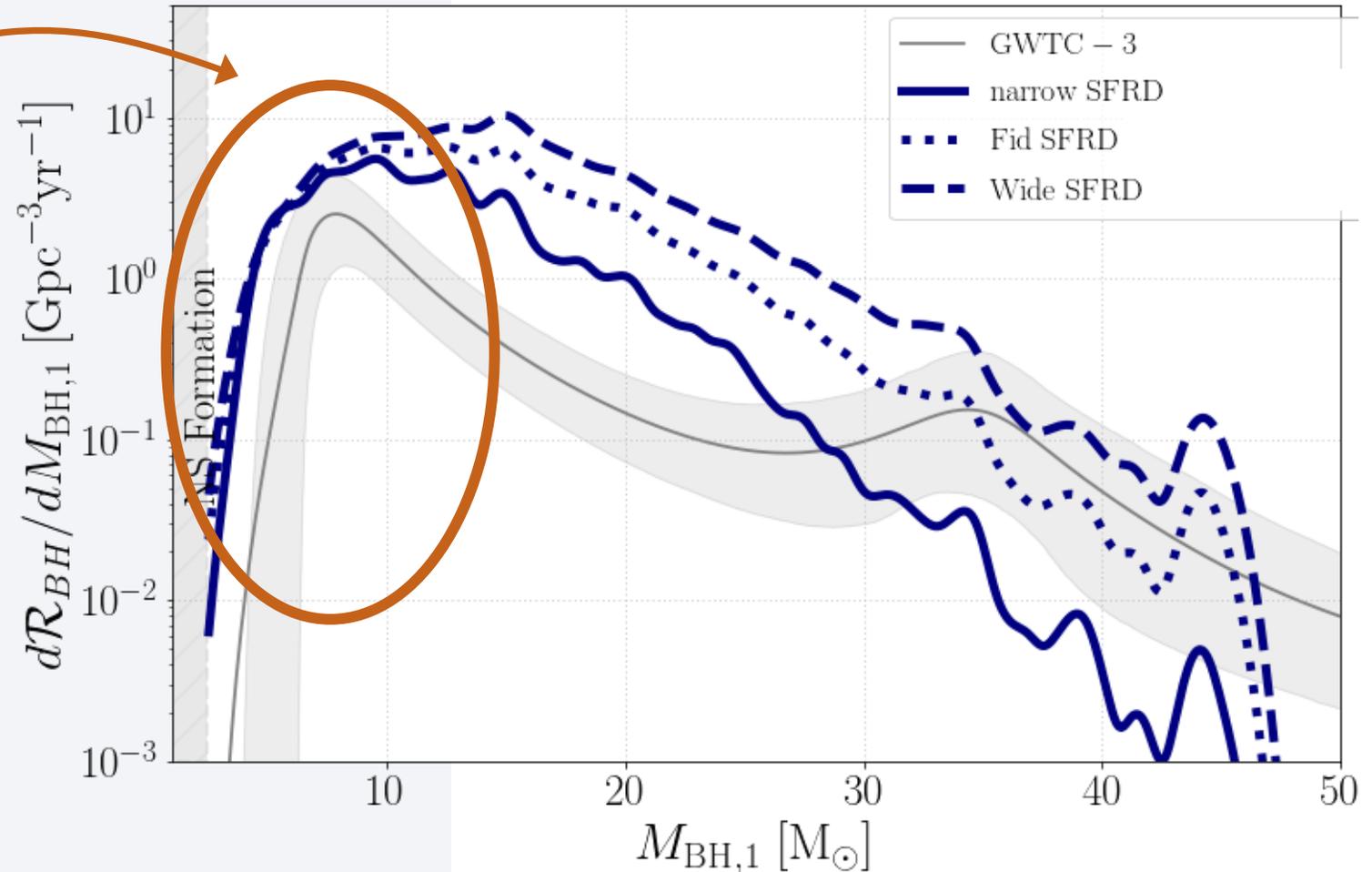






# The low mass end is a great place to start

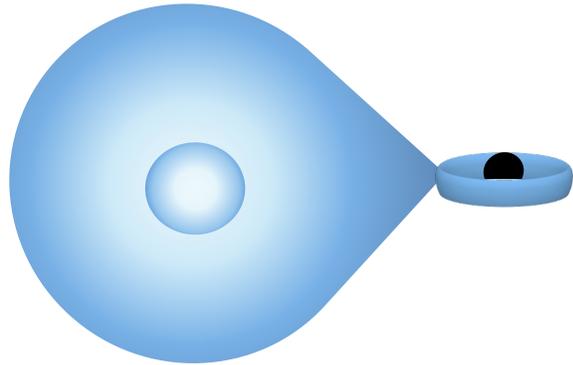
less bothered by  
metallicity dependent  
star formation uncertainty



# What about accretion onto the black hole?

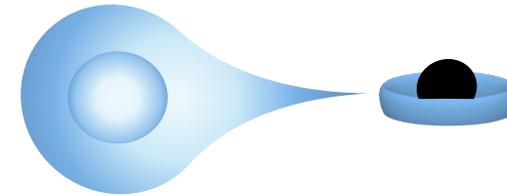
(fully conservative)

