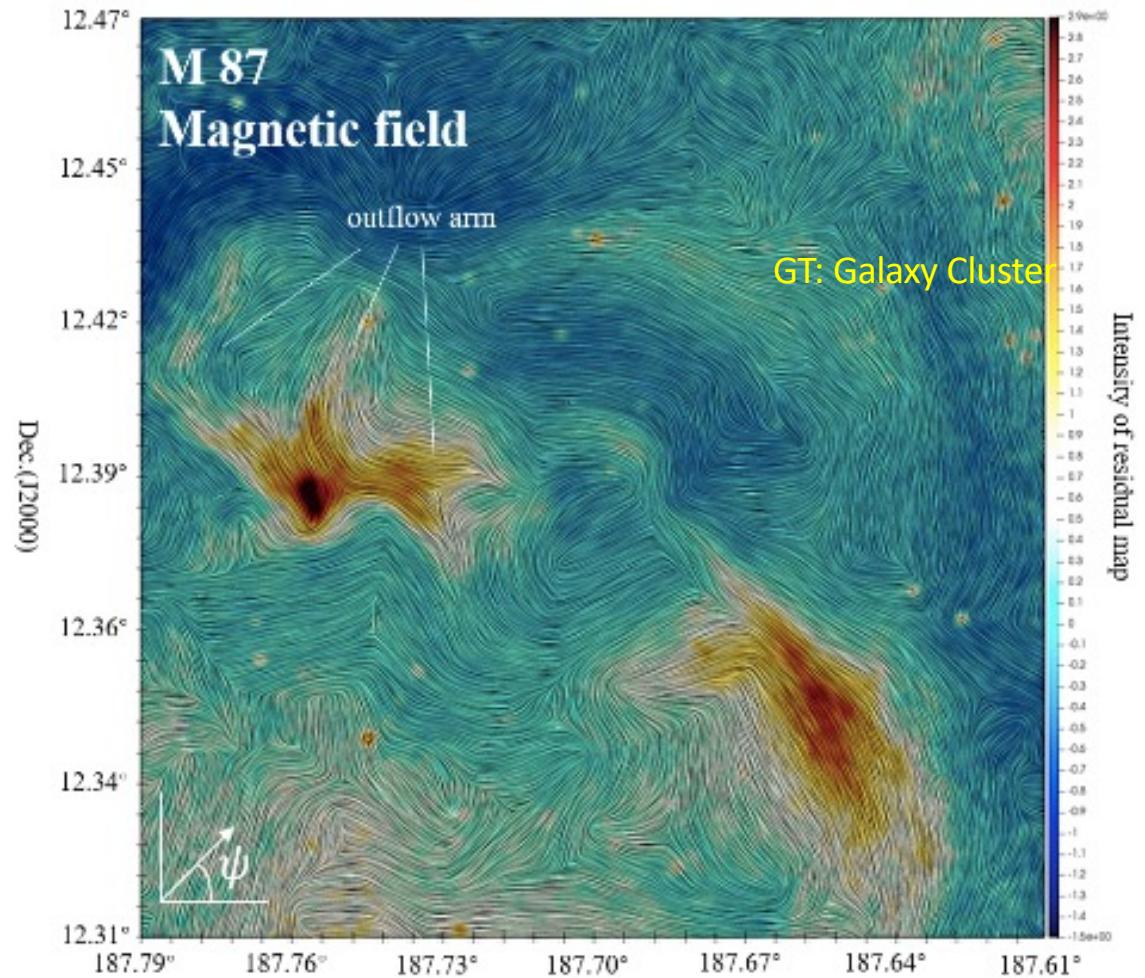


Magnetic field structure in the ICM and its effects

Alex Lazarian
University of Wisconsin-Madison



Special Thanks: Gianfranco Brunetti, Annalisa Bonafede, Chiara Stuardi,
Yue Hue, Li Yuan, G-M Lou, Irina Zhuravleva, Siyao Xu

Please note Yue Hu, Van Vleck Prize Winner:



Is going to get PhD degree with me in 2023 and will apply for positions this Fall

Magnetic fields radically change the properties of ICM plasmas

For instance:

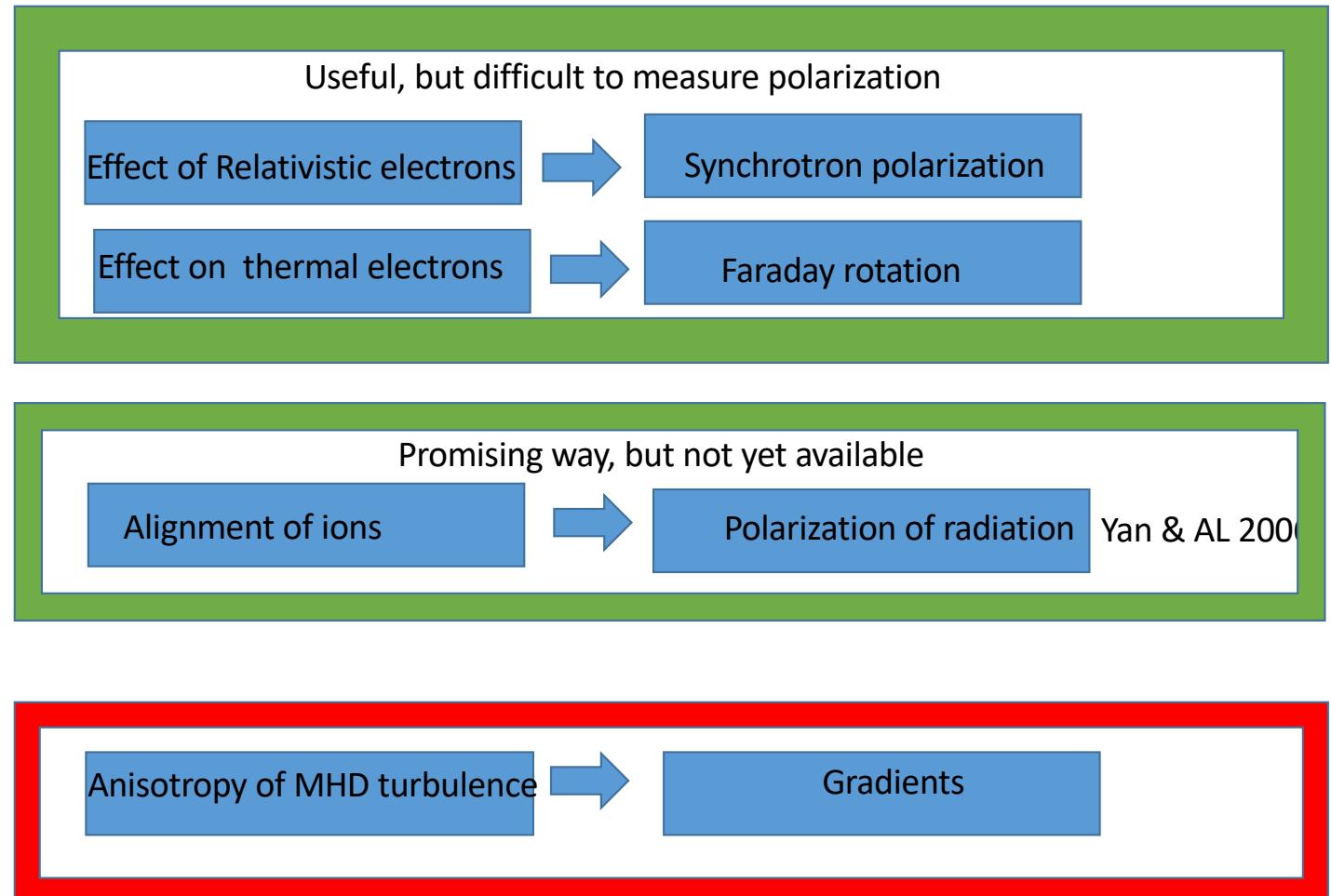
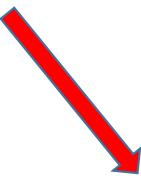
1. Effect on thermal conductivity
2. Transfer from collisionless to effectively collisional state
3. Coupling plasmas with cosmic rays

Questions to address:

1. How can one study magnetic fields?
2. What are the quantitative effects?

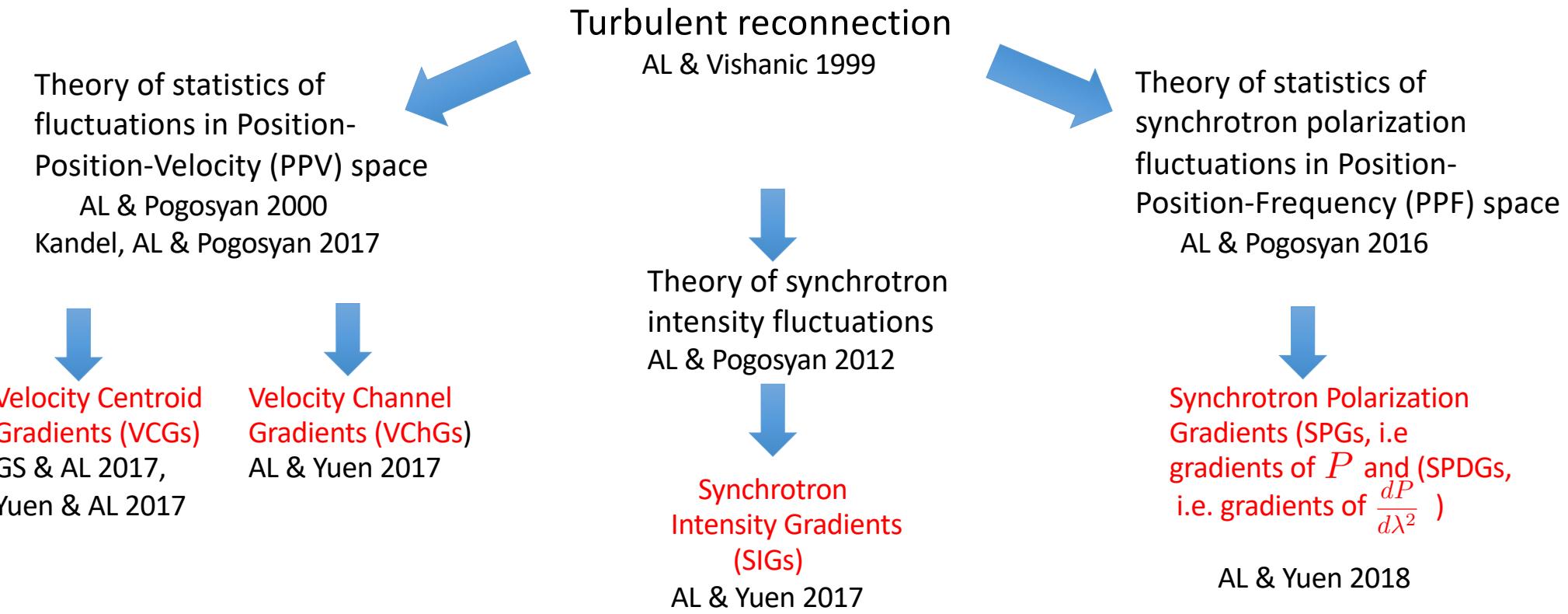
Clusters' magnetic fields: how do we measure if we don't see

Magnetic field



This talk

Gradient Technique (GT): foundations and incarnations

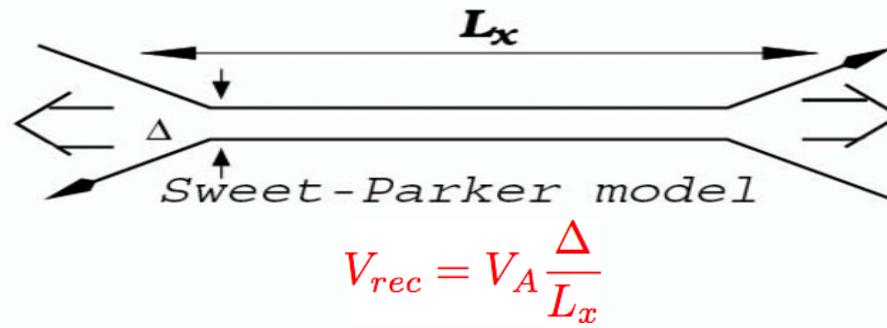


Full theory of gradients is in AL, Yuen & Pogosyan 2022

Turbulent magnetic fields reconnect fast

LV99 prediction:

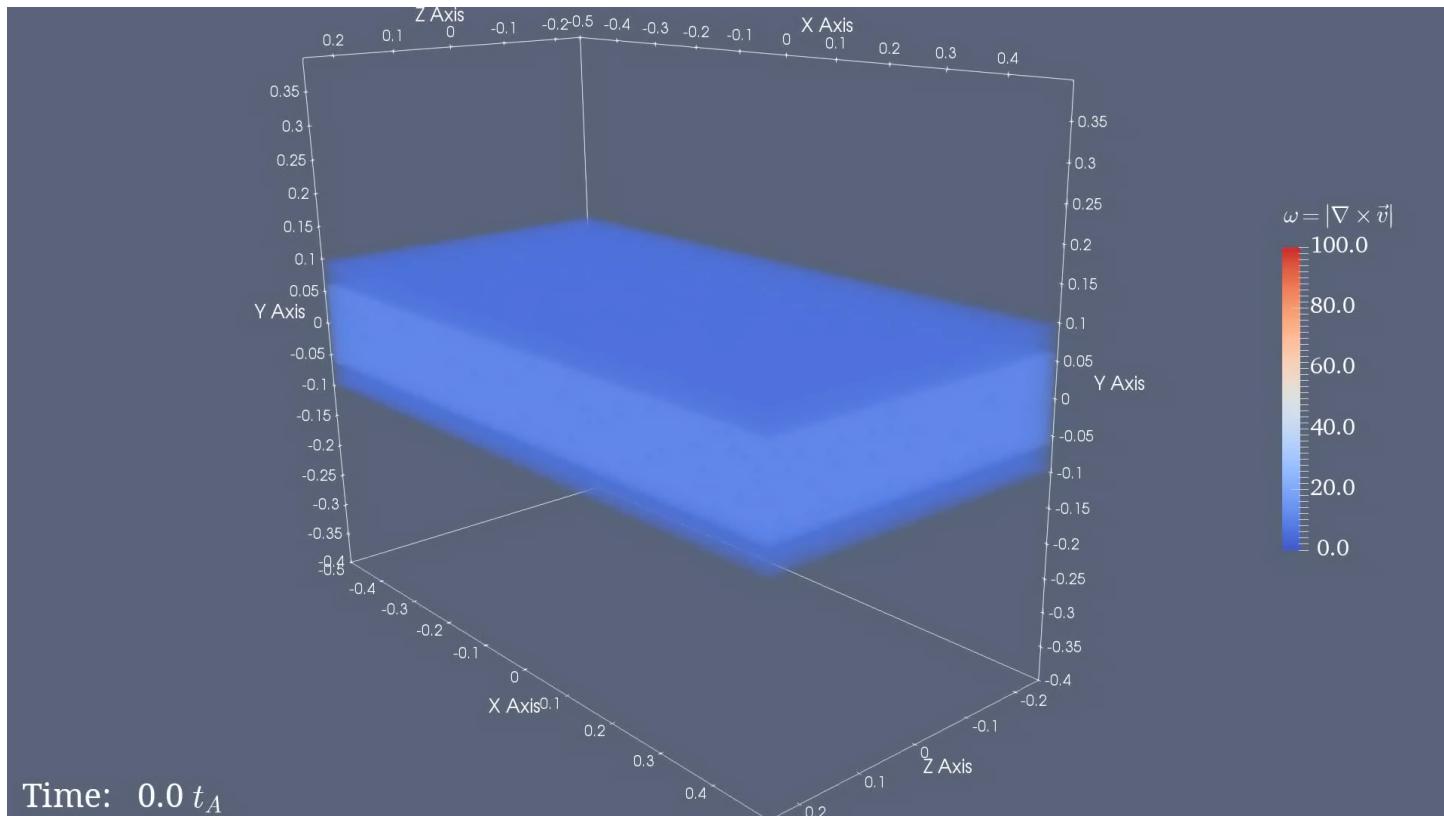
$$V_{rec} \approx V_A \left(\frac{V_{inj}}{V_A} \right)^2 \left(\frac{L_{inj}}{L_y} \right)^{1/2}$$



E. Vishniac

AL & Vishniac (1999)

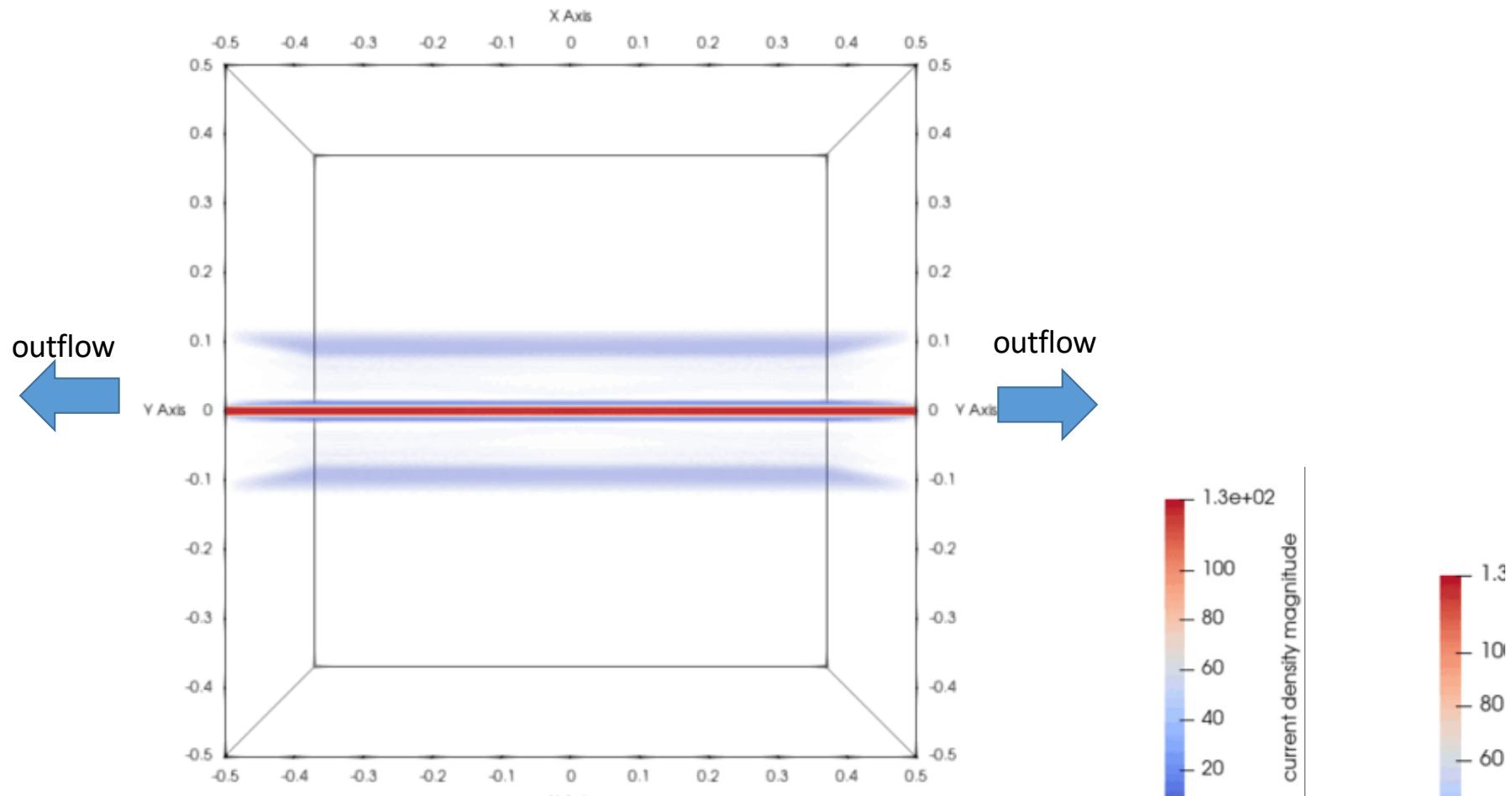
Turbulence is inevitable in 3D reconnection: development of turbulence through Kelvin-Helmholz instability



Kowal et al. 2017, 2020

Example: flares of reconnection happen in low beta plasmas

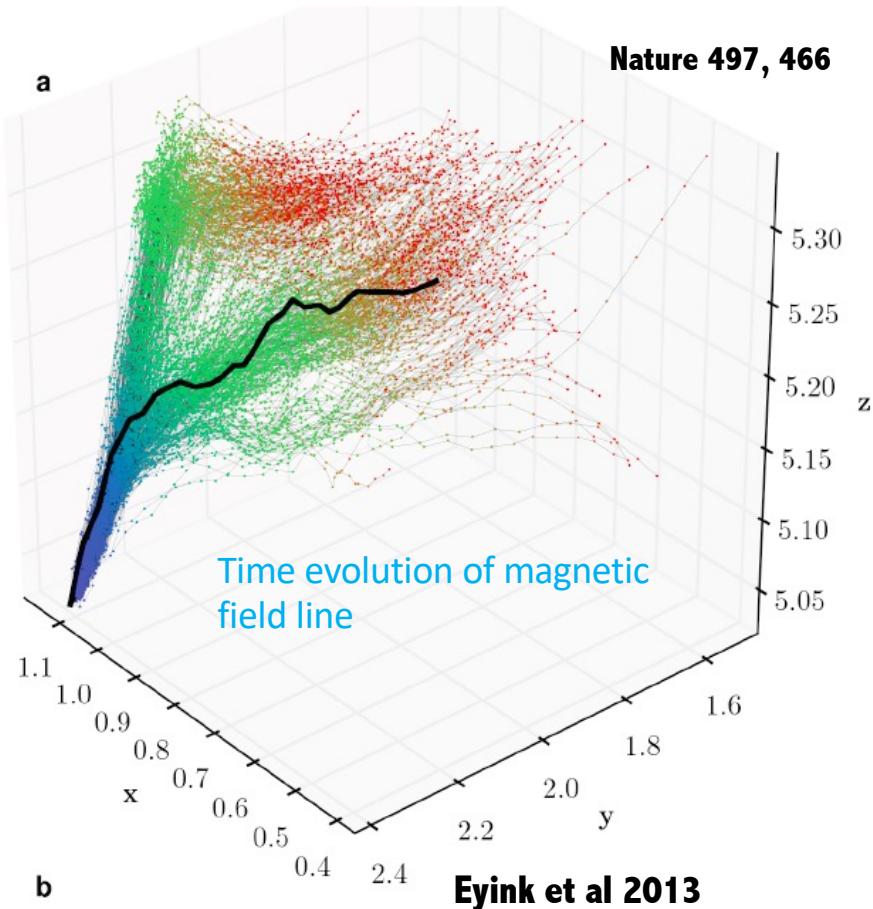
Kowal et al. 2022



Magnetic flux freezing is violated in turbulence due to turbulent reconnection



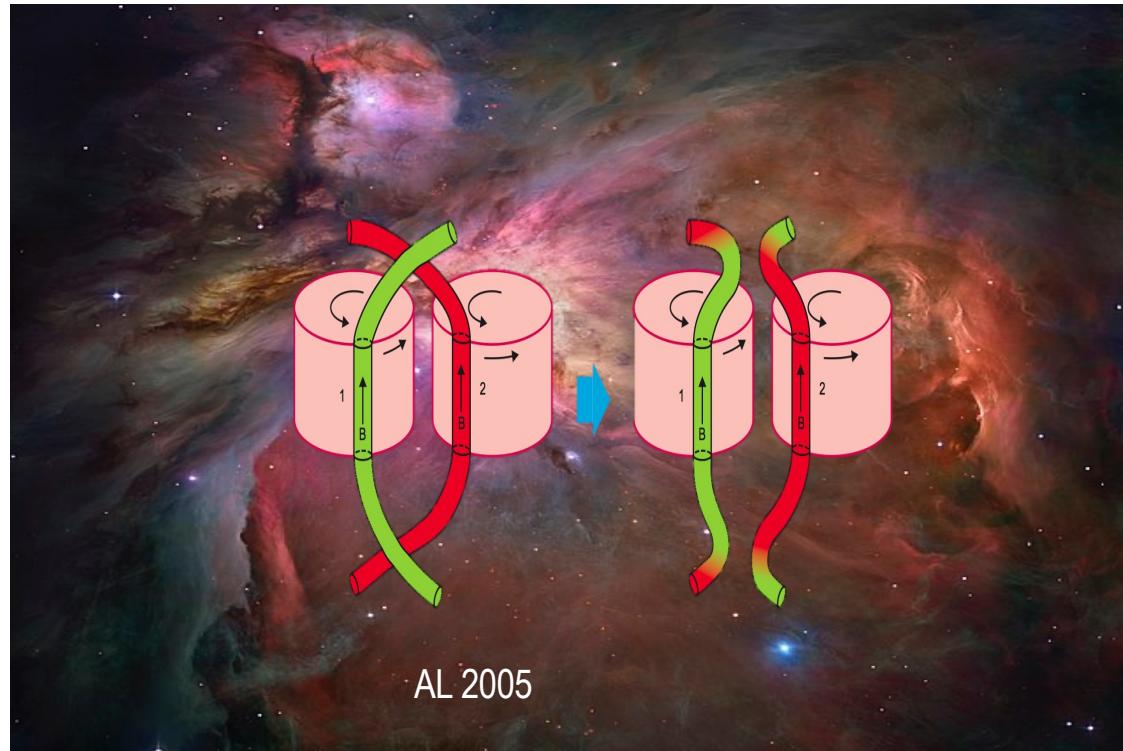
G. Eyink



Alfven theorem:
magnetic field line can
only be deformed

Reality: any given
magnetic field line has
billions of parents

Flux conservation (Alfvén theorem 1942) is violated in any turbulent medium



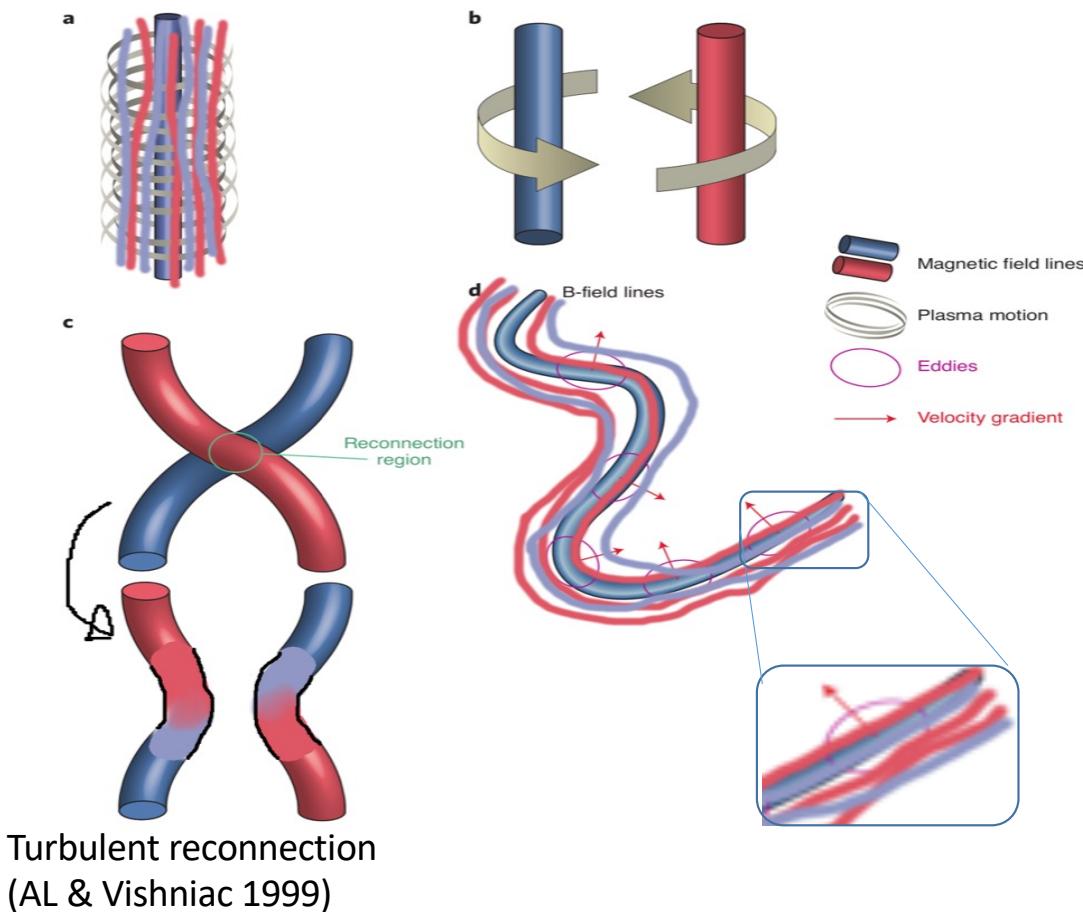
Consequence: reconnection diffusion



H. Alfvén

Reconnection diffusion induces heat transfer

Turbulent reconnection happens within an eddy turnover time, it favors eddies aligned with B-field: Gradients are perpendicular to local B-field



Types of Gradients:

1. Velocity gradients
2. Synchrotron intensity gradients
3. Synchrotron polarization gradients
4. Faraday rotation gradients

For subsonic turbulence, density acts as a passive scalar reflecting velocity statistics.

