



Exploring the Dark Universe with gravitational waves

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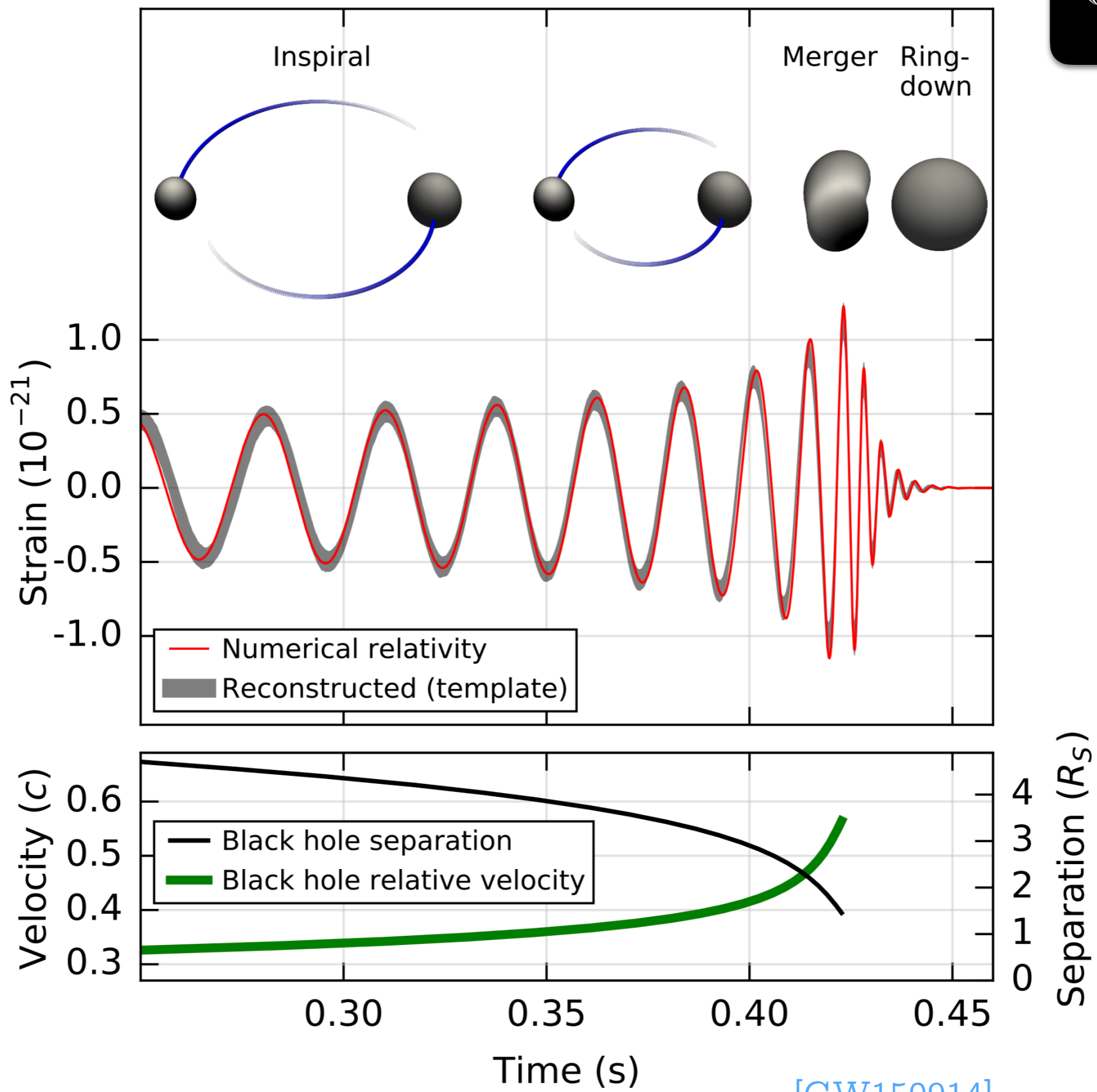
ezquiaga.github.io

VILLUM FONDEN

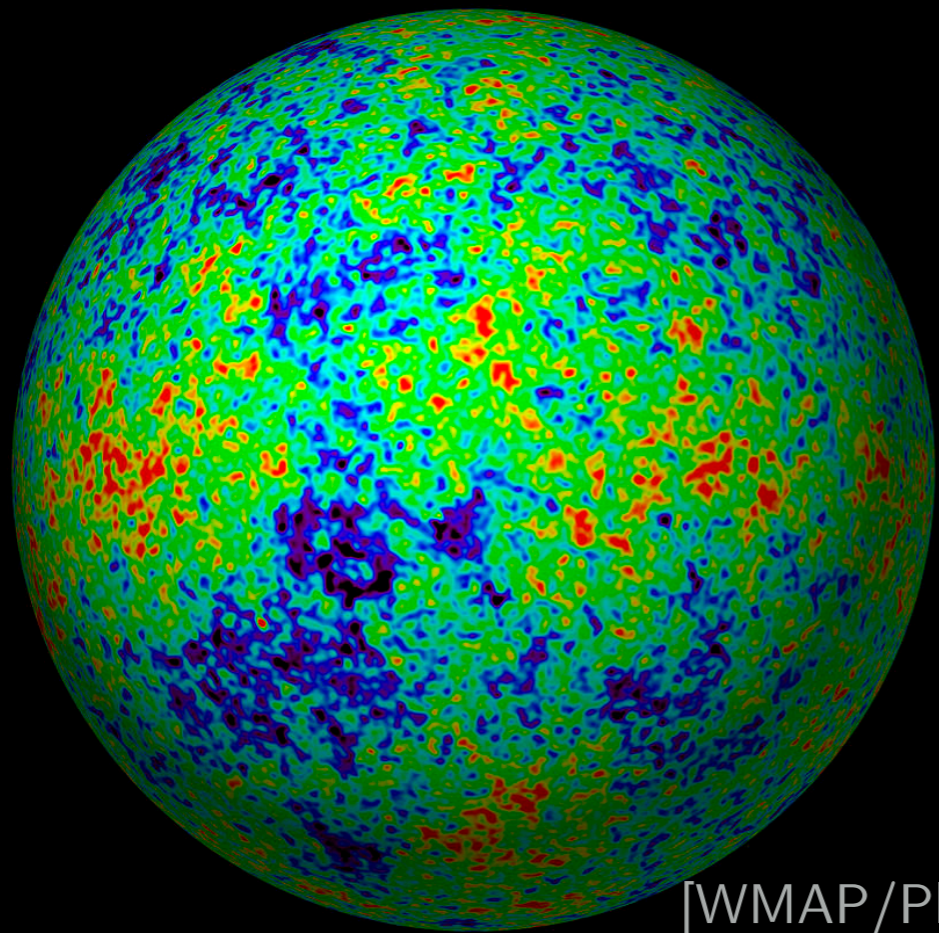


KØBENHAVNS
UNIVERSITET

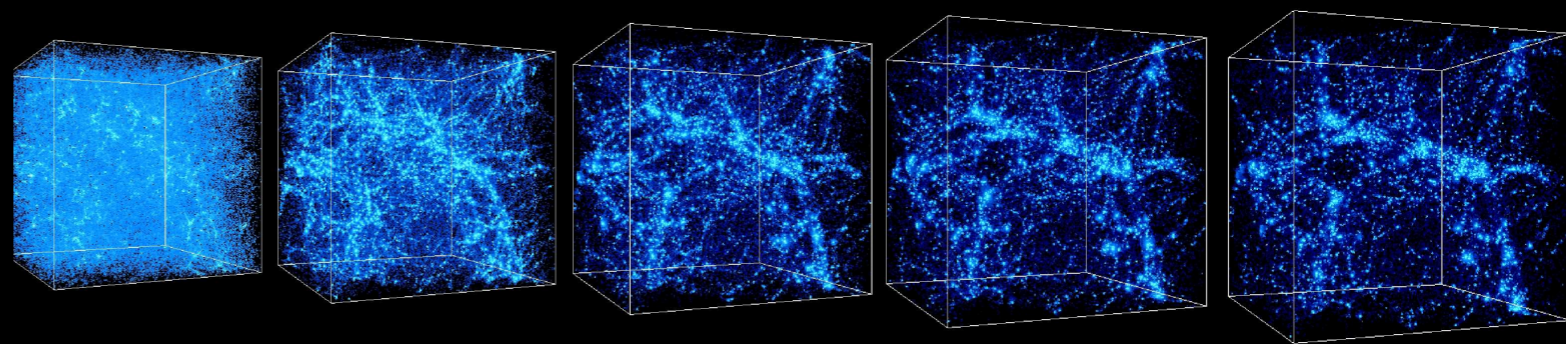
[Yayoi Kusama, Louisiana Museum]



[GW150914]



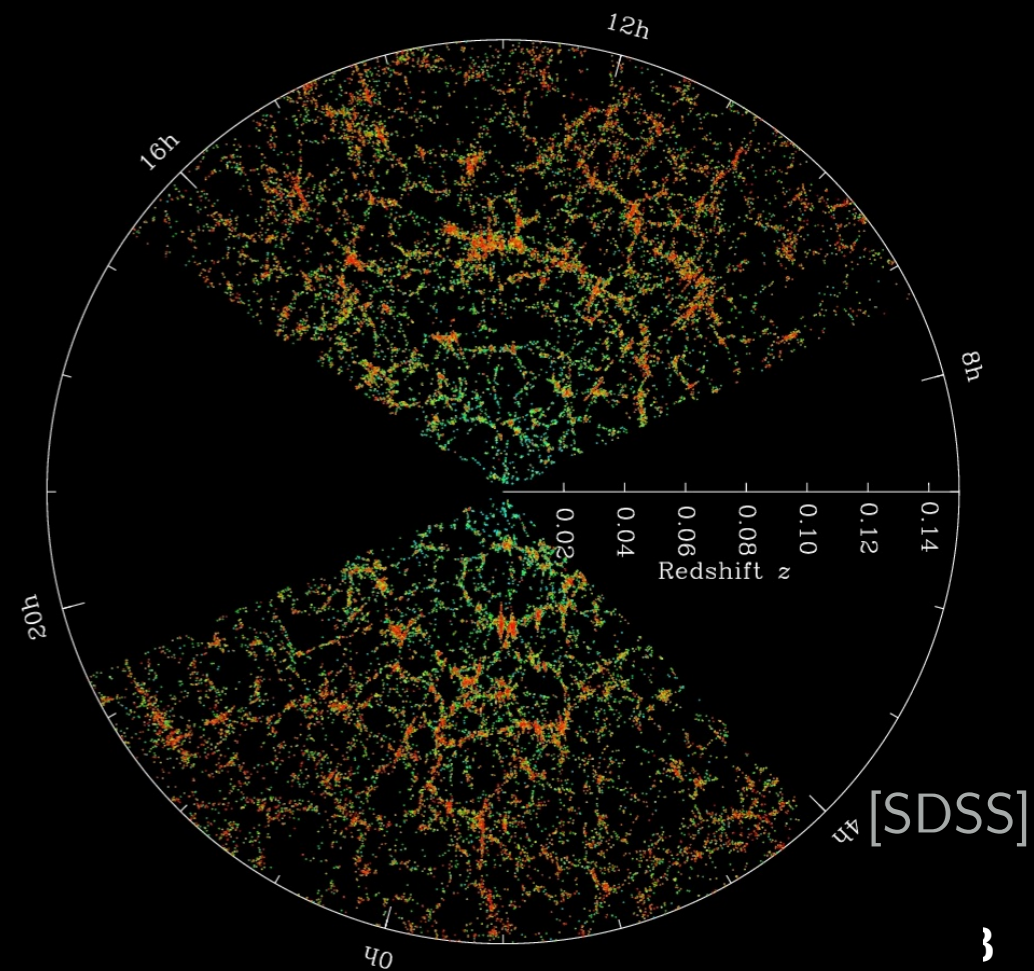
[WMAP/Planck]



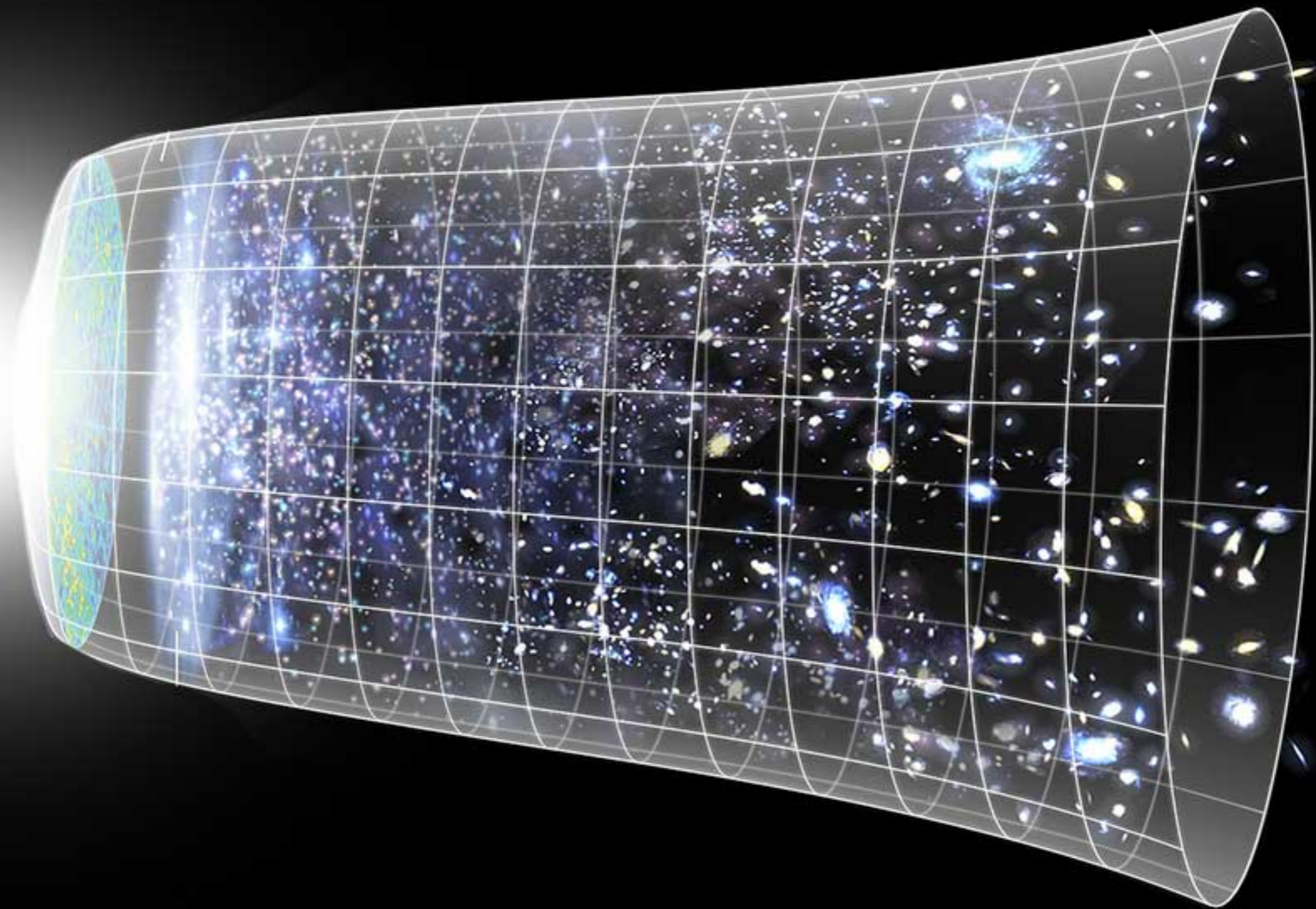
[Kravtsov]



[HST]



[SDSS]



ΛCDM

H_0

Ω_Λ

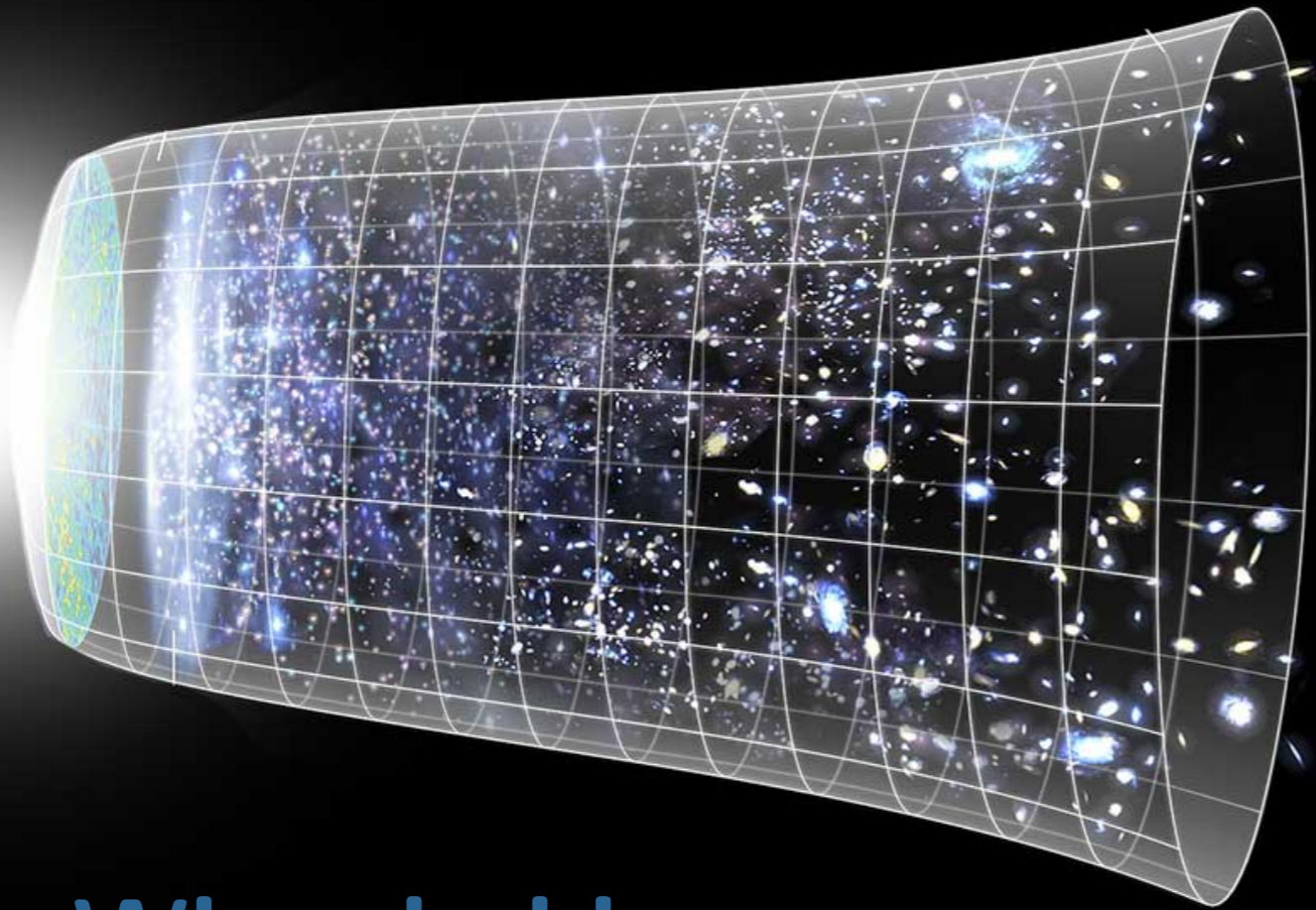
Ω_M

Ω_R

cosmological principle

general relativity

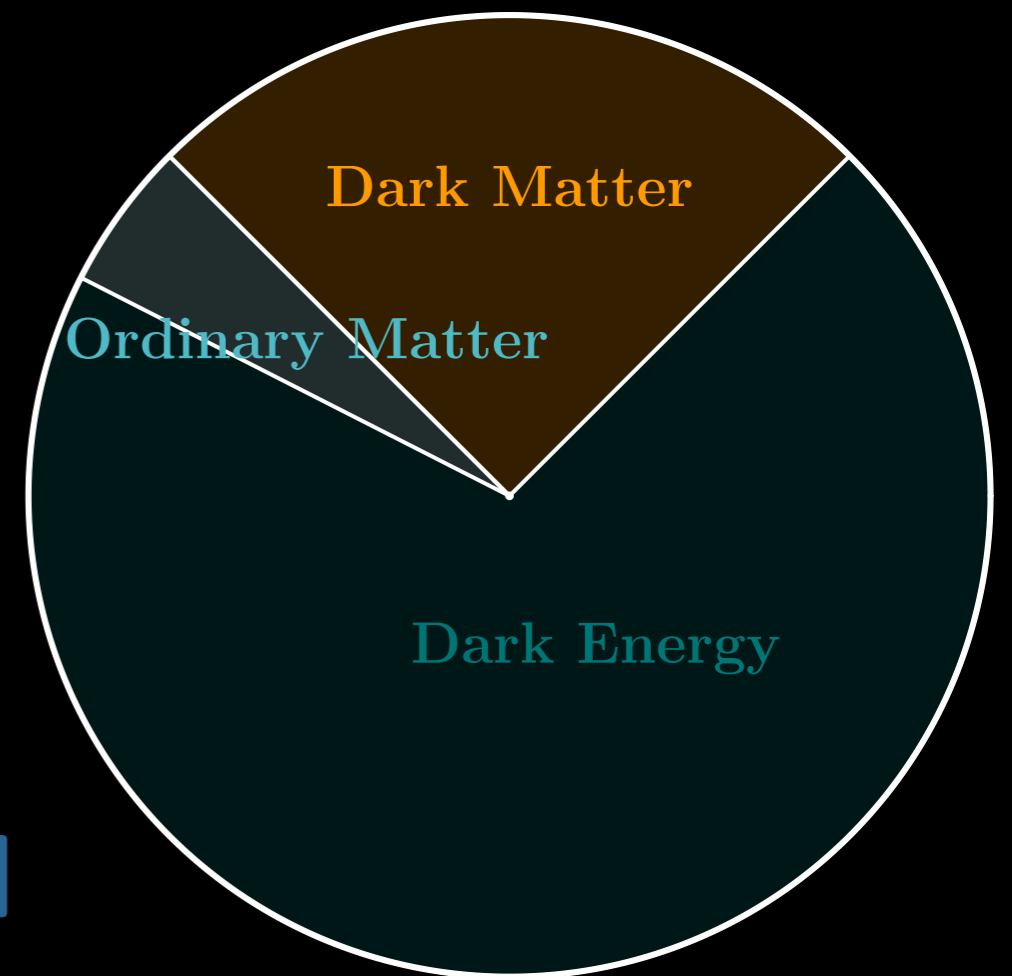
We **don't** understand the basics of our Universe

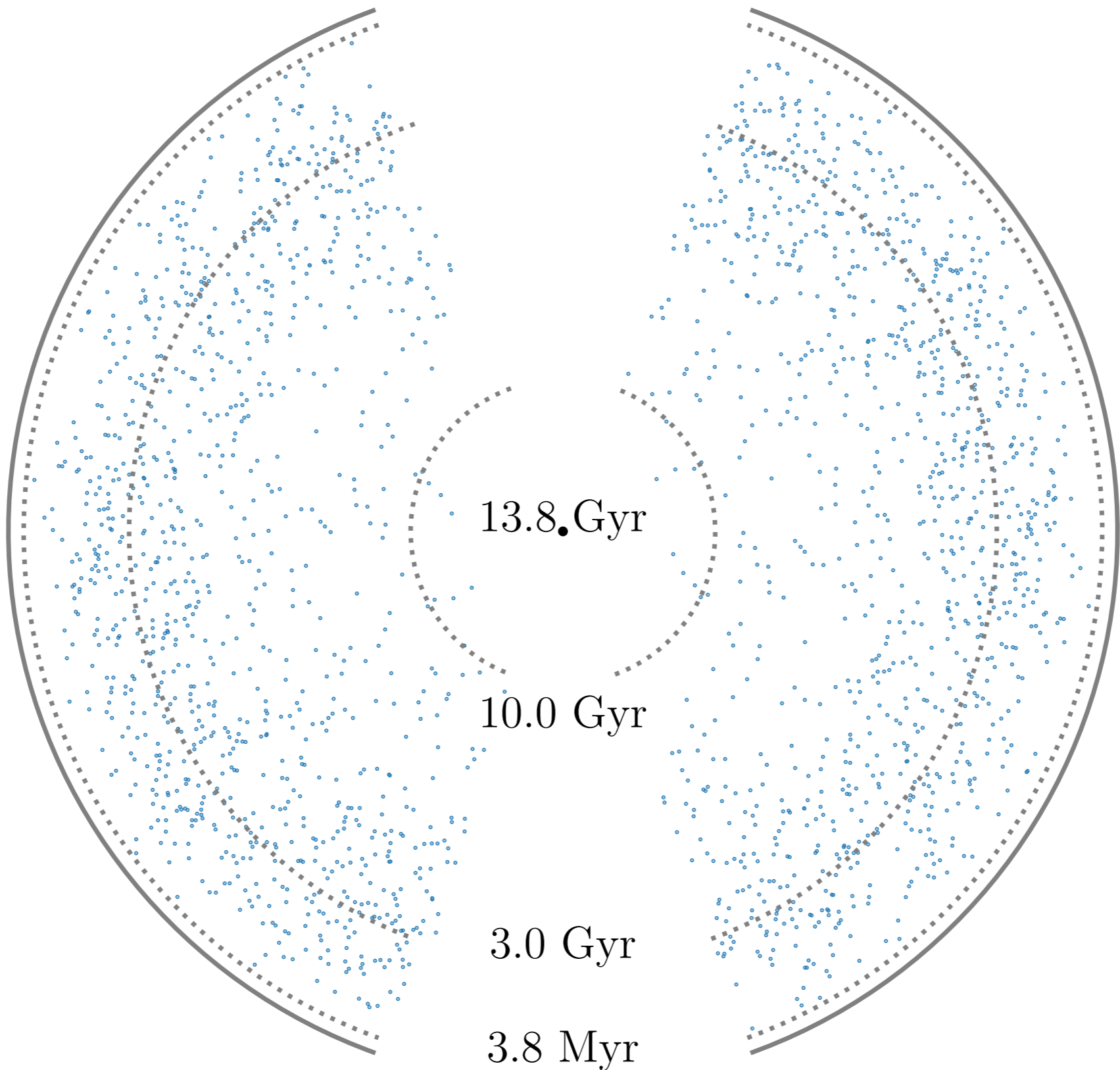


Why the Universe expands ever faster?

What holds galaxies together?

Is Einstein gravity valid at cosmological scales?

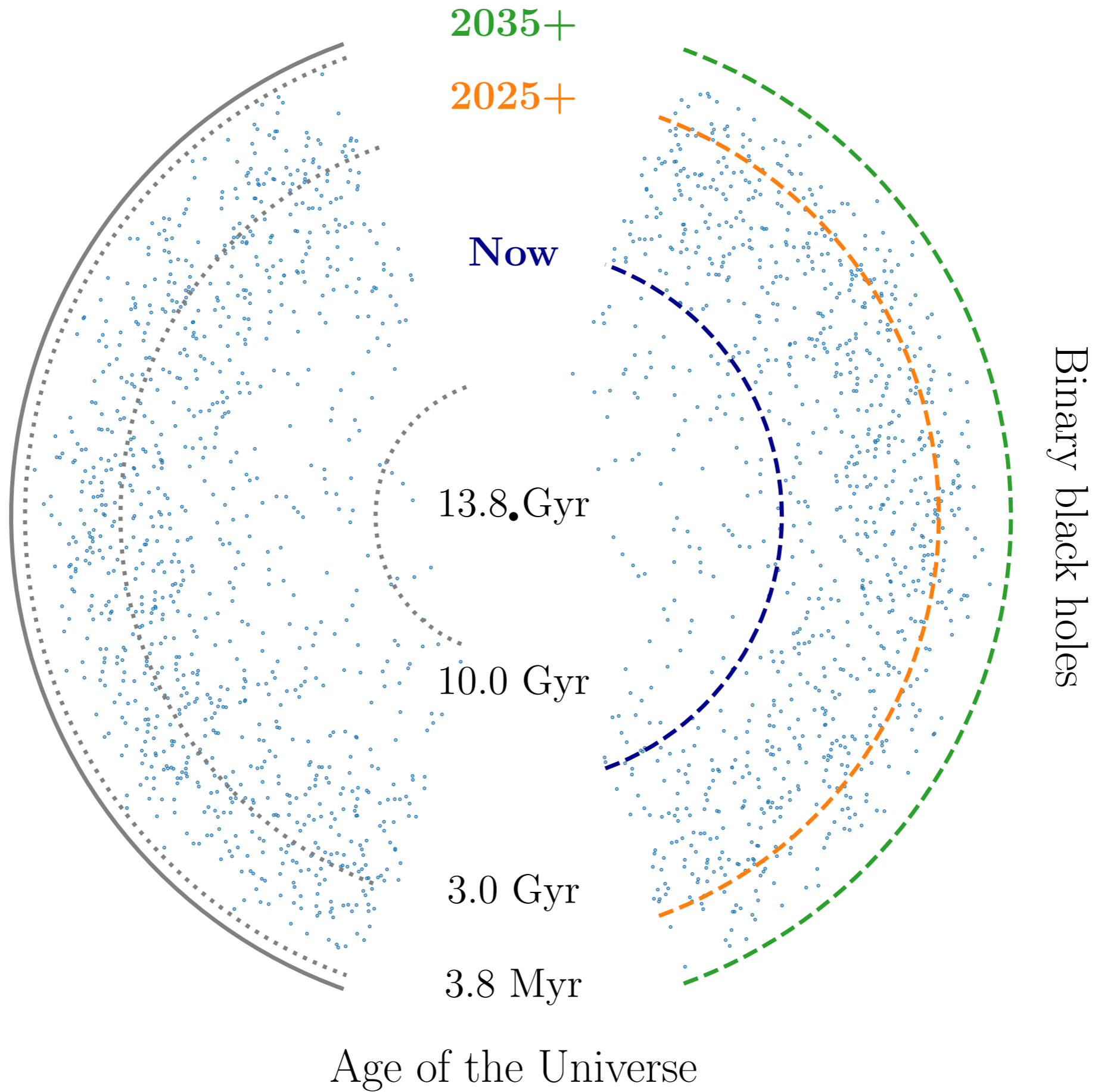




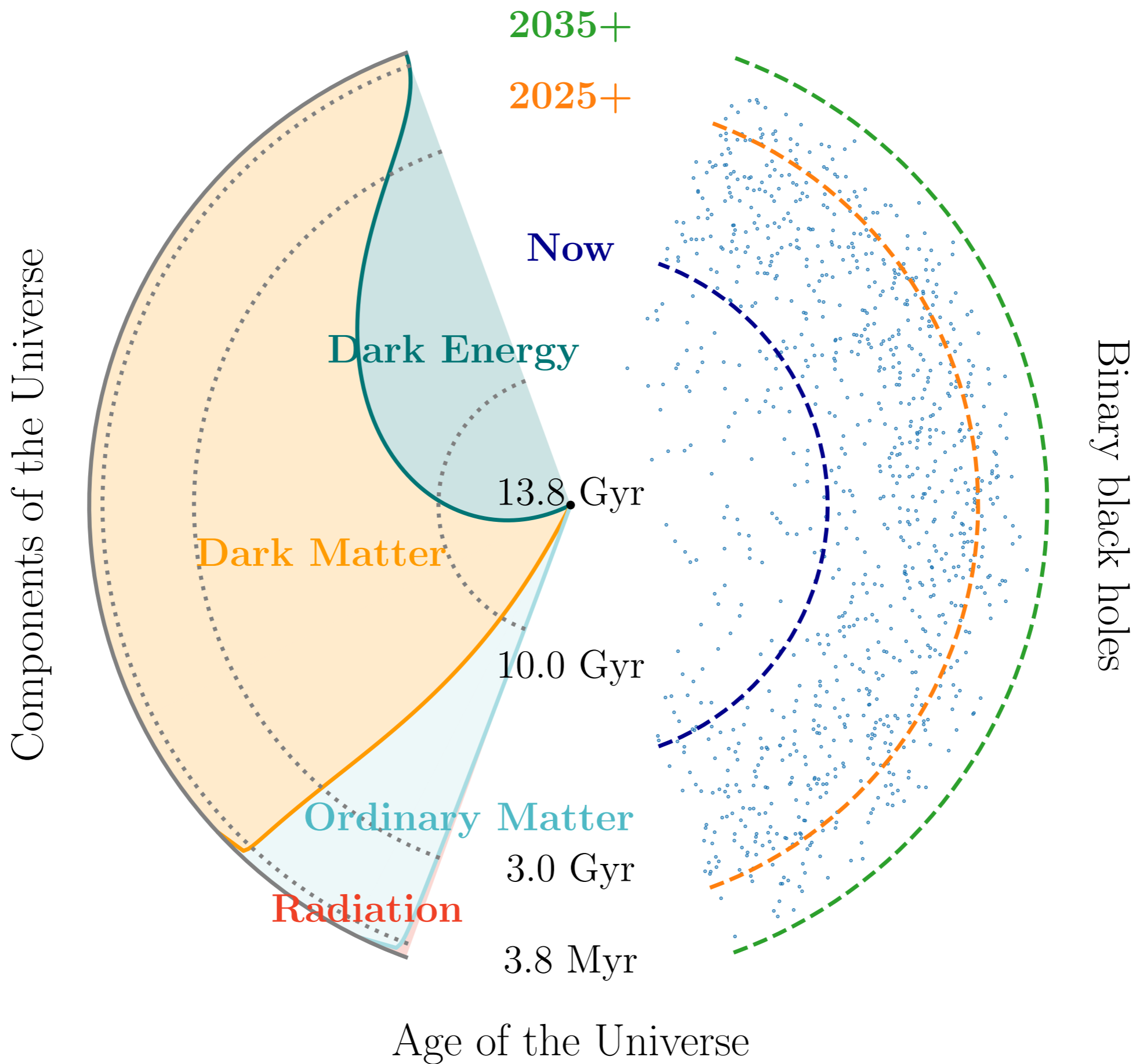
Binary black holes

Age of the Universe

Gravitational Wave horizons

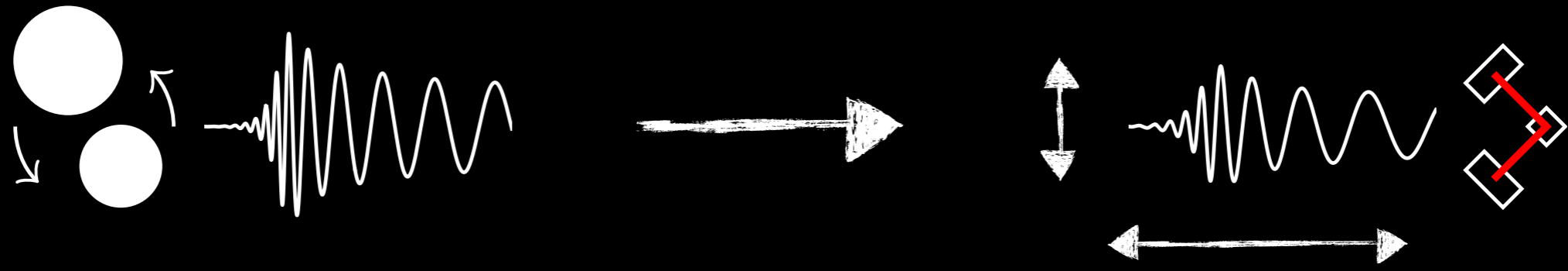


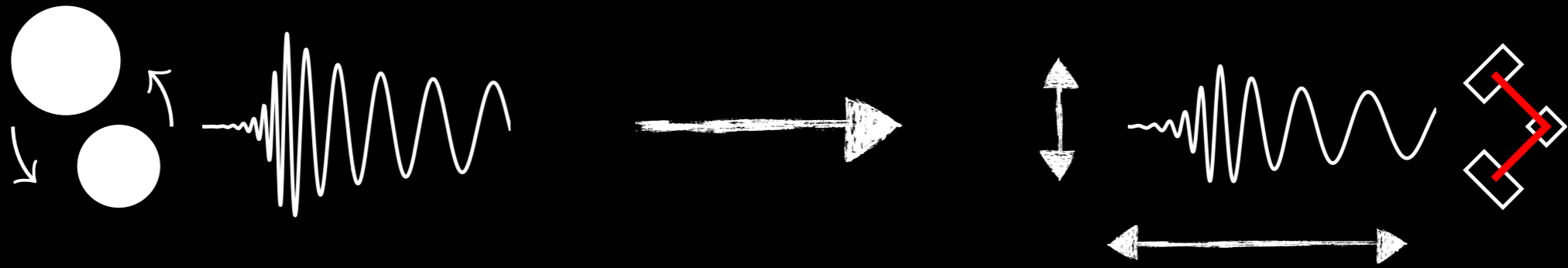
Gravitational Wave horizons



Standard Sirens

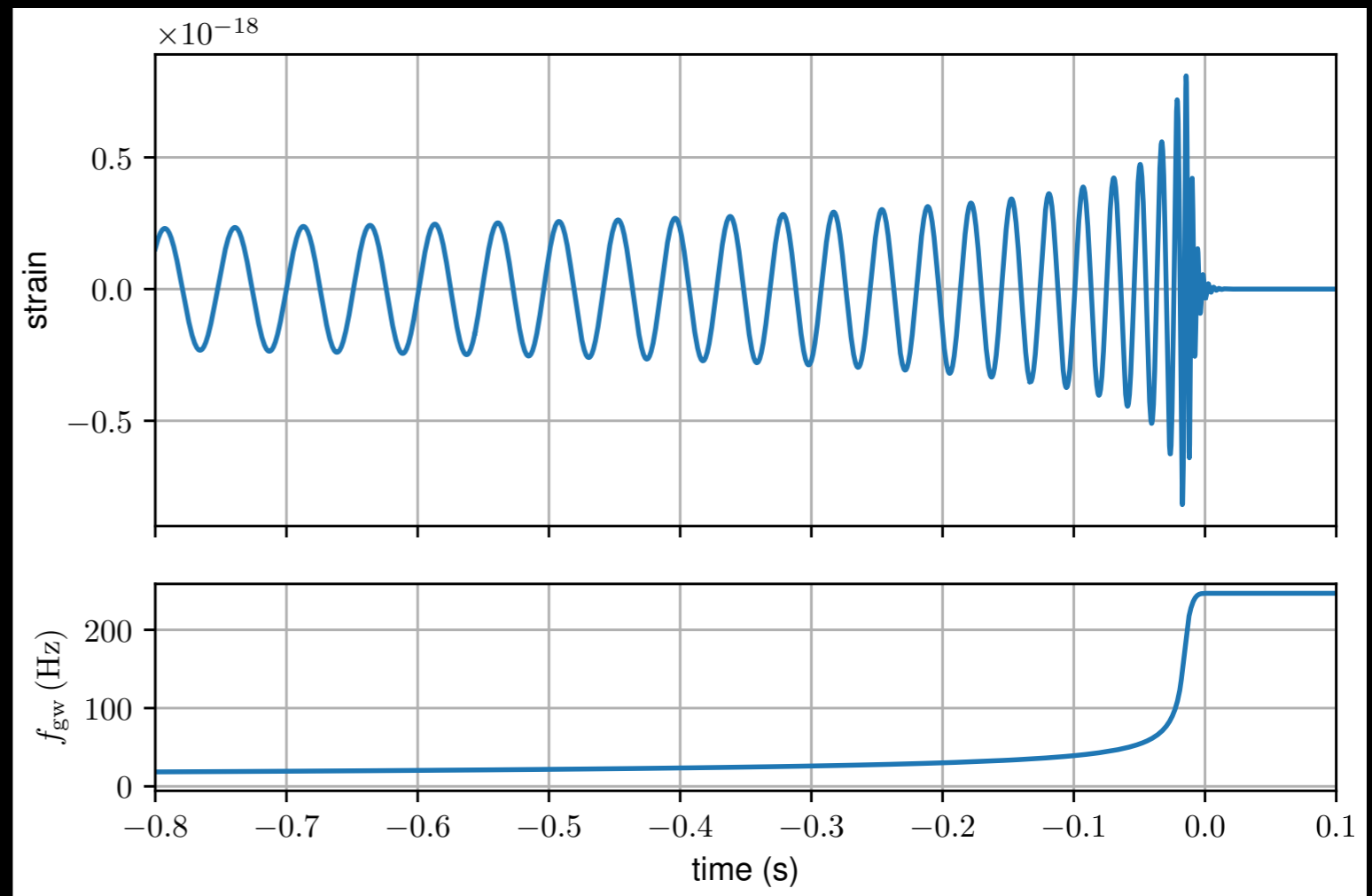
- *General relativity* predicts the waveform of a compact binary coalescence
- Gravitational waves *do not interact* with the medium
- Compact binaries are detected at *cosmological* distances