$$M_{\text{donor}} > M_{\text{accretor}}$$



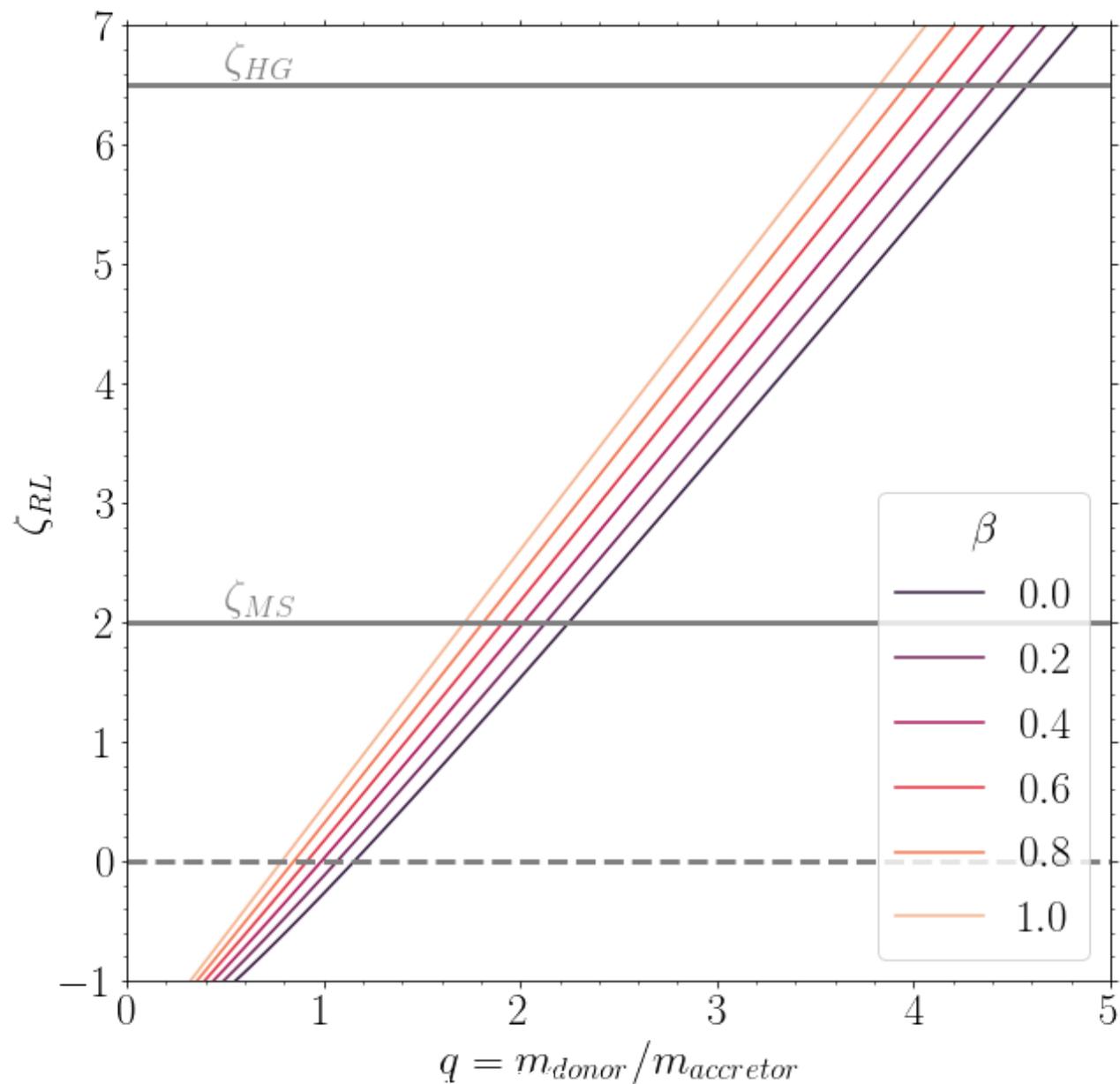
**Orbit shrinks**

$$M_{\text{donor}} < M_{\text{accretor}}$$



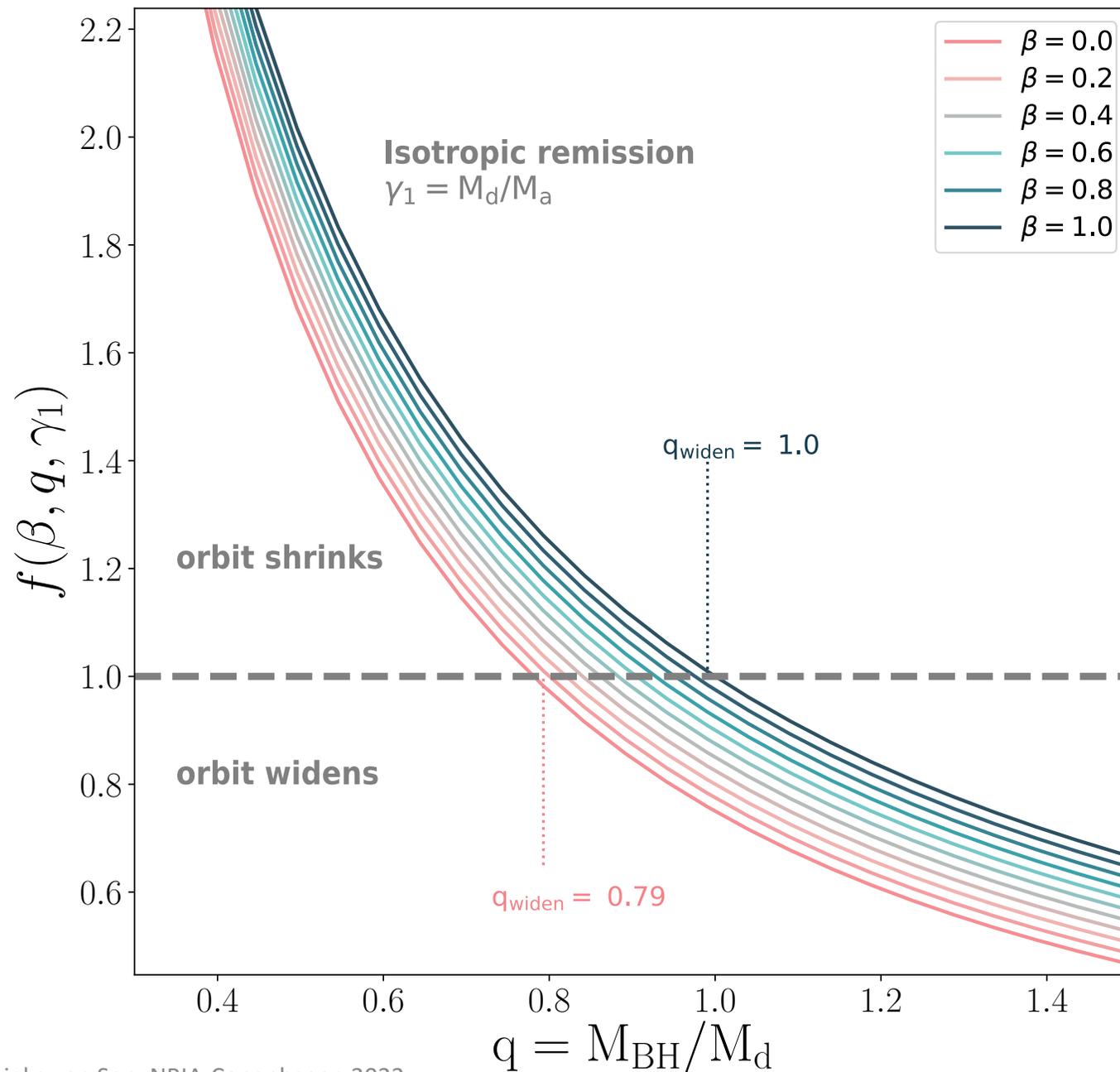
**Orbit widens**

# Mass transfer stability



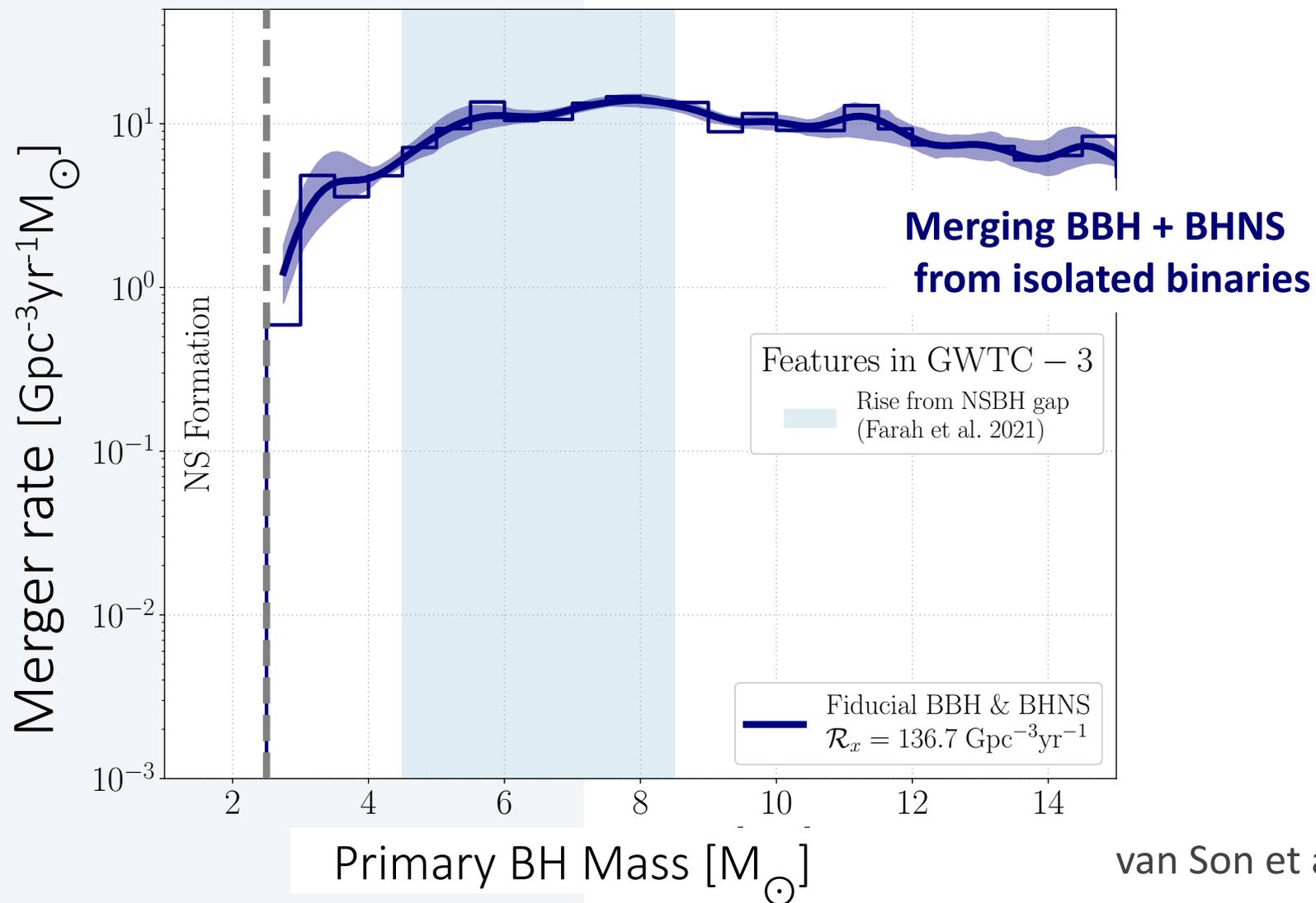
$$\frac{\dot{a}}{a} = -2 \frac{\dot{M}_d}{M_d} \left[ 1 - \beta \frac{M_d}{M_a} - (1 - \beta) \left( \gamma + \frac{1}{2} \right) \frac{M_d}{M_d + M_a} \right]$$

Considering total angular momentum



B)