5. Density gradients

Fact Two: Turbulent gradients are dominated by the smallest resolved scales

If we measure below the turbulence injection scale

For velocity $v_l \sim l_{\perp}^{1/3}$



Gradient \perp to B $v_l/l_{\perp} \sim l_{\perp}^{1/3}/l_{\perp} = l_{\perp}^{-2/3}$

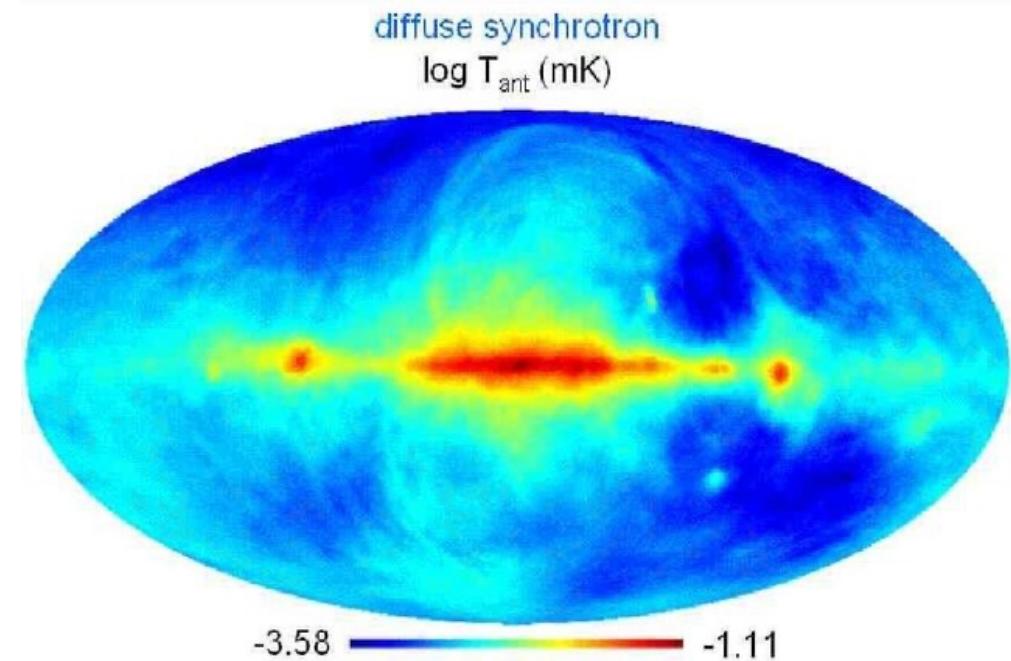
Large scale shear does not affect gradients, gradients are dominated by motions at the smallest resolved turbulence scales

For Alfvénic motions, B and V are interchangeable, thus **synchrotron intensity gradients** trace B.

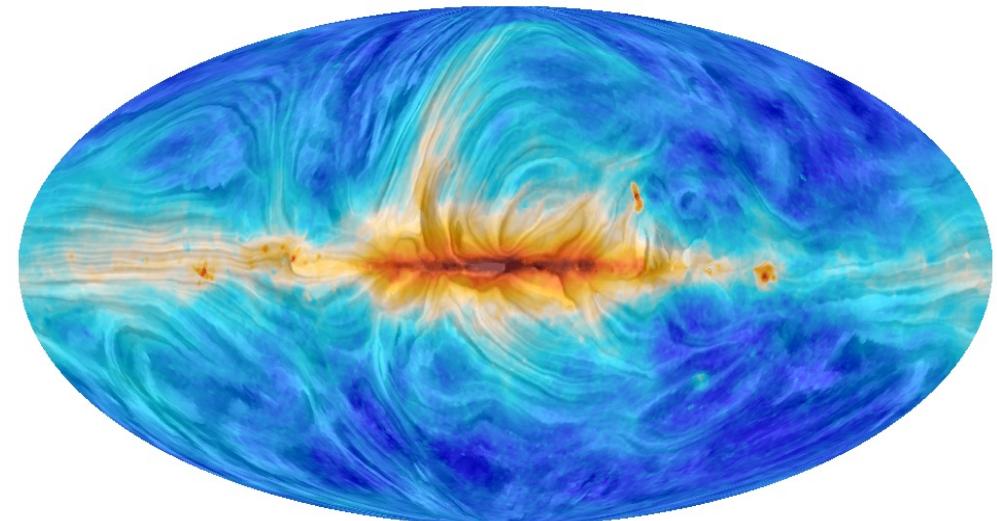
For subsonic turbulence, density statistics mimics velocity statistics, thus **intensity gradients** trace B.

