

ETERNAL BINARIES

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26th Capra meeting @ Copenhagen

JAIME REDONDO-YUSTE

In collaboration with



V. Cardoso

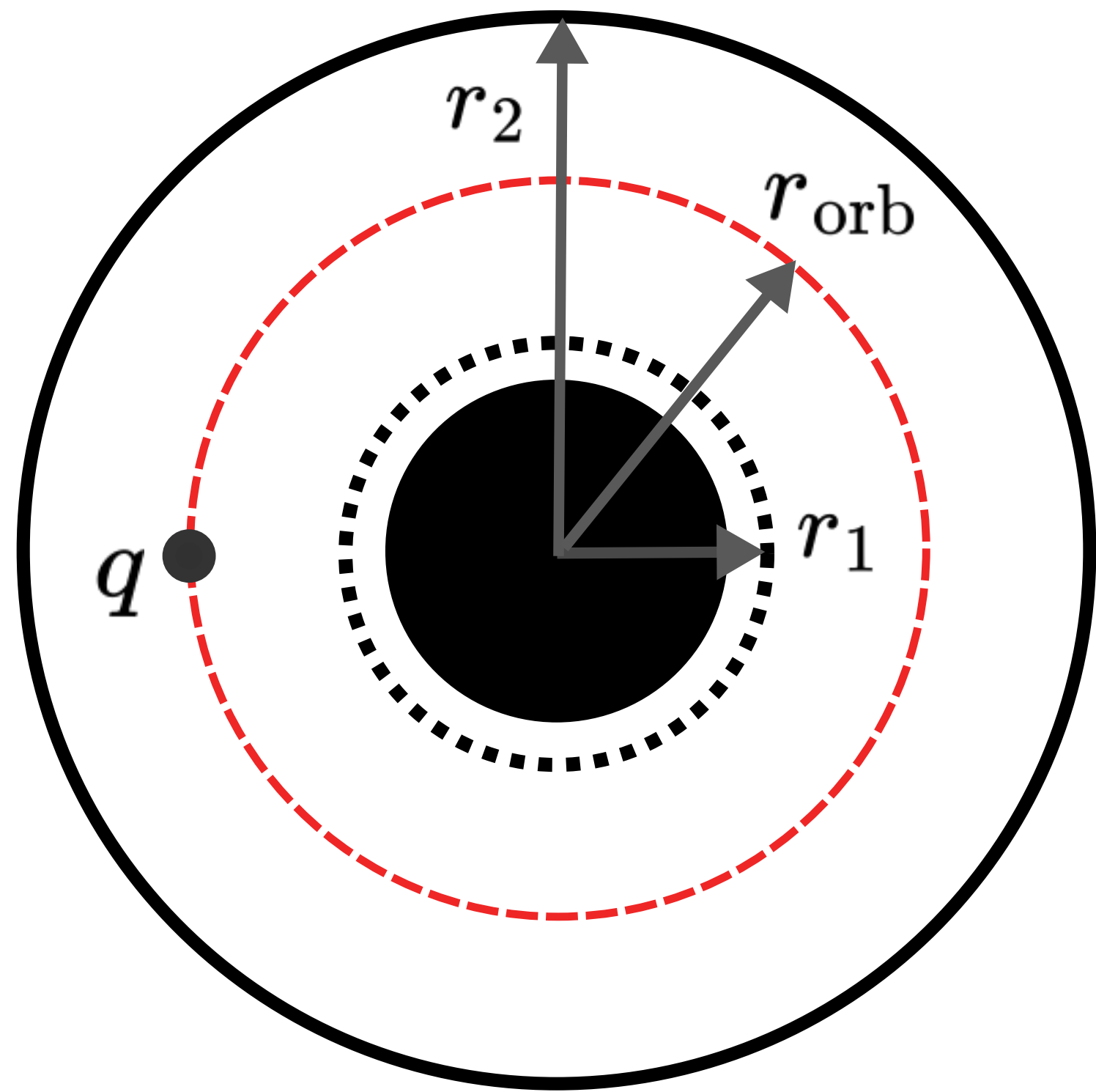


C. Macedo

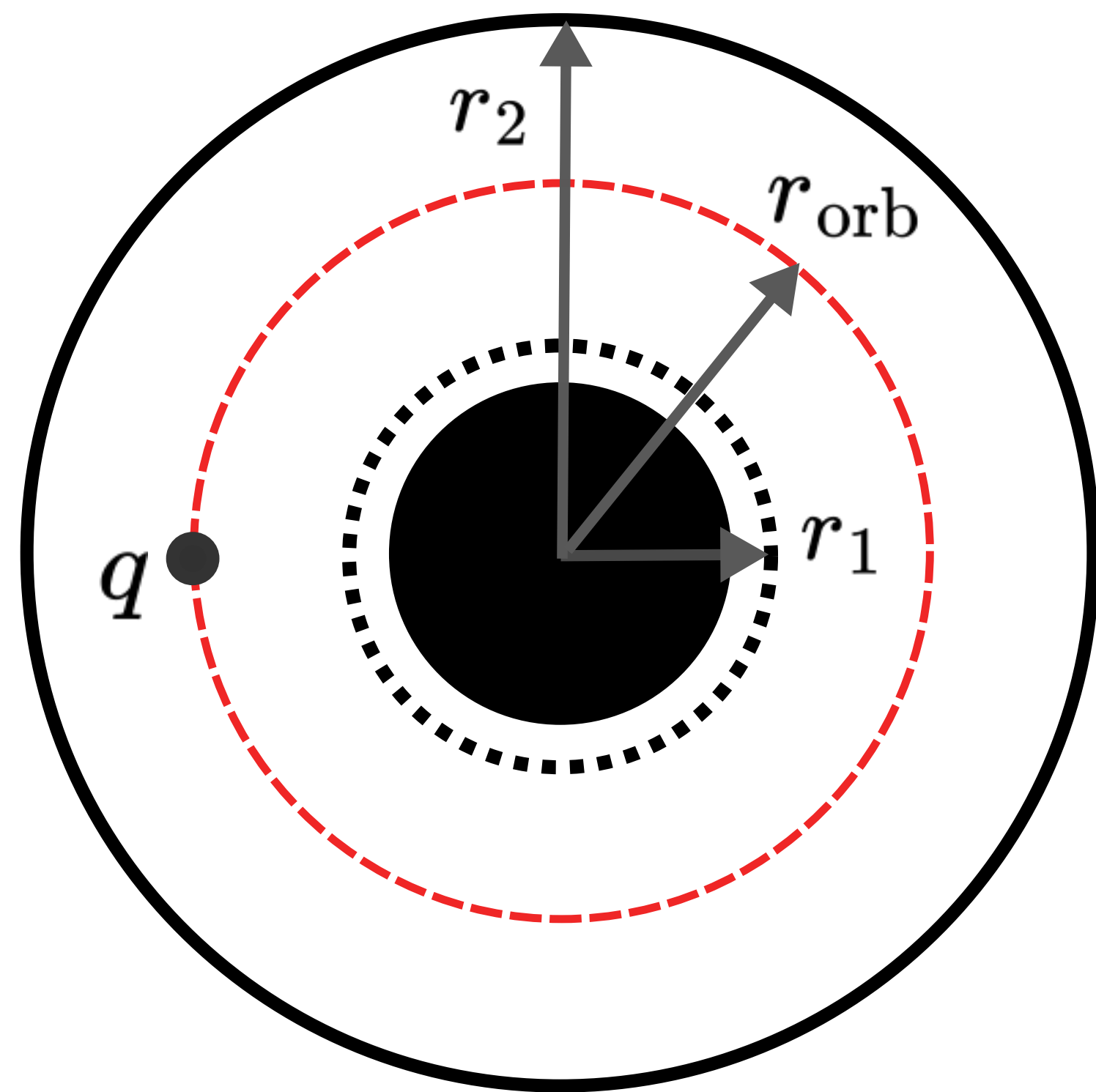


M. van de Meent

(Scalar) EMRI IN A BOX

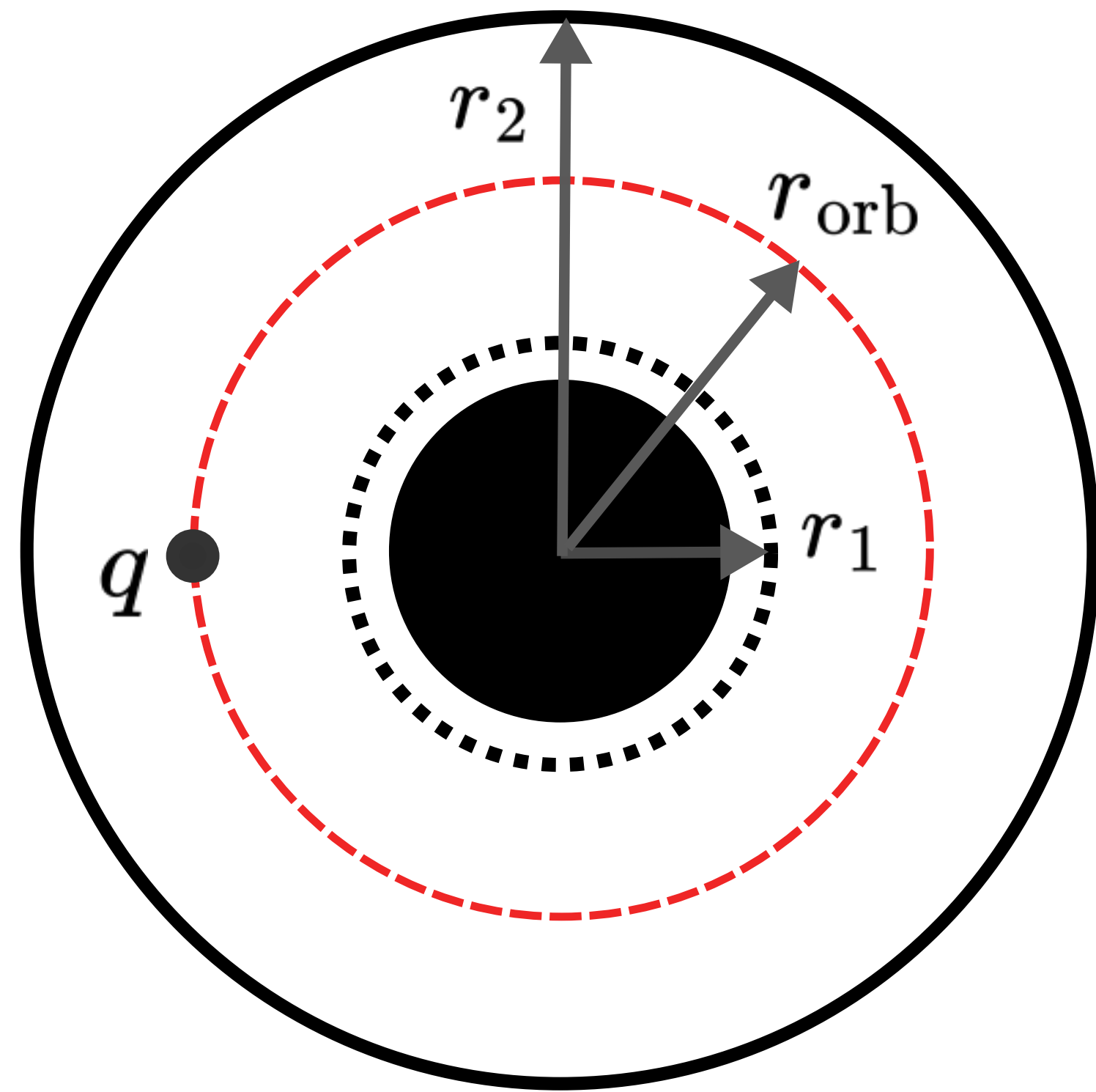


(Scalar) EMRI IN A BOX



? Dynamics governed by the conservative self-force

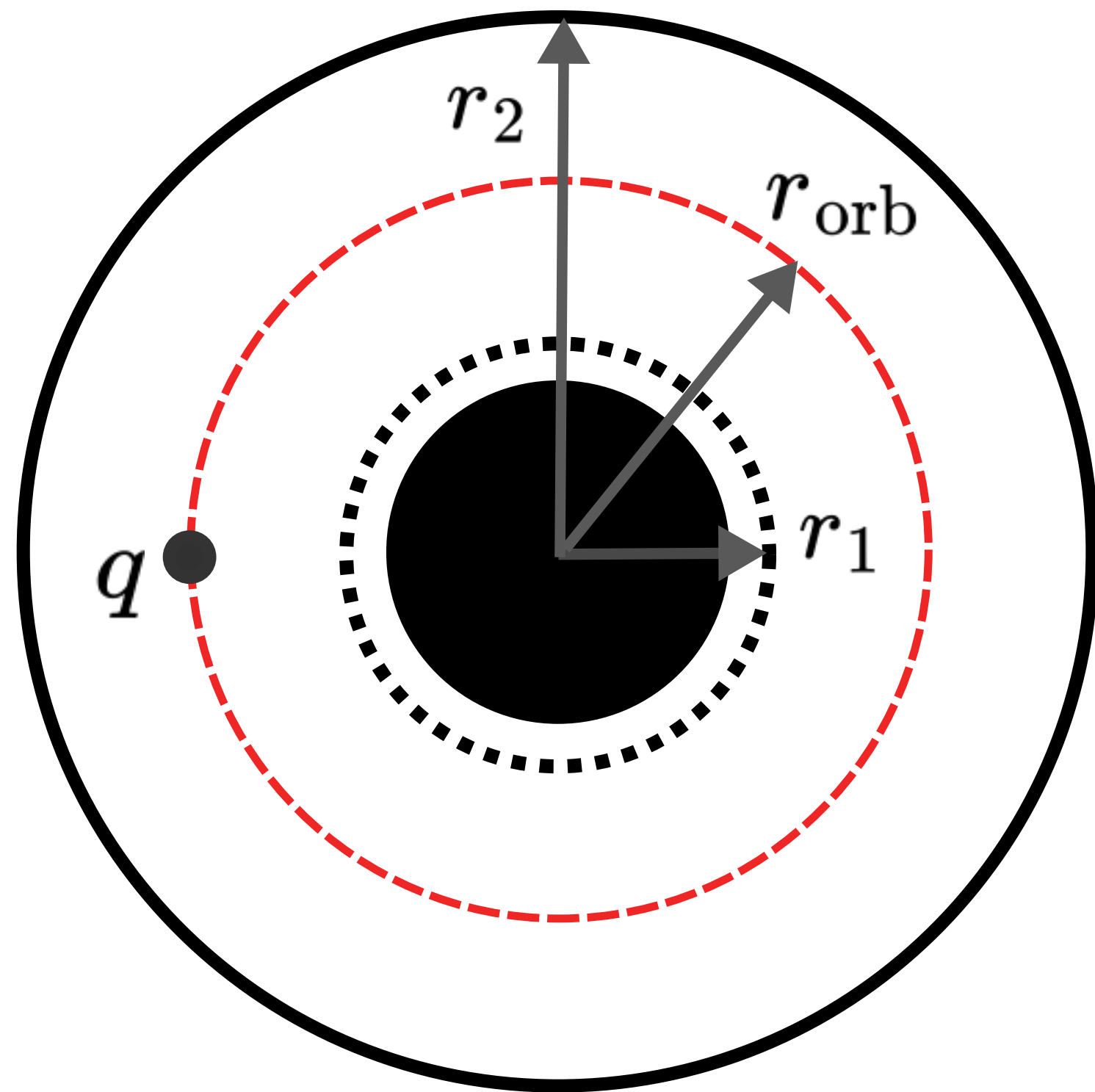
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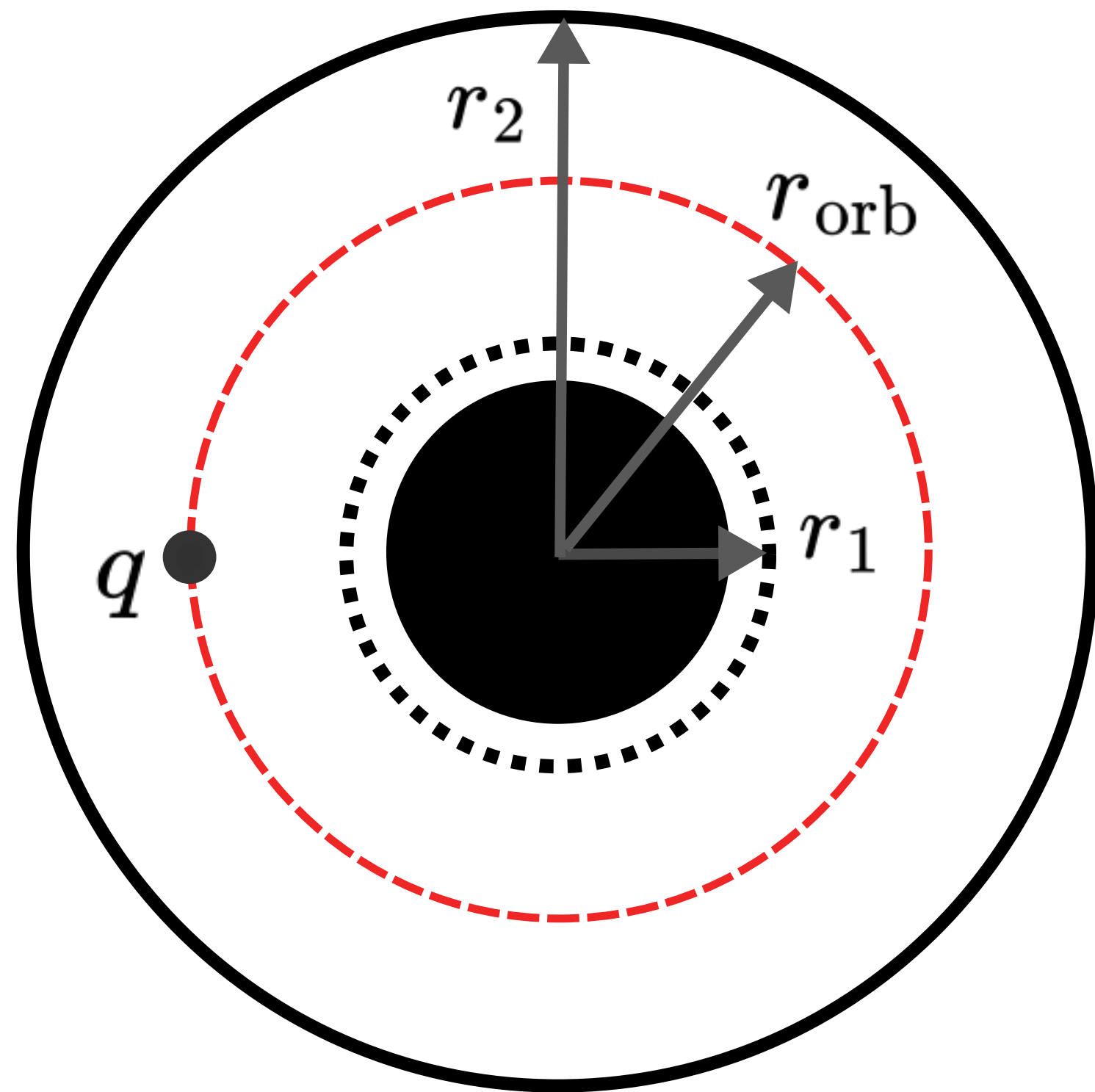
