

# Sky Anisotropies of High-Energy Neutrino Flavours

Bernanda Telalovic, Mauricio Bustamante

What are the astrophysical neutrino  
flavour ratio directions?

T  
HERE  
&  
EVERYWHERE  
E



Could we see new physics  
if they're different?

# What?

High-energy astrophysical neutrinos (**TeV–PeV**):



# What?

High-energy astrophysical neutrinos (**TeV–PeV**):

- originate from HE hadronic processes.



# What?

High-energy astrophysical neutrinos (**TeV–PeV**):

- originate from HE hadronic processes.
- travel distances  $\sim$  **Gpc**.



# What?

High-energy astrophysical neutrinos (**TeV–PeV**):

- originate from HE hadronic processes.
- travel distances  $\sim$  **Gpc**.
- **rich phenomenology** for physics  
beyond the Standard Model



# What?

High-energy astrophysical neutrinos (**TeV–PeV**):

- originate from HE hadronic processes.
- travel distances  $\sim$  **Gpc**.
- **rich phenomenology** for physics  
beyond the Standard Model

IceCube has seen a flux of high-energy astrophysical neutrinos!

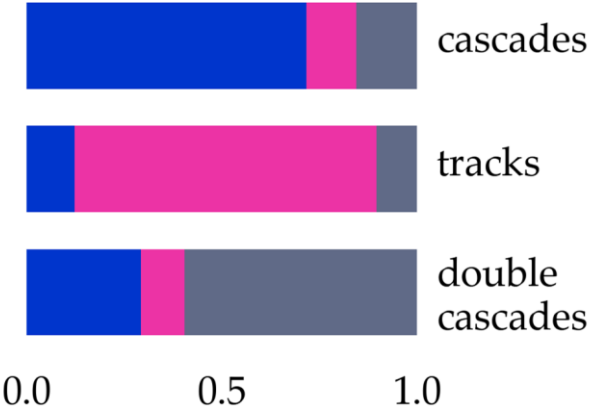
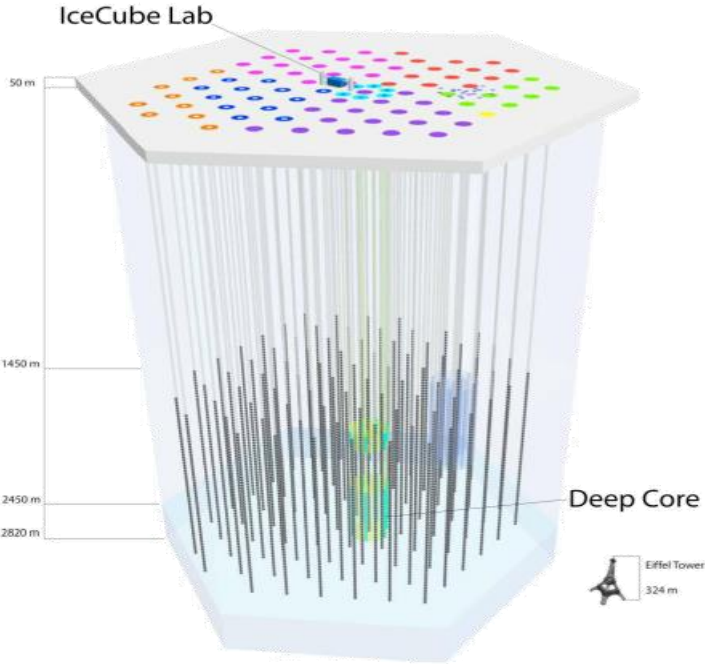
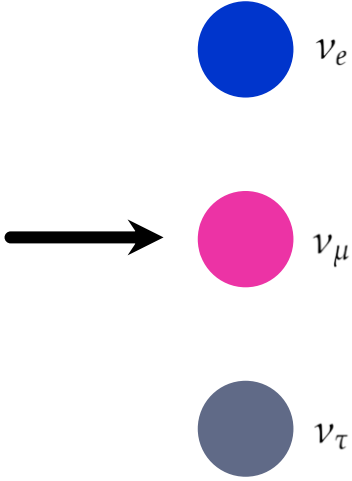


# IceCube Detection

Neutrino

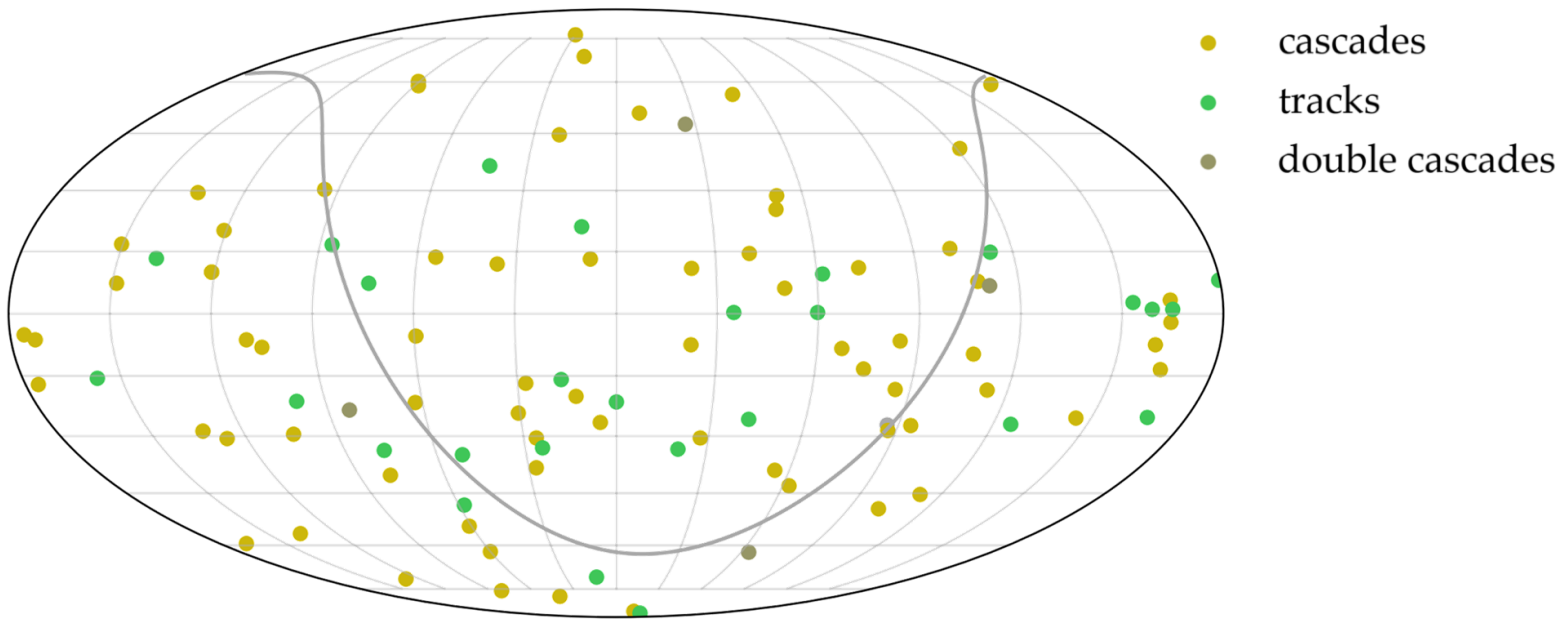
detected in IceCube

as morphology:



interacts as flavour

IceCube HESE 7.5 year event sample – best fit locations (102 events)