Can we directly get magnetic field orientation from synchrotron intensity

Synchrotron Intensity

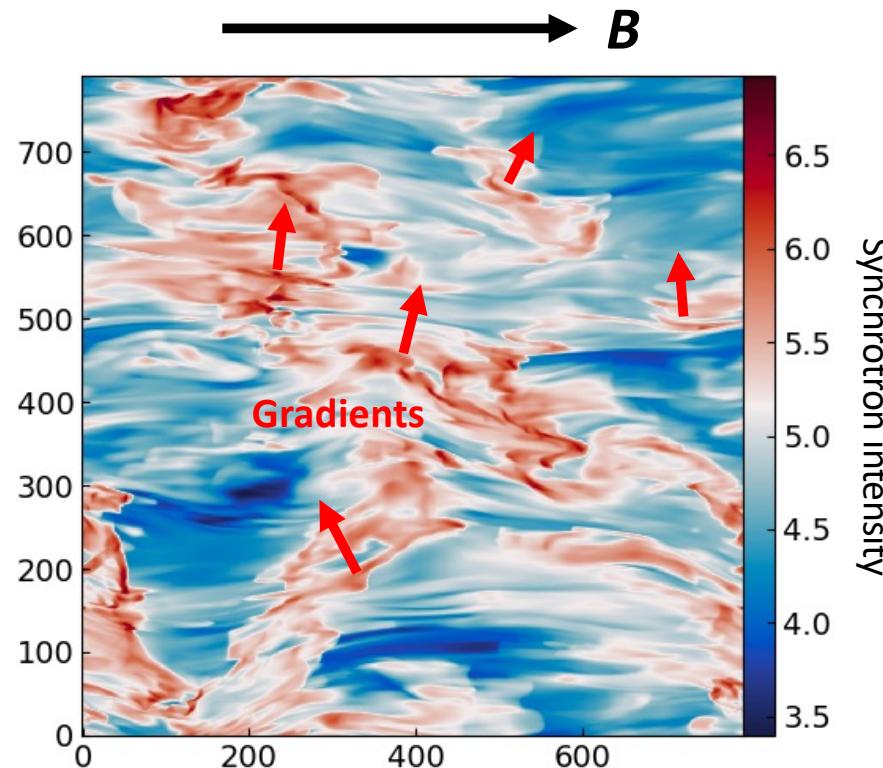


Magnetic field lines traced
by synchrotron polarization



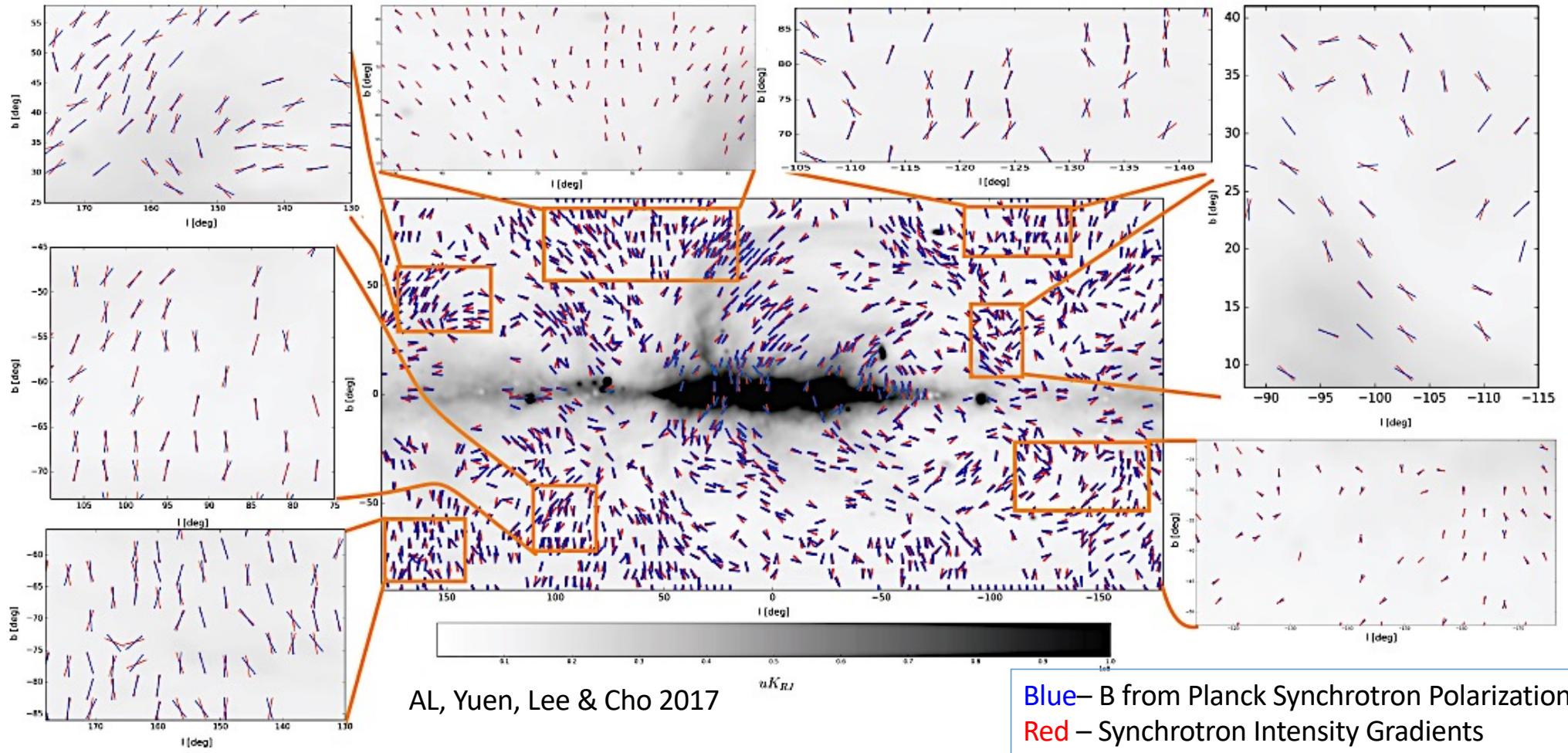
Planck collaboration

Visualization of synchrotron intensities in MHD simulations

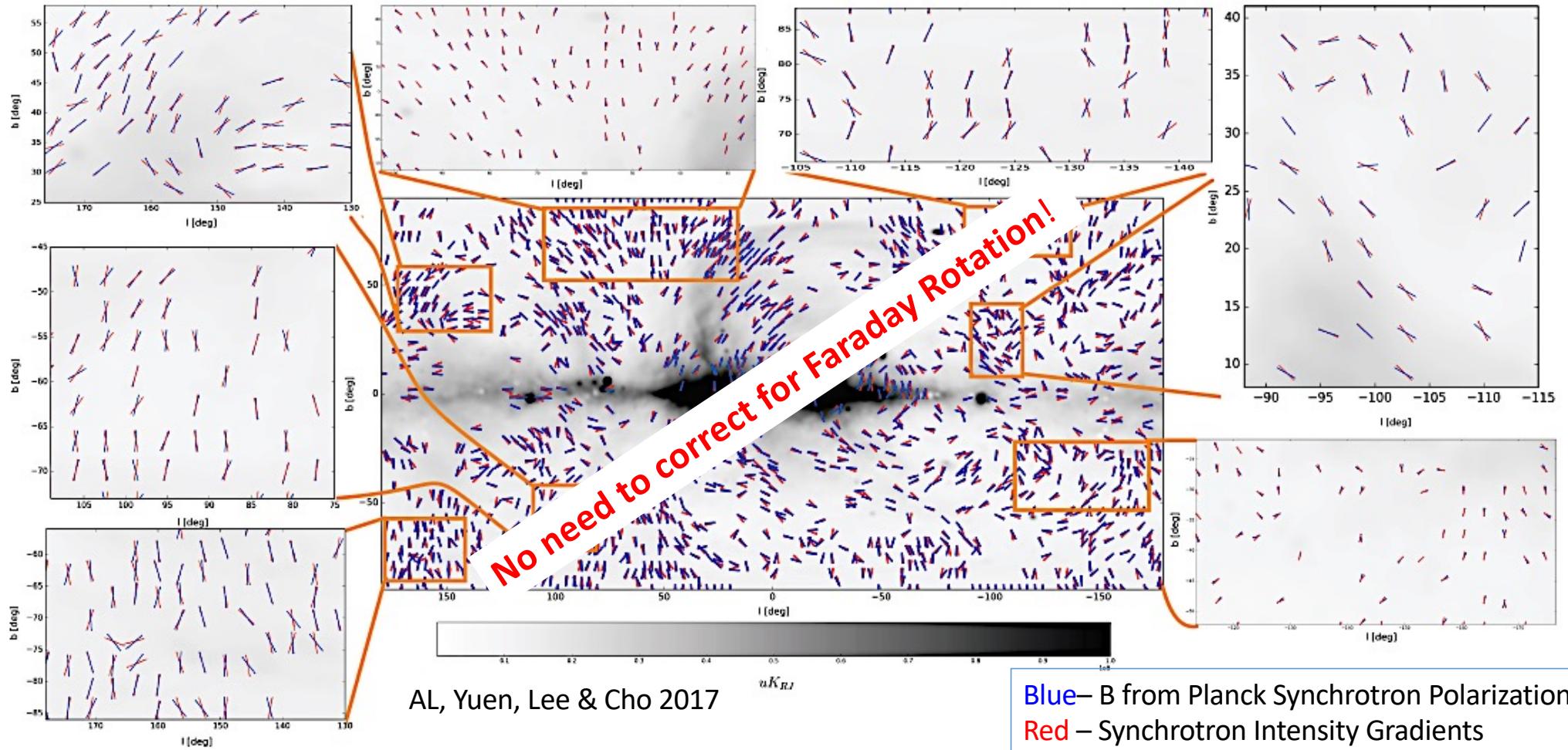


AL et al. 2017

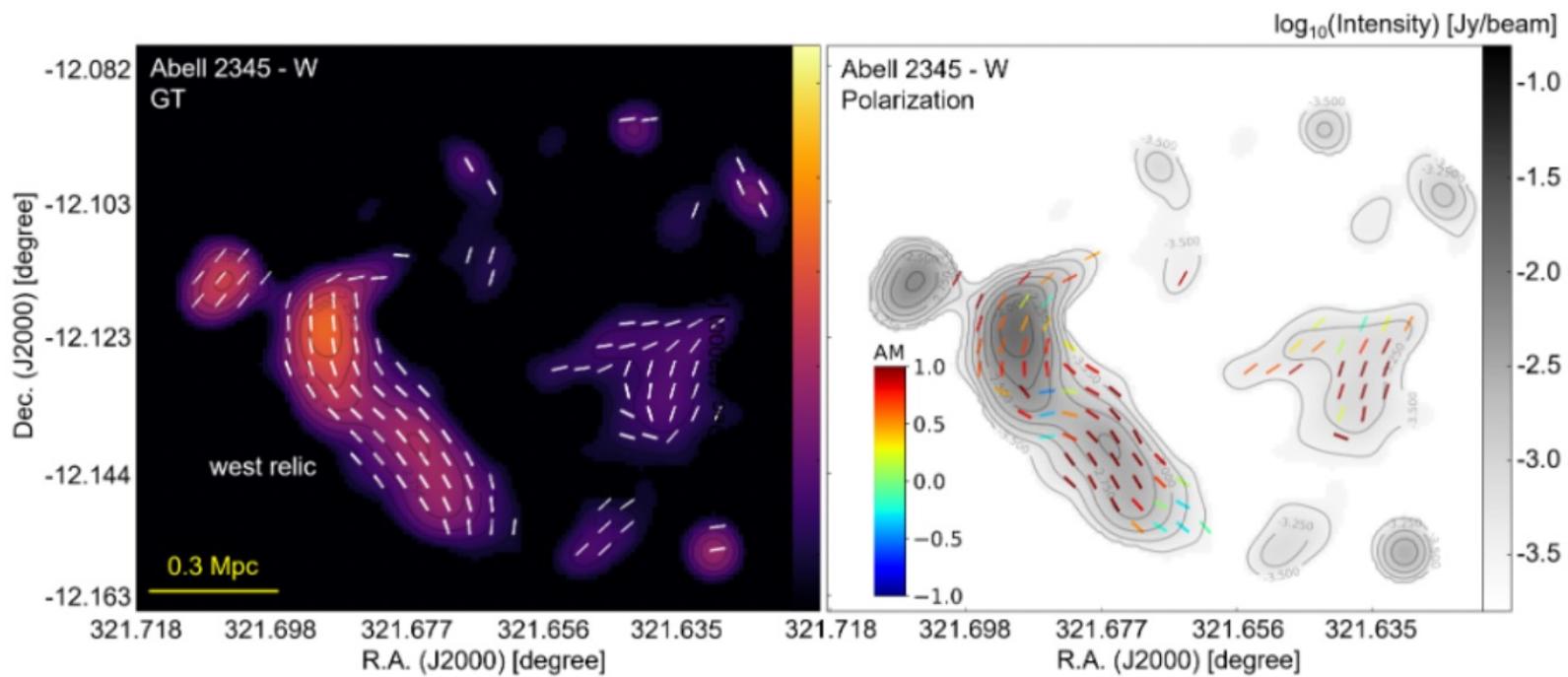
The maximum synchrotron intensity gradient (rotated by 90°) aligned with magnetic field



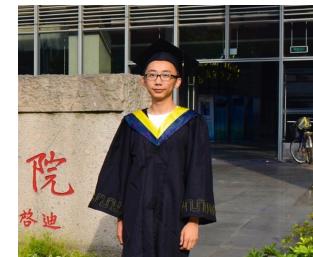
The maximum synchrotron intensity gradient (rotated by 90°) aligned with magnetic field



Good correspondence with the existing polarization

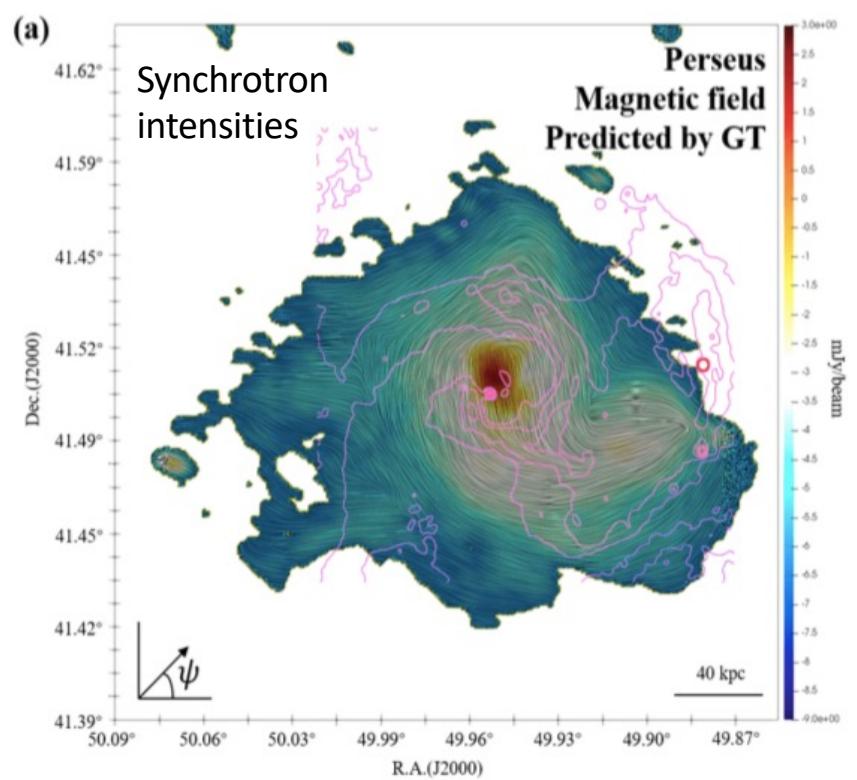
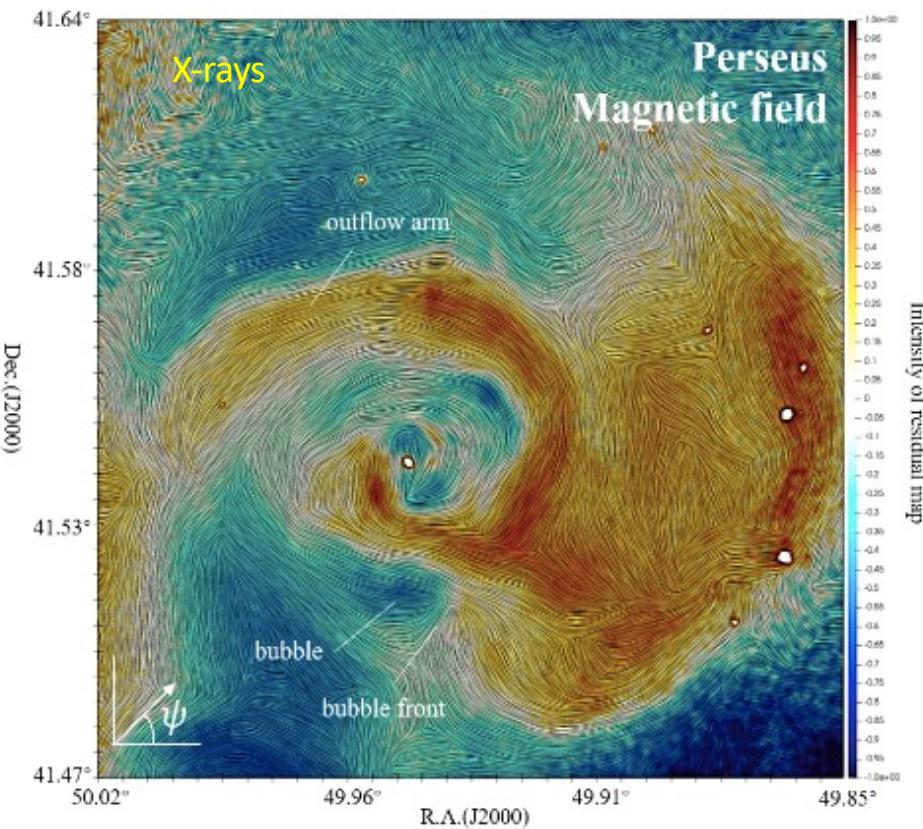


Hu et al. 2022



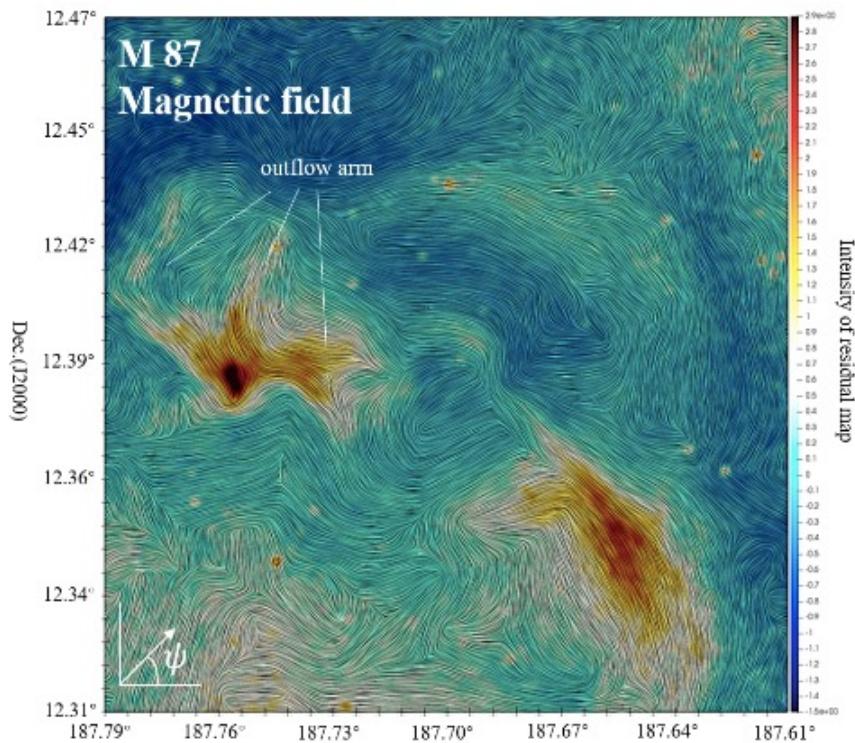
Yue Hu

Density for low sonic Mach numbers reflects the velocity pattern. X-ray and synchrotron intensity gradients reveal magnetic field directions in galaxy clusters



Hu et al. 2020

The magnetic field structure of other clusters was obtained using X-ray and synchrotron emission images

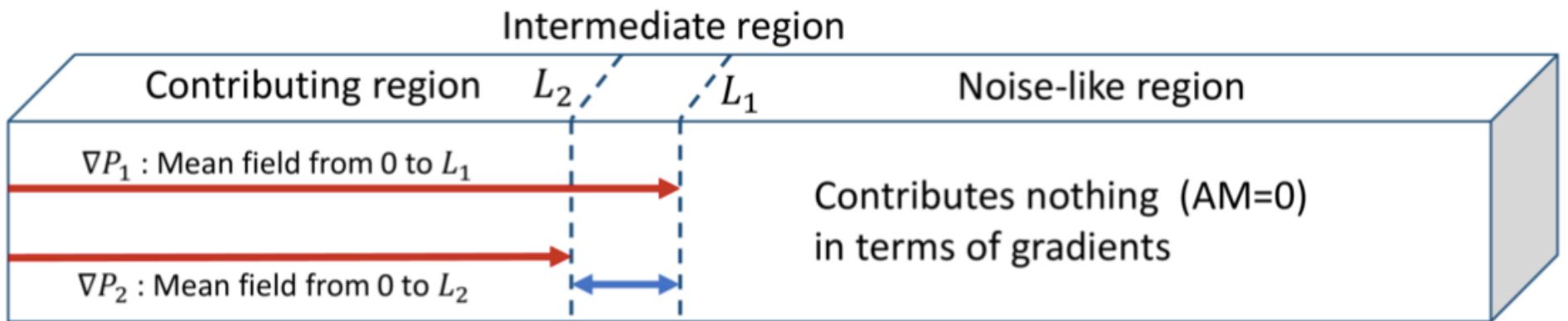


Hu et al. 2020

And many more in a new paper by Hu et al. 2022 using synchrotron emission

The next step will be the tomography of magnetic field using gradients

Faraday depolarization effect provides the boundary up to which the polarized synchrotron is sampled: Allows to study 3D distribution



$$\nabla(\Delta P) = \nabla \int_{L_2}^{L_1} dz P_i e^{2i\lambda_1^2 \phi(z)}$$

tells the mean field in slice $l \in [L_2, L_1]$

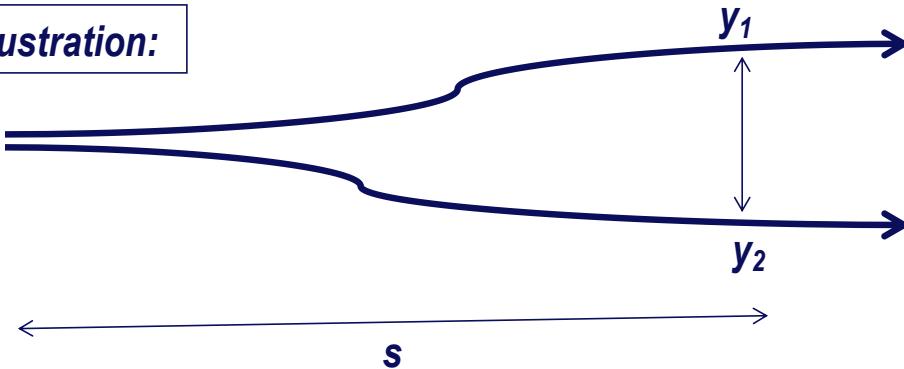
Unlike polarization directions the directions of the gradients of $|P|$ are not affected by Faraday rotation. This provides a unique way to map the perpendicular to line of sight B-field in 3D.