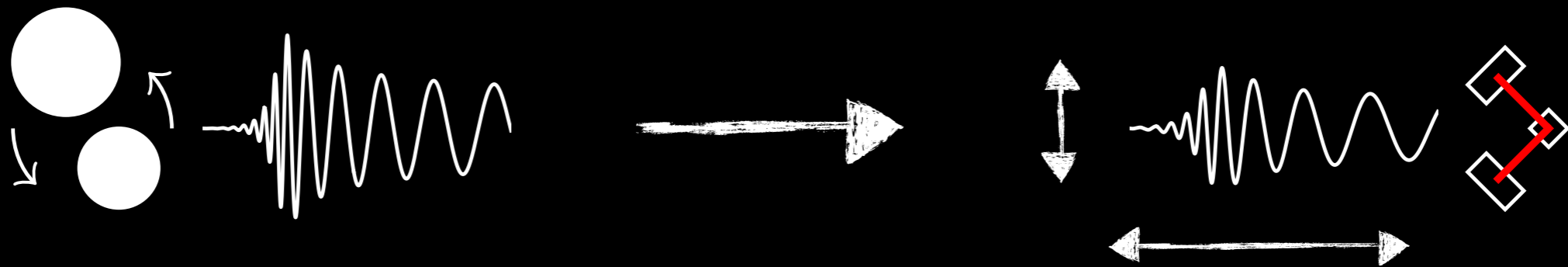
$$h \sim \frac{\mathcal{M}_{\text{det}}^{5/3} f_{\text{det}}^{2/3}}{d_L}$$

$$\dot{f}_{\text{det}} \sim \mathcal{M}_{\text{det}}^{5/3} f_{\text{det}}^{11/3}$$



For more details see:

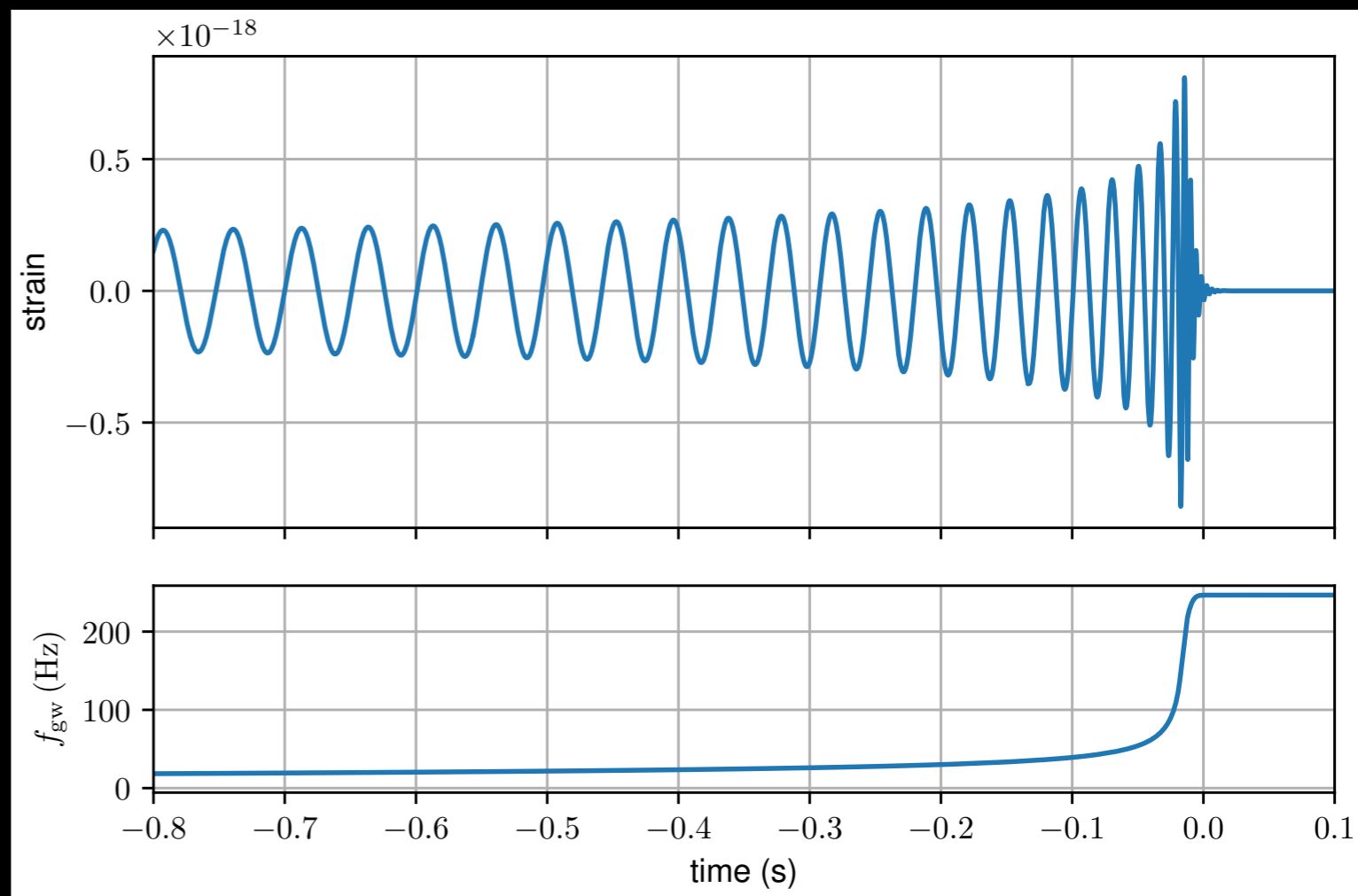
Gravitational Waves Vol. I, M. Maggiore



$$\{d_L(z), m_{\text{det}} = (1+z)m\}$$

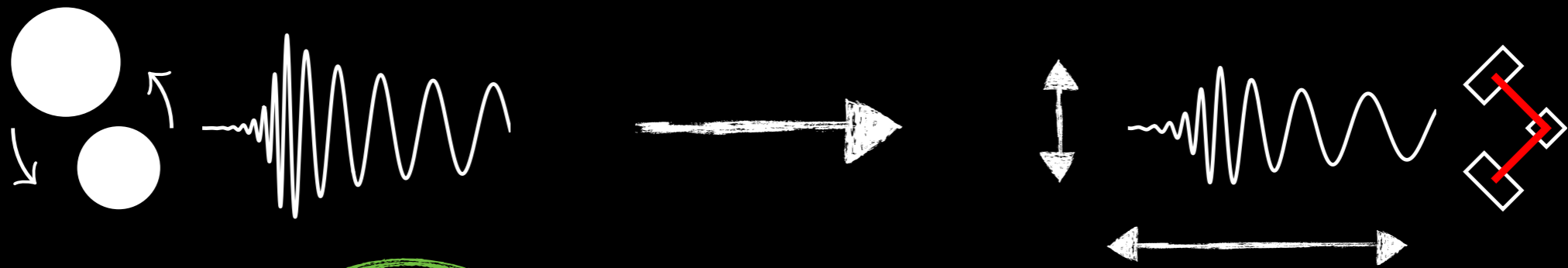
$$h \sim \frac{\mathcal{M}_{\text{det}}^{5/3} f_{\text{det}}^{2/3}}{d_L}$$

$$\dot{f}_{\text{det}} \sim \mathcal{M}_{\text{det}}^{5/3} f_{\text{det}}^{11/3}$$



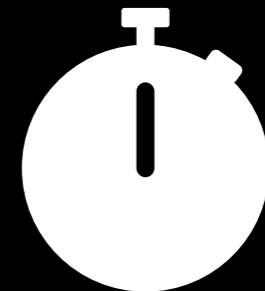
For more details see:

Gravitational Waves Vol. I, M. Maggiore



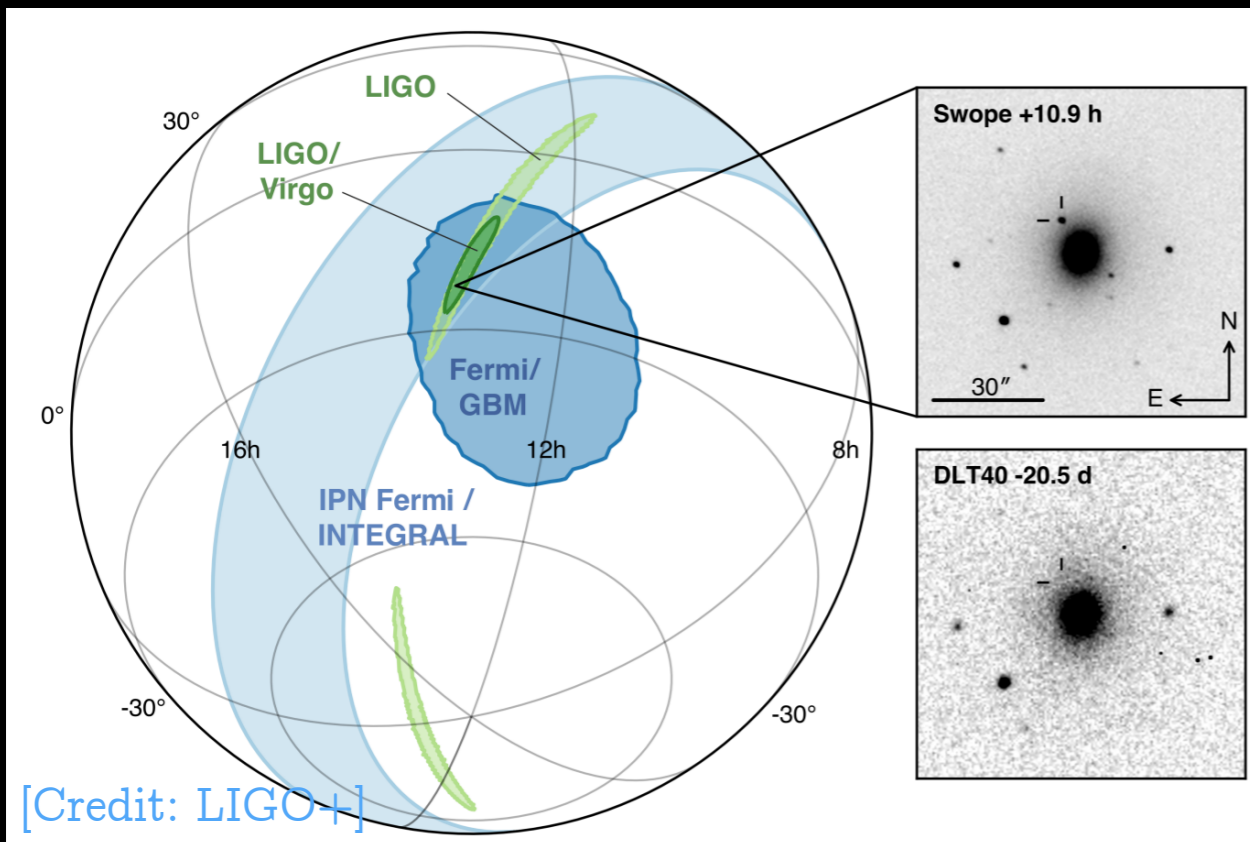
$$\{d_L(z) m_{\text{det}} = (1 + z)m\}$$

*Gravitational waves give direct information of their distance, but to measure the expansion rate of the Universe we need some **timing** information*



BRIGHT SIRENS

- Redshift from electromagnetic counterpart (e.g. identifying host galaxy)
- E.g. GW170817
- Need matter around merger: **neutron stars!**, AGN?
- Bright counterpart at high- z ?



Please log in to view full database contents.

LIGO/Virgo/KAGRA Public Alerts

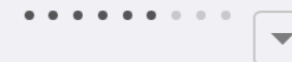
- More details about public alerts are provided in the [LIGO/Virgo/KAGRA Alerts User Guide](#).
- Retractions are marked in **red**. Retraction means that the candidate was manually vetted and is no longer considered a candidate of interest.
- Less-significant events are marked in **grey**, and are not manually vetted. Consult the [LVK Alerts User Guide](#) for more information on significance in O4.

O4 Significant Detection Candidates: **19** (24 Total - 5 Retracted)

O4 Low Significance Detection Candidates: **299** (Total)

Show All Public Events

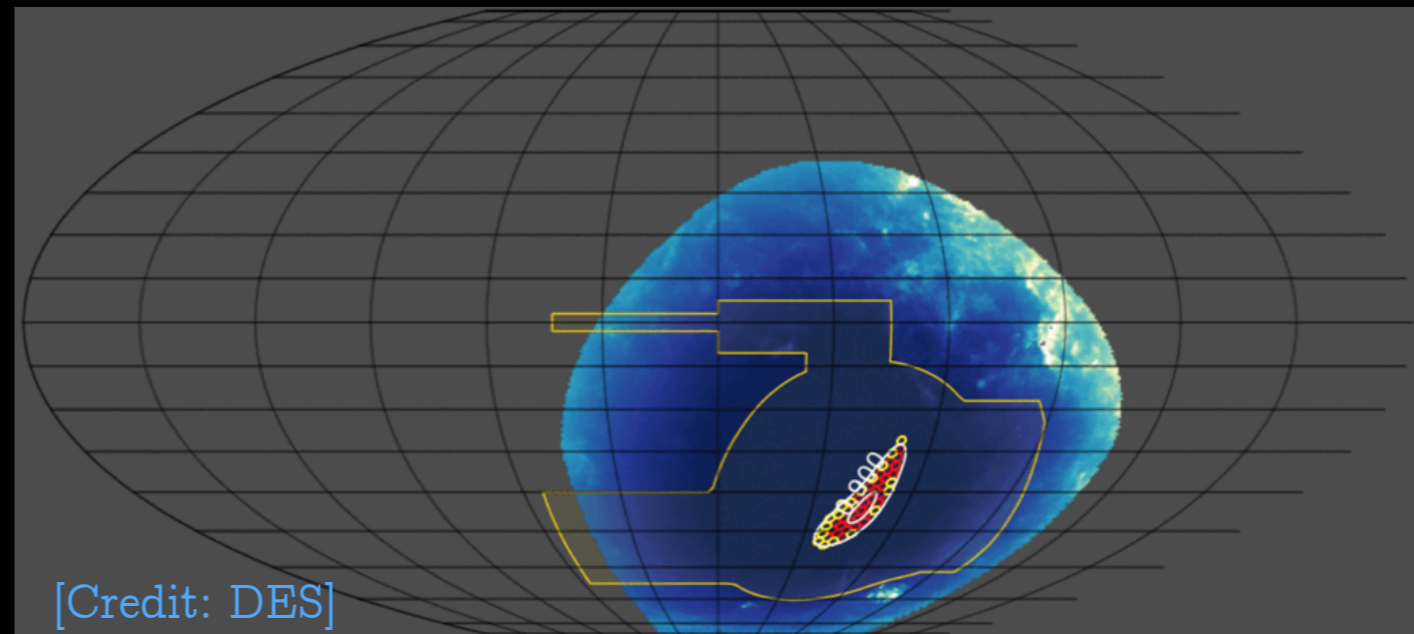
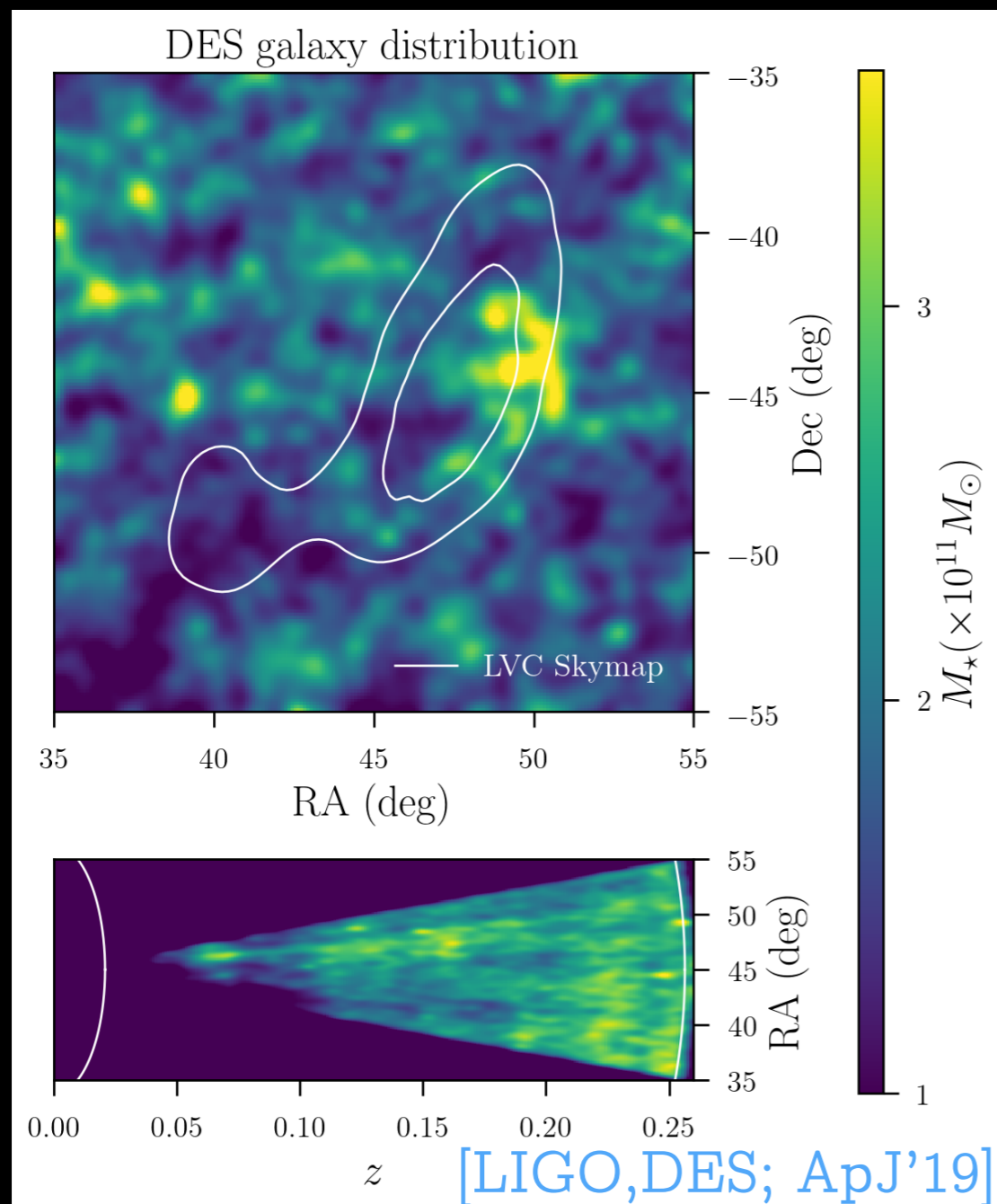
SORT: EVENT ID (A-Z) ▾



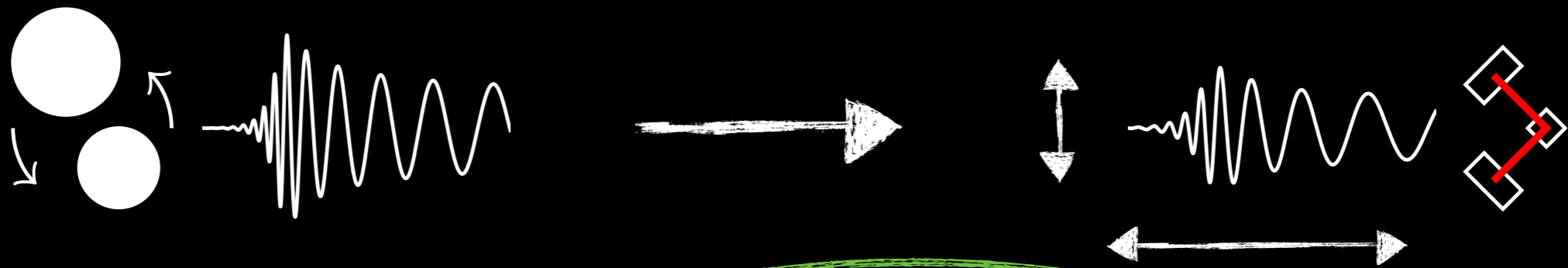
Event ID	Possible Source (Probability)	Significant	UTC	GCN	Location
S230715bw	NSBH (91%), BBH (9%)	Yes	July 15, 2023 19:05:37 UTC	GCN Circular Query Notices VOE	
S230712a	BBH (>99%)	Yes	July 12, 2023 00:53:57 UTC	GCN Circular Query Notices VOE	
S230709bi	BBH (>99%)	Yes	July 9, 2023 12:27:27 UTC	GCN Circular Query Notices VOE	

DARK SIRENS

- Statistically infer z from galaxies in localization volume
- E.g. GW170814
- Need good localization and **complete** galaxy catalogs!

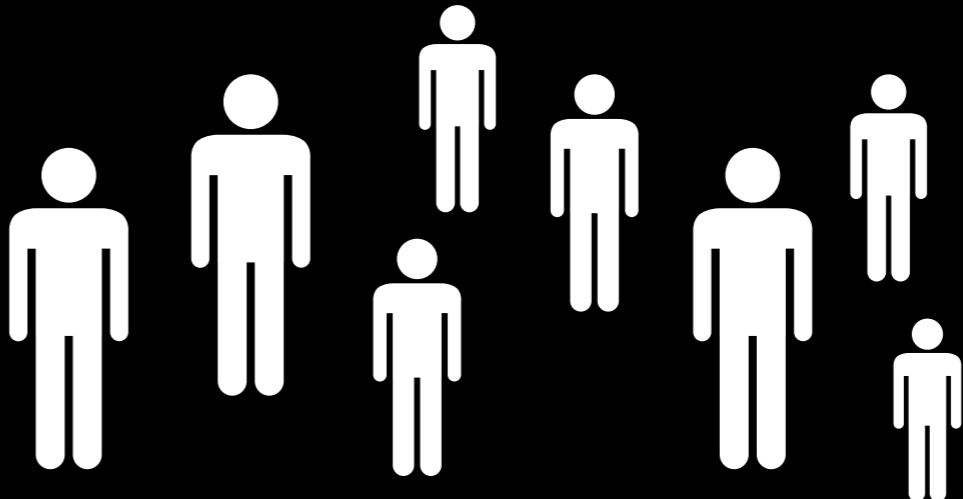


For more details see:
Hitchhiker guide GW galaxy catalog cosmo
([arXiv 2212.08694](https://arxiv.org/abs/2212.08694))



$$\{d_L(z), m_{\text{det}} = (1+z)m\}$$

*Gravitational waves alone can provide redshift information if studied as a **population***



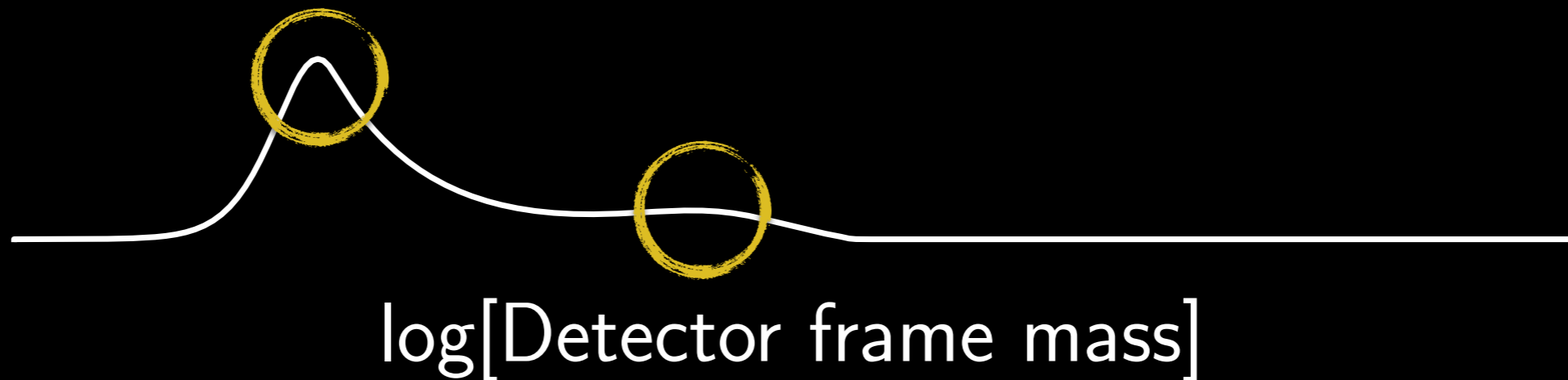
SPECTRAL SIRENS

$$\{d_L(z), m_{\text{det}} = (1+z)m\}$$

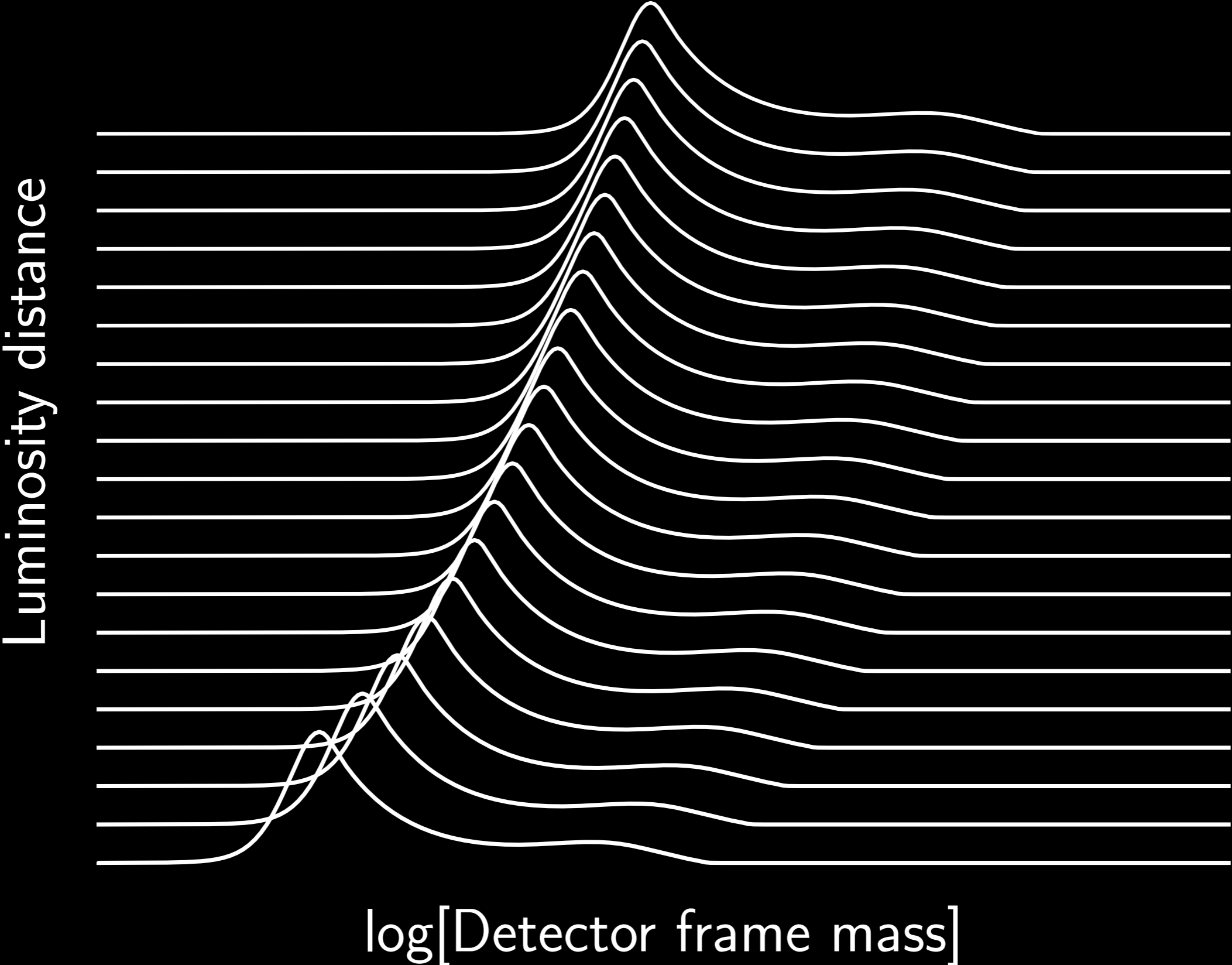


SPECTRAL SIRENS

$$\{d_L(z), m_{\text{det}} = (1+z)m\}$$

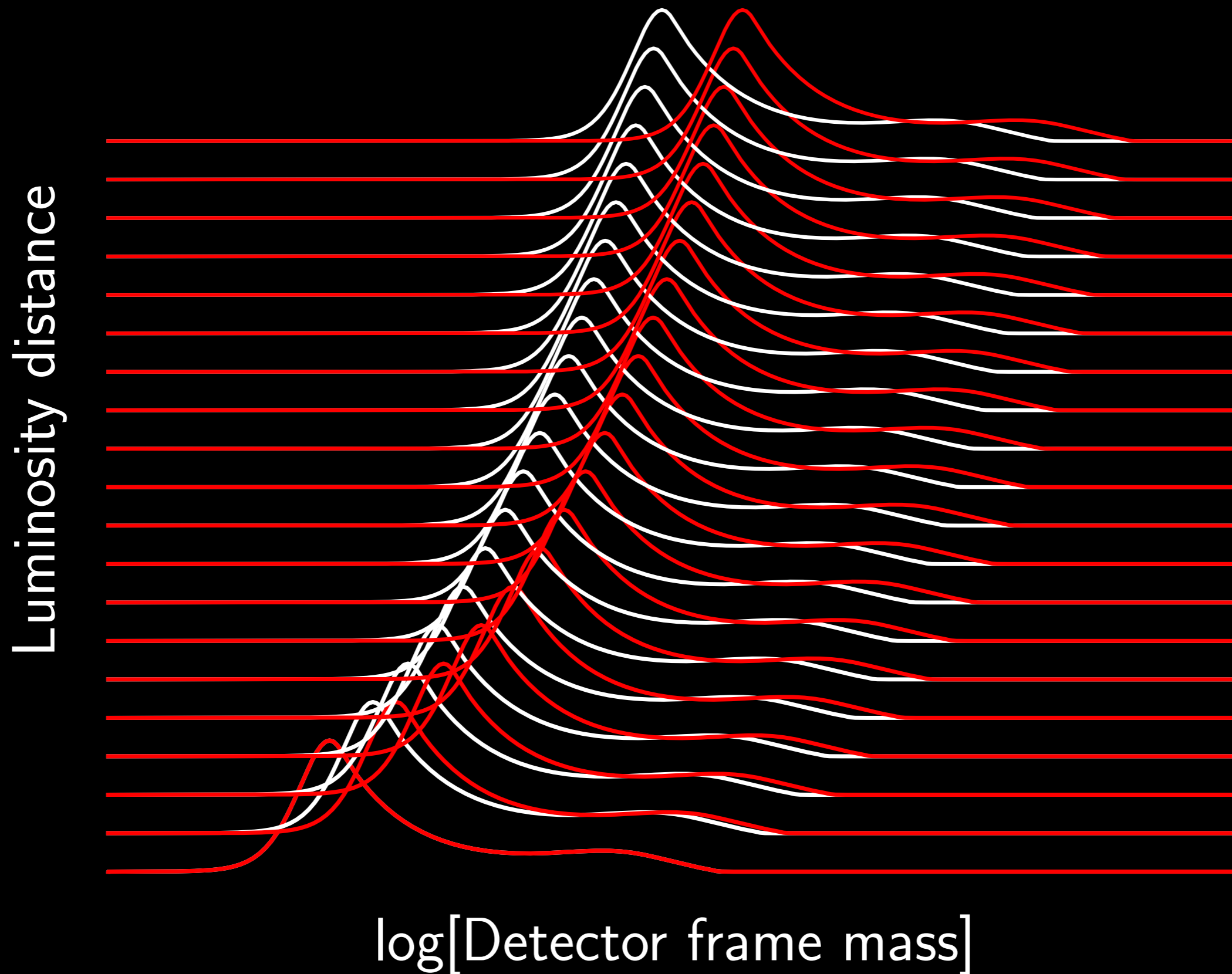


SPECTRAL SIRENS



SPECTRAL SIRENS

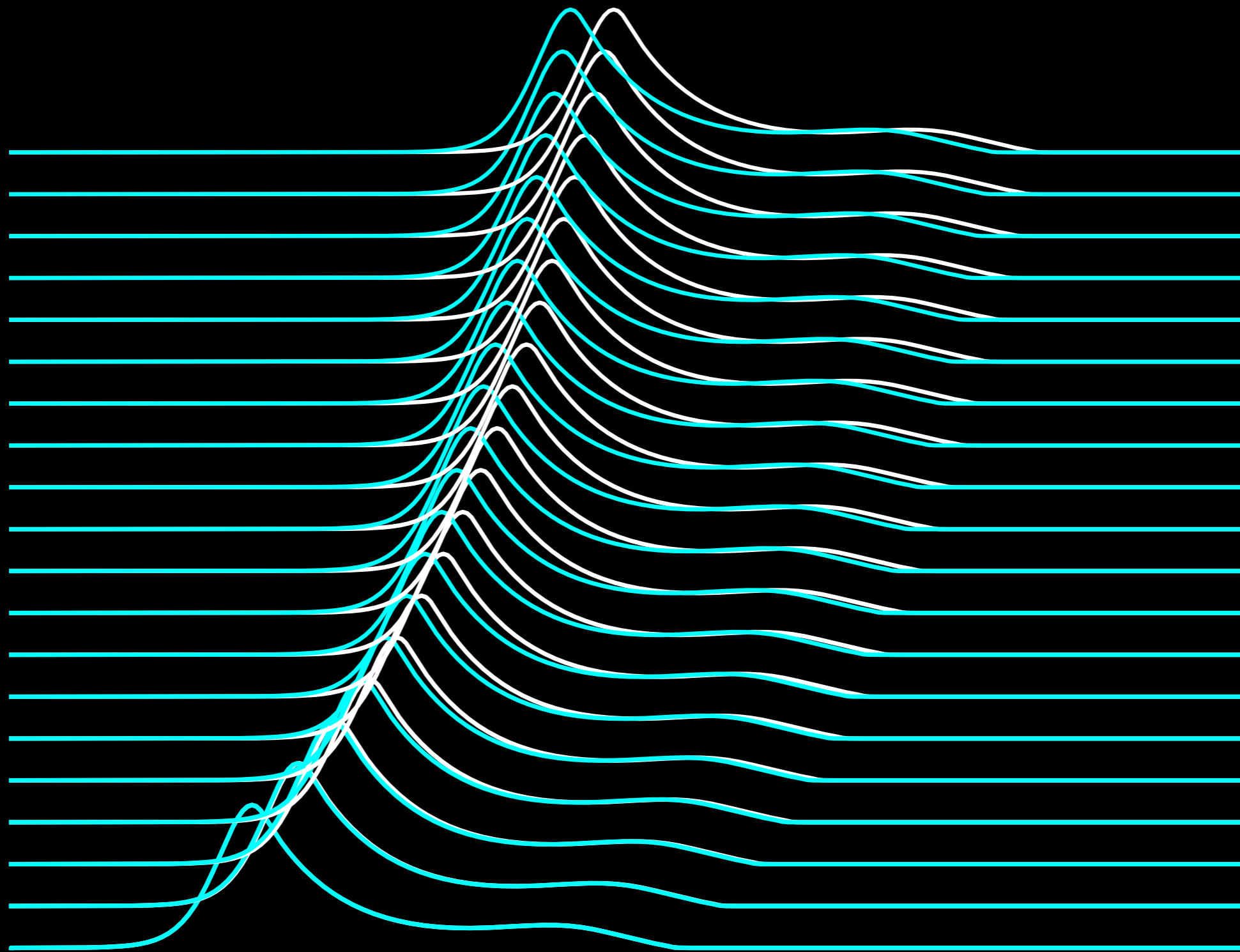
higher H_0



SPECTRAL SIRENS

lower Ω_m

Luminosity distance



log[Detector frame mass]

