

Diffusive shock acceleration and multi-messenger radiation from wind bubbles

Enrico Peretti

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**Topical Seminar at «Here, There & Everywhere»
PhD Summer School on Neutrinos, NBI, Copenhagen**

VILLUM FONDEN


UNIVERSITY OF
COPENHAGEN



Niels Bohr Institutet



The Niels Bohr
International Academy



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Outline

- Transport equation of Cosmic Rays
- Transport approach to diffusive shock acceleration
 - Wind blown bubbles
- Modeling acceleration and multi-messenger radiation

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Cosmic Rays

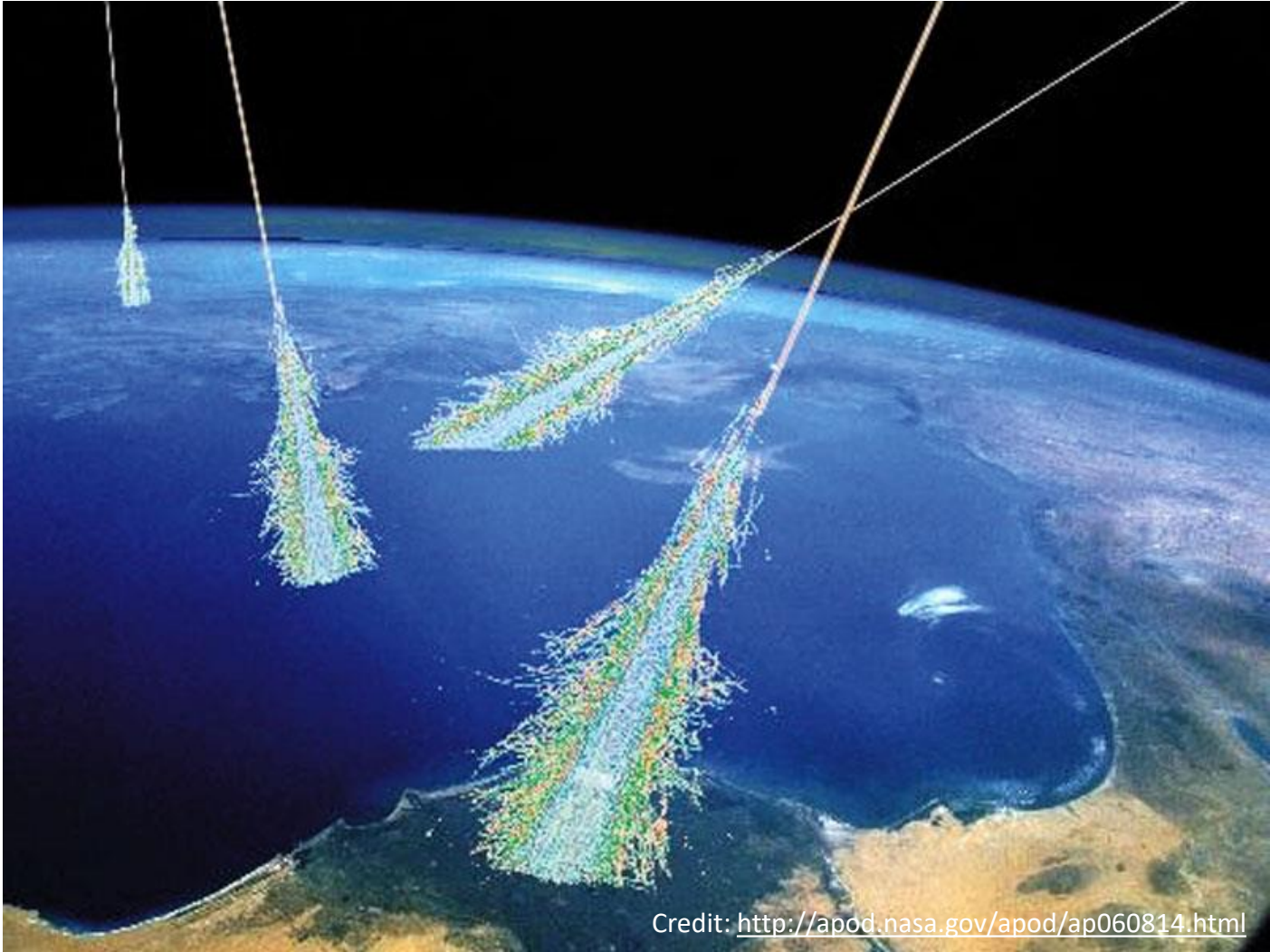
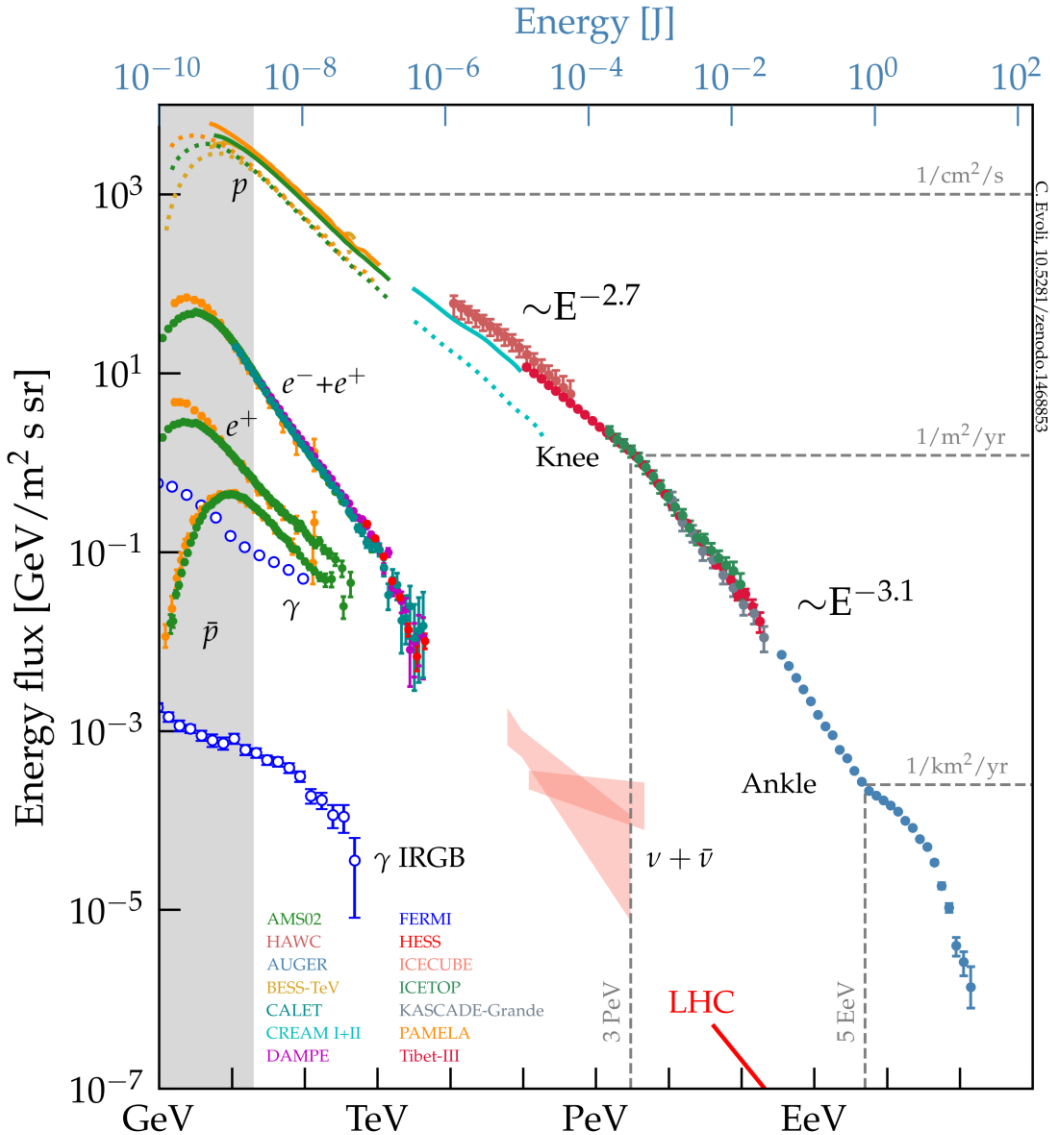
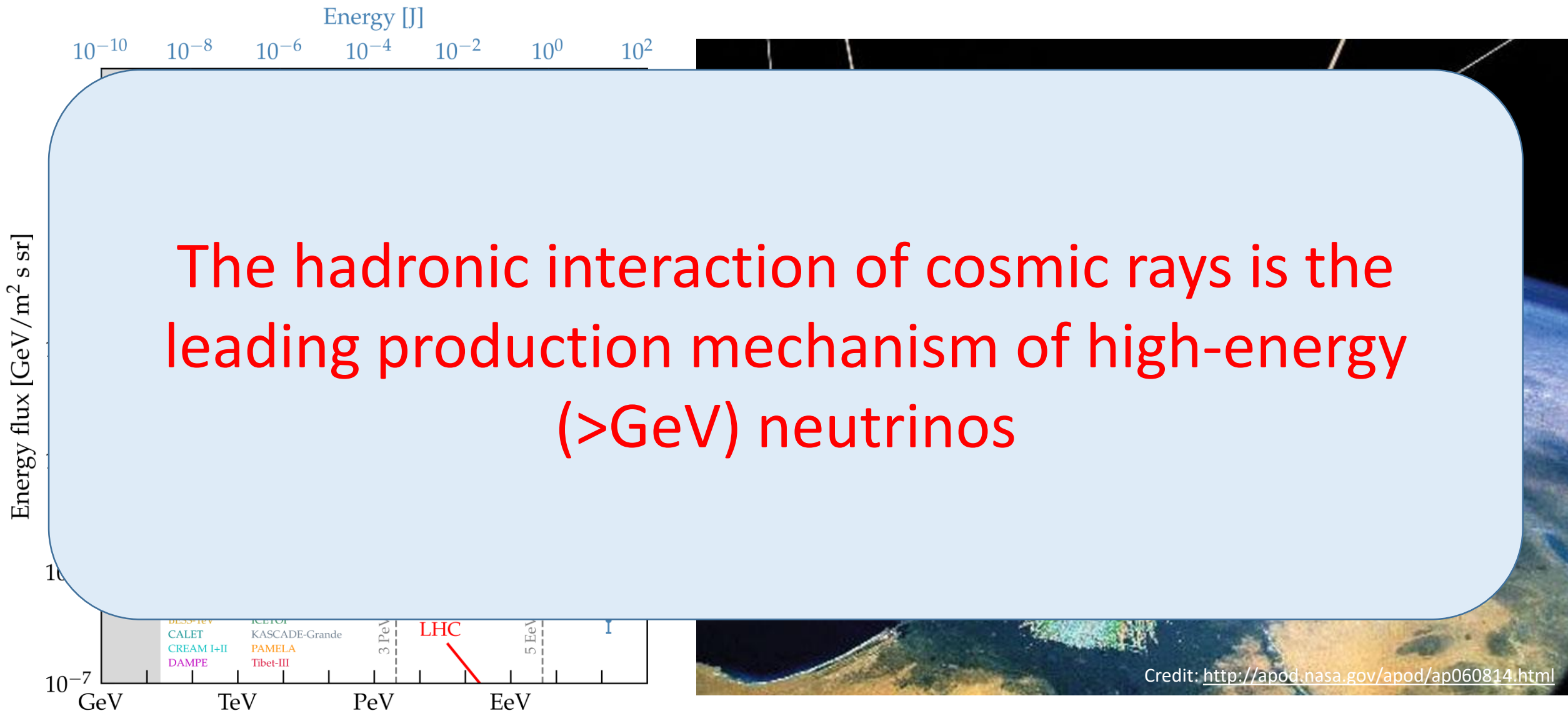


Fig. from Evoli2018

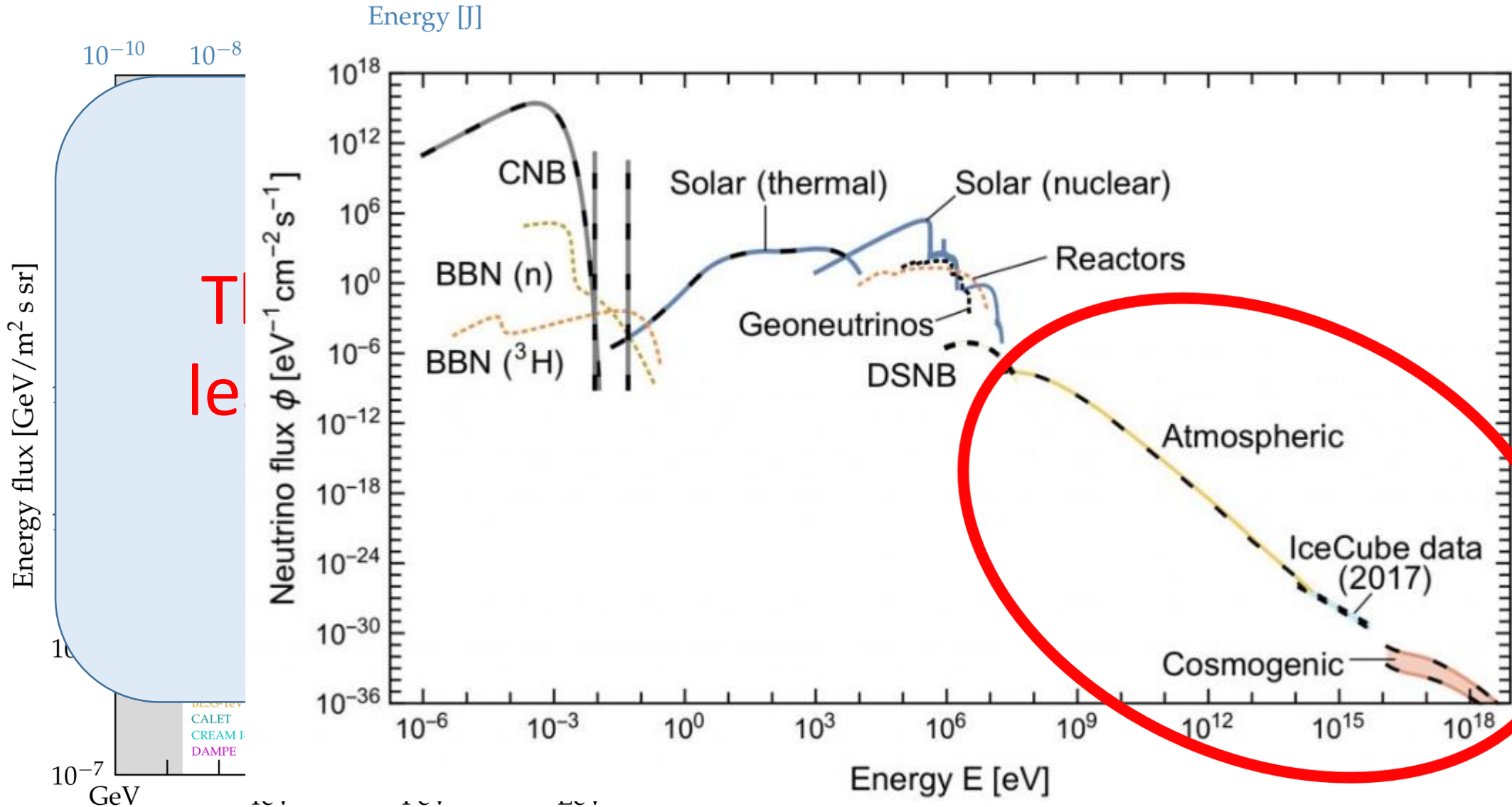
Cosmic Rays



Credit: <http://apod.nasa.gov/apod/ap060814.html>

Fig. from Evoli2018

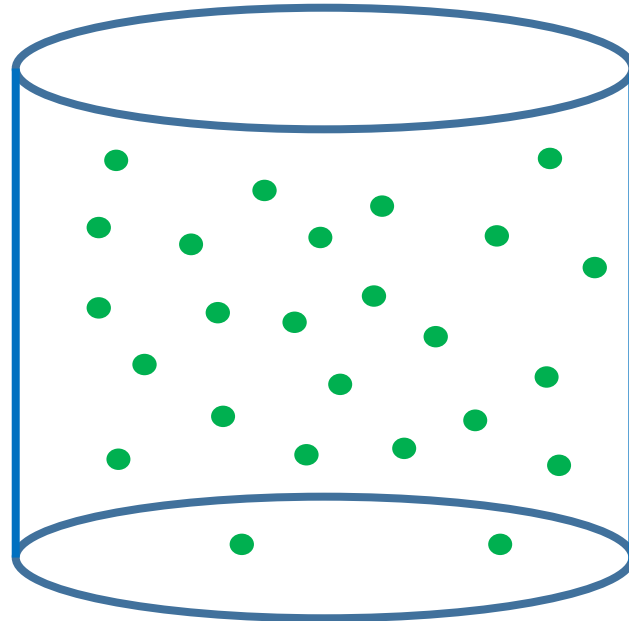
Cosmic Rays



[ov/apod/ap060814.html](http://ov.apod/ap060814.html)

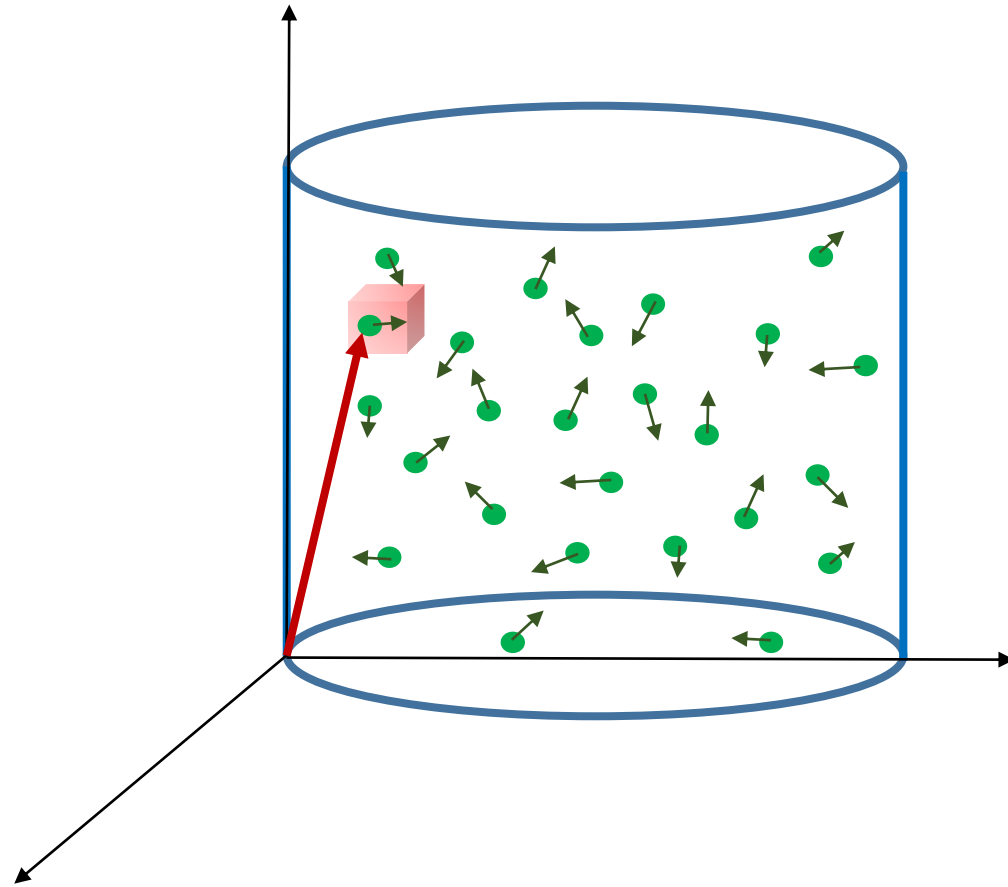
Fig. from Evoli2018

Transport equation of Cosmic Rays



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- Cosmic rays \rightarrow phase space density $\rightarrow f(t, \vec{x}, \vec{p}) = \frac{dN}{dV \cdot d^3p}$



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Time evolution = Injection + diff. + adv. + adb. + loss.

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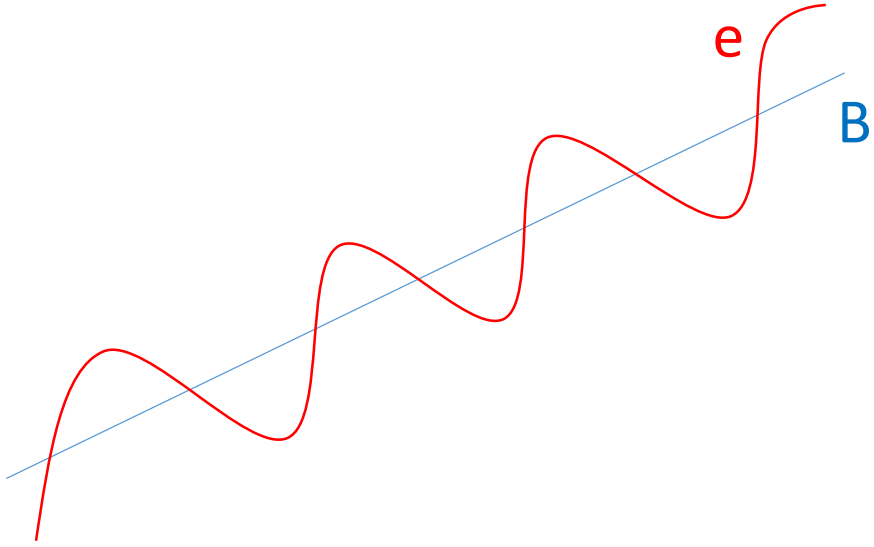
Topic of the upcoming slides

Transport equation of Cosmic Rays

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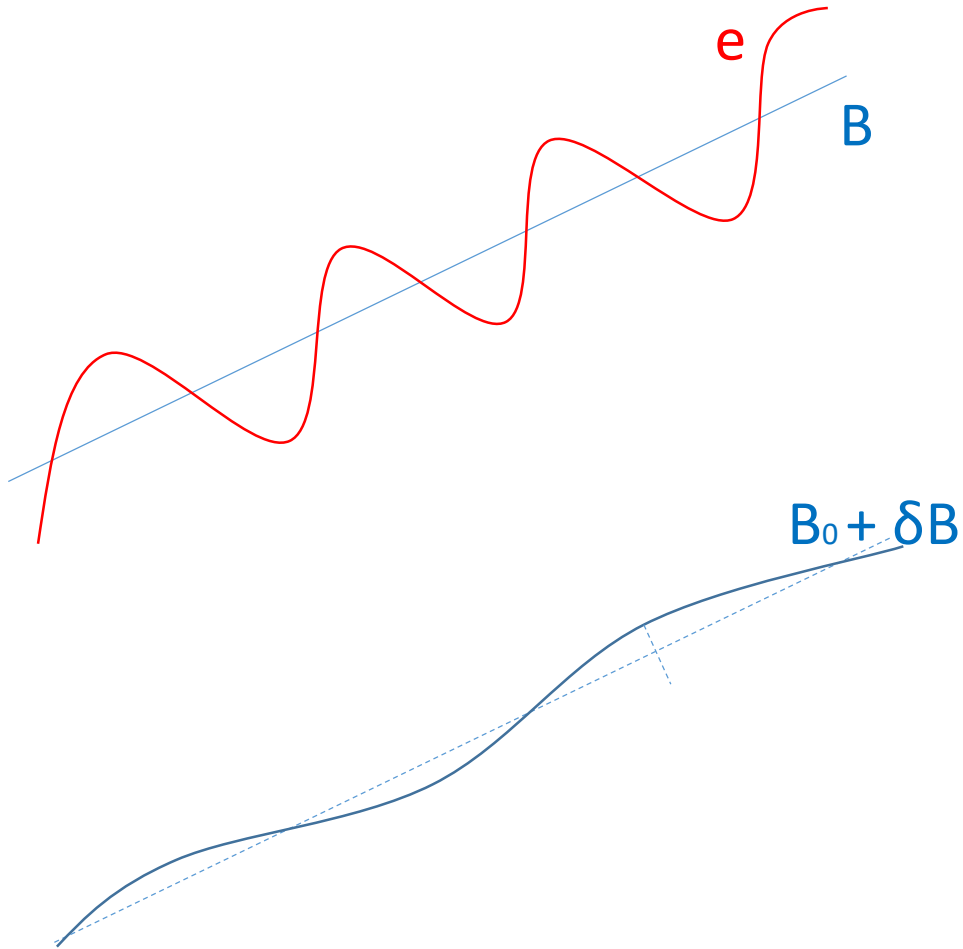
Time evolution = Injection + diff. + adv. + adb. + loss.

Physics of cosmic rays: Diffusion - 1



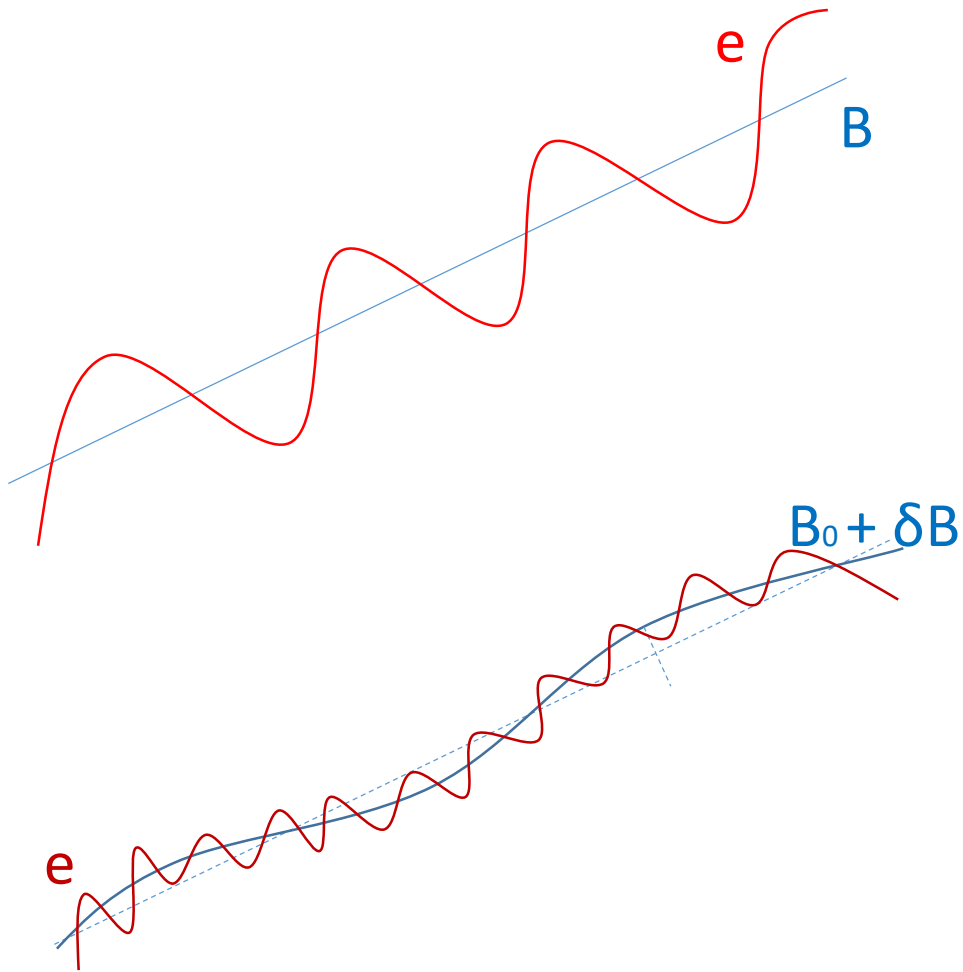
- Charged particles follow helical paths around magnetic field line in ideal conditions

Physics of cosmic rays: Diffusion - 1



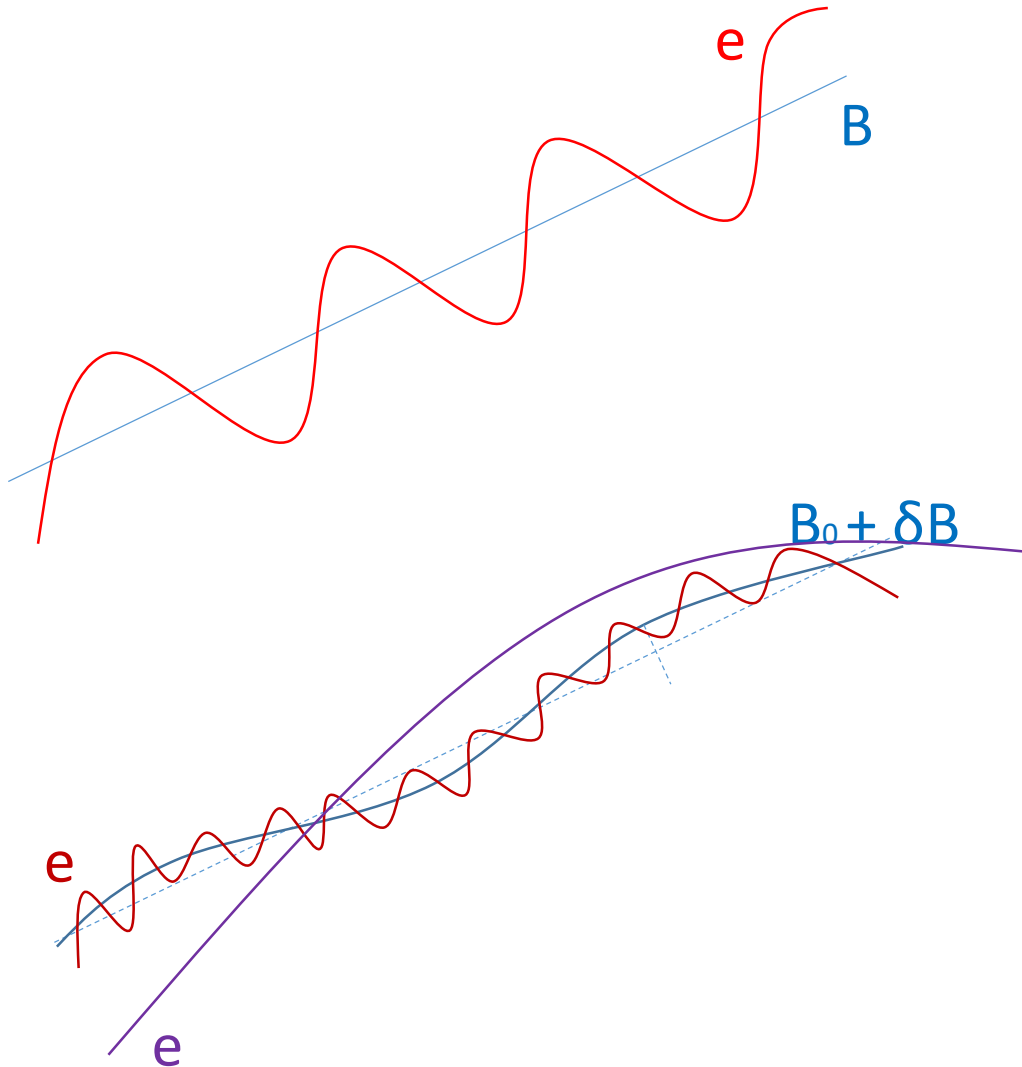
- The ISM is a turbulent plasma
- The magnetic field is also turbulent (δB)

Physics of cosmic rays: Diffusion - 1



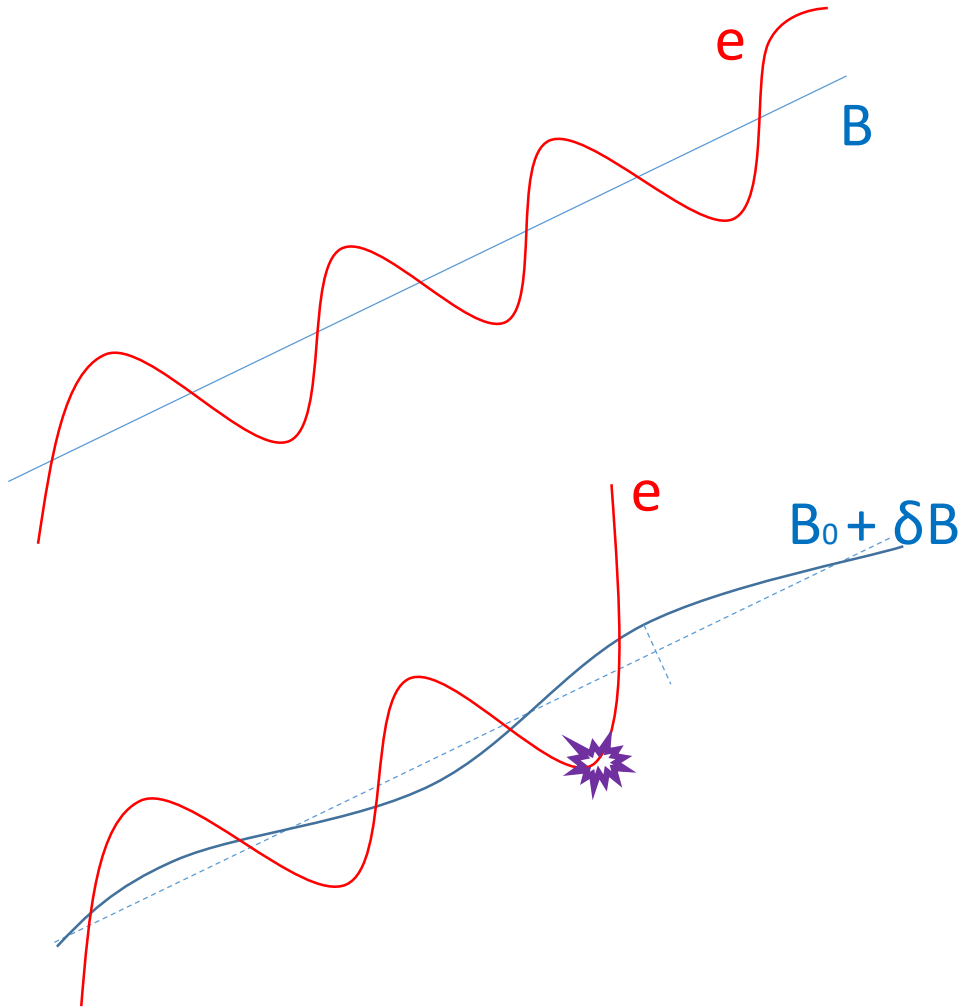
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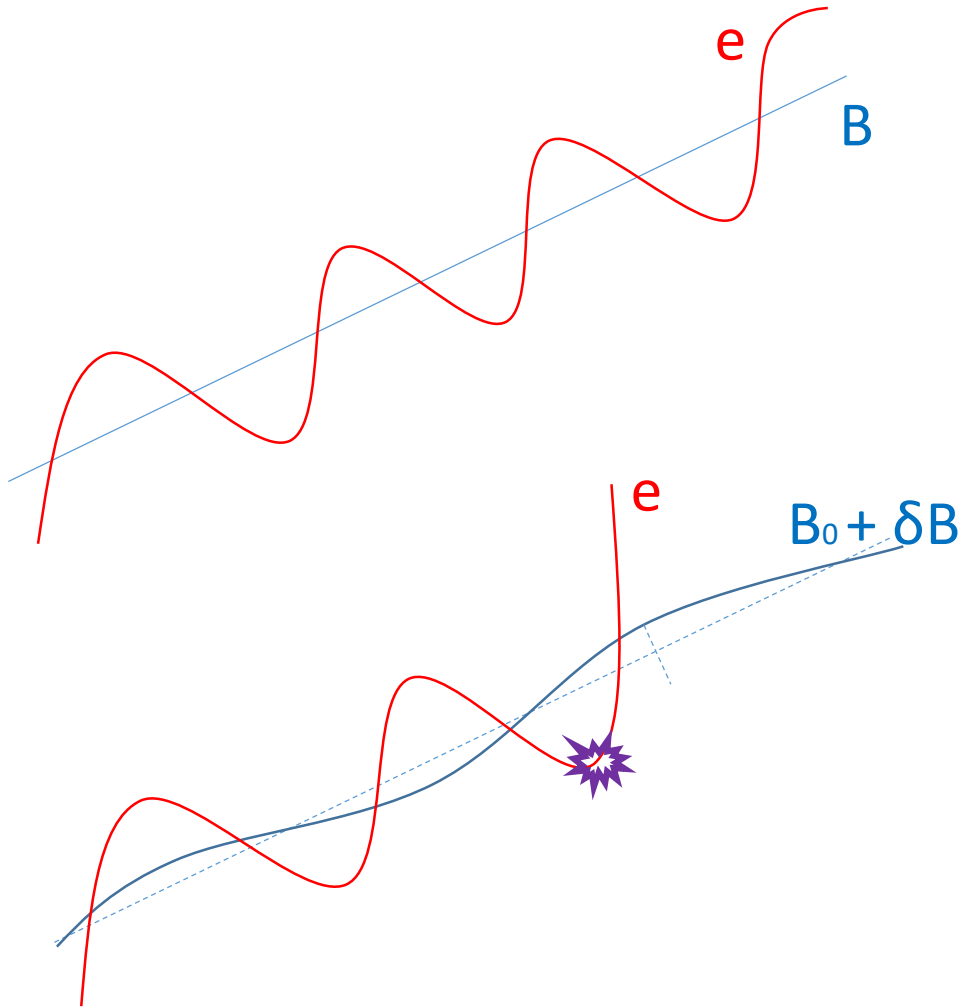
Physics of cosmic rays: Diffusion - 1



