

$$\tilde{\psi}_{lm}^{\pm}(t,r) \coloneqq \sum_{n=-\infty}^{\infty} \tilde{\psi}_{lmn}^{\pm}(r) e^{-i\omega_{mn}t}$$