All compact binaries are standard sirens, no electromagnetic information is necessary



All compact binaries are standard sirens, no electromagnetic information is necessary



Ezquiaga & Holz; *Spectral sirens: Cosmology from full mass distribution of compact binaries* (PRL '22, [arXiv 2202.08240](https://arxiv.org/abs/2202.08240))

[\[Chernoff&Finn'93\]](#)

[\[Farr+'19\]](#)

[\[Mastrogiovanni+'21\]](#)

[\[Ezquiaga&Holz'20\]](#)

[\[Taylor+'11\]](#)

[\[You+'20\]](#)

[\[LVC Cosmo GWTC-3 '21\]](#)

ΛCDM

H_0

Ω_Λ

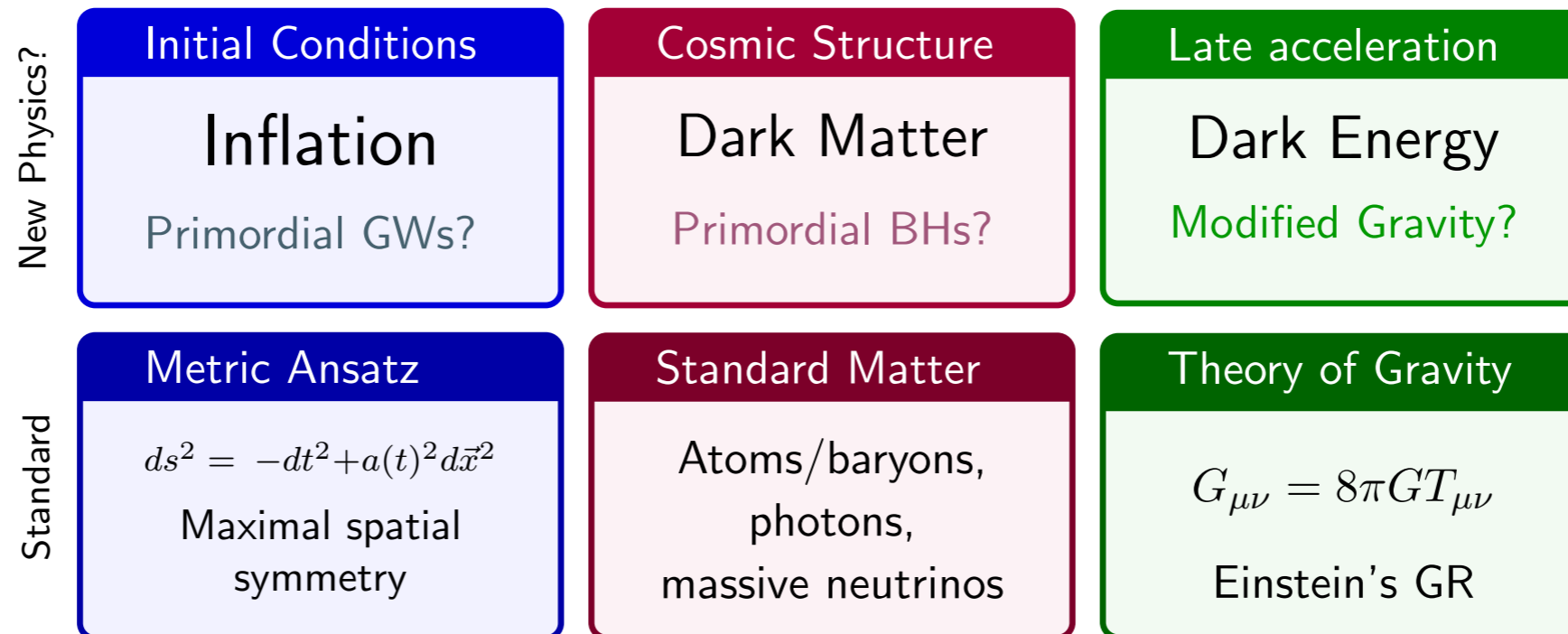
Ω_M

Ω_R

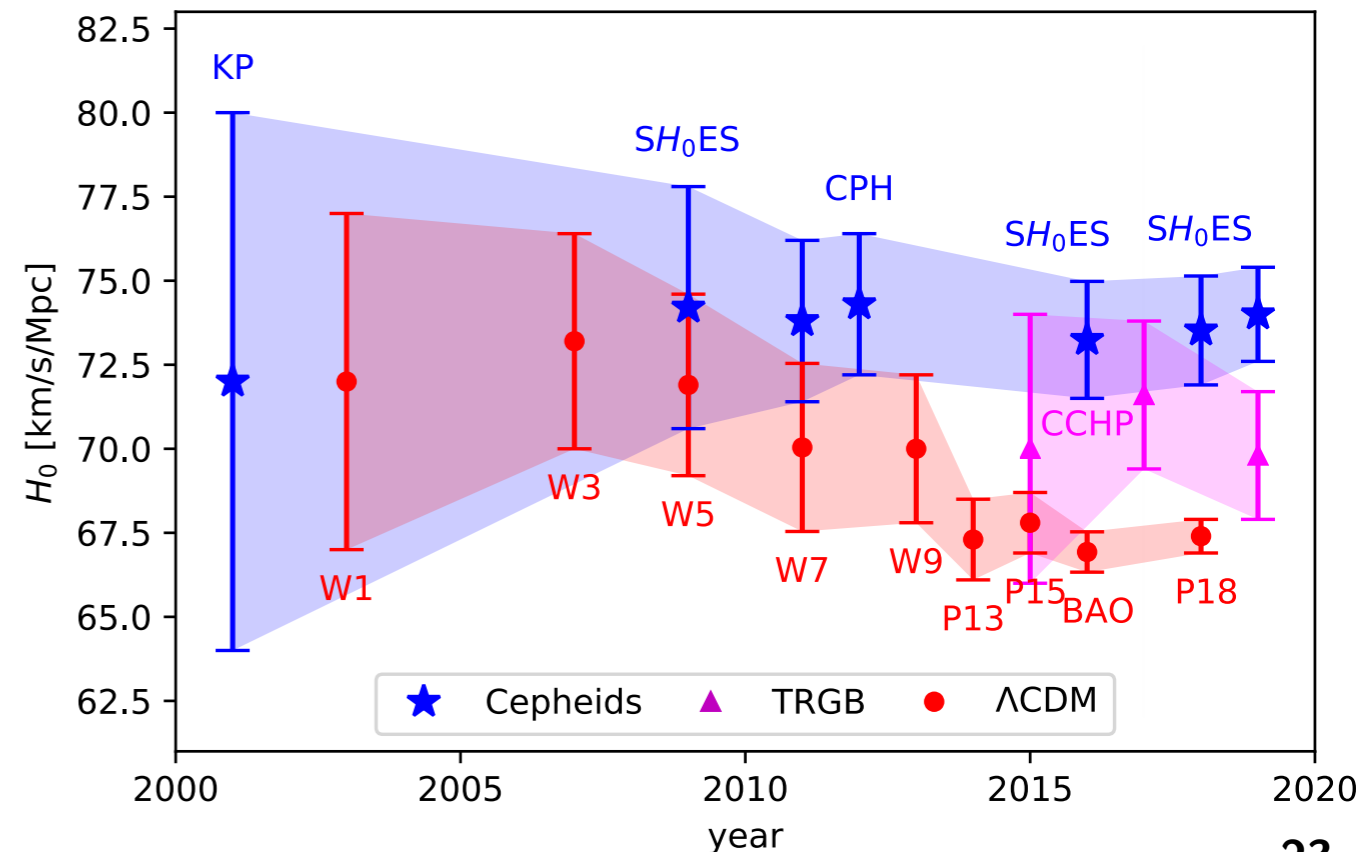
cosmological principle

general relativity

The standard model of cosmology - open questions



- *What drives the late time cosmic acceleration?*
- *Is GR valid at cosmological scales?*
- *Is there new physics associated to the tension in H_0 ?*



Λ CDM

H_0

Ω_Λ

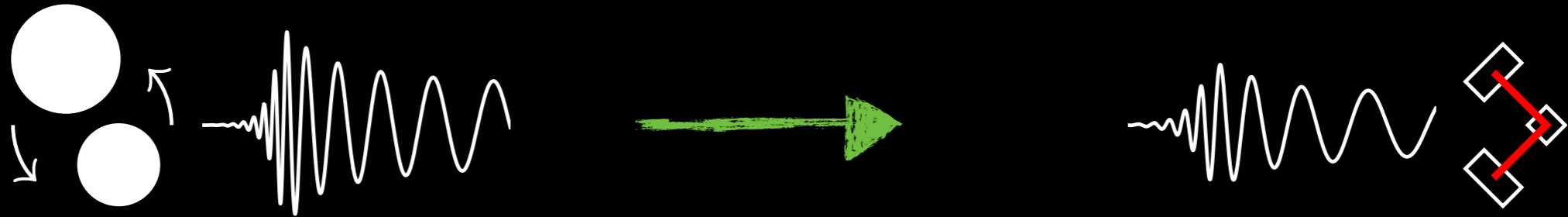
Ω_M

Ω_R

cosmological principle

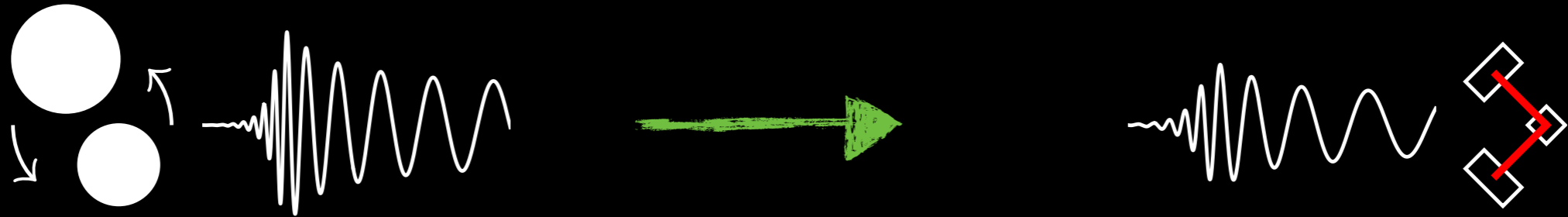
general relativity

Cosmological GW propagation



$$H(z) = H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_\Lambda + \Omega_r (1+z)^4}$$

Cosmological GW propagation



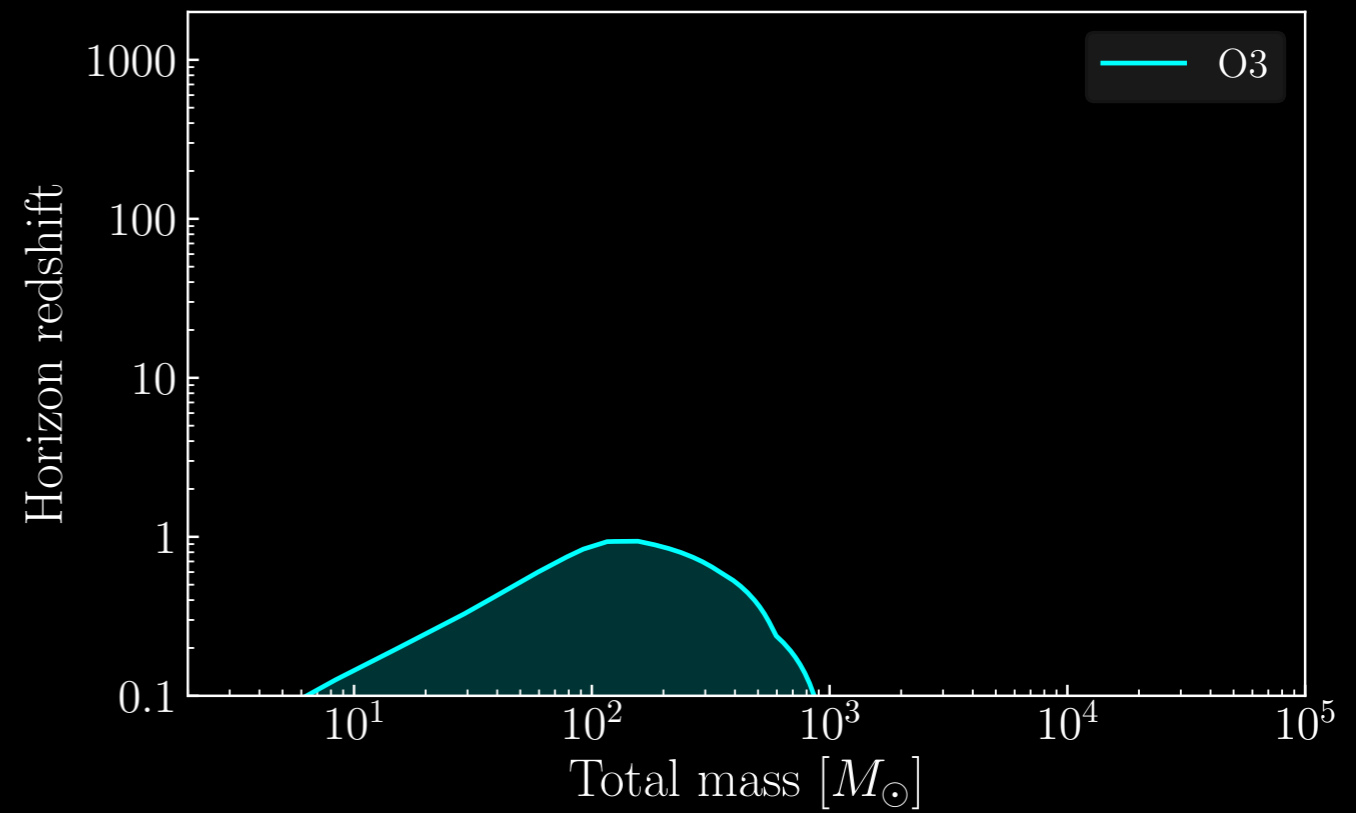
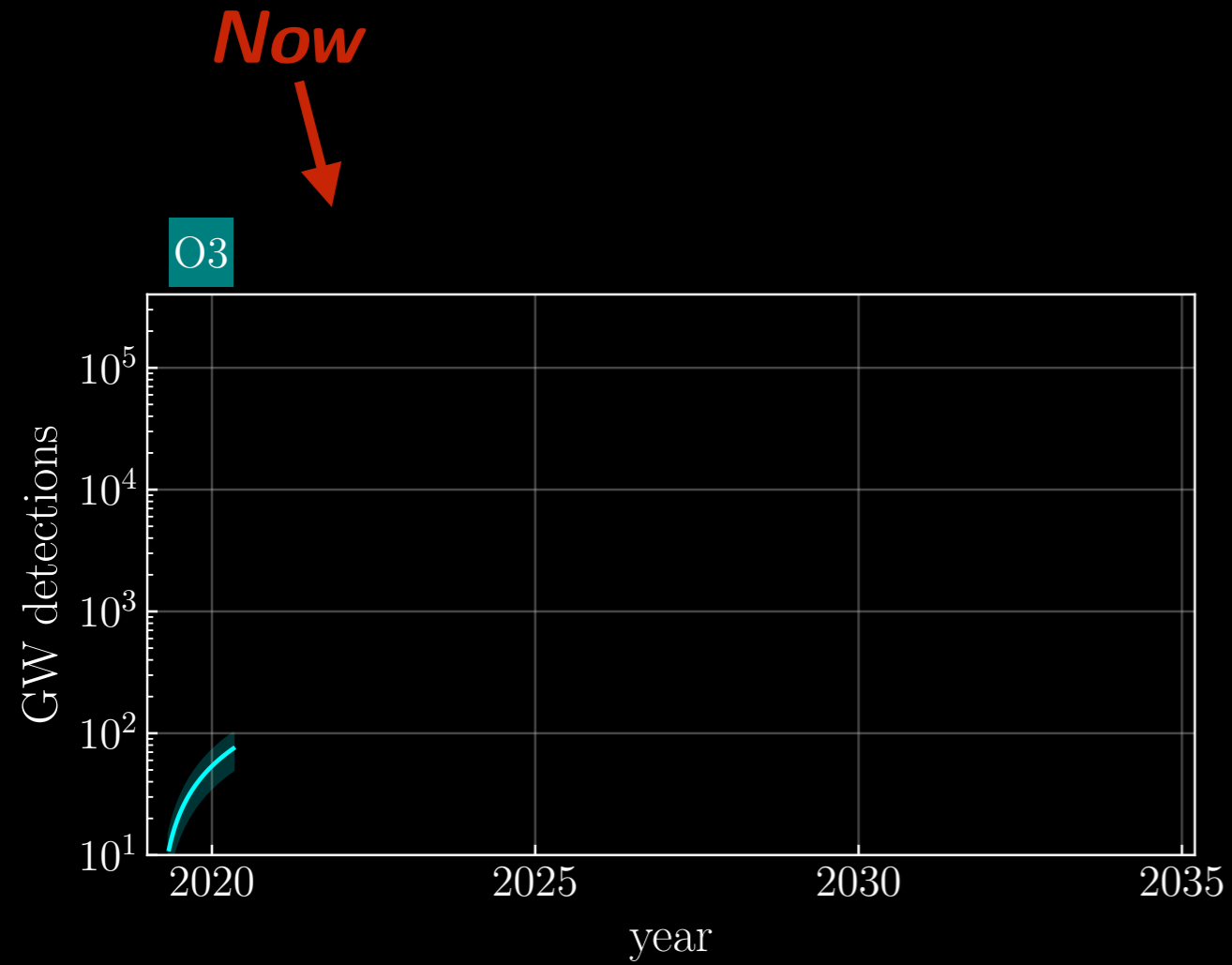
$$h''_A + 2\mathcal{H}h'_A + c^2k^2h_A = 0$$

- **Expansion rate:** changes GW amplitude

$$d_L = (1 + z) \int_0^z \frac{cdz}{H(z)}$$

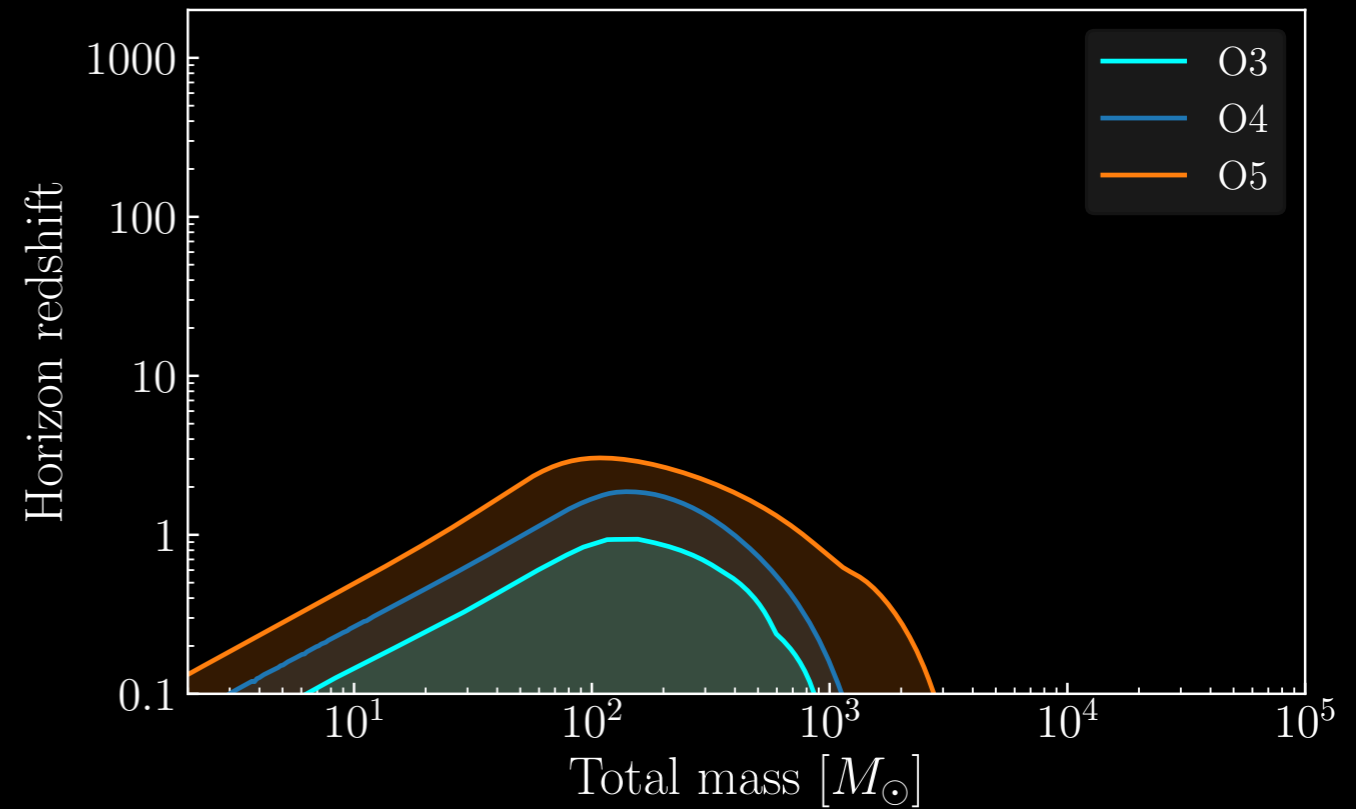
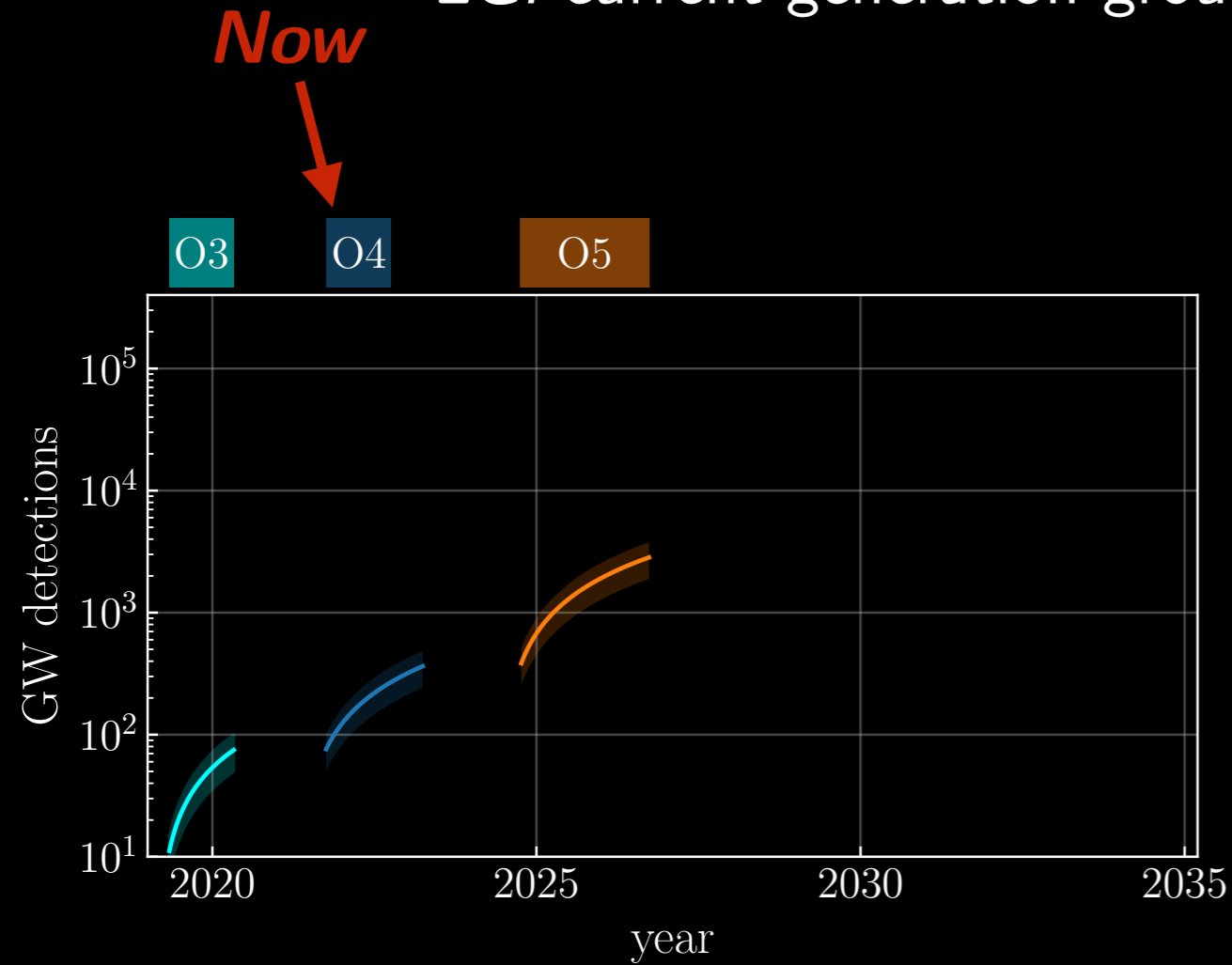
$$H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda + \Omega_r(1+z)^4}$$

Gravitational wave detectors will constrain expansion history at different redshifts, measuring e.g. H_0 , EoS of Dark Energy, Dark Matter



Approx. 100
events typically at
 $z < 0.6$

2G: current generation ground-based GW detectors



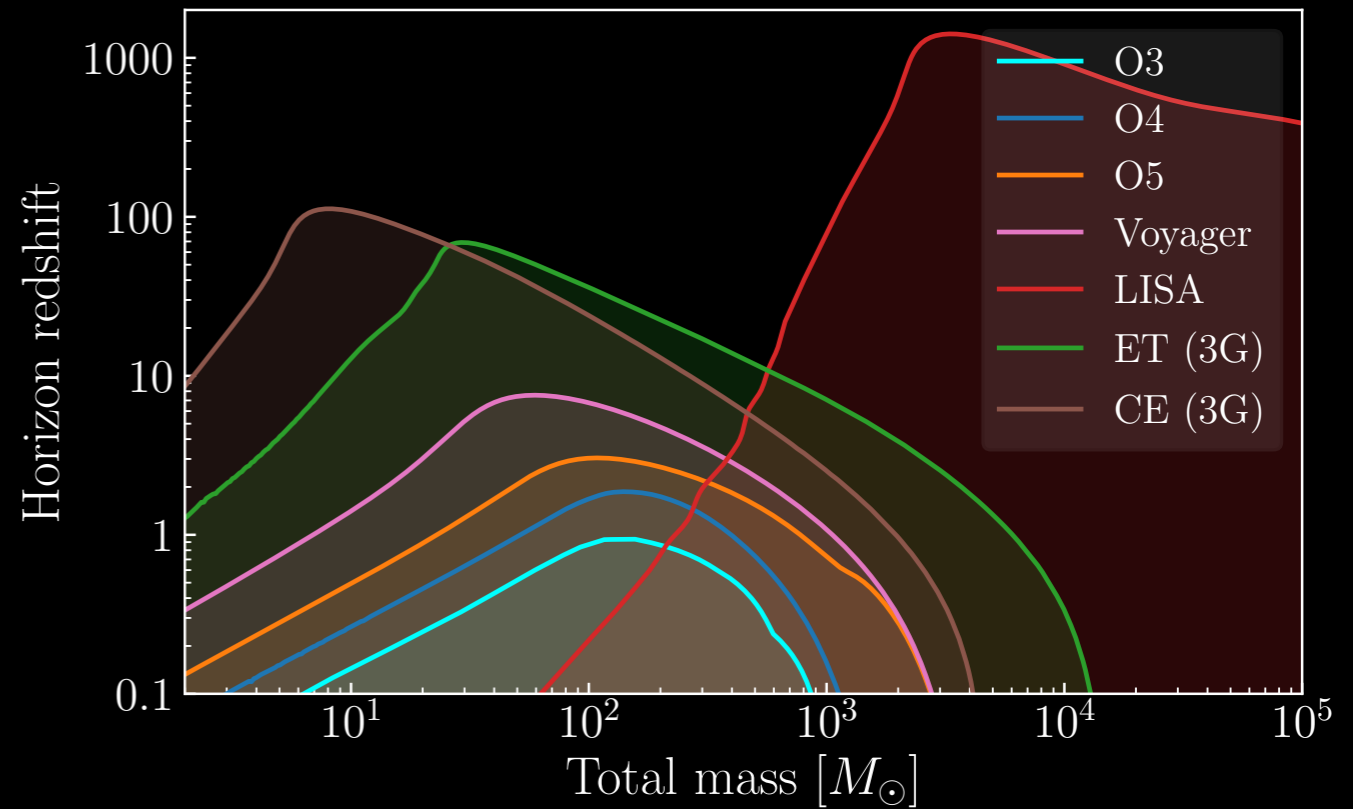
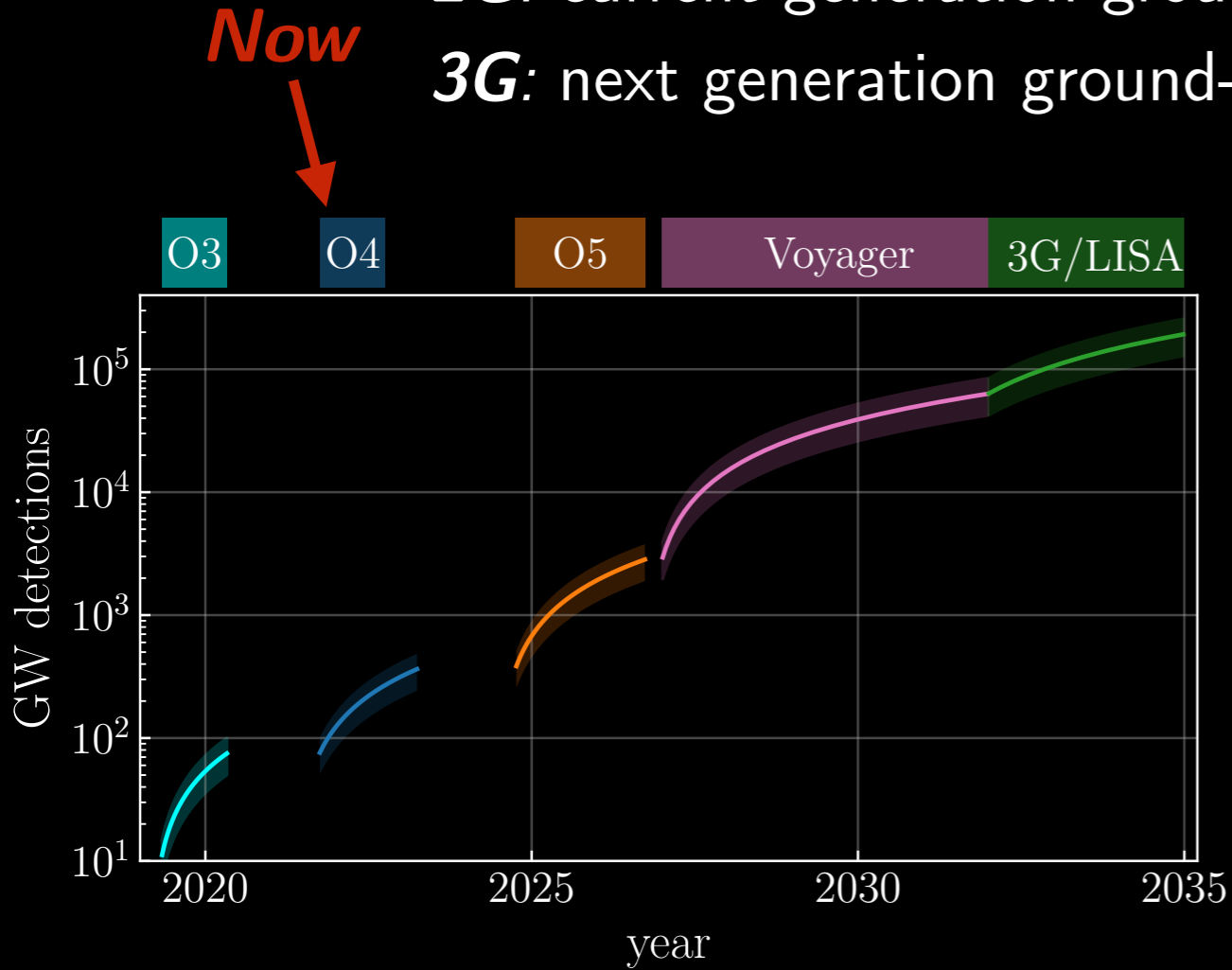
Approx. 100
events typically at
 $z < 0.6$