- The ISM is a turbulent plasma
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- Particles pitch angle evolves in time when in presence of magnetic field disturbances

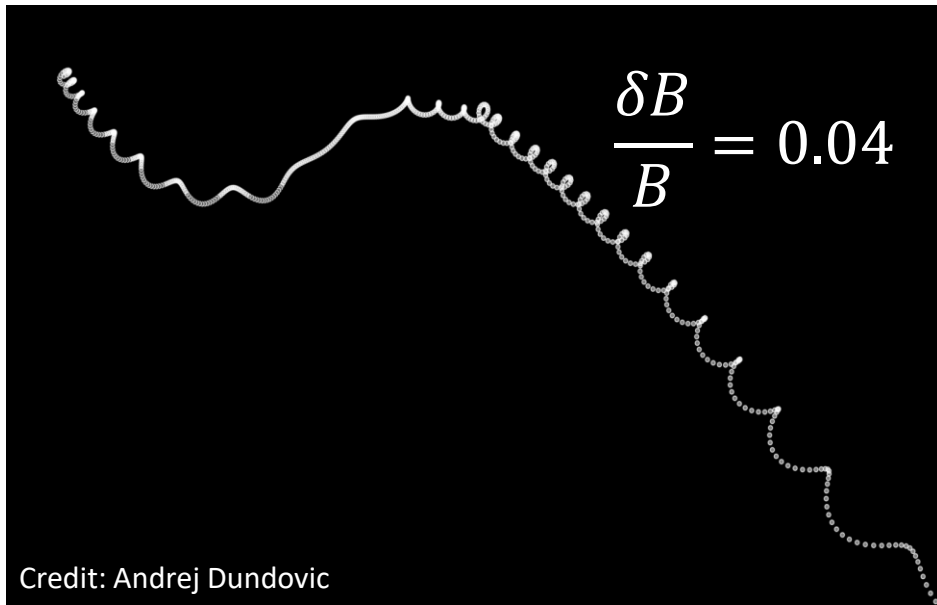
Helical motion \rightarrow Spatial diffusion

Physics of cosmic rays: Diffusion - 1



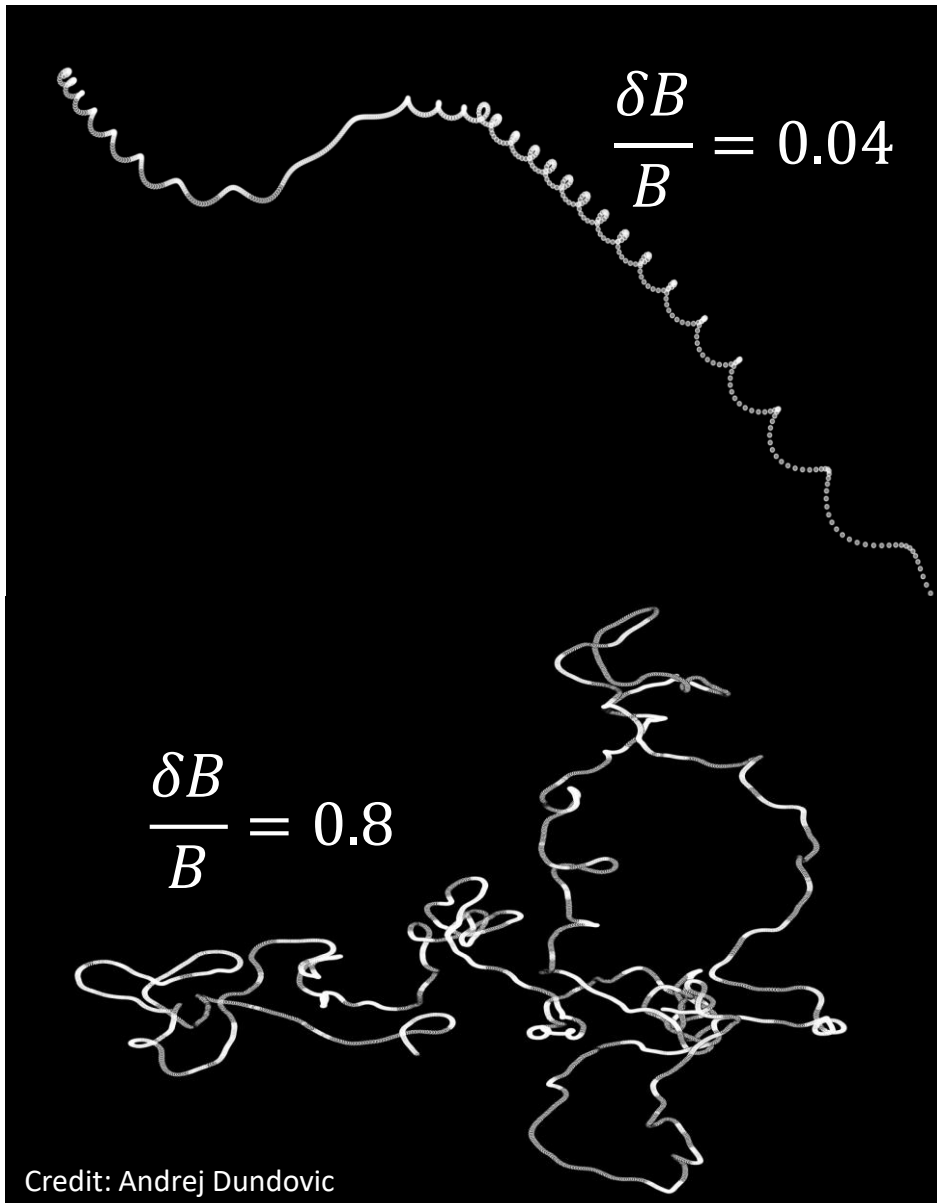
- The ISM is a turbulent plasma
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- Particles pitch angle evolves in time when in presence of magnetic field disturbances
Helical motion → Spatial diffusion
- Diffusion tensor/coefficient: $D(\vec{x}, \vec{p})$

Physics of cosmic rays: Diffusion - 2



- Low turbulence environment allows to observe standard helical motions

Physics of cosmic rays: Diffusion - 2



- Low turbulence environment allows to observe standard helical motions
- When the turbulence is strong the motion of particles from helicoidal becomes diffusive

$$\tau_{diff} \approx \frac{H^2}{D(E)}$$

Jokipii1966, Blandford+1987, Blasi2013, Snodin+2016, Subedi+2017, Dundovic+2020, Kuhlen+2022

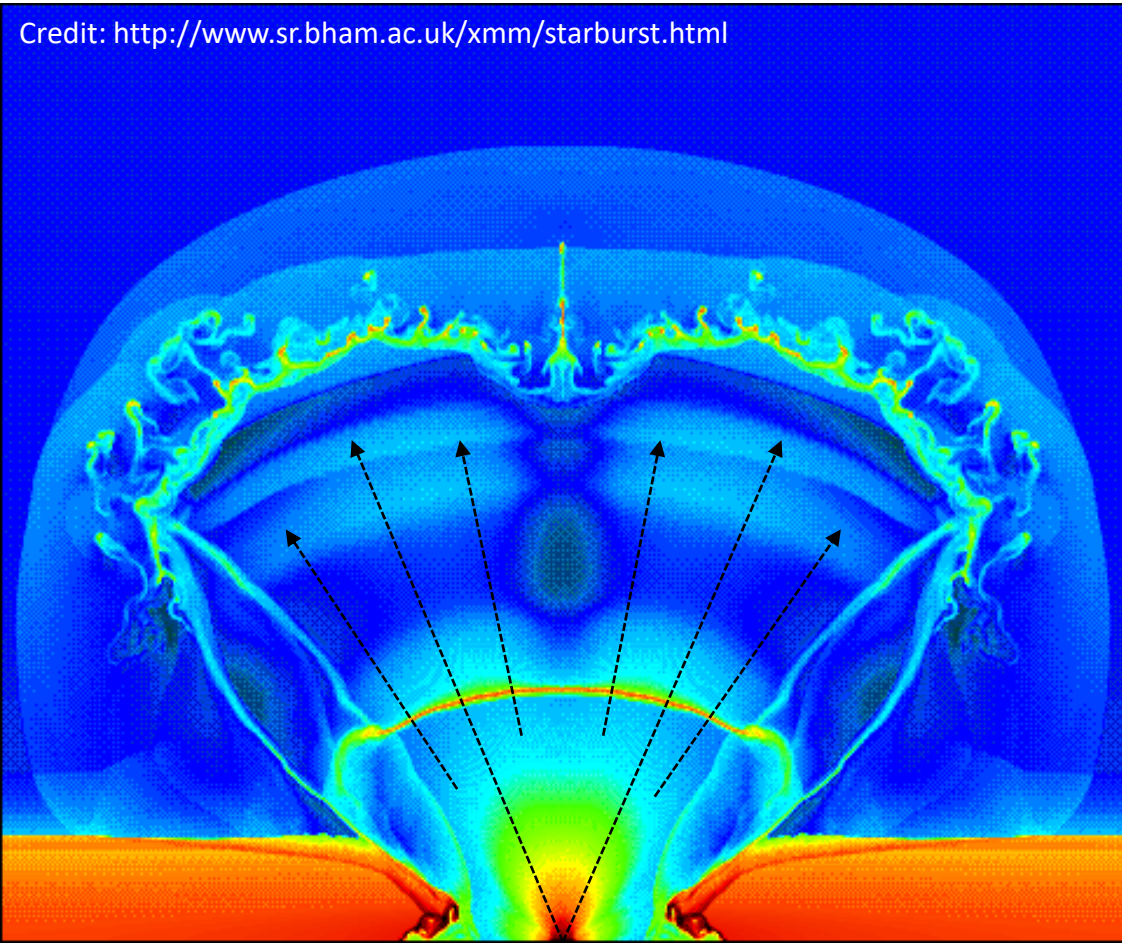
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Physics of cosmic rays: Advection and Adbiabatic losses

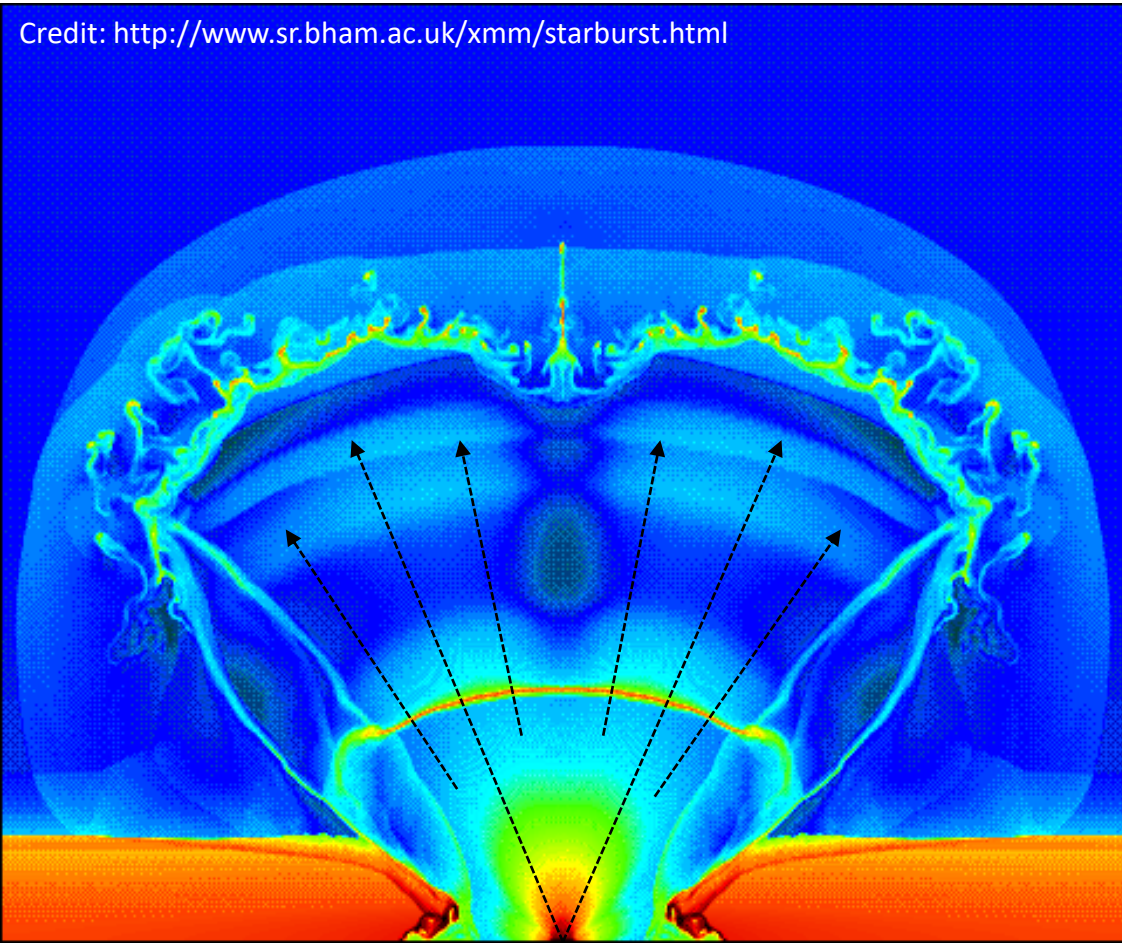
Credit: <http://www.sr.bham.ac.uk/xmm/starburst.html>



- The interstellar medium (ISM) can be characterized by large scale bulk motions

Physics of cosmic rays: Advection and Adbiabatic losses

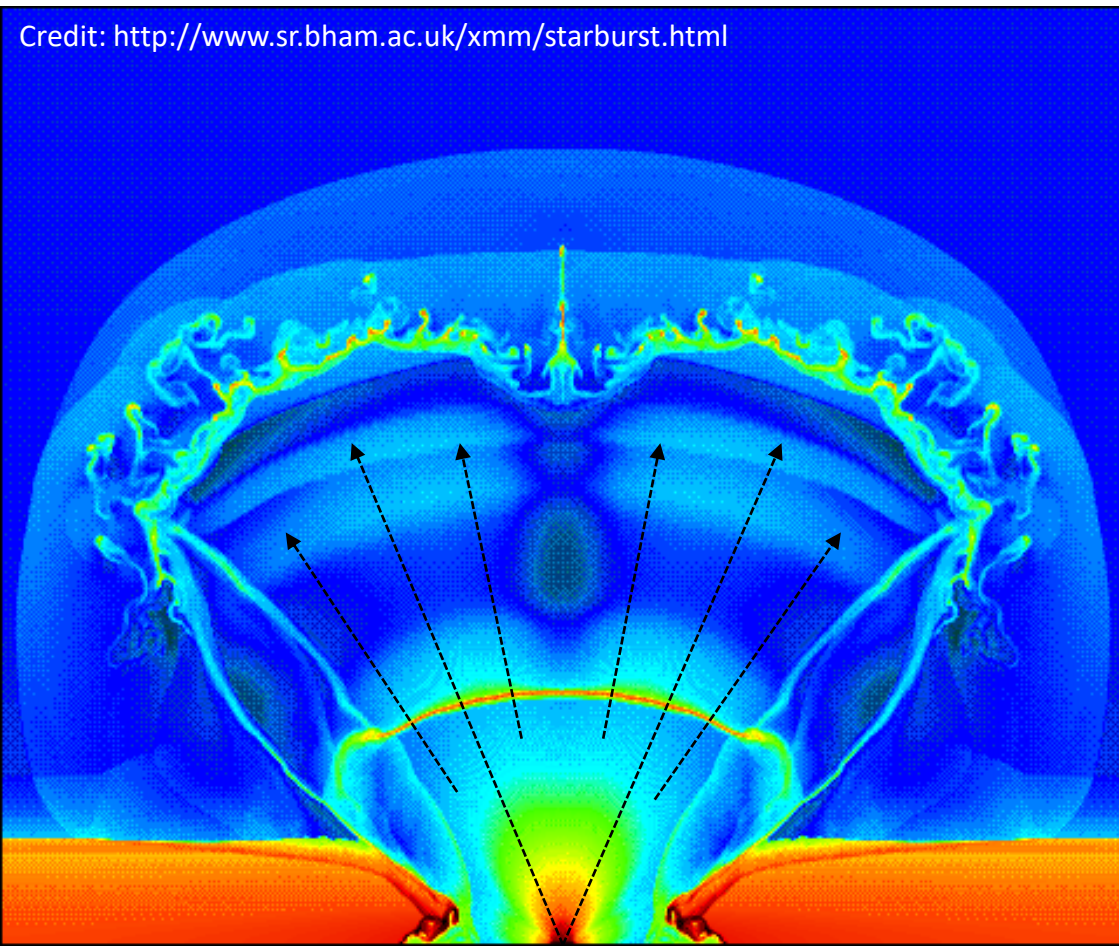
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- The interstellar medium (ISM) can be characterized by large scale bulk motions
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$$\tau_{adv} \approx \frac{H}{v}$$

Physics of cosmic rays: Advection and Adbiabatic losses



- The interstellar medium (ISM) can be characterized by large scale bulk motions
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$$\tau_{adv} \approx \frac{H}{v}$$

- CRs can lose or gain energy adiabatically

Transport equation of Cosmic Rays

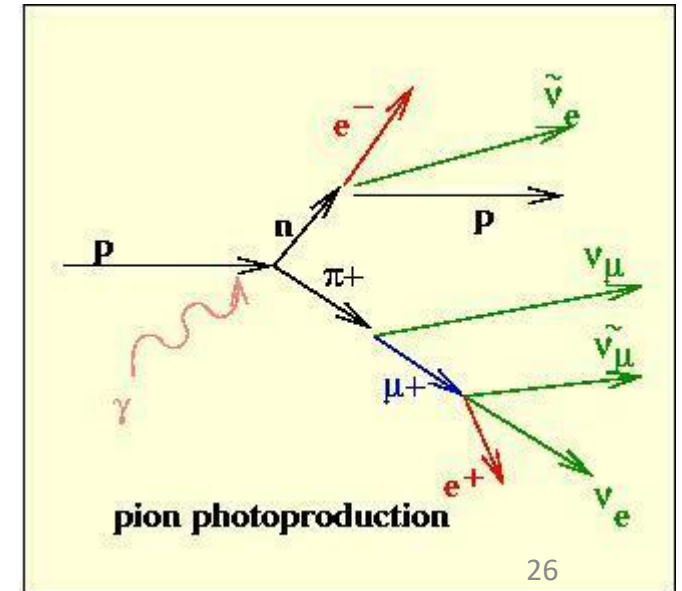
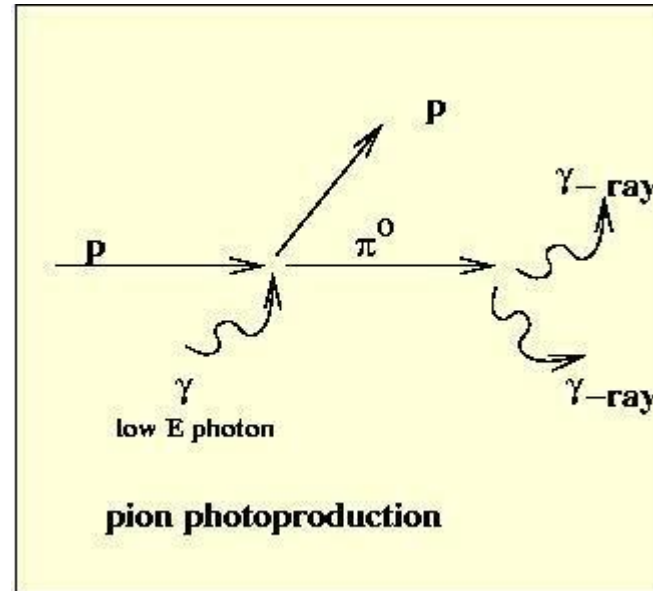
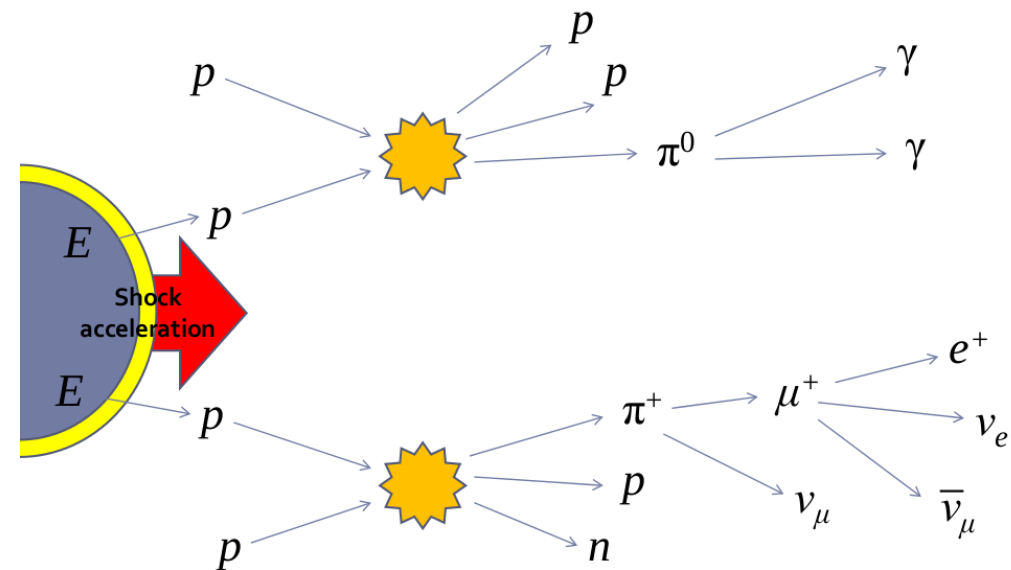
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$$\frac{\partial f}{\partial t} = Q + \nabla \cdot [D \nabla f] - \vec{u} \cdot \nabla f + \frac{\nabla \cdot \vec{u}}{3} p \frac{\partial f}{\partial p} - L$$

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- When the transport is stationary, homogeneous and isotropic:

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$$\cancel{\frac{\partial f}{\partial t}} = \underbrace{Q}_{\text{green}} + \underbrace{\nabla \cdot [D \nabla f]}_{\text{yellow}} - \underbrace{\vec{u} \cdot \nabla f}_{\text{purple}} + \cancel{\frac{\nabla \cdot \vec{u}}{3} p \frac{\partial f}{\partial p}} - \underbrace{L}_{\text{red}}$$

- When the transport is stationary, homogeneous and isotropic:

$$Q = \frac{f}{\tau_{diff}} + \frac{f}{\tau_{adv}} + \frac{f}{\tau_{loss}}$$

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Diffusive Shock Acceleration

- Shocks are the result of explosions or motion of supersonic flows → very common in astrophysical environments



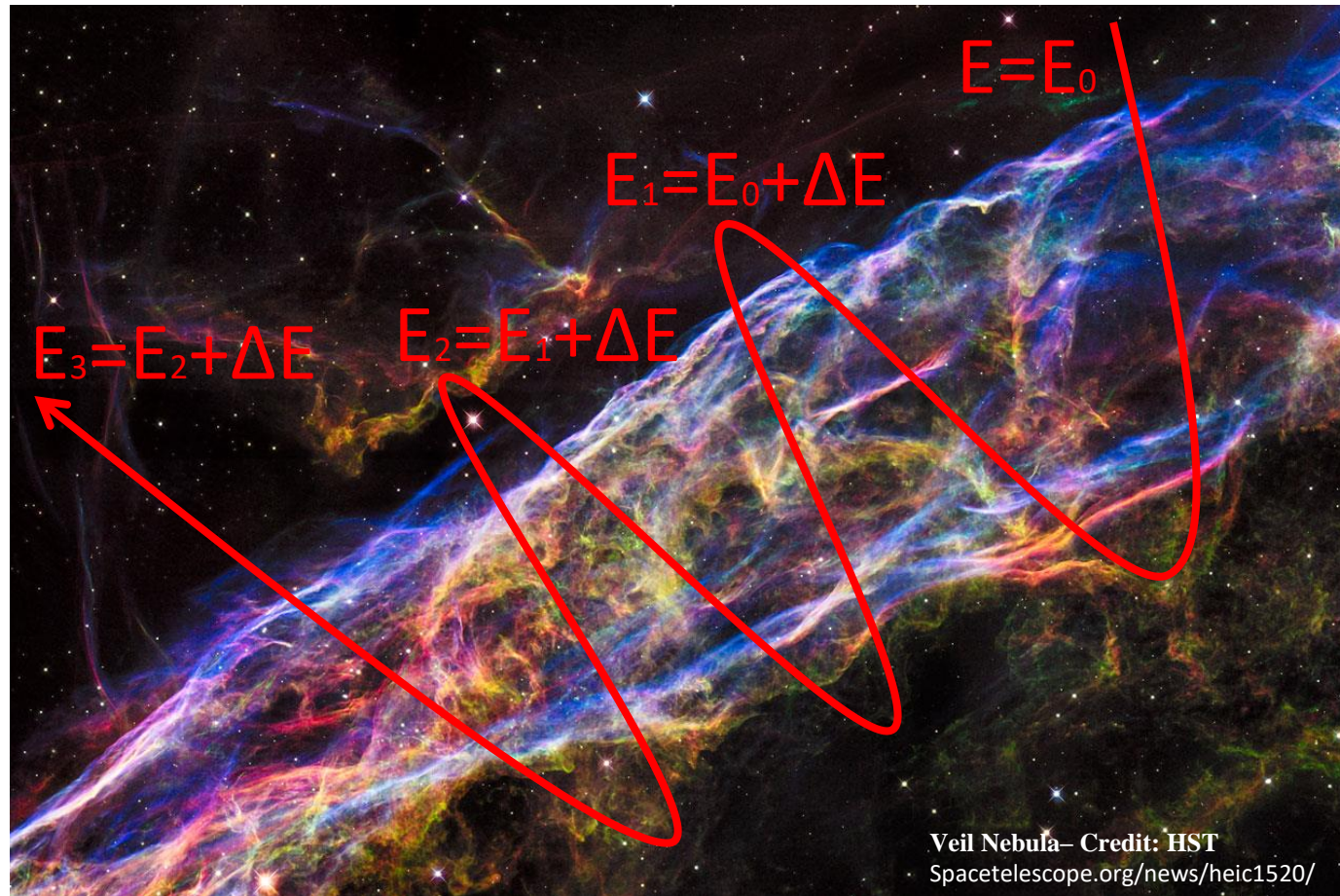
Diffusive Shock Acceleration



Veil Nebula– Credit: HST
Spacetelescope.org/news/heic1520/

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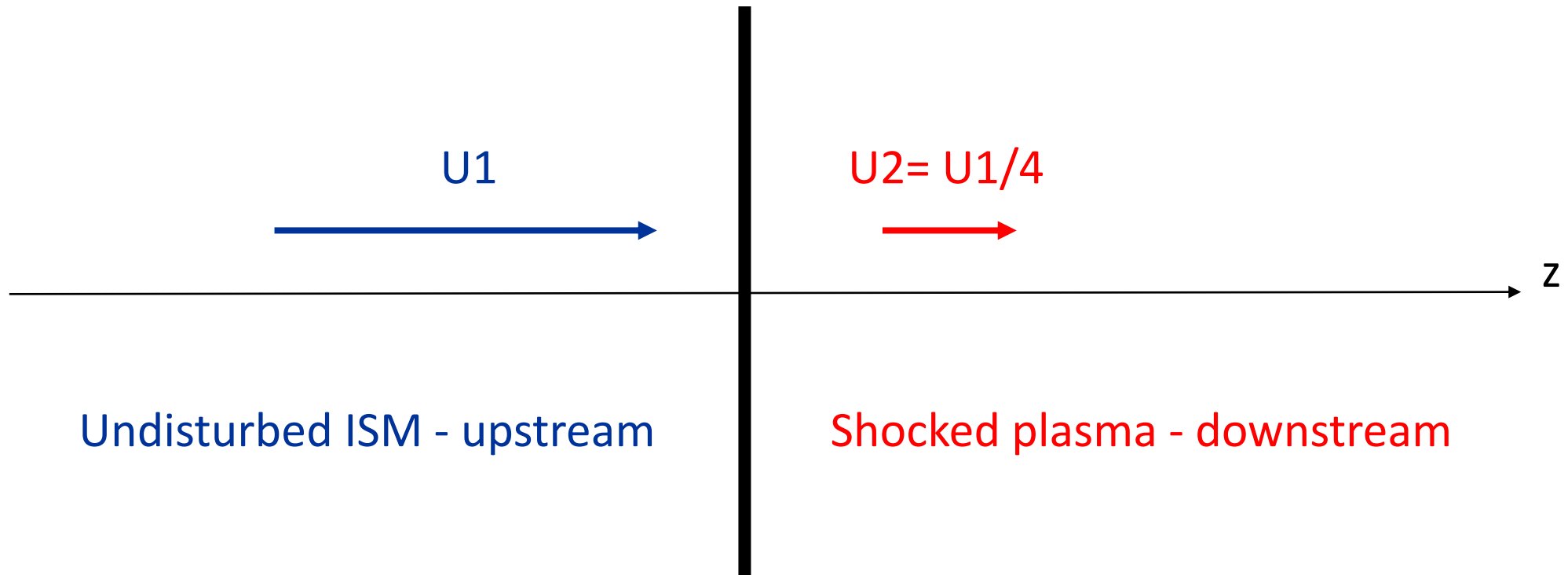


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- One of the most simple and efficient first order Fermi mechanism we know in Nature
- Particles diffuse across shock waves gaining energy at each cycle

$$\Delta E / E \propto \beta_{sh}$$

Transport approach to DSA

$$\frac{\partial f}{\partial t} + v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q - \frac{f}{\tau_{loss}}$$

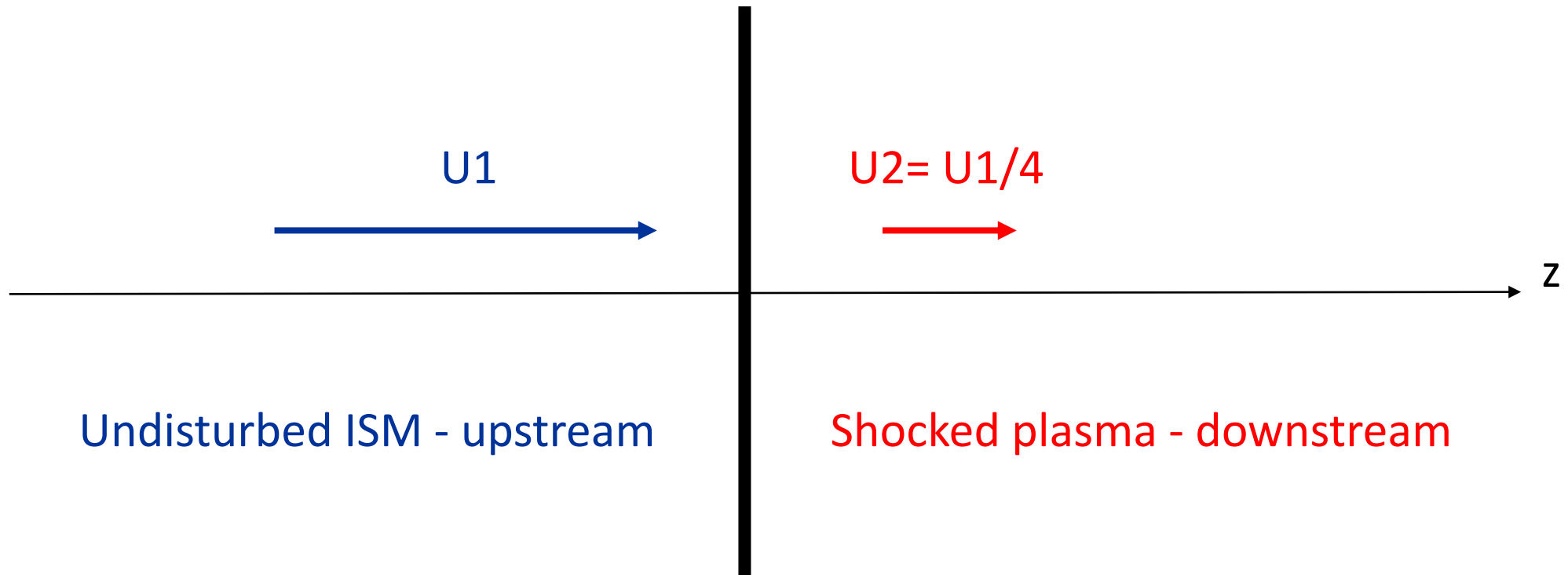


Transport approach to DSA

STATIONARY

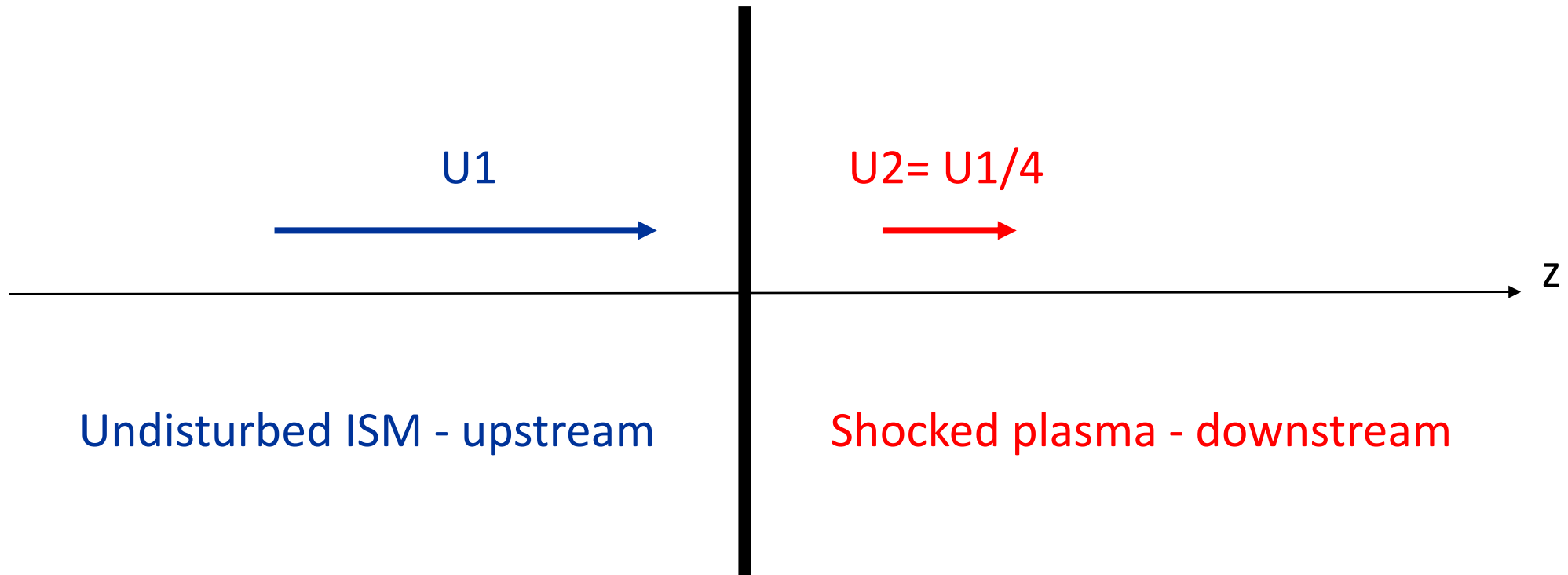
$$\cancel{\frac{\partial f}{\partial t}} + v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q - \cancel{\frac{f}{\tau_{loss}}}$$