The flavour-flux at Earth:

$$\Phi_{\alpha} = \frac{\Phi_0}{4\pi} f_{\alpha} (1 + \Delta\Phi_{\alpha})$$

The flavour-flux at Earth:

all-flavour flux  
↓

$$\Phi_{\alpha} = \frac{\Phi_0}{4\pi} f_{\alpha} (1 + \Delta\Phi_{\alpha})$$

# The Flux Model

The flavour-flux at Earth:

$$\Phi_{\alpha} = \frac{\overset{\text{all-flavour flux}}{\downarrow} \Phi_0}{4\pi} \overset{\text{isotropic flavour ratio}}{\downarrow} f_{\alpha} (1 + \Delta\Phi_{\alpha})$$

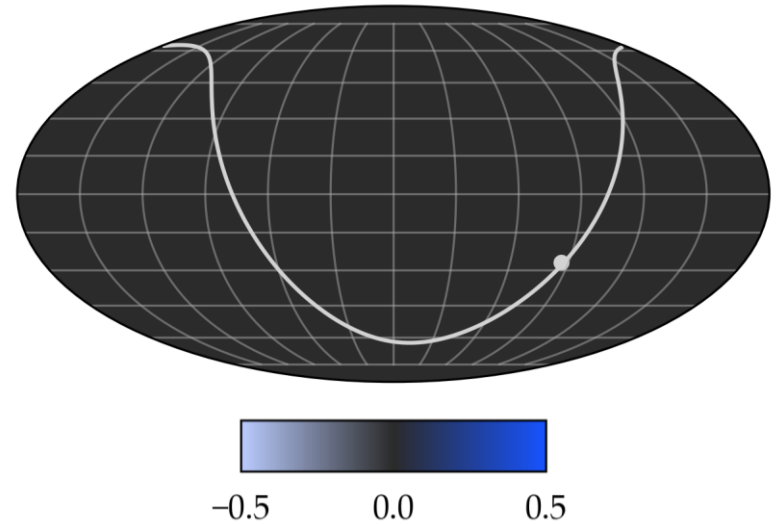


# The Flux Model

The flavour-flux at Earth:

$$\Phi_{\alpha} = \frac{\overset{\text{all-flavour flux}}{\downarrow} \Phi_0}{4\pi} f_{\alpha} \overset{\text{isotropic flavour ratio}}{\downarrow} (1 + \Delta\Phi_{\alpha})$$

$$\Delta\Phi^e = \Delta\Phi^{\tau}$$



# The Flux Model

The flavour-flux at Earth:

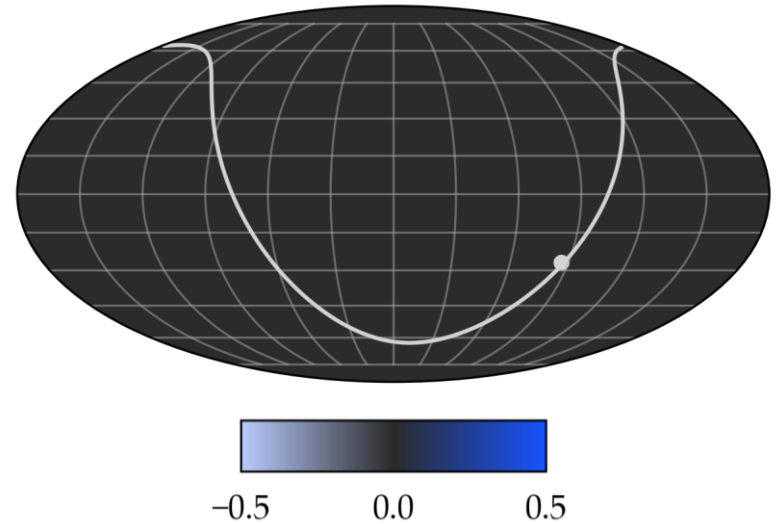
$$\Phi_{\alpha} = \frac{\Phi_0}{4\pi} f_{\alpha} (1 + \Delta\Phi_{\alpha})$$

all-flavour flux  
↓  
 $\Phi_0$

isotropic flavour ratio  
↓  
 $f_{\alpha}$

flavour anisotropy:  
↑  
 $\Delta\Phi_{\alpha}$

$$\Delta\Phi^e = \Delta\Phi^{\tau}$$



# The Flux Model

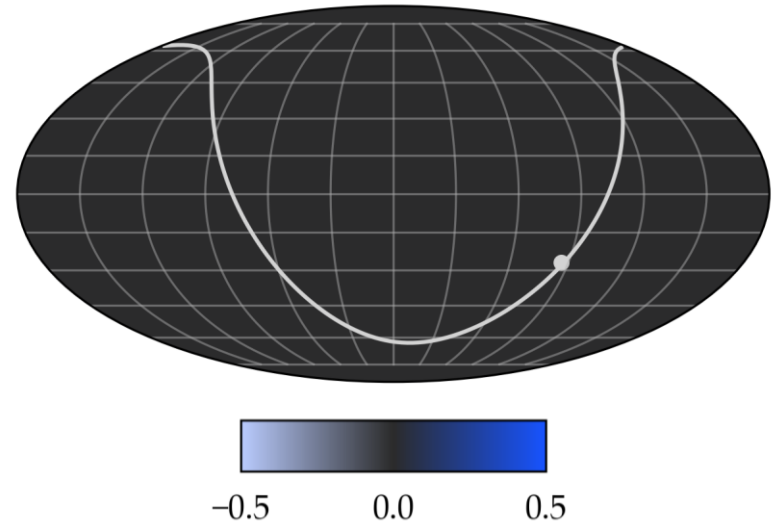
The flavour-flux at Earth:

$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

all-flavour flux  $\downarrow$   $\Phi_0$   
isotropic flavour ratio  $\downarrow$   $f_\alpha$

flavour anisotropy:  $\Delta\Phi_\alpha = \sum_{\ell>0, m} a_{\ell, m}^\alpha Y_{\ell, m}$

$$\Delta\Phi^e = \Delta\Phi^\tau$$



# The Flux Model

The flavour-flux at Earth:

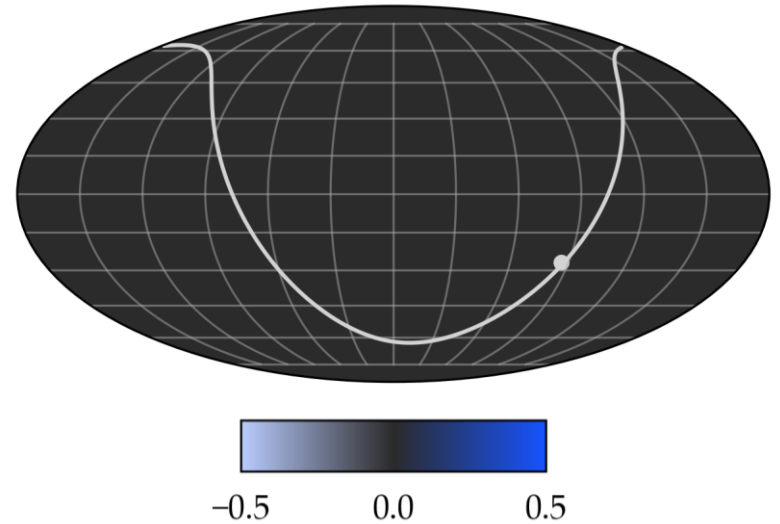
$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

all-flavour flux  $\downarrow$   $\Phi_0$   
isotropic flavour ratio  $\downarrow$   $f_\alpha$

flavour anisotropy:  $\Delta\Phi_\alpha = \sum_{\ell>0, m} a_{\ell, m}^\alpha Y_{\ell, m}$

anisotropy coefficients  $\uparrow$   $a_{\ell, m}^\alpha$

$$\Delta\Phi^e = \Delta\Phi^\tau$$



# The Flux Model

The flavour-flux at Earth:

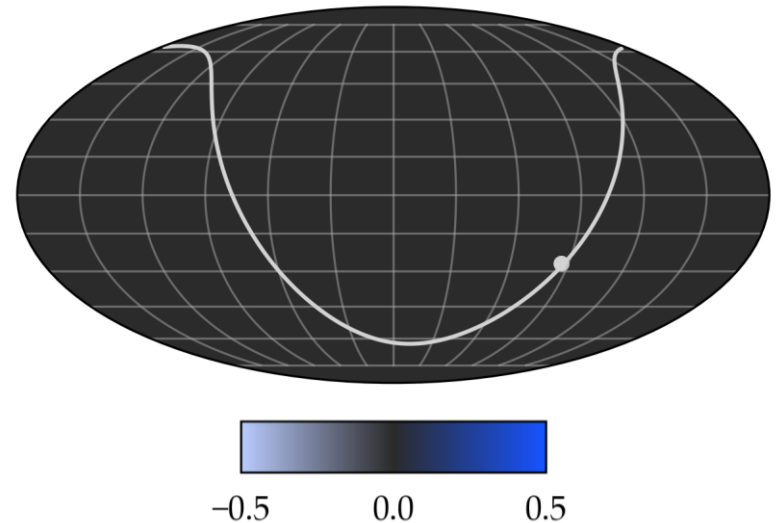
$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

all-flavour flux  
 ↓  
 $\Phi_0$   
 isotropic flavour ratio  
 ↓  
 $f_\alpha$

flavour anisotropy:  $\Delta\Phi_\alpha = \sum_{\ell>0, m} a_{\ell, m}^\alpha Y_{\ell, m}$

↑  
 anisotropy coefficients  
 ↓  
 real spherical harmonics

$$\Delta\Phi^e = \Delta\Phi^\tau$$





# The Flux Model

The flavour-flux at Earth:

$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

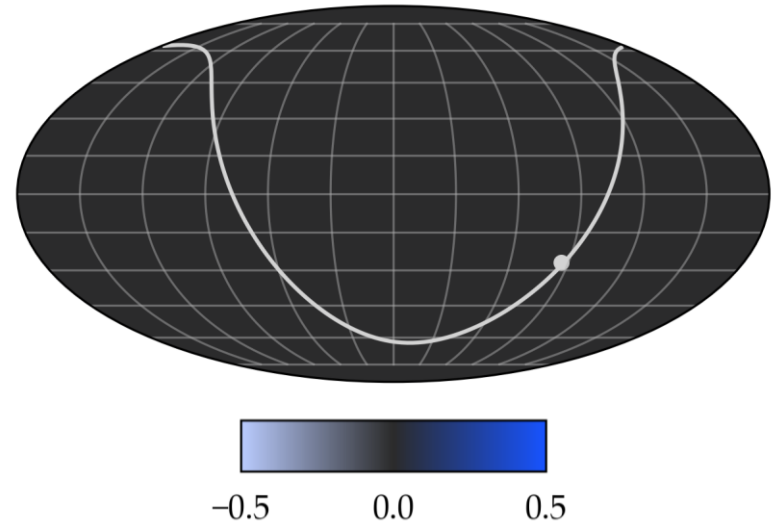
all-flavour flux  
 ↓  
 $\Phi_0$   
 isotropic flavour ratio  
 ↓  
 $f_\alpha$

flavour anisotropy:  $\Delta\Phi_\alpha =$

$$\sum_{l,m} a_{l,m} Y_{l,m}$$

**new physics?**  
 ↓  
 anisotropy coefficients

$$\Delta\Phi^e = \Delta\Phi^\tau$$



real spherical harmonics

# The Flux Model

The flavour-flux at Earth:

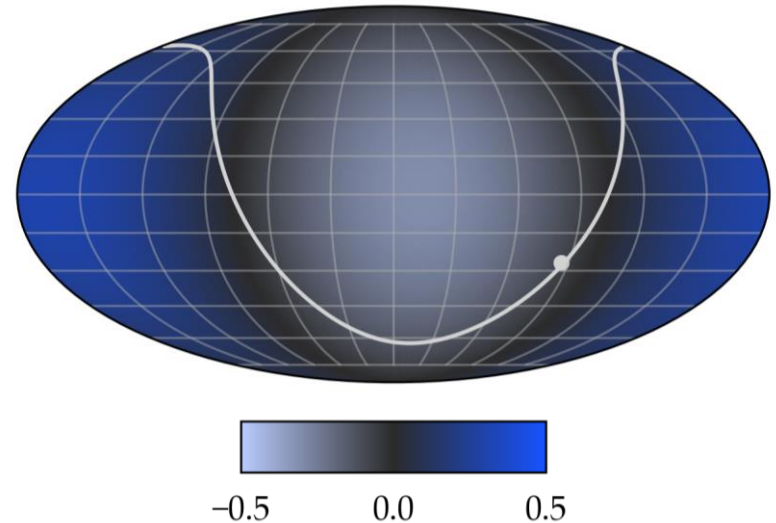
$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

all-flavour flux  
 ↓  
 $\Phi_0$   
 isotropic flavour ratio  
 ↓  
 $f_\alpha$

flavour anisotropy:  $\Delta\Phi_\alpha = \sum_{\ell>0, m} a_{\ell, m}^\alpha Y_{\ell, m}$

↑  
 anisotropy coefficients  
 ↓  
 real spherical harmonics

$$\Delta\Phi^e = \Delta\Phi^\tau$$



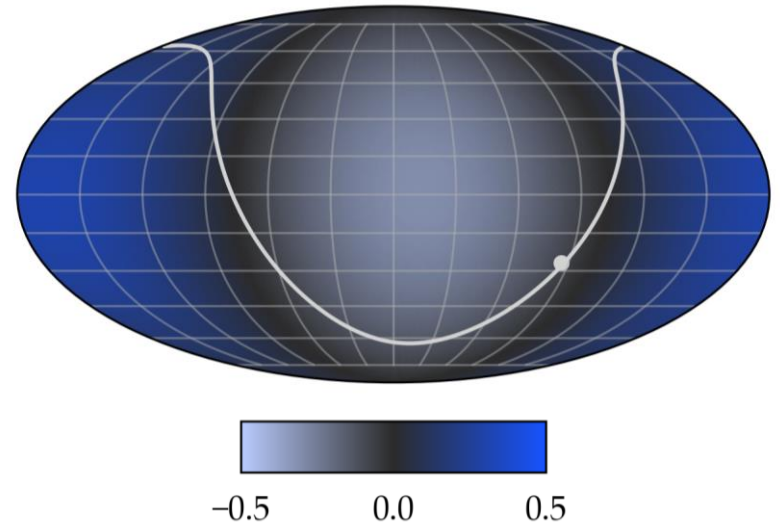
# The Flux Model

The flavour-flux at Earth:

$$\Phi_\alpha = \frac{\Phi_0}{4\pi} f_\alpha (1 + \Delta\Phi_\alpha)$$

all-flavour flux  $\downarrow$   $\Phi_0$   
 isotropic flavour ratio  $\downarrow$   $f_\alpha$

$$\Delta\Phi^e = \Delta\Phi^\tau$$



real spherical harmonics  $\downarrow$

directional anisotropy:  $\Delta\Phi_\alpha = \sum_{\ell>0, m} a_{\ell, m}^\alpha Y_{\ell, m}$

anisotropy coefficients  $\uparrow$

*Are flavour ratios directionally-dependent?*

# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

**Detection**

*Lots of  
stuff*



# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Detection



# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Detection



# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Detection





# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Detection





# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

**Production**

*Lots of  
stuff*

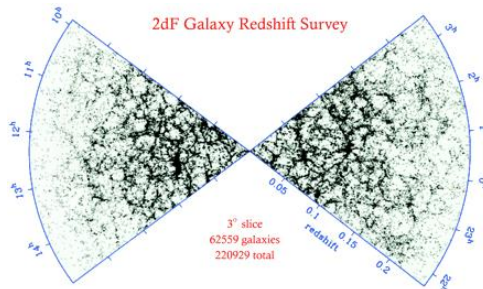


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Production

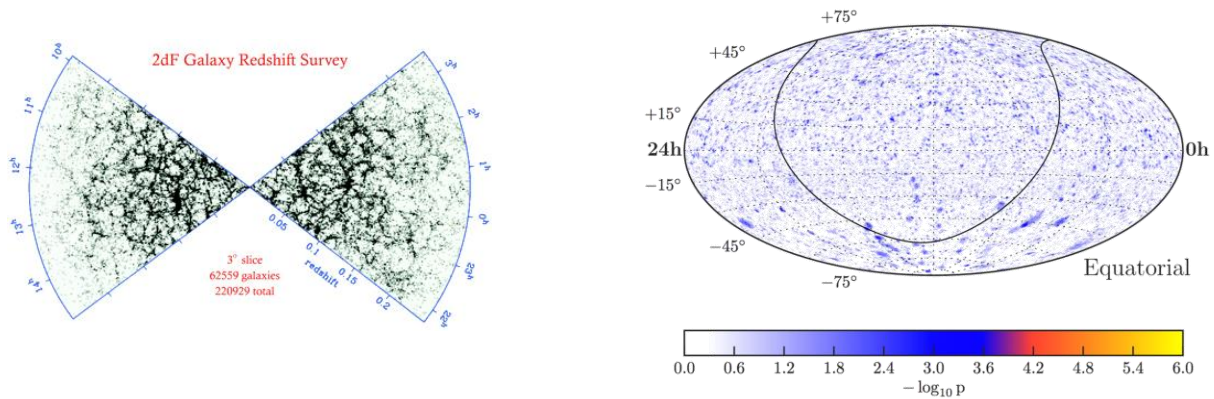


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Production

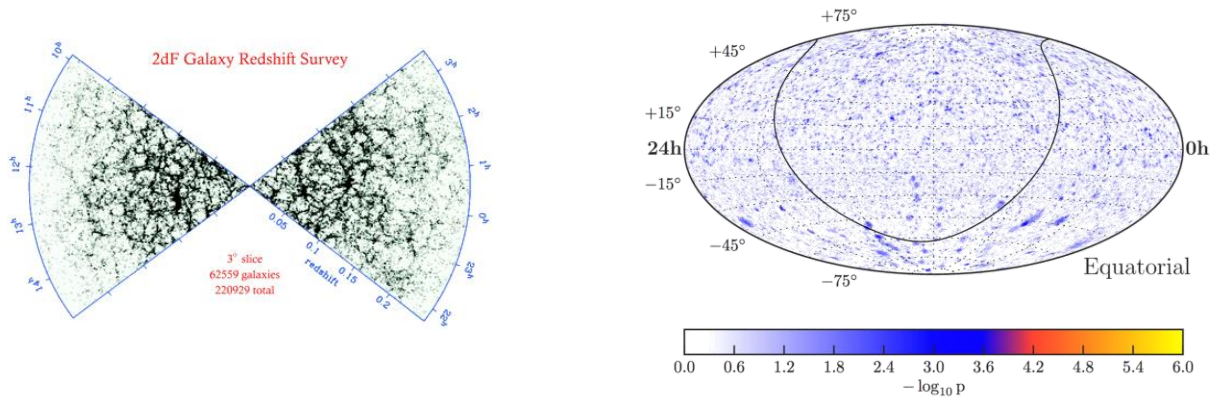


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Production



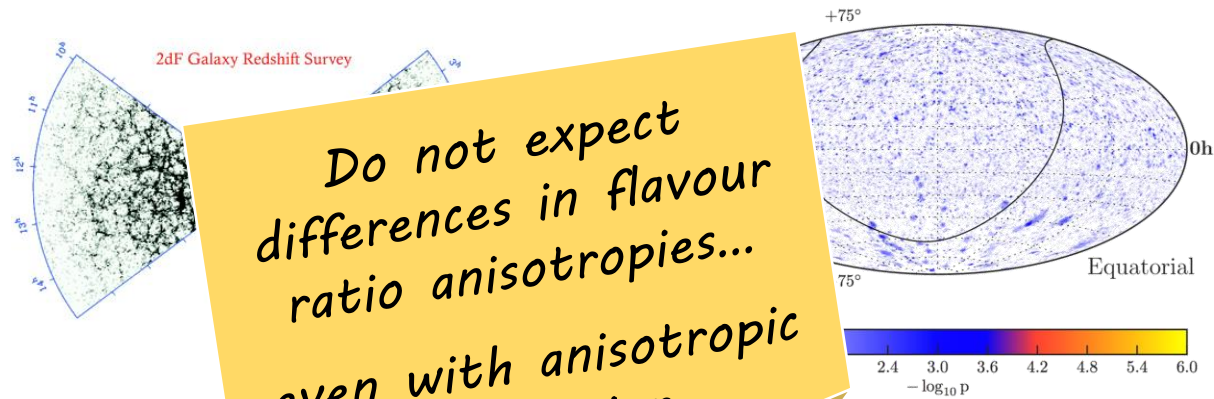
But we care about  
flavour ratios

# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Production



*Do not expect differences in flavour ratio anisotropies... even with anisotropic production*

about flavour ratios

# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

**Propagation**

*Lots of  
stuff*

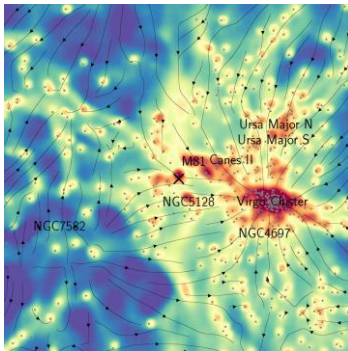


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Propagation

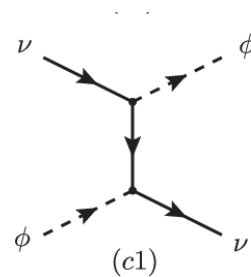
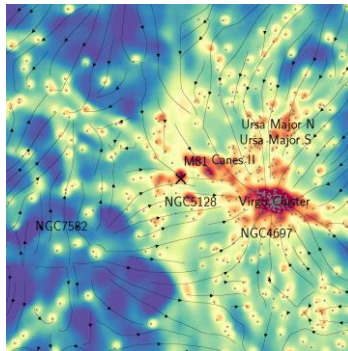