1000s / year
with some $z > 1$

2G: current generation ground-based GW detectors

3G: next generation ground-based GW detectors



Approx. 100
events typically at
 $z < 0.6$



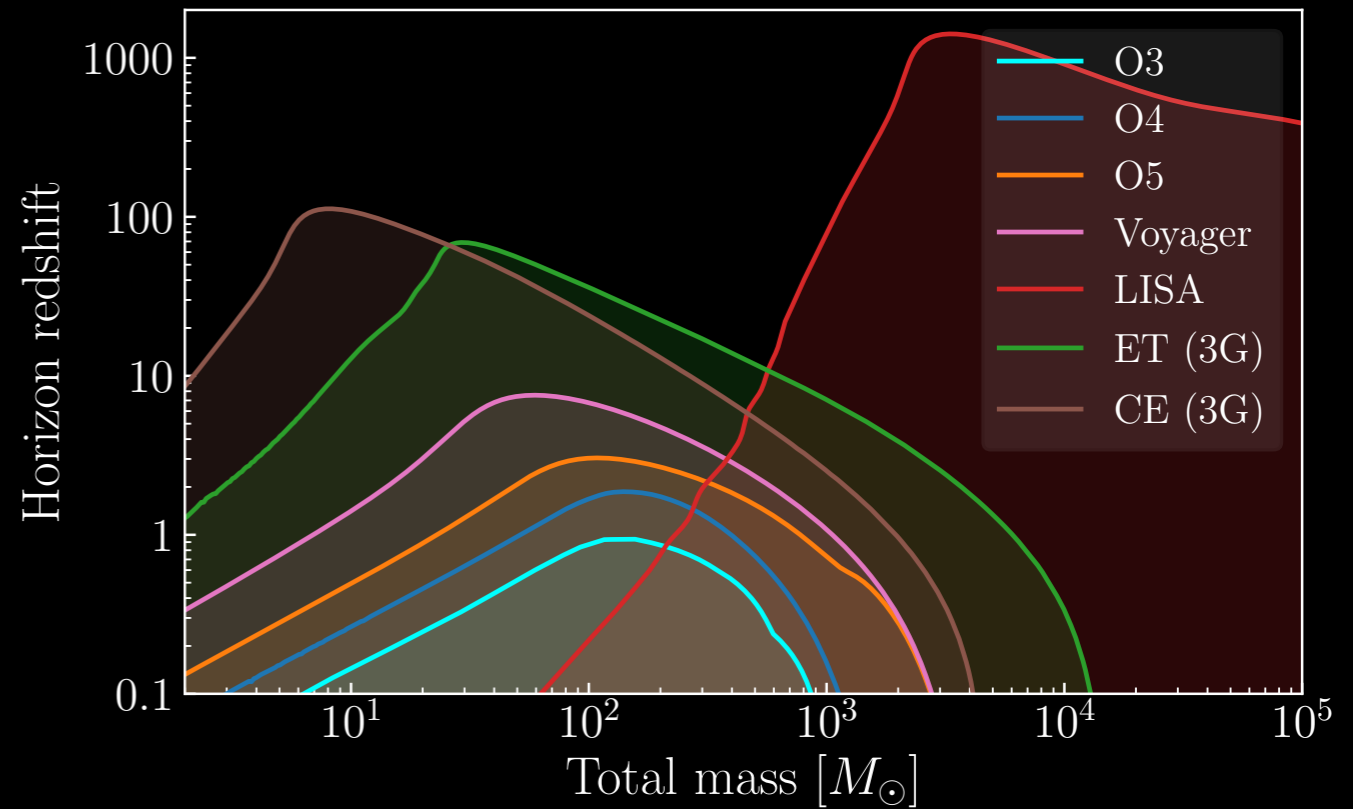
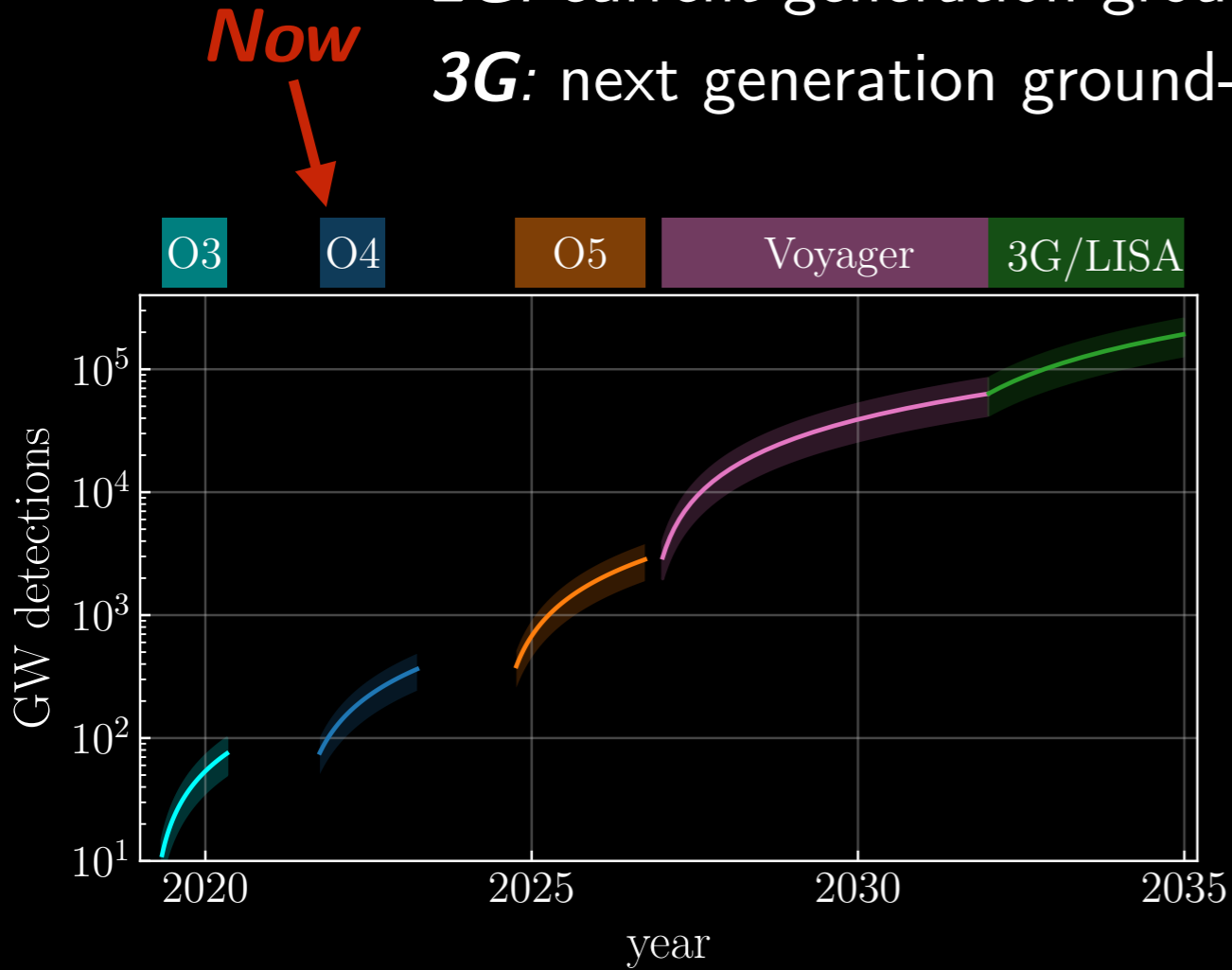
1000s / year
with some $z > 1$



100,000s / year
with most $z > 1$

2G: current generation ground-based GW detectors

3G: next generation ground-based GW detectors



Approx. 100

events typically at

$z < 0.6$



1000s / year

with some $z > 1$



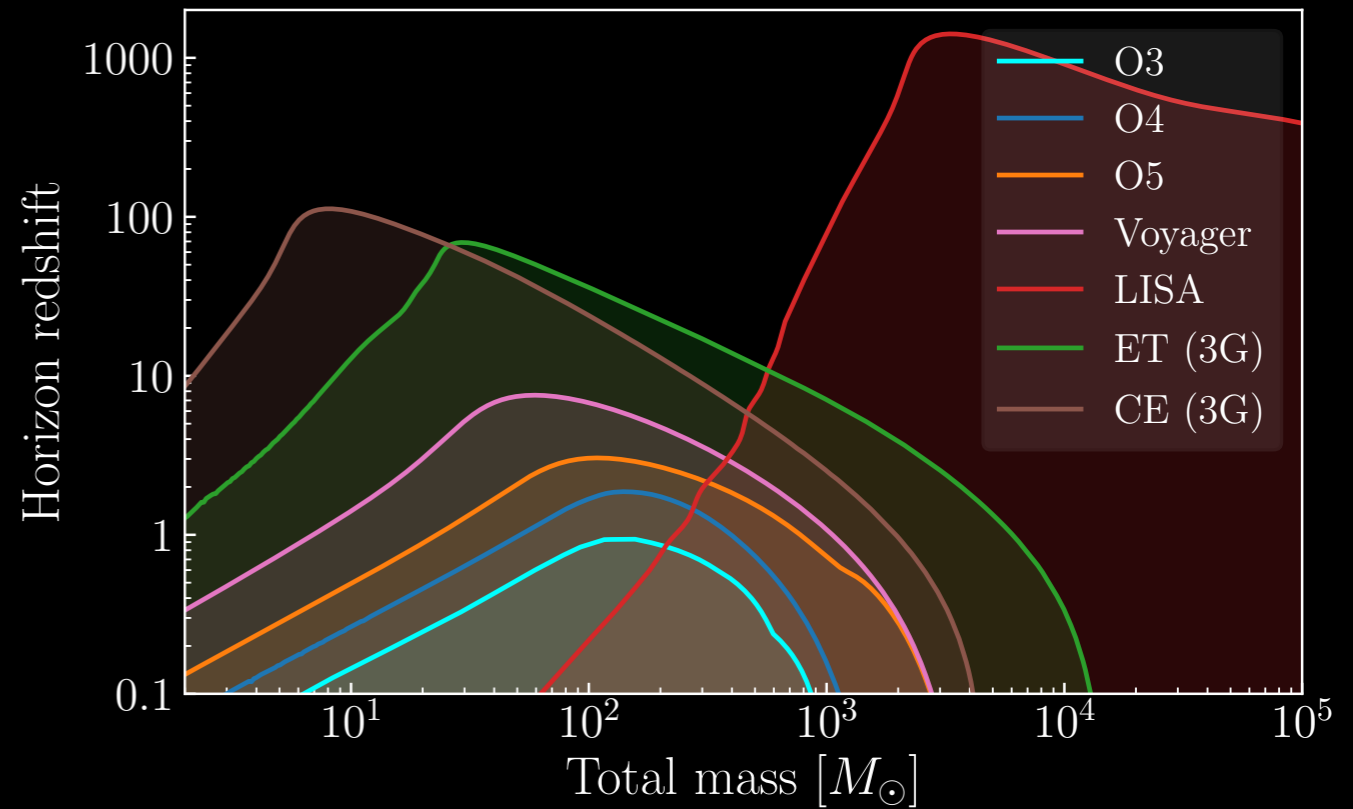
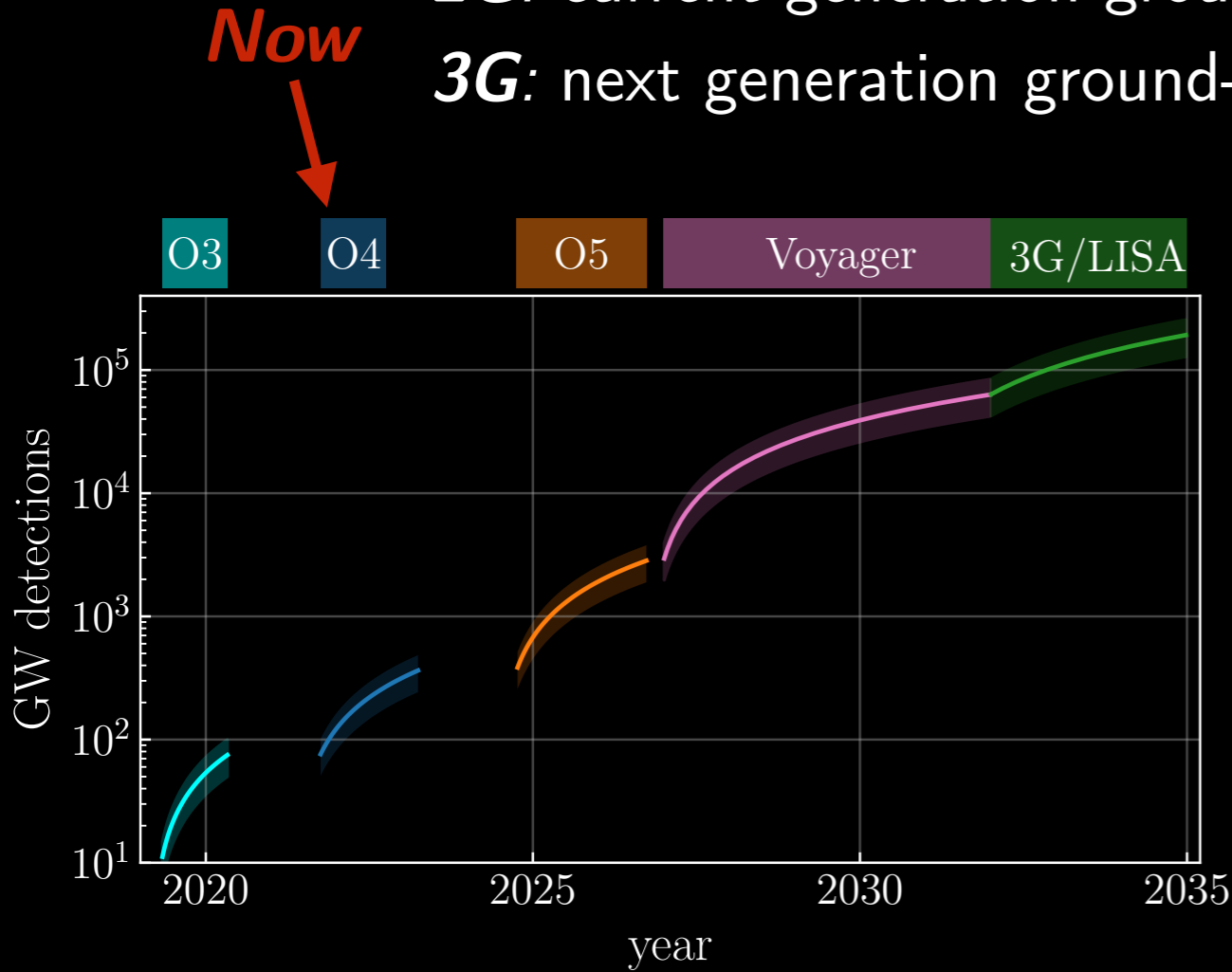
100,000s / year

with most $z > 1$

2G: BNS constraints H_0 , enough to help with Hubble tension?

2G: current generation ground-based GW detectors

3G: next generation ground-based GW detectors



Approx. 100

events typically at

$z < 0.6$



1000s / year

with some $z > 1$



100,000s / year

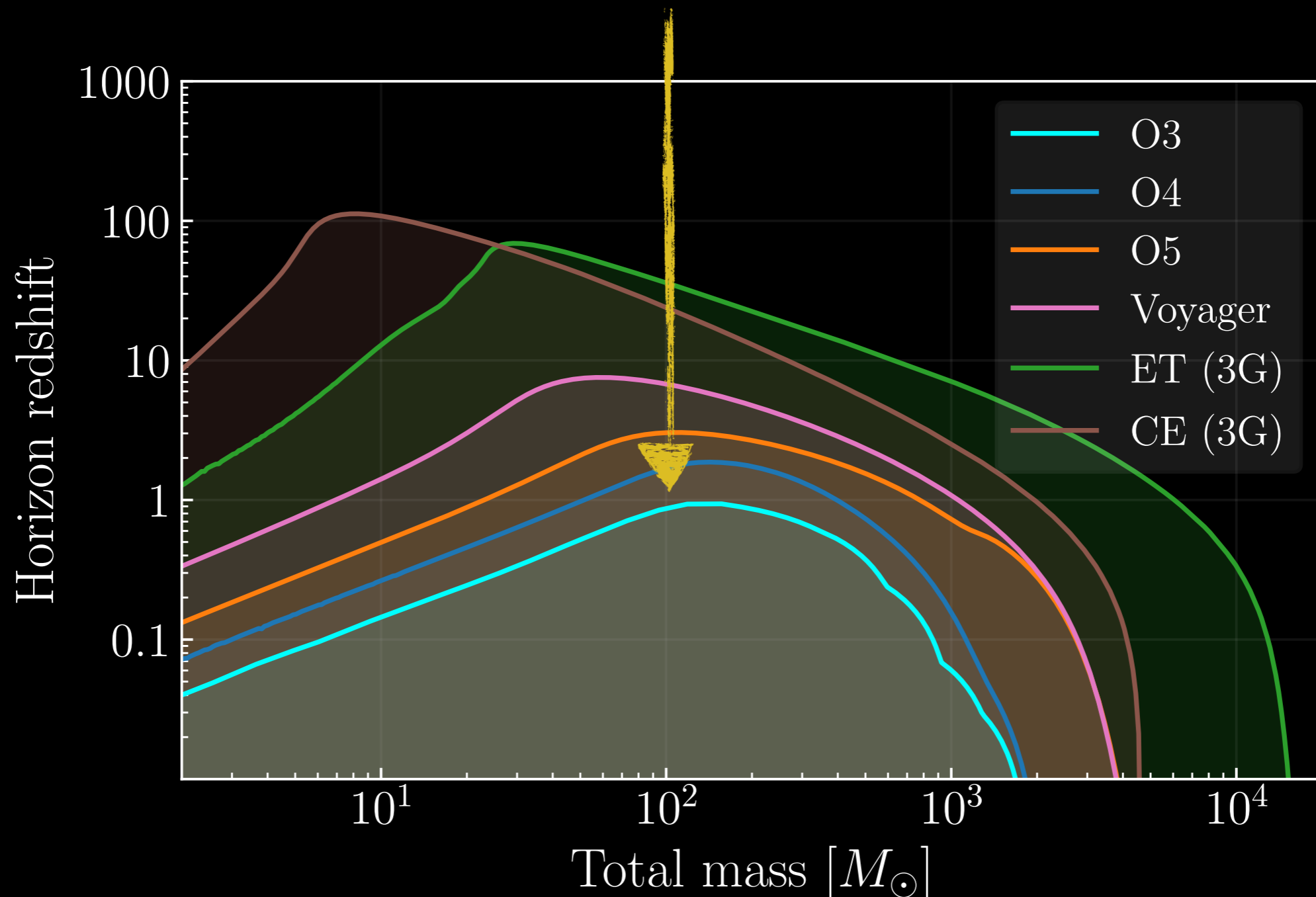
with most $z > 1$

2G: BNS constraints H_0 , enough to help with Hubble tension?

3G: BBHs spectral sirens $H(z > 2)$, new physics?

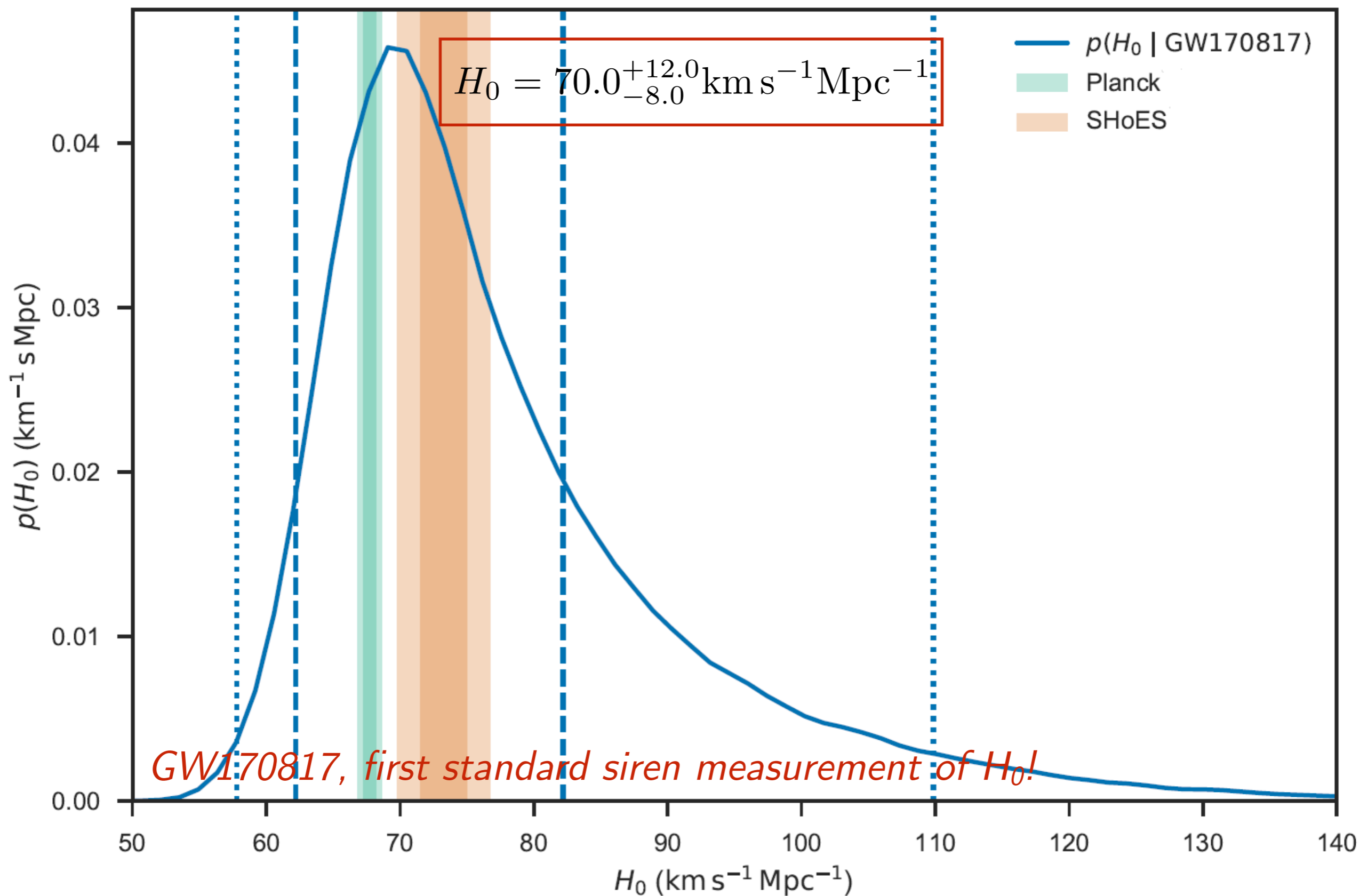
All compact binaries are standard sirens, no electromagnetic information is necessary

Currently, binary black holes most promising

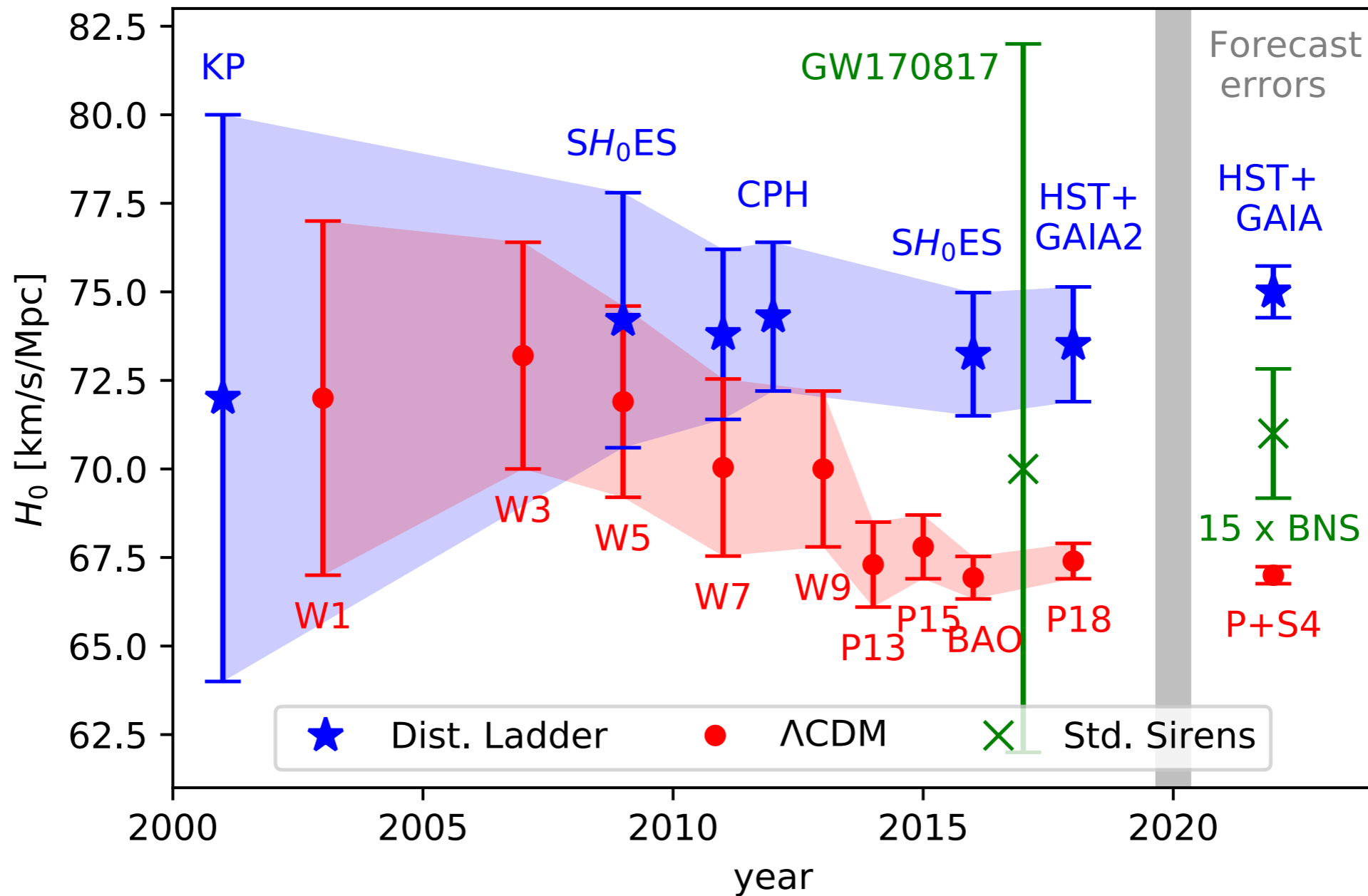


Bright sirens

[Nature 551, 85 (2017)]



Solve Hubble tension?



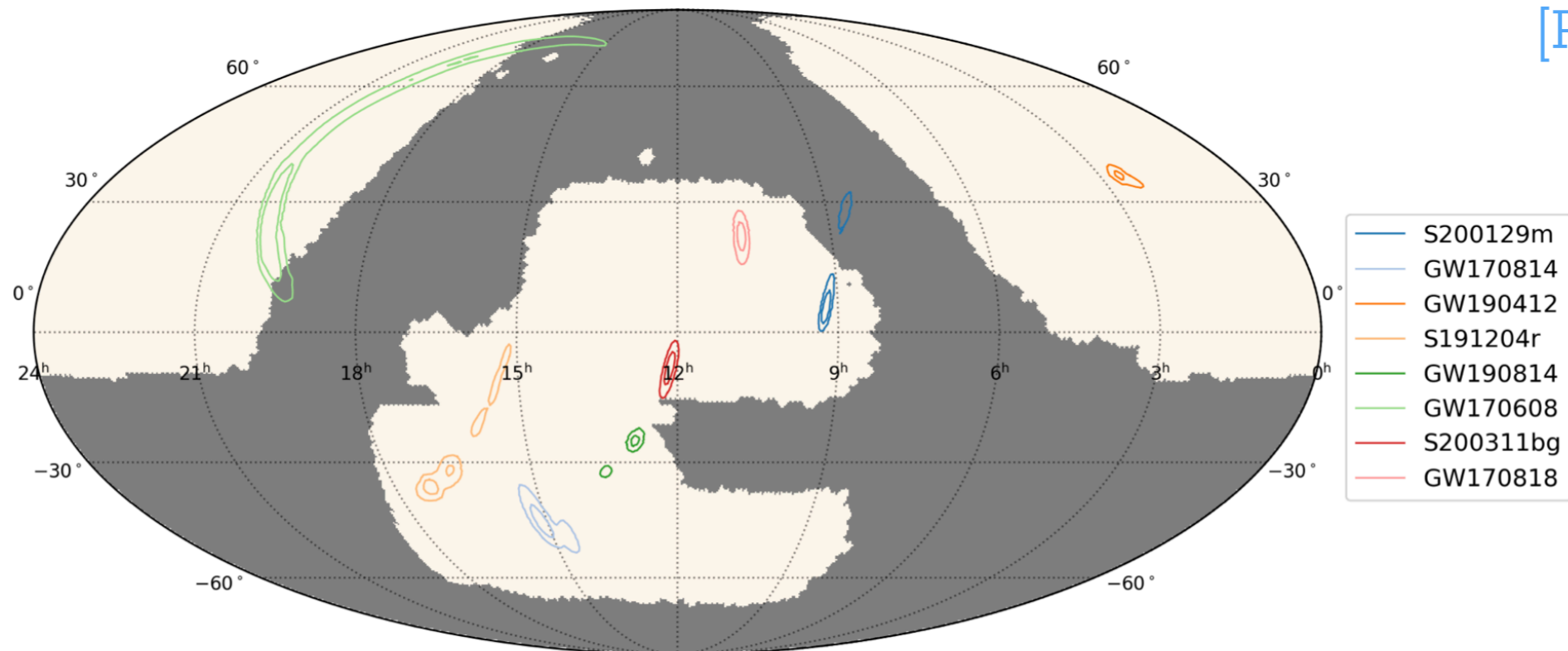
Predictions for O4: $7.7^{+11.9}_{-5.7} \text{ yr}^{-1}$ BNS

[\[2204.07592\]](#)

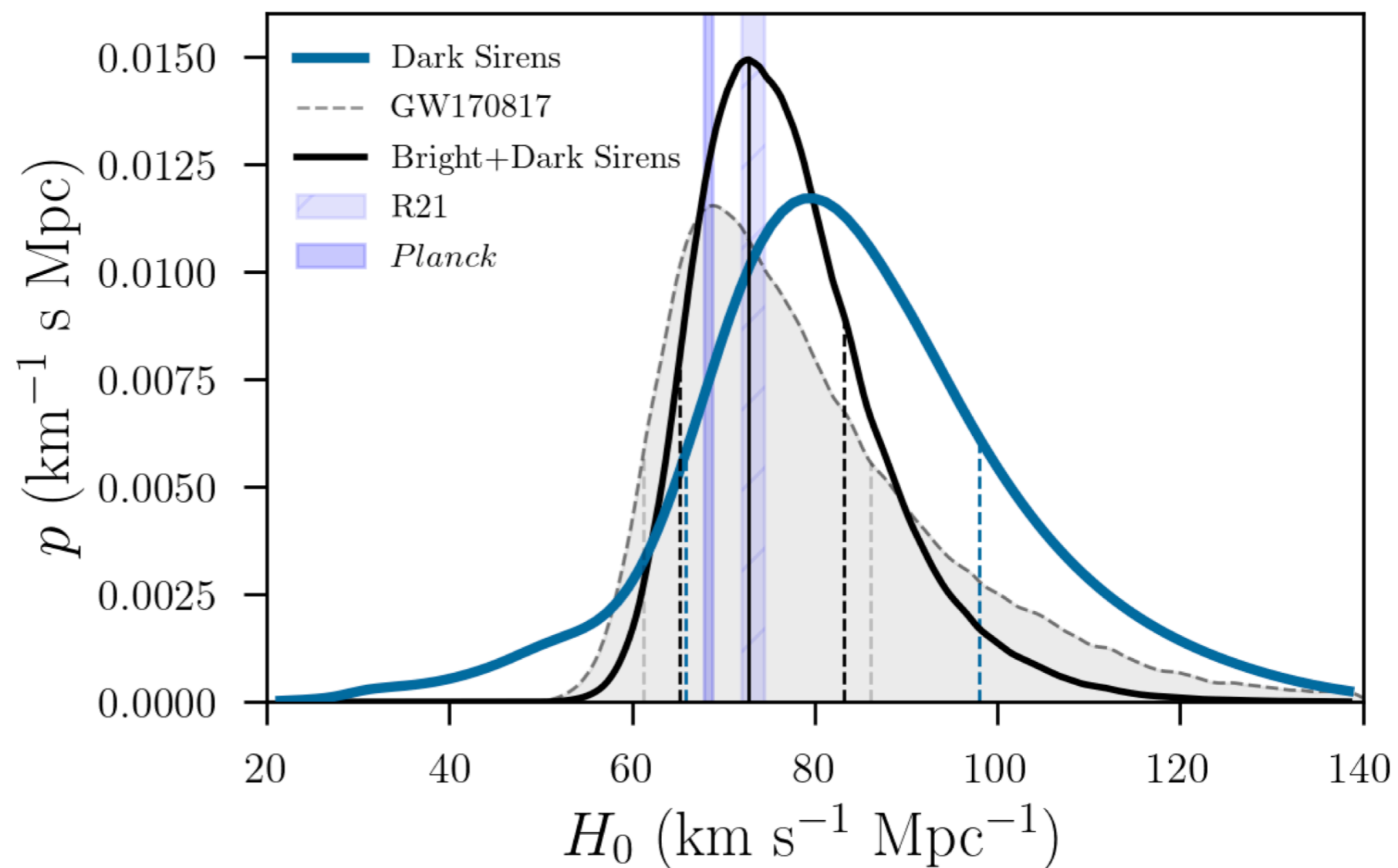
74% kilonova, 2% GRB

DESI imaging dark siren coverage

[Palmese et al., ApJ'23]

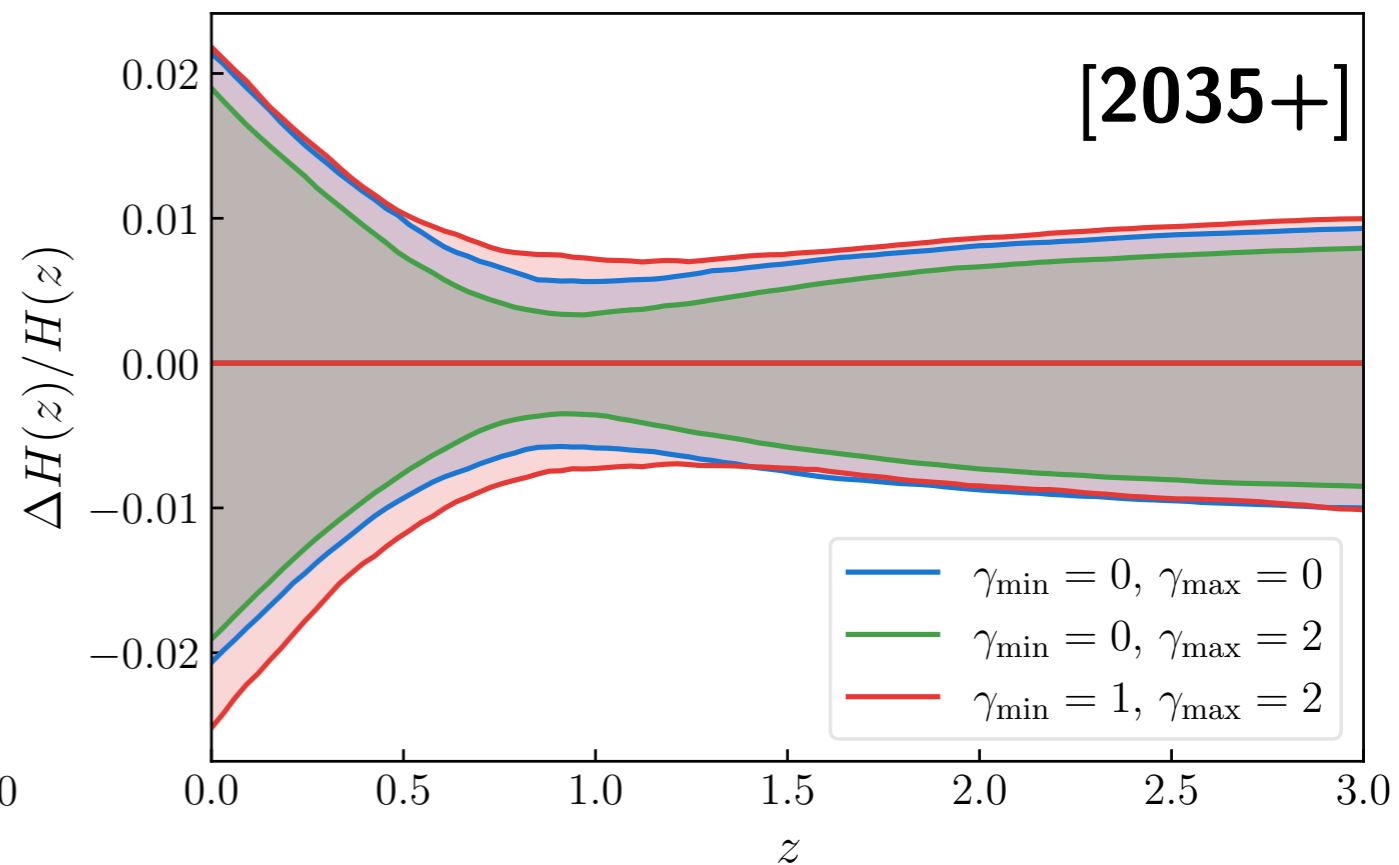
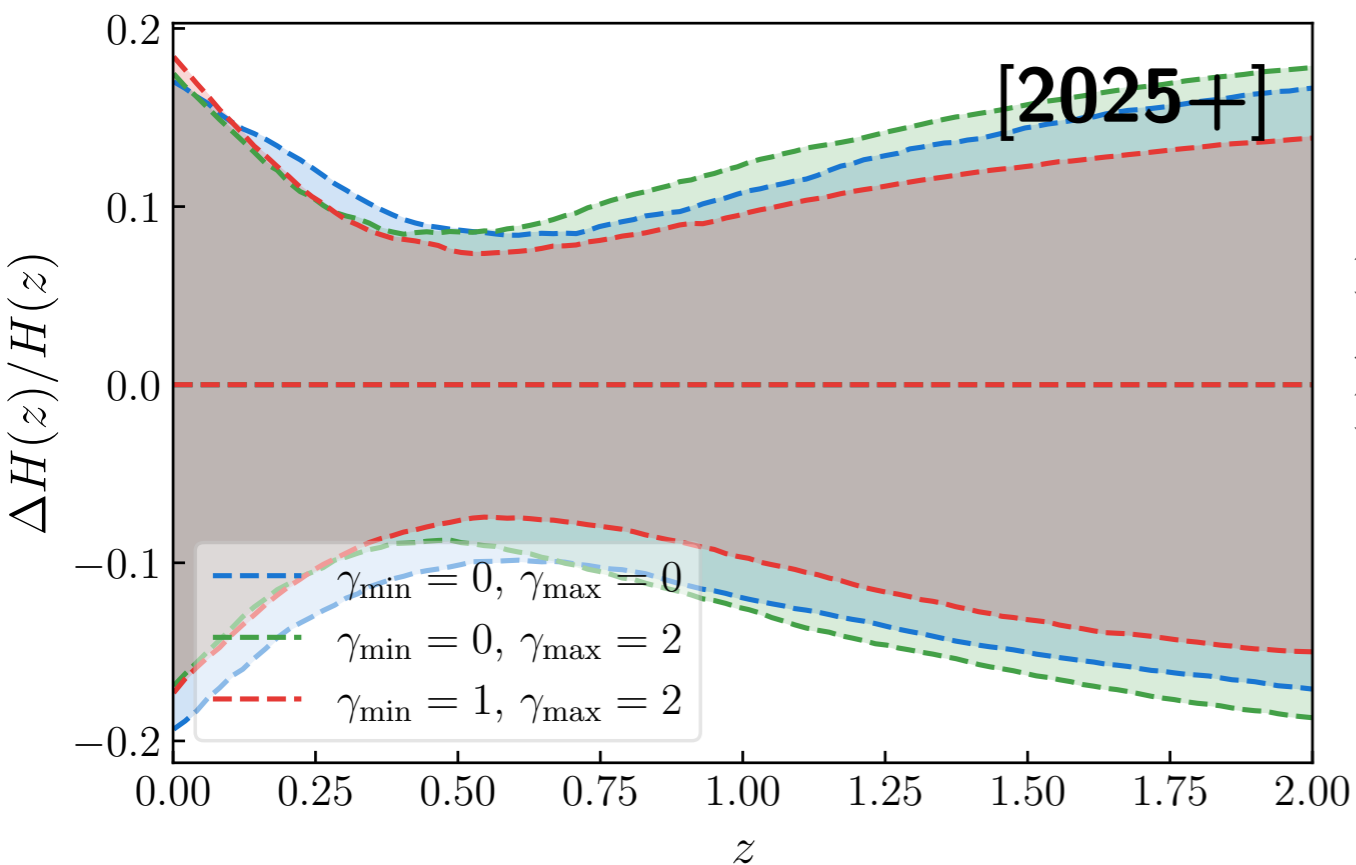


Dark sirens



Spectral sirens: forecasts

[BBHs between NSBH and PISN gap]



2G: <10% within 1 year at approx. $z=0.7$

3G: Sub-percent within 1 month. High-redshift!