? No dissipation: are the orbits eternal?

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- ? Dynamics governed by the conservative self-force
- ? No dissipation: are the orbits eternal?
- ? Normal mode frequencies are real: what happens when $\omega_{lmn} = m\Omega$?

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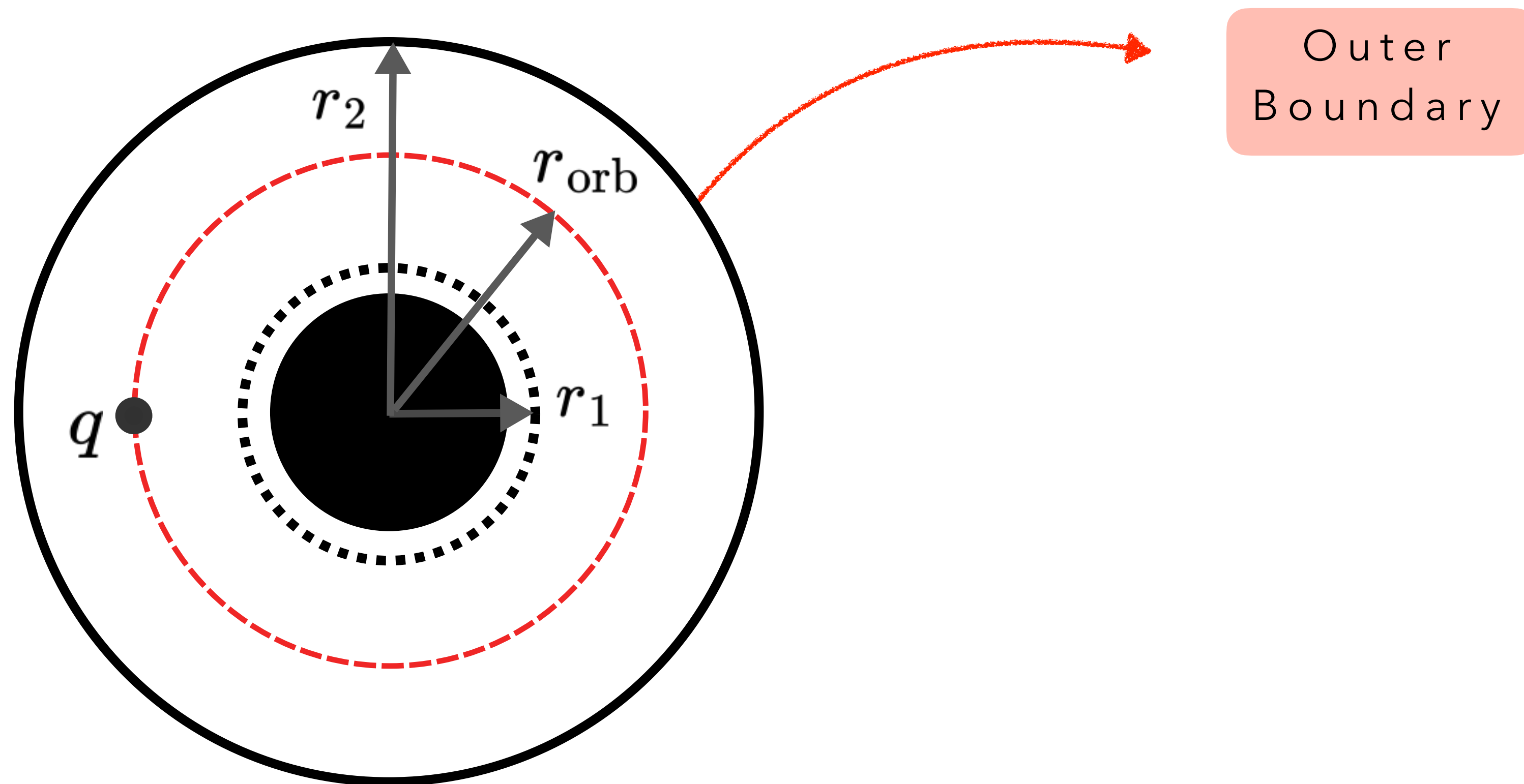
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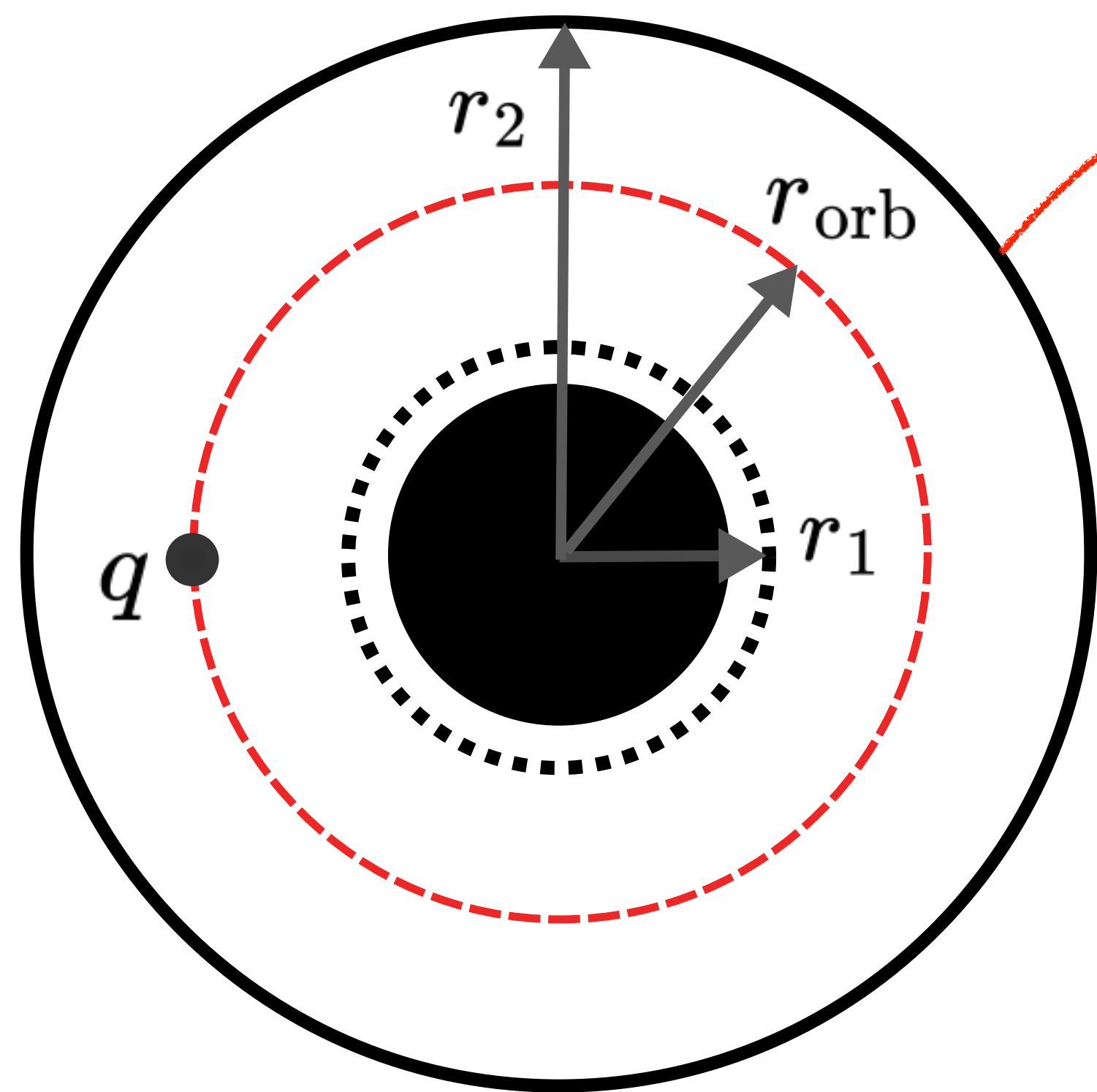
? Normal mode frequencies are real: what happens when $\omega_{lmn} = m\Omega$?