NEGLIGIBLE



Boundary conditions

$$v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q$$



Boundary conditions

Far upstream the particle distribution function as well as the associated flux are negligible



Boundary conditions

$$f(-\infty) = \partial_z f|_{-\infty} = 0$$

**The strong turbulence homogenizes the
particle distribution function in the
downstream region**



Boundary conditions

$$f(-\infty) = \partial_z f|_{-\infty} = 0$$

$$\partial_z f|_{z>0} = 0$$

Undisturb

**The injection of high energy particles
takes place only at the shock**

downstream

z

Boundary conditions

$$f(-\infty) = \partial_z f|_{-\infty} = 0$$

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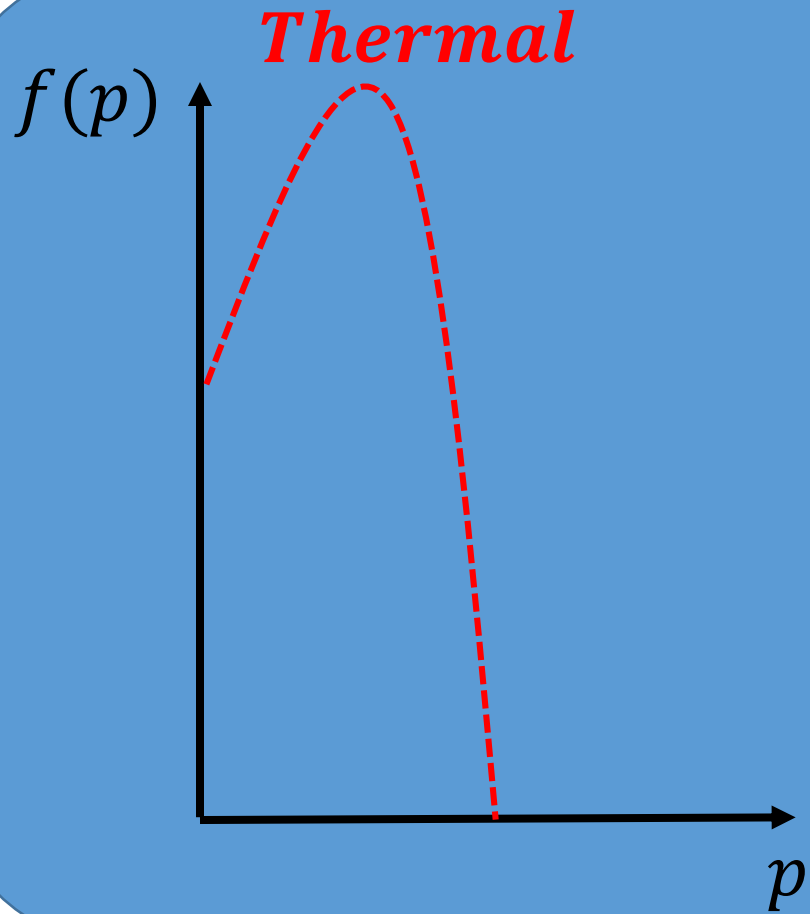
Undisturb

$$Q(z, p) = \xi_{CR} \frac{n_1 u_1}{4\pi p^2} \delta[p - p_{inj}] \delta[z]$$

downstream

z

Boundary conditions



$$f(-\infty) = \partial_z f$$

$$\partial_z f|_{z>0} =$$



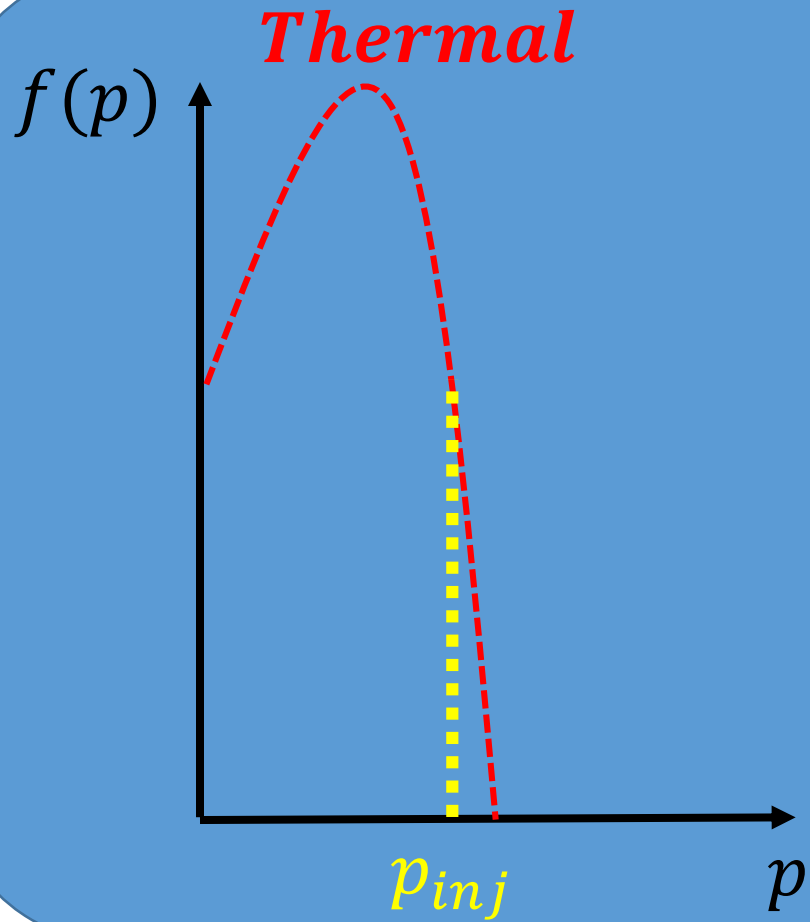
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Boundary conditions



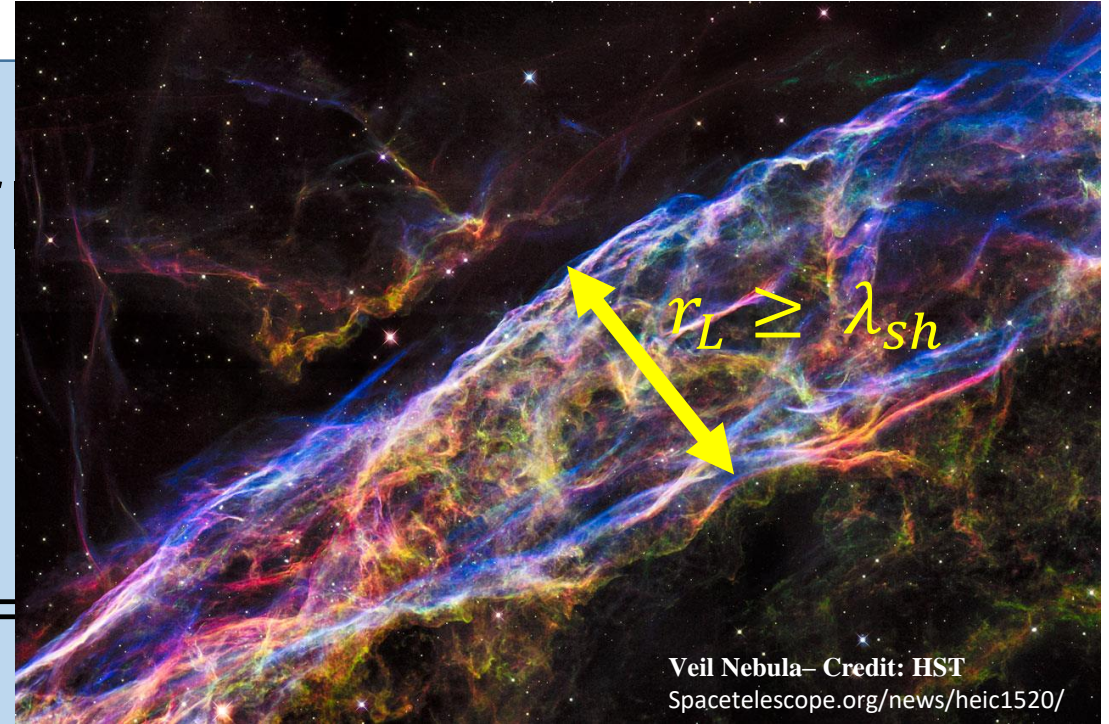
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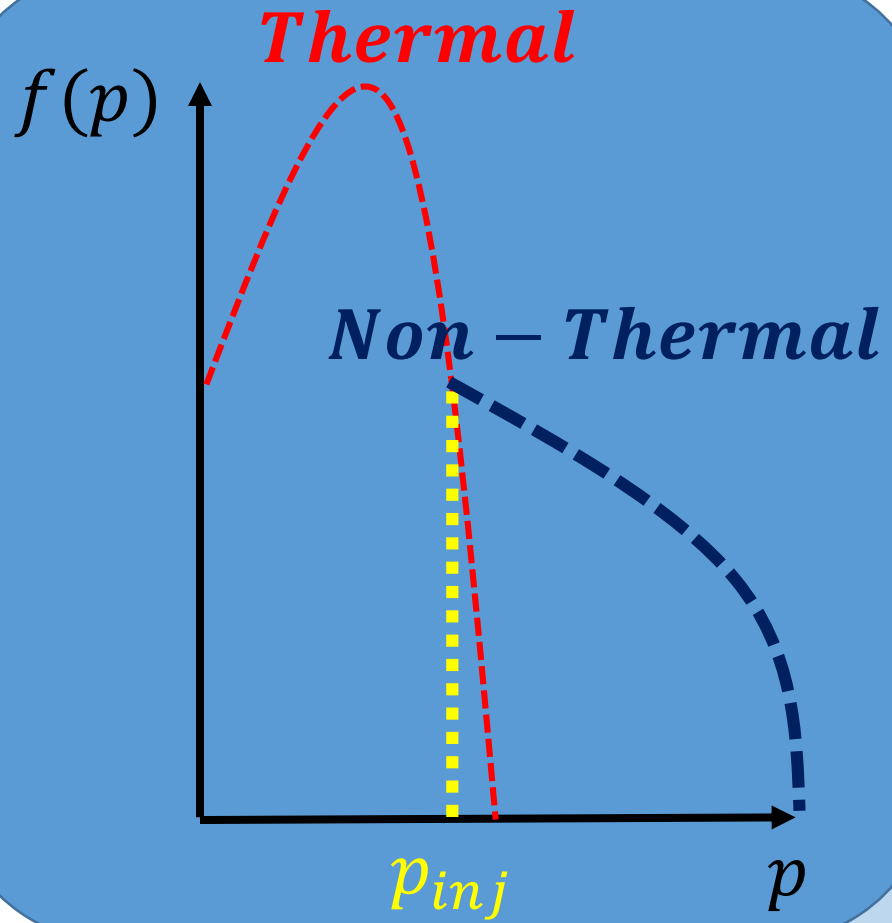
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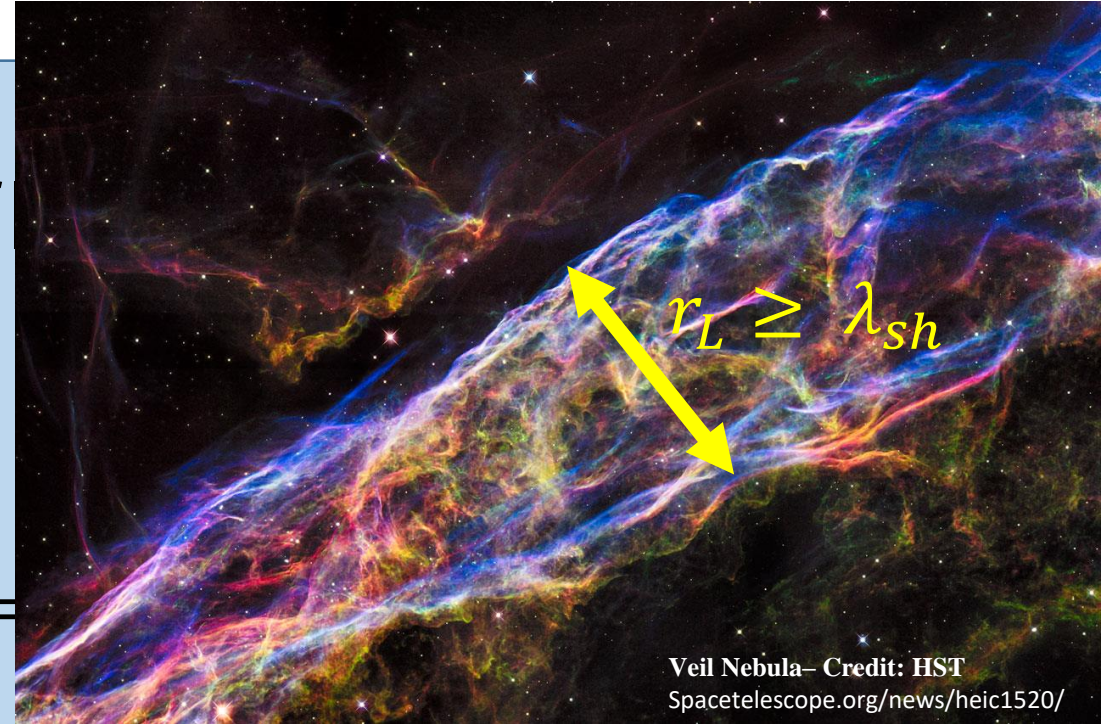
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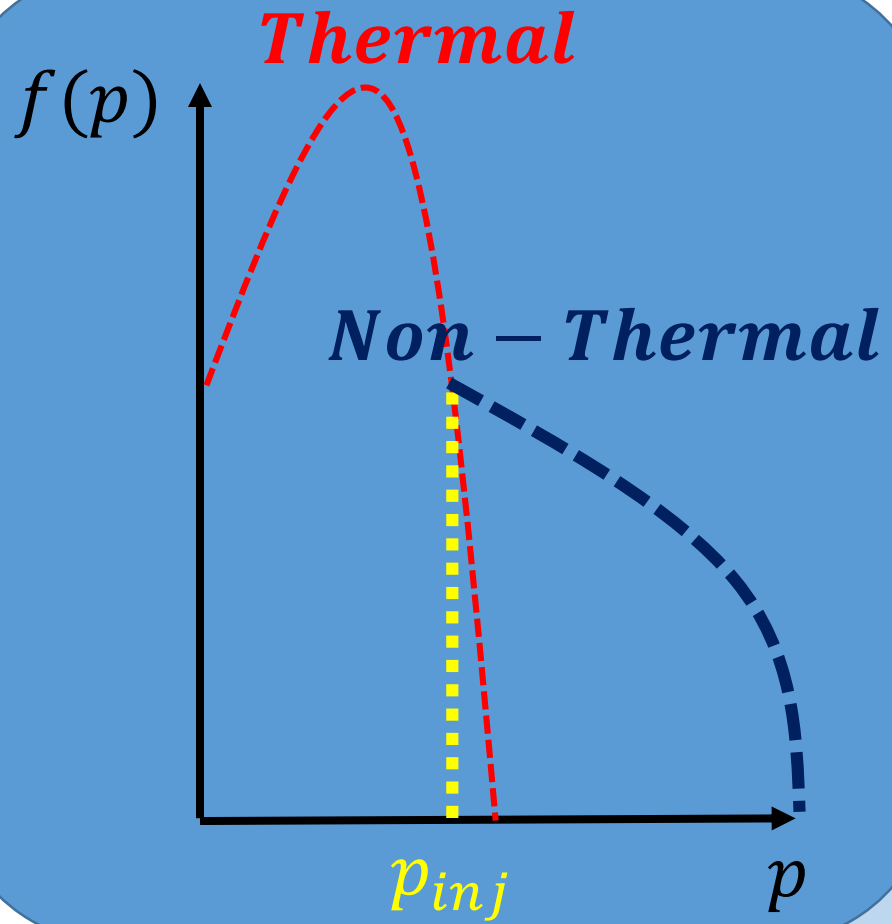
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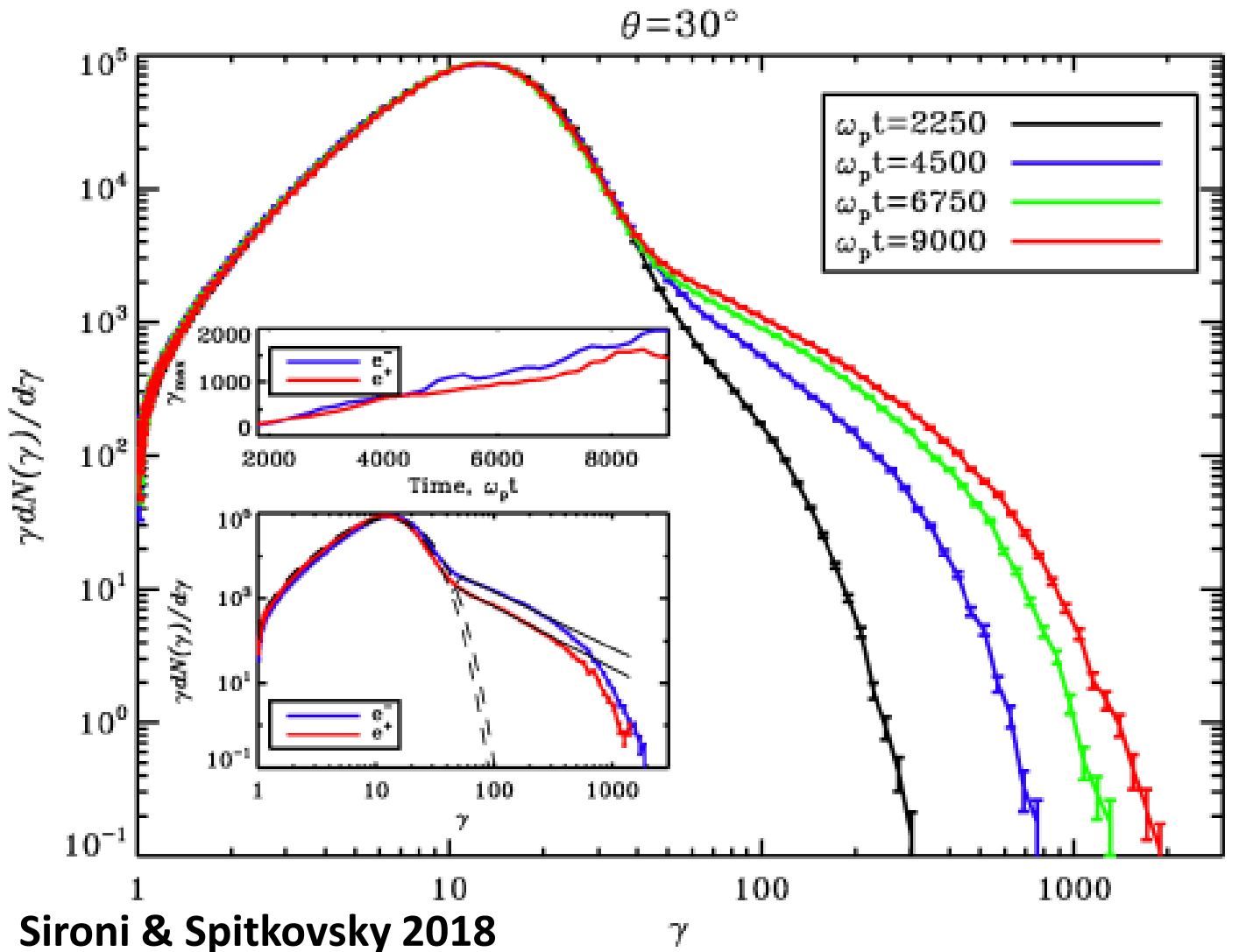
z

Boundary conditions



Undisturbed

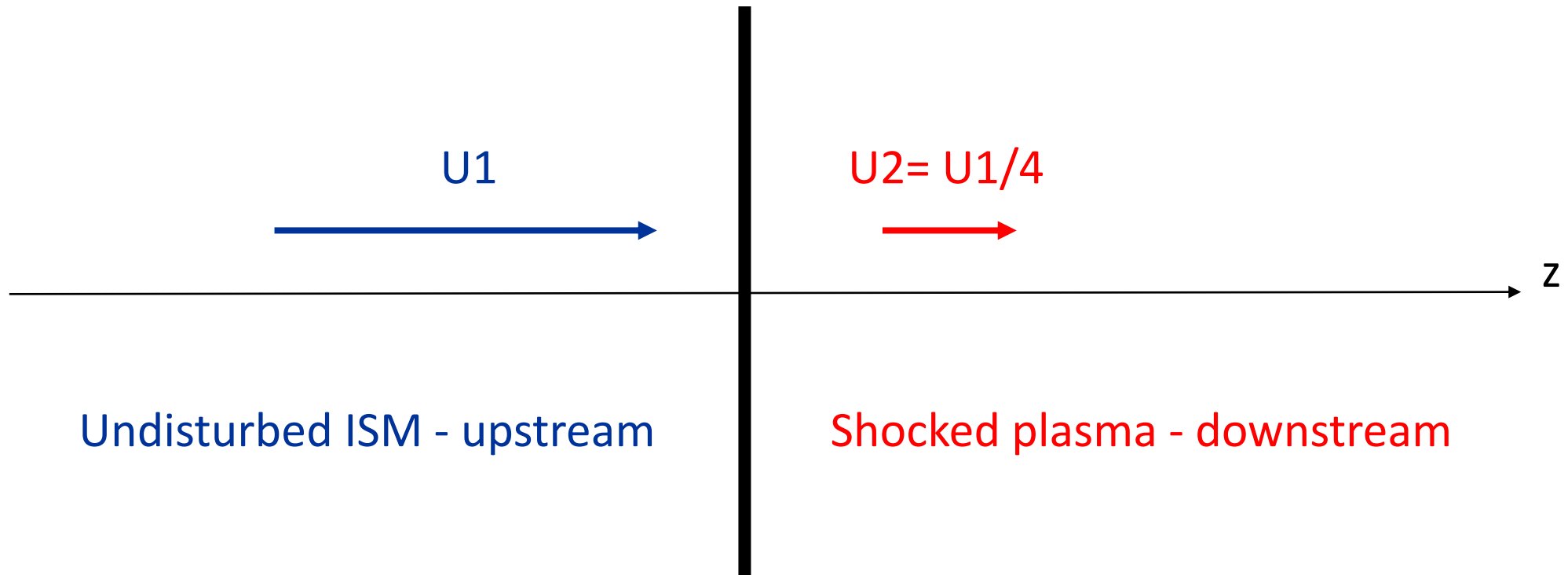
$$Q(z, p) =$$



Sironi & Spitkovsky 2018

Upstream solution

$$v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q$$



Upstream solution

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$$\int_{-\infty}^z dz' \text{ T.E.} \rightarrow v f|_{-\infty}^z = D \partial_z f|_{-\infty}^z + 0 + 0$$

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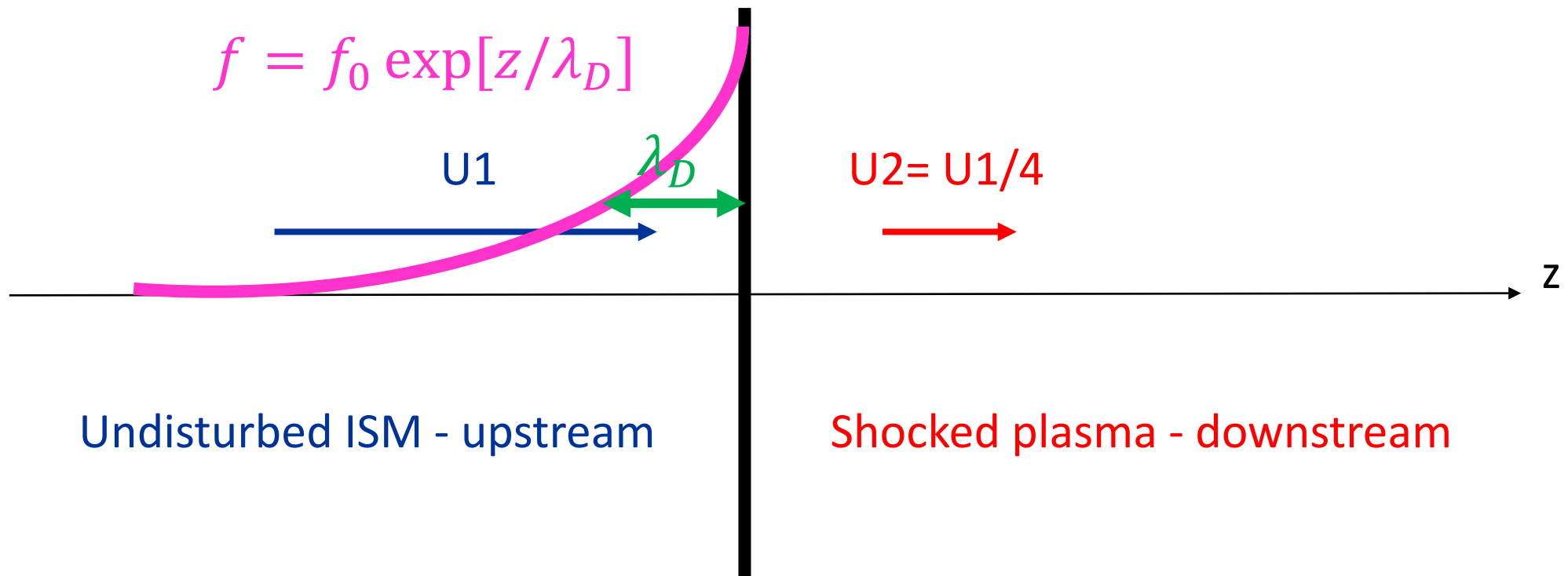
$$v f = D \partial_z f$$

$$f = f_0 \exp[z/\lambda_D]$$

$$\lambda_D = D/U_1$$

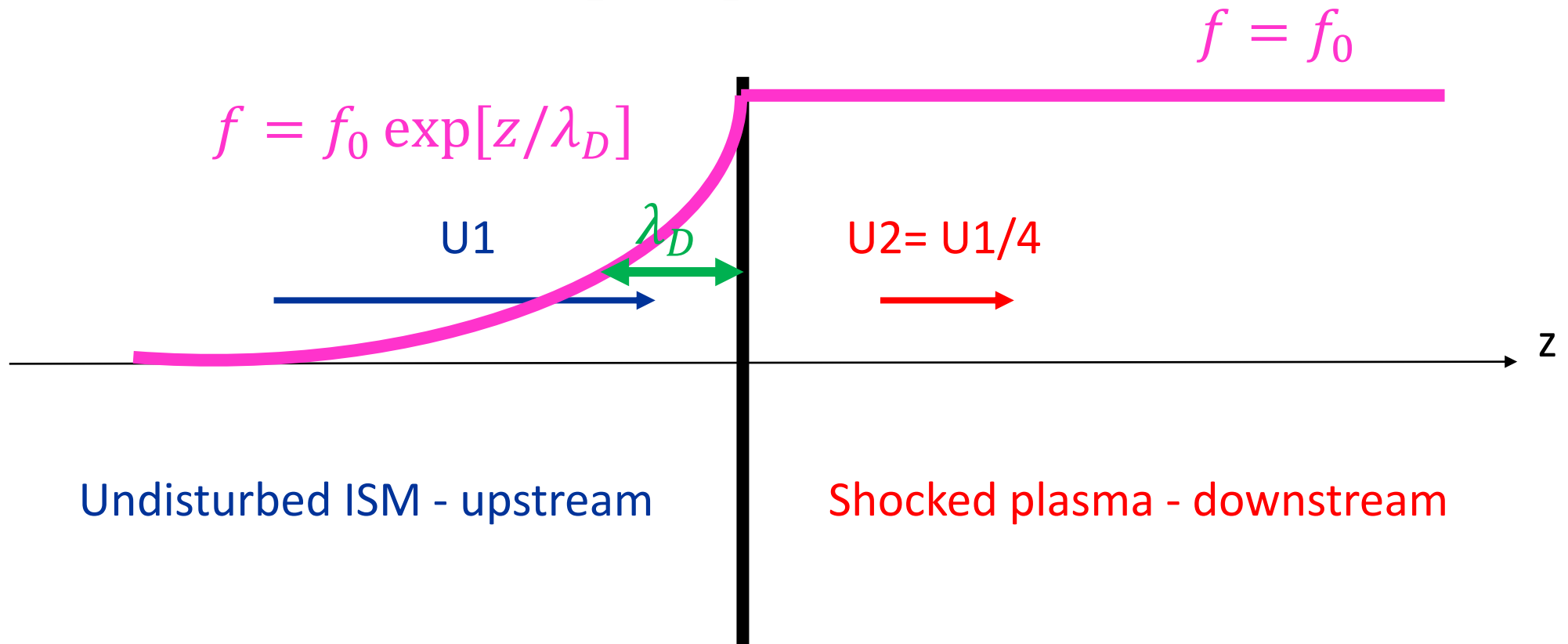
Radial distribution

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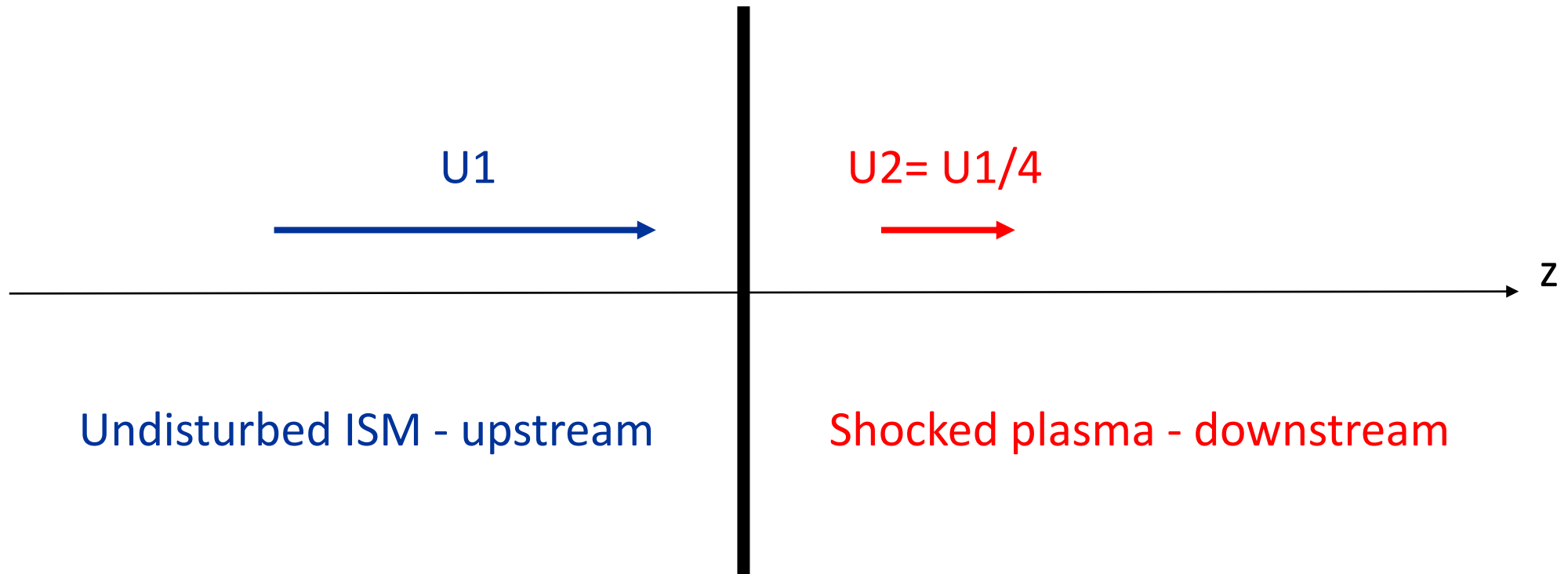
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Solution at the shock

$$v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q$$



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$$\int_{0^-}^{0^+} dz' \text{ T.E.}$$

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$$v(z) = U_1 + (U_2 - U_1) \theta[z]$$

Solution at the shock

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$$v(z) = U_1 + (U_2 - U_1) \theta[z]$$

$$\frac{\partial v}{\partial z} = (U_2 - U_1) \delta[z]$$

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$$\int_{0^-}^{0^+} dz' v \frac{\partial f}{\partial z'} = 0$$

Solution at the shock

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$$\int_{0^-}^{0^+} dz' T.E. \rightarrow 0 =$$

Solution at the shock

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$$\int_{0^-}^{0^+} dz' \frac{\partial}{\partial z'} \left[D \frac{\partial f}{\partial z'} \right] = D \partial_z f \Big|_{0^-}^{0^+} = -D \partial_z f_0$$

$$\int_{0^-}^{0^+} dz' \text{ T.E.} \rightarrow 0 = -D \partial_z f_0$$

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$$\int_{0^-}^{0^+} dz' \frac{1}{3} \frac{\partial v}{\partial z'} p \frac{\partial f}{\partial p} = \frac{(U_2 - U_1)}{3} p \partial_p f_0$$

$$\int_{0^-}^{0^+} dz' \text{ T.E.} \rightarrow 0 = -D \partial_z f_0 + \frac{(U_2 - U_1)}{3} p \partial_p f_0$$

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$$\int_{0^-}^{0^+} dz' Q(z', p) = \int_{0^-}^{0^+} dz' Q_0(p) \delta[z'] = Q_0(p)$$

$$\int_{0^-}^{0^+} dz' \text{ T.E.} \rightarrow 0 = -D \partial_z f_0 + \frac{(U_2 - U_1)}{3} p \partial_p f_0 + Q_0(p)$$

Solution at the shock

$$0 = -D\partial_z f_0 + \frac{(U_2 - U_1)}{3} p \partial_p f_0 + Q_0(p)$$

$U_1 f_0 = D \partial_z f_0$ - Upstream flux conservation

Solution at the shock

$$0 = -U_1 f_0 + \frac{(U_2 - U_1)}{3} p \partial_p f_0 + Q_0(p)$$

Solution at the shock

$$0 = -U_1 f_0 + \frac{(U_2 - U_1)}{3} p \partial_p f_0 + Q_0(p)$$

$$0 = -s f_0 - p \partial_p f_0 + s \frac{Q_0(p)}{U_1} \qquad s = \frac{3U_1}{(U_1 - U_2)}$$

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$$\partial_p f_0 + \frac{s}{p} f_0 = \frac{s}{p} \frac{Q_0(p)}{U_1}$$

$$\partial_p [f_0 p^s] = \frac{s}{p} \frac{Q_0(p)}{U_1} p^s$$

Solution at the shock

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Solution at the shock

$$\partial_p [f_0 p^s] = \frac{s}{p} \frac{Q_0(p)}{U_1} p^s$$

$$f_0 p^s = C + \int dp' \frac{s}{p'} \frac{Q_0(p')}{U_1} p'^s$$

Solution at the shock

$$\partial_p [f_0 p^s] = \frac{s}{p} \frac{Q_0(p)}{U_1} p^s$$

$$f_0 p^s = C + \int dp' \frac{s}{p'} \frac{Q_0(p')}{U_1} p'^s$$

$$f_0(p) = \frac{s \xi_{CR} n_1}{4\pi p_{inj}^3} \left(\frac{p_{inj}}{p}\right)^s$$

General considerations on the solution

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$$f_0(p) \sim p^{-4} \rightarrow f_0(E) = 4\pi p^2 f_0(p) \frac{dp}{dE} \sim E^{-2} \text{ (} pc \approx E\text{)}$$

General considerations on the solution

CR pressure divergence

$$P_{CR} = \frac{1}{3} \int dp \, 4\pi p^2 [pv(p)] f(p) \sim \int dp \, p^{3-s} \sim \ln(p) \rightarrow \infty$$

$$f_0(p) \sim p^{-4} \rightarrow f_0(E) = 4\pi p^2 f_0(p) \frac{dp}{dE} \sim E^{-2} \quad (pc \approx E)$$

