

$$\rho_{lm}(t, r) = \frac{q \hat{C}_{lm} P_{\ell}^m(0)}{r_p(t)^2 u^t} \delta[r - r_p(t)] e^{-im\varphi_p(t)}$$