? Initial data does not leave the system

(Scalar) EMRI IN A BOX



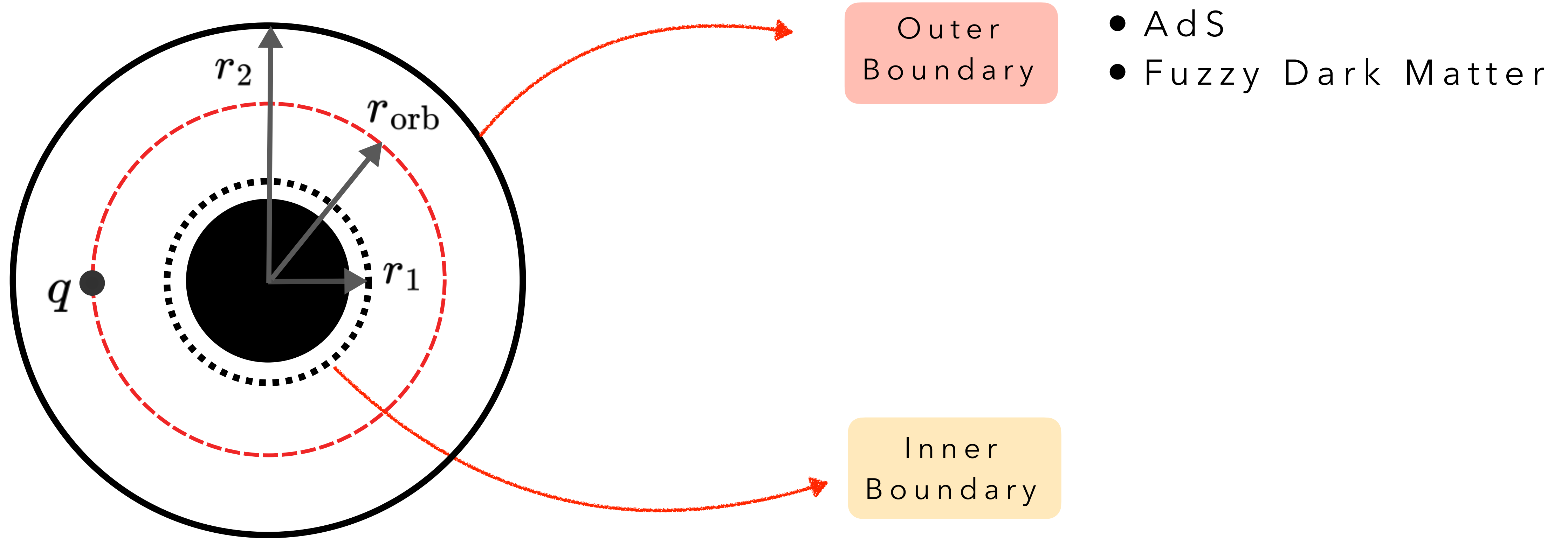
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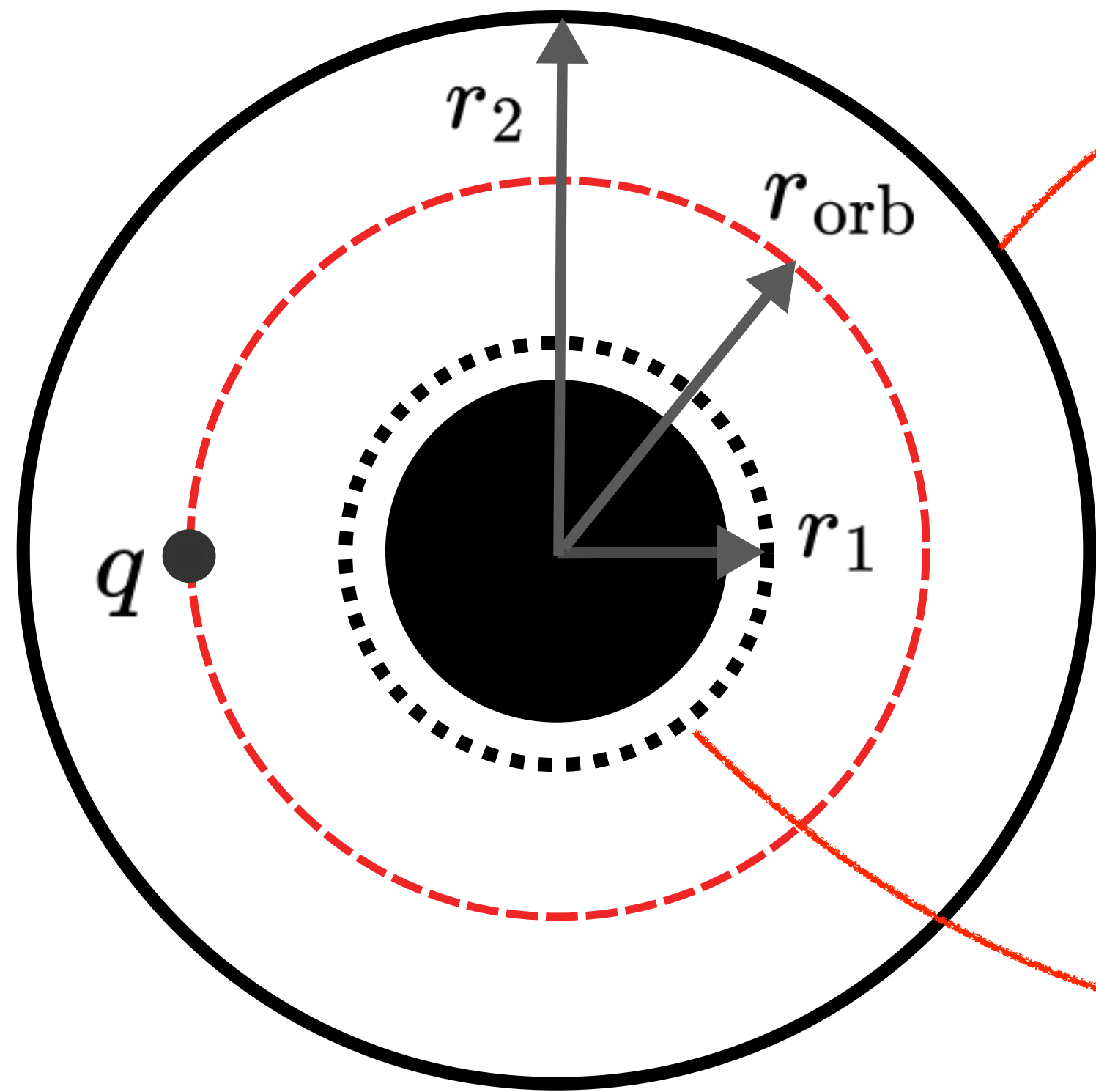
Outer
Boundary