On the maximum energy

The existence of a maximum energy can solve the problem of the divergence in the pressure

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A revision in the boundary conditions is required

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Possibilities:

1. The transport is time-dependent
2. The size of the system is finite

On the maximum energy

The existence of a maximum energy can solve the problem of the divergence in the pressure

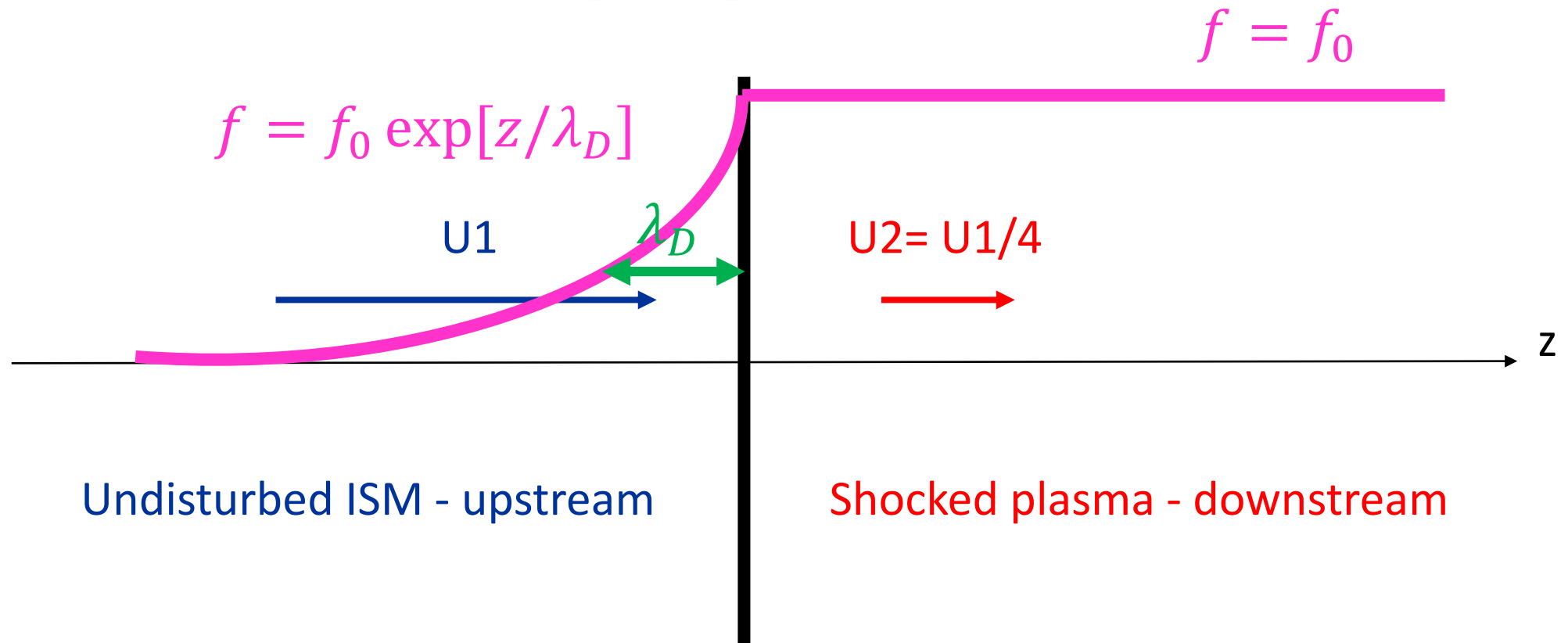
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Possibilities:

1. The transport is time-dependent
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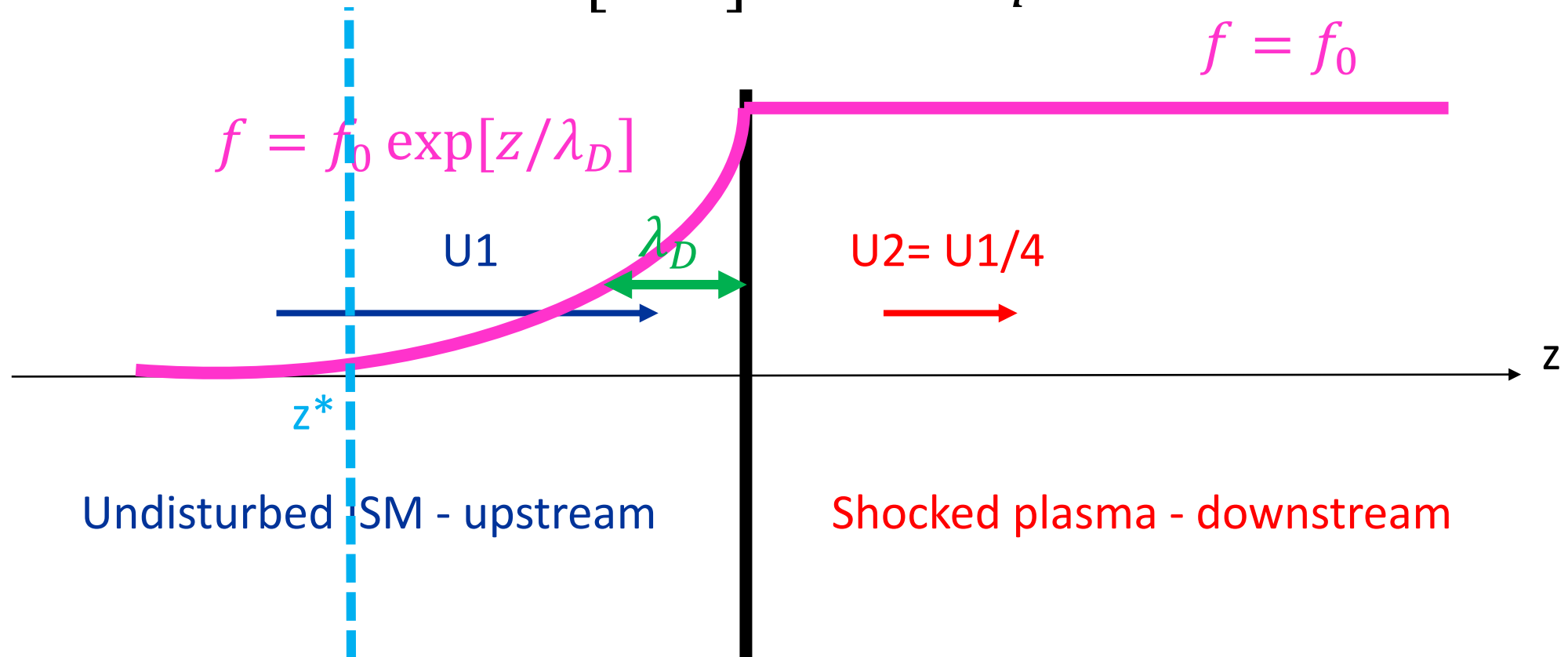
On the maximum Energy

$$v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q$$

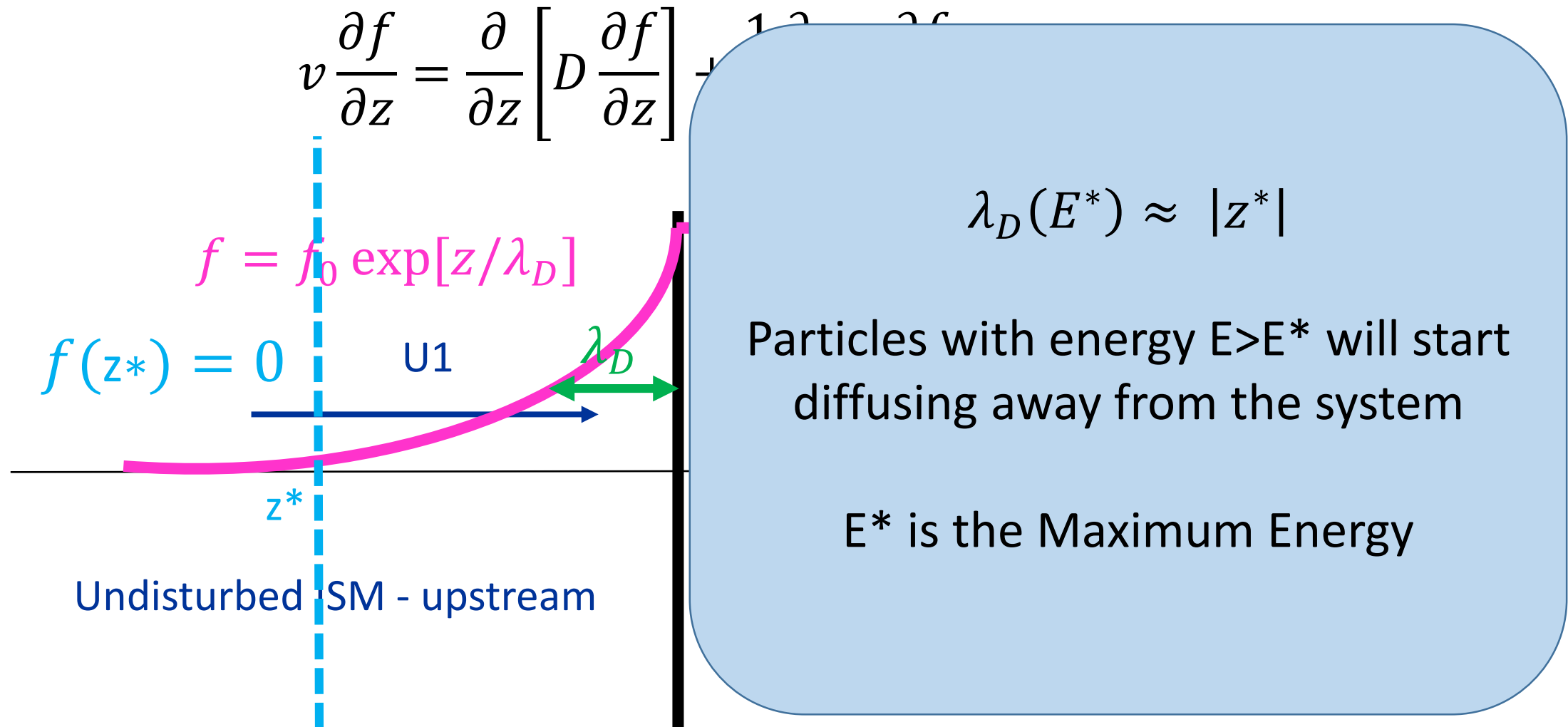


On the maximum Energy

$$v \frac{\partial f}{\partial z} = \frac{\partial}{\partial z} \left[D \frac{\partial f}{\partial z} \right] + \frac{1}{3} \frac{\partial v}{\partial z} p \frac{\partial f}{\partial p} + Q$$



On the maximum Energy



On the maximum Energy

Possible exercise:

**Try to solve the transport equation
at the infinite planar
shock introducing the free escape
boundary condition**

***What is the mathematical
expression of the HE cutoff?***

$$\psi(E^*) \approx |z^*|$$

energy $E > E^*$ will start
away from the system

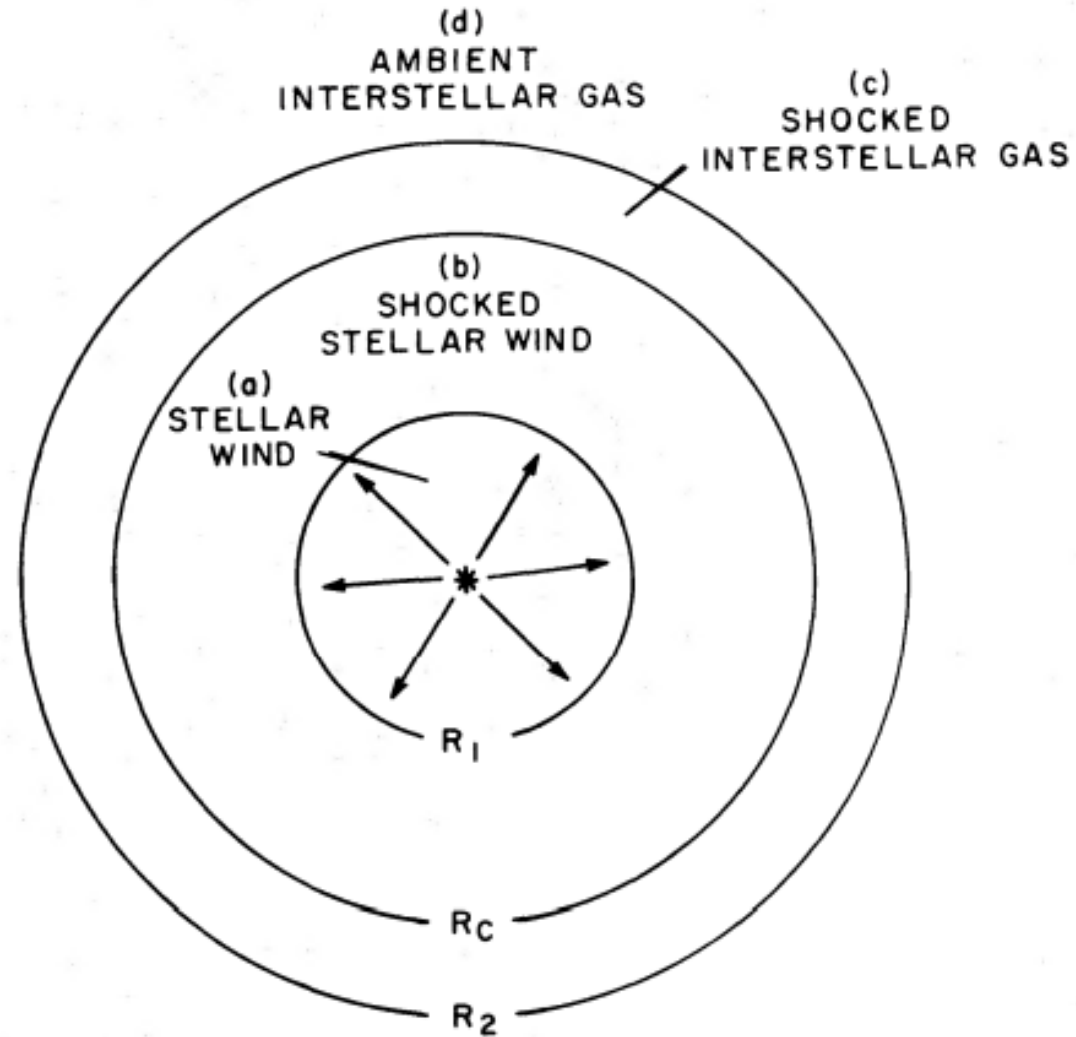
E^* is the Maximum Energy

Outline

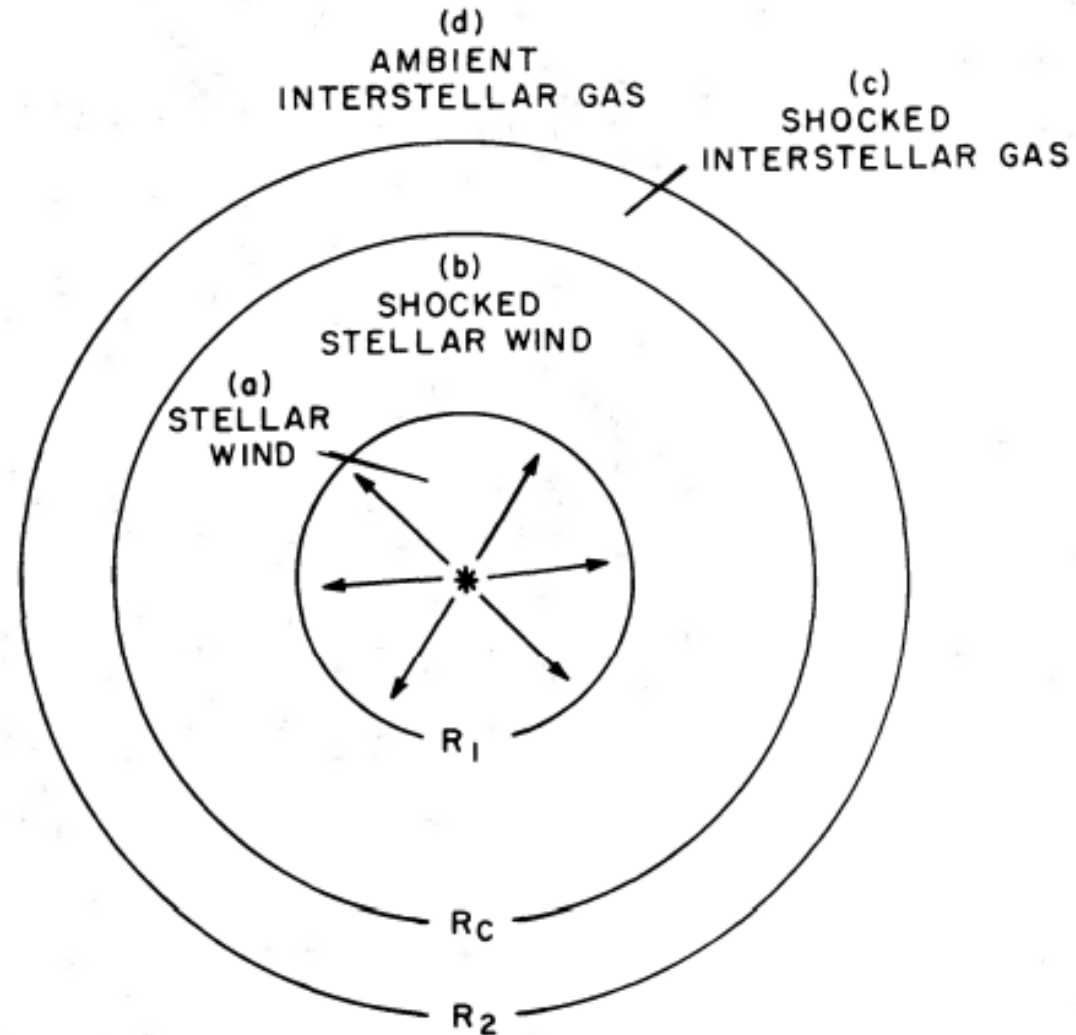
- Transport equation of Cosmic Rays
- Transport approach to diffusive shock acceleration
 - Wind blown bubbles
- Modeling acceleration and multi-messenger radiation

Diverging flows (wind bubbles)

- **Cavity in the ISM** excavated by the activity of a source blowing a **steady wind** with high velocity and large opening angle



Diverging flows (wind bubbles)

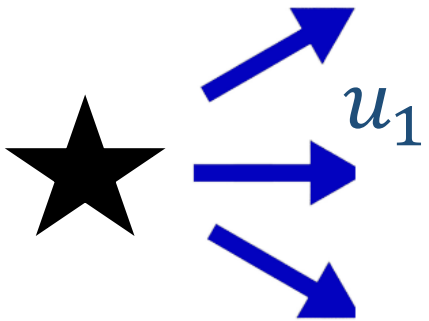


- **Cavity in the ISM** excavated by the activity of a source blowing a **steady wind** with high velocity and large opening angle

- Main macroscopic parameters:

1. Terminal wind speed: V_∞
2. Mass loss rate: \dot{M}
3. External medium: n_{ISM}
4. Age of the system: t_{age}

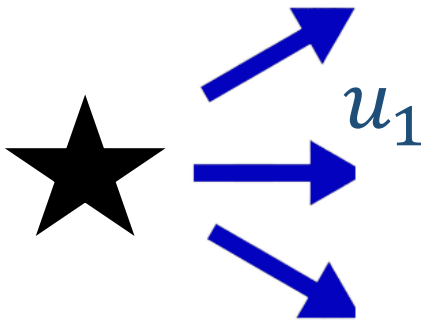
Structure and Evolution



1. The outflow is launched - t_0

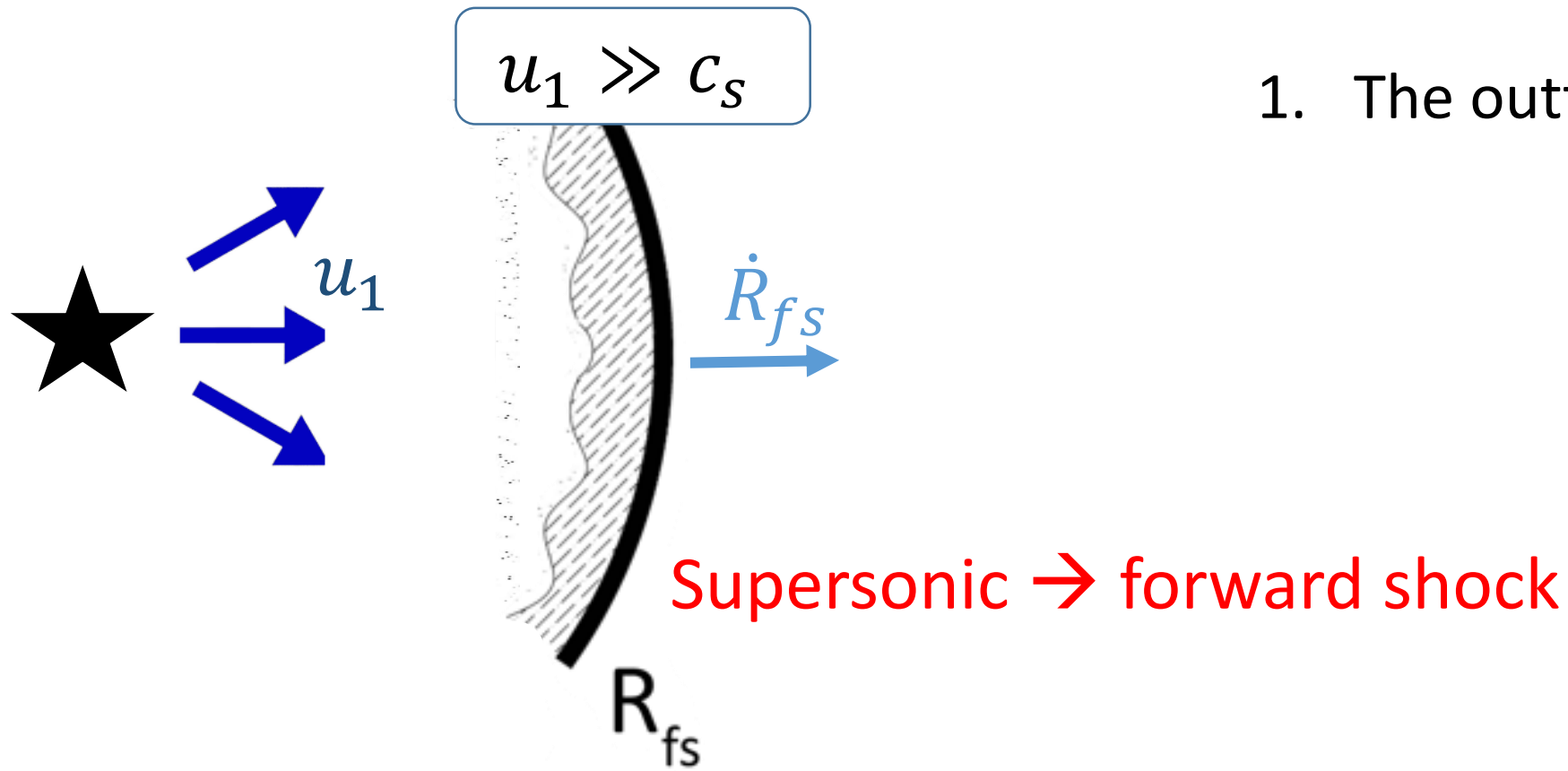
Structure and Evolution

$$u_1 \gg c_s$$



1. The outflow is launched - t_0

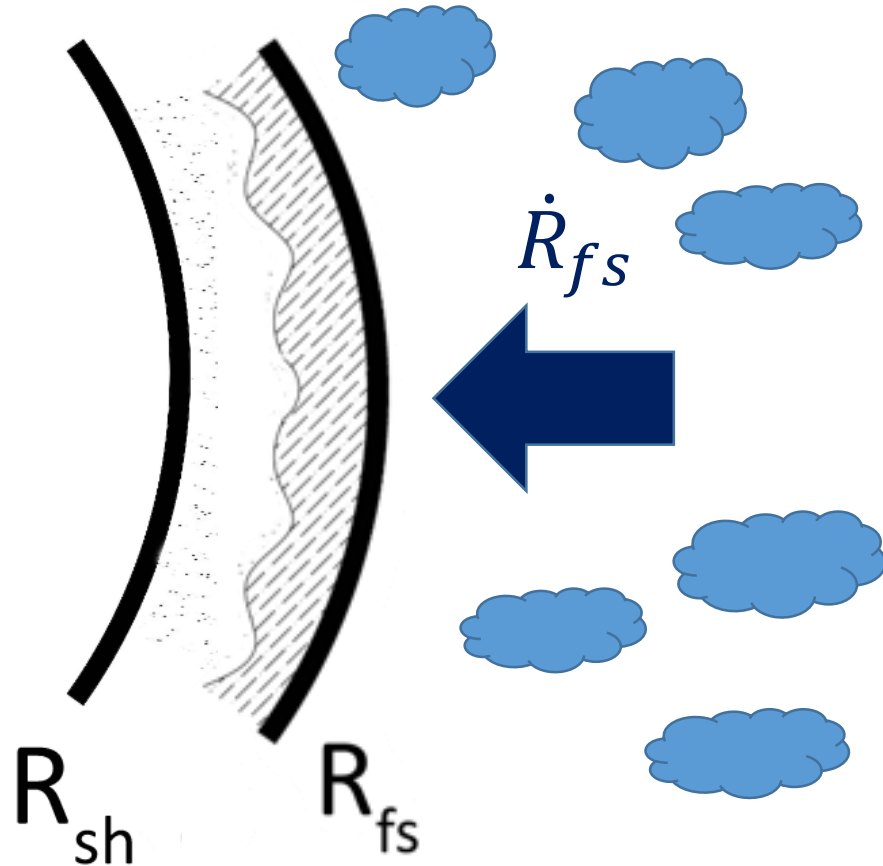
Structure and Evolution



1. The outflow is launched - t_0

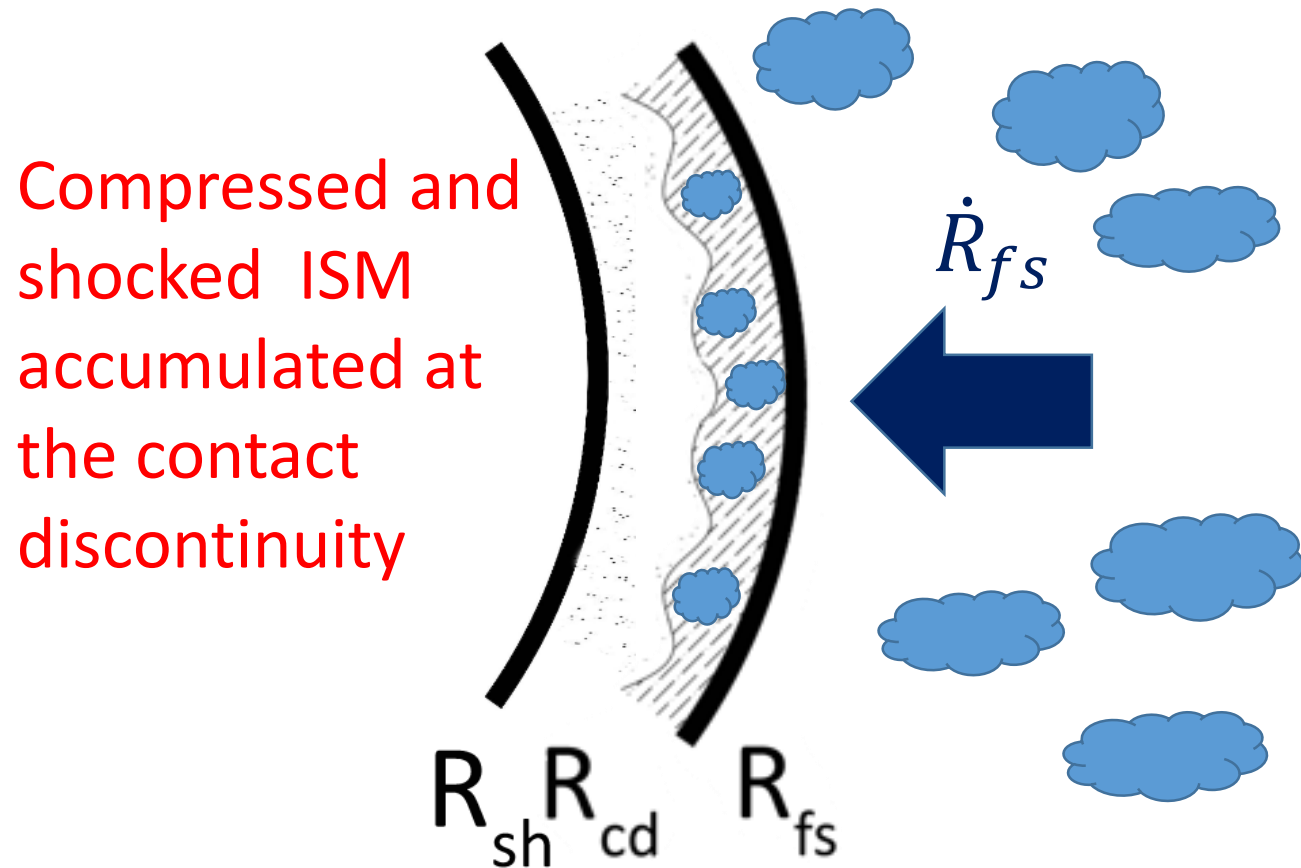
Structure and Evolution

Collision with ISM \rightarrow wind shock



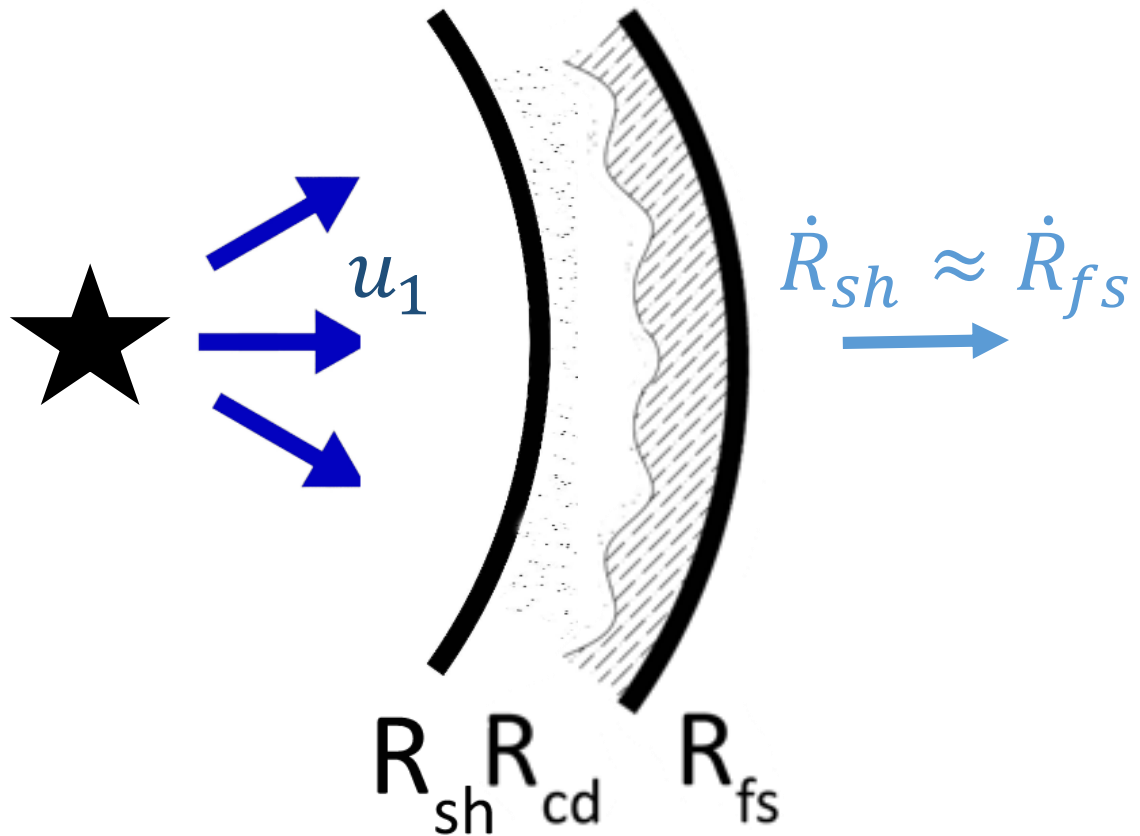
1. The outflow is launched - t_0

Structure and Evolution



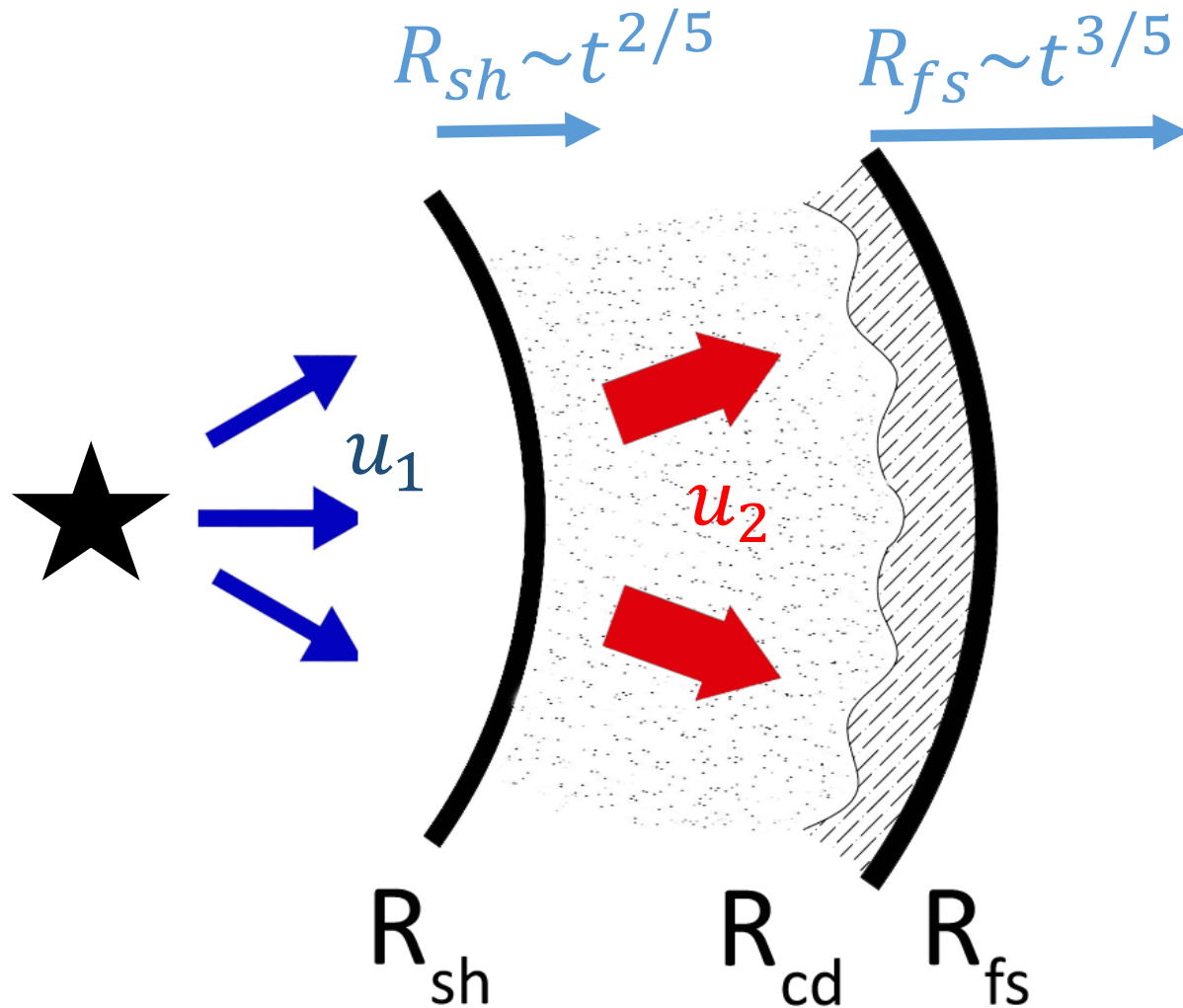
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Structure and Evolution