# What do we expect from isolated binaries?



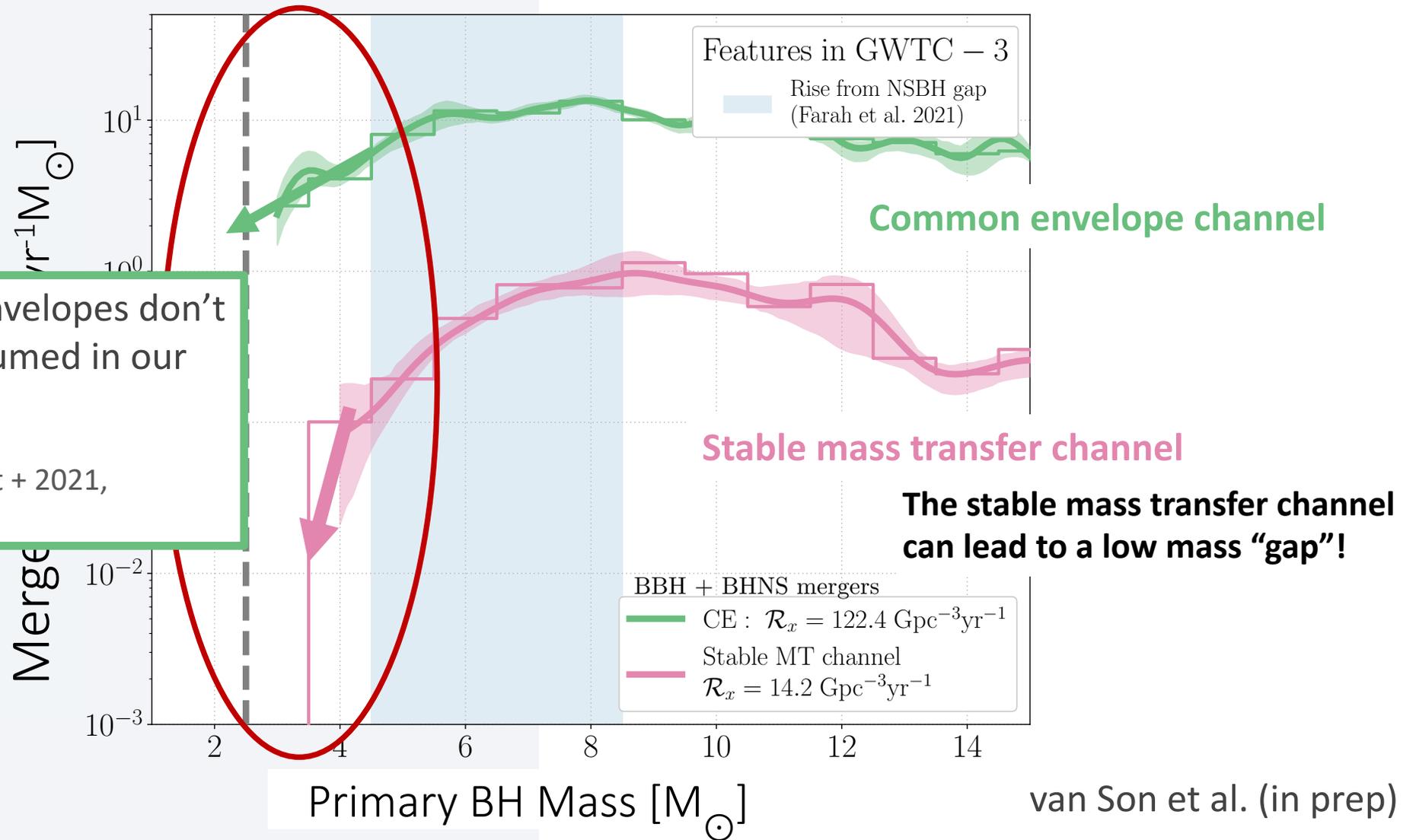
Calculated using



van Son et al. (in prep)

B)

# Let's split isolated binaries into sub-channels

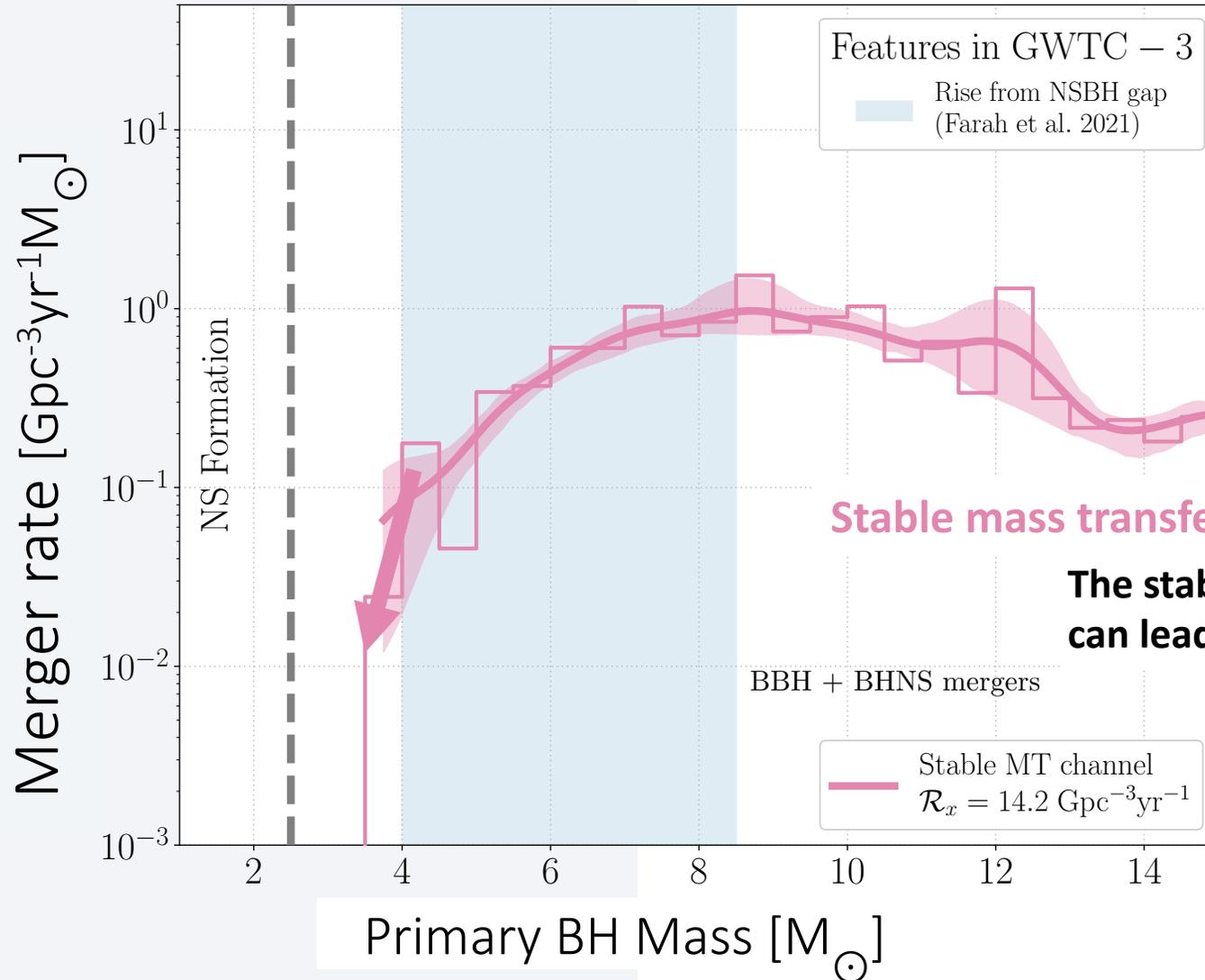


Calculated using



B)