Suggested in AL & Yuen 2018. Tested successfully in Ho et al. 2020

Properties of the magnetic field that must be accounted for: effects of heat conduction and cosmic ray physics

Diffusion of electrons along magnetic field induces thermal conductivity

Simplified illustration:



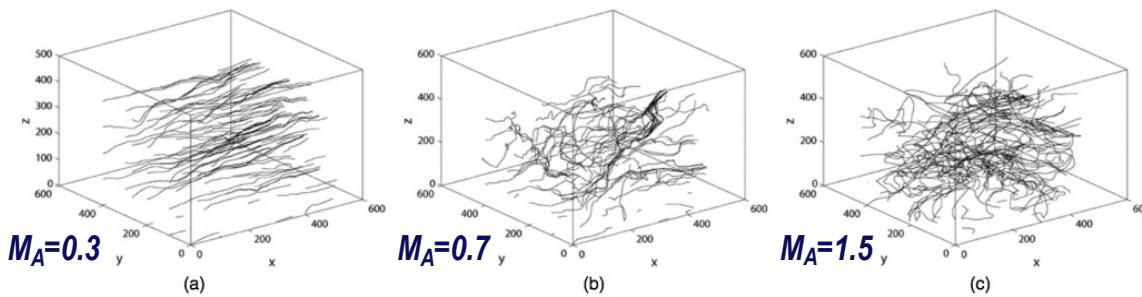
For $y <$ injection scale

$$\langle |y_1(s) - y_2(s)|^2 \rangle \sim s^3 M_A^4$$

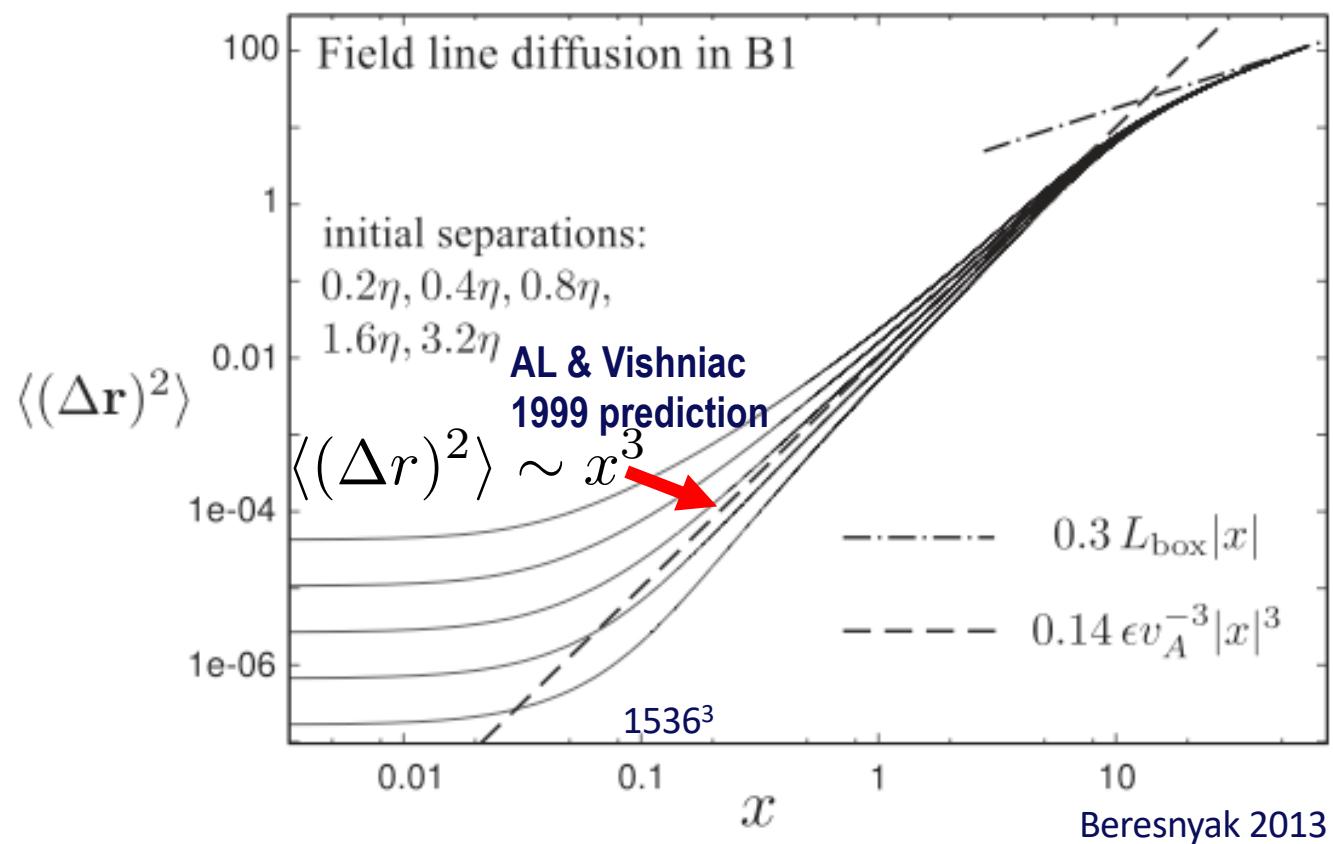
$$M_A = V_{\text{injection}} / V_{\text{Alfven}}$$

Is Alfvén Mach number

AL & Vishniac 1999



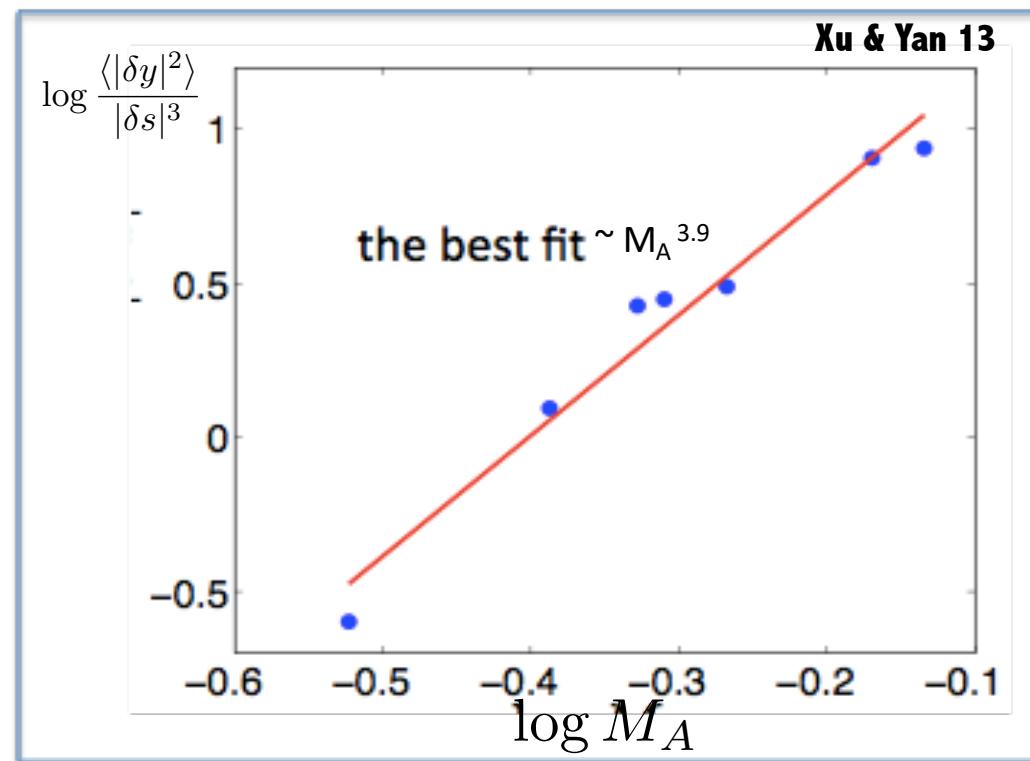
Superdiffusion is confirmed by tracing magnetic field line separation



... as well as with tracing particles following magnetic field

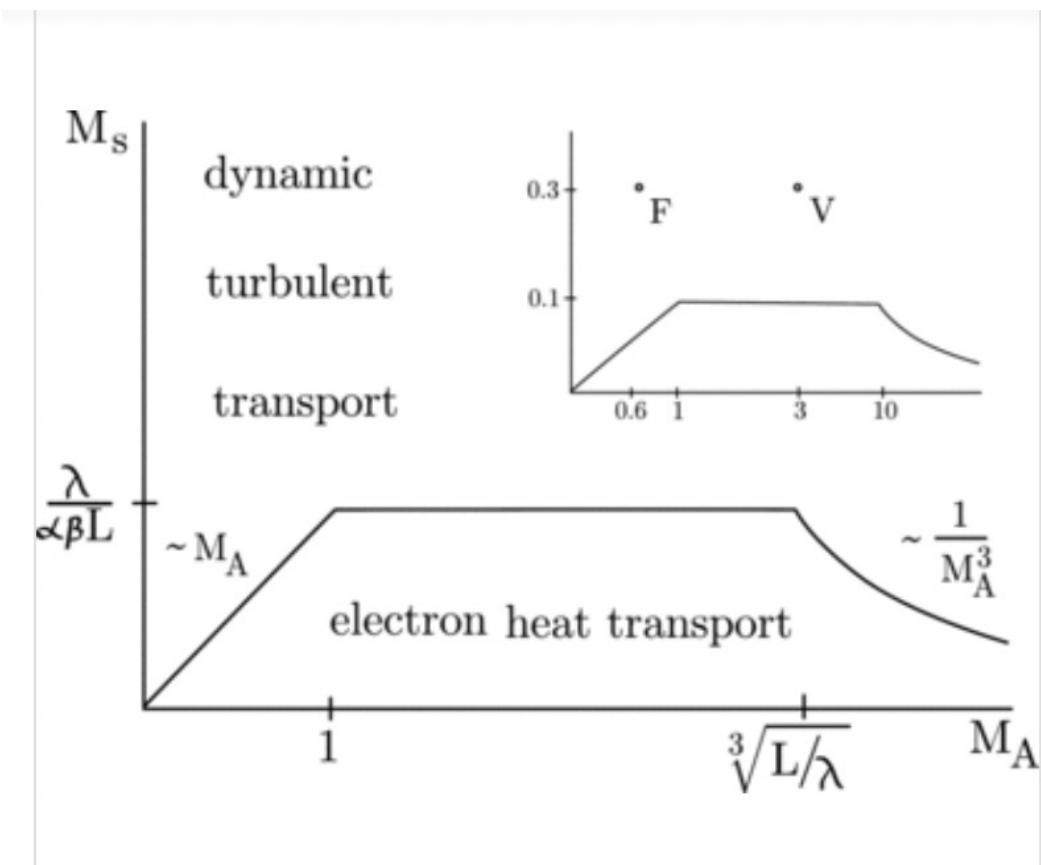
$$\langle |y_1(s) - y_2(s)|^2 \rangle \sim s^3 M_A^4$$

$$M_A = \frac{V_{inj}}{V_A}$$



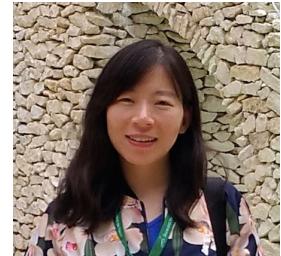
Changes CR acceleration in shocks (AL & Yan 2014)

For clusters of galaxies the turbulent transport enabled by reconnection diffusion is the most important

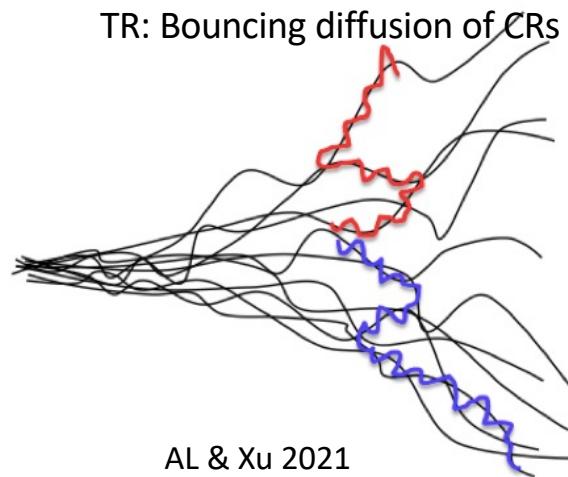


AL 2006

Magnetic wandering enables efficient second-order Fermi and magnetic bottle removal