ΛCDM

H_0

Ω_Λ

Ω_M

Ω_R

cosmological principle

general relativity

General Relativity

Unique theory
of massless $g_{\mu\nu}$





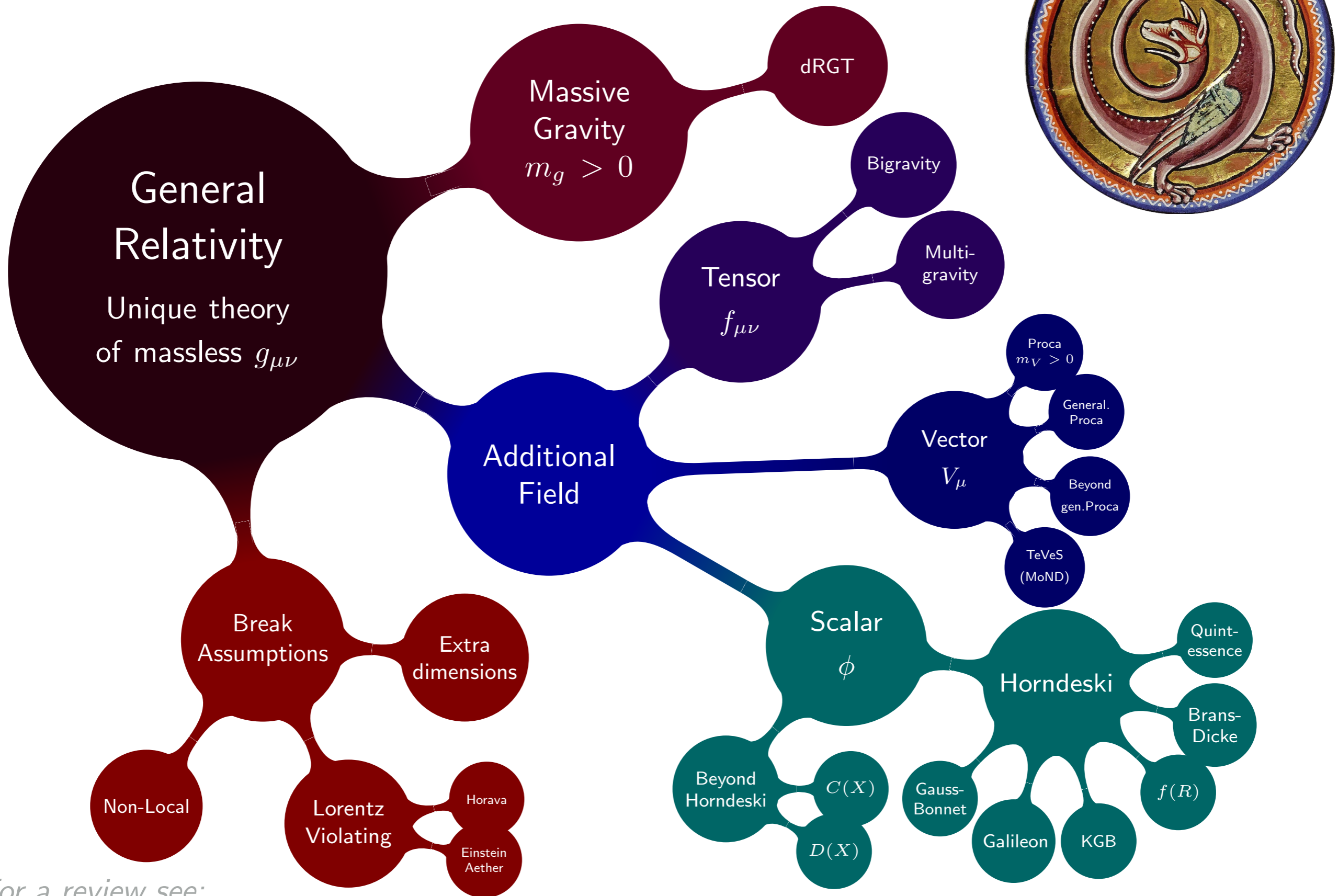
General Relativity

Unique theory
of massless $g_{\mu\nu}$

Basic GW properties

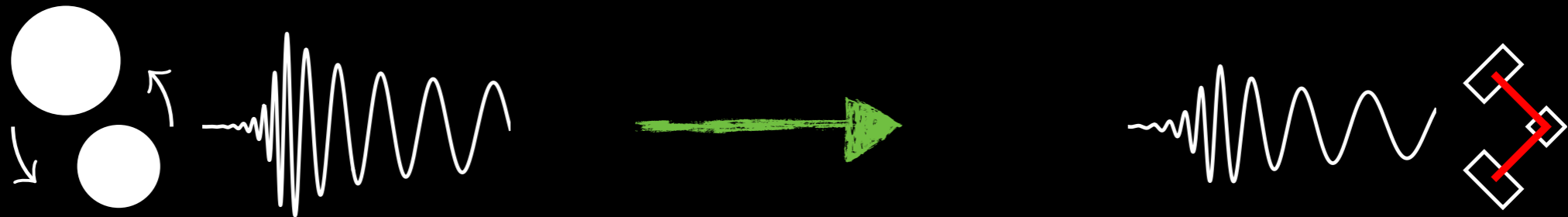
- Propagate speed of light
- Amplitude scales with inverse of distance
- No dispersion
- Two tensor polarizations propagating equally

Modified gravity roadmap



For a review see:

Modified GW propagation



$$h''_A + (2 + \nu) \mathcal{H} h'_A + (c_g^2 k^2 + \Delta\omega) h_A = \mathcal{O}_{AB} h_B$$

- **Speed**: changes arrival time
- **Amplitude**: modifies luminosity distance
- **Phase**: may produce waveform distortions
- **Polarization**: birefringence, additional tensor modes

Small deviations accumulate over cosmological propagation times!

For propagation effects beyond cosmological backgrounds:

Ezquiaga & Zumalacárregui; GW lensing beyond GR (PRD, [arXiv 2009.12187](https://arxiv.org/abs/2009.12187))

The speed of GWs

General relativity predicts:

$$c_g = c$$

The speed of GWs

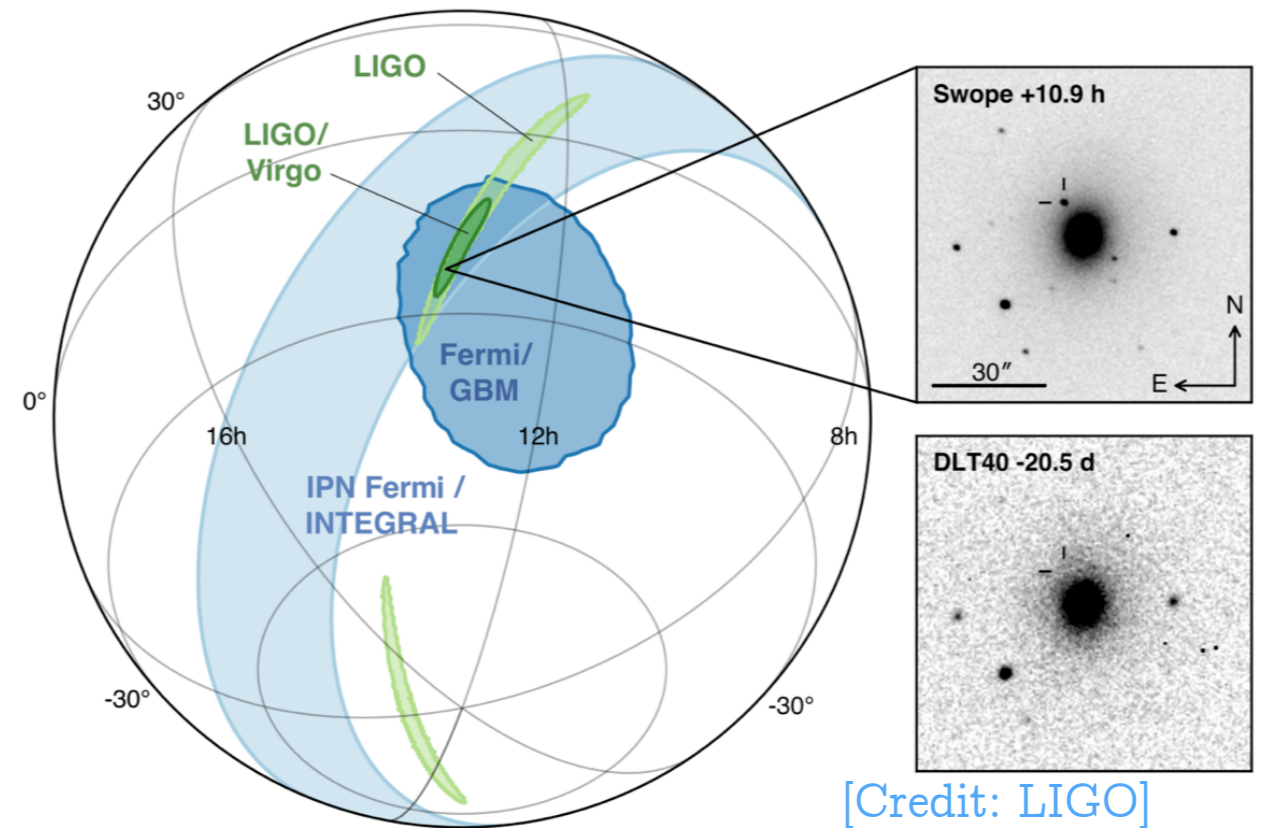
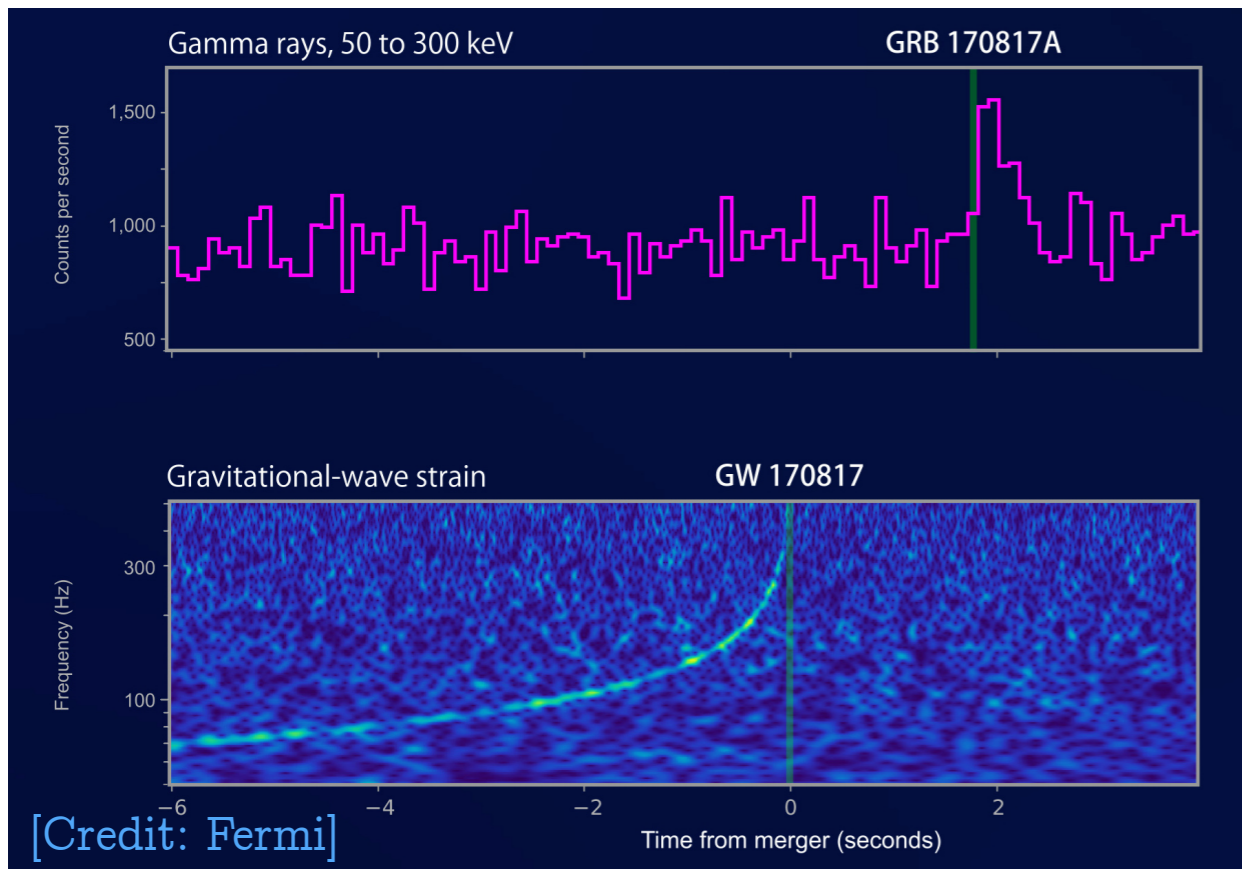
General relativity predicts:

$$c_g = c$$

GW170817: *multi-messenger* event

[LVC, Fermi, INTEGRAL'17]

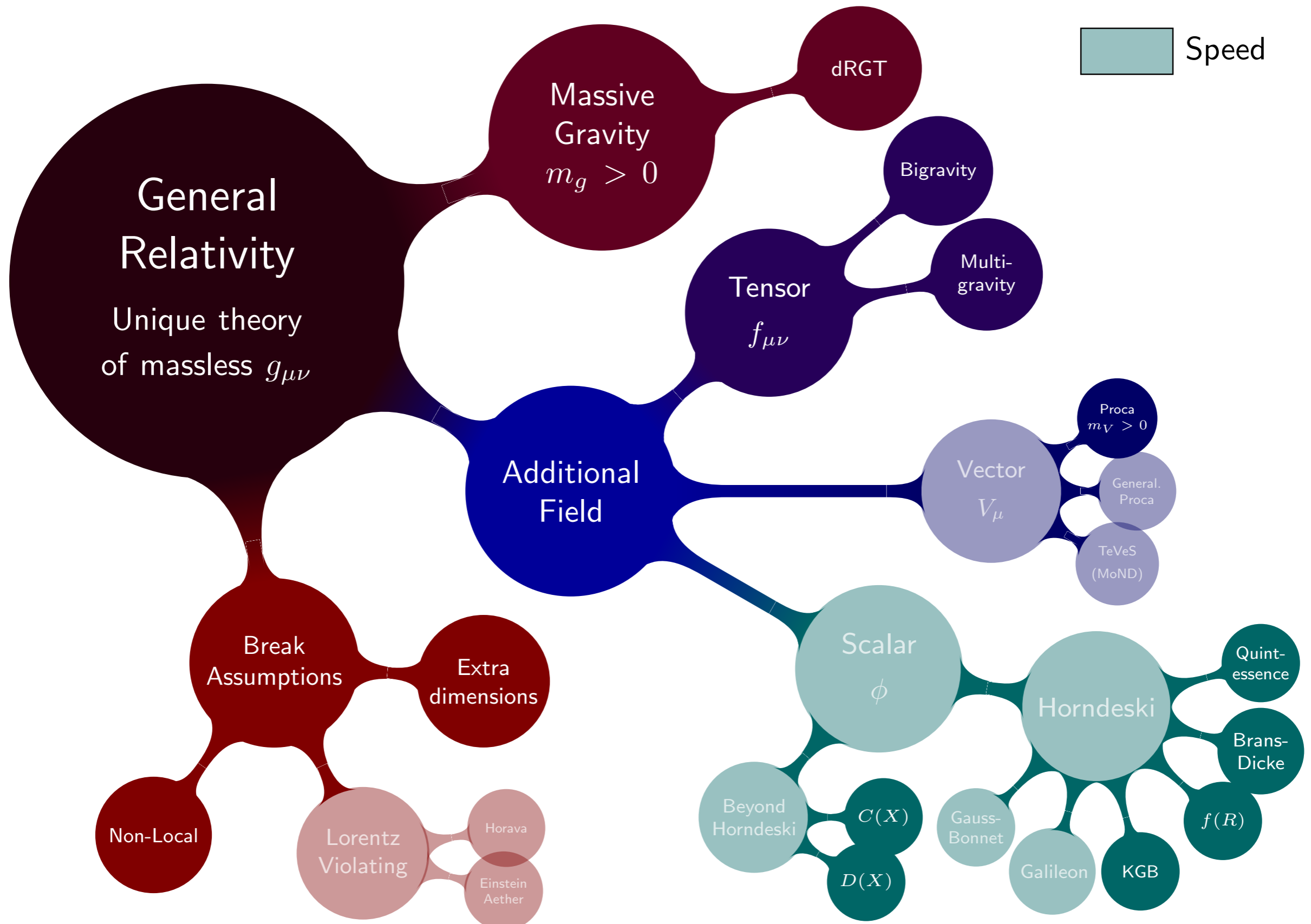
$$-3 \cdot 10^{-15} \leq c_g/c - 1 \leq 7 \cdot 10^{-16}$$



Modified gravity roadmap and GW astronomy

Constrained by

Speed



GW luminosity distance

General relativity predicts:

$$d_L^{\text{gw}} = d_L^{\text{em}}$$

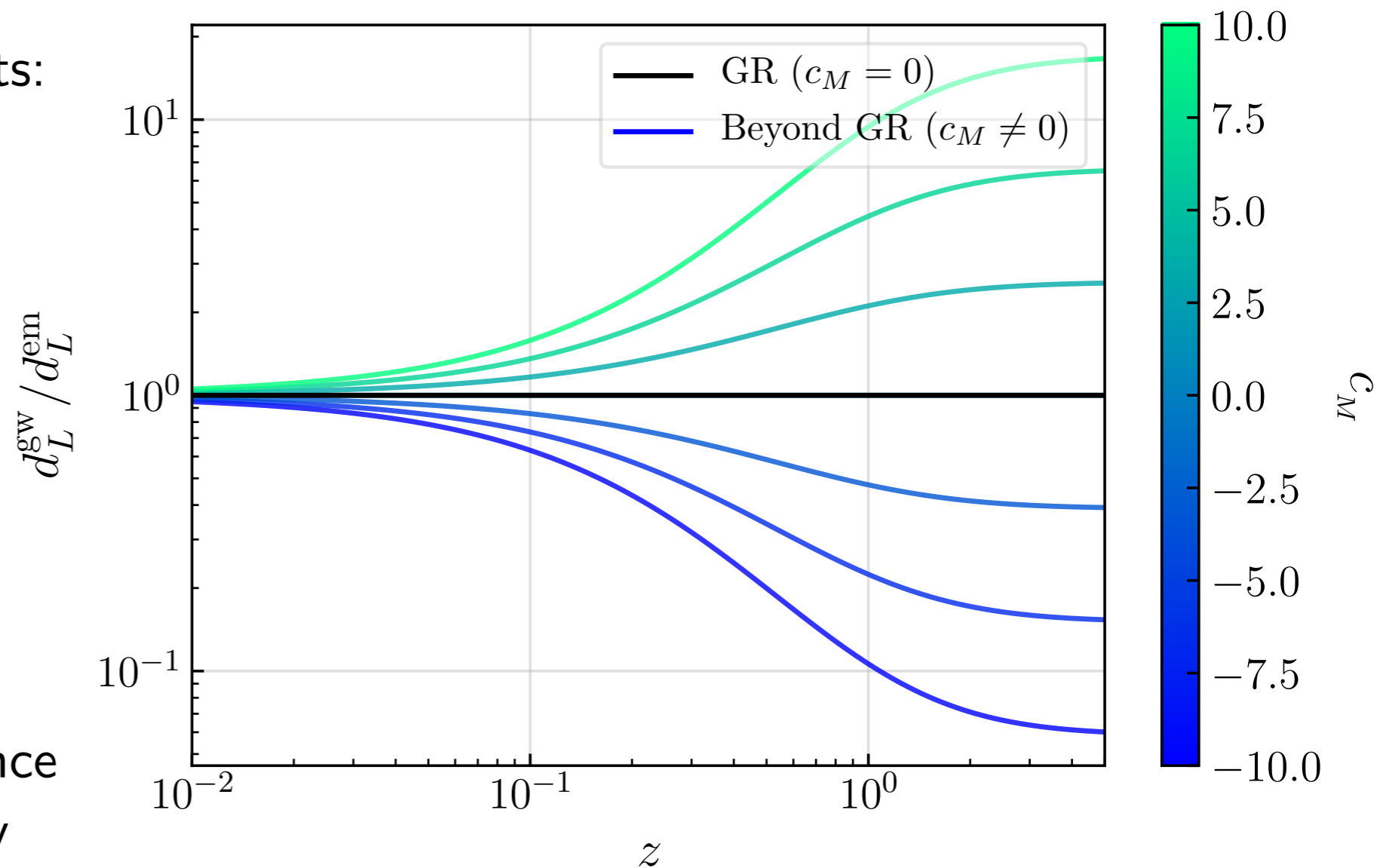
GW luminosity distance

General relativity predicts:

$$d_L^{\text{gw}} = d_L^{\text{em}}$$

Modified luminosity distance
triggered by dark energy

$$\frac{d_L^{\text{gw}}}{d_L^{\text{em}}} = \exp \left[\frac{c_M}{2} \int_0^z \frac{\Omega_{DE}(z')}{(1+z')\Omega_{DE}(0)} dz' \right]$$



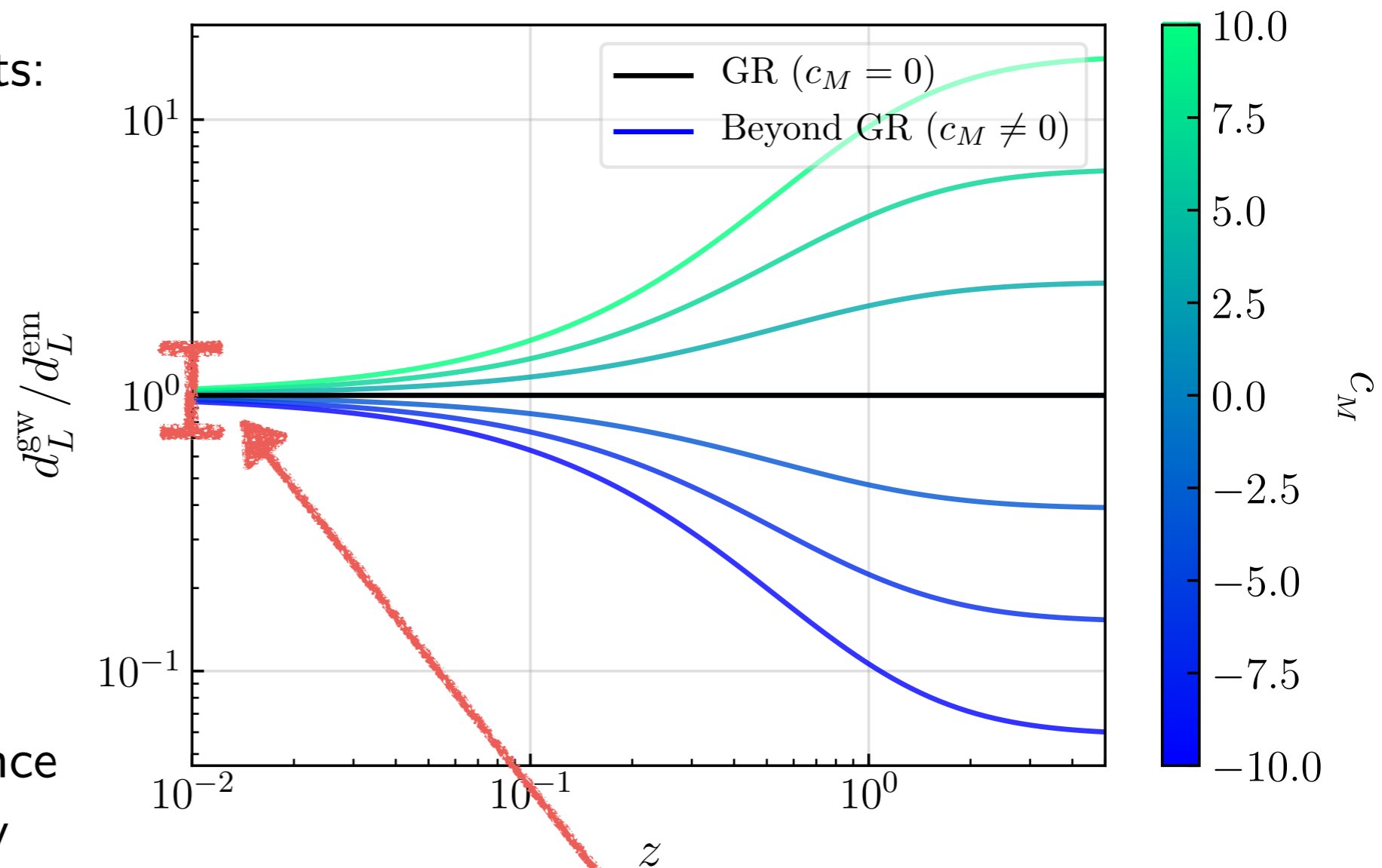
GW luminosity distance

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Modified luminosity distance
triggered by dark energy

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Bright sirens (GW170817)

$$c_M = -9_{-28}^{+21}$$

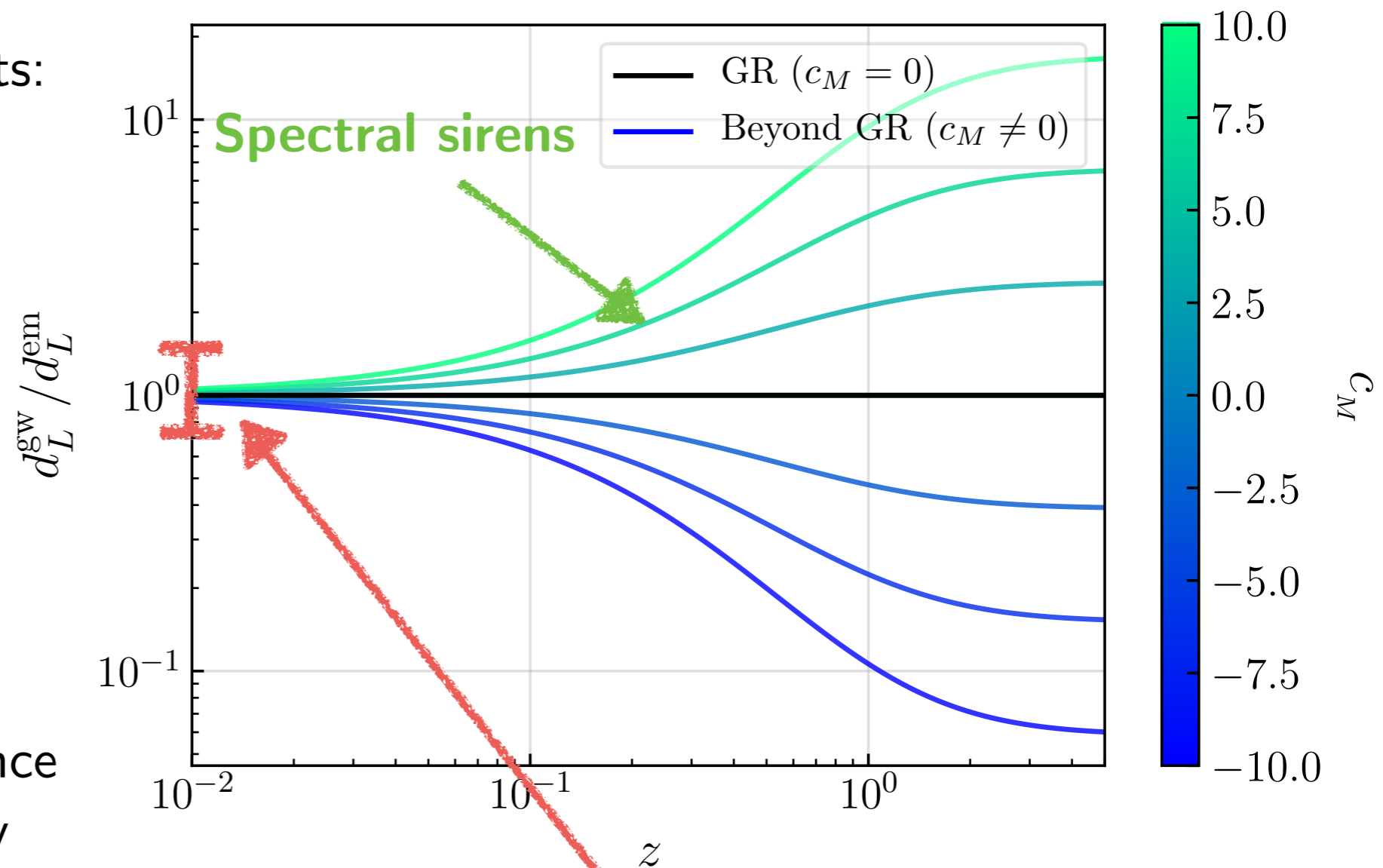
GW luminosity distance

General relativity predicts:

$$d_L^{\text{gw}} = d_L^{\text{em}}$$

Modified luminosity distance
triggered by dark energy

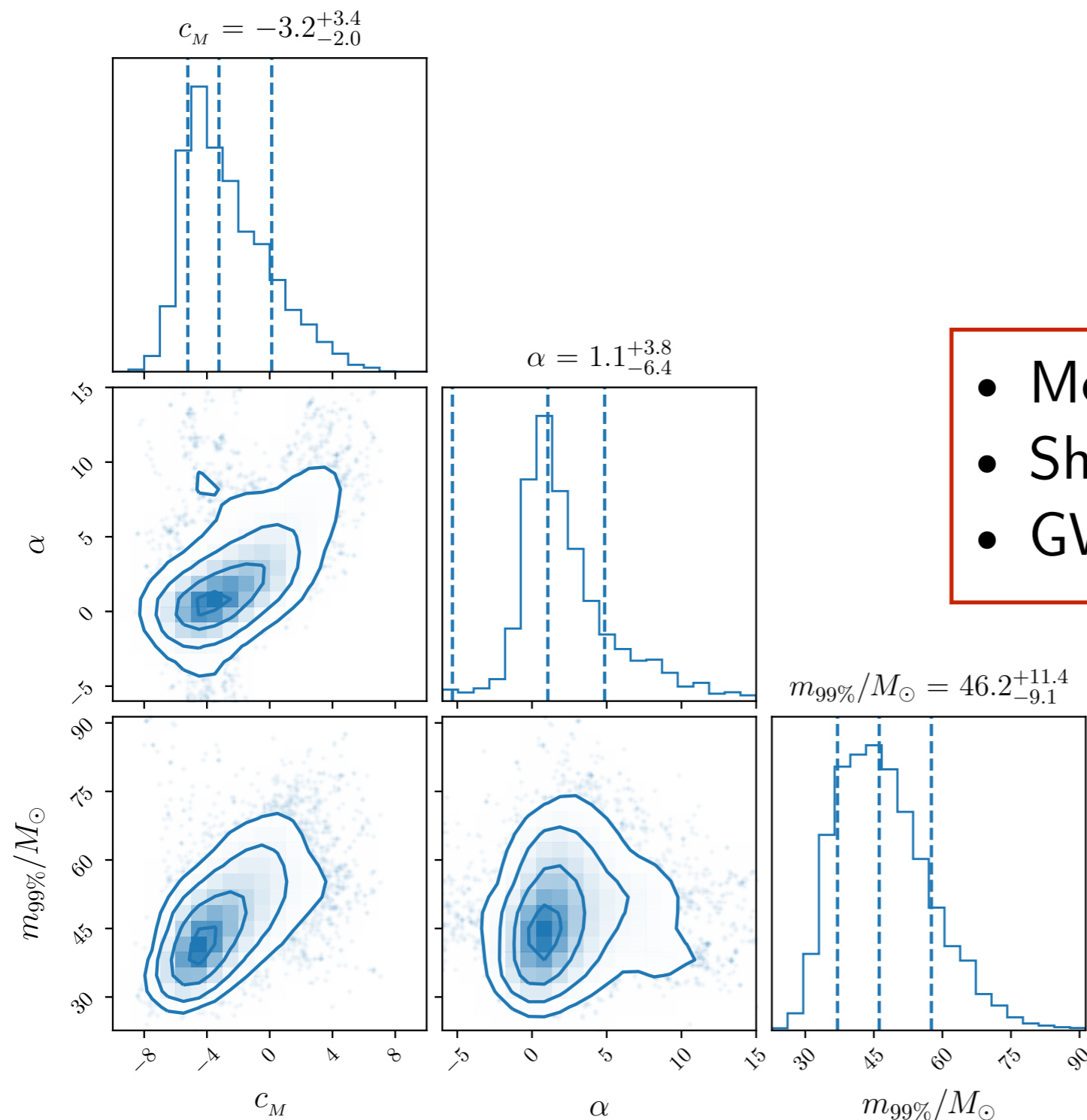
$$\frac{d_L^{\text{gw}}}{d_L^{\text{em}}} = \exp \left[\frac{c_M}{2} \int_0^z \frac{\Omega_{DE}(z')}{(1+z')\Omega_{DE}(0)} dz' \right]$$



Bright sirens (GW170817)

$$c_M = -9_{-28}^{+21}$$

Results from GWTC-2



$$c_M = -3.2^{+3.4}_{-2.0}$$

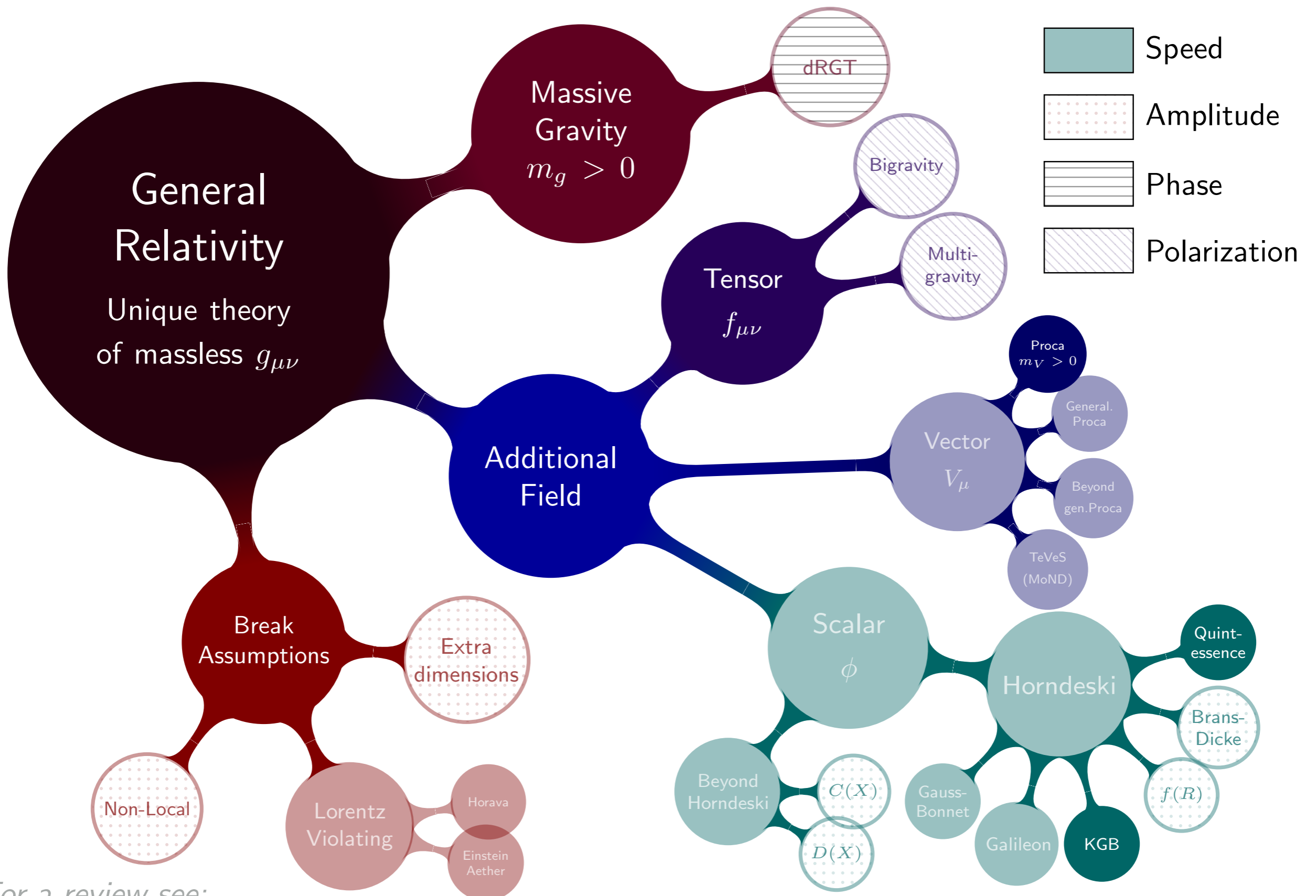
- More constraining than GW170817
- Shifts $m_{99\%}$ to lower values
- GW data only!