# What does the stable channel predict? BBH + BHNS

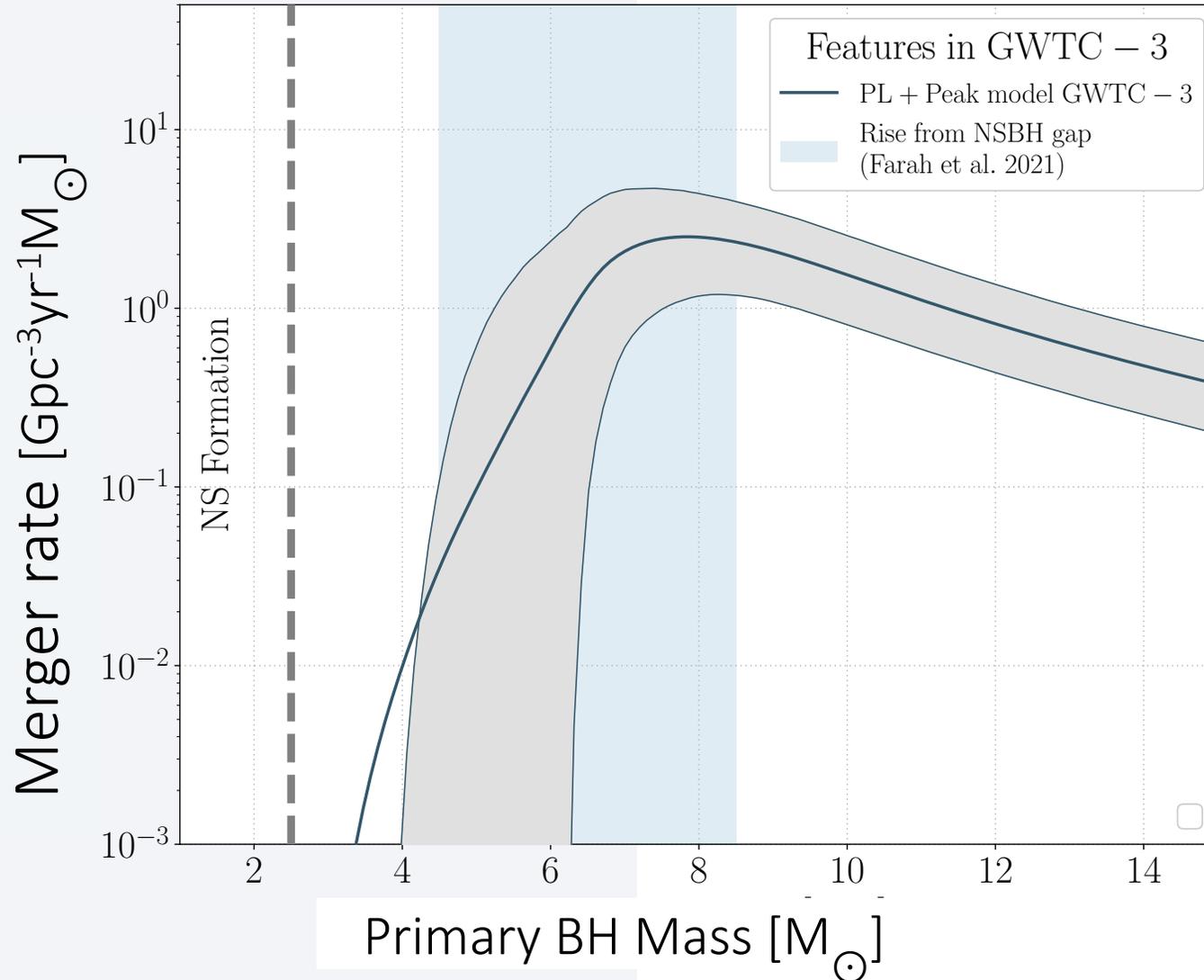


Calculated using



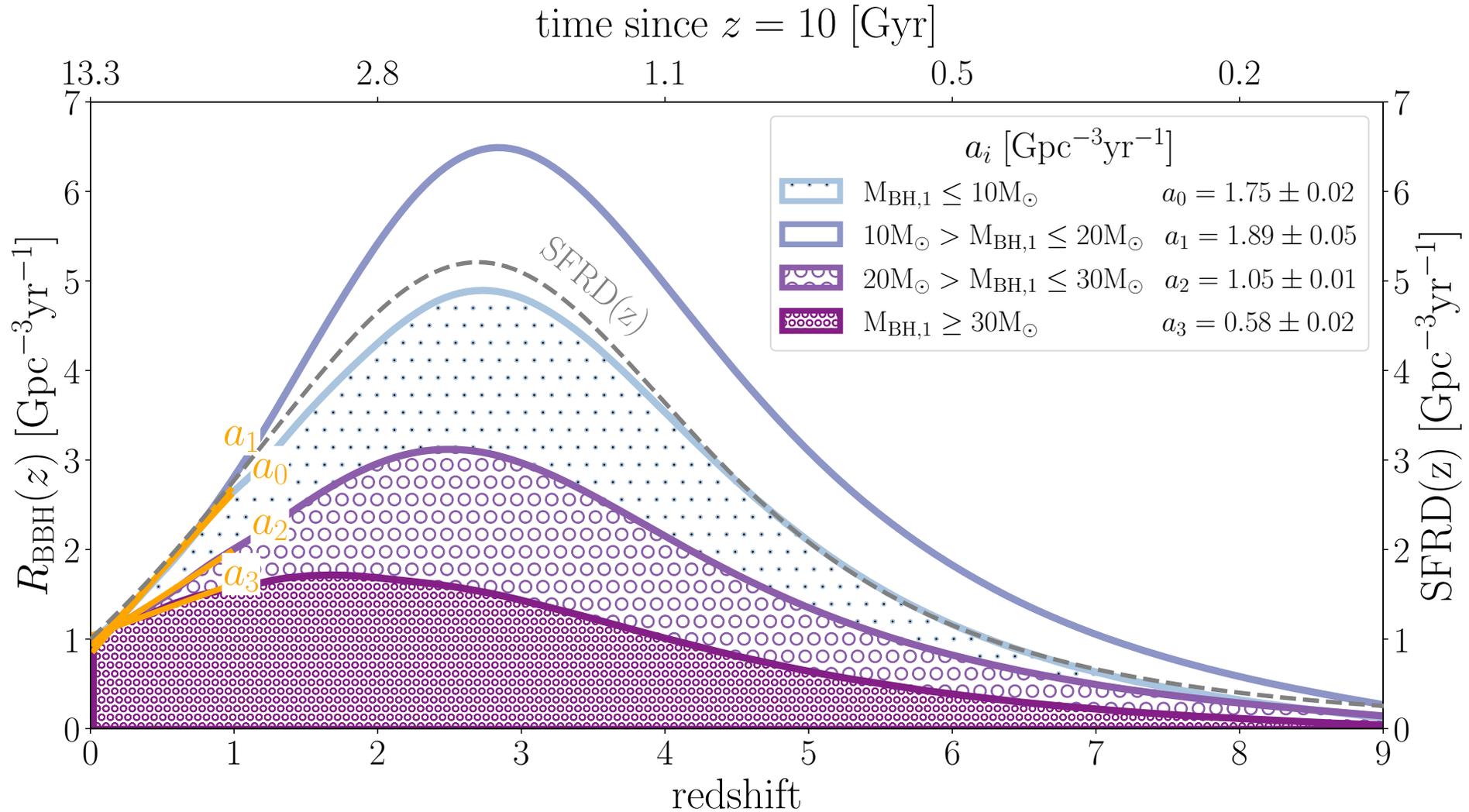
van Son et al. (in prep)

B) The peak at  $8 M_{\odot}$  and a dearth between  $3-5 M_{\odot}$  are two sides of the same coin

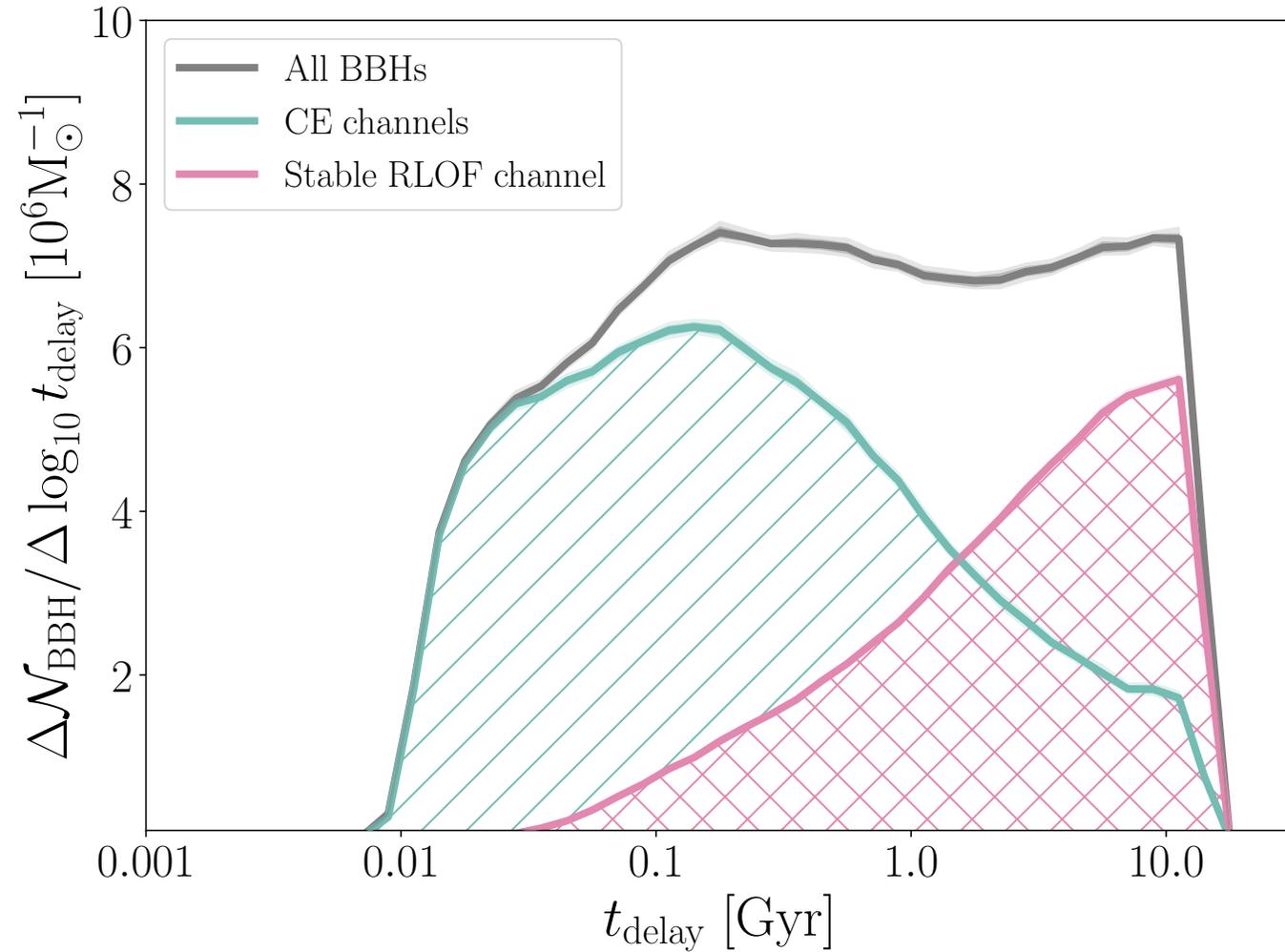


van Son et al. (in prep)