Siyao Xu

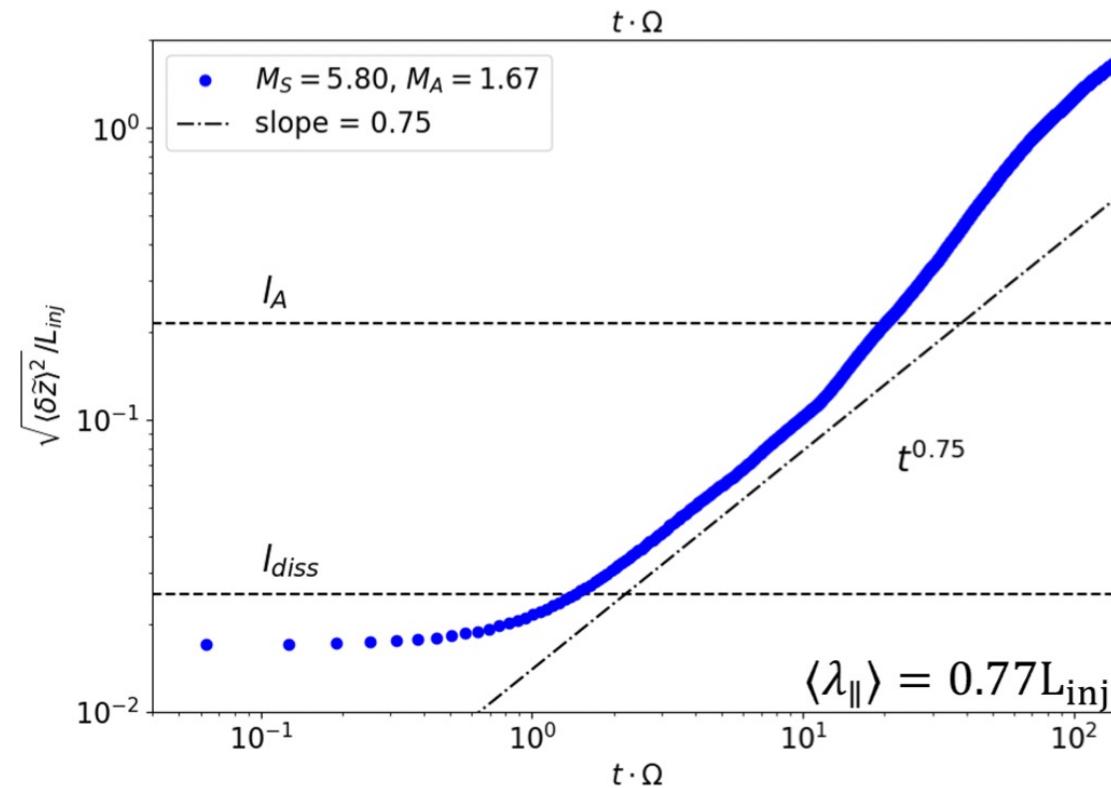


Due to superdiffusion particles are not trapped by magnetic mirrors and propagate perpendicular to B as $y^2 \sim s^{5/2}$ and experience 2nd order Fermi bouncing acceleration

AI & Xu 2022

Xu 2021 explanation of the gamma-ray emission from supernovae remnants

In the presence of scattering the perpendicular diffusion law changes

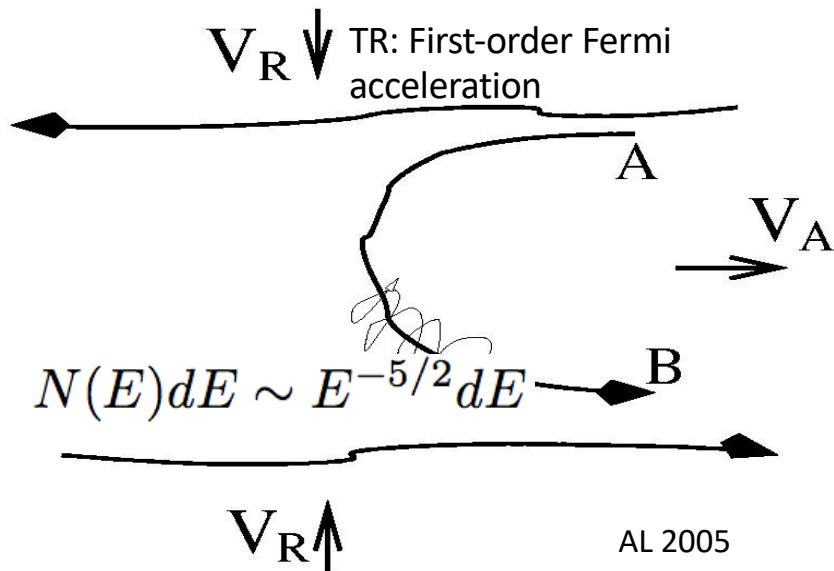


Yue Hu

Hu, AL & Xu 2022

TR: First order Fermi acceleration of Cosmic Rays (CRs) in 3D

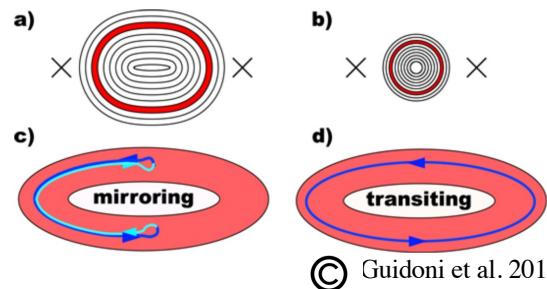
Acceleration in LV99 reconnection:



De Gouveia Dal Pino & AL 2005

Parallel momentum increases due to bouncing
from convergent magnetic mirrors

Alternative idea of acceleration in
2D islands by Drake et al. 2006:



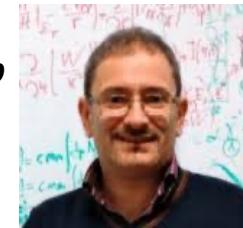
“2D islands are graveyards of CRs”
L. Sironi 2022

1.5 order Fermi Acceleration by reconnection in MHD turbulence

Within reconnection regions in turbulent flow CRs momentum increase $\delta p > p$

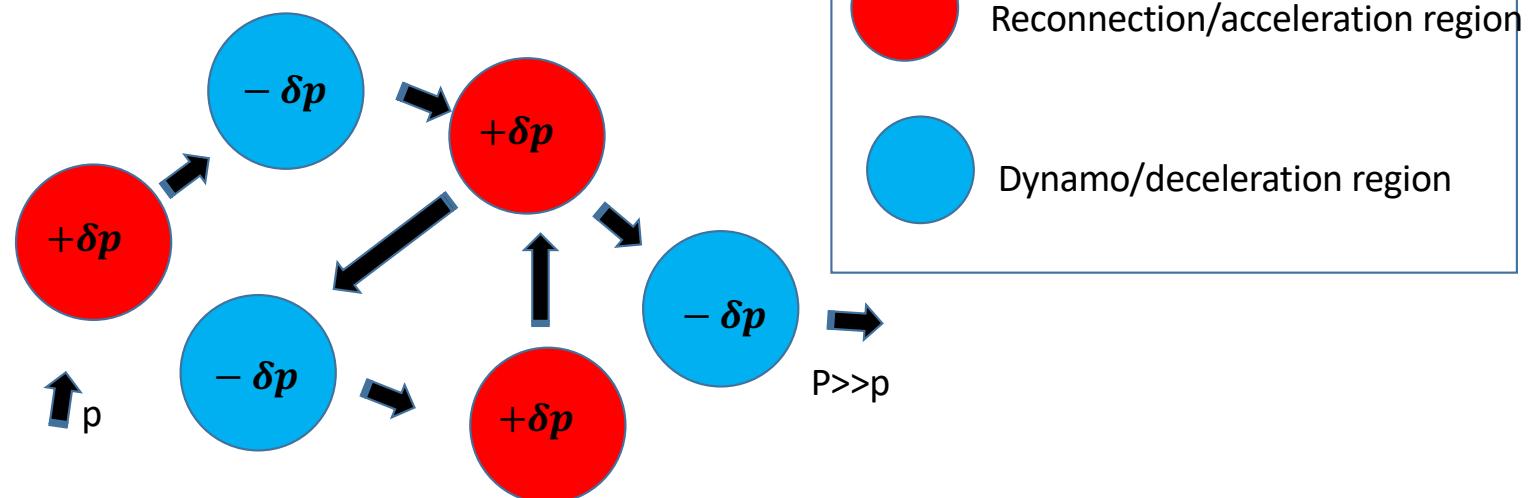
1.5 order Fermi acceleration: random walk with large increments $\delta p > p$

In MHD turbulence kinetic energy and magnetic energy constantly transfer into each other



G. Brunetti

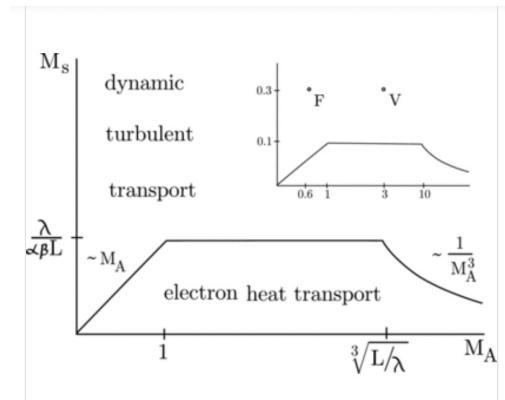
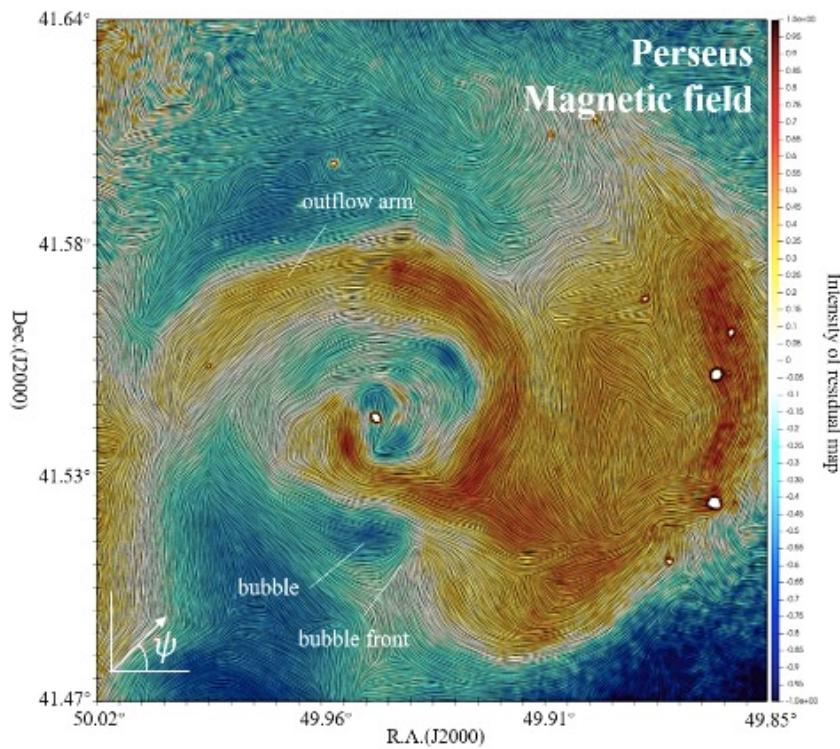
1.5 Fermi: Random walk with $\delta p > p$



Brunetti & AL 2016 first application to clusters of galaxies electron acceleration,
explaining spectra of gamma-ray bursts in Xu & Zhang 2020....

Summary

Gradient technique opens a new way to study magnetic fields in galaxy clusters.
Magnetic field deeply affects the physics of ICM.



Differential Measure Approach instead of DCF

Using not dispersions by differential measures, i.e. small R separation
structure function of centroid velocity

$$D_v(R) = \langle (v(X + R) - v(X))^2 \rangle$$

and angle instead of σ_v

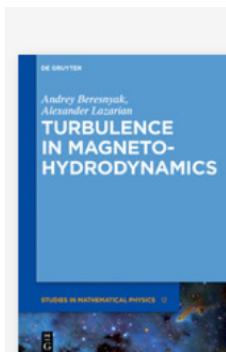
$$D_\phi(R) = \langle (\phi(X + R) - \phi(X))^2 \rangle$$

instead of dispersions of σ_ϕ

This allows:

1. Decrease the amount of data required.
2. Measure B for $B_{mean} < \delta B$
3. Remove velocity regular distortions due to galactic shear.
4. Remove B-field distortions due to gravity.
5. Study variations of $B_{\perp,mean}$

Using the theory of MHD turbulence rather than linear Alfvén waves



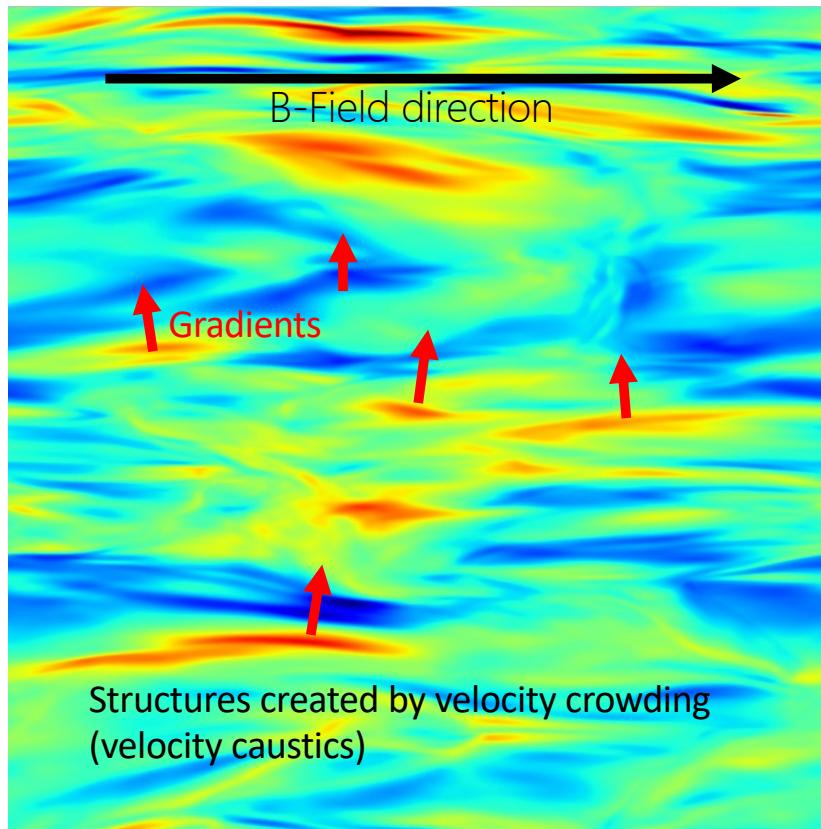
Beresnyak, Andrey / Lazarian, Alexander
Turbulence in Magnetohydrodynamics

Series: [De Gruyter Studies in Mathematical Physics 12](#)

This allows obtaining analytical expressions for realistic turbulent media

Implemented in AL, Yuen & Pogosyan (2020, 2021)