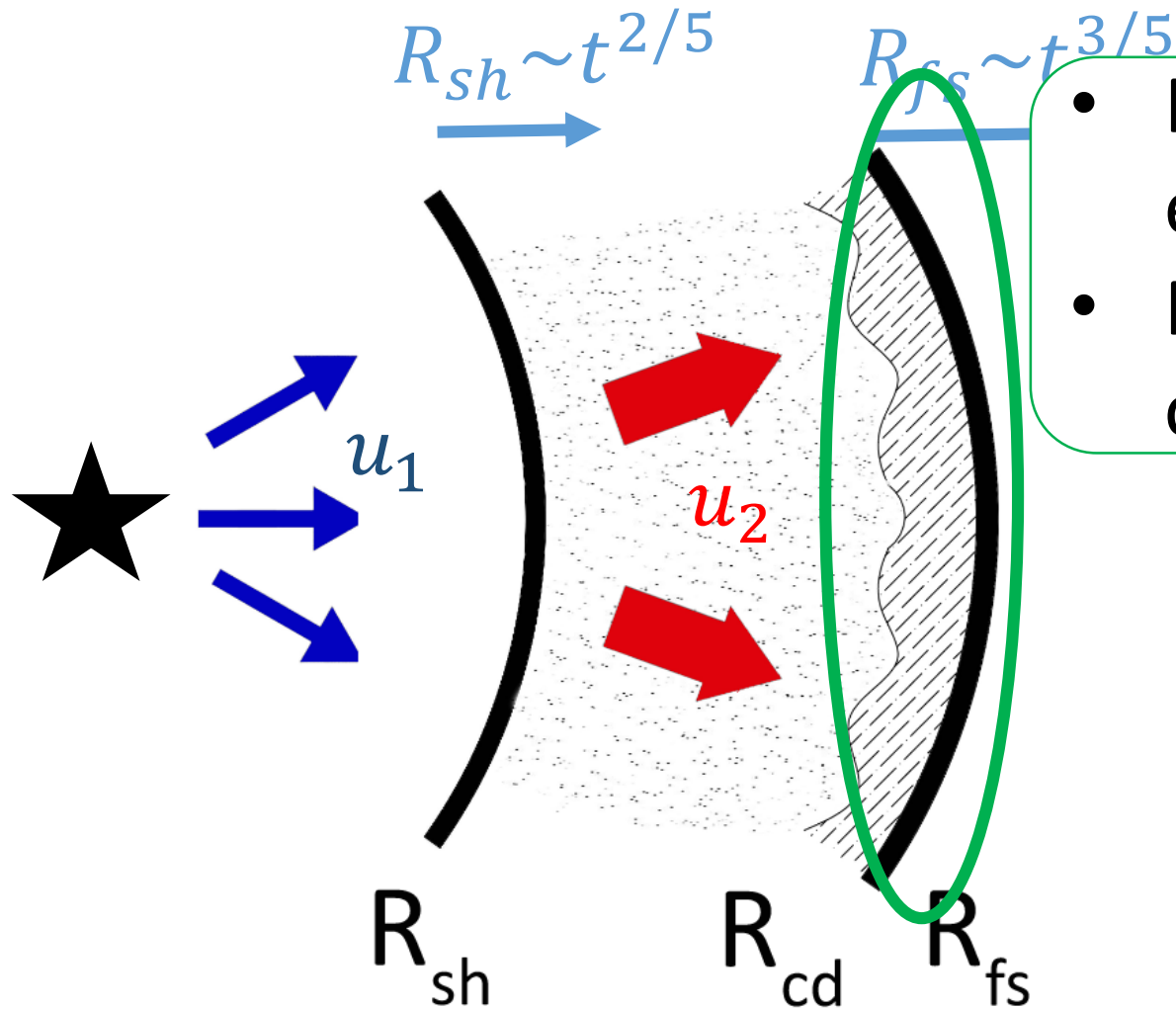
1. The outflow is launched - t_0
2. Free expansion phase - t_1

Structure and Evolution



1. The outflow is launched - t_0
2. Free expansion phase - t_1
3. Deceleration phase - $t > t_1$

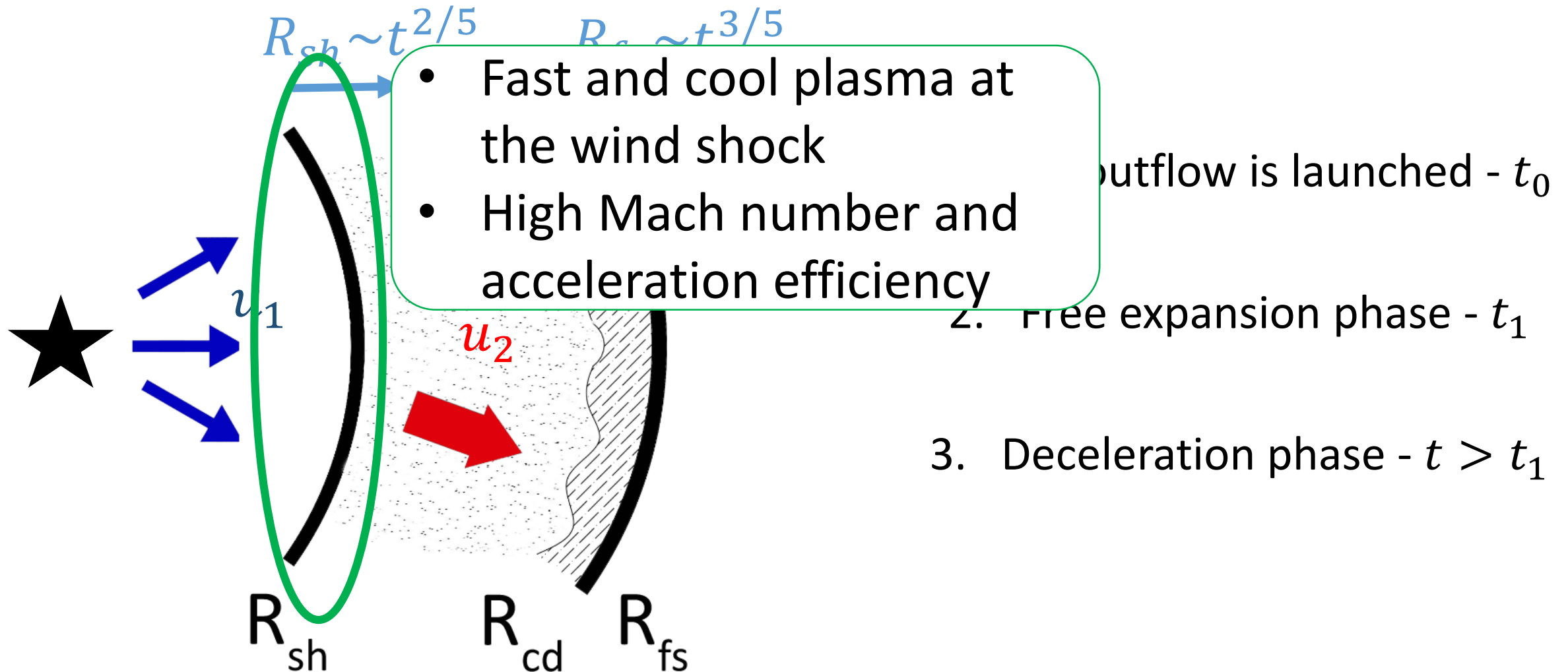
Characterizing the accelerator



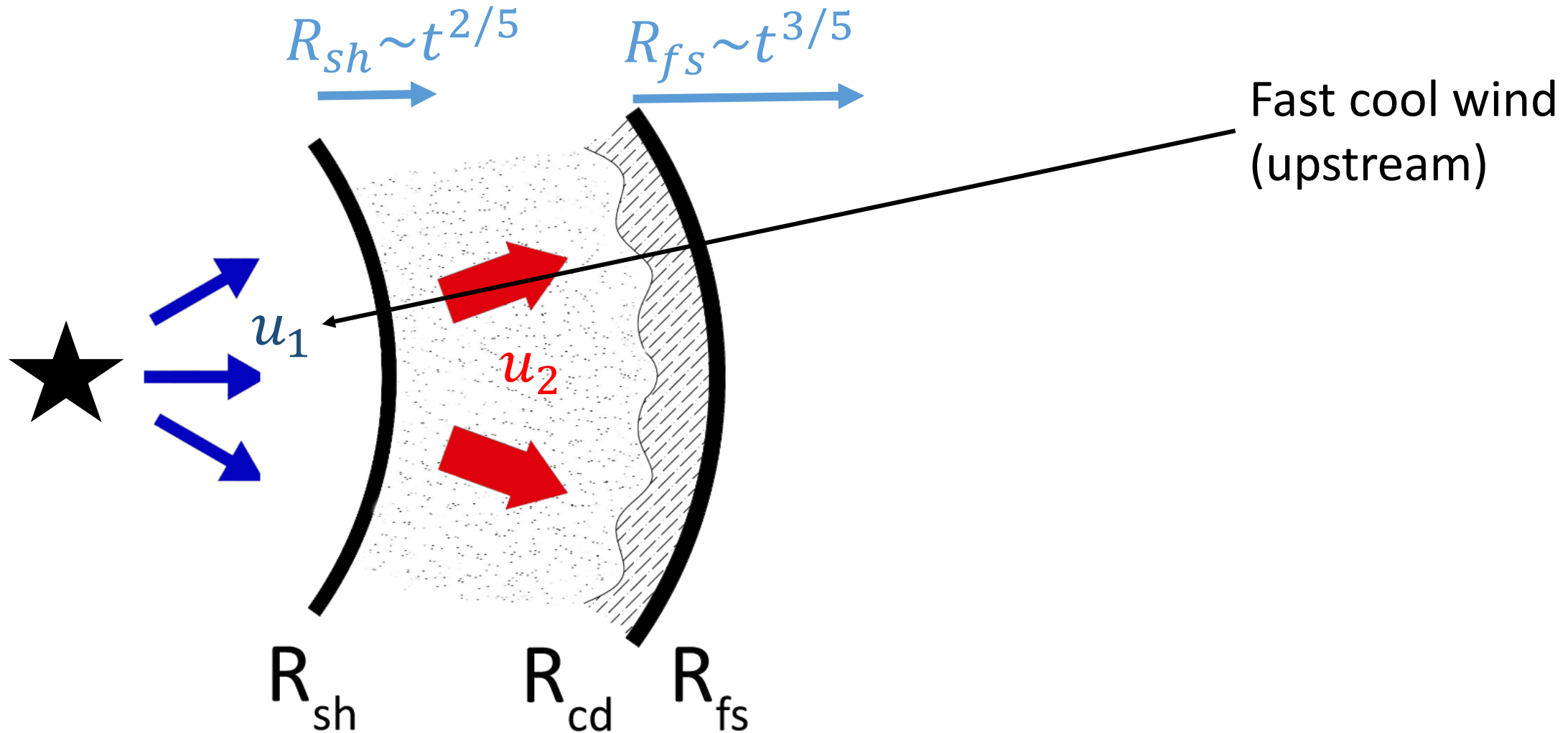
- Rapid fall of acceleration efficiency in time
- Mach number dependent on the external medium

1. Acceleration phase - $t < t_0$
2. Free expansion phase - t_1
3. Deceleration phase - $t > t_1$

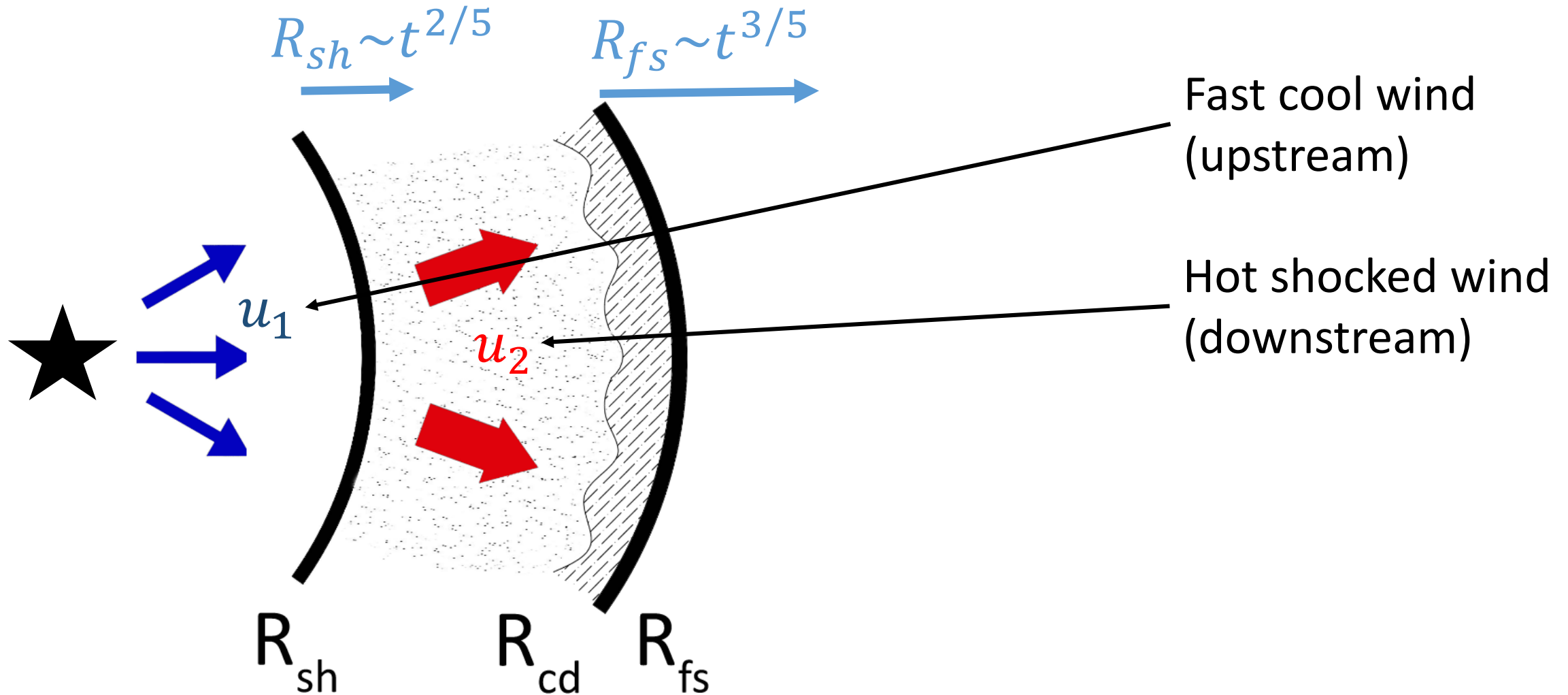
Characterizing the accelerator



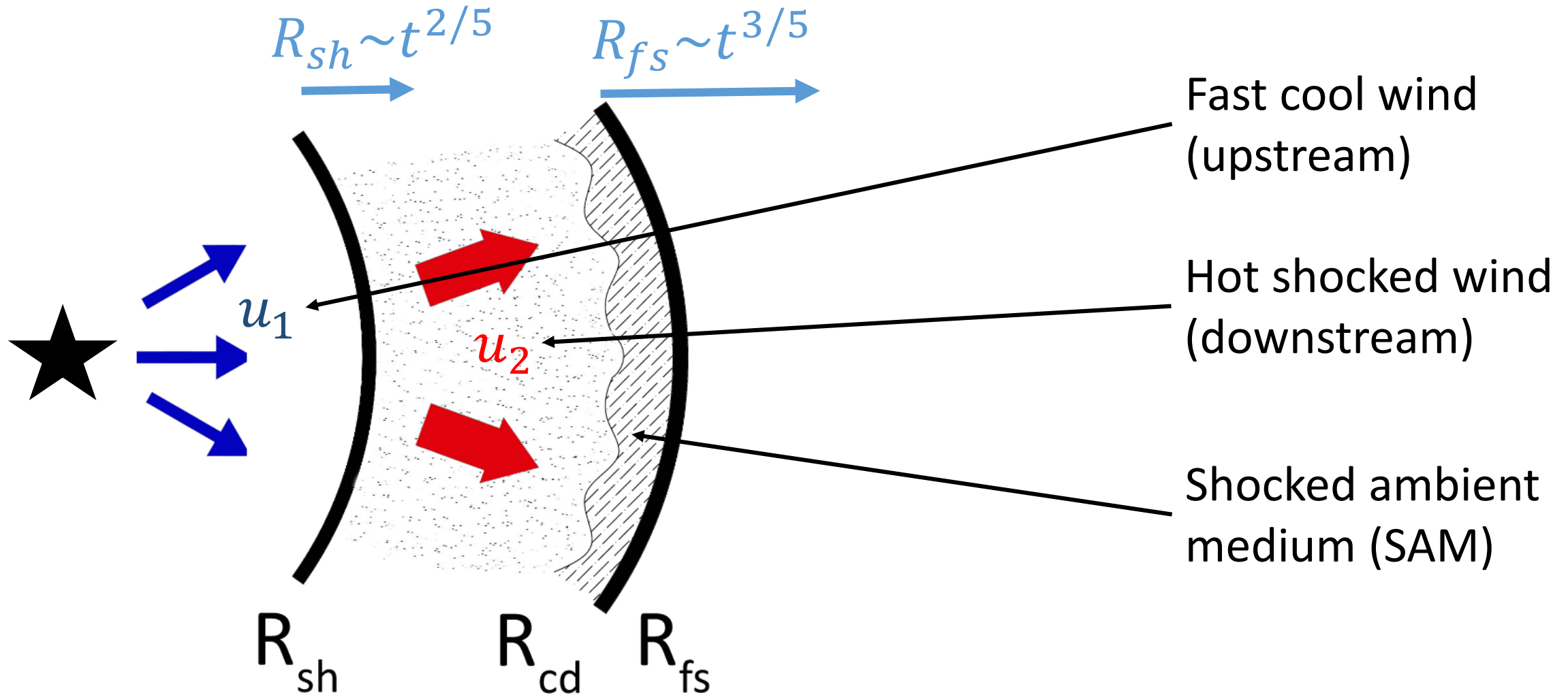
Characterizing the accelerator



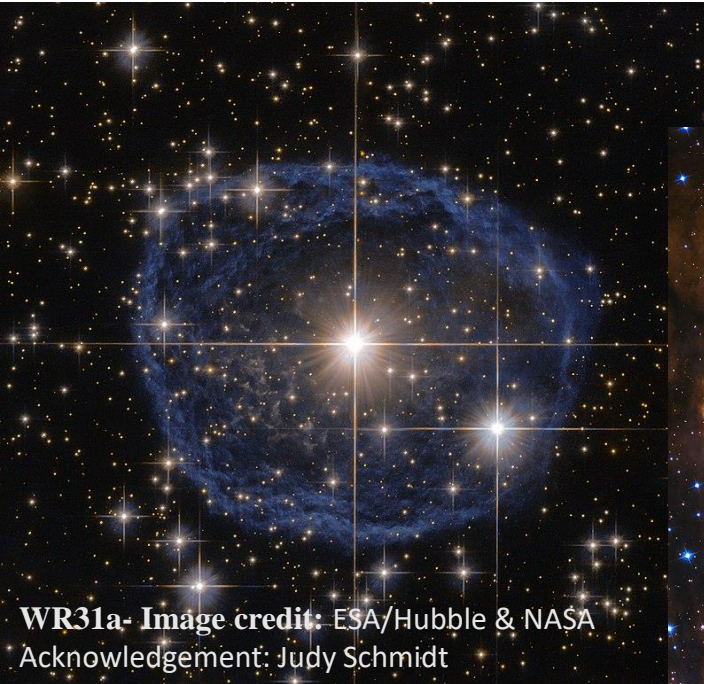
Characterizing the accelerator



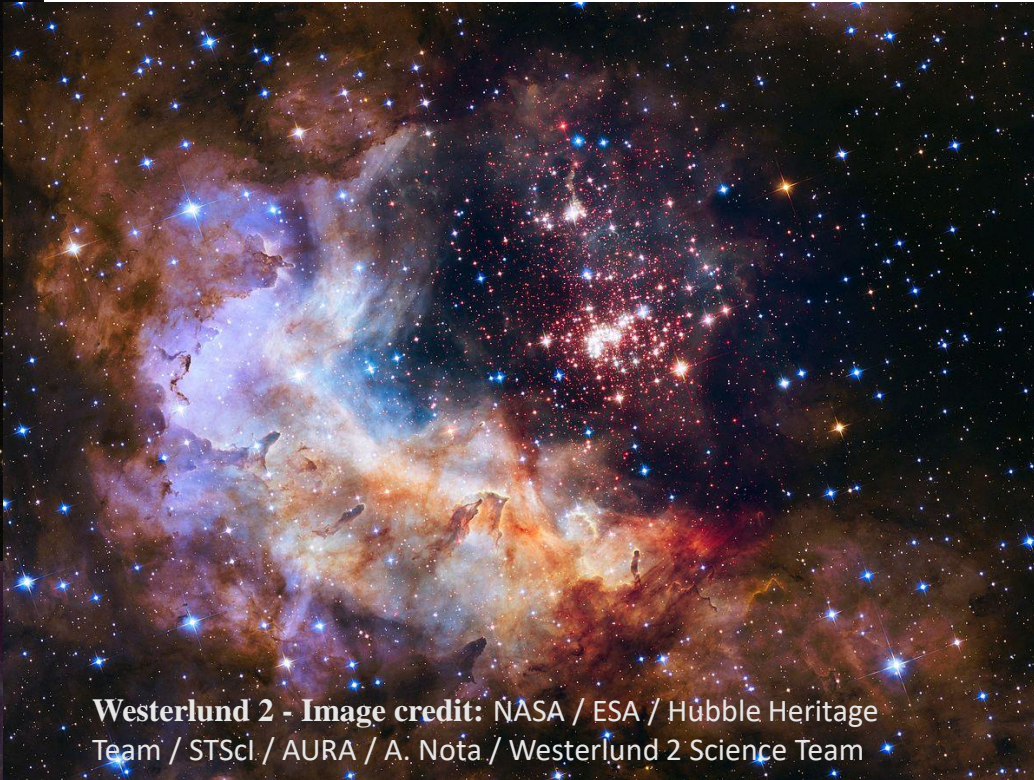
Characterizing the accelerator



Scale and power



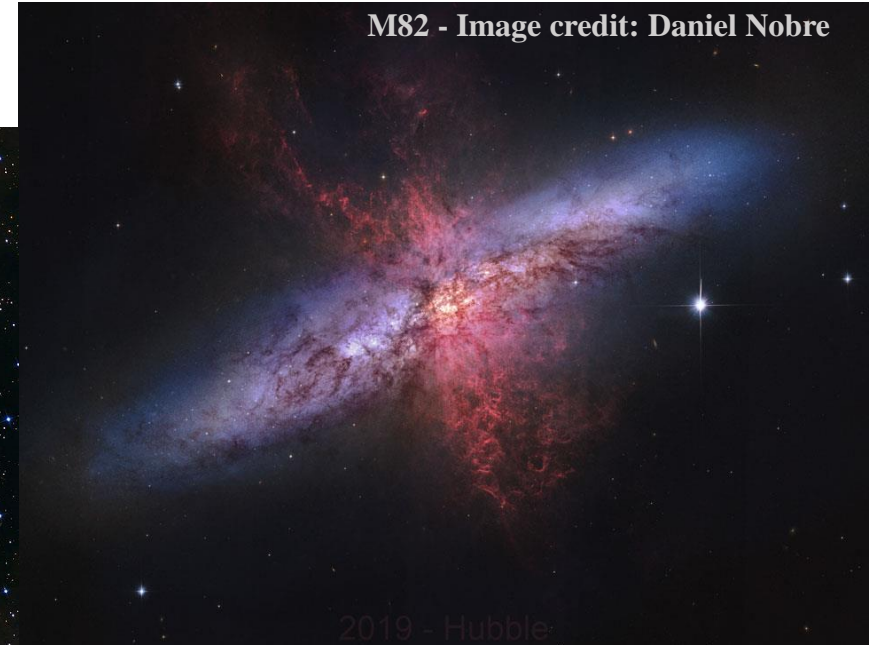
WR31a- Image credit: ESA/Hubble & NASA
Acknowledgement: Judy Schmidt



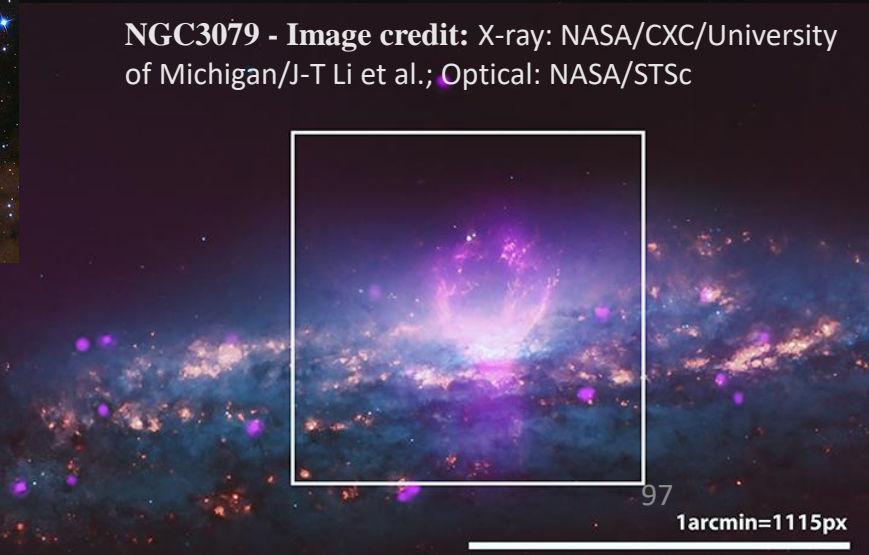
Westerlund 2 - Image credit: NASA / ESA / Hubble Heritage Team / STScI / AURA / A. Nota / Westerlund 2 Science Team



NGC7635- Image credit: NASA Goddard Space Flight Center from Greenbelt, MD, USA



M82 - Image credit: Daniel Nobre



NGC3079 - Image credit: X-ray: NASA/CXC/University of Michigan/J-T Li et al.; Optical: NASA/STSc

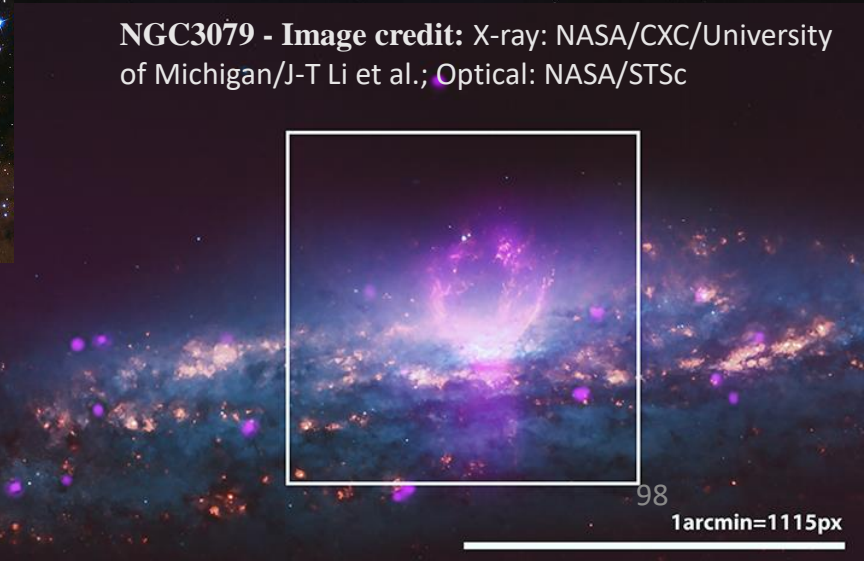
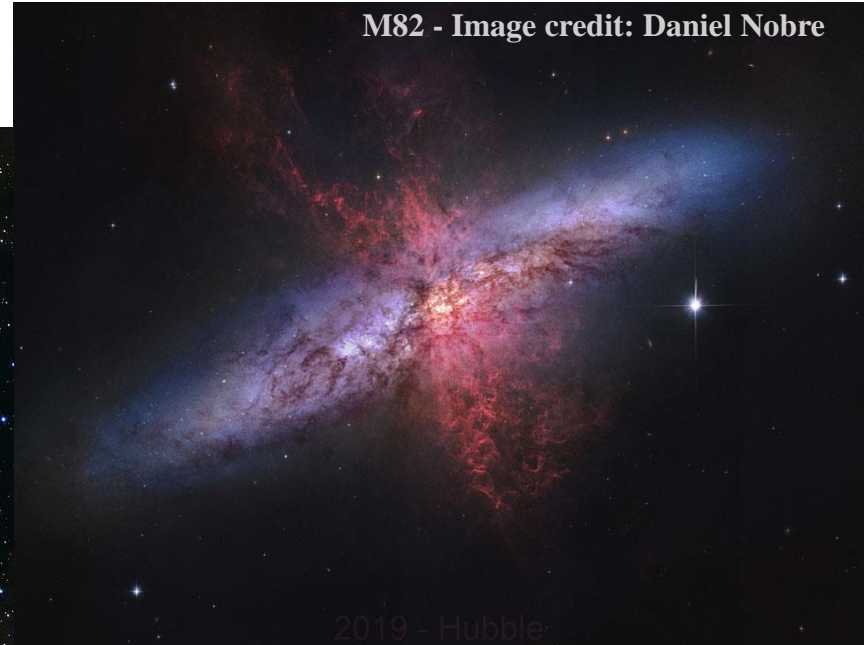
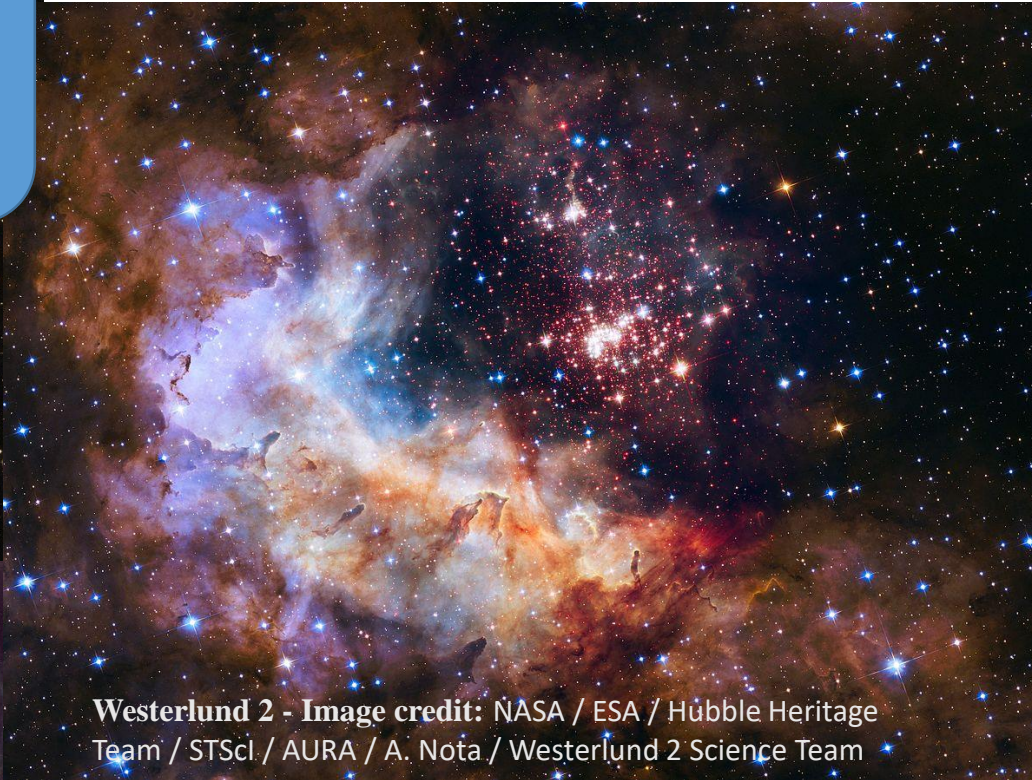
97
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Scale and power

Massive stars:

$$V_{\infty} \approx 10^2 - 10^3 \text{ km/s}$$

$$\dot{M} \lesssim 10^{-5} M_{\odot}/\text{yr}$$



Scale and power

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Star clusters:

$$V_{\infty} \approx 10^3 \text{ km/s}$$

$$\dot{M} \approx 10^{-4} M_{\odot}/\text{yr}$$

WR31a - Image credit: [unclear]
Acknowledgement: Judy

Westerlund 2 - Image credit: NASA / ESA / Hubble Heritage Team / STScI / AURA / A. Nota / Westerlund 2 Science Team

NGC7635 - Image credit: NASA Goddard Space Flight Center from Greenbelt, MD, USA

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2019 - Hubble

NGC3079 - Image credit: X-ray: NASA/CXC/University of Michigan/J-T Li et al.; Optical: NASA/STSc



99

1arcmin=1115px

Scale and power

Massive stars:

$$V_{\infty} \approx 10^2 - 10^3 \text{ km/s}$$

$$\dot{M} \lesssim 10^{-5} M_{\odot}/\text{yr}$$

Starbursts:

$$V_{\infty} \approx 10^3 \text{ km/s}$$

$$\dot{M} \approx 10^{-2} - 10^2 M_{\odot}/\text{yr}$$

Star clusters:

$$V_{\infty} \approx 10^3 \text{ km/s}$$

$$\dot{M} \approx 10^{-4} M_{\odot}/\text{yr}$$

M82 - Image credit: Daniel Nobre

2019 - Hubble

NGC3079 - Image credit: X-ray: NASA/CXC/University of Michigan/J-T Li et al.; Optical: NASA/STSc

Westerlund 2 - Image credit: NASA / ESA / Hubble Heritage Team / STScI / AURA / A. Nota / Westerlund 2 Science Team

100

1arcmin=1115px

WR31a- Image credit: f
Acknowledgement: Judy

NGC7635- Image credit: NASA Goddard Space Flight Center from Greenbelt, MD, USA

Scale and power

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AGN:

$$V_{\infty} \approx 10^2 - 10^5 \text{ km/s}$$
$$\dot{M} \approx 10^{-3} - 10^3 M_{\odot}/\text{yr}$$

M82 - Image credit: Daniel Nobre

WR31a - Image credit: [unclear]
Acknowledgement: Judy

Image credit: NASA/CXC/University
Image credit: NASA/STSc

Westerlund 2 - Image credit: NASA / ESA / Hubble Heritage
Team / STScI / AURA / A. Nota / Westerlund 2 Science Team