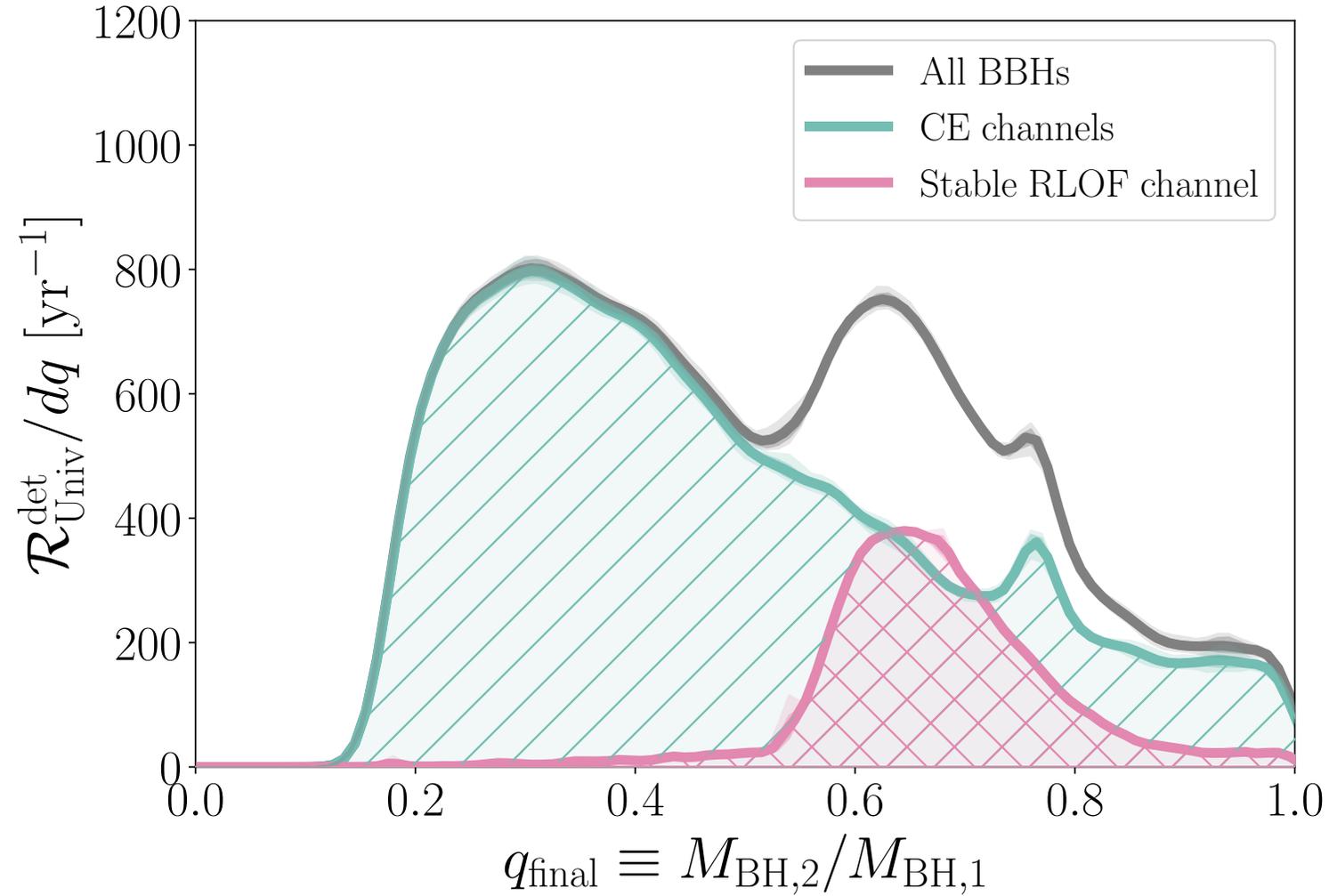
# Rate – redshift evolution



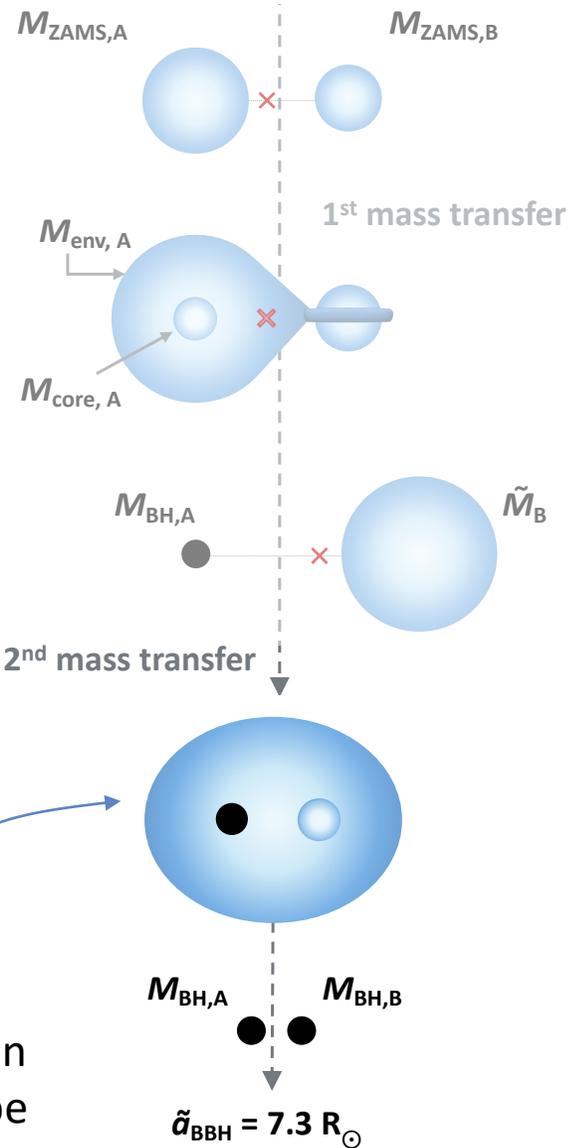
# Delay time distributions



# Final mass ratio



## Common envelope channel



Common envelope

Common envelope channel  $\rightarrow$  lower mass BHs

You need high mass stars ( $> 60M_{\odot}$ ) for high mass BHs ( $> 30M_{\odot}$ )

These stars:

- I. **Don't have much of an envelope**  
- due to wind stripping
- II. **Don't like to engage in a common envelope** (unstable mass transfer)  
- radiative envelopes contract when losing mass
- III. **Are unlikely to survive a common envelope event**  
- too hot!
- IV. **Reverse CE is unlikely**  
- due to accretion from first mass transfer

- I) LBV e.g. Smith 2014; Sanyal et al. 2017; Kalari et al. 2018; Davies et al. 2018; Higgins & Vink 2020; Sabhahit et al. 2021; Gilkiset al. 2021,  
 $\rightarrow$  no RLOF: Mennekens & Vanbeveren + 2014; Belczynski + 2016, deMink et al. 2008;
- II) Hjellming & Webbink 1987, : Pavlovskii & Ivanova 2015; Pavlovskii et al. 2017; Marchant + 2021; Klencki et al. 2020  
Lieke van Son, NBIA-Copenhagen 2022
- III) Convective envelope needed: Klencki + 2020, 2021; Marchant + 2021; Monica Gallegos-Garcia + 2021

