

$$\psi_{lm}^{R,\pm}(t,r)=\sum_{n=-\infty}^{\infty}\psi_{lmn}^{R,\pm}(r)e^{-i\omega_{mn}t}$$