NGC7635 - Image credit: NASA Goddard Space
Flight Center from Greenbelt, MD, USA

101
1arcmin=1115px

Maximum Energy: a first guess

$$\lambda_D(E_{max}) \approx R_{sh}$$

$$D(E_{max})/U_1 \approx R_{sh}$$

$$\xi^{-1} R_L(E_{max})c/U_1 \approx R_{sh}$$

$$\xi^{-1} E_{max}c/qBU_1 \approx R_{sh}$$

Maximum Energy: a first guess

$$E_{max} \approx \xi q B \frac{u_1}{c} R_{sh}$$

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$$E_{max} \approx \xi q B \frac{u_1}{c} R_{sh}$$

$$U_B = \epsilon_B P_{ram} = \epsilon_B \frac{\dot{M}}{4\pi R_{sh}^2} u_1$$

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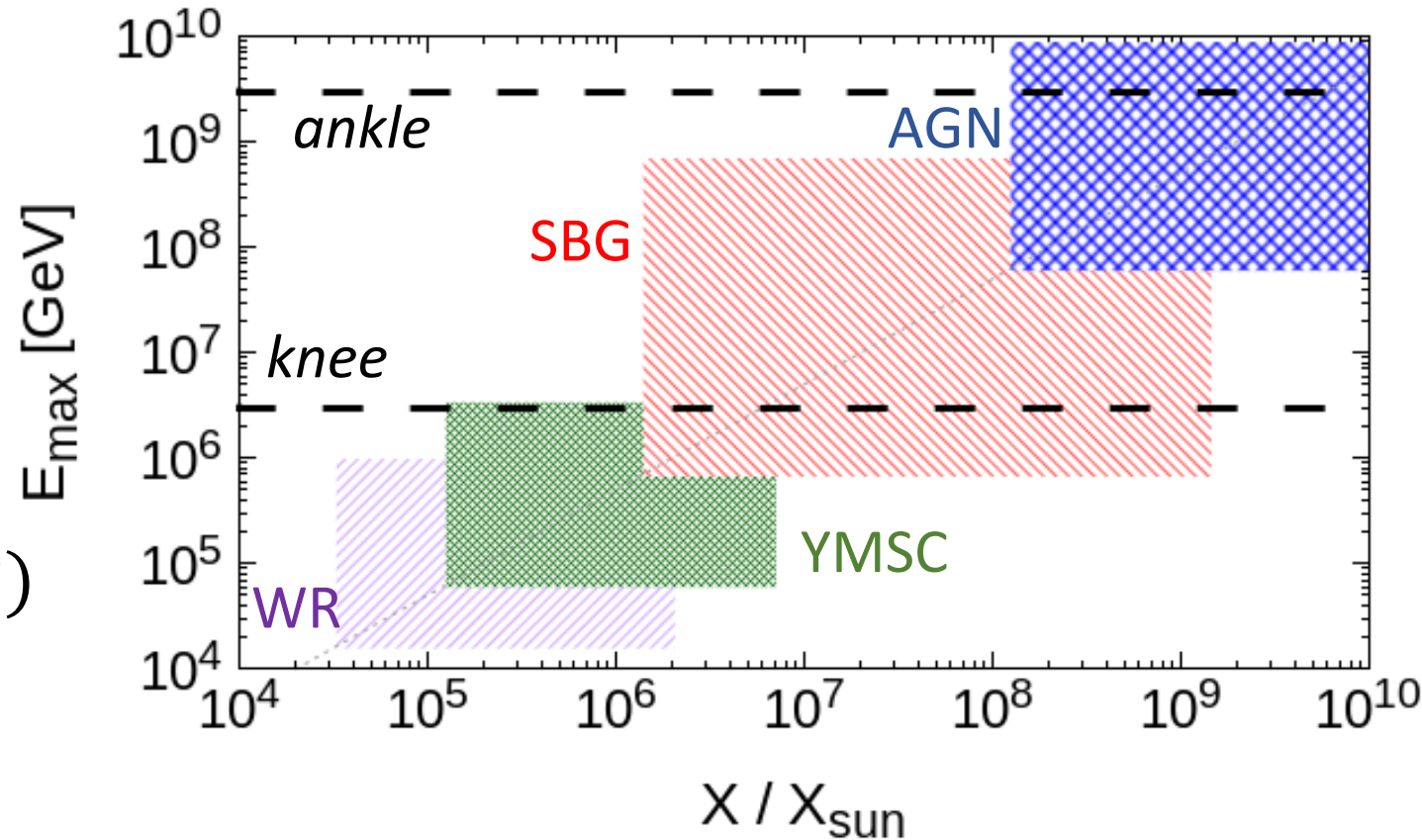
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$$E_{max} = E_{max}(u_1, \dot{M}) = E_{max}(\dot{E}, \dot{P})$$

$$X = \dot{E} \dot{P}^{-1/2}$$



Diverging flows as cosmic-ray sources

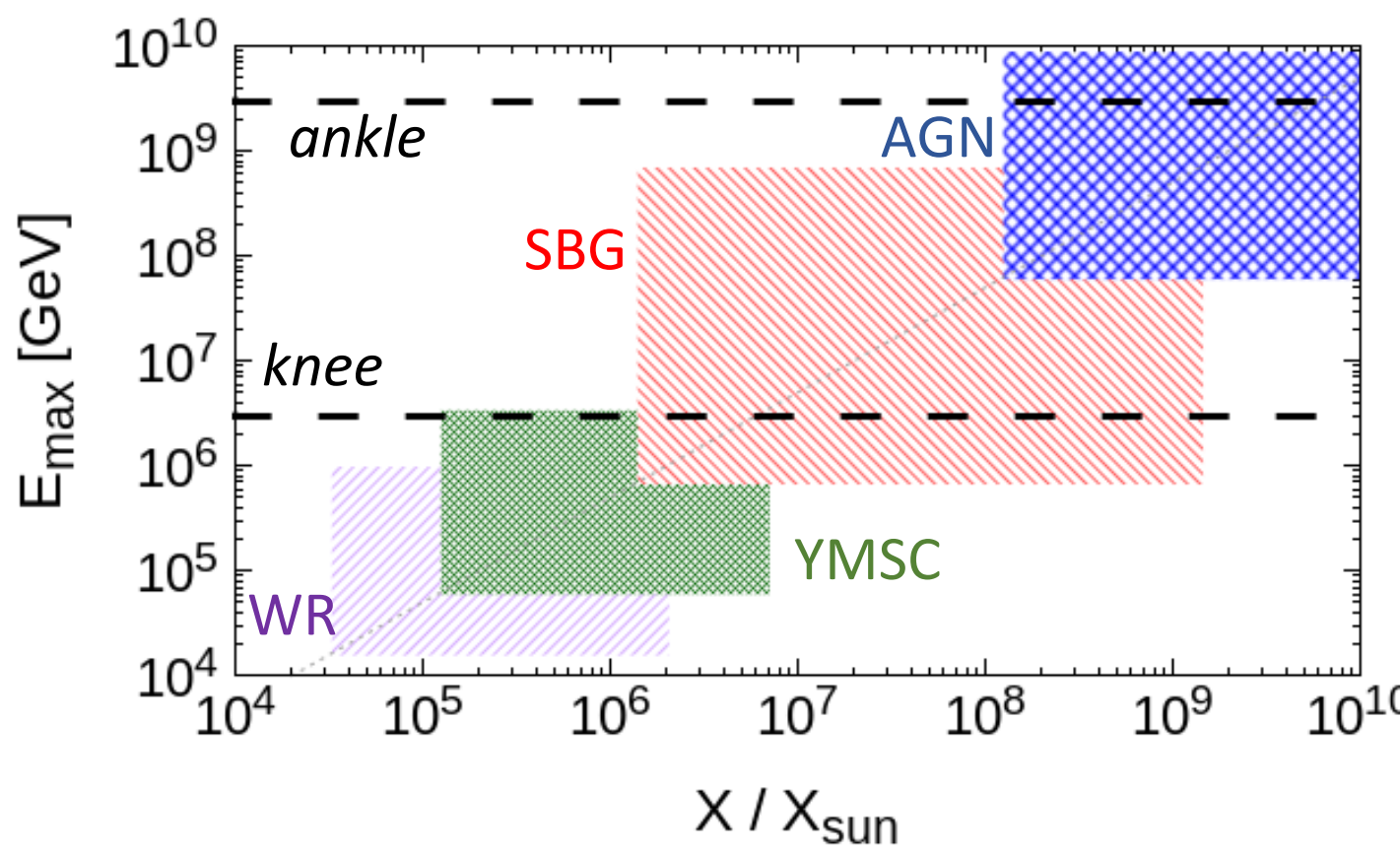
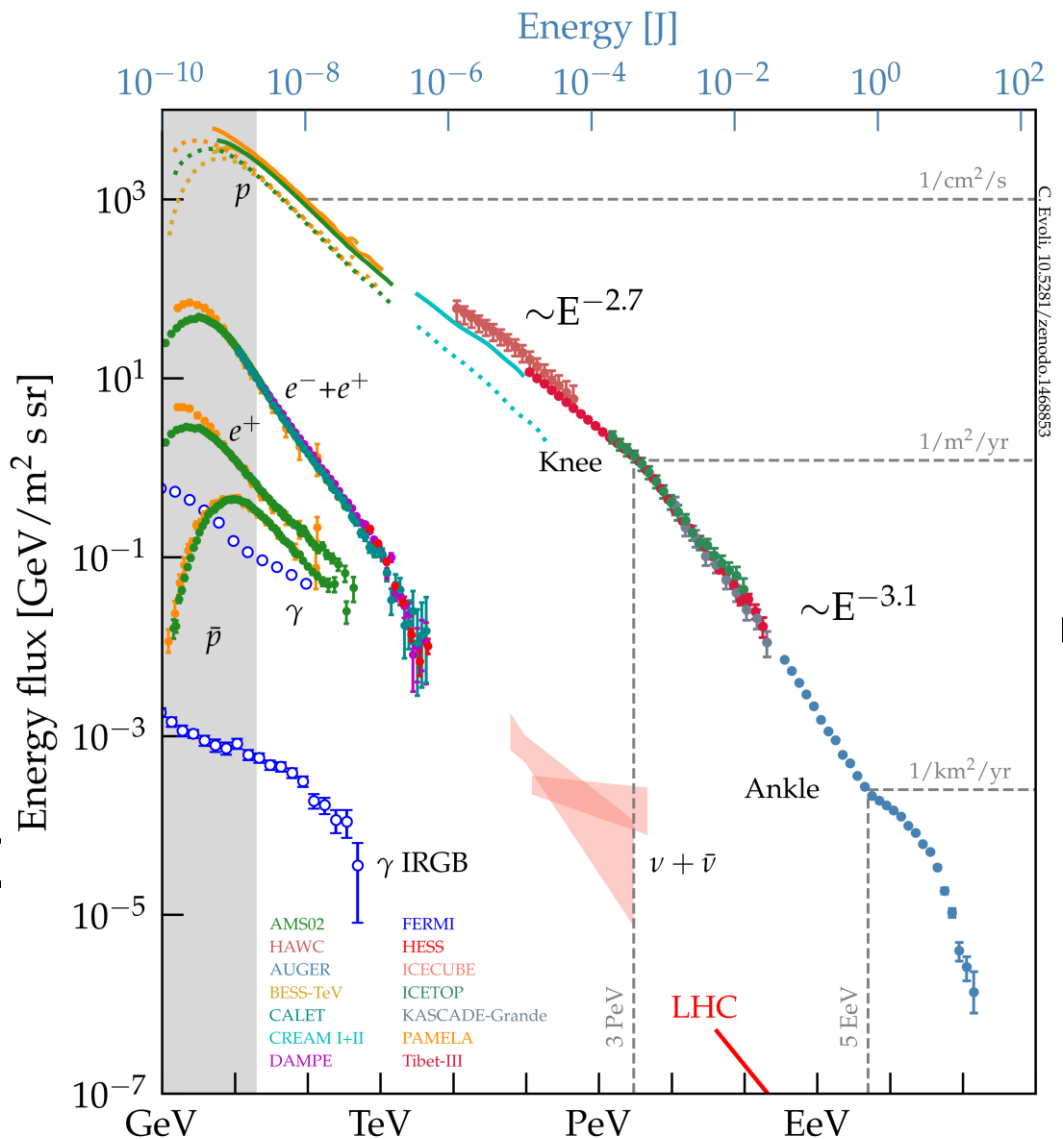
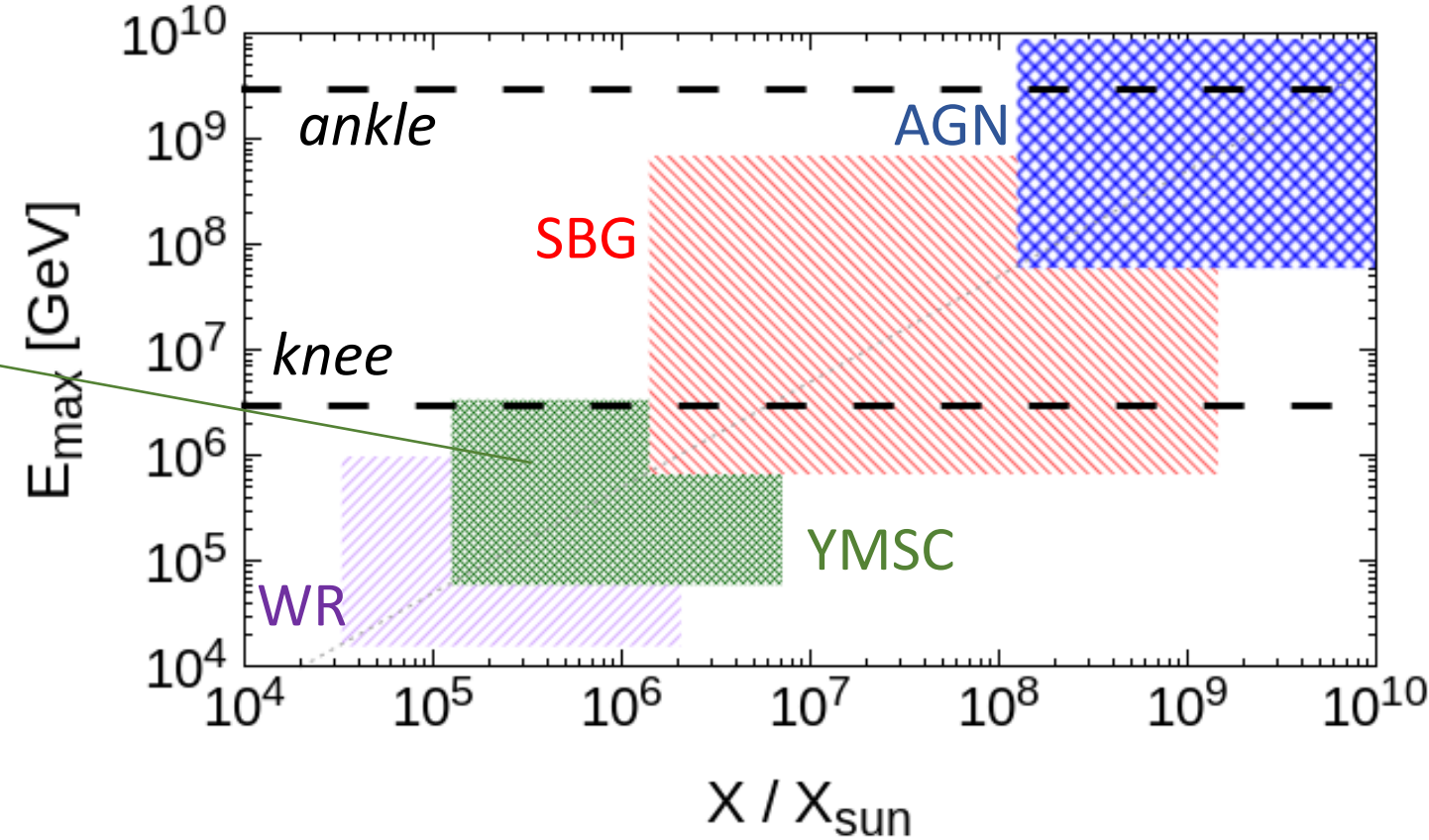
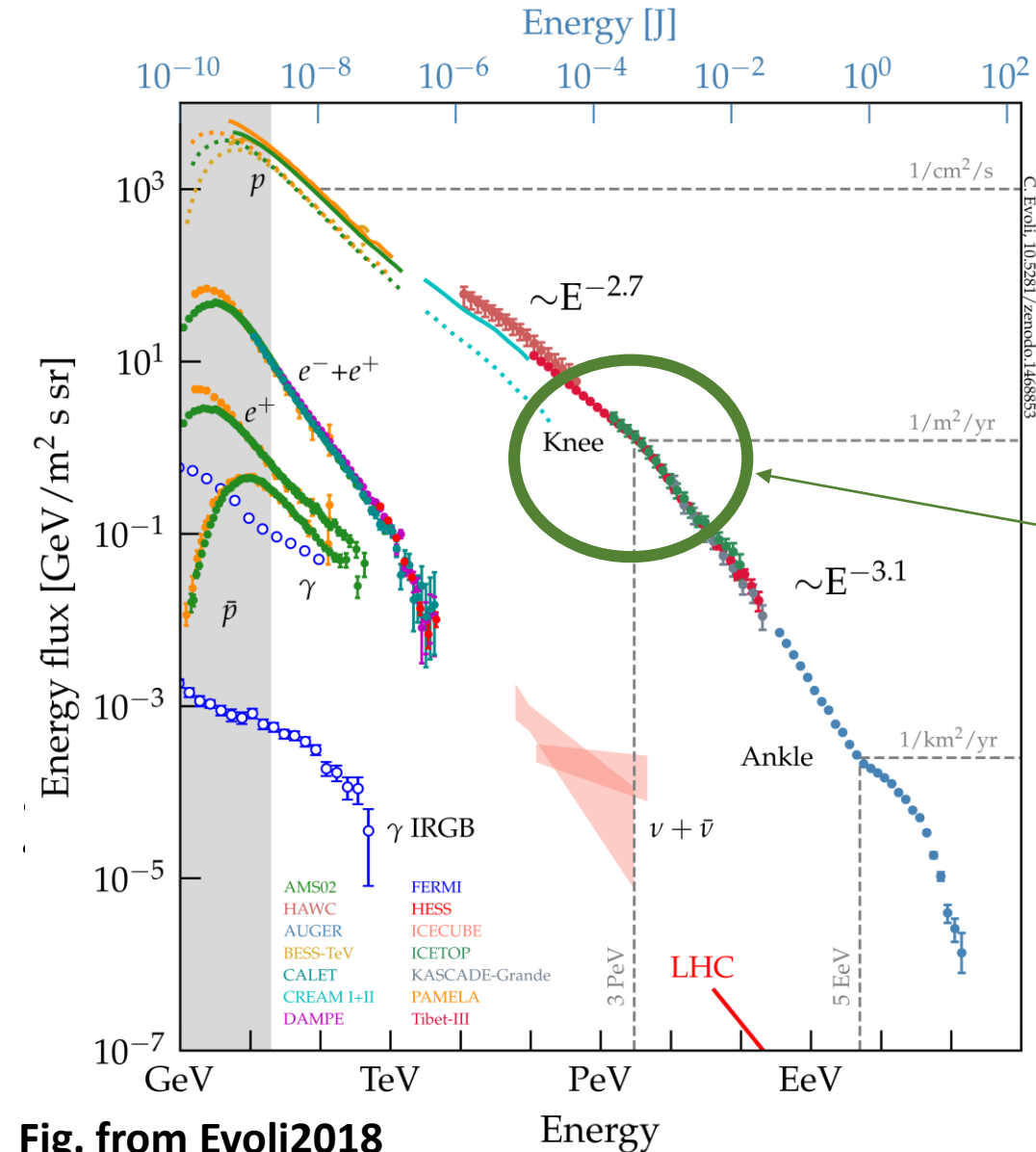
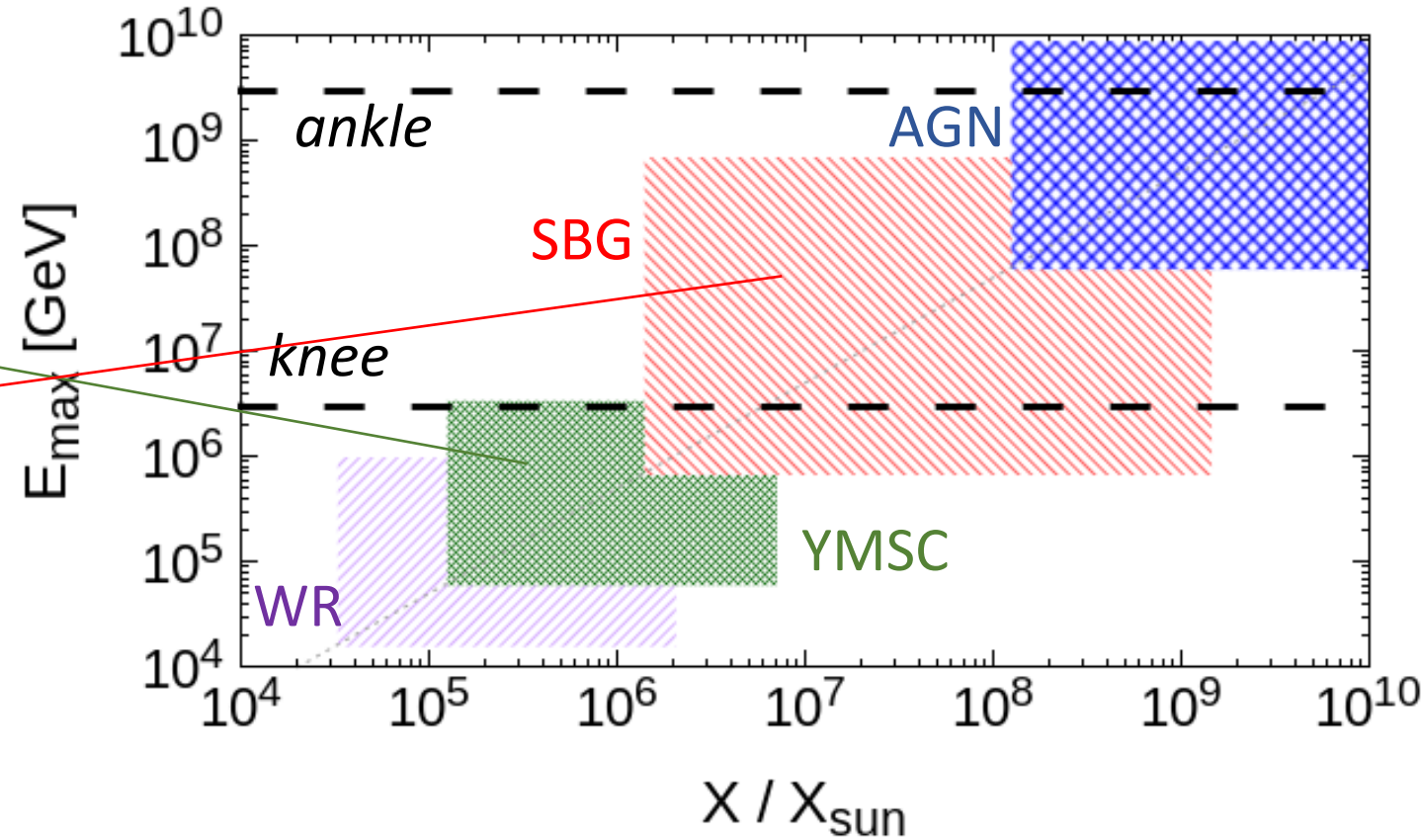
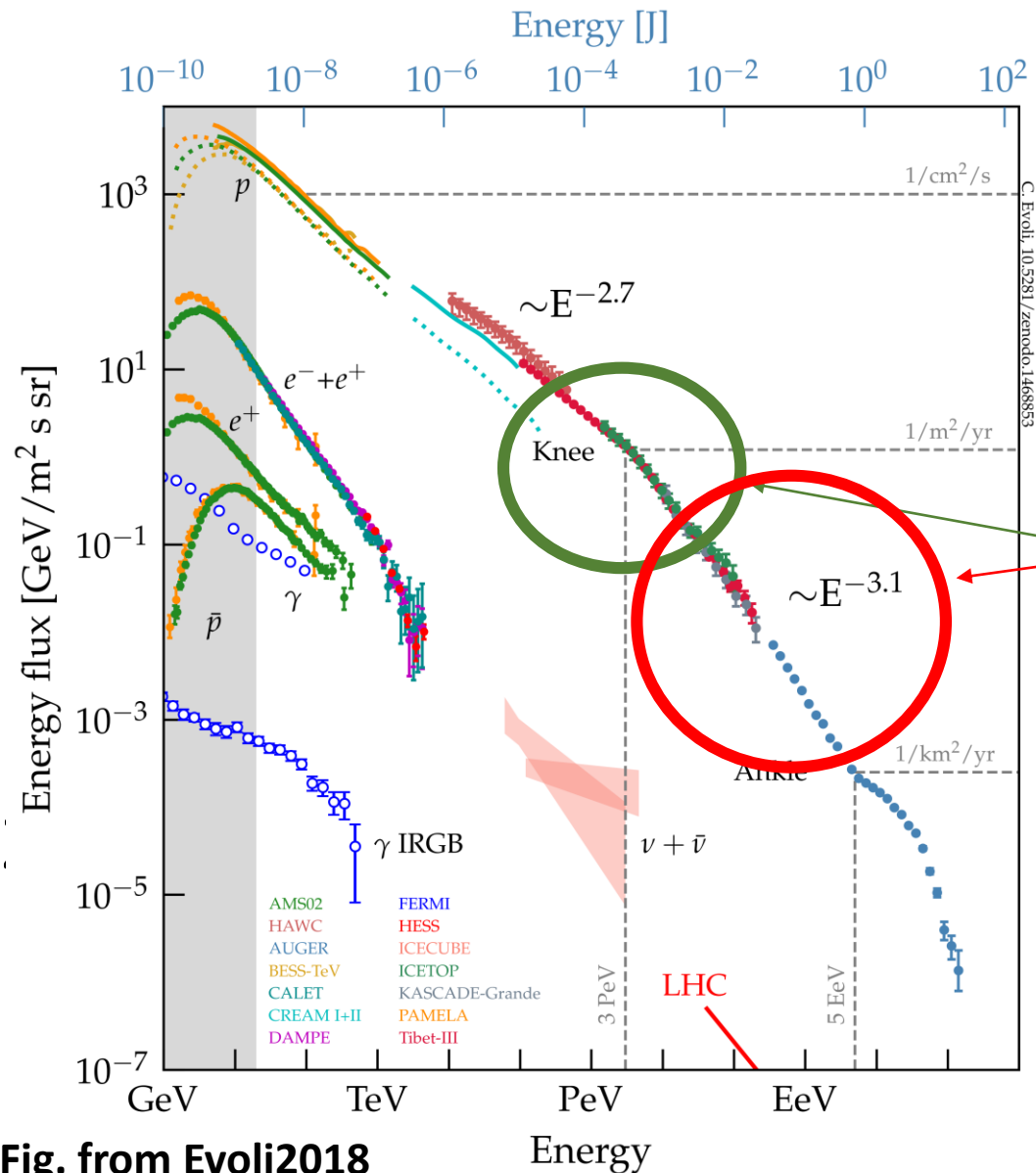


Fig. from Evoli2018

Diverging flows as cosmic-ray sources



Diverging flows as cosmic-ray sources



Diverging flows as cosmic-ray sources

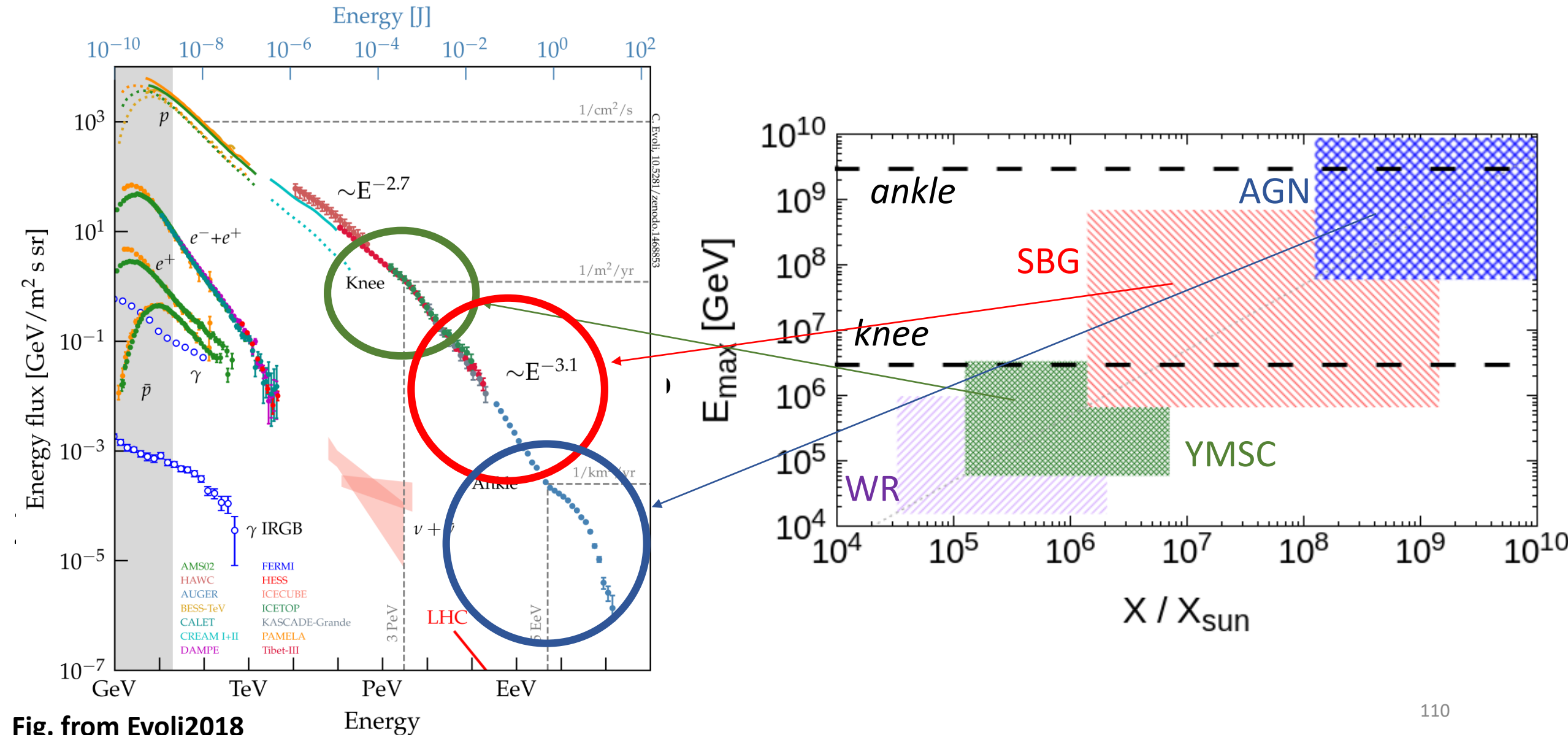


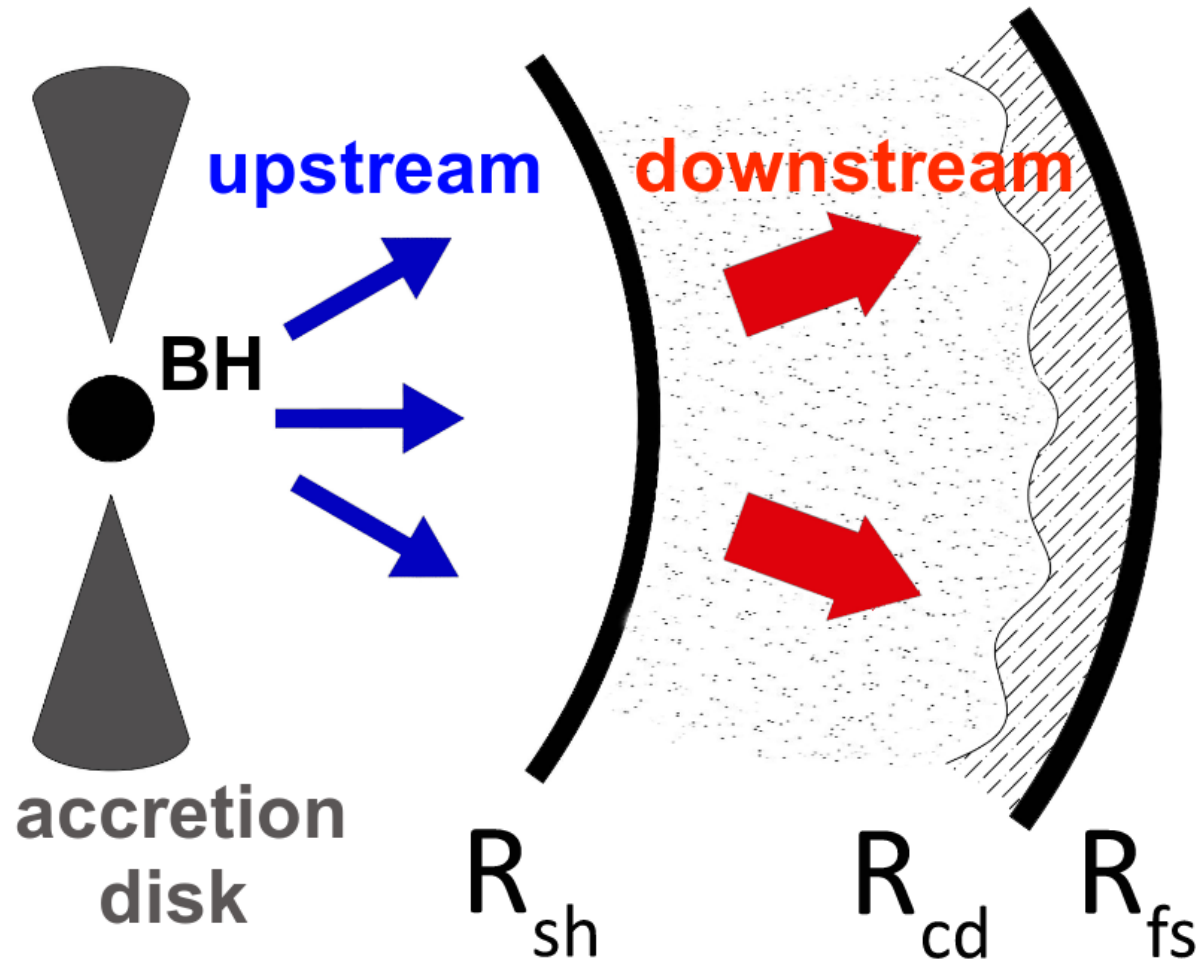
Fig. from Evoli2018

Outline

- Transport equation of Cosmic Rays
- Transport approach to diffusive shock acceleration
 - Wind blown bubbles
- Modeling acceleration and multi-messenger radiation

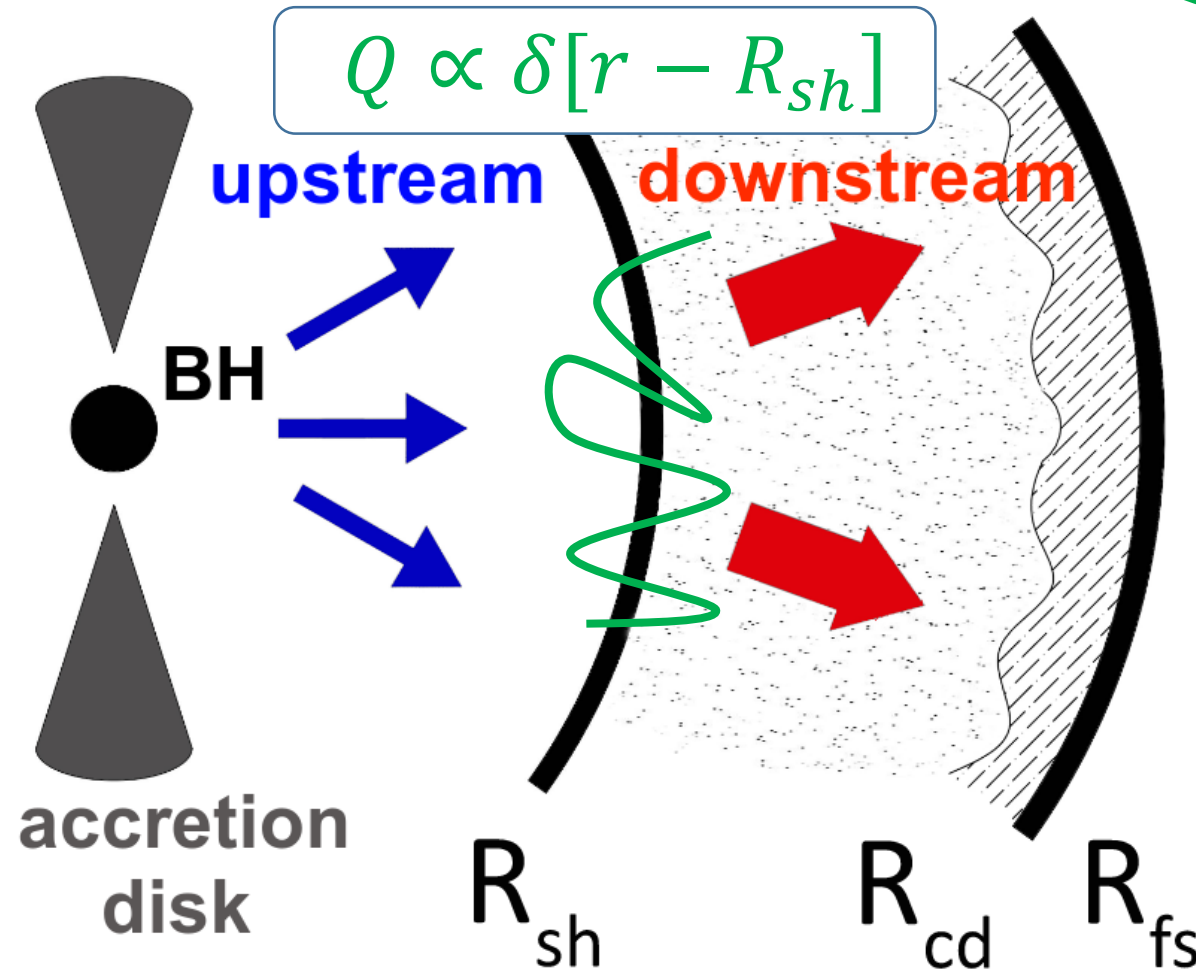
Acceleration and transport model

$$r^2 u(r) \partial_r f = \partial_r [r^2 D(r, p) \partial_r f] + \frac{1}{3} \partial_r [r^2 u(r)] p \partial_p f + r^2 Q(r, p) - r^2 \Lambda(r, p)$$