- AdS
- Fuzzy Dark Matter

(Scalar) EMRI IN A BOX



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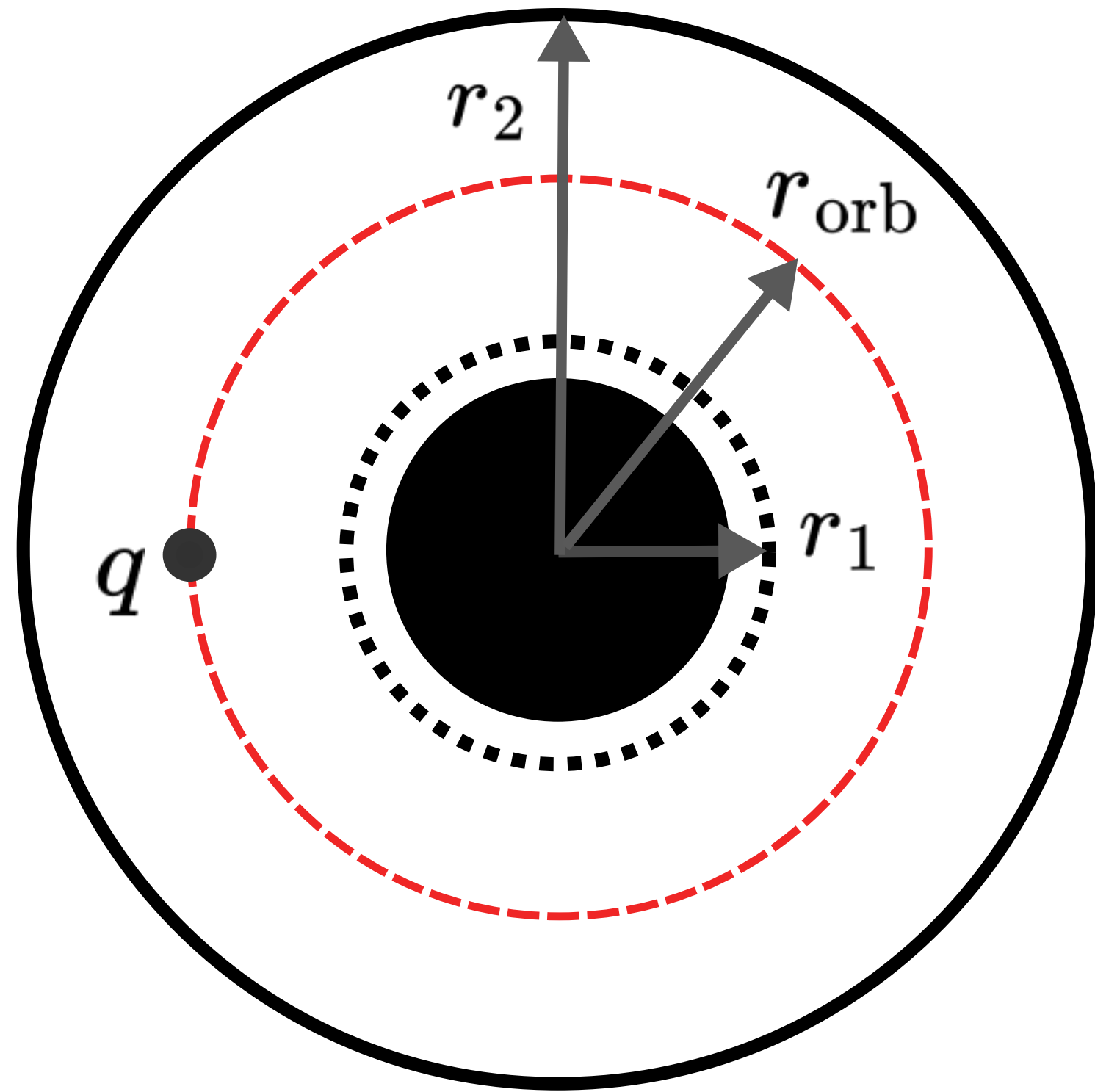
Outer
Boundary

- AdS
- Fuzzy Dark Matter

Inner
Boundary

- Compact stars
- Exotic compact objects

(Scalar) EMRI IN A BOX



EMRI $\longrightarrow m \ll M$

Charge $\longrightarrow q/m \ll 1$

Orbit $\longrightarrow r_{\text{orb}} \in [r_{\text{ISCO}}, r_2]$

Cavity $\longrightarrow R = r_2 - r_1$

RESULTS

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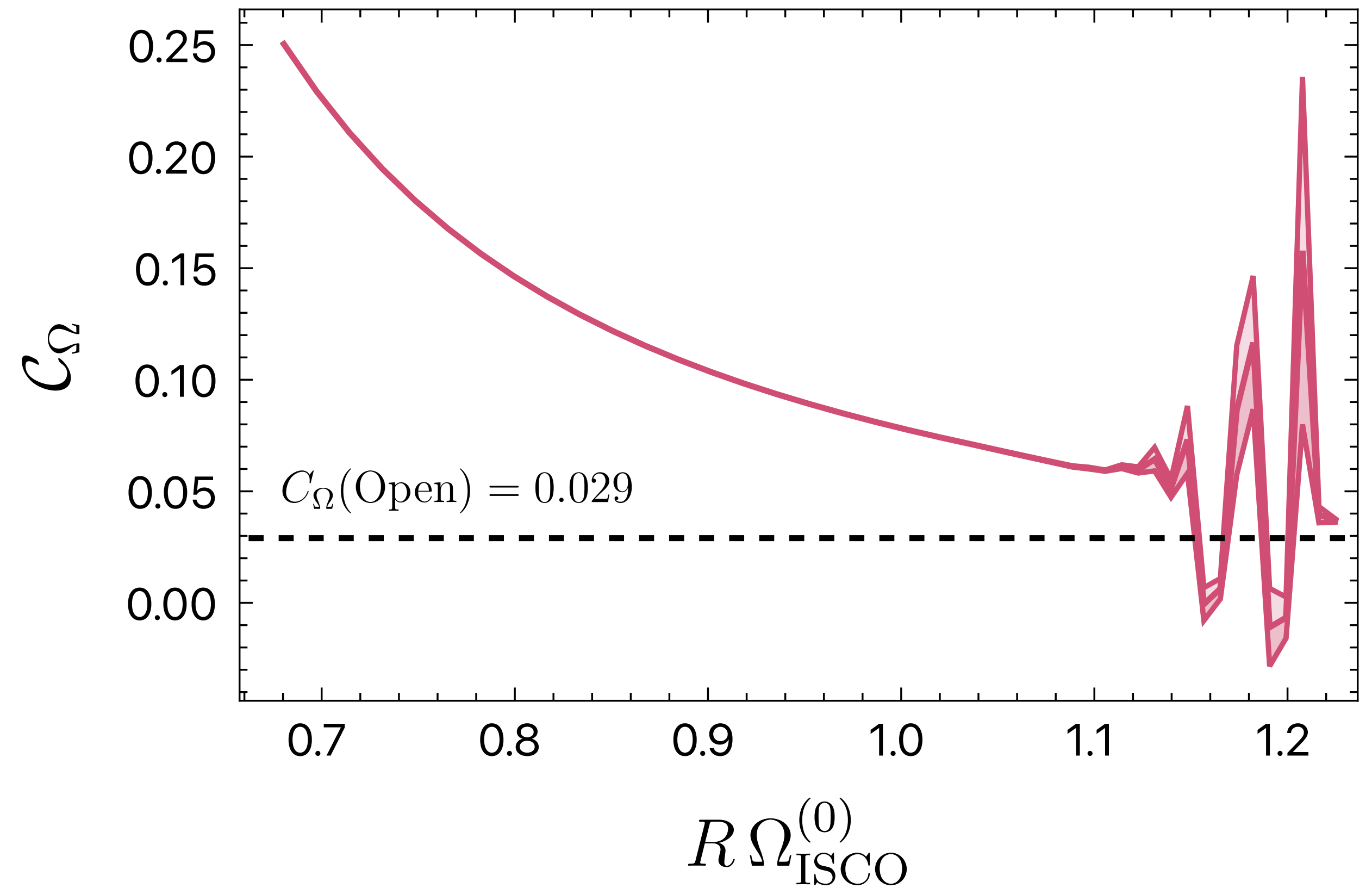
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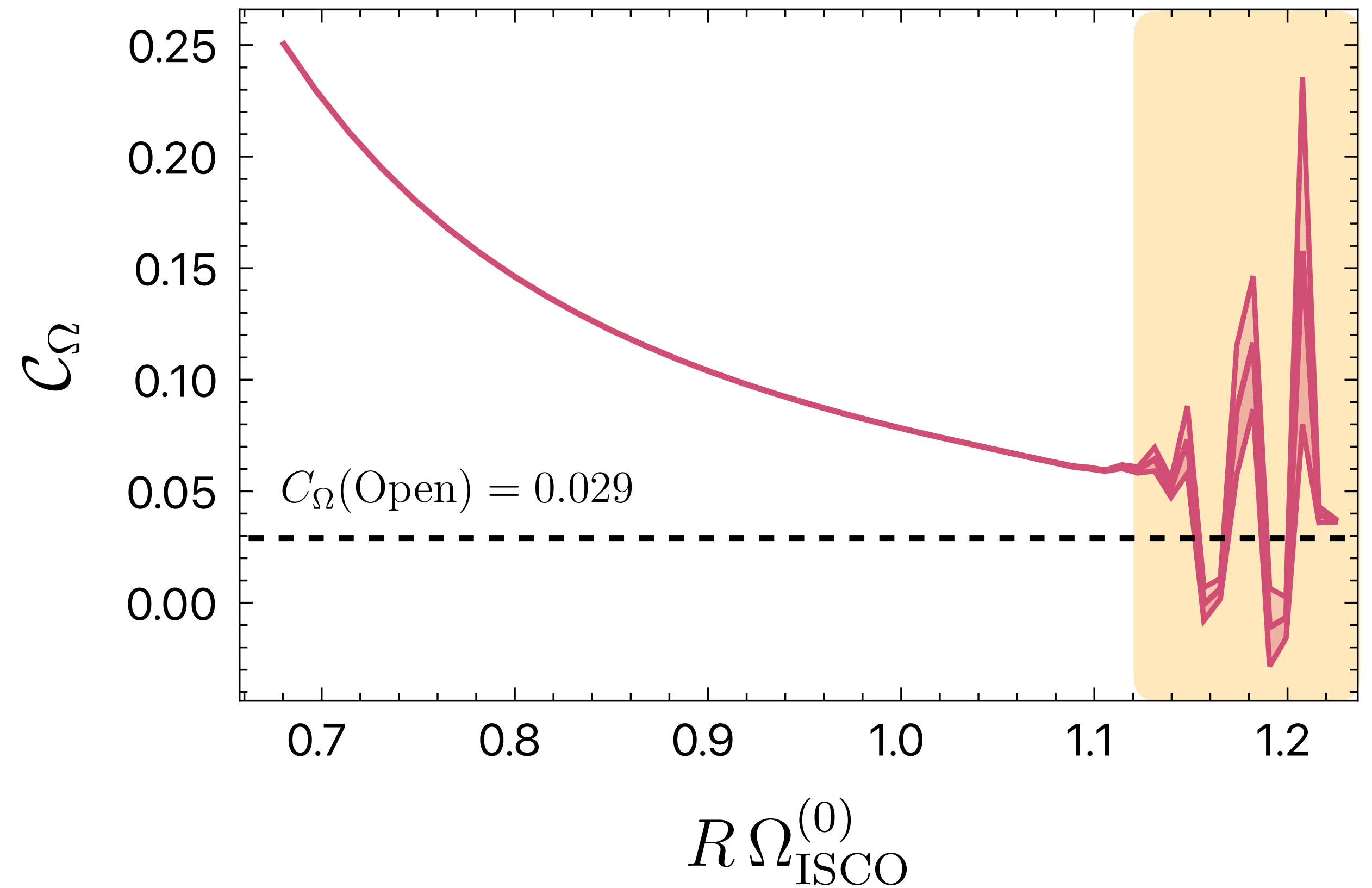
✓ Dissipative scalar self-force vanishes*

* Depends on the initial conditions!