B-field direction can be revealed by gradients in velocity channel maps



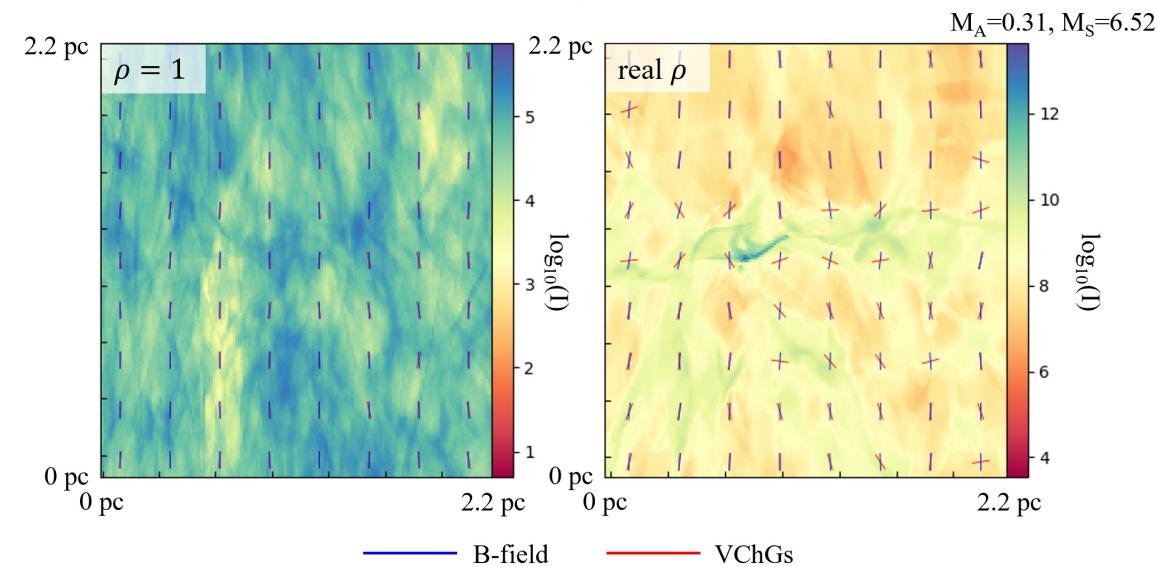
We turn velocity gradients 90 degrees to trace magnetic field direction

Filaments are clearly seen in channel maps obtained with incompressible simulations

AL & Yuen 2018

The controversy of what is seen in channel maps can be resolved by using the Velocity Decomposition Algorithm (VDA)

Talk tomorrow by Ka Ho Yuen



$$p_v = p - (\langle pI \rangle - \langle p \rangle \langle I \rangle) \frac{I - \langle I \rangle}{\sigma_I^2}$$

$$p_d = p - p_v$$

$$= (\langle pI \rangle - \langle p \rangle \langle I \rangle) \frac{I - \langle I \rangle}{\sigma_I^2}$$

p_v is the channel intensity due to velocity caustics

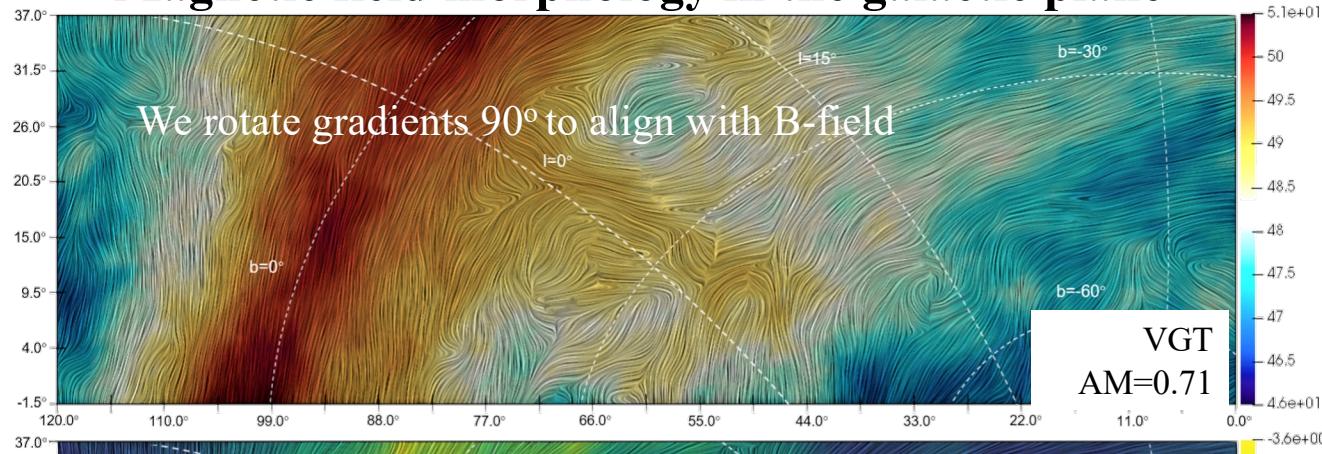
p_d is the channel intensity due to density effects

Distortions in Channel Maps are induced by densities. VDA removes the contribution of density.