GWTC-2 = O1+O2+O3a

GWTC-3 = O1+O2+O3a+O3b

See [Mancarella et al.'21](#) and [Leyde et al.'22](#) for GWTC-3 constraints!

Modified gravity roadmap and GW astronomy



For a review see:

Λ CDM

H_0

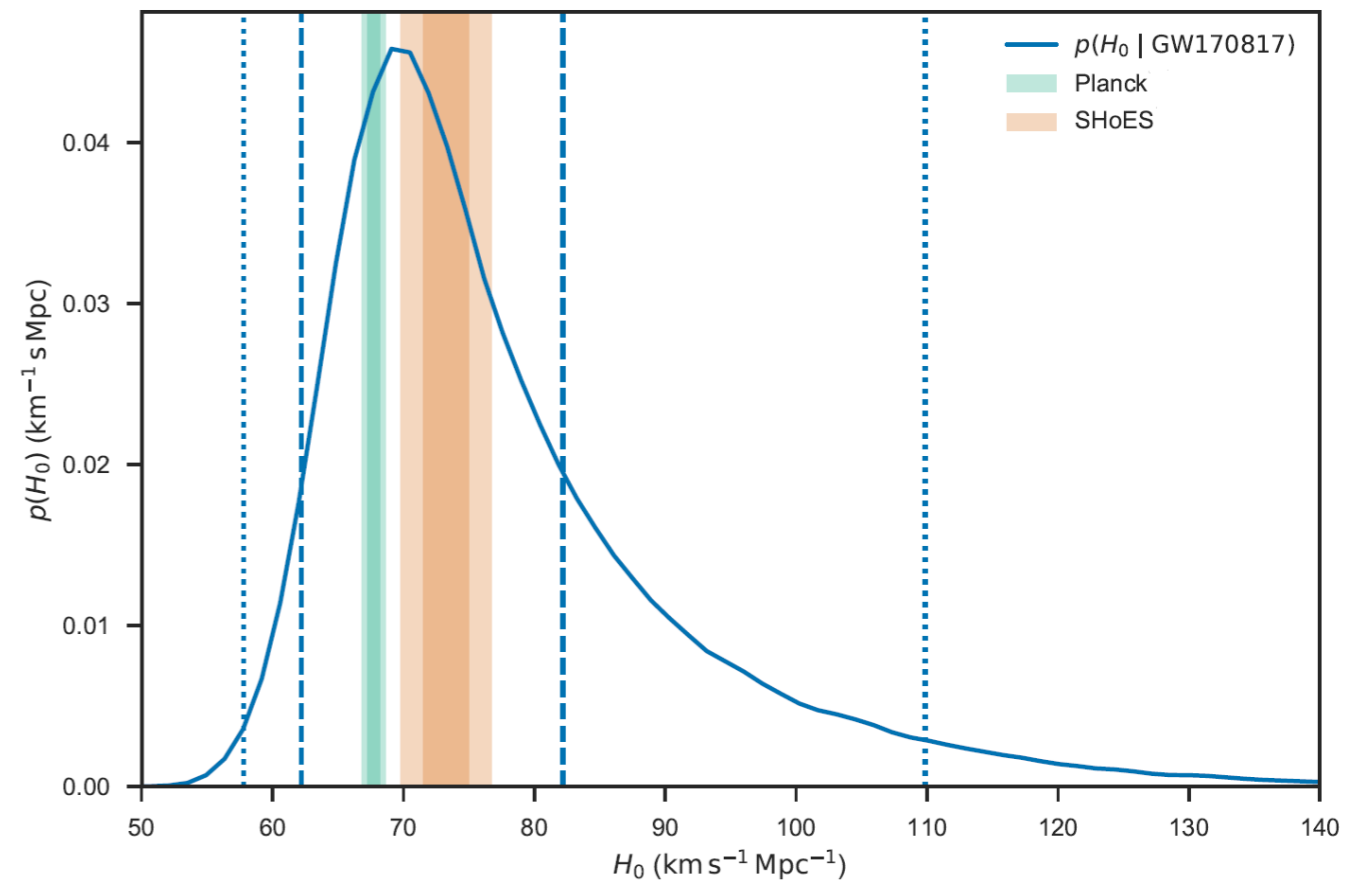
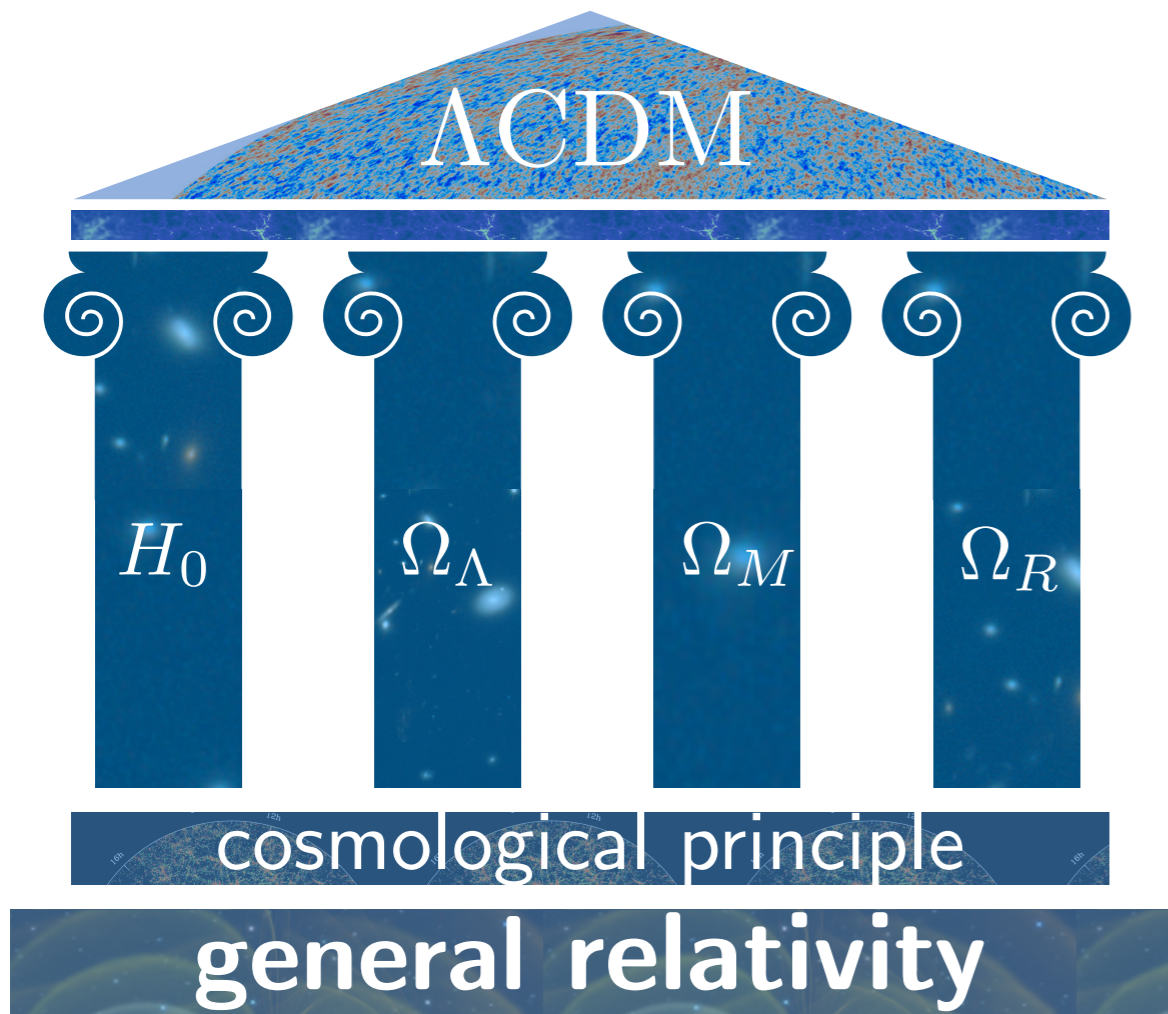
Ω_Λ

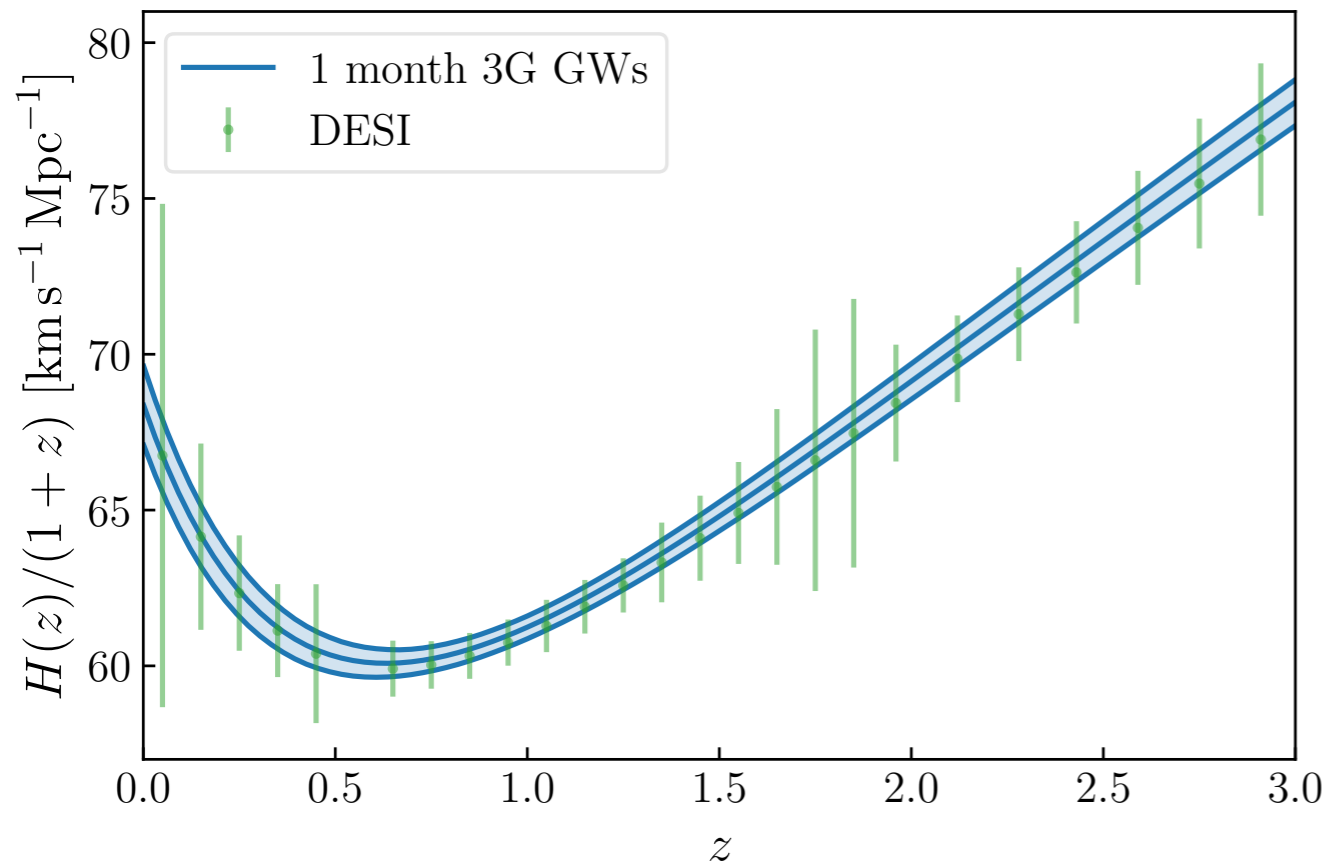
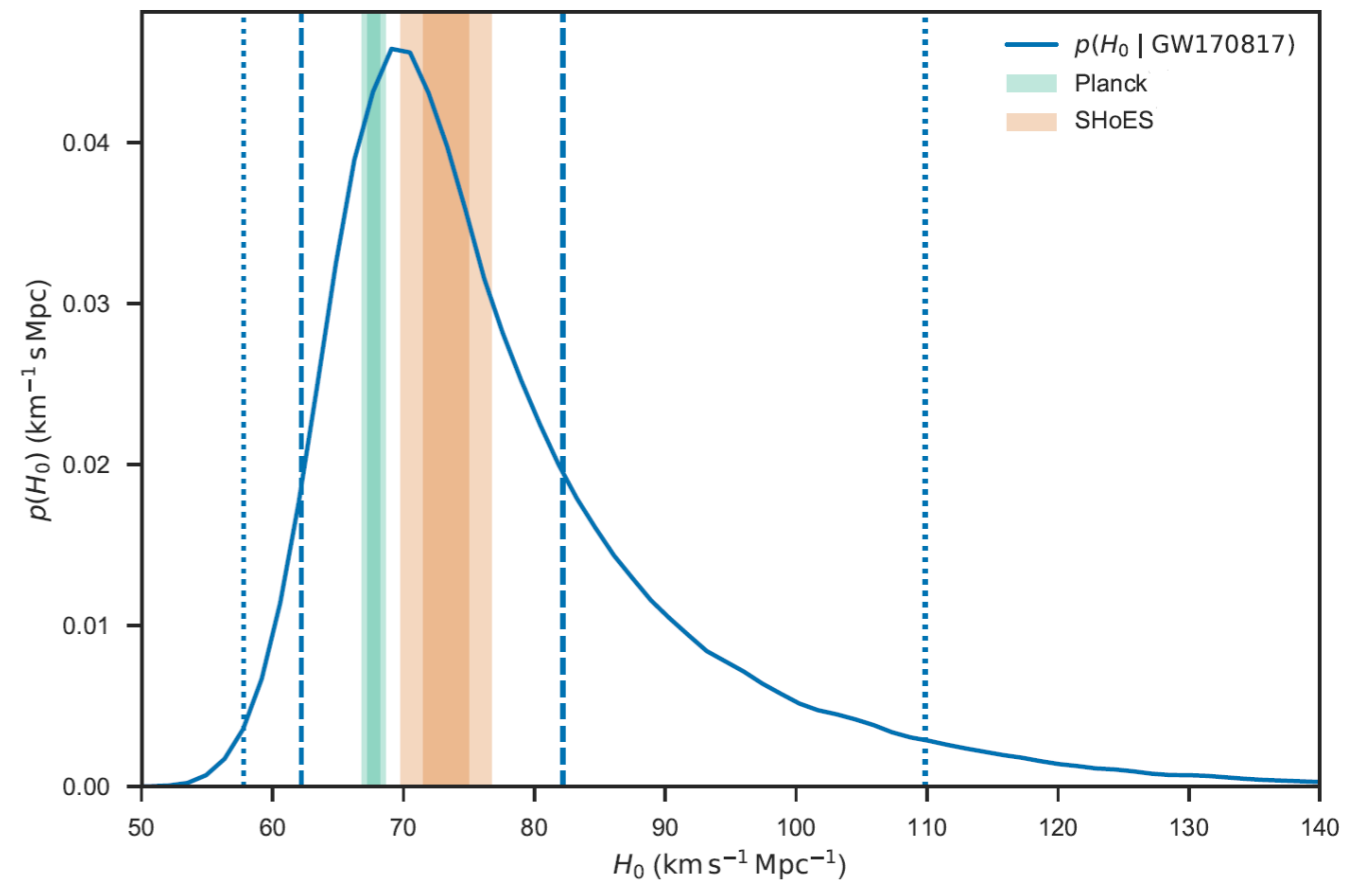
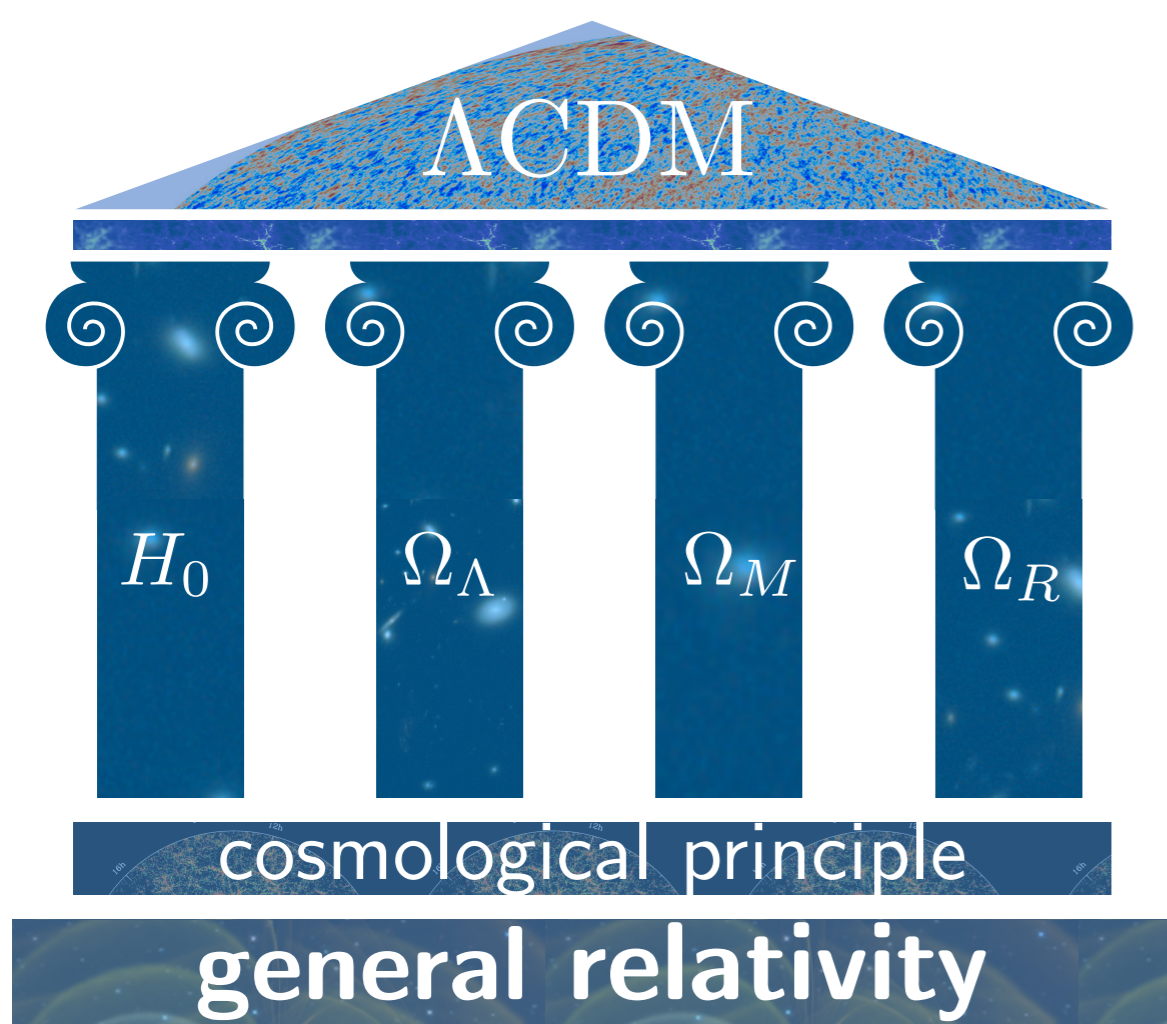
Ω_M

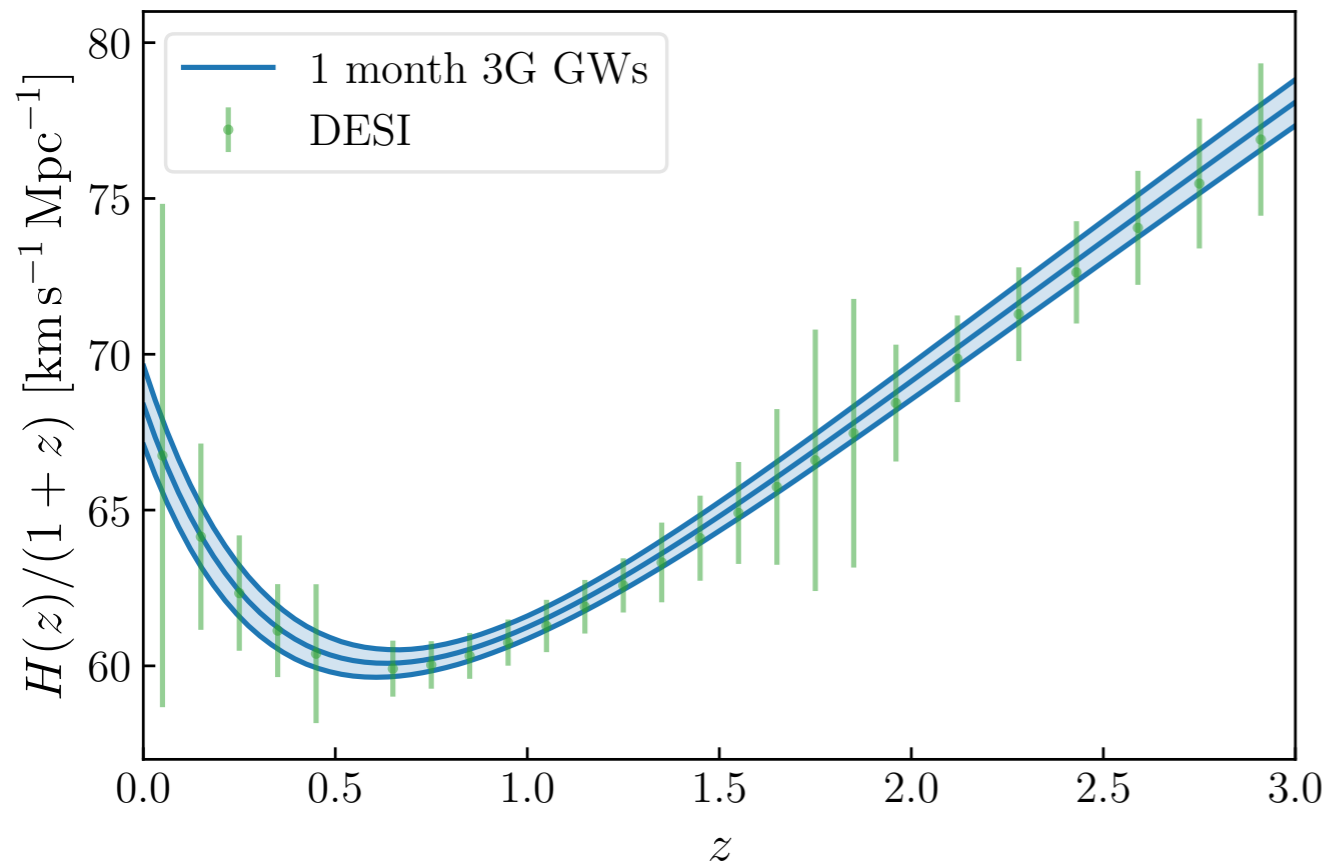
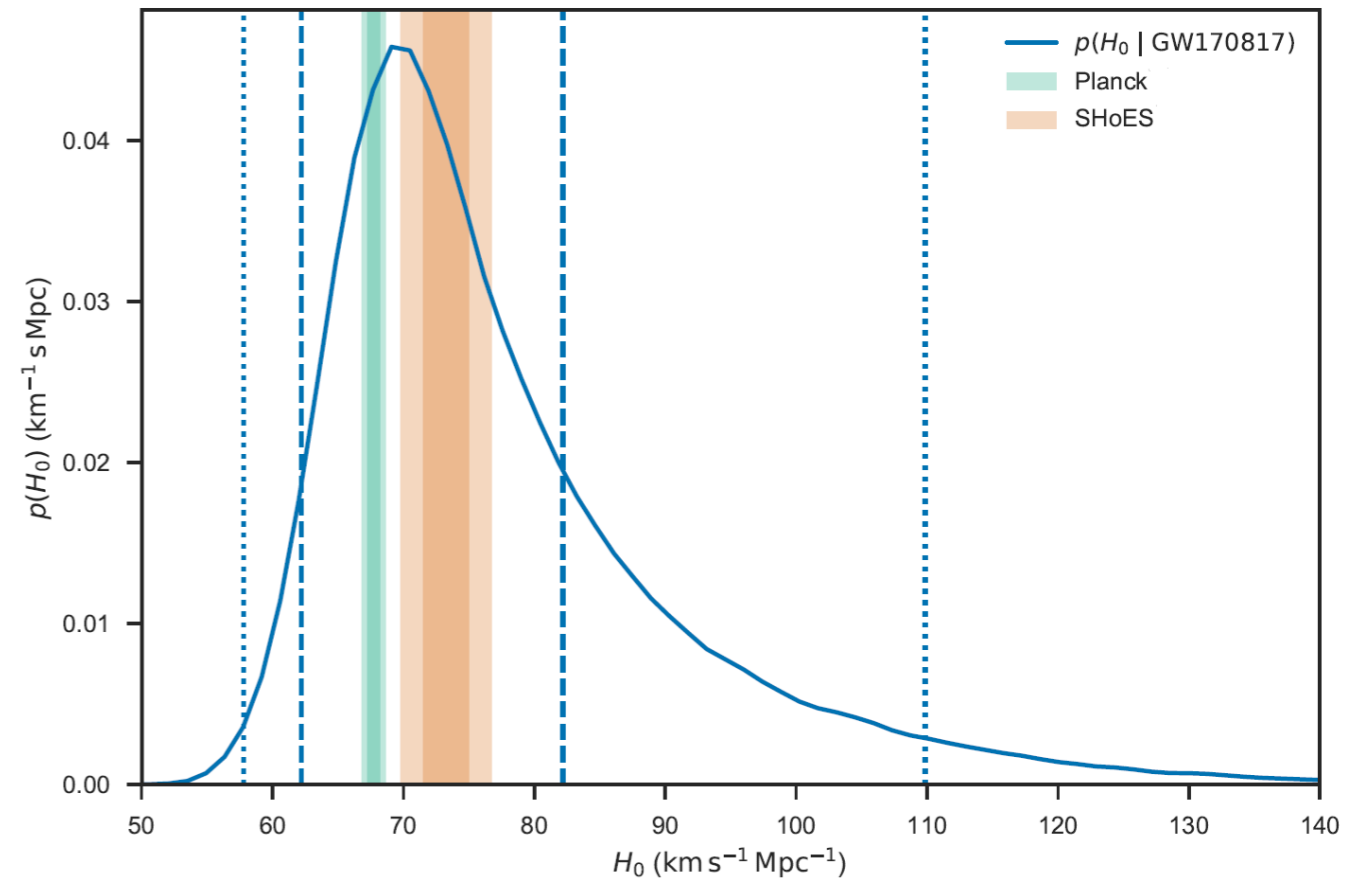
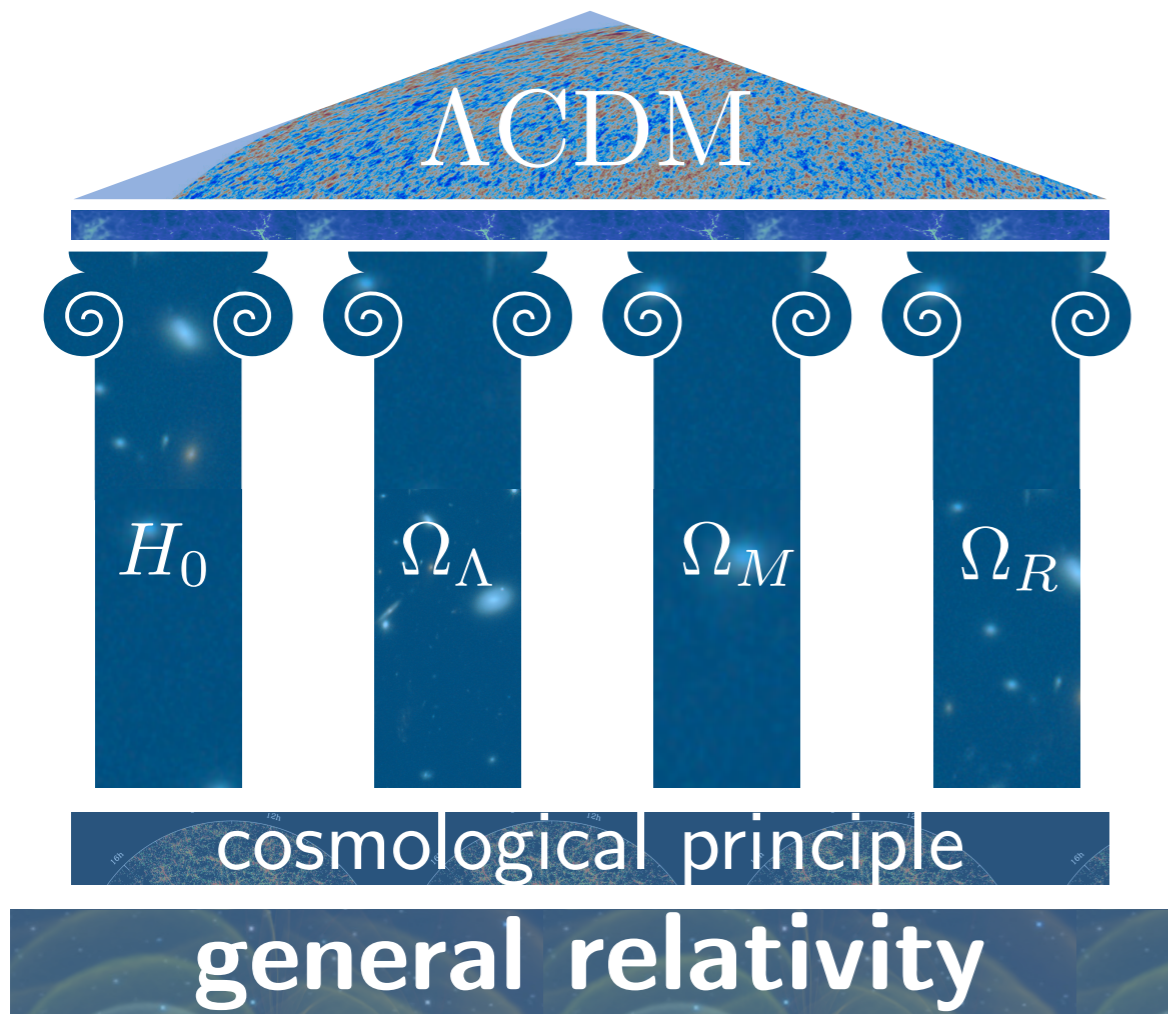
Ω_R

cosmological principle

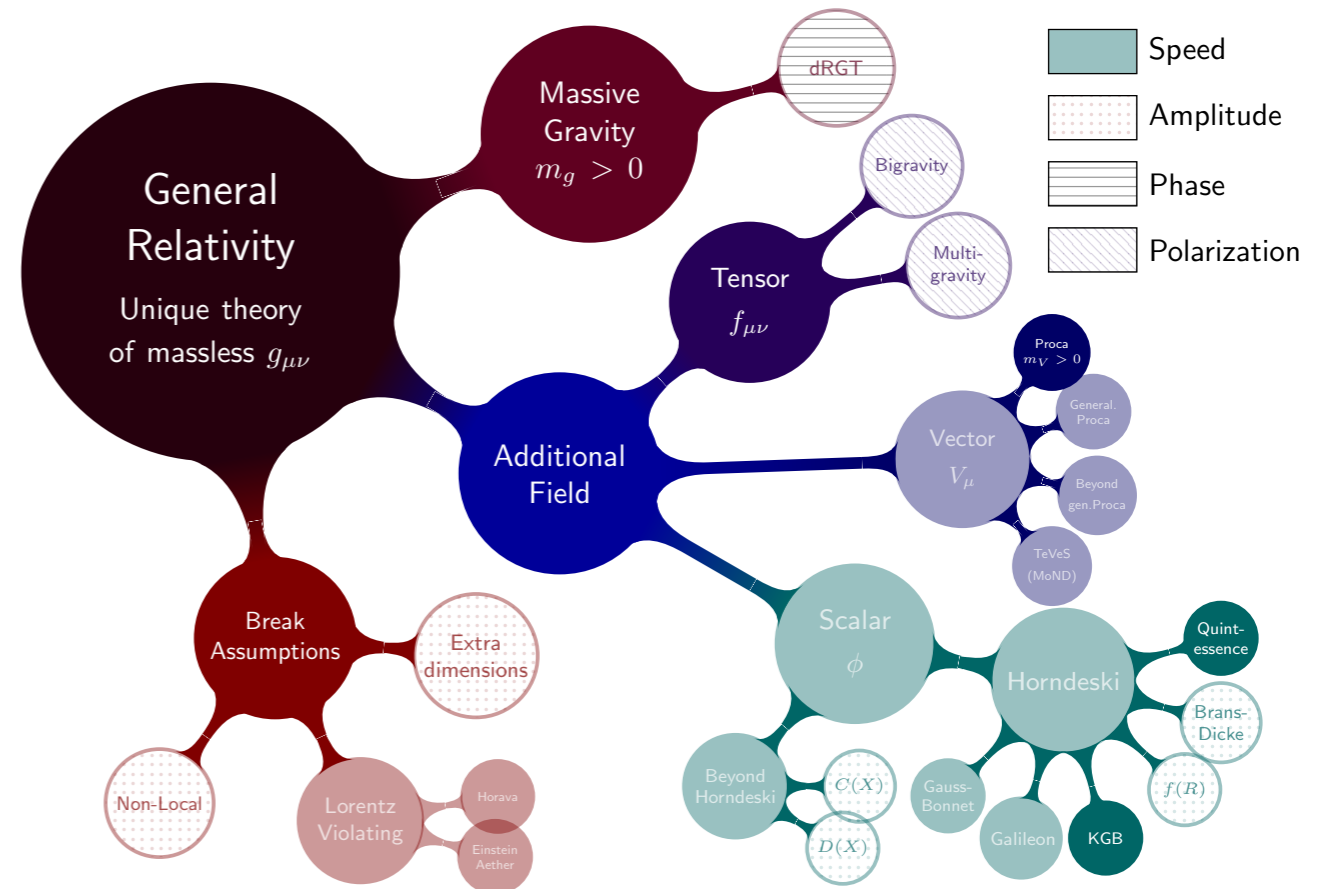
general relativity







Modified gravity roadmap and GW astronomy





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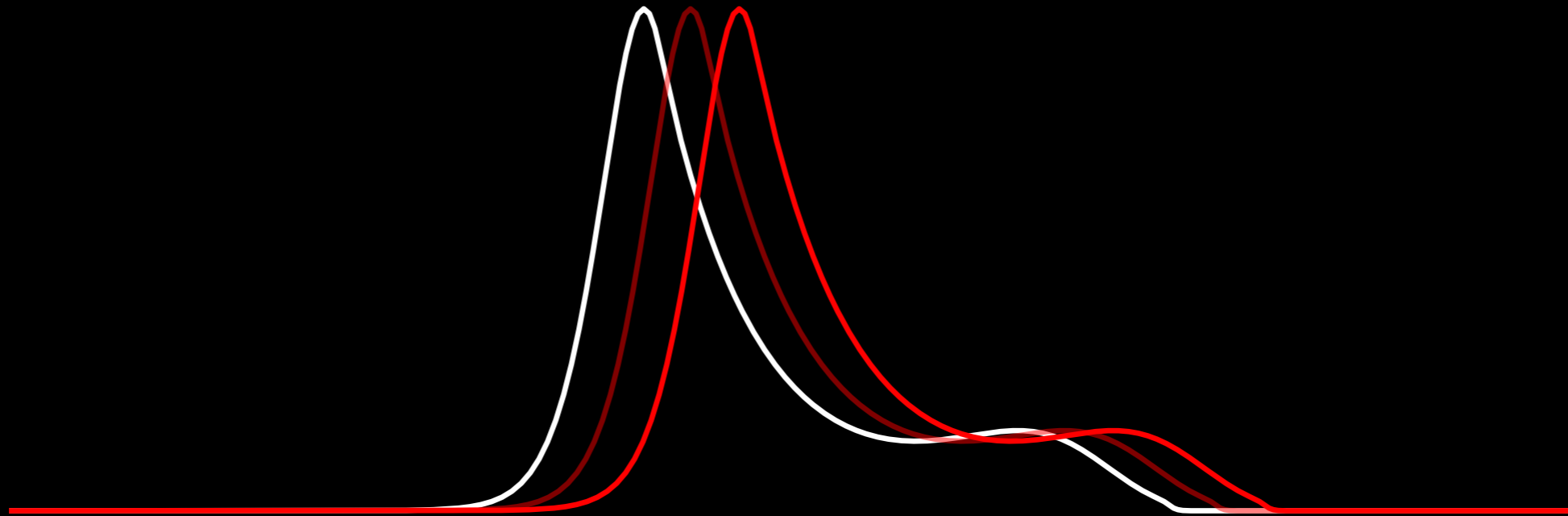
INTERACTIONS