✓ ISCO frequency shifts

✓ The system has **resonances**

(Only if the cavity is large enough)



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$$A_k = \phi_k^{\text{I}} + \frac{\pi_k^{\text{I}}}{i\omega_k} + \frac{S_k}{i(\omega_k - \Omega)}$$

RESULTS

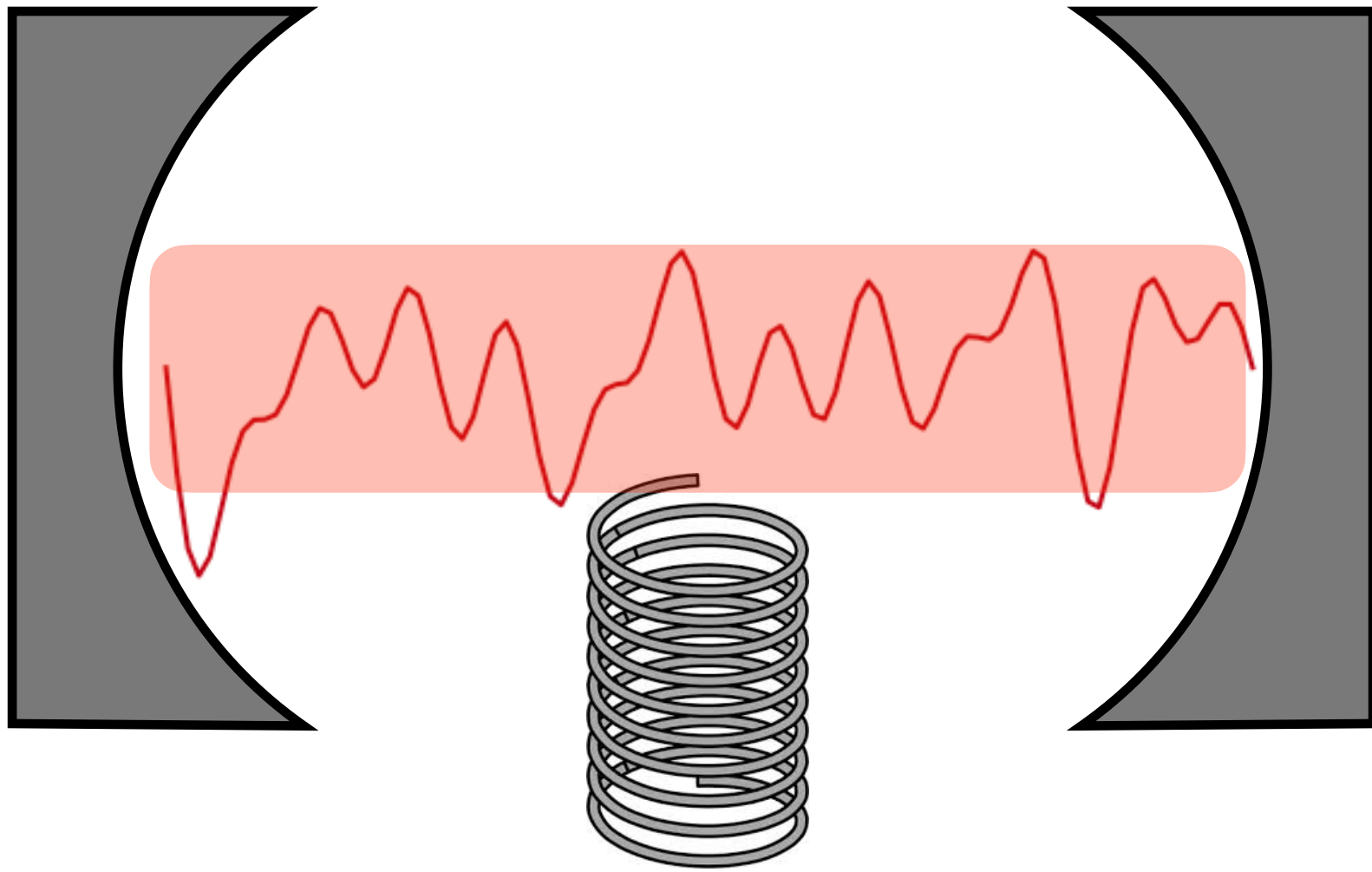
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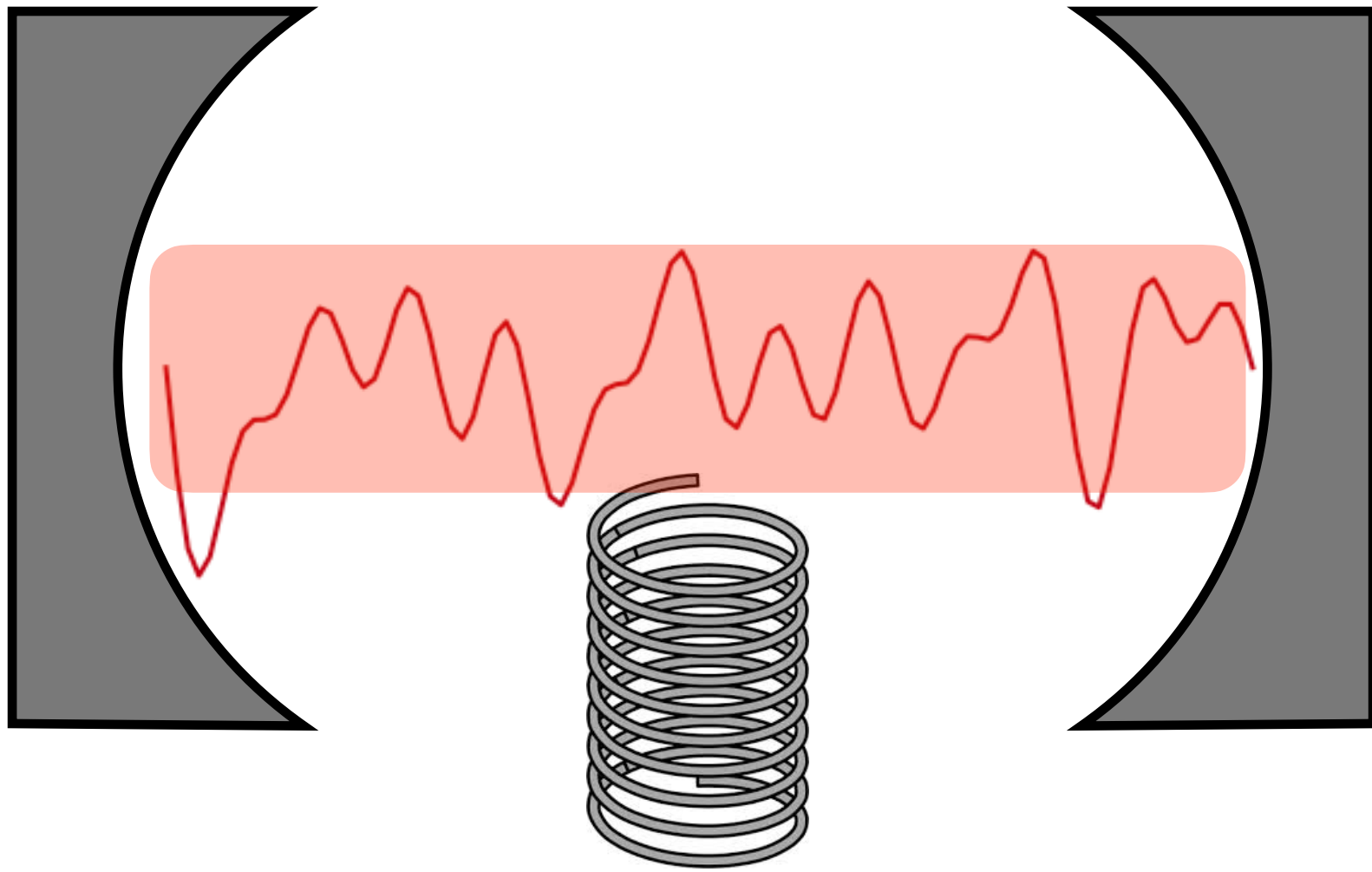
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TIME EVOLUTION MATTERS



$$H = H_{\text{Cavity}}(\pi, \phi) + H_{\text{Osc}}(p, q) - \frac{\varepsilon}{L} \cos\left(\frac{q}{L}\right) \int_0^L dx \frac{\phi(x) S(x)}{L}$$

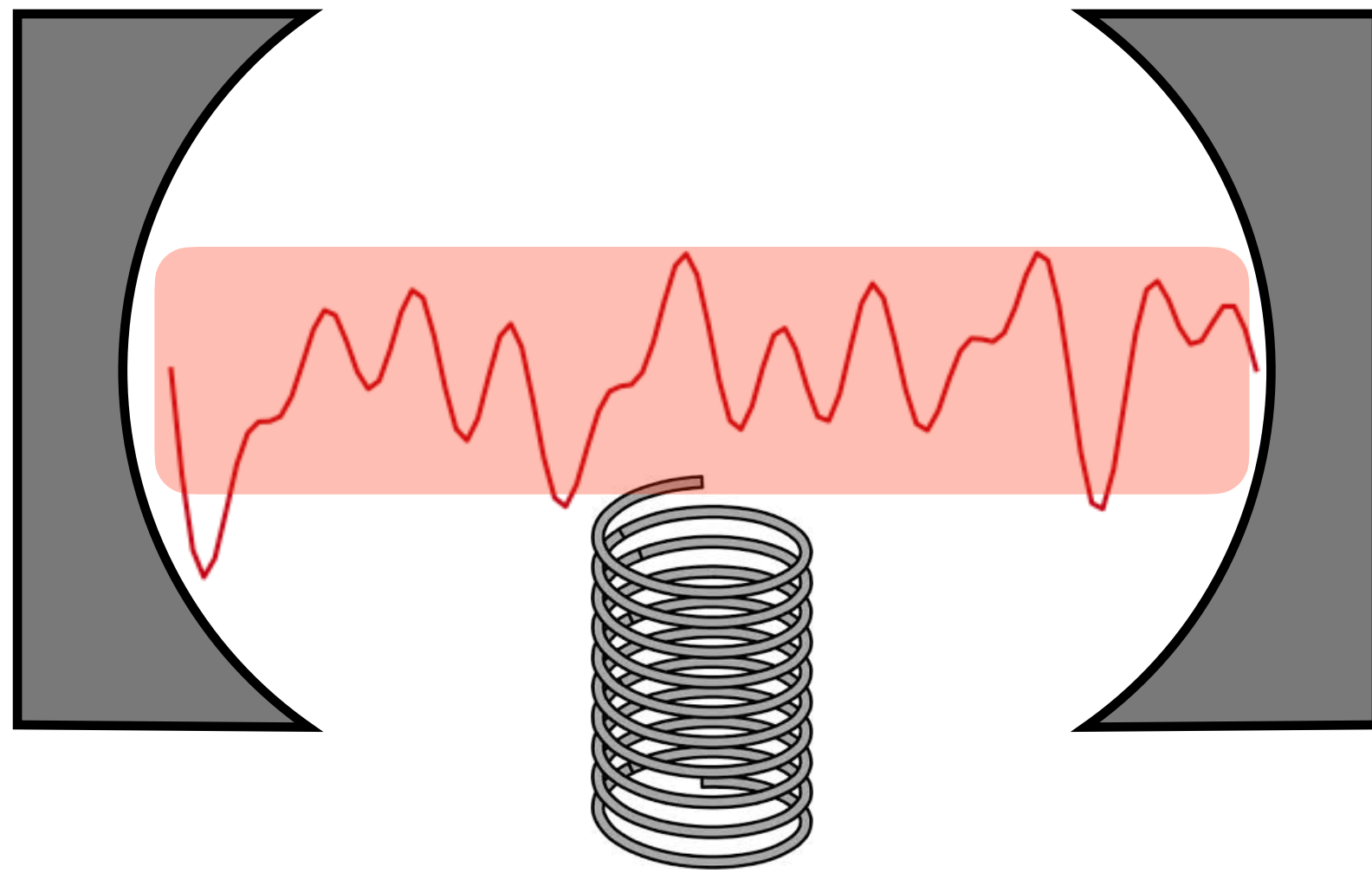
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Near Identity Transformation