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Propagation



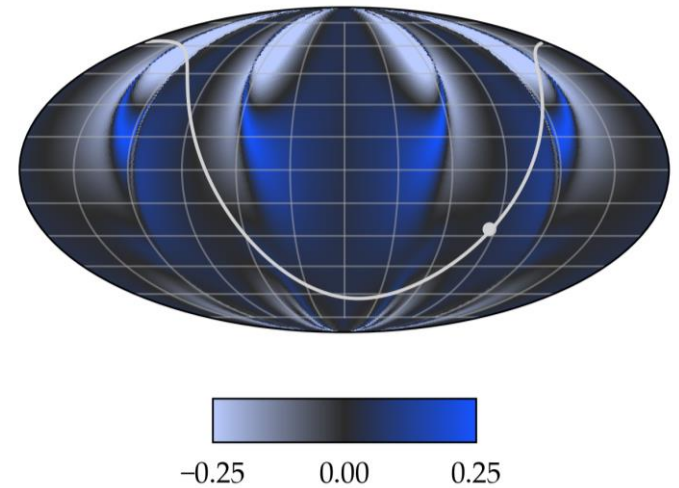
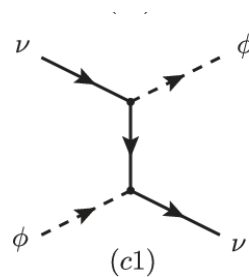
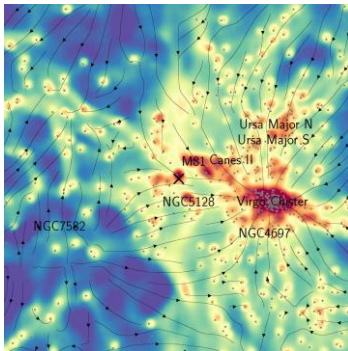


# Why new physics?

Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Propagation

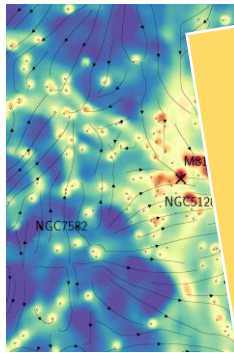


# Why new physics?

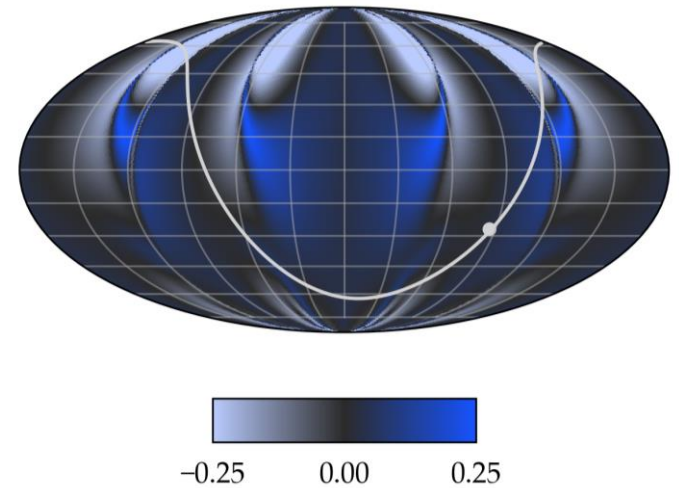
Say that  $\nu_e$ ,  $\nu_\mu$  and  $\nu_\tau$  have different arrival directions.

What could cause this?

## Propagation



Lots of  
new physics  
stuff :D



# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$



# Lorentz Invariance Violation (LIV)

couples to momentum 4-vector  
↓

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$



# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$

$$H_{\text{LIV}} = \sum_{d=3} E^{d-3} \sum_{\ell, m} \hat{\mathbf{a}}_{\ell, m} Y_{\ell, m}$$



# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$

$$H_{\text{LIV}} = \sum_{d=3} E^{d-3} \sum_{\ell,m} \hat{\mathbf{a}}_{\ell,m} Y_{\ell,m}$$

When:

$$d = 4 \quad \wedge \quad \hat{\mathbf{a}}_{1,-1} \neq 0$$



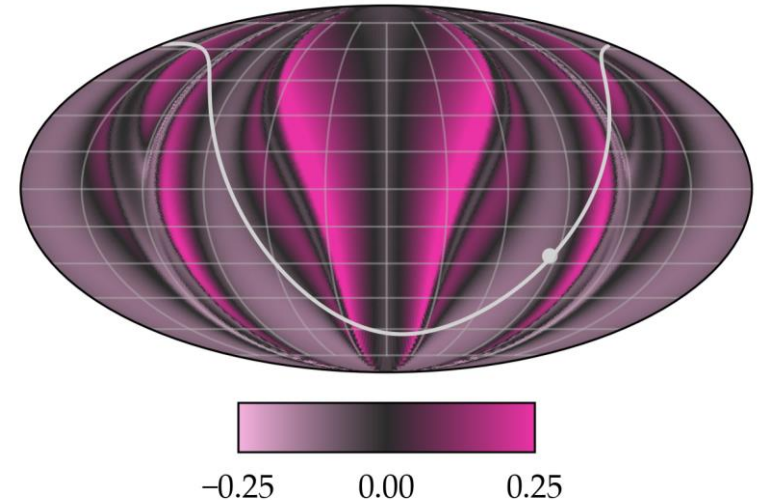
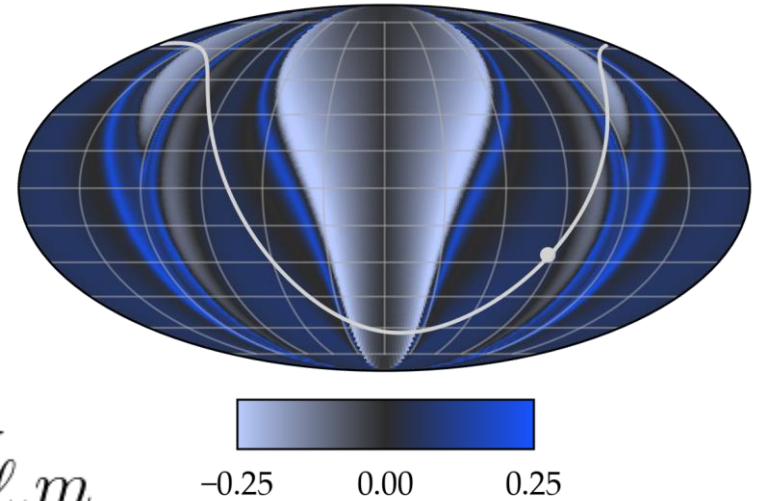
# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$

$$H_{\text{LIV}} = \sum_{d=3} E^{d-3} \sum_{\ell, m} \hat{\mathbf{a}}_{\ell, m} Y_{\ell, m}$$