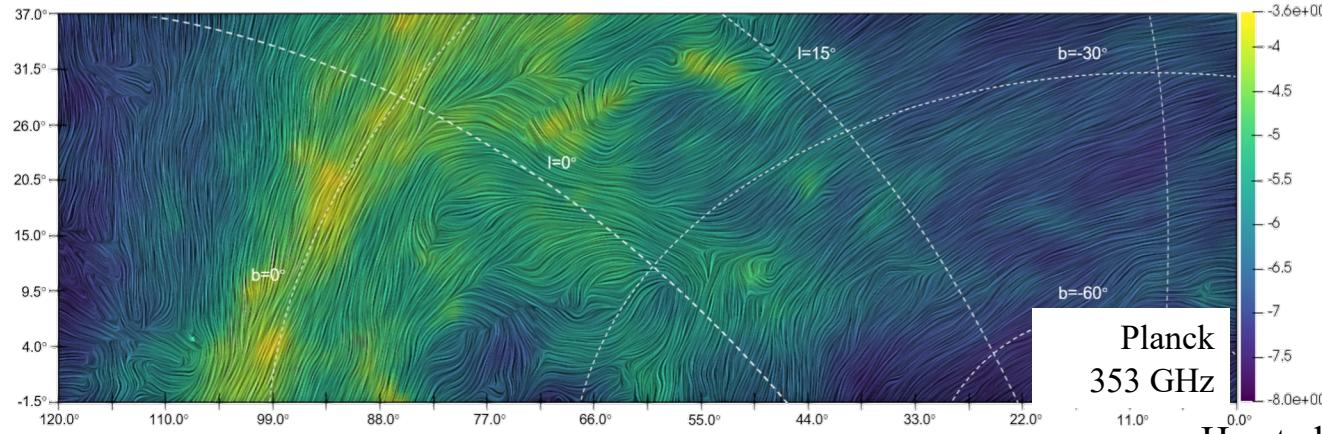
Yuen, Ho & AL 2021

Good correspondence with Planck polarization polarization

Magnetic field morphology in the galactic plane

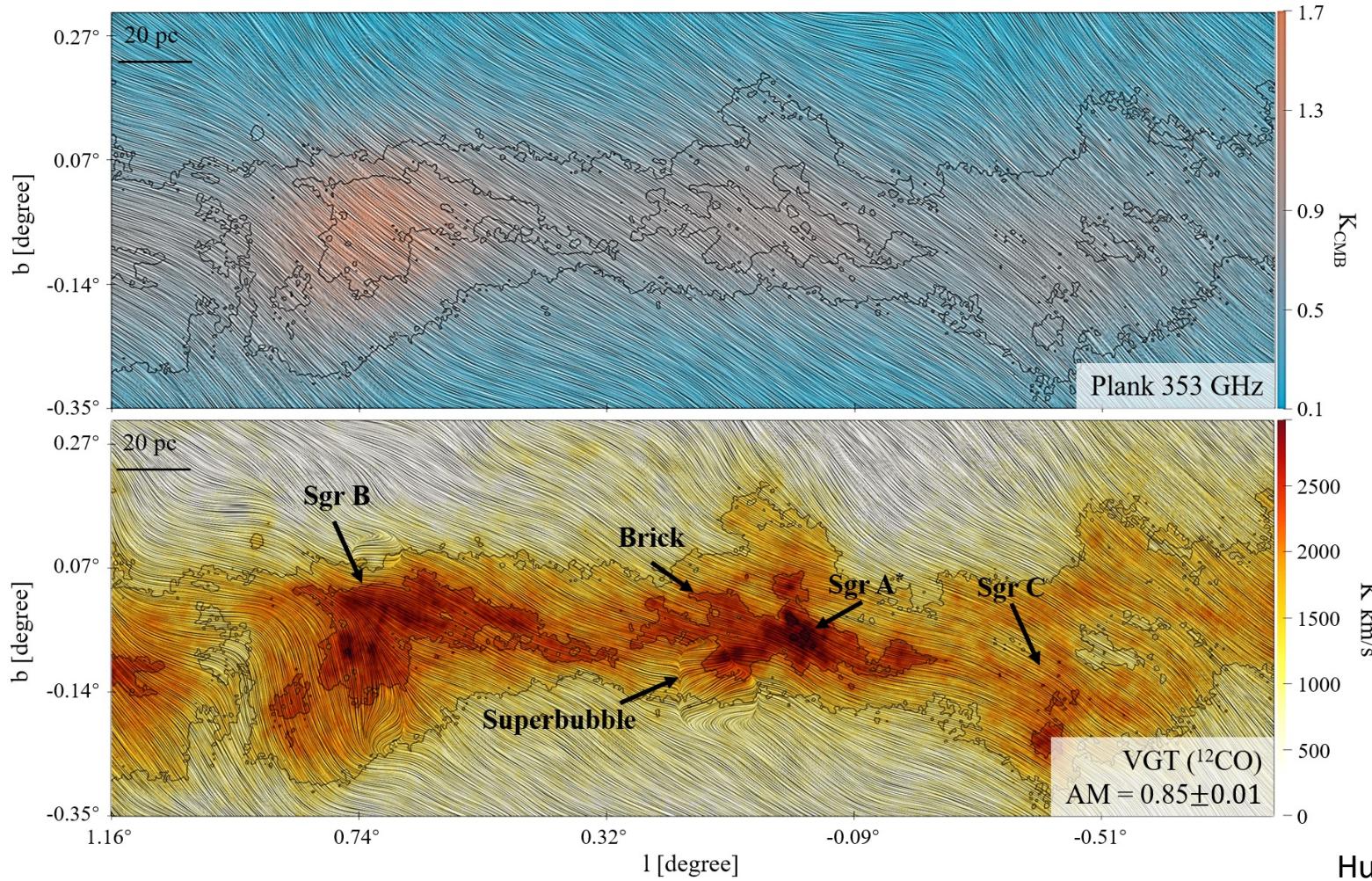


More in the talk tomorrow by Dmitri Pogosyan



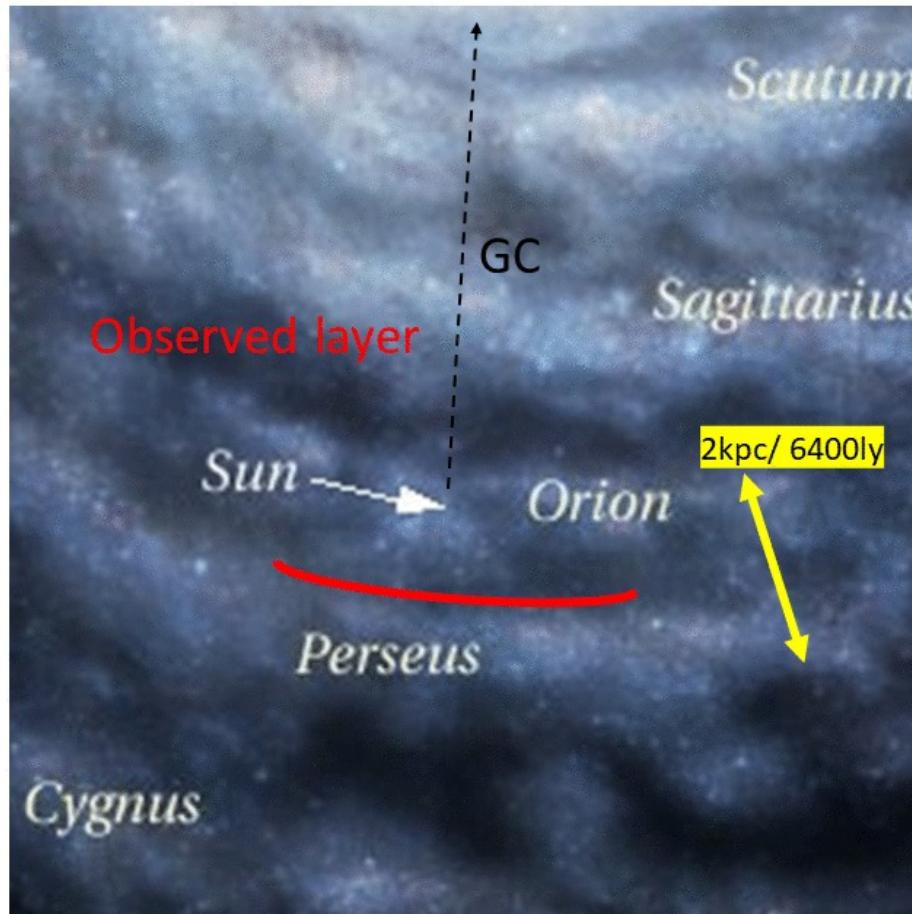
Hu et al. (2020) Lu, AL, Pogosyan 2020

Gradients and polarization for the Central Molecular Zone

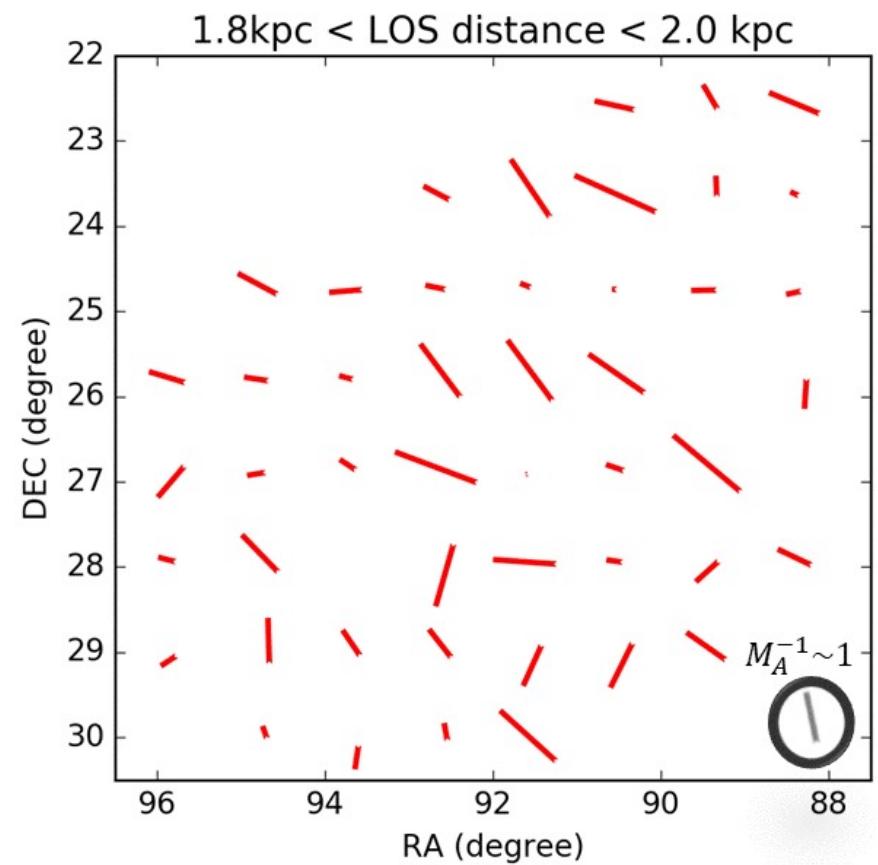


Hu, AL & Wang 2021

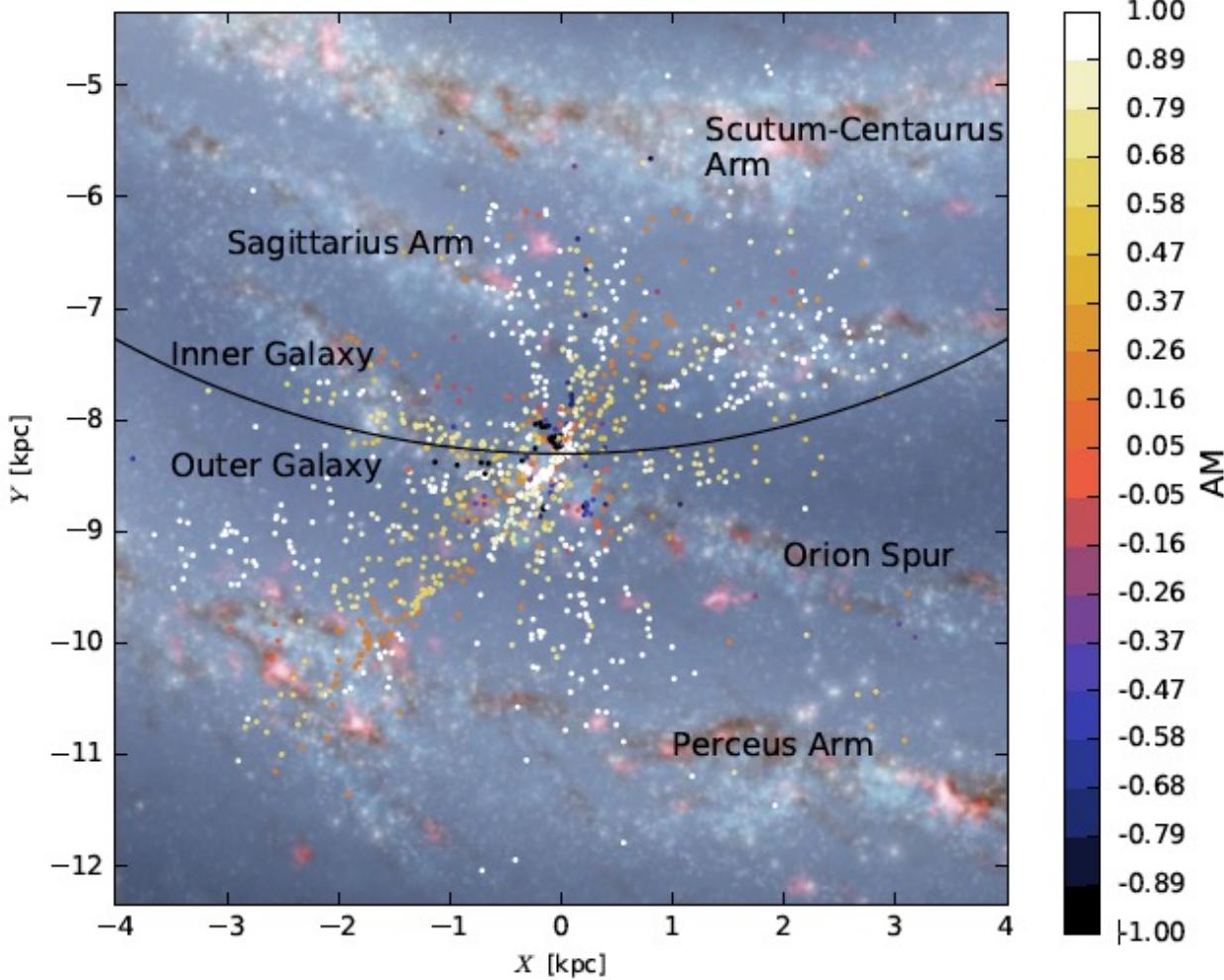
More information compared to polarization: it is possible to study 3D structure of magnetic field in galactic disk



Voron et al. 2019



3D B-field distribution corresponds well to starlight polarization

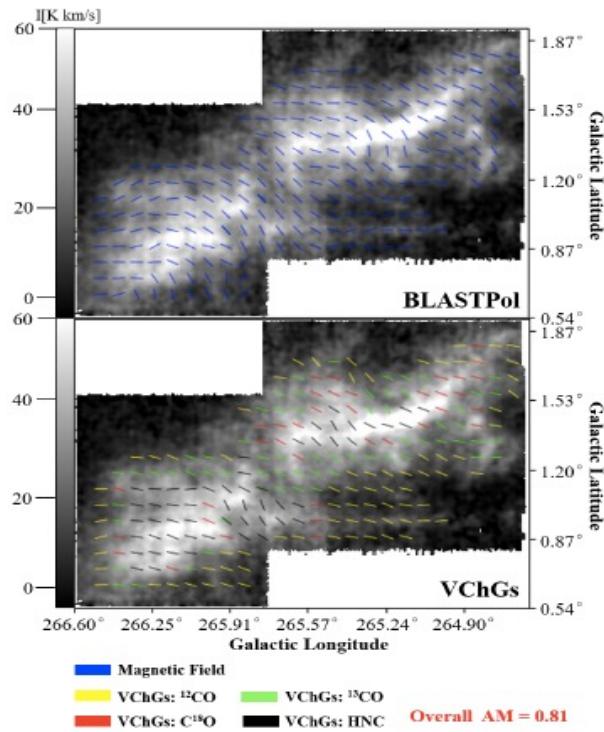


Star polarization versus predictions with our 3D model of galactic magnetic field. This demonstrates that the model is correct!

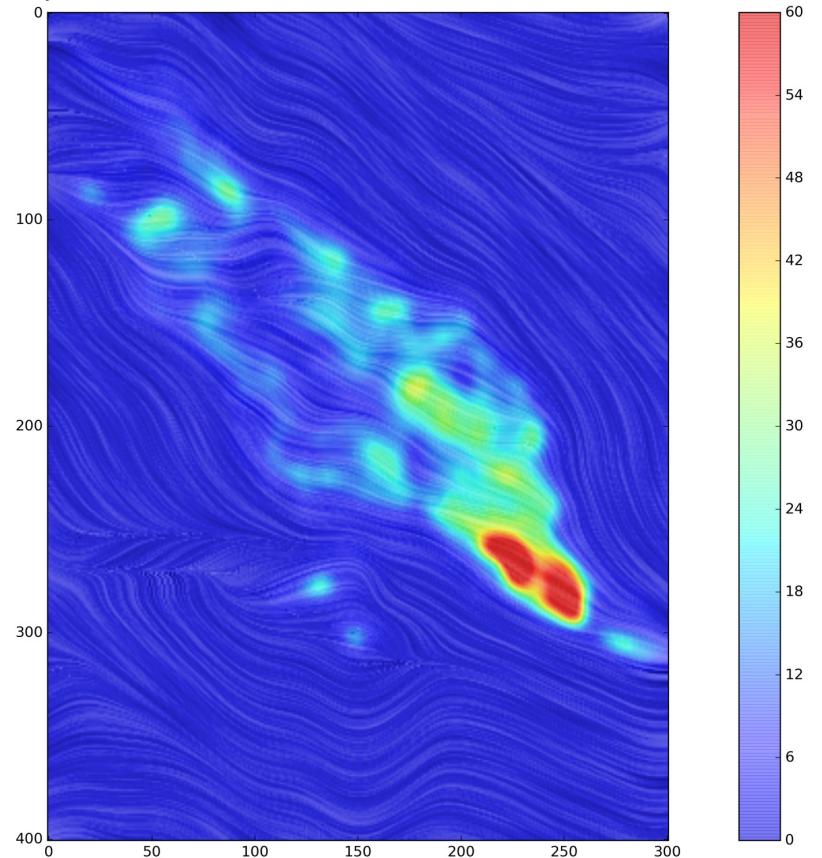
Gonsalvez-Casanova & AL 2018

Velocity gradients provide unique ways to study B-fields

3D structure of B-field with different tracers

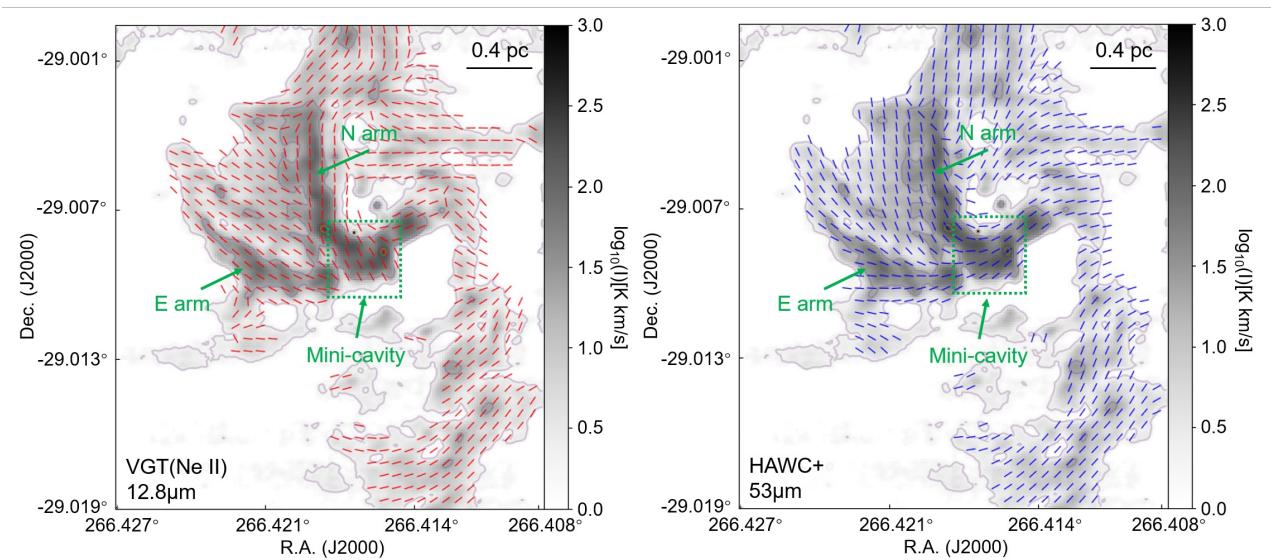


B-field of Smith high velocity cloud too faint for polarization

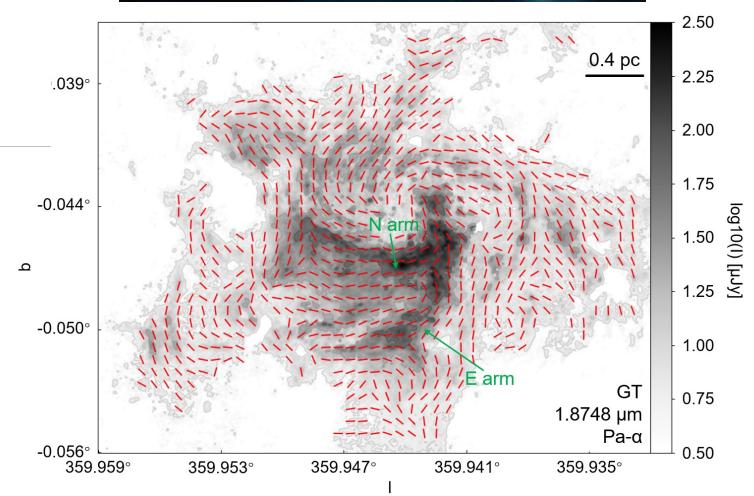
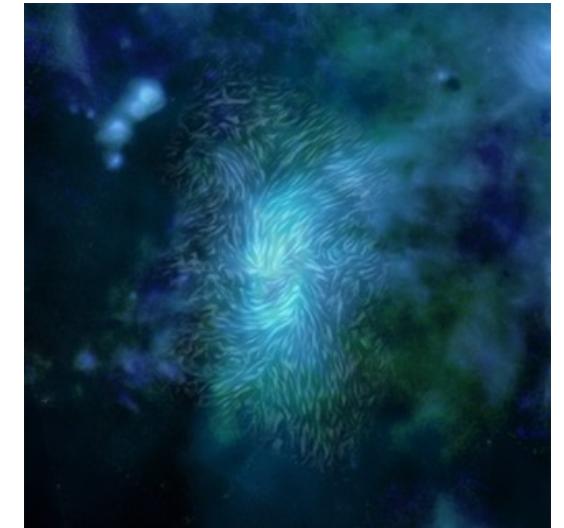


Hu et al. 2019

Gradients reveal that magnetic field in different phases varies in direction



Galactic center region



Hu, AL & Wang 2021