TIME EVOLUTION MATTERS

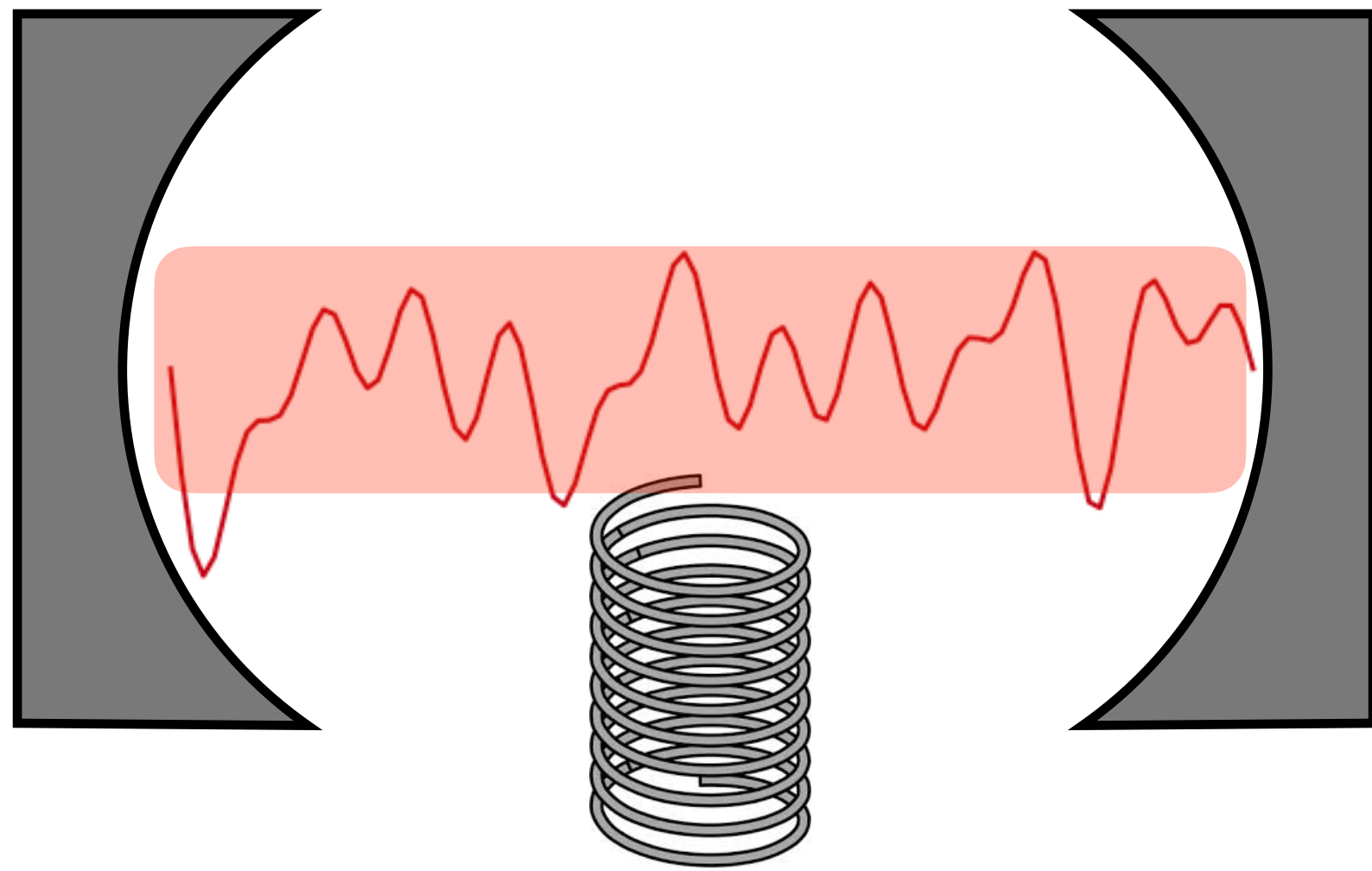


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Near Identity Transformation

$$p \xrightarrow{t \rightarrow \infty} p_0 + \frac{\varepsilon}{\omega - p_0} F^{(1)}(\phi_0, \omega) + \varepsilon^2 F^{(2)}(\phi_0, \omega)$$

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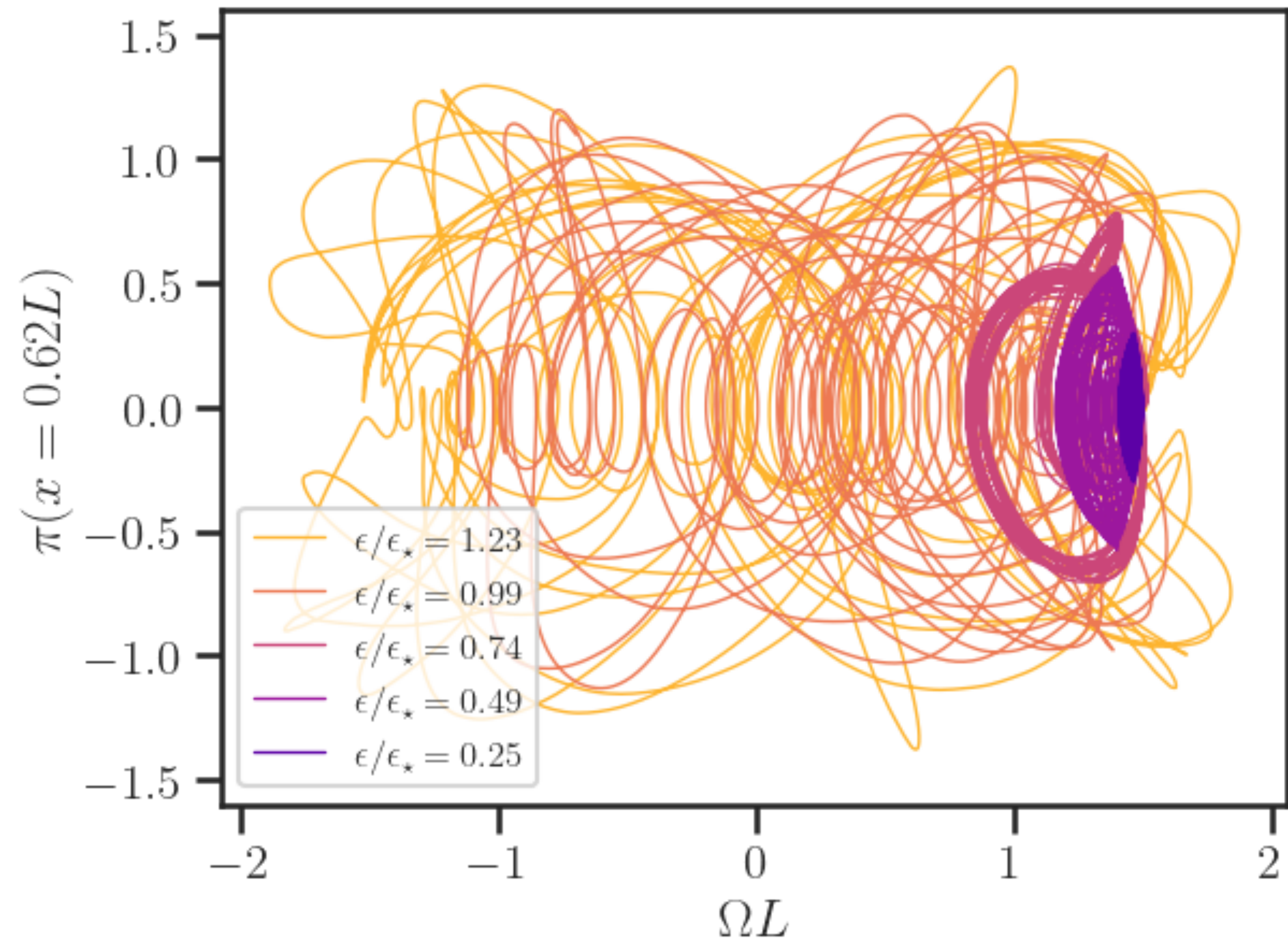
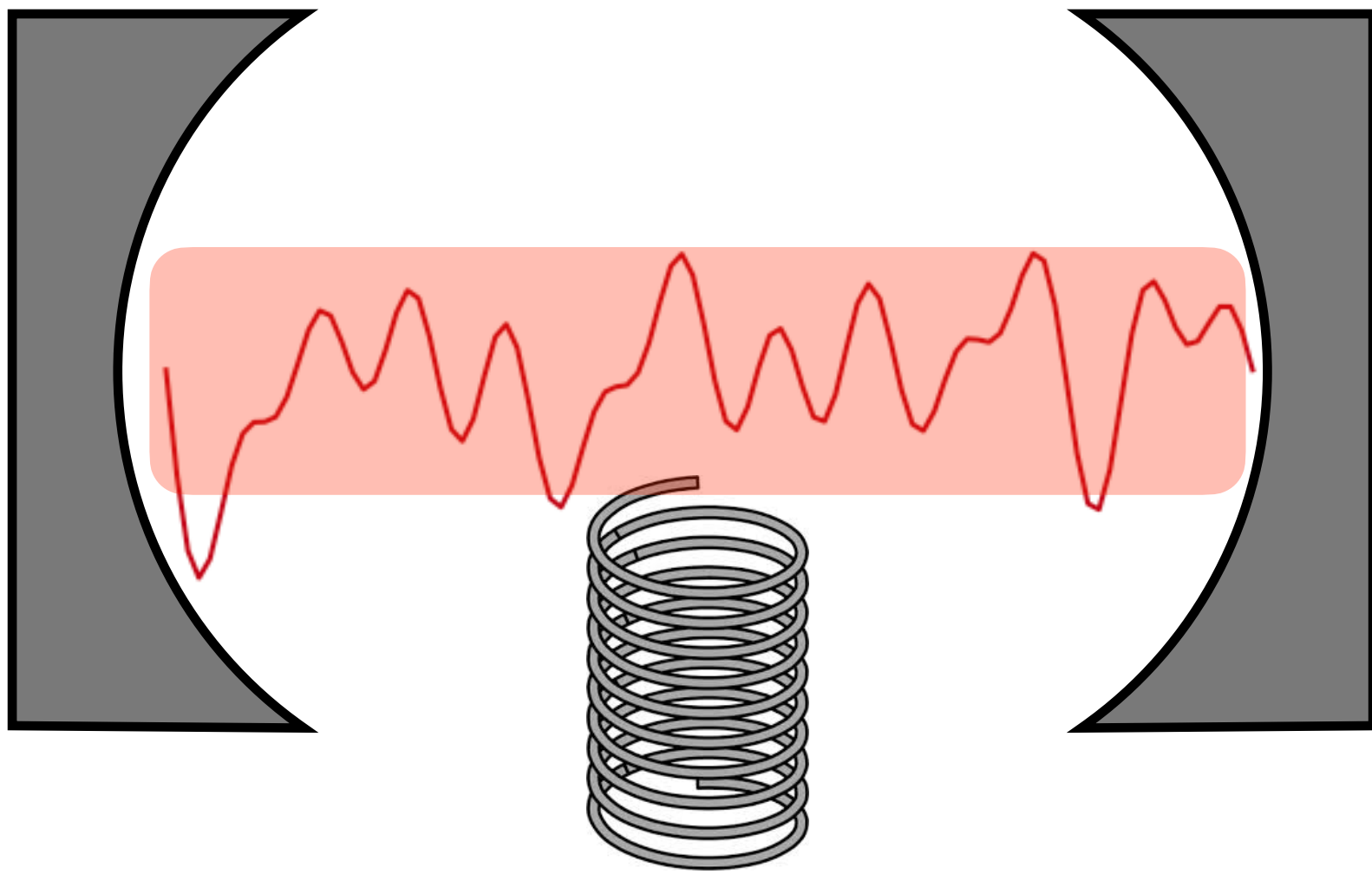
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There exists ICs such that the drift vanishes up to second order!