When:

$$d = 4 \quad \wedge \quad \hat{\mathbf{a}}_{1, -1} \neq 0$$



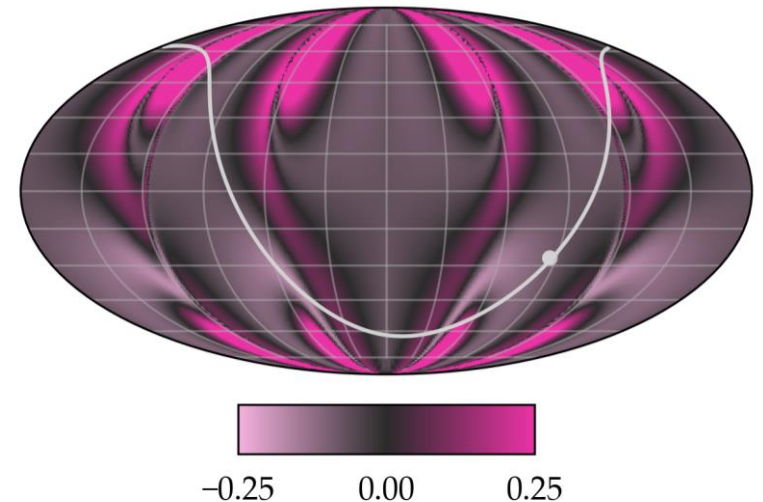
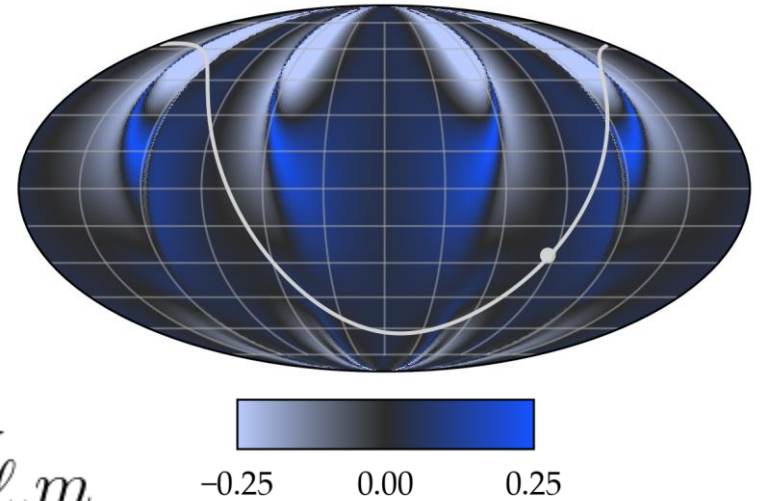
# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_{\text{vac}} + H_{\text{LIV}}$$

$$H_{\text{LIV}} = \sum_{d=3} E^{d-3} \sum_{\ell, m} \hat{\mathbf{a}}_{\ell, m} Y_{\ell, m}$$

When:

$$d = 5 \quad \wedge \quad \hat{\mathbf{a}}_{1,0} \neq 0$$





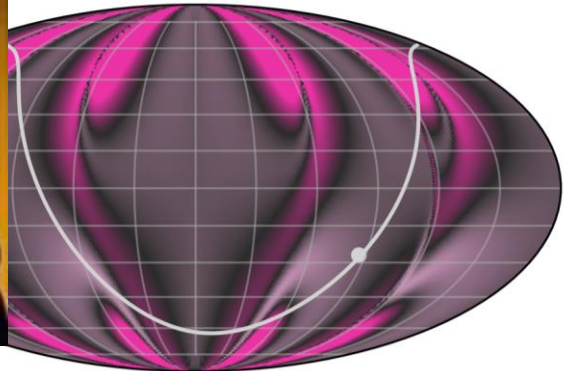
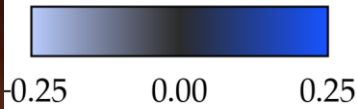
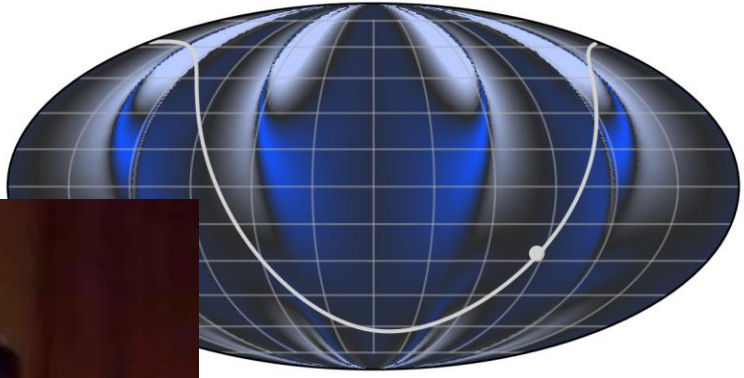
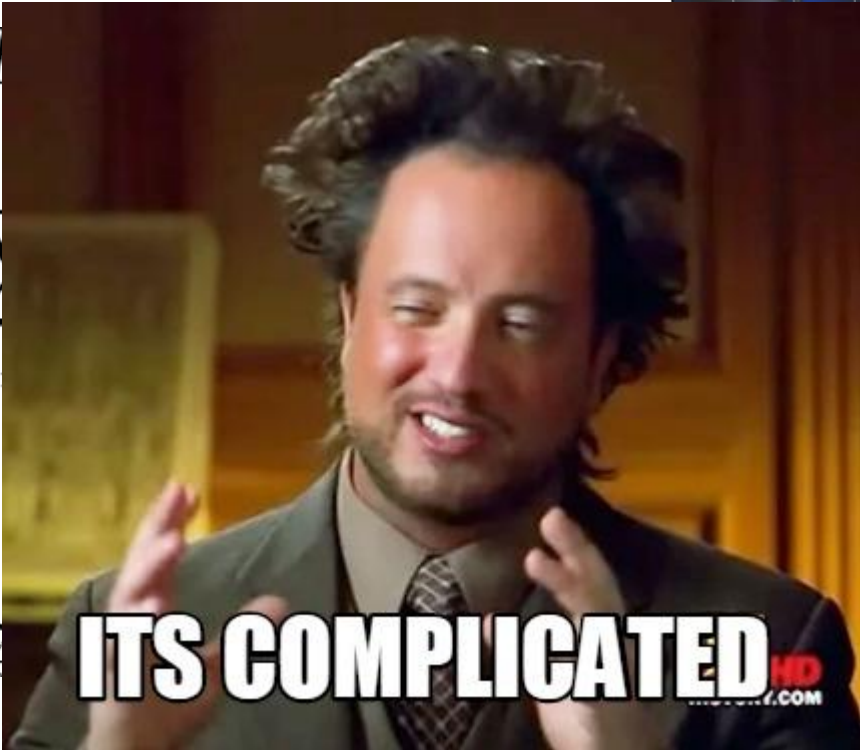
# Lorentz Invariance Violation (LIV)

$$H_{\text{tot}} = H_0 + H_{\text{LIV}}$$

$$H_{\text{LIV}} = \sum_{d=1}^n \frac{1}{d} \dots$$

When:

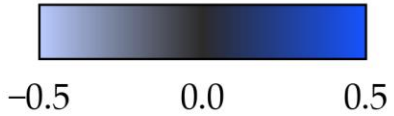
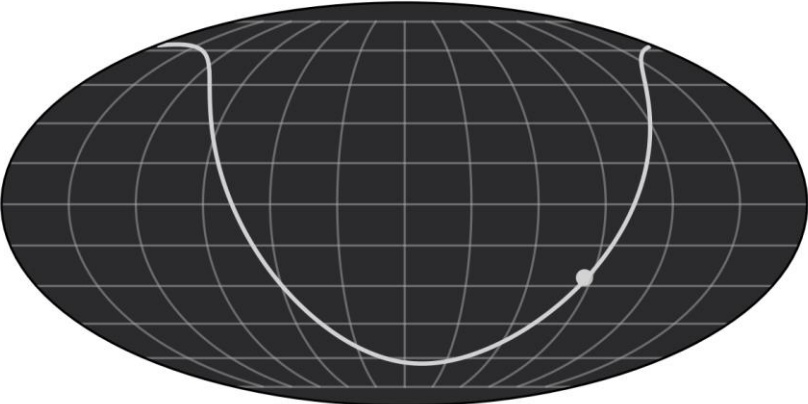
$$d = 1$$



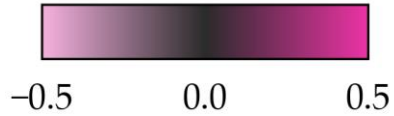
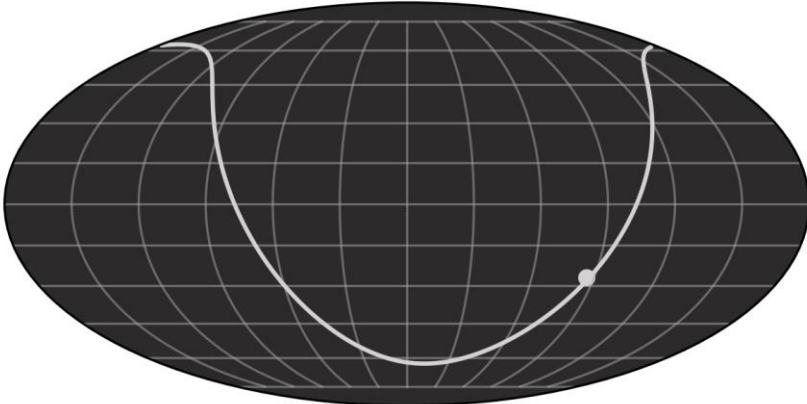
# Ok, but are they the same?

If the distributions were isotropic:

$$\Delta\Phi^e = \Delta\Phi^\tau$$



$$\Delta\Phi^\mu$$

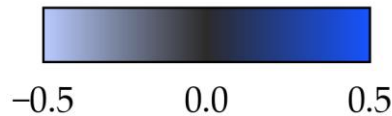
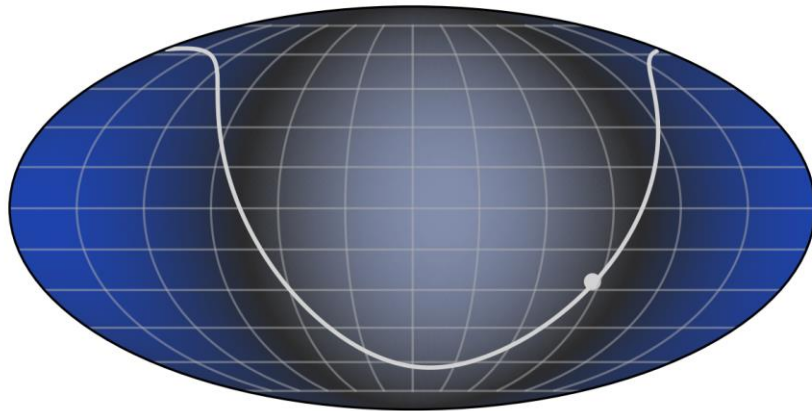


Equatorial

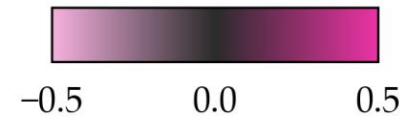
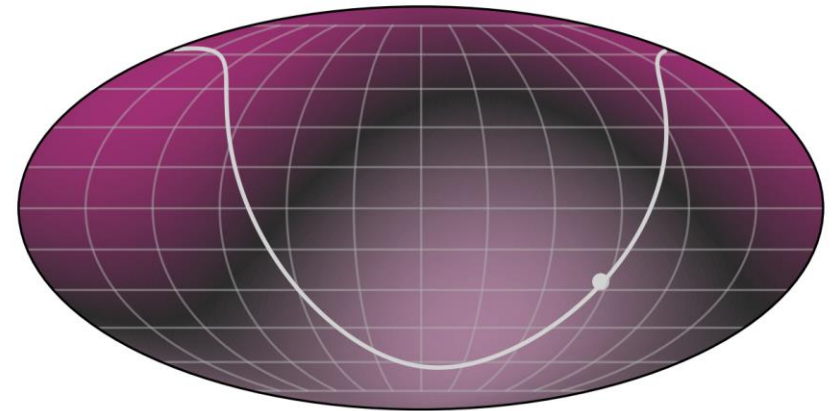
# Ok, but are they the same?

The flavour all-sky-average current **dipole** anisotropy best fits:

$$\Delta\Phi^e = \Delta\Phi^\tau$$



$$\Delta\Phi^\mu$$



Equatorial

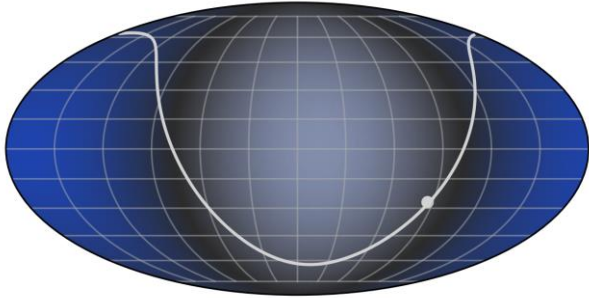
**Currently large uncertainties**—compatible with isotropy at  $1\sigma$ .

“We don’t expect different anisotropies in flavour ratios”