## Stable RLOF channel → long delay times

Stable RLOF leads to **wider separations**

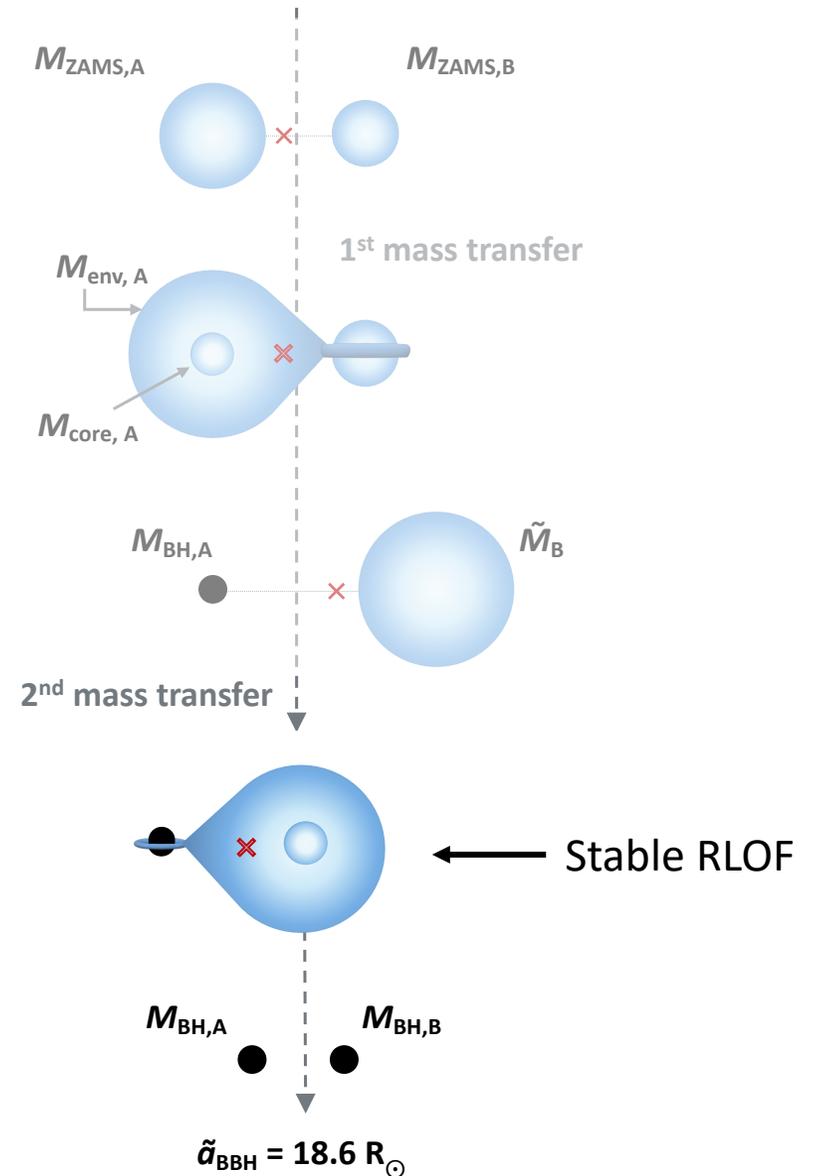
→ Longer delay time

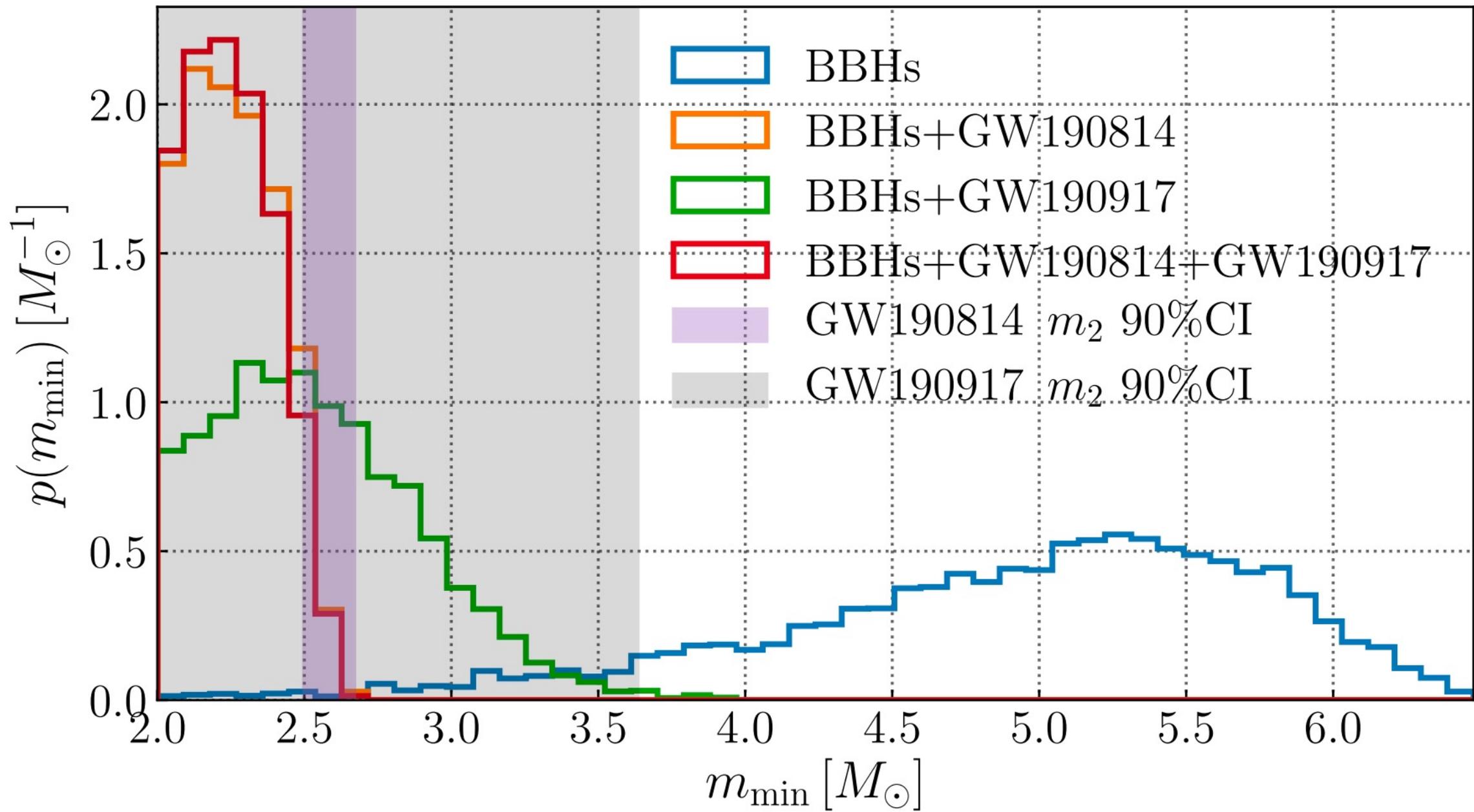
$$T_c(a_0) = a_0^4 / (4\beta)$$

$$\beta = \frac{64 G^3 m_1 m_2 (m_1 + m_2)}{5 c^5}$$

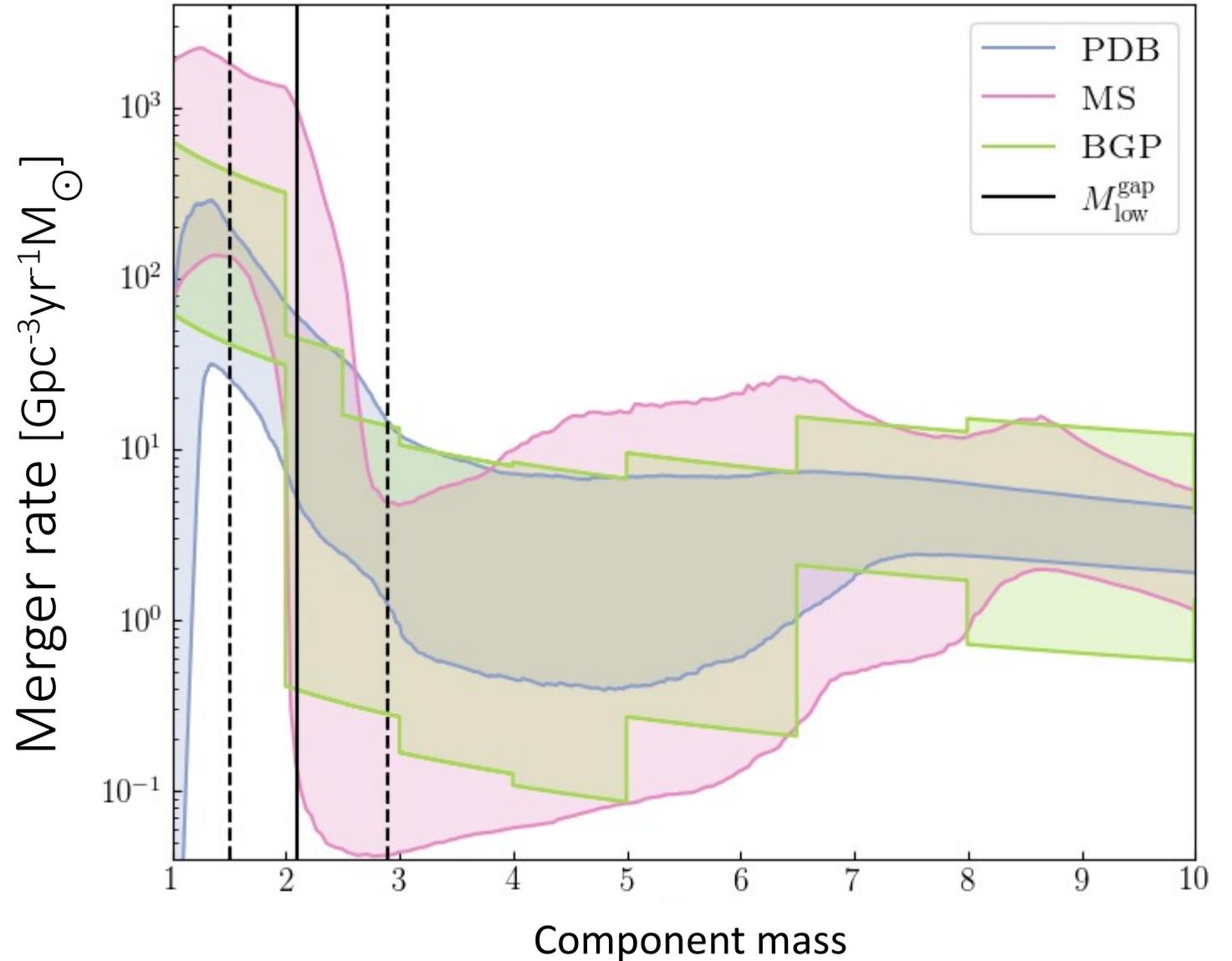
Peters (1964) Orbital evolution: Soberman et al. 1997