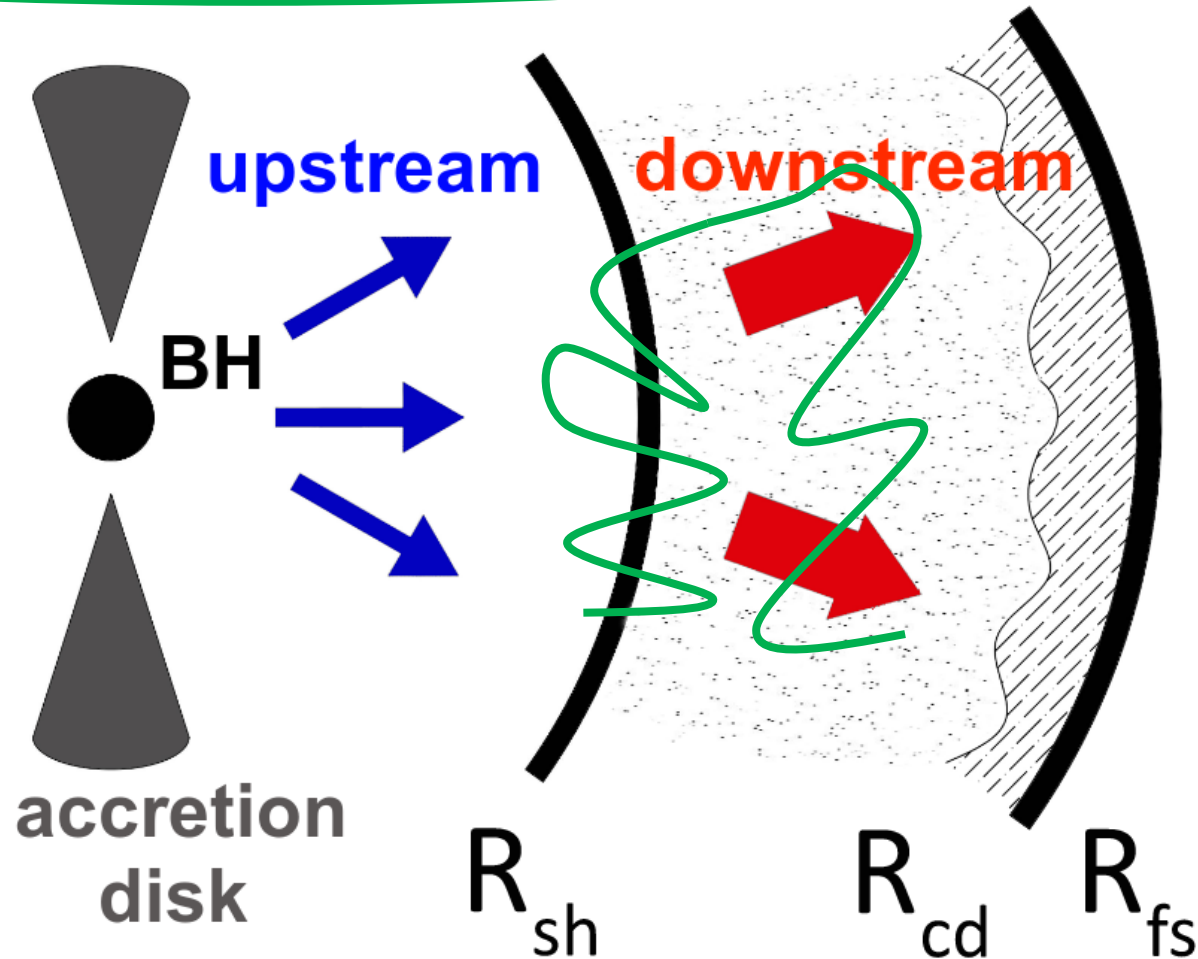
Acceleration and transport model

$$r^2 u(r) \partial_r f = \partial_r [r^2 D(r, p) \partial_r f] + \frac{1}{3} \partial_r [r^2 u(r)] p \partial_p f + r^2 Q(r, p) - r^2 \Lambda(r, p)$$



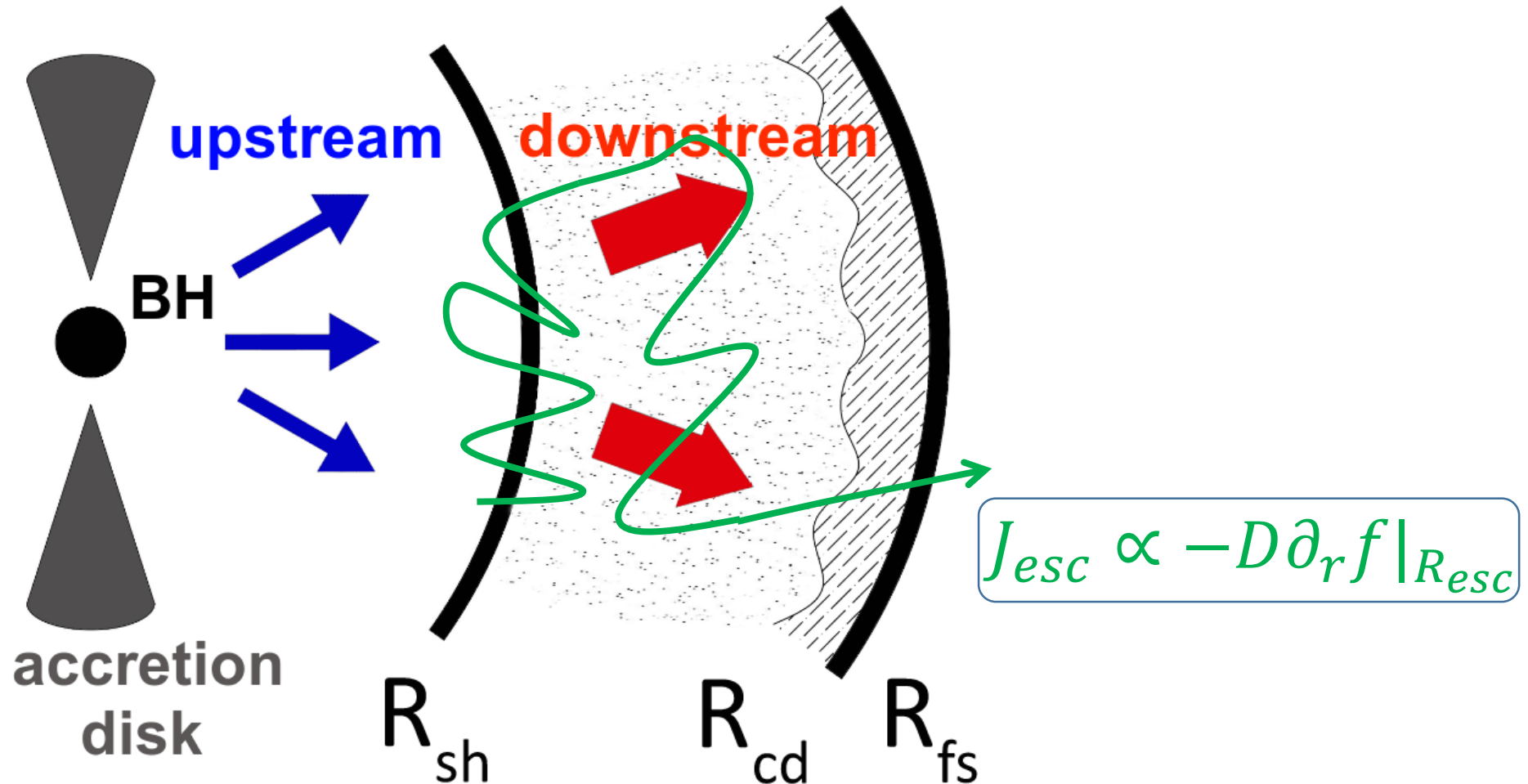
Acceleration and transport model

$$r^2 u(r) \partial_r f = \partial_r [r^2 D(r, p) \partial_r f] + \frac{1}{3} \partial_r [r^2 u(r)] p \partial_p f + r^2 Q(r, p) - r^2 \Lambda(r, p)$$



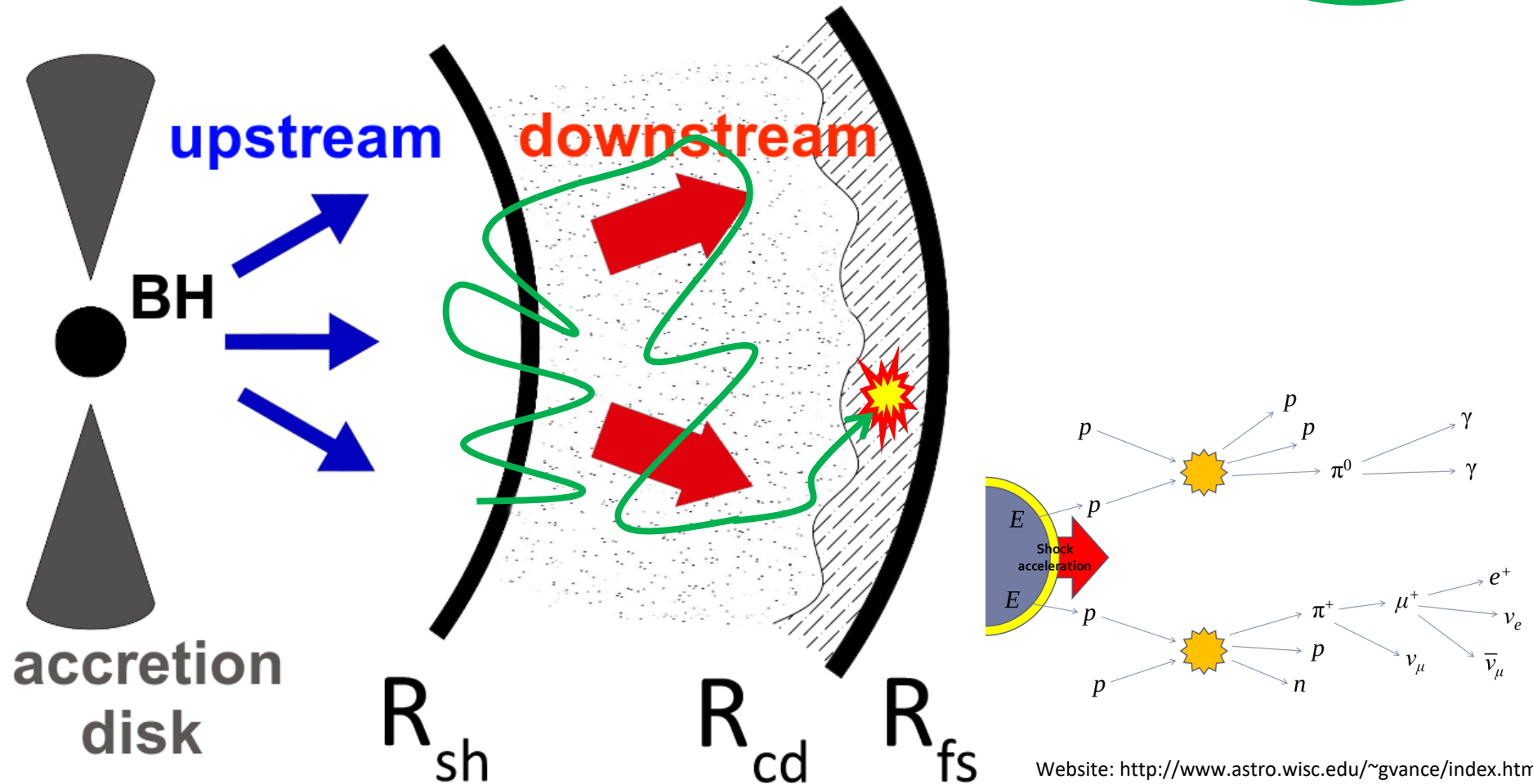
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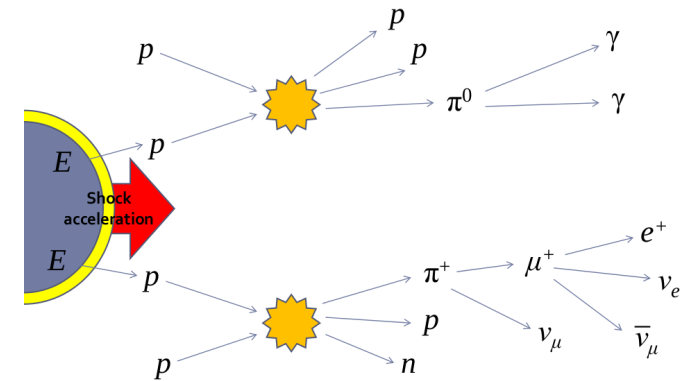
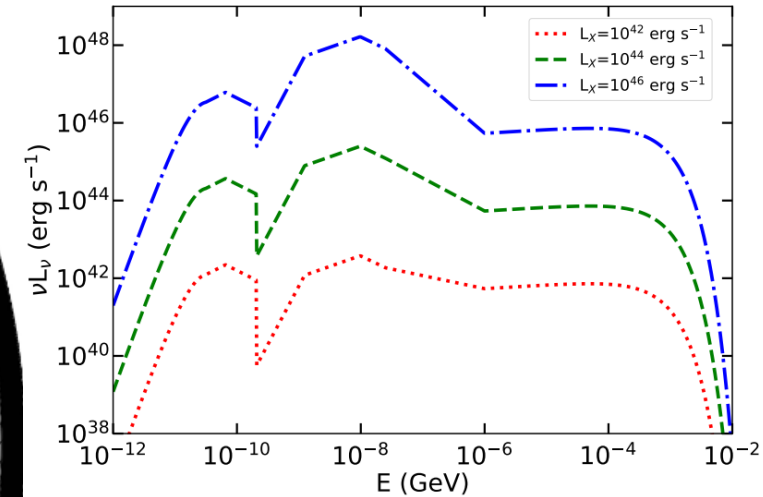
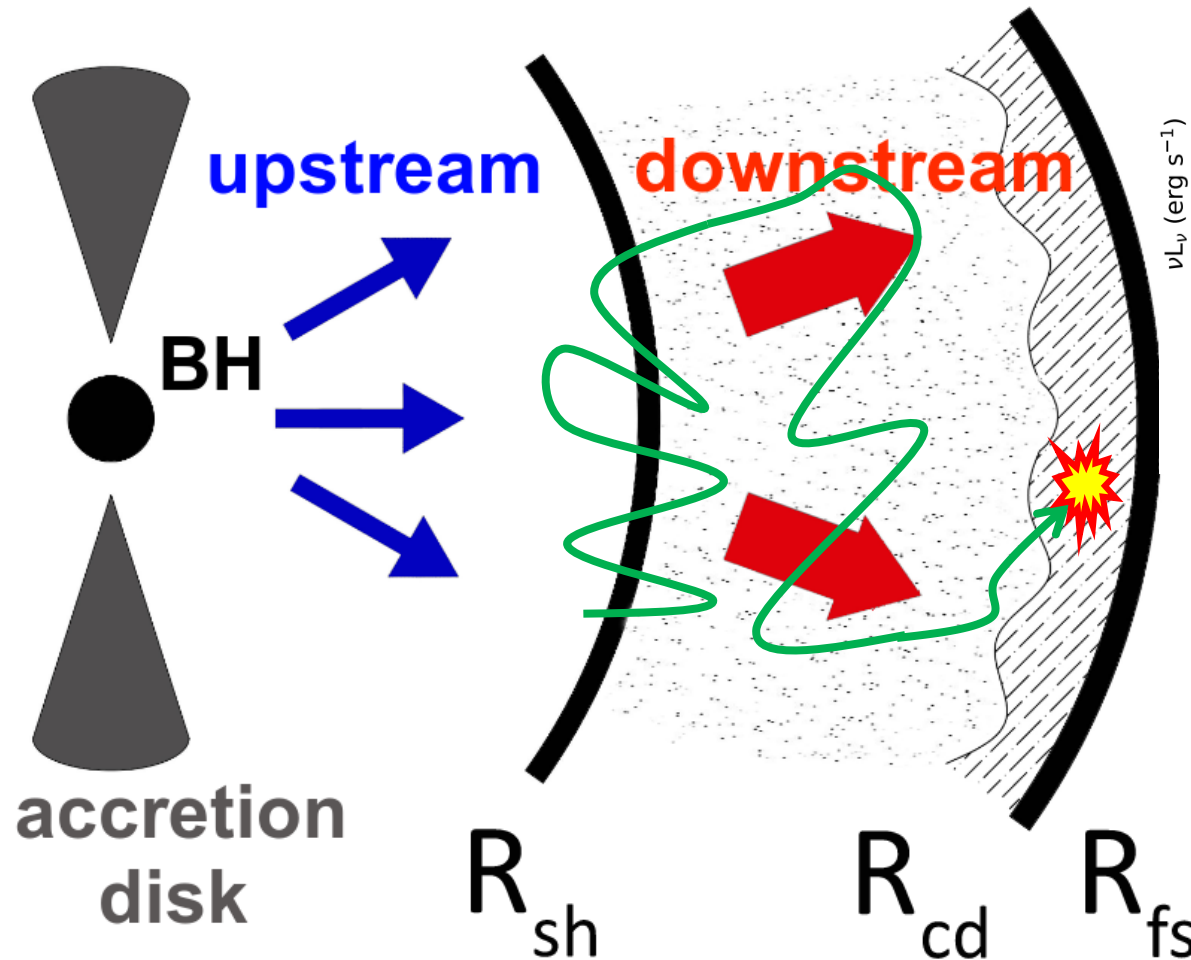
Acceleration and transport model

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Acceleration and transport model

$$r^2 u(r) \partial_r f = \partial_r [r^2 D(r, p) \partial_r f] + \frac{1}{3} \partial_r [r^2 u(r)] p \partial_p f + r^2 Q(r, p) - r^2 \Lambda(r, p)$$



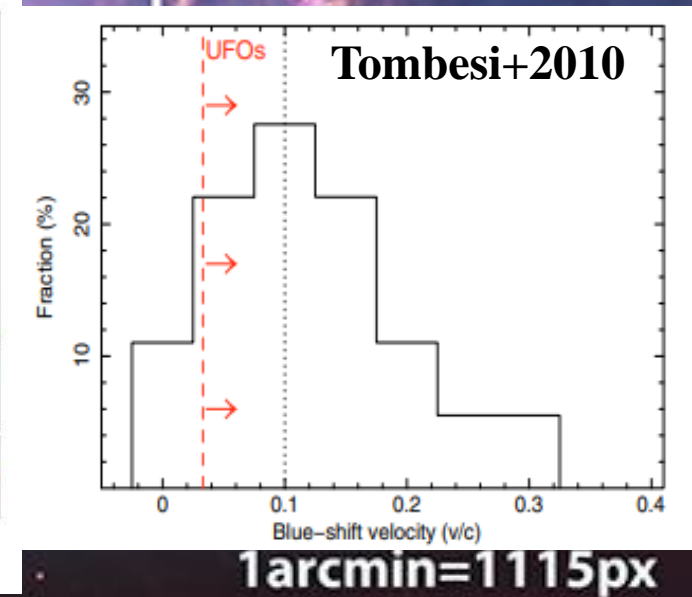
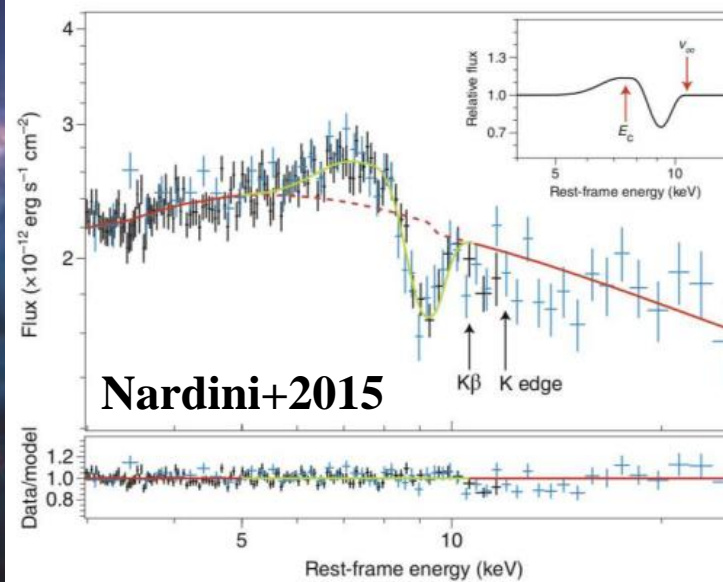
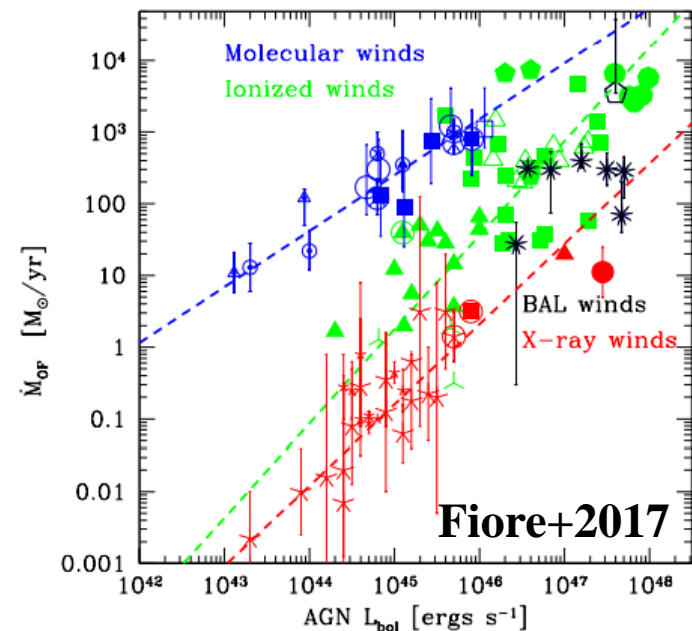
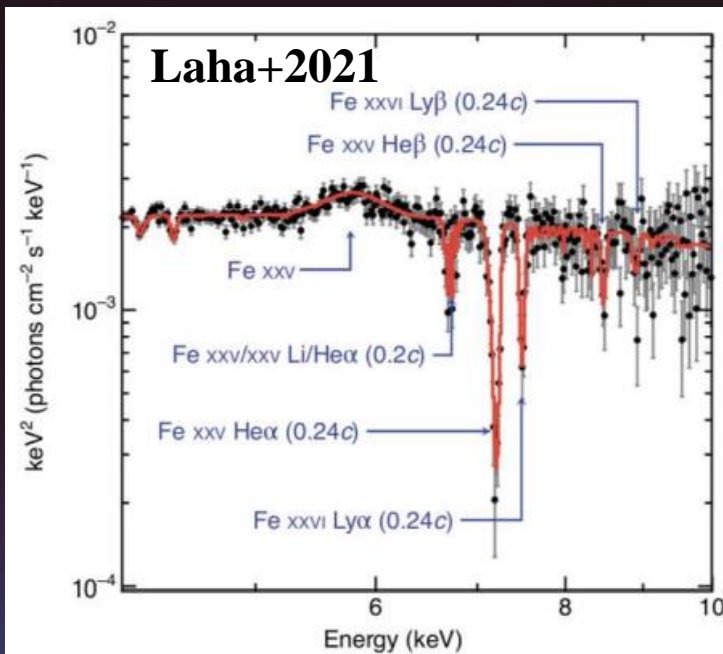
AGN-driven wind bubbles (UFOs)



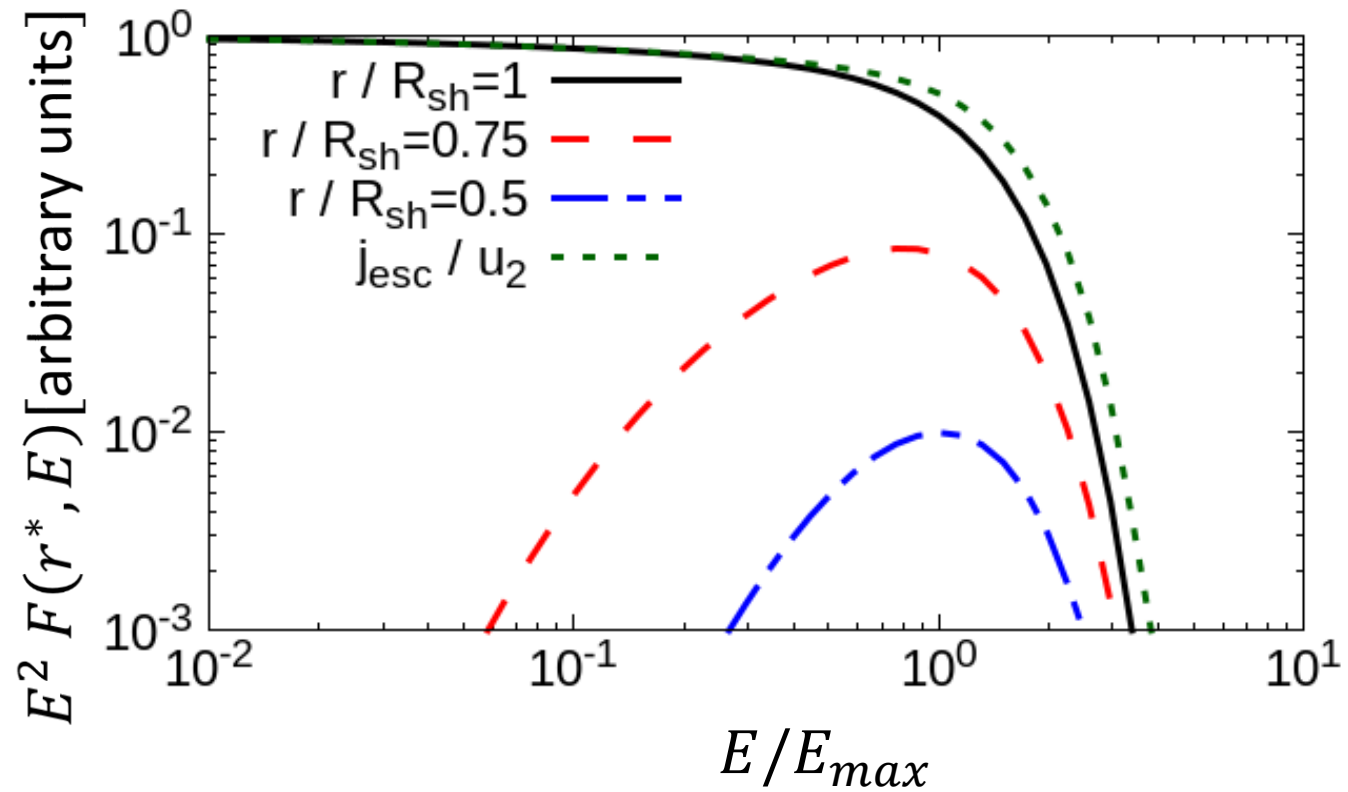
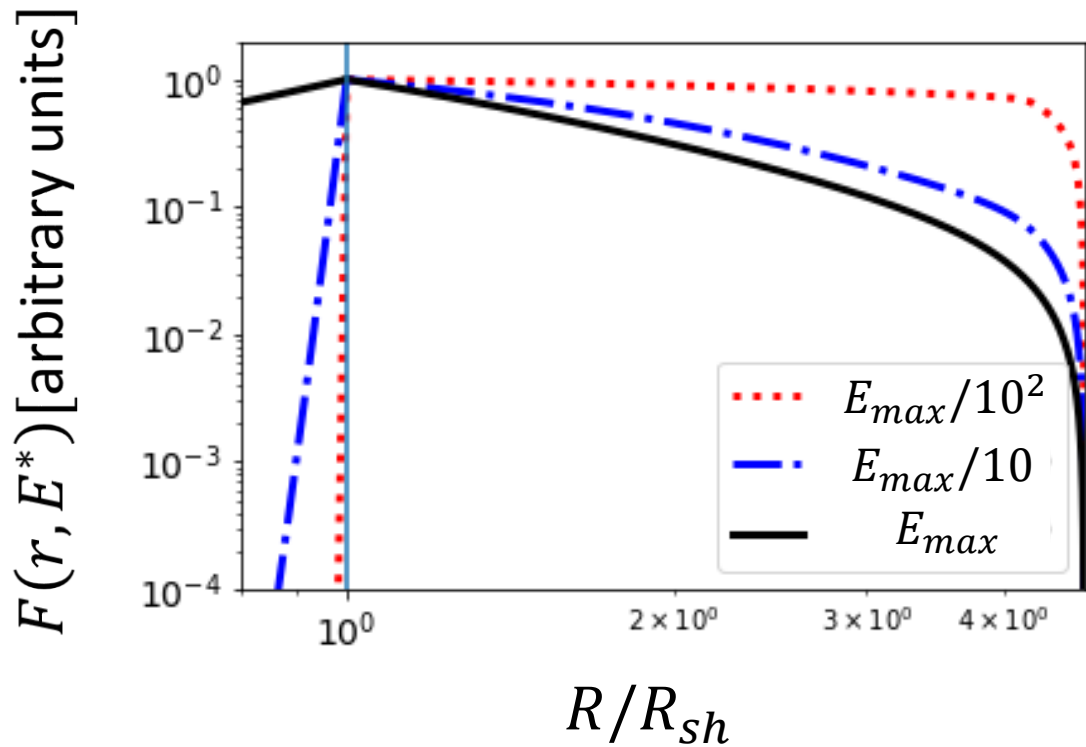
1 arcmin = 1115 px

Ultra-Fast Outflows (UFOs)

- Dist. scale = $10^{-4} - 10$ pc
- $v \approx 0.03 c - 0.3 c$
- $\Omega \gtrsim 3\pi$ sr
- $\dot{M} \approx 10^{-3} - 10 M_{\odot} \text{yr}^{-1}$

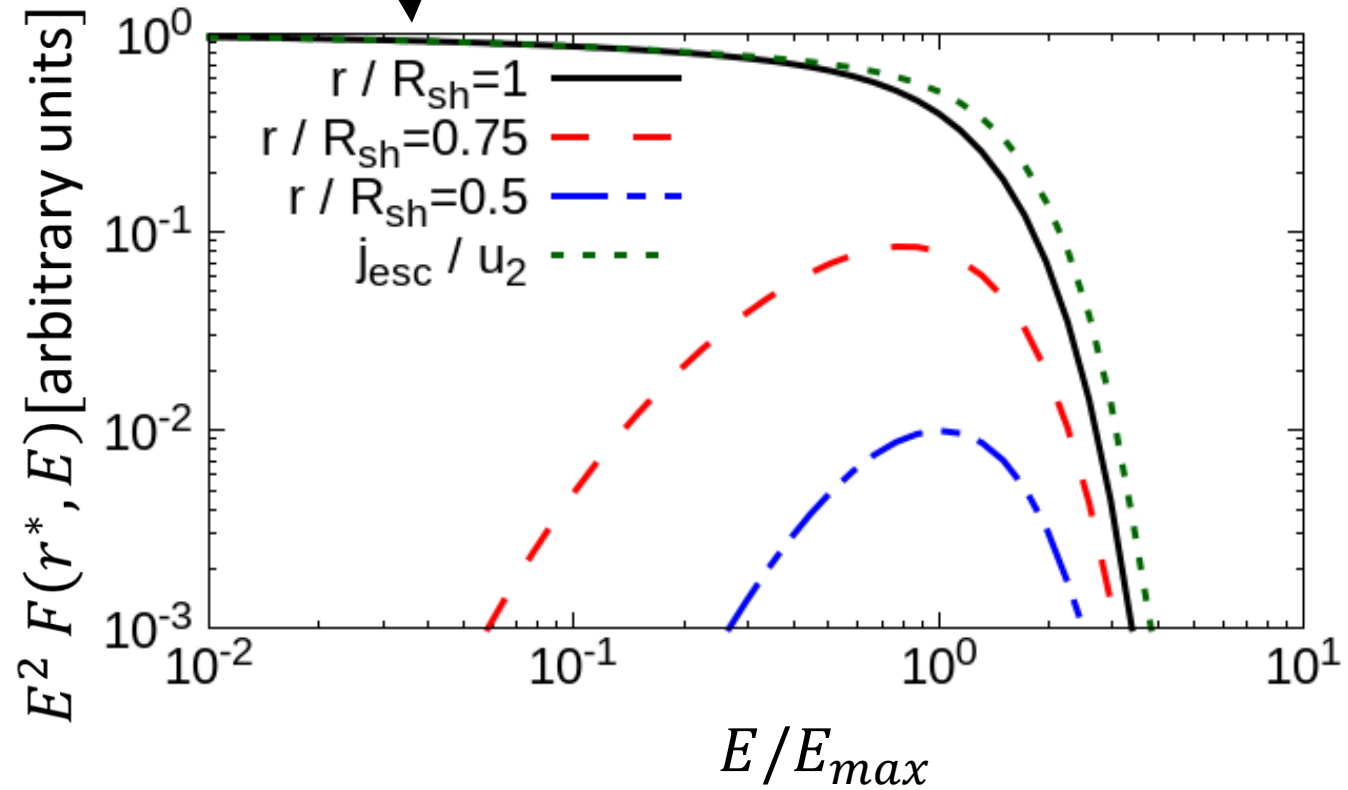
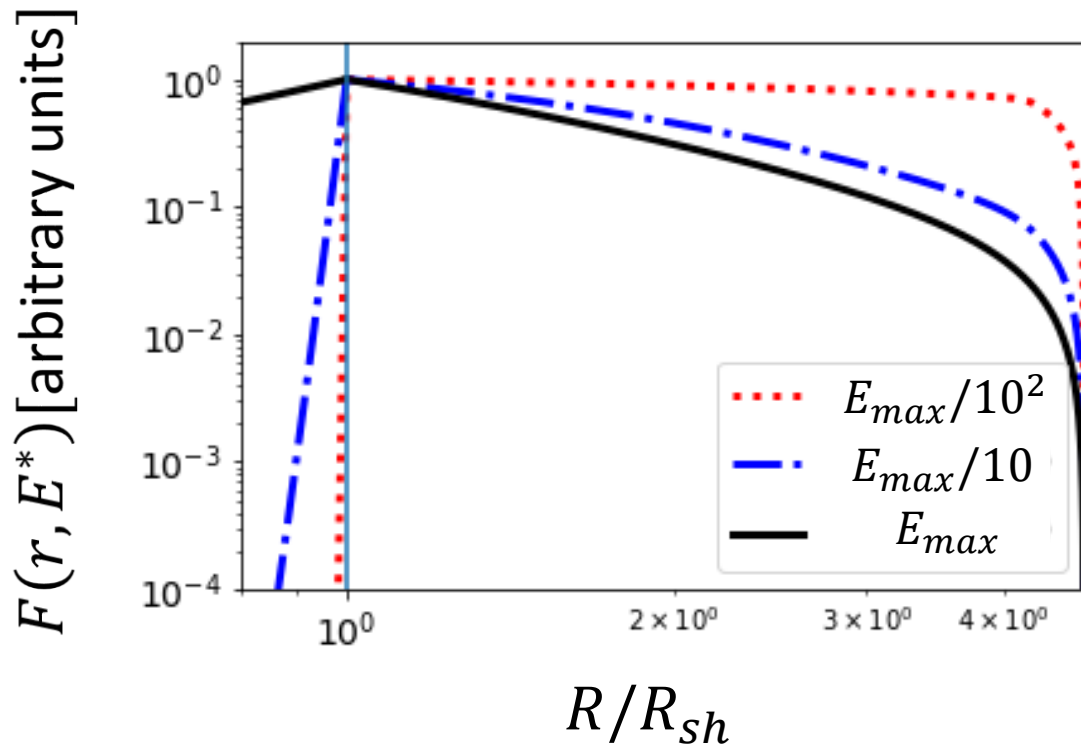