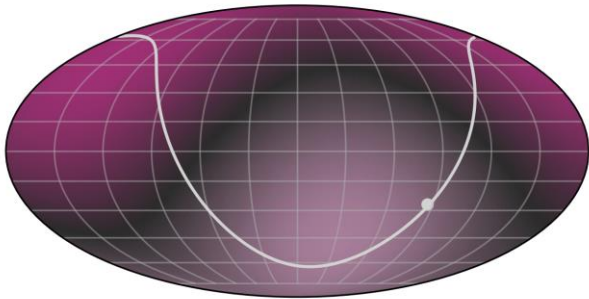
# “We don't expect different anisotropies in flavour ratios”

$$\Delta\Phi^e = \Delta\Phi^\tau$$

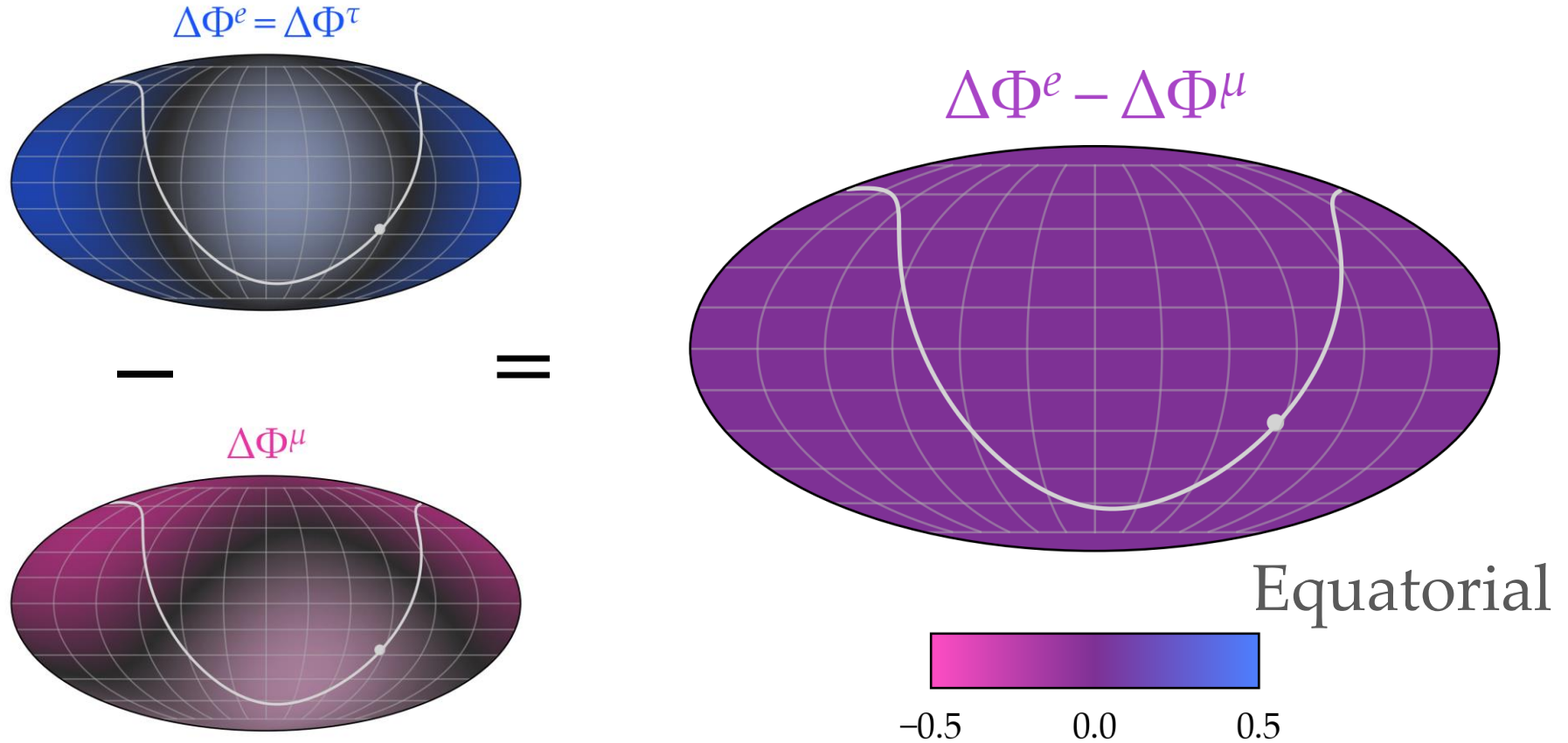


— =

$$\Delta\Phi^\mu$$

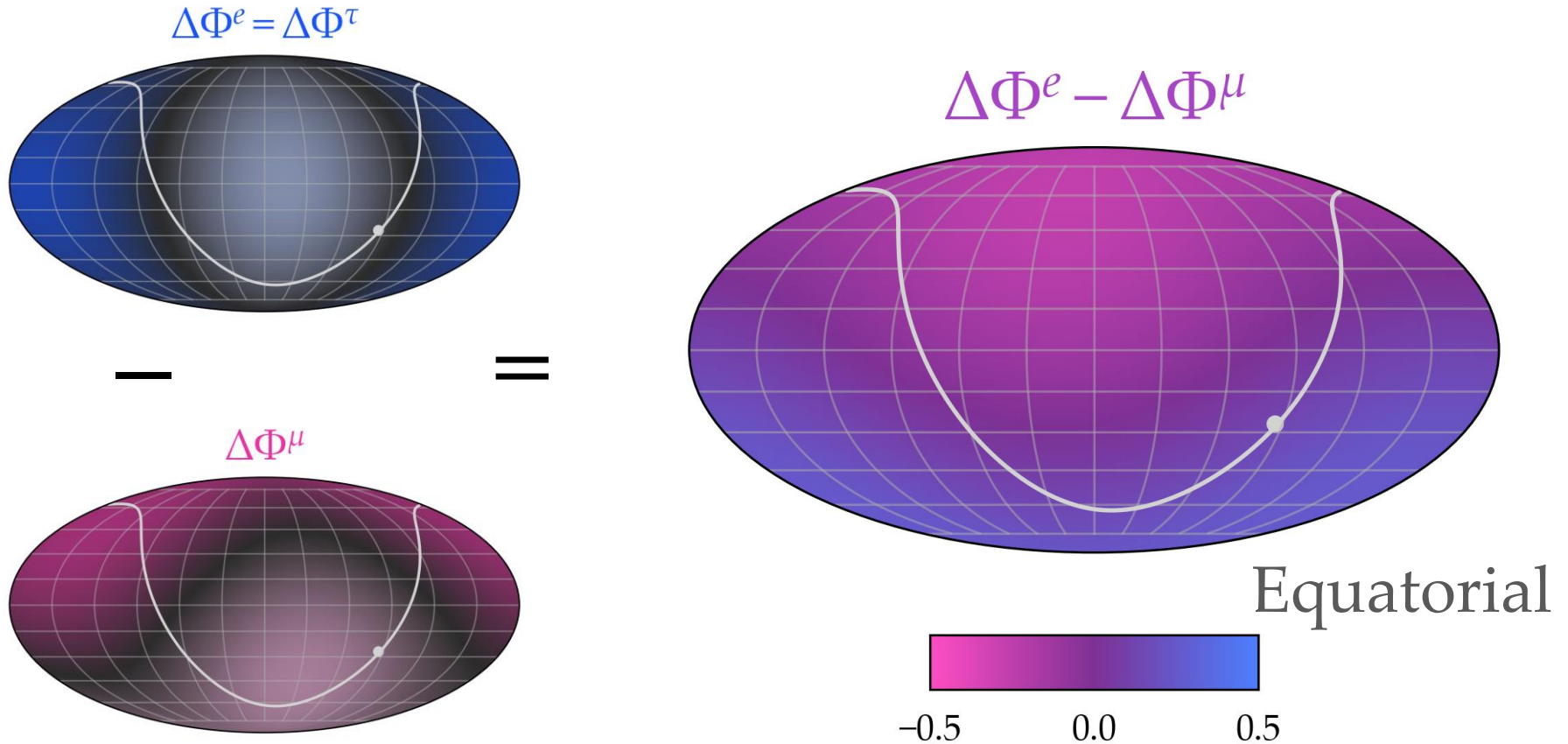


# “We don't expect different anisotropies in flavour ratios”