## Stable RLOF channel



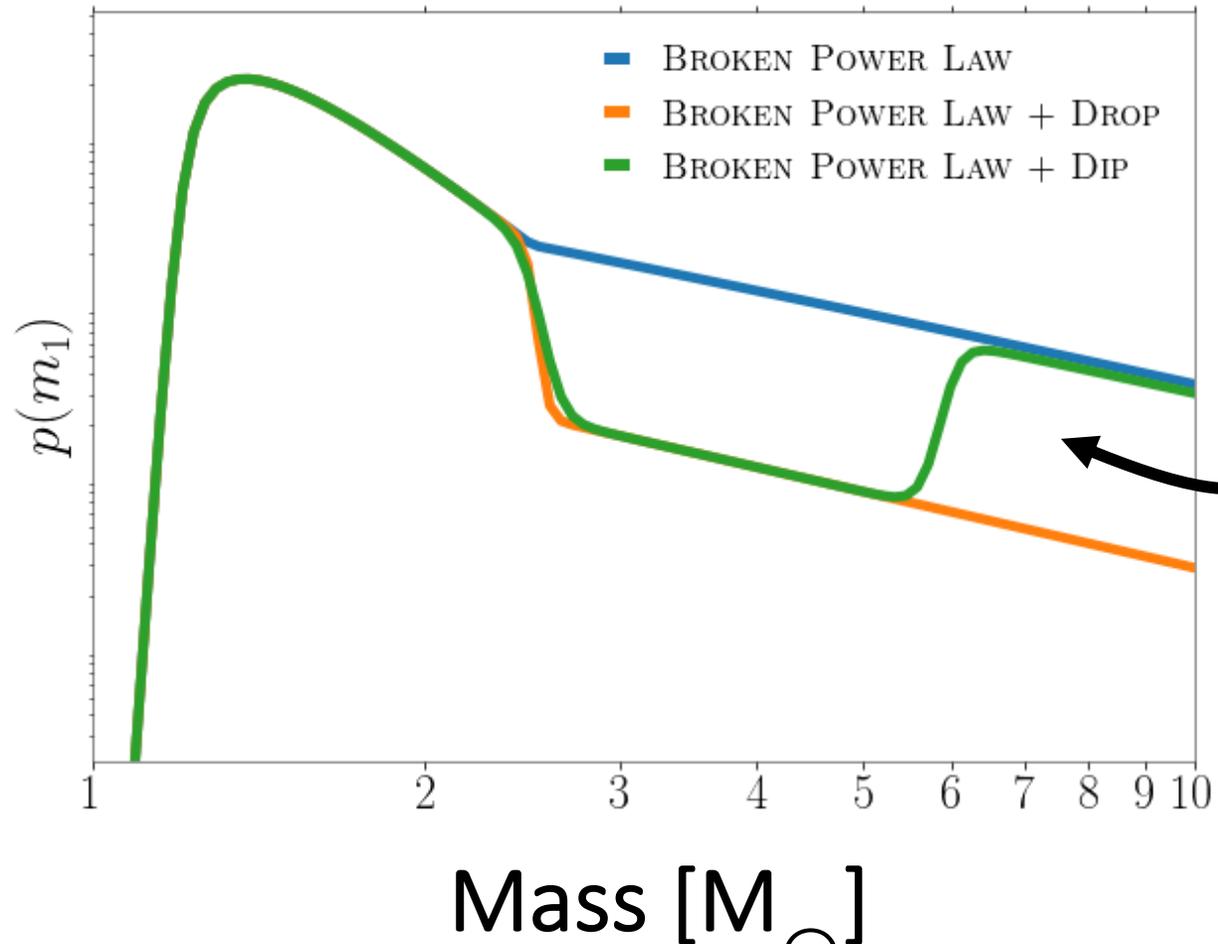


# Mass distribution from LIGO

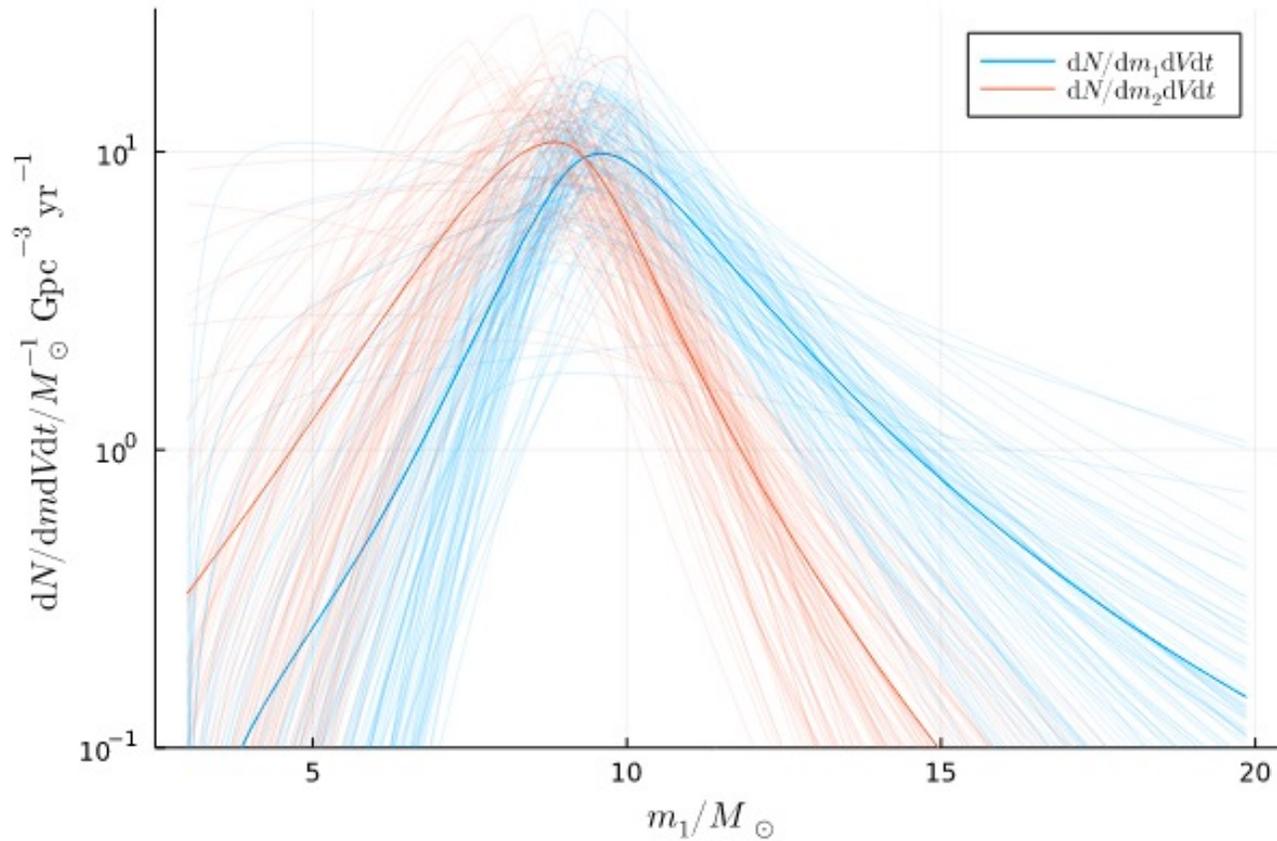


# Does the data prefer a drop below $7M_{\odot}$ or not?

Farah et al. 2021



# Does the data prefer a drop below $7 M_{\odot}$ or not?



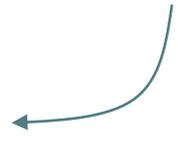
# Derivation of minimum BH mass (part I)

$$q_{\text{preMT},2} = \frac{\tilde{M}_2}{M_{\text{BH},1}} \leq q_{\text{crit},2}. \quad (1)$$


$$\tilde{M}_2 \approx M_{\text{ZAMS},2} + M_{\text{ZAMS},1} \cdot \beta_{\text{acc}}(1 - f_{\text{core},1}), \quad (2)$$

and  $M_{\text{BH},1}$  as,

$$M_{\text{BH},1} = f_{\text{core},1} \cdot M_{\text{ZAMS},1} - dM_{\text{SN},1}, \quad (3)$$

$$\frac{q_{\text{ZAMS}} + \beta_{\text{acc}}(1 - f_{\text{core},1})}{f_{\text{core},1} - \frac{dM_{\text{SN},1}}{M_{\text{ZAMS},1}}} \leq q_{\text{crit},2} \quad (4)$$


# Derivation of minimum BH mass (part I)

$$\frac{q_{\text{crit},2} f_{\text{core},1} - \beta_{\text{acc}}(1 - f_{\text{core},1}) - q_{\text{ZAMS}}}{q_{\text{crit},2}} \geq \frac{dM_{\text{SN},1}}{M_{\text{ZAMS},1}}$$

$$dM_{\text{SN}}(M_{\text{core}}) = \begin{cases} a_{sn} M_{\text{core}} + b_{sn} & M_{\text{core}} \leq M_{\text{thresh}} \\ 0 & M_{\text{core}} > M_{\text{thresh}} \end{cases} \quad (5)$$

$$M_{\text{ZAMS},1} \geq \frac{b_{sn} \cdot q_{\text{crit},2}}{q_{\text{crit},2} f_{\text{core},1} (1 - a_{sn}) - \beta_{\text{acc}}(1 - f_{\text{core},1}) - q_{\text{ZAMS}}}$$

# Derivation of minimum BH mass (part II)

$$\min(M_{\text{BH},1}) \approx f_{\text{core},1} \cdot \min(M_{\text{ZAMS},1}) - dM_{\text{SN},1} \quad (11)$$

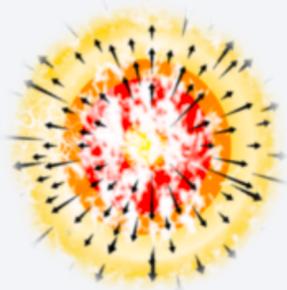
$$\min(M_{\text{BH},2}) \approx f_{\text{core},2} \cdot \min(\tilde{M}_2) - dM_{\text{SN},2} \quad (12)$$

$$\min(\tilde{M}_2) = q_{\text{crit},2} \min(M_{\text{BH},1}).$$

$$\min(M_{\text{m.mass BH}}) = \max \{ \min(M_{\text{BH},1}), \min(M_{\text{BH},2}) \}$$