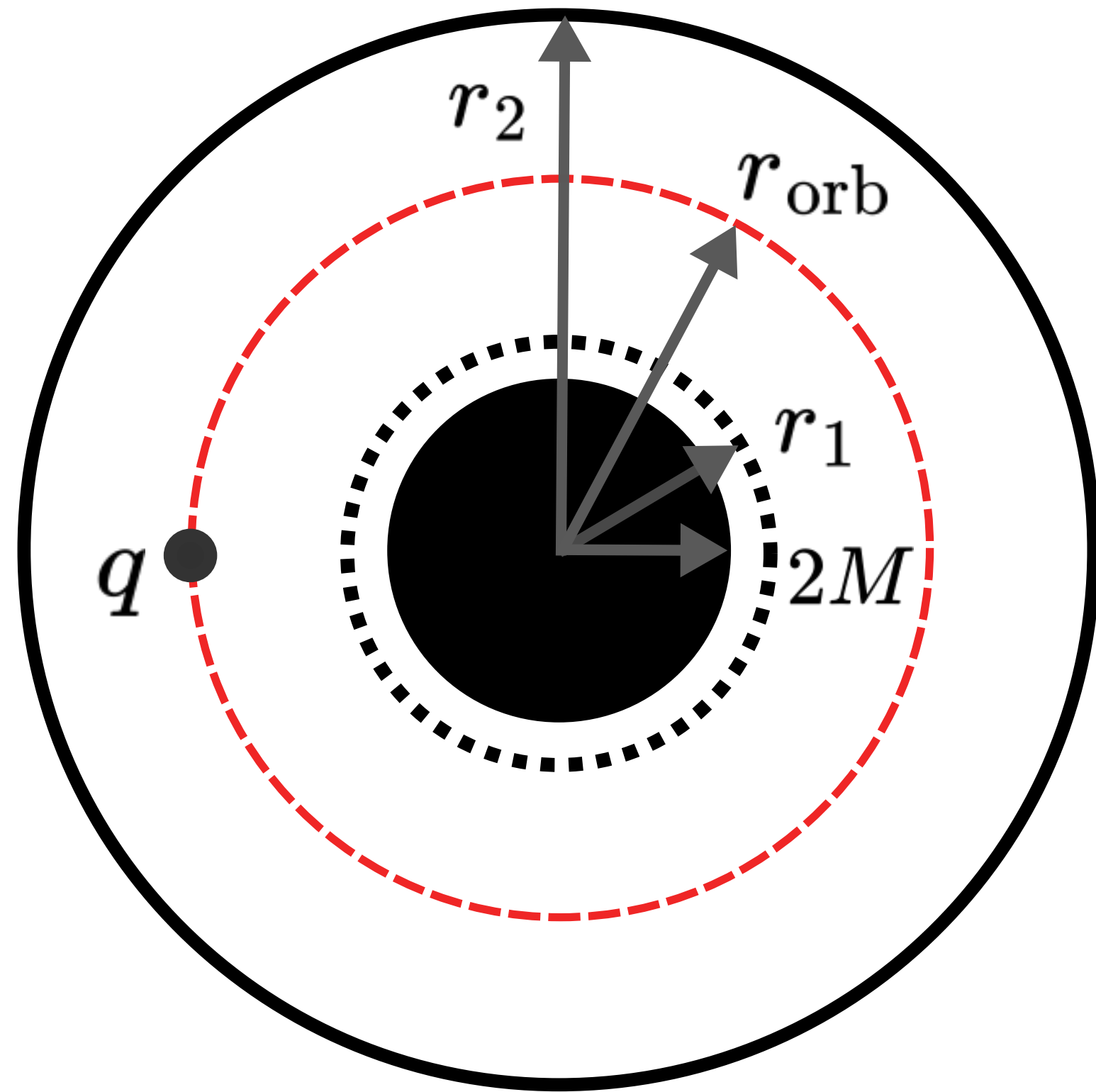
TIME EVOLUTION MATTERS



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$$\epsilon_*, \text{ s. t. } p - p_0 \sim |\omega_{n+1} - \omega_n|$$

POSSIBLE OUTCOMES



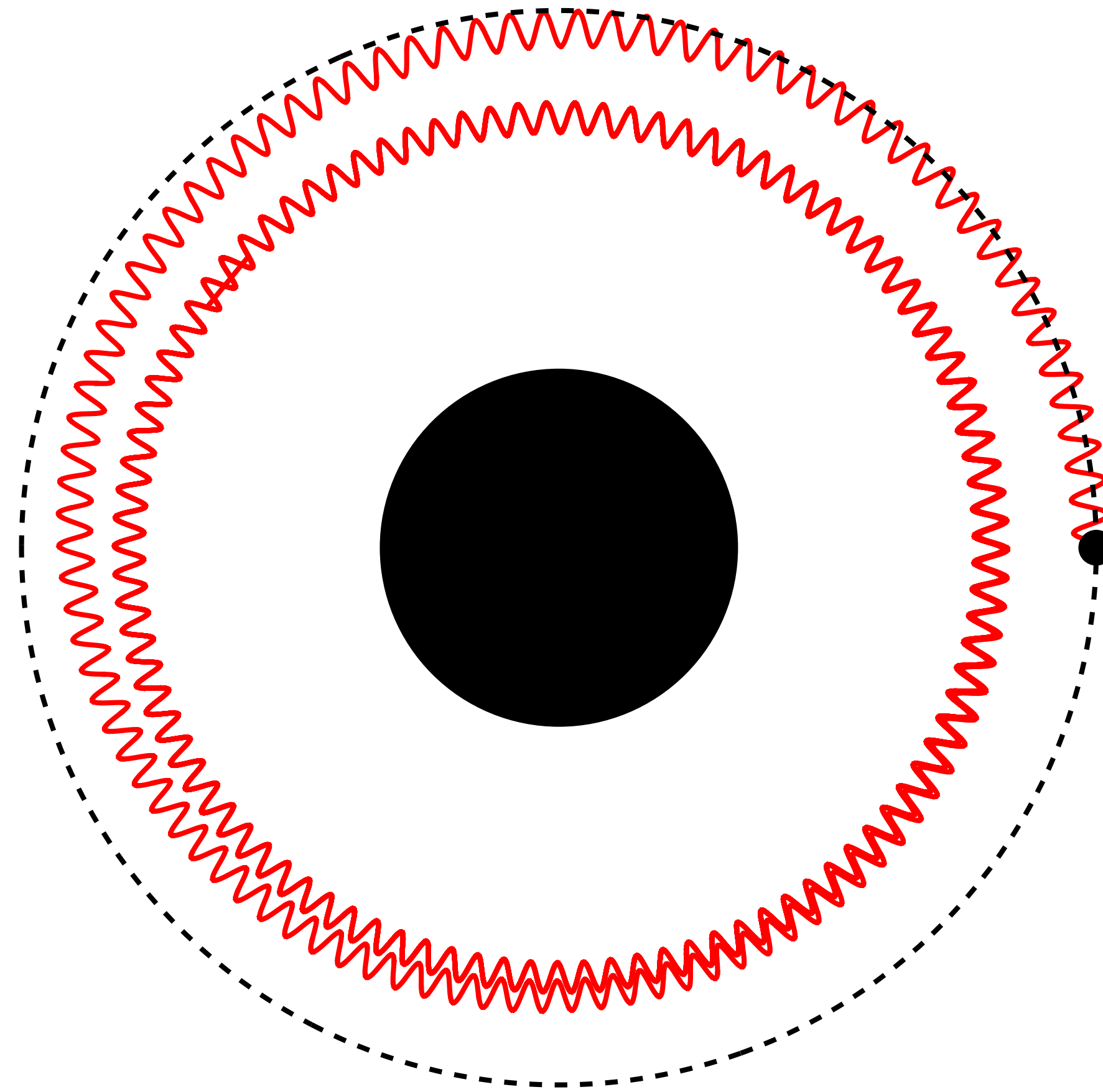
I. Eternal Orbit

II. Chaos

III. Merger

POSSIBLE OUTCOMES

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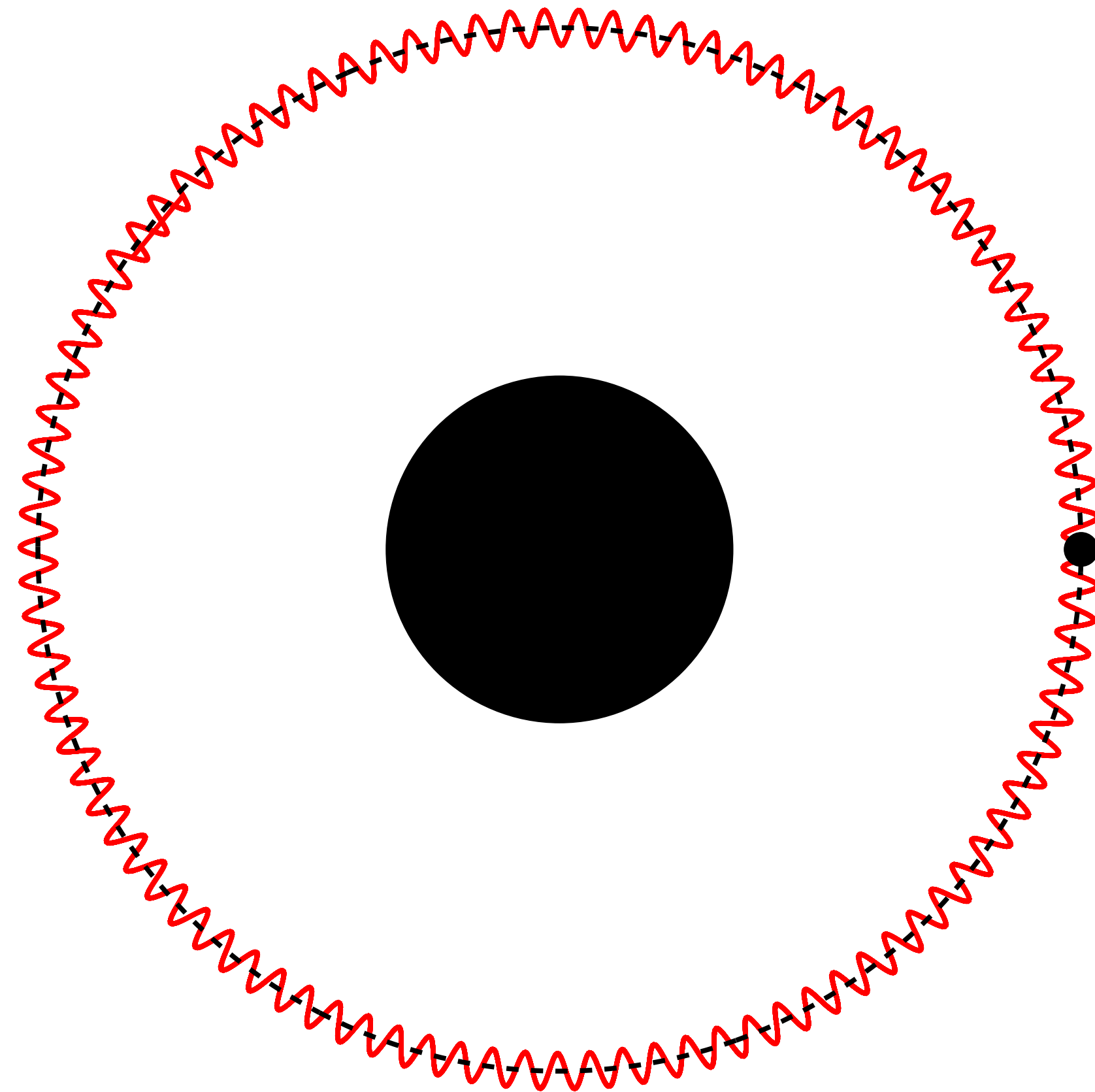


