

$$\psi^{\mathcal{R}}_{lm}(t,r)=\lim_{N\rightarrow\infty}\sum_{n=-N}^N\psi^{\mathcal{R}}_{lmn}(r)e^{-i\omega_{mn}t}$$