# Isolated binaries don't make BHs with $\sim 45-140 M_{\odot}$

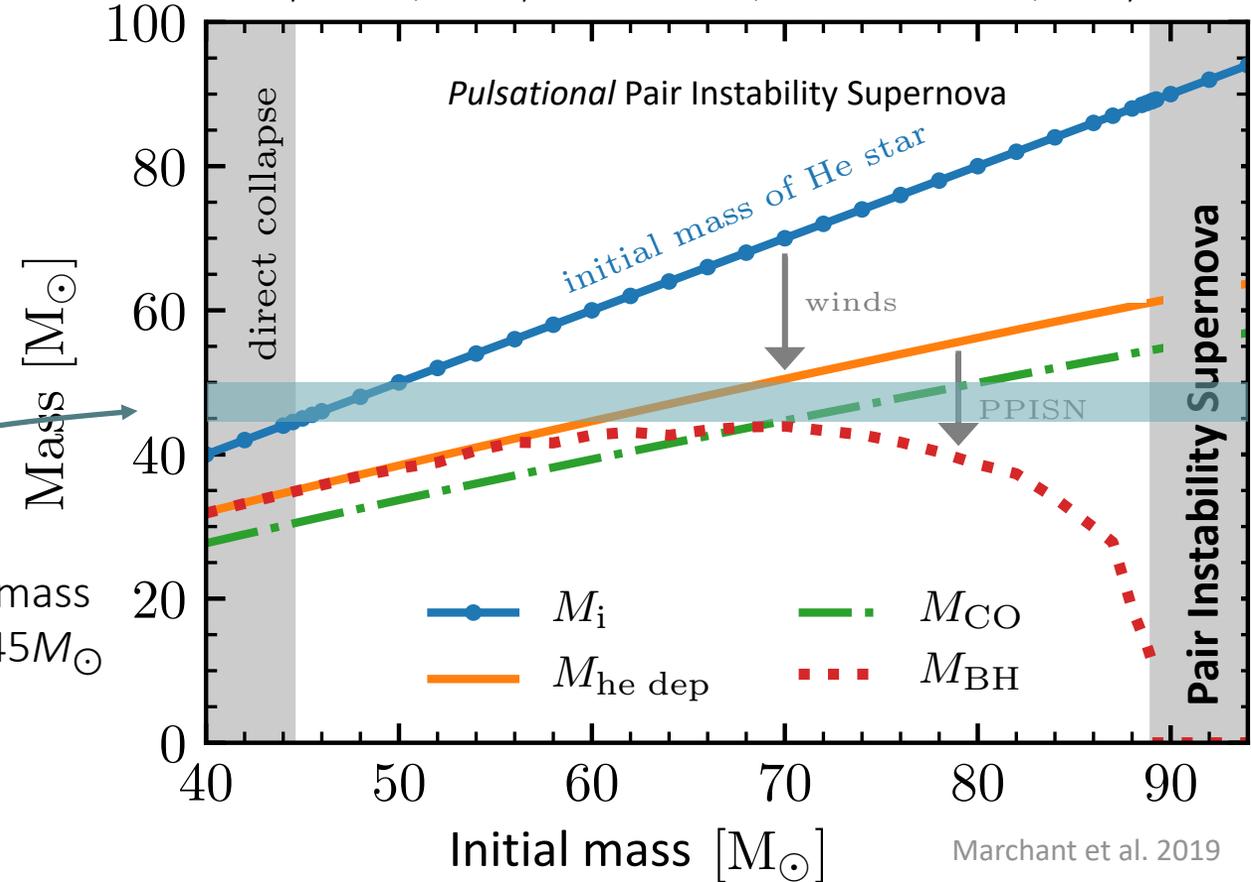
## Pair-instability Supernovae



(Renzo et al. 2020)

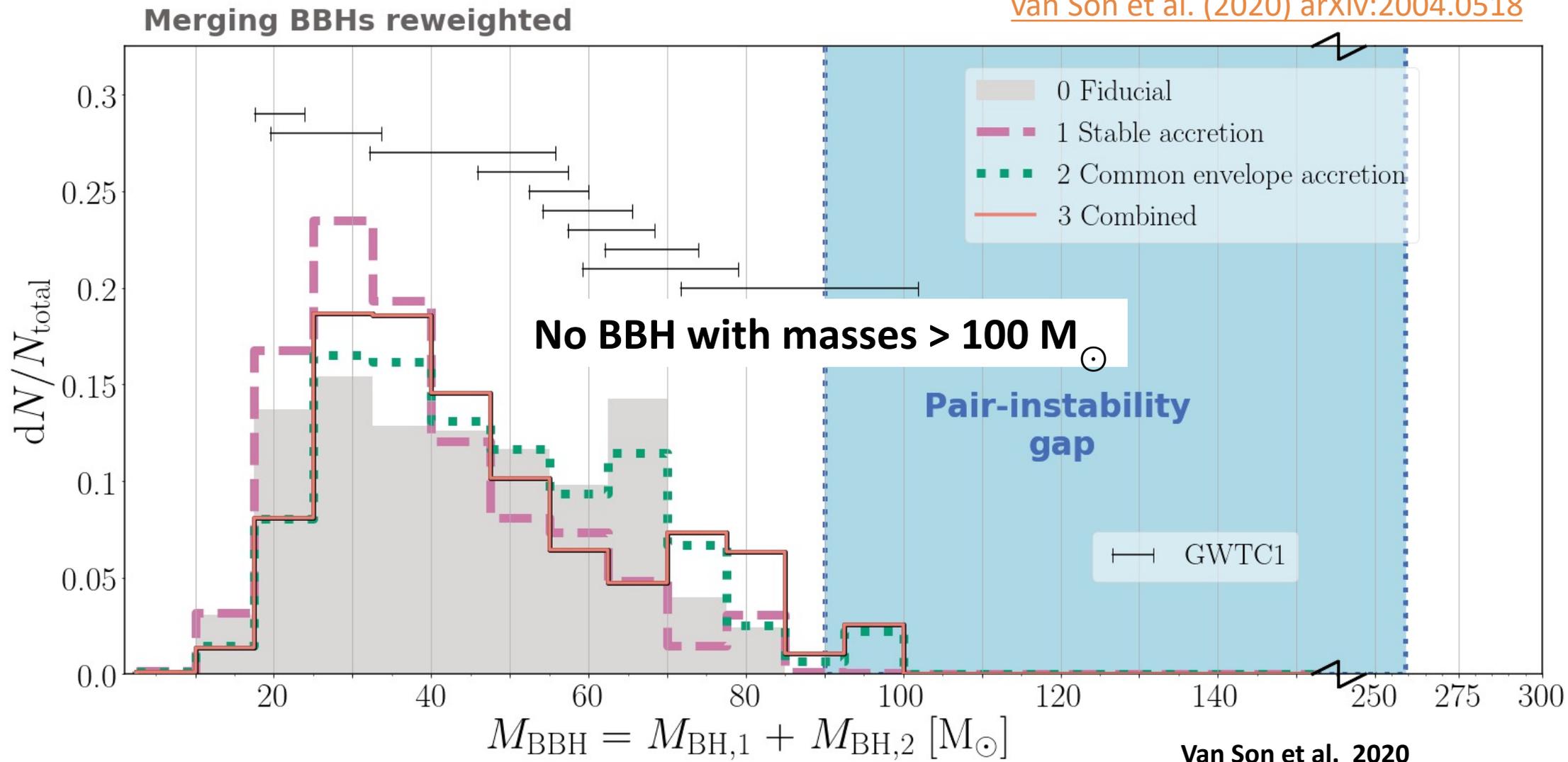
Max BH mass  
around  $45 M_{\odot}$

PISN: Fowler & Hoyle 1964; Rakavy & Shaviv 1967; Barkat et al. 1967; Fraley 1968

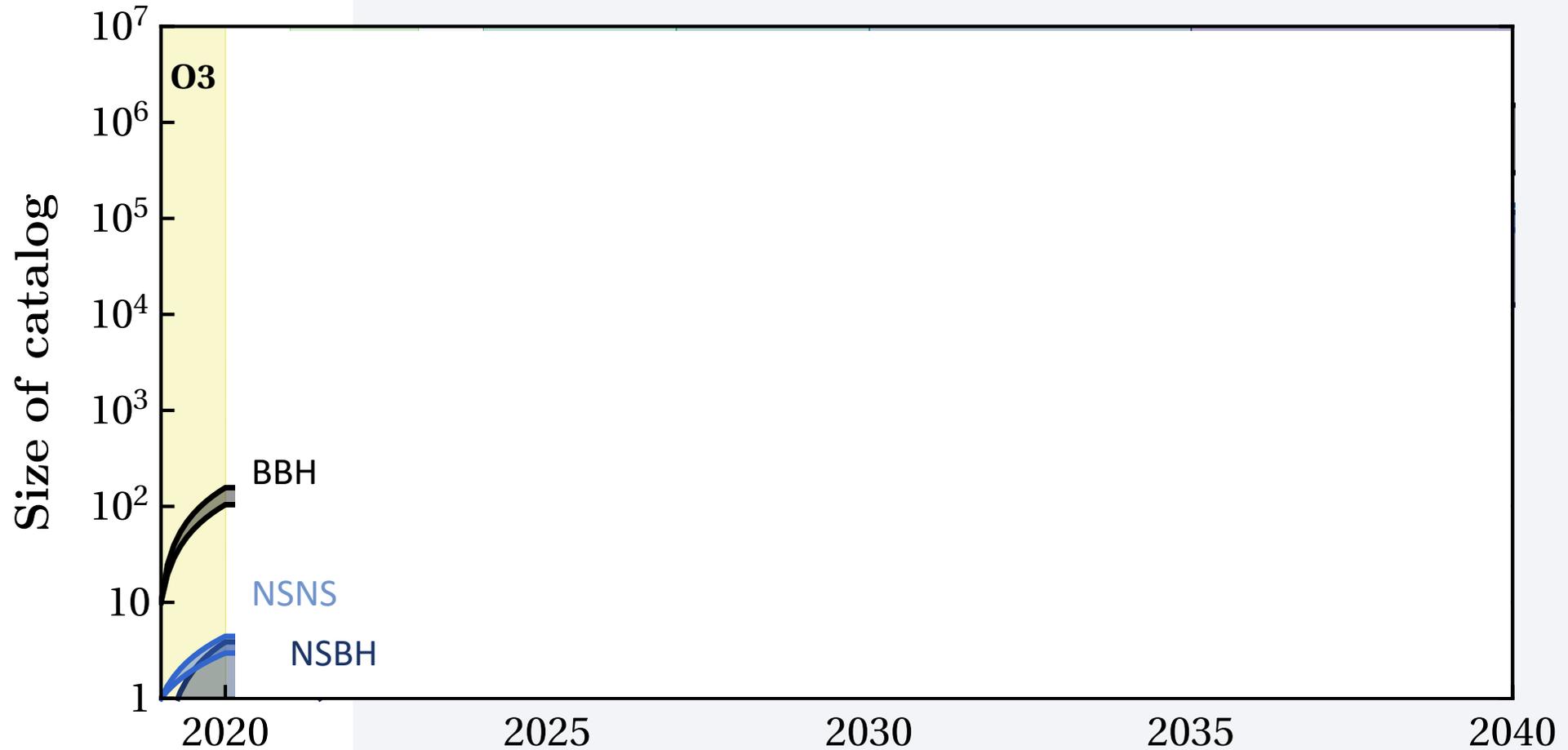


# This is true even under extreme assumptions

[van Son et al. \(2020\) arXiv:2004.0518](#)



# A lot more data is imminent



Baibhav et al. 2019