

$$S_{lmn}^{\text{eff},\pm}(r) = \frac{1}{T_r} \int_0^{T_r} S_{lm}^{\text{eff},\pm}(t,r) e^{i\omega_{mn}t} dt$$