VILLUM FONDEN

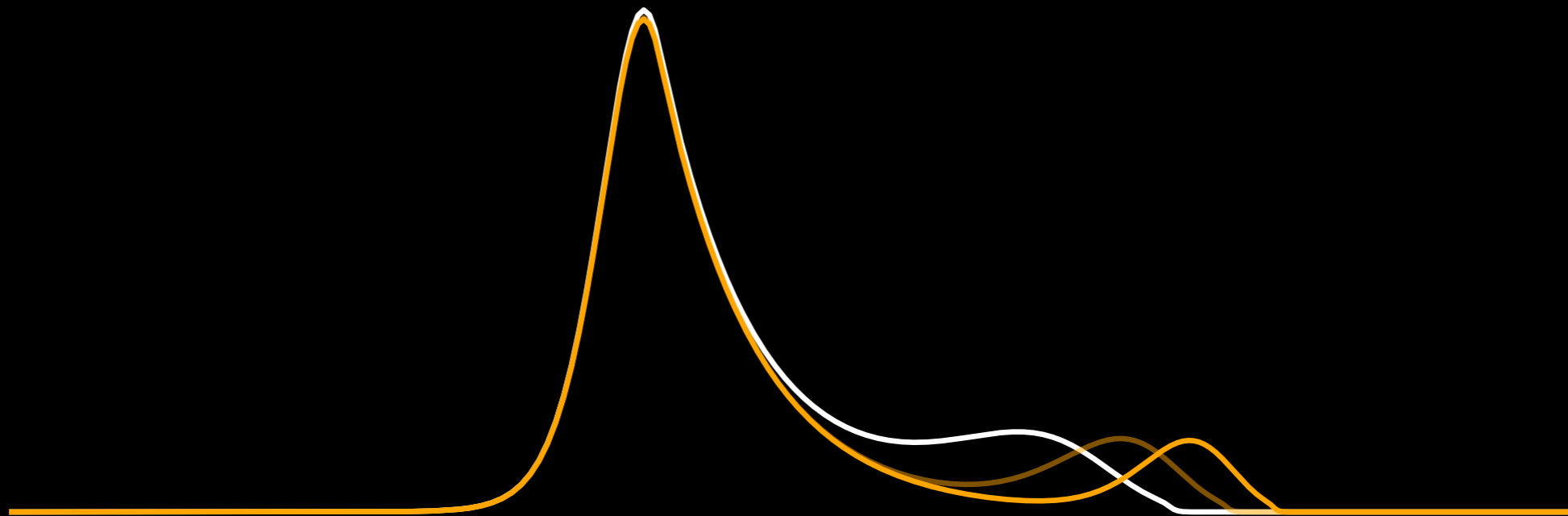


Supplemental material

Cosmology

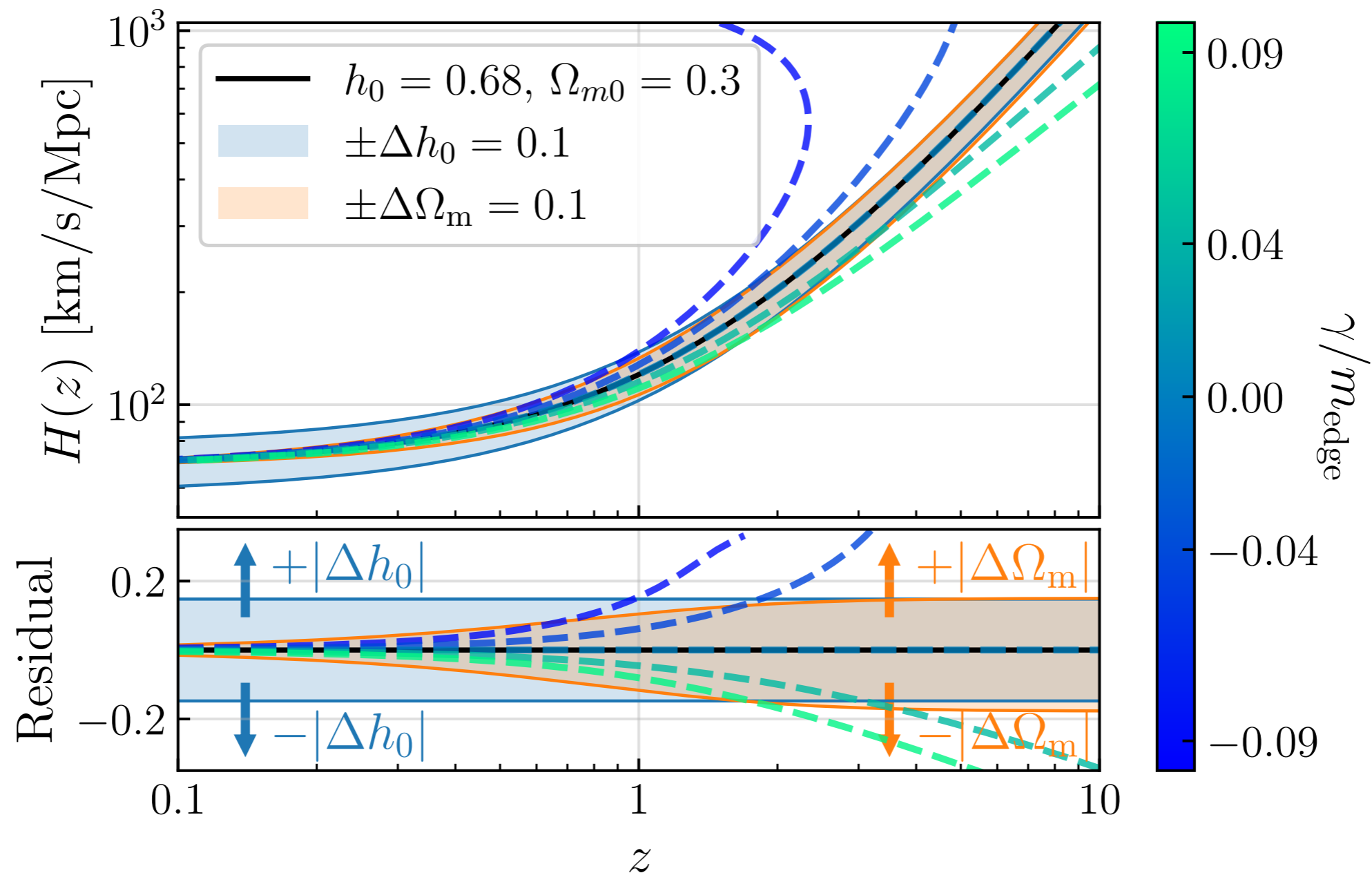


Astrophysics



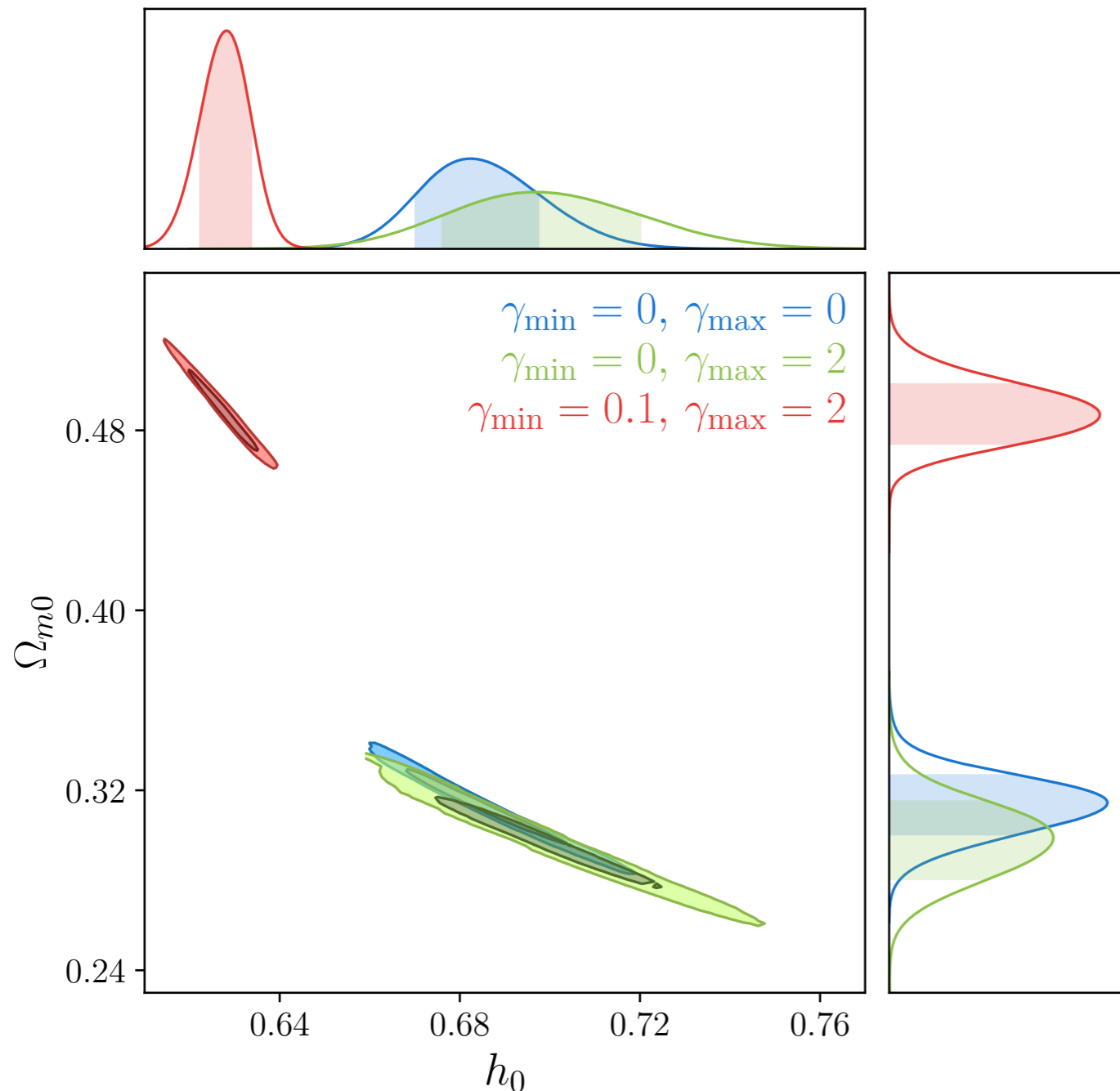
$\log[\text{Detector frame mass}]$

“By using the full mass distribution, we demonstrate that **degeneracies** between mass evolution and cosmological evolution **can be broken**, unless an astrophysical conspiracy shifts all features of the full mass distribution simultaneously following the (non-trivial) Hubble diagram evolution.”



Example: 3G cosmo inference

[10,000 **BBHs** between NSBH and PISN gap (1 month)]



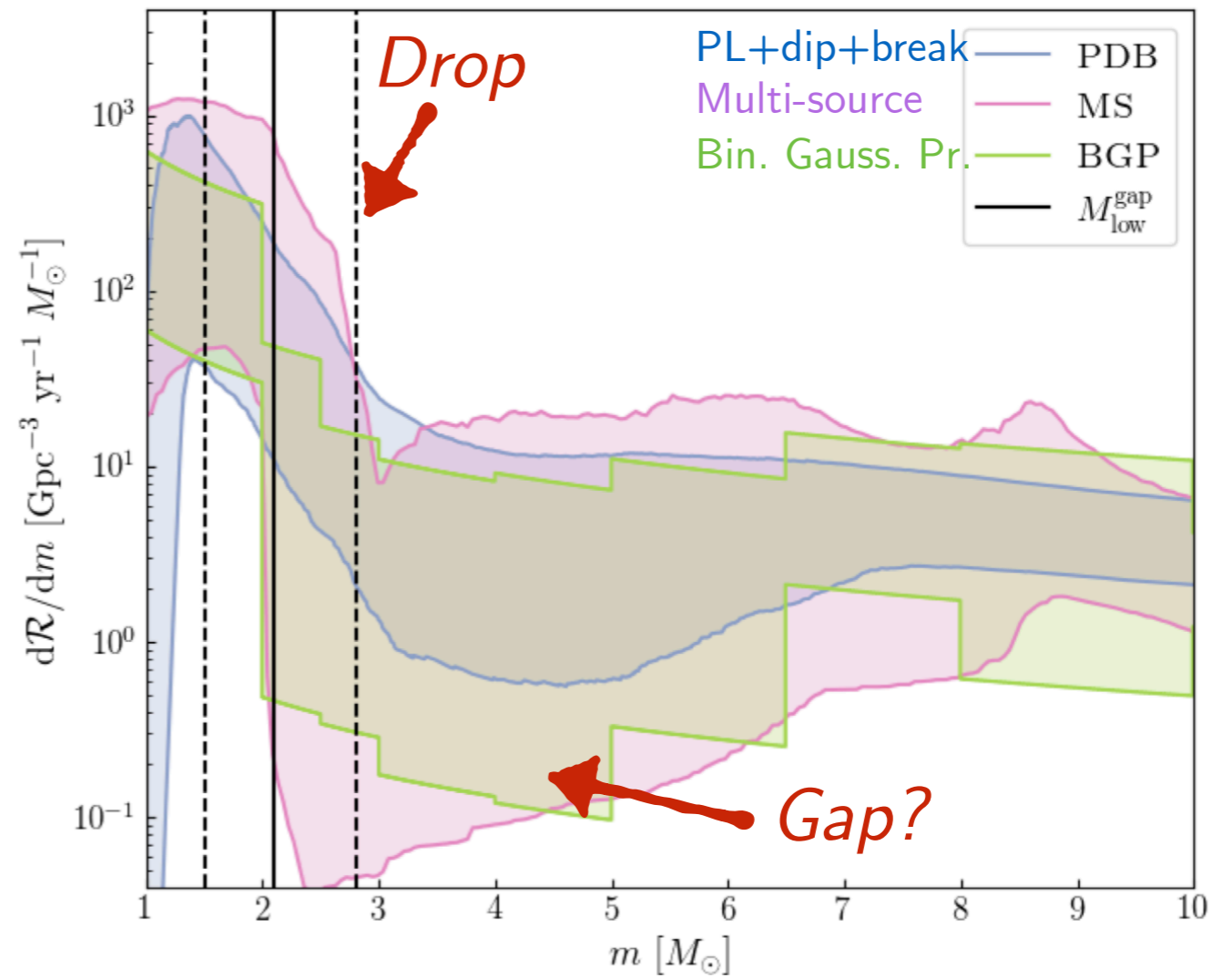
Without evolution in the model:
cosmology can be biased

GWTC-3

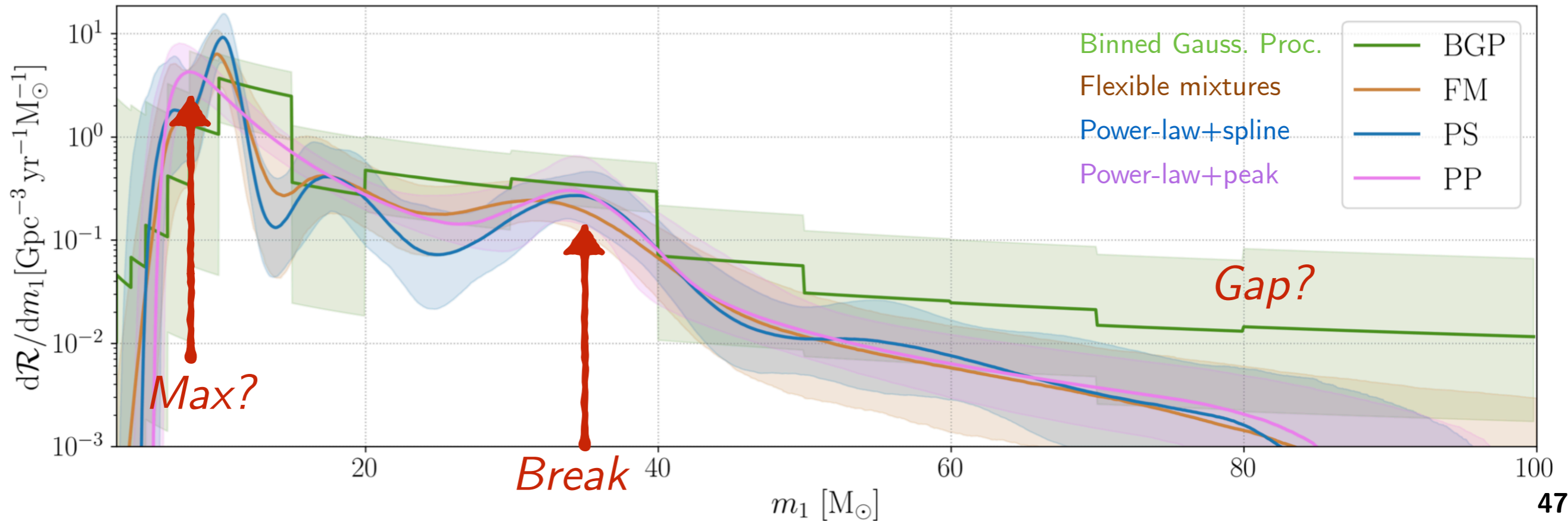
[latest LIGO-Virgo catalog]

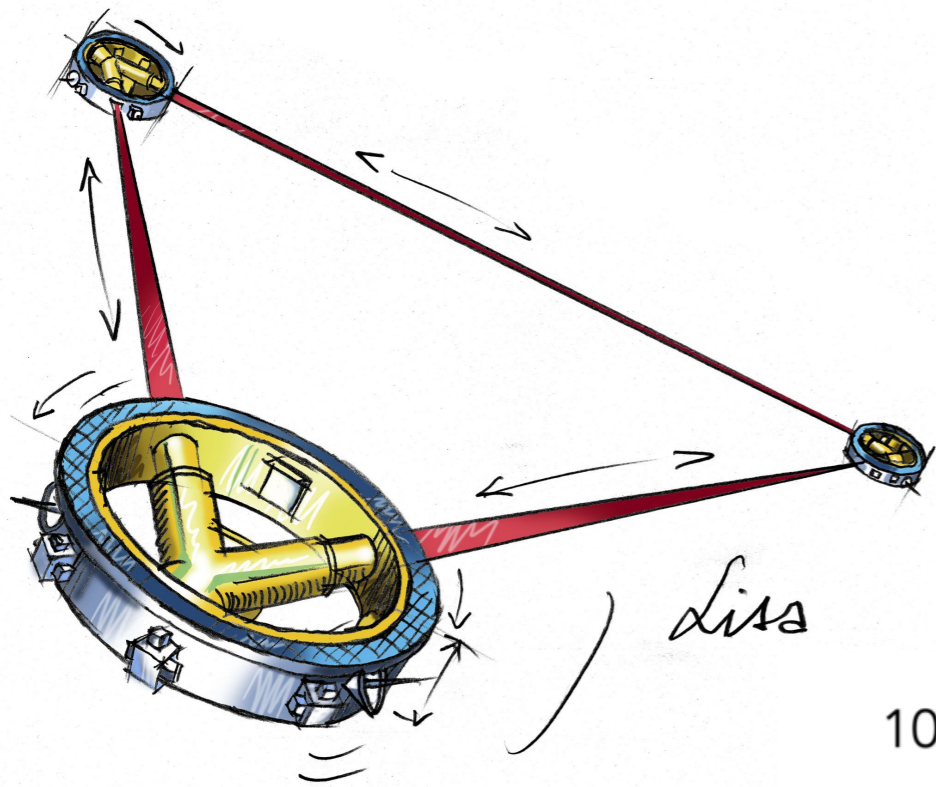
[LVC GWTC-3 '21]

Low-mass mass distribution

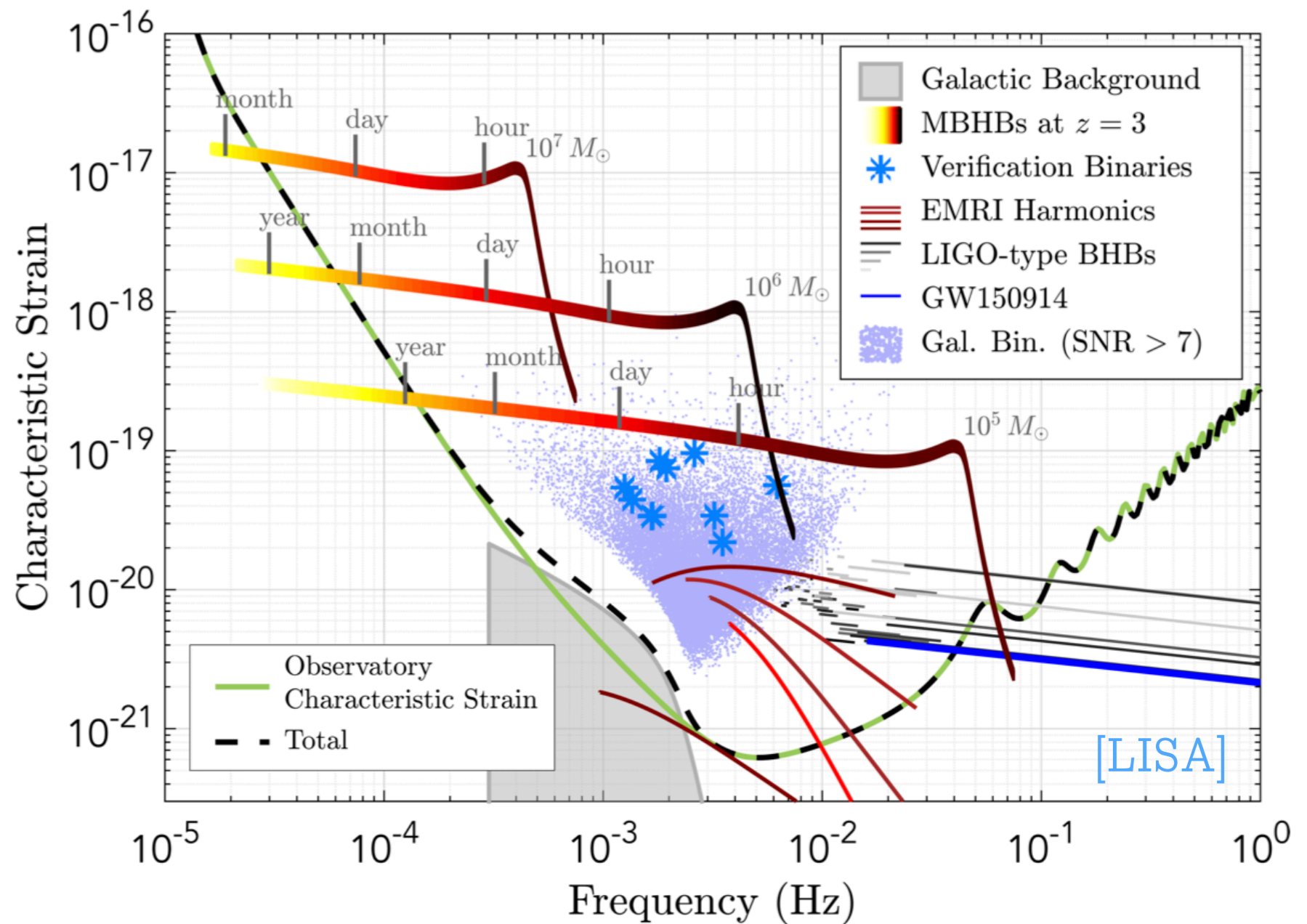


BBH mass distribution



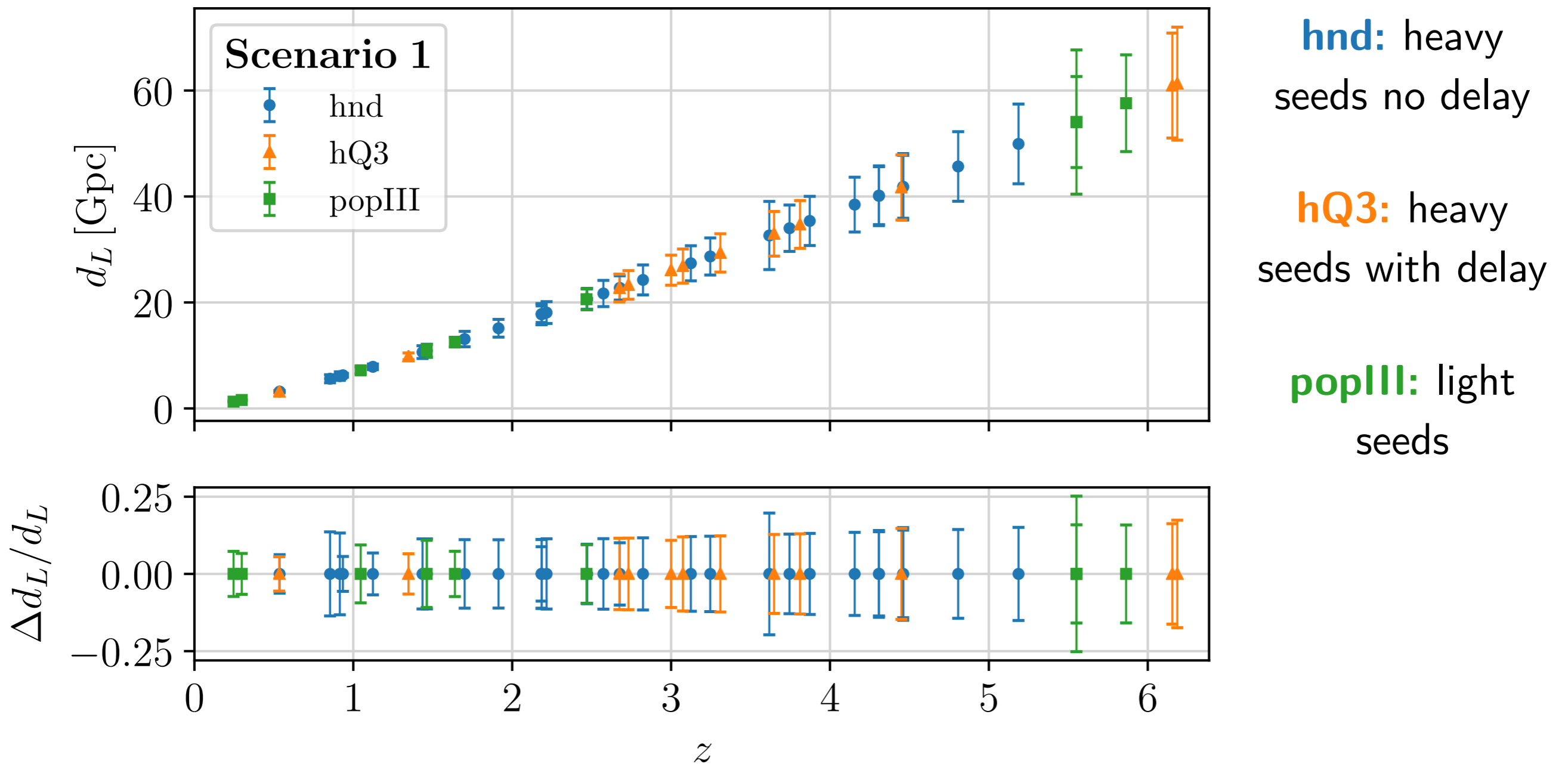


LISA's perspective

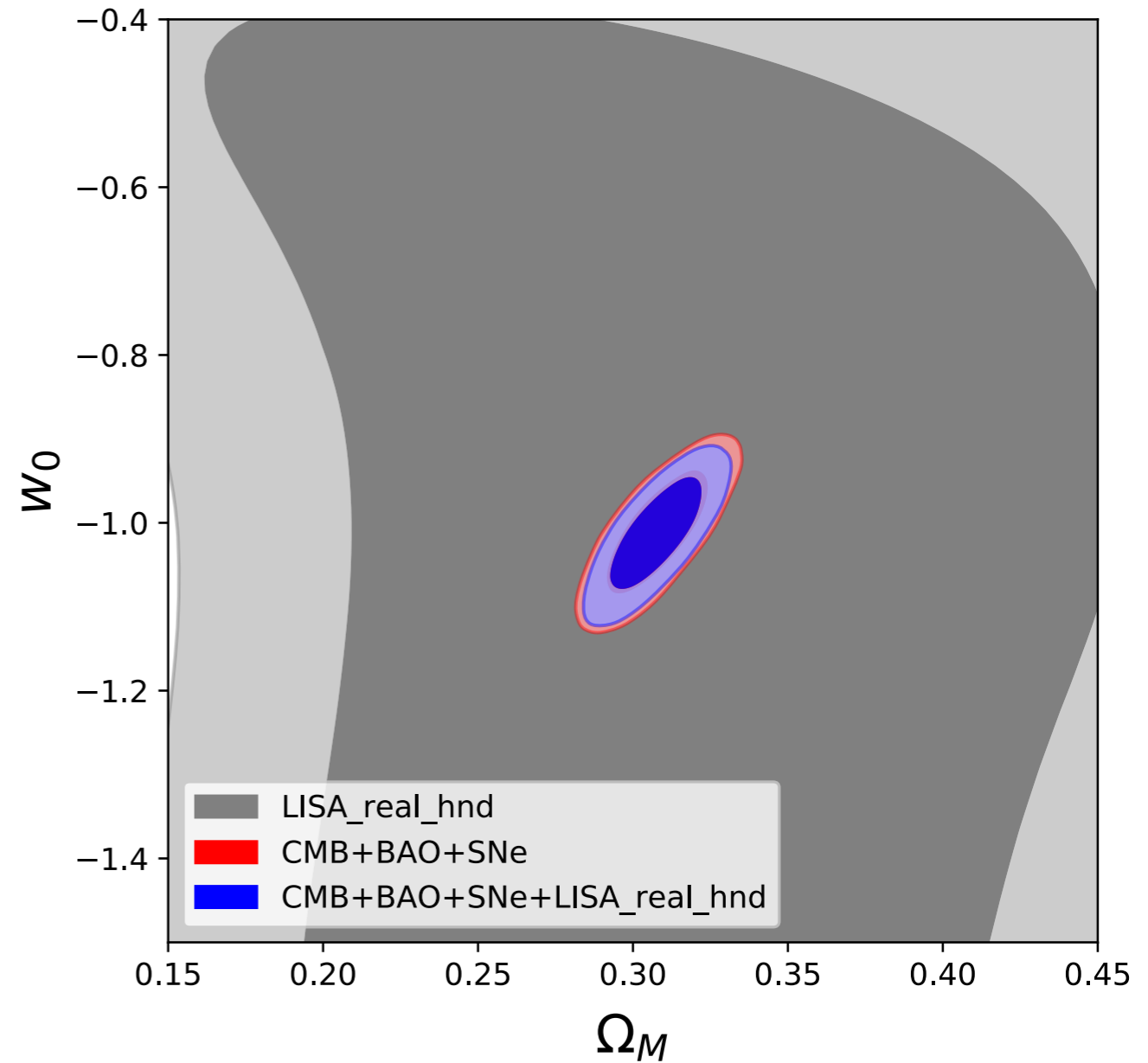
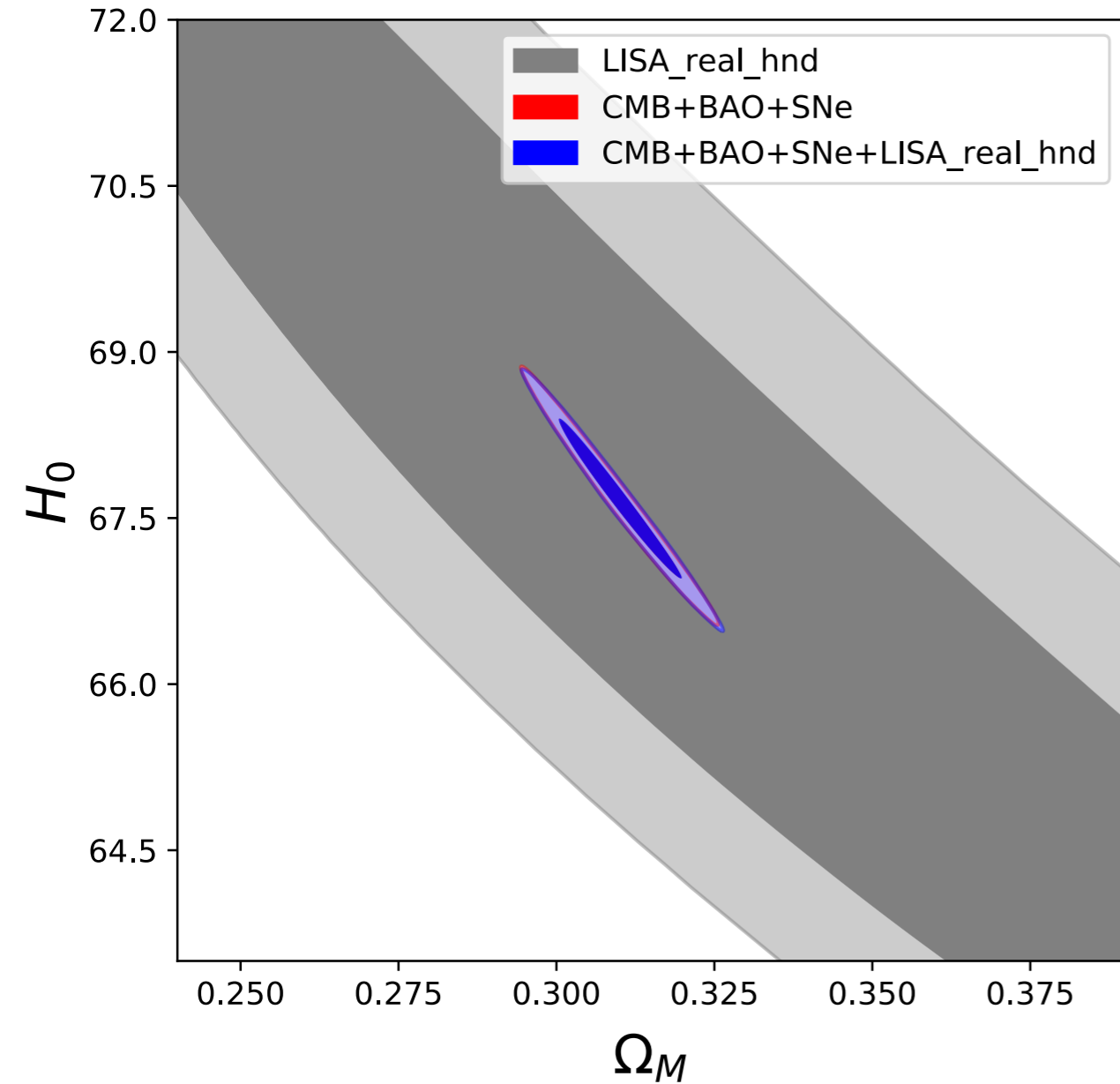