Fast dynamics
+ secular drift

POSSIBLE OUTCOMES

I. Eternal Orbit

+ fine-tuned initial
conditions

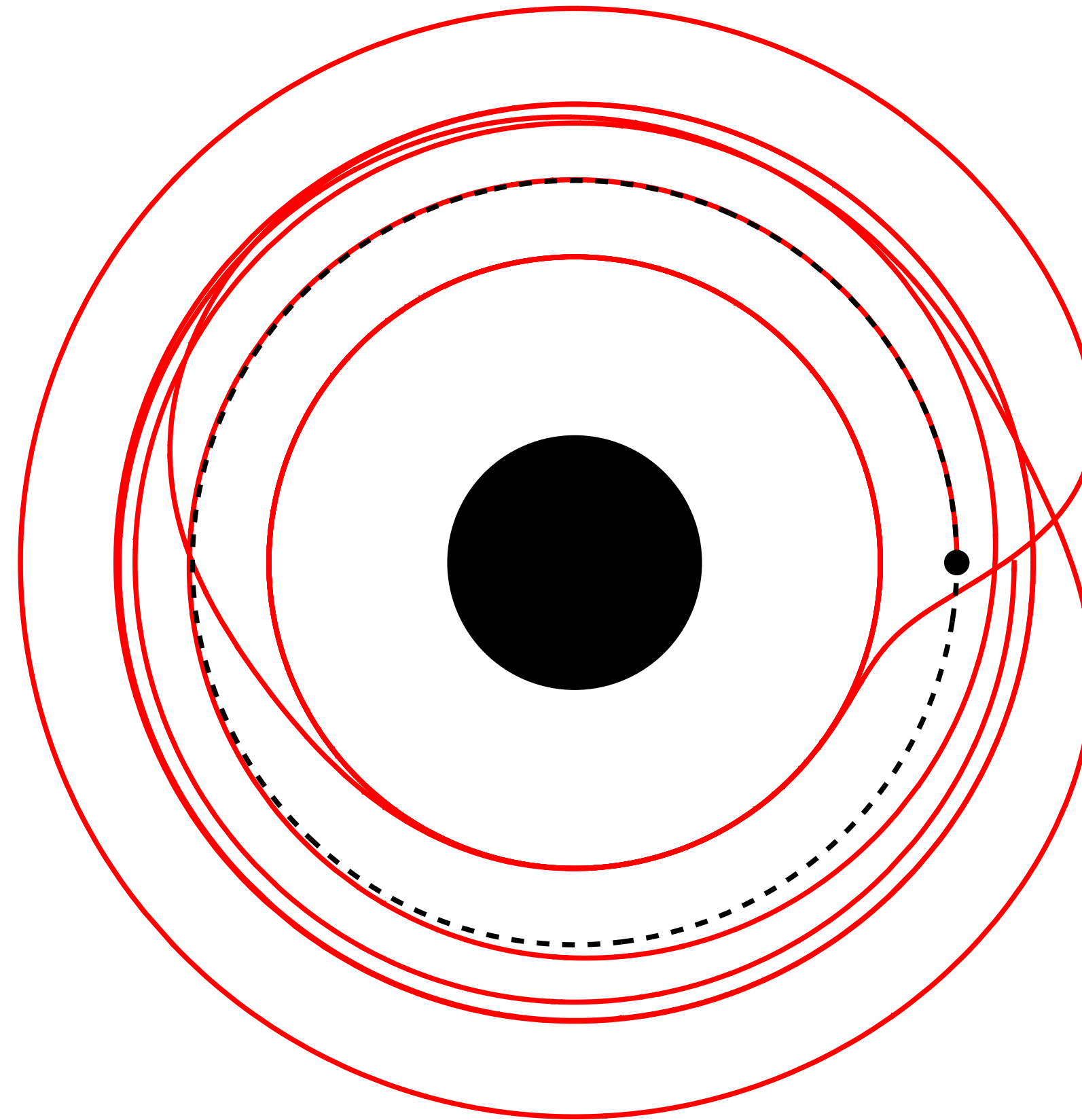


Fast dynamics
No secular piece

POSSIBLE OUTCOMES

II. Chaos

Only if the cavity is large enough



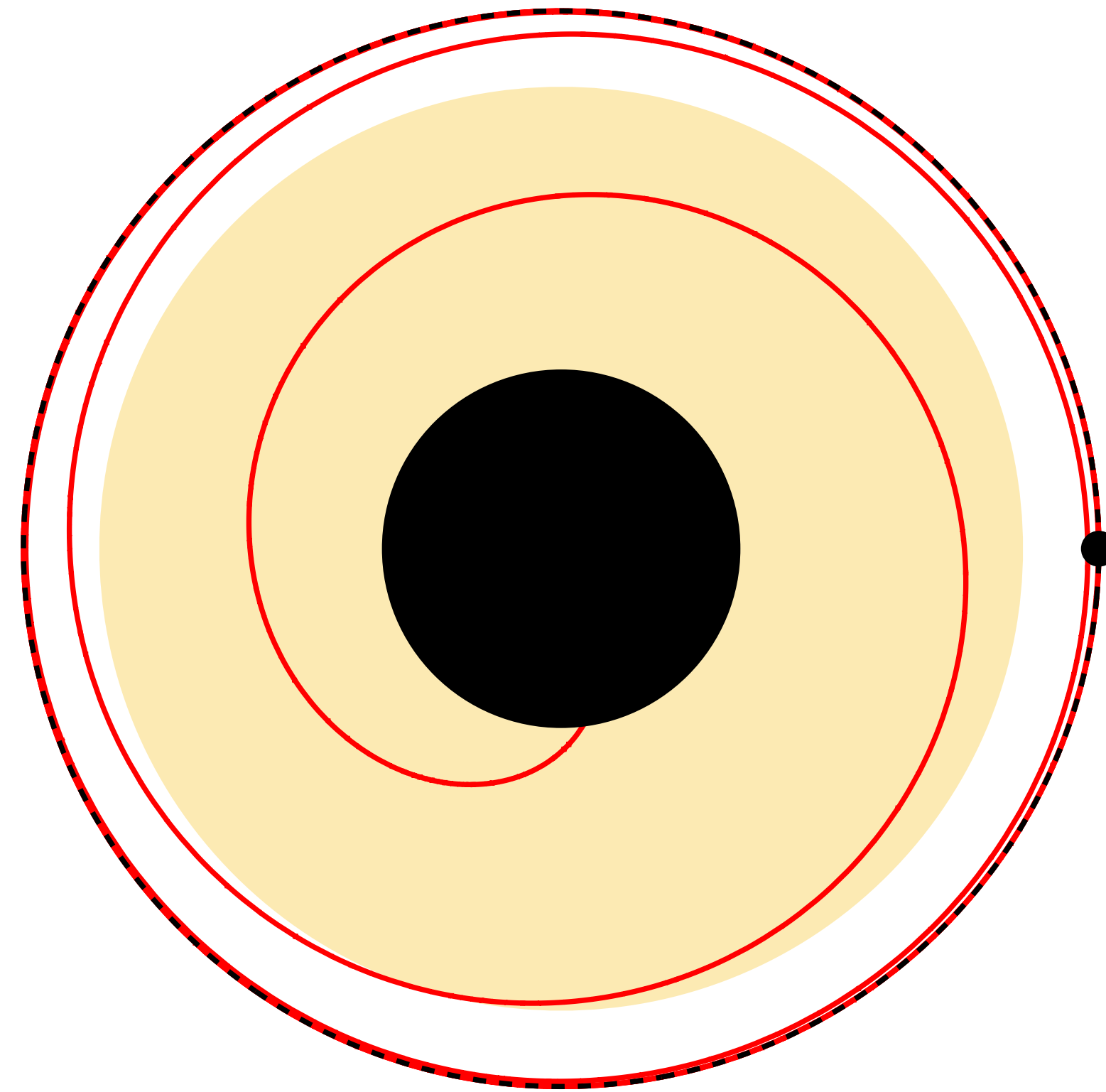
Needs large q/m

– or –

Starting close to a resonant orbit

POSSIBLE OUTCOMES

III. Merger

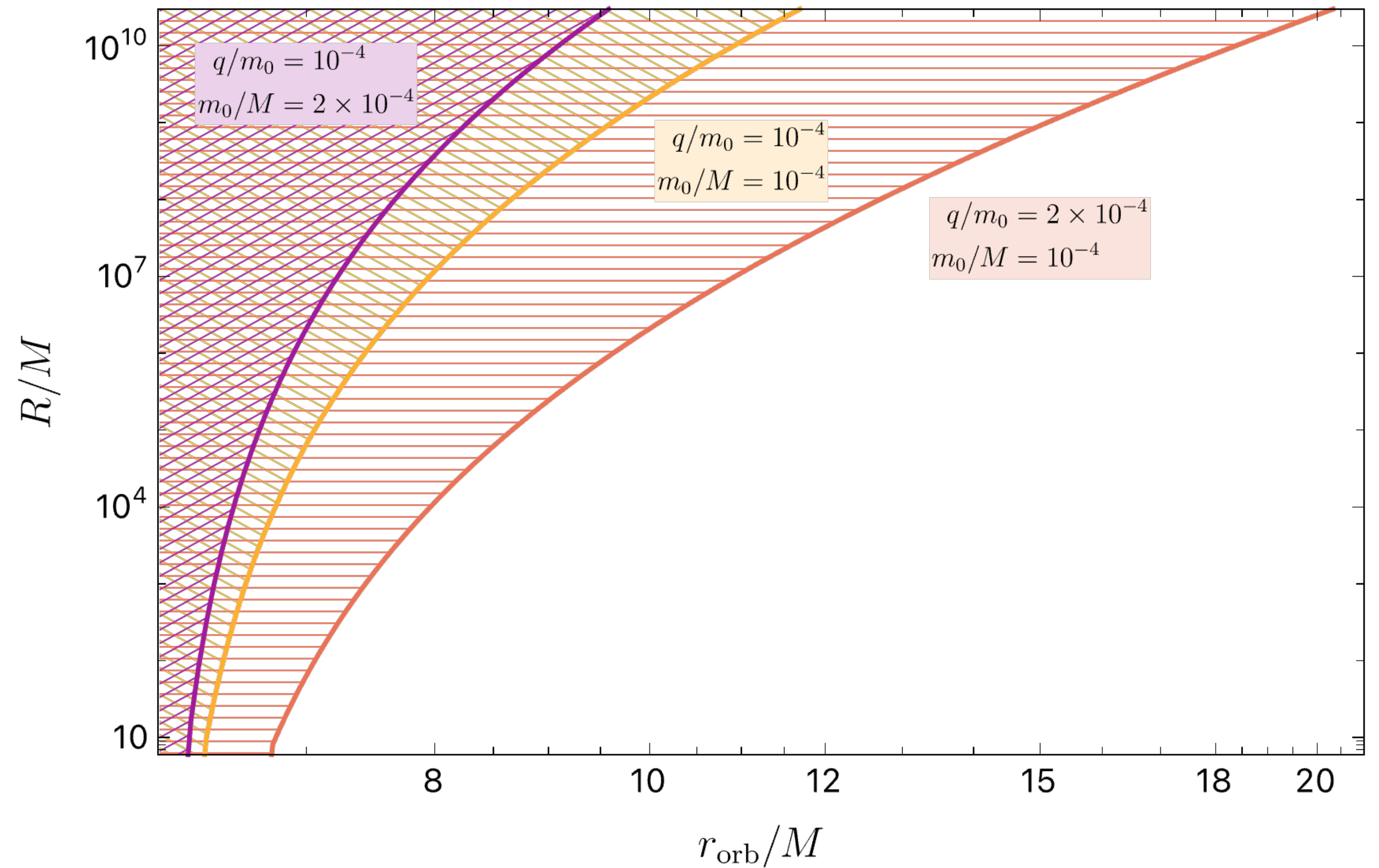


POSSIBLE OUTCOMES

III. Merger

If initially in vacuum

$$\frac{q}{m} \lesssim \sqrt{\frac{M}{m}} \left(\frac{R}{M}\right)^{\frac{1}{10}} \left(\frac{M}{r_{\text{orb}} - r_{\text{ISCO}}}\right)^{\frac{3}{4}}$$



TAKE-AWAYS

- Closed systems are useful to illustrate **conservative effects**
- There is astrophysical & theoretical motivation
- Secular effects appear depending on the **initial conditions**
- Resonances can drastically impact the dynamics: **chaos(?)**
- **Problem of scales**: large cavities have richer possibilities