Solution: radial behavior and spectra



Solution: radial behavior and spectra

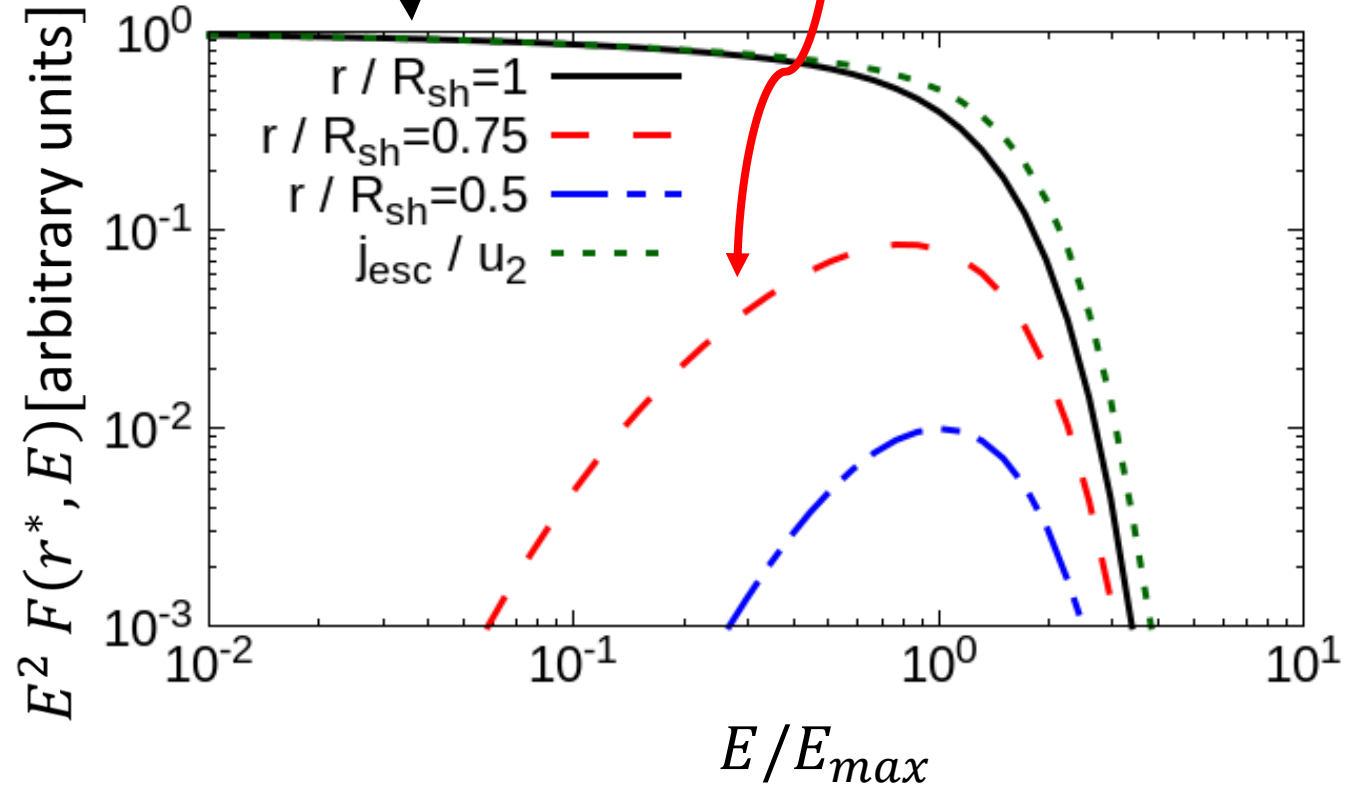
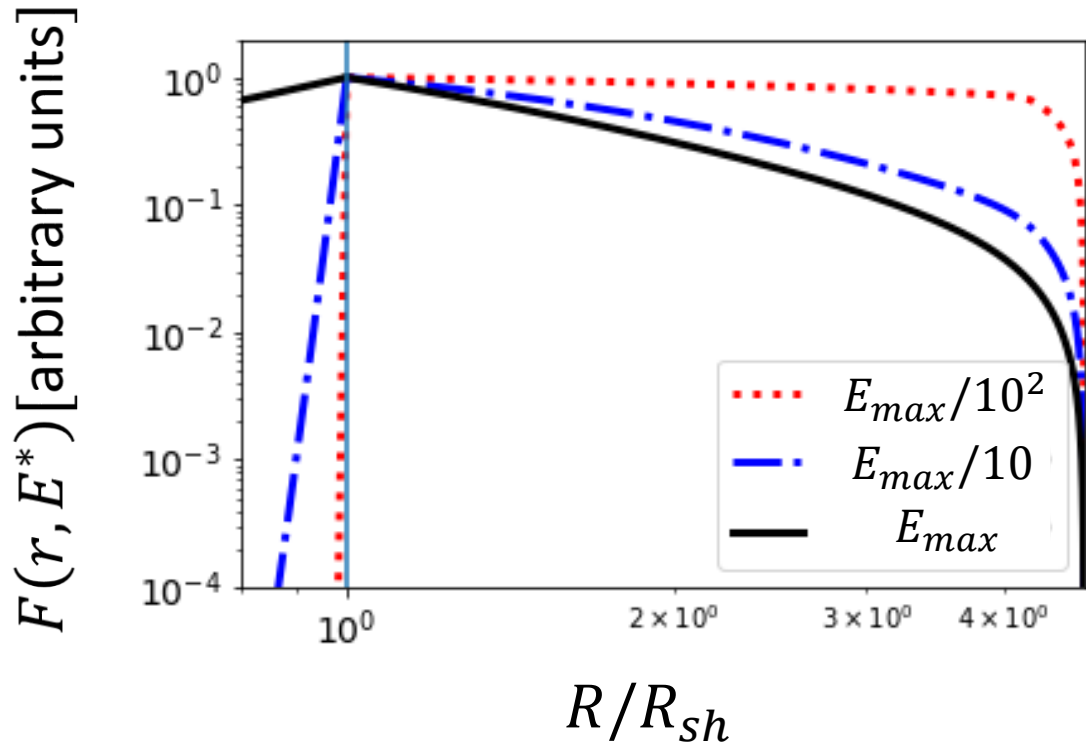
Solution at the shock



Solution: radial behavior and spectra

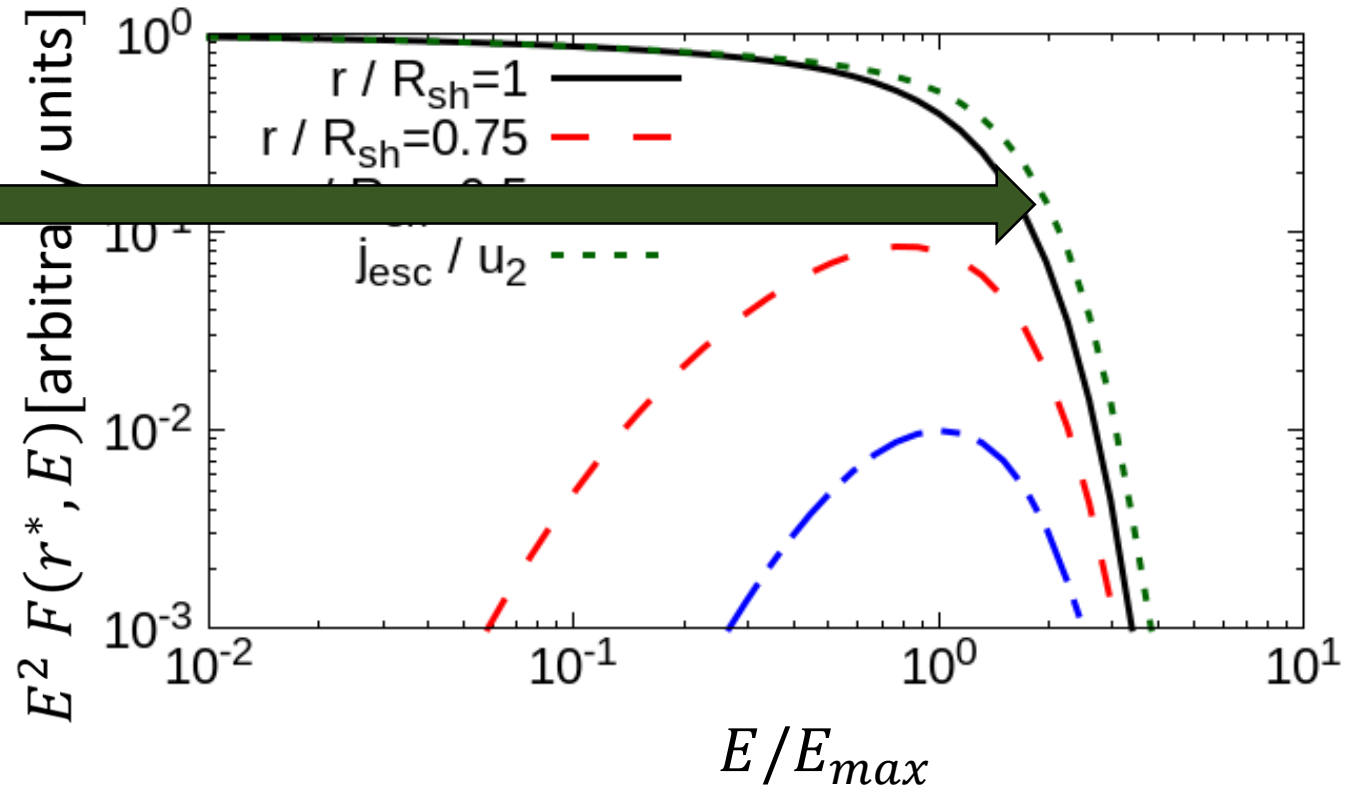
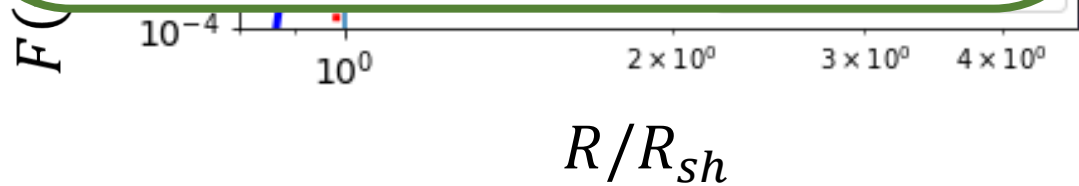
Solution at the shock

Upstream spectrum

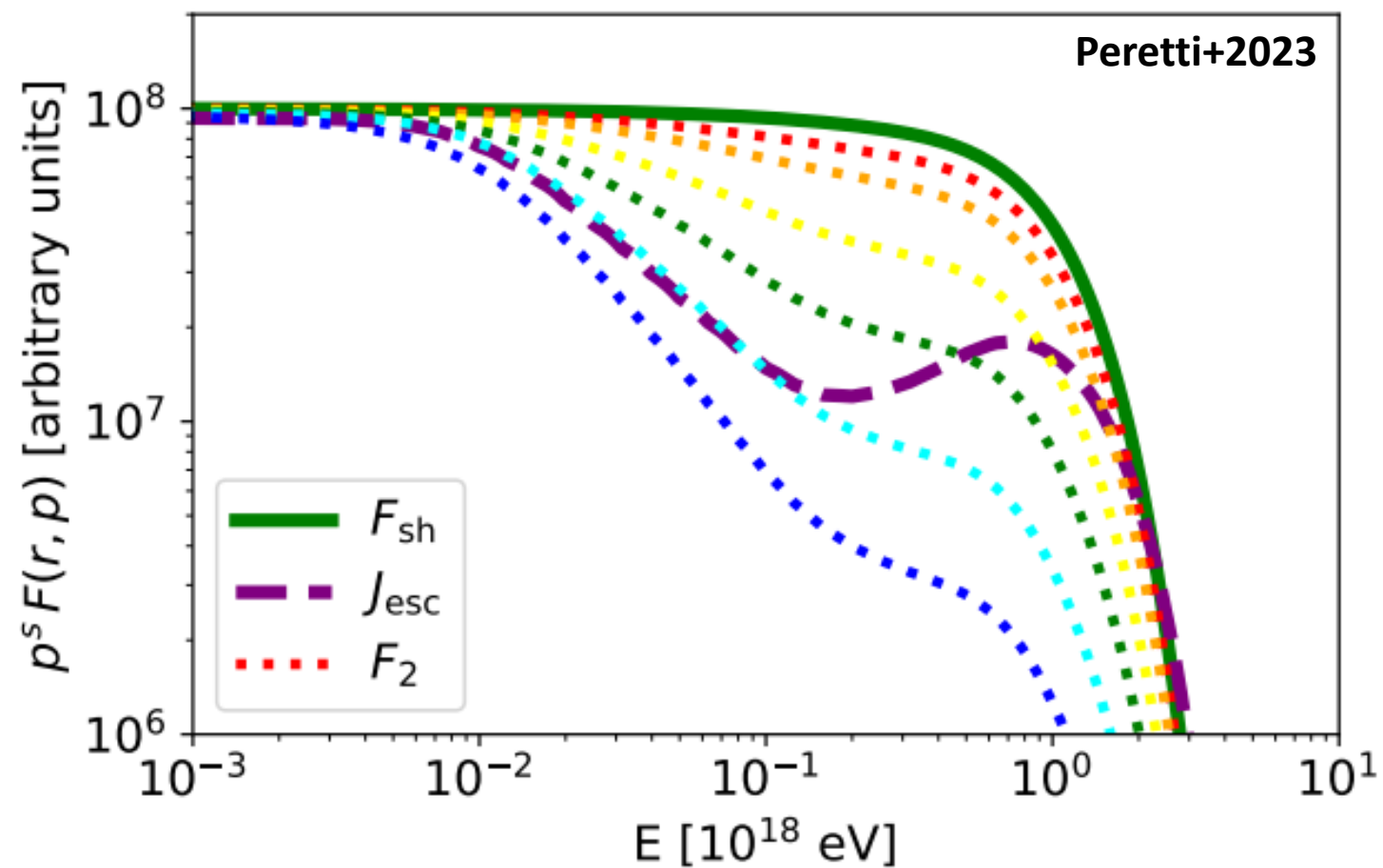


Solution: radial behavior and spectra

Negligible energy losses result in no relevant difference between the spectrum at the shock and the escaping flux

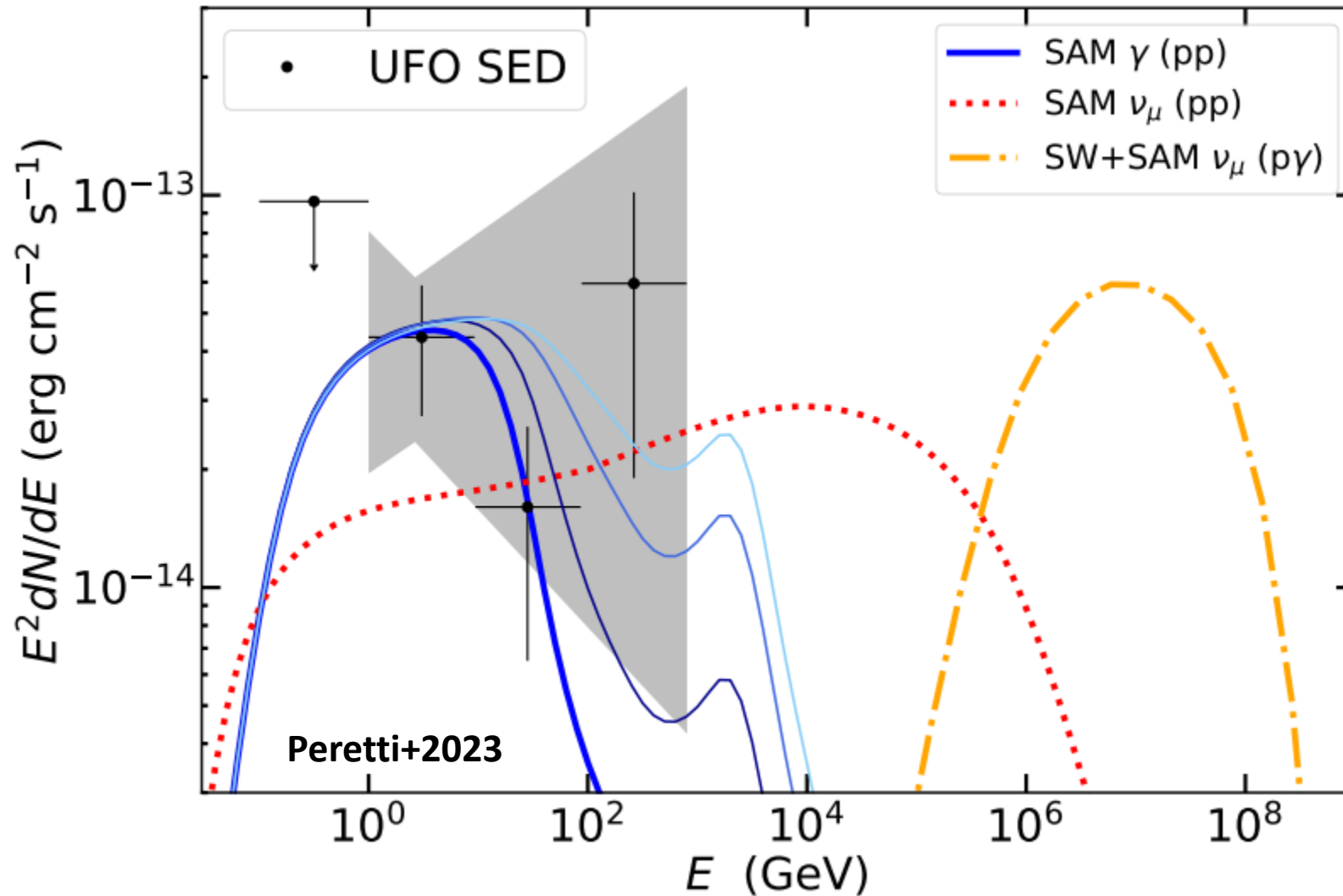


The prototype UFO



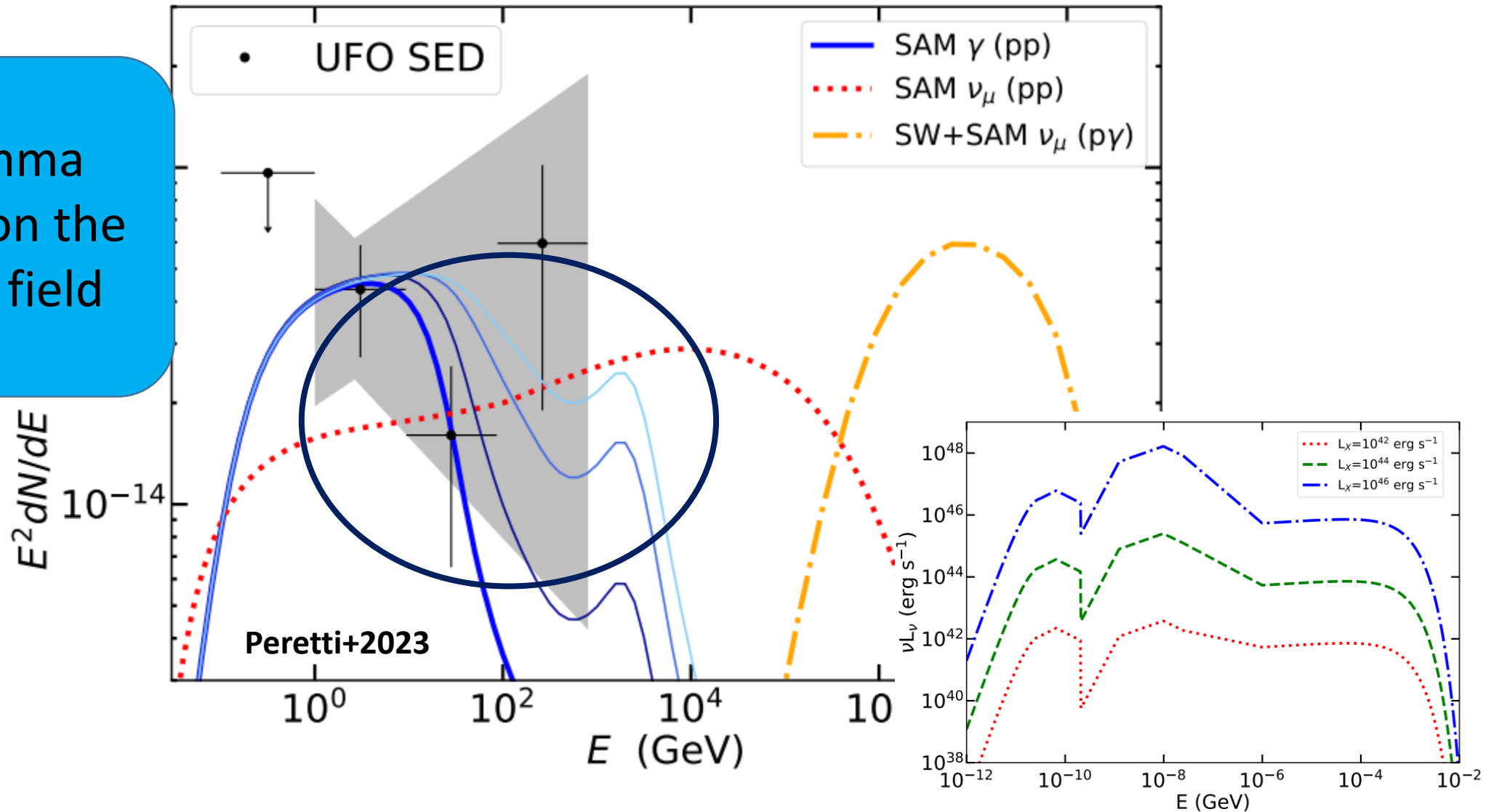
Parameter	benchmark
u_1/c	0.2
\dot{M} [$M_{\odot} \text{ yr}^{-1}$]	10^{-1}
ξ_{CR}	0.05
ϵ_{B}	0.05
l_c [pc]	10^{-2}
δ	3/2
L_X [erg s^{-1}]	10^{44}
n_{ISM} [cm^{-3}]	10^4
t_{age} [yr]	10^3

UFO model applied to Fermi-LAT results



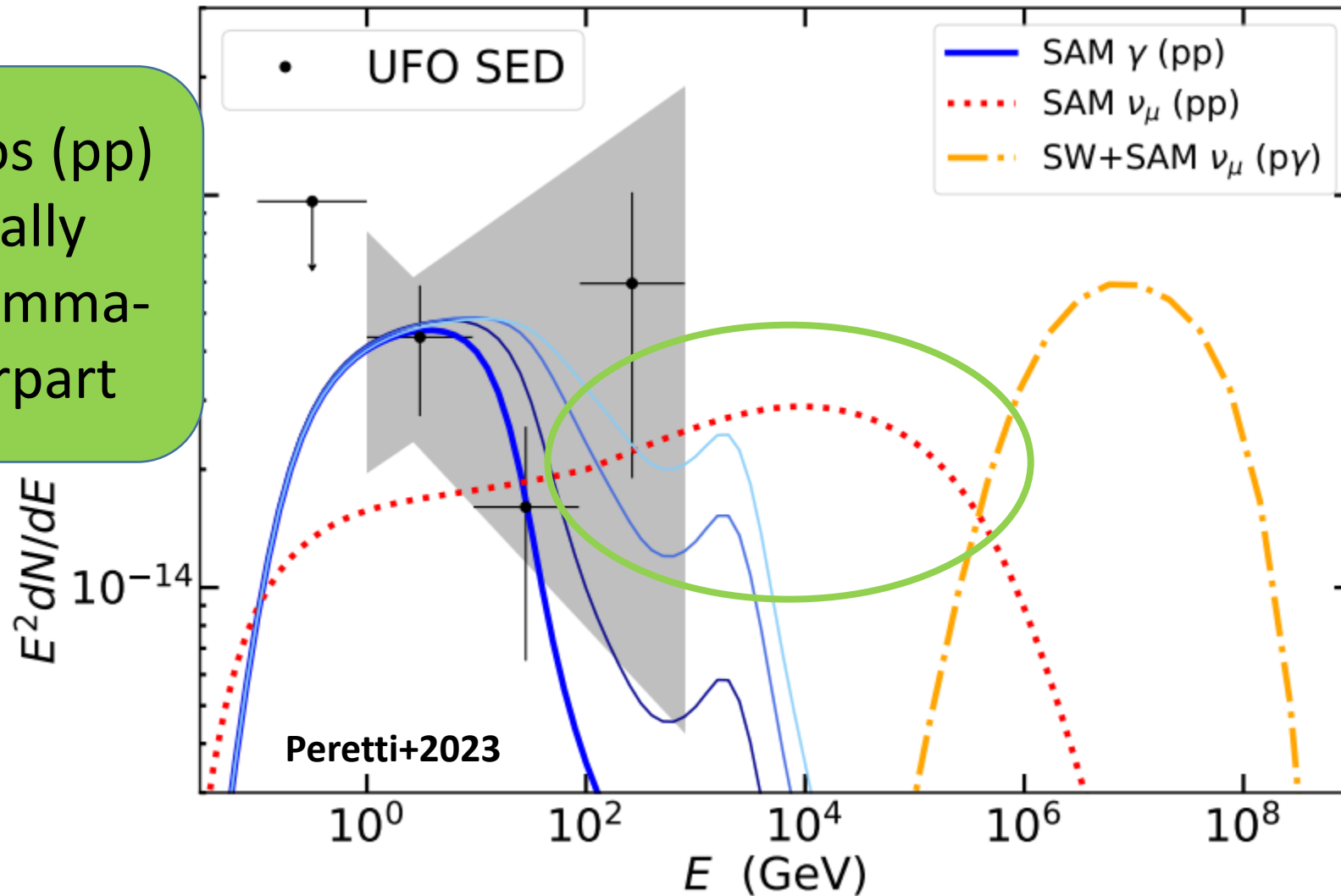
UFO model applied to Fermi-LAT results

Gamma-gamma absorption on the BKG photon field



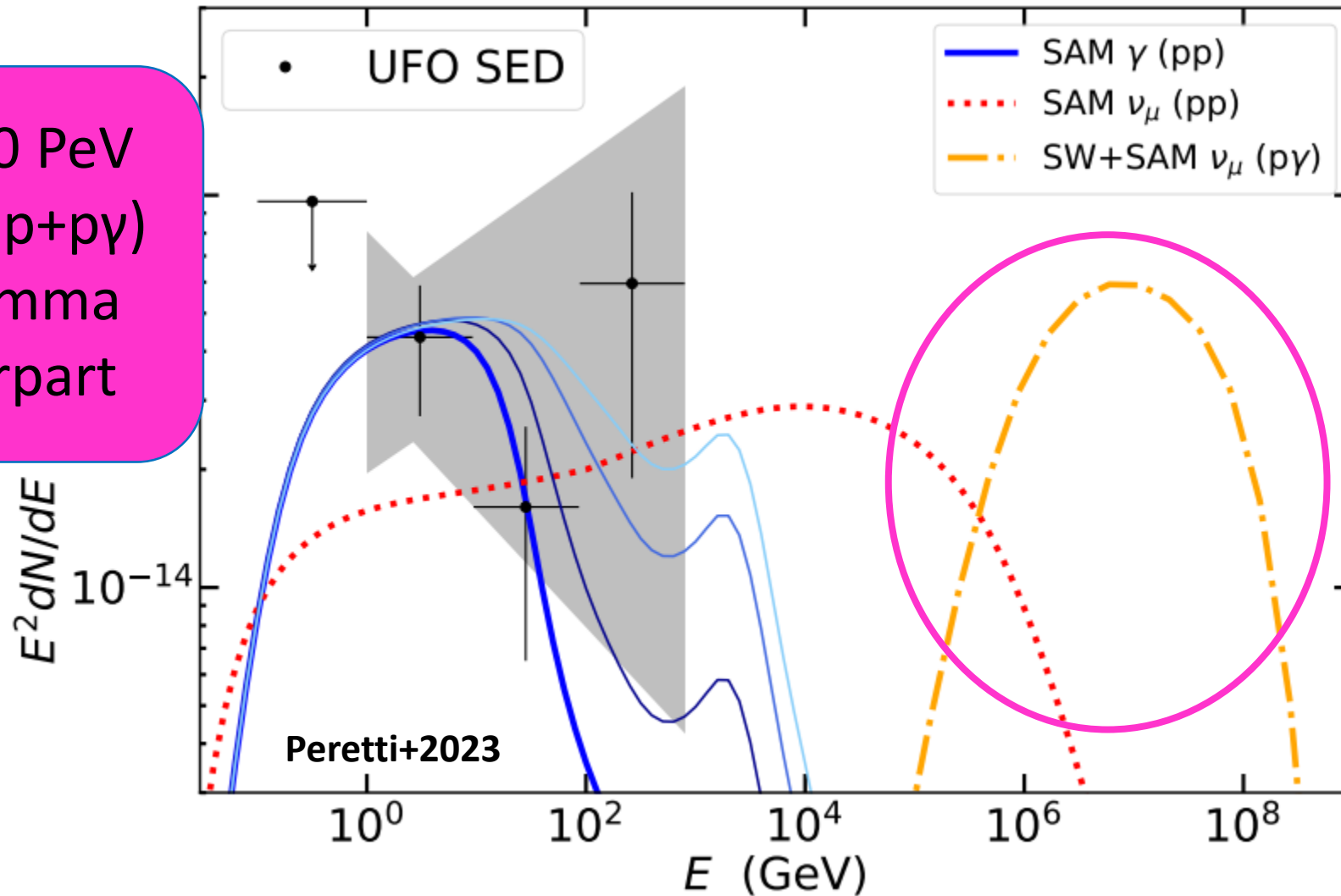
UFO model applied to Fermi-LAT results

TeV neutrinos (pp)
with partially
absorbed gamma-
ray counterpart



UFO model applied to Fermi-LAT results

100 TeV-100 PeV
neutrinos (pp+p γ)
without gamma
ray counterpart



Take home message

- Diffusive shock acceleration is an evergreen mechanism
 - Wind bubbles are promising sites for DSA
- Multi-messenger radiation is efficiently produced in WBs
 - Energies as high as EeV can be produced in UFOs

THANKS FOR YOUR ATTENTION!

BACK UP

Wind Bubble dynamics – Forward shock

$$M(R) = \int_0^R dr 4\pi r^2 \rho_0(r)$$

$$\frac{d}{dt} [M(R)\dot{R}] = 4\pi R^2 P$$

$$\frac{d}{dt} \left[\frac{4}{3} \pi R^3 \frac{P}{\gamma_g - 1} \right] = L_w + 4\pi R^2 \dot{R} P - L_c$$

$$R(t) = At^{-\alpha} \rightarrow \alpha = 3/5$$

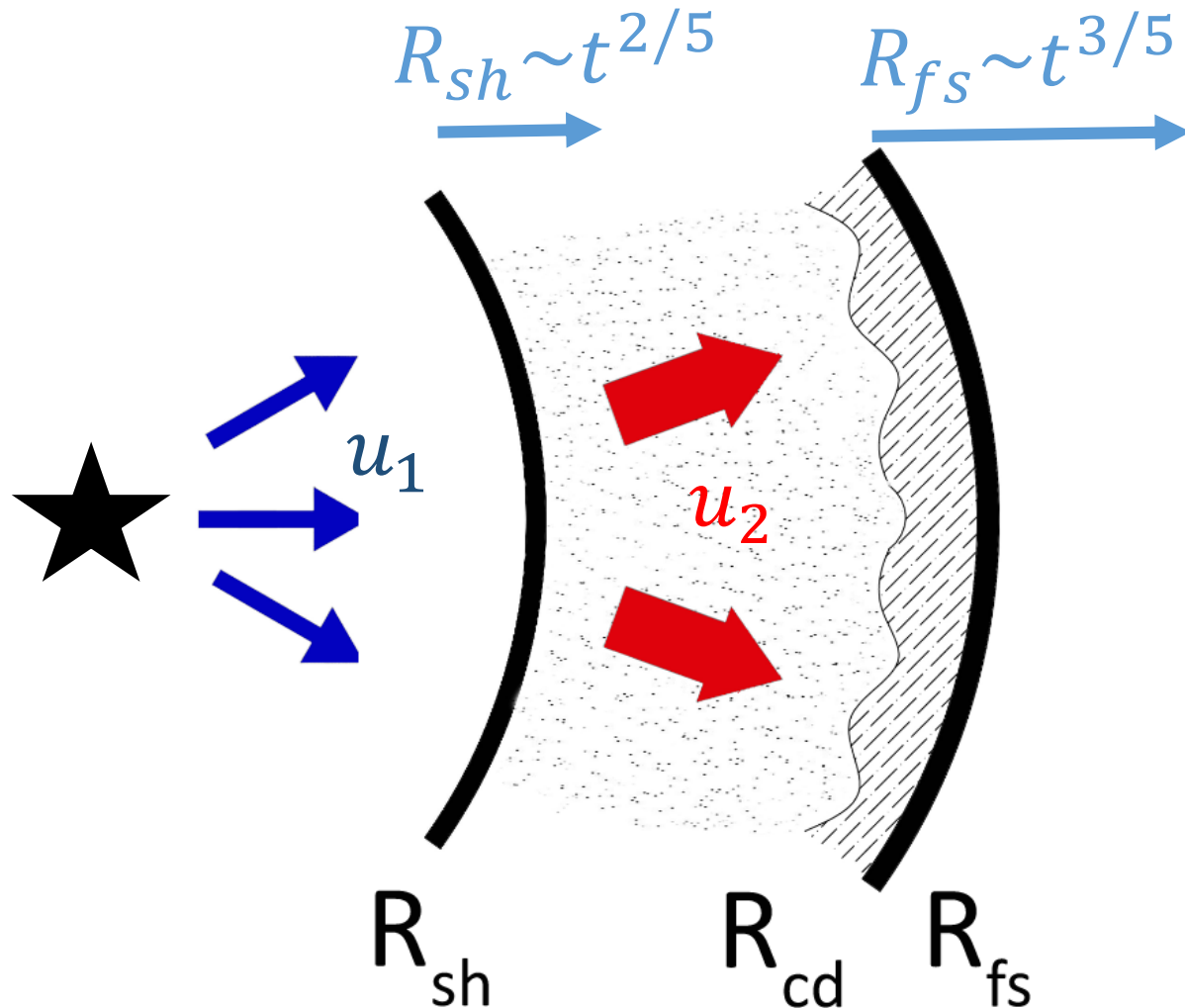
Wind Bubble dynamics – Wind termination shock

$$P_{ram,sh} = P_{sw}$$

$$\frac{\dot{M}u_1}{4\pi R_{sh}^2} = \frac{7}{25} A^2 \rho_0 t^{-4/5}$$

$$R_{sh}(t) \propto t^{2/5}$$

Characterizing the accelerator



Geometry of the accelerator:

Diverging flows such as wind bubbles formed by ultra-fast outflow feature a strong qualitative difference from standard cosmic accelerators such as supernova remnants.

Here the escape takes is only possible through the downstream region.

Characterizing the accelerator

Time (in)dependence of the accelerator:

Sitting in the reference frame of the central engine the velocity of the fast cool wind is much larger than the shock velocities.

The timescales for HE particles are shorter than the dynamical time of the system.

τ_{sh}

τ_{cd}

τ_{fs}

Geometry of the accelerator:

Diverging flows such as wind bubbles formed by ultra-fast outflow feature a strong qualitative difference from standard cosmic accelerators such as supernova remnants.

Here the escape takes is only possible through the downstream region.

Characterizing the accelerator

Time (in)dependence of the
accelerator:

Stationary diffusive shock
acceleration is a good
approximation.

Ω_{sh}

Ω_{cd}

Ω_{fs}

Geometry of the accelerator:

We can get very high
maximum energies
«for free».