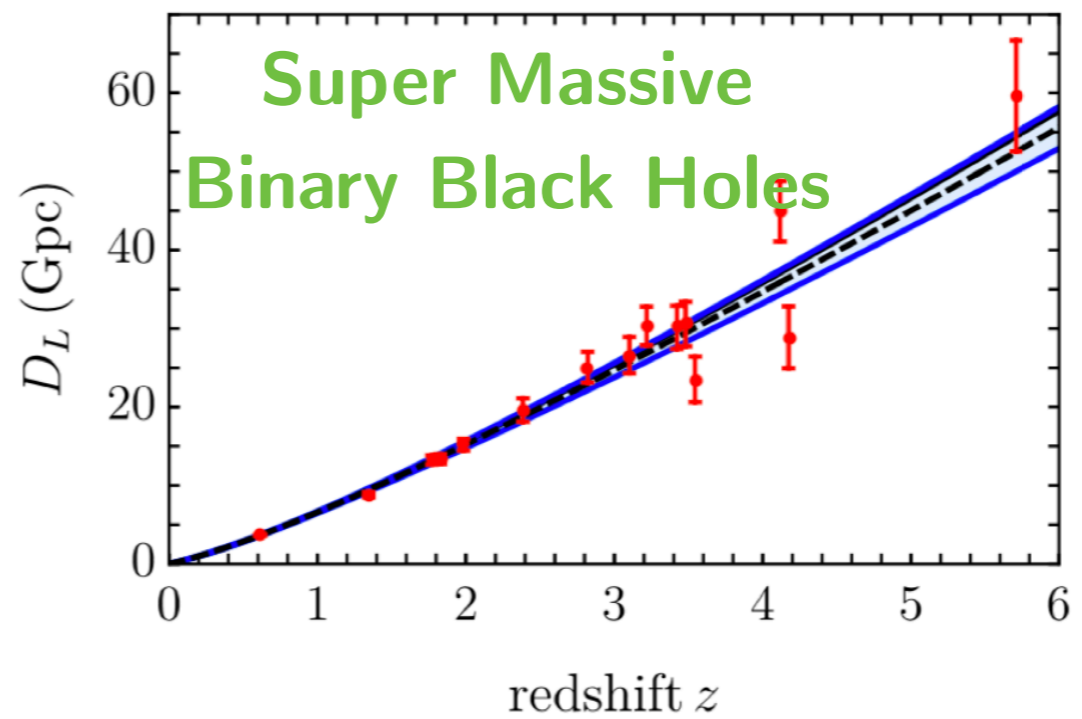
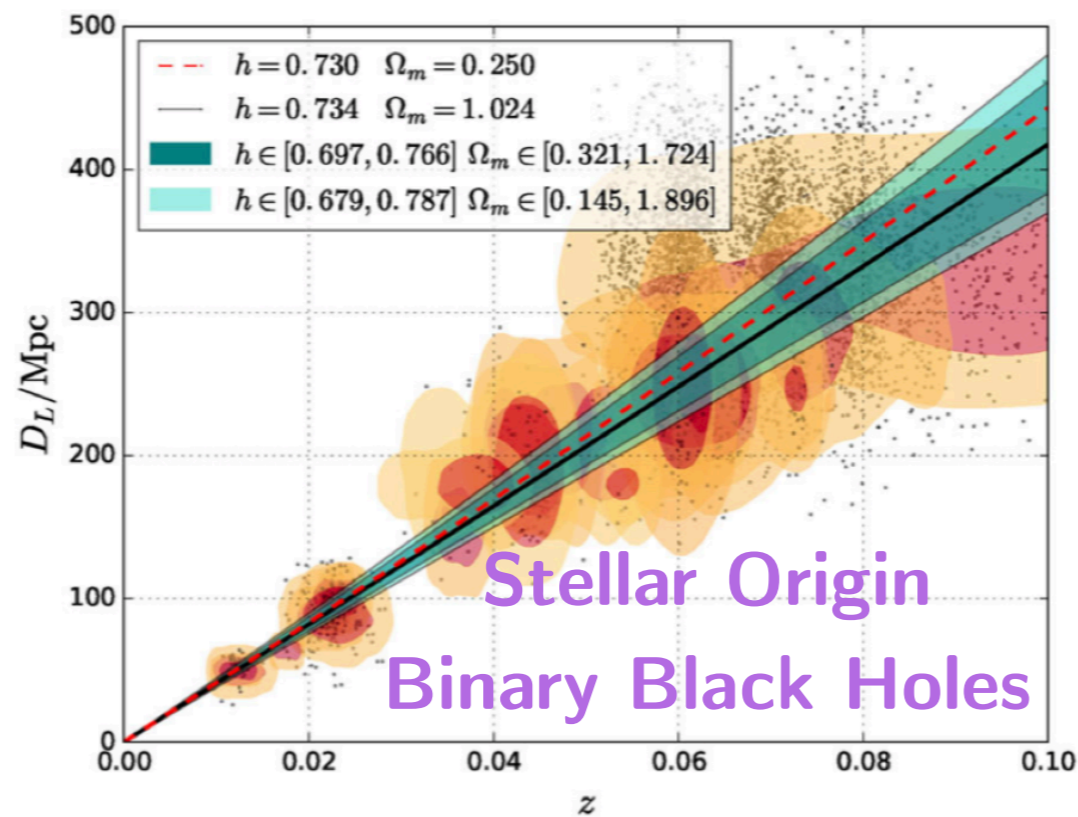
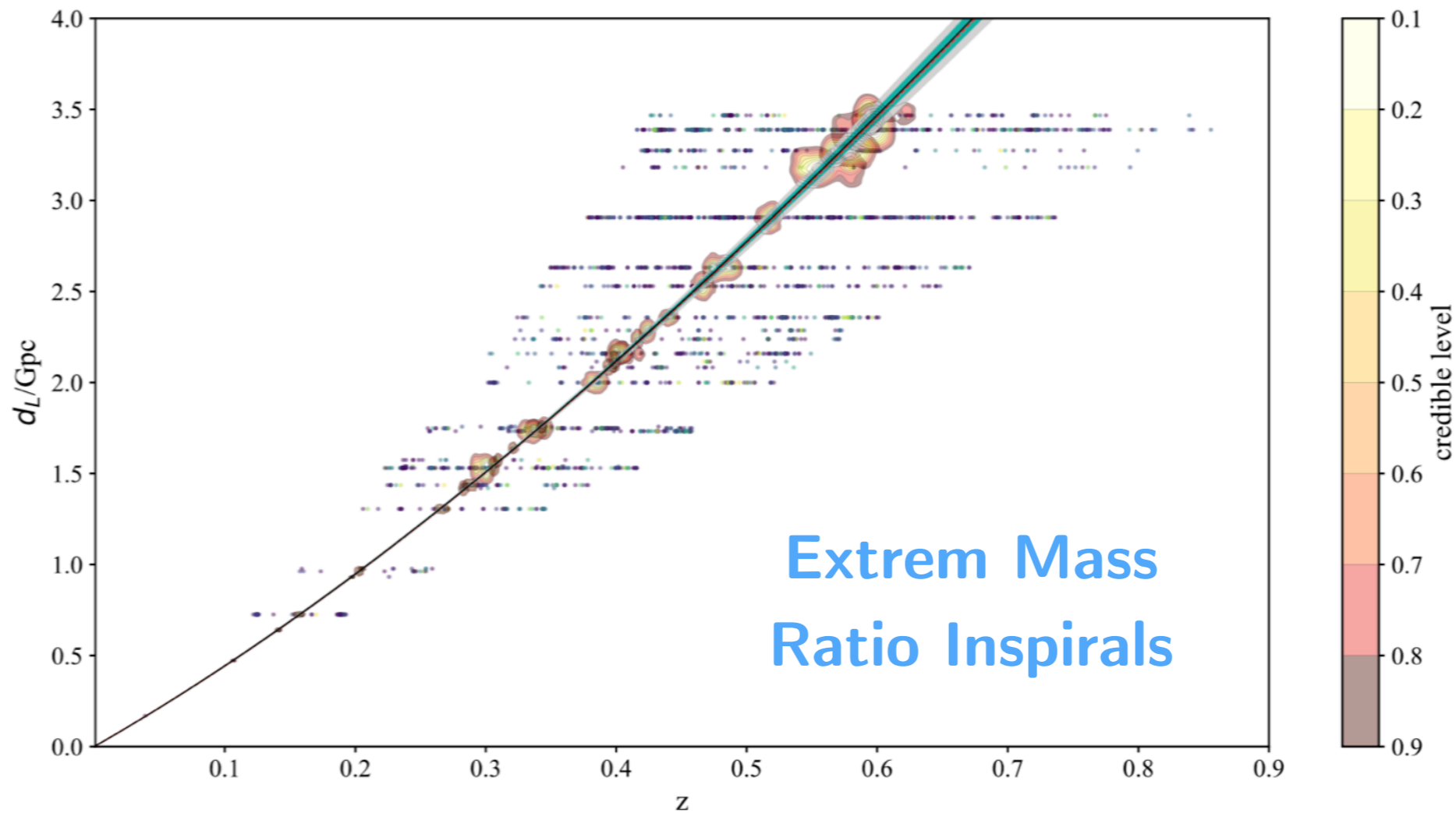
LISA forecasts: SMBBHs

[approx. 10-30 bright sirens (4 yrs)]



LISA forecasts: SMBBHs





Modified dispersion relation (MDR)

General relativity predicts:

$$\omega(k) = c \cdot k$$

Massive graviton:

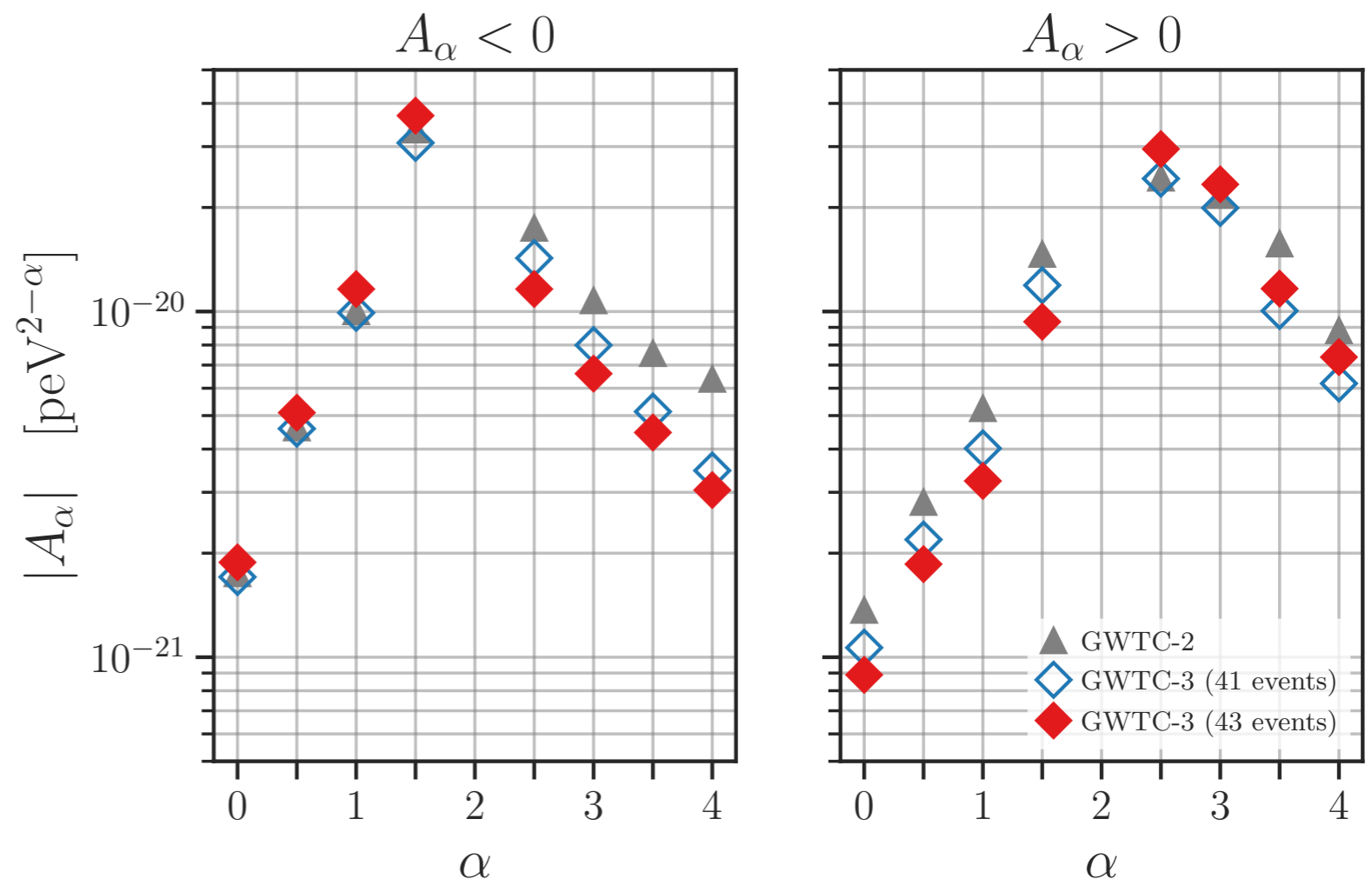
$$\omega^2 = c^2 k^2 + m^2 c^4$$

[Will'98]

General MDR:

$$\omega^2 = c^2 k^2 + \Lambda (ck)^\alpha$$

[Mirshekari et al.'11]



[LVK TGR GWTC-3]

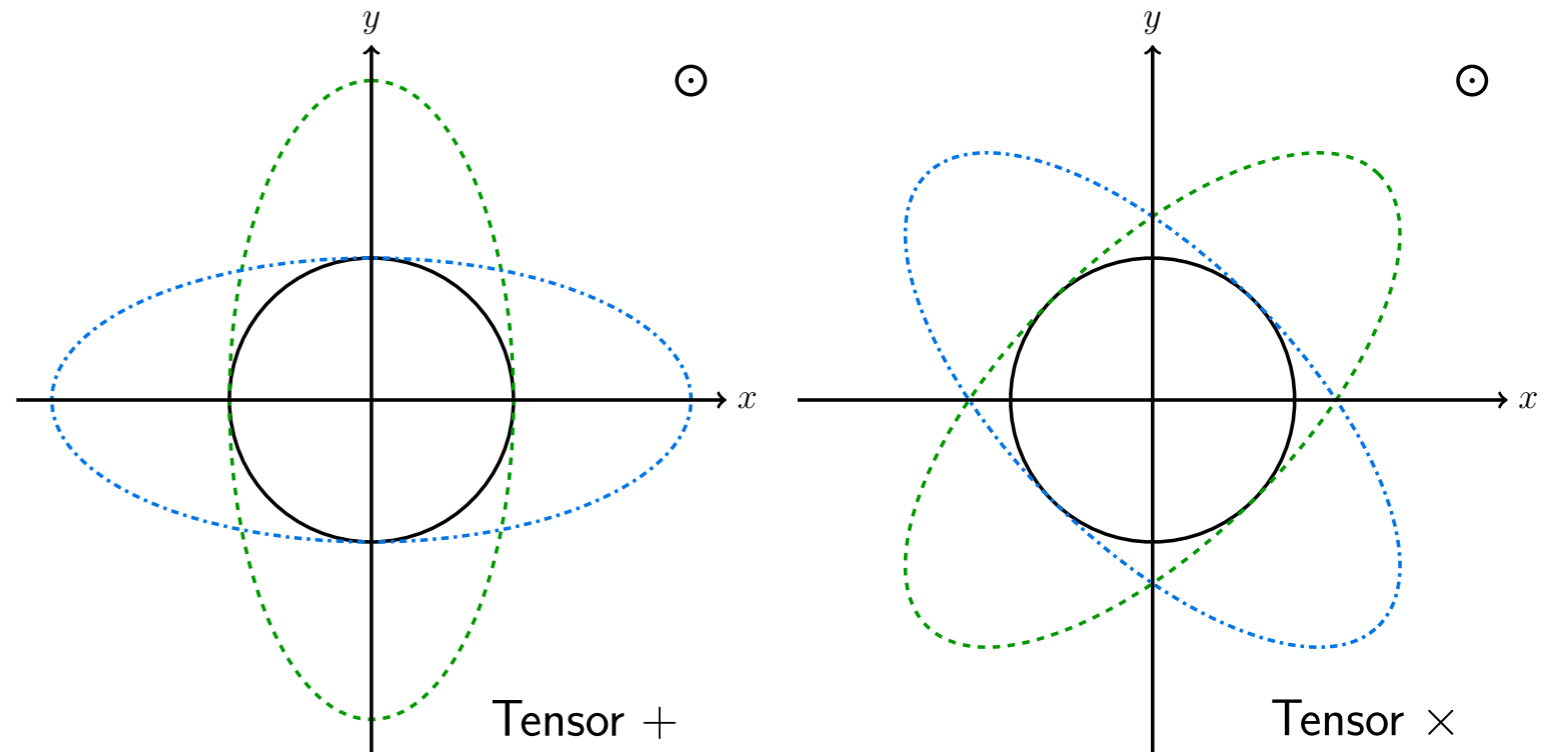
Tensor polarizations

Gravitational Wave Polarizations

General relativity predicts:

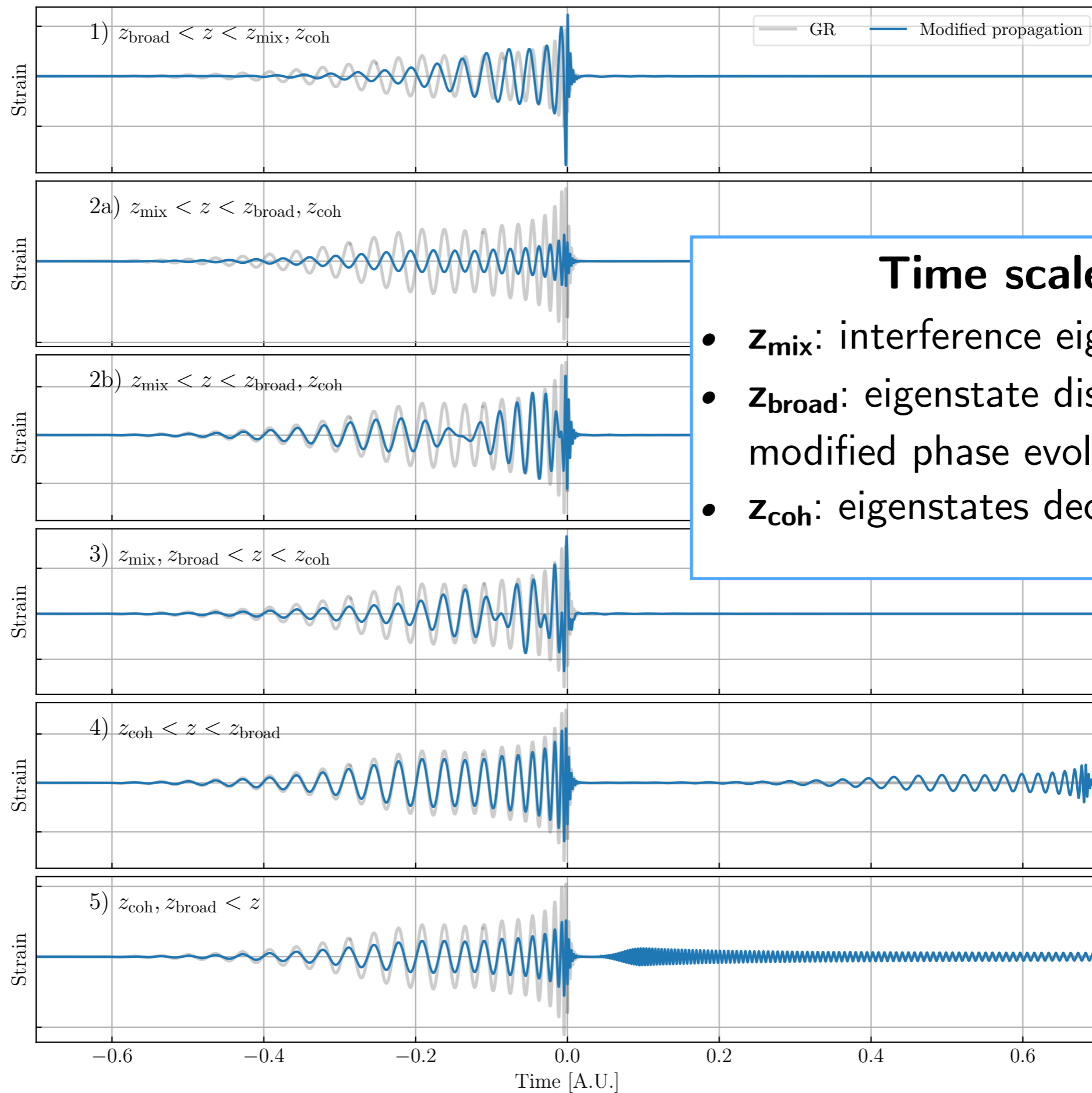
$$h_+, \quad h_\times$$

$$\square h_{+,\times} = 0$$

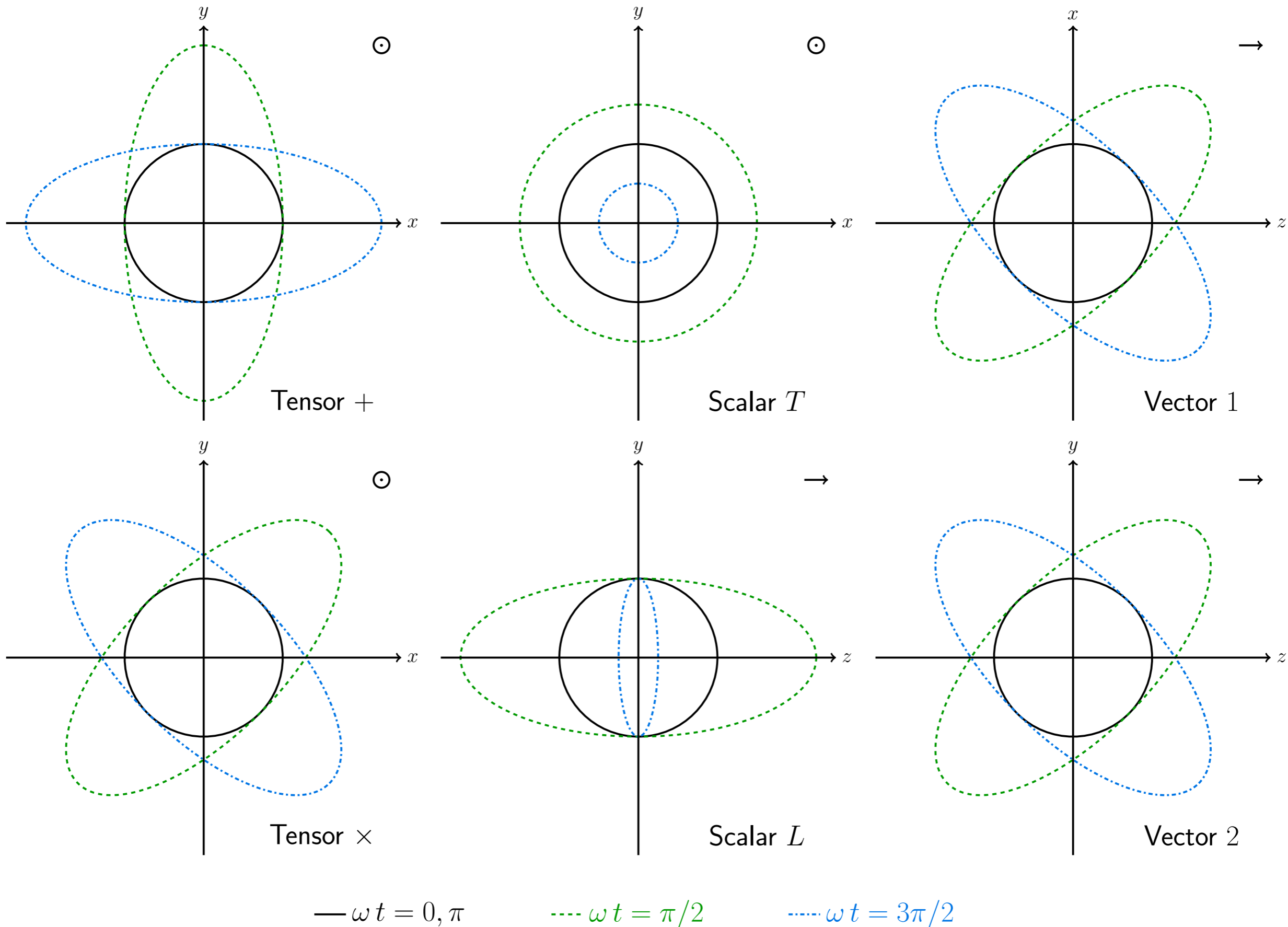


Mixing cosmological tensor fields (similar to neutrino oscillations)

$$\left[\hat{I} \left(\frac{d^2}{d\eta^2} + (ck)^2 \right) + \begin{pmatrix} m_h^2 & m_{hs}^2 \\ m_{hs}^2 & m_s^2 \end{pmatrix} \right] \begin{pmatrix} h_{+,\times} \\ s_{+,\times} \end{pmatrix} = 0$$



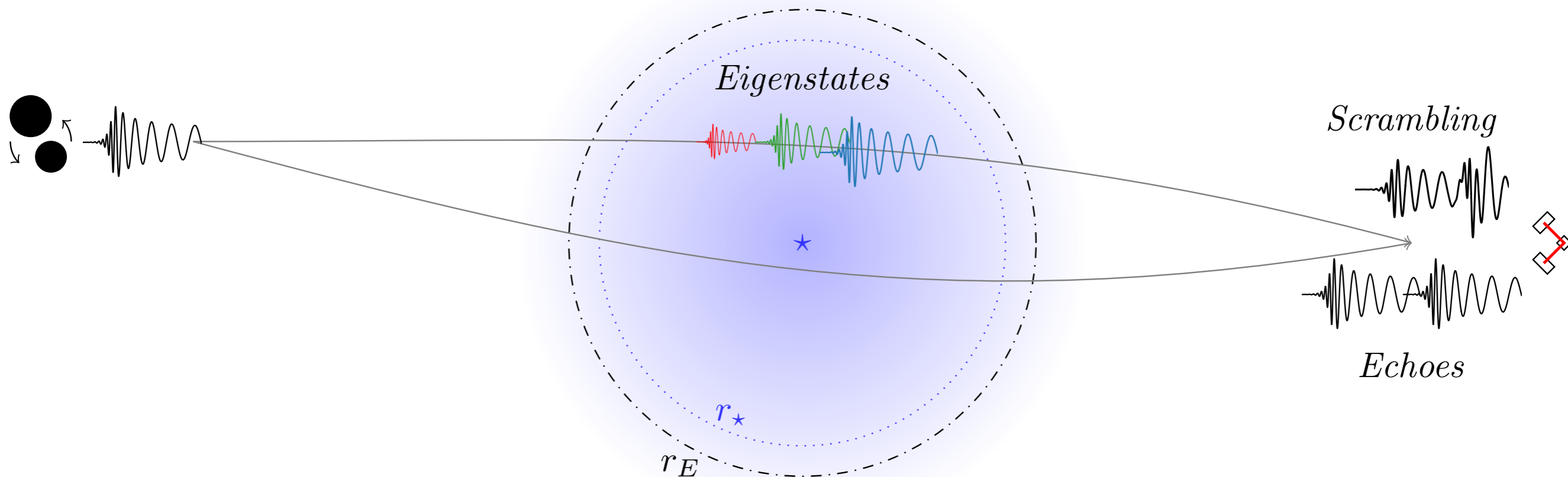
Gravitational Wave Polarizations



GW lensing beyond GR



- Beyond GR the background of the additional fields $\phi(r)$ modify propagation (besides the change in gravitational potential)



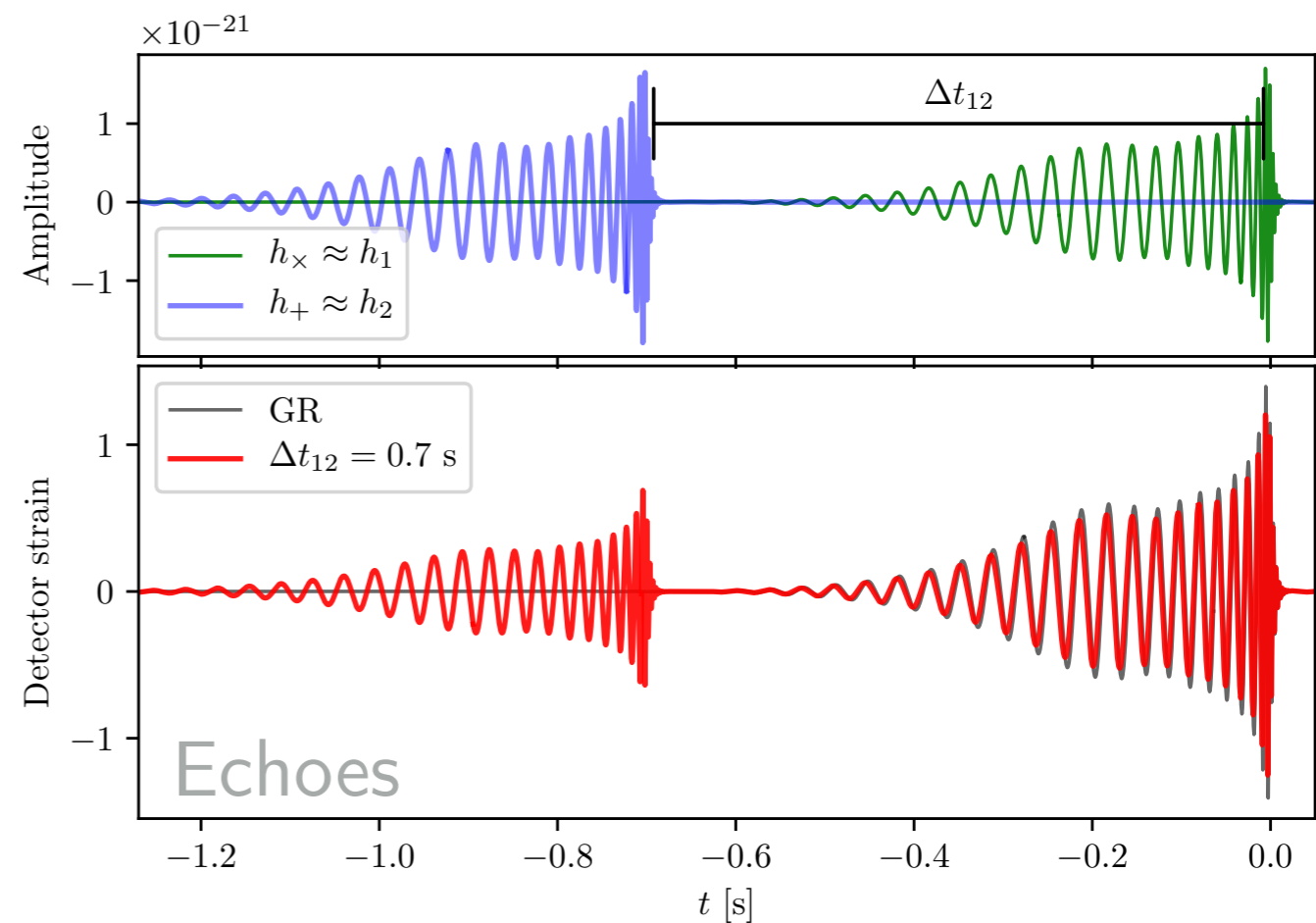
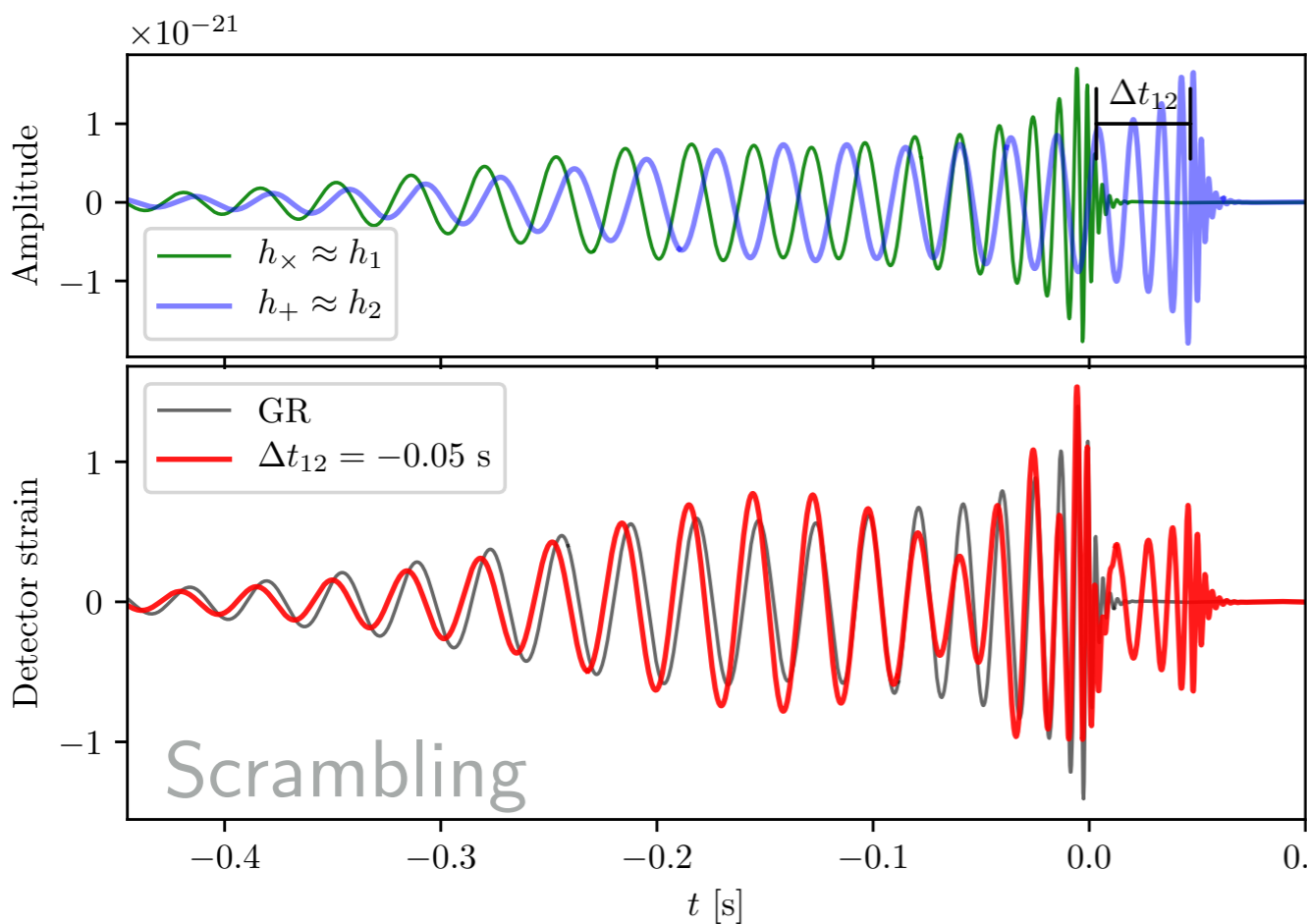
GWs can **mix** with the additional fields. The propagation **eigenstates** may have different speeds, **splitting** or **distorting** each image

GW lensing beyond GR

Modified effective metric for each eigenstate and polarization mixing

Time delays

Birefringence



- No need of EM counterpart! Extend cosmological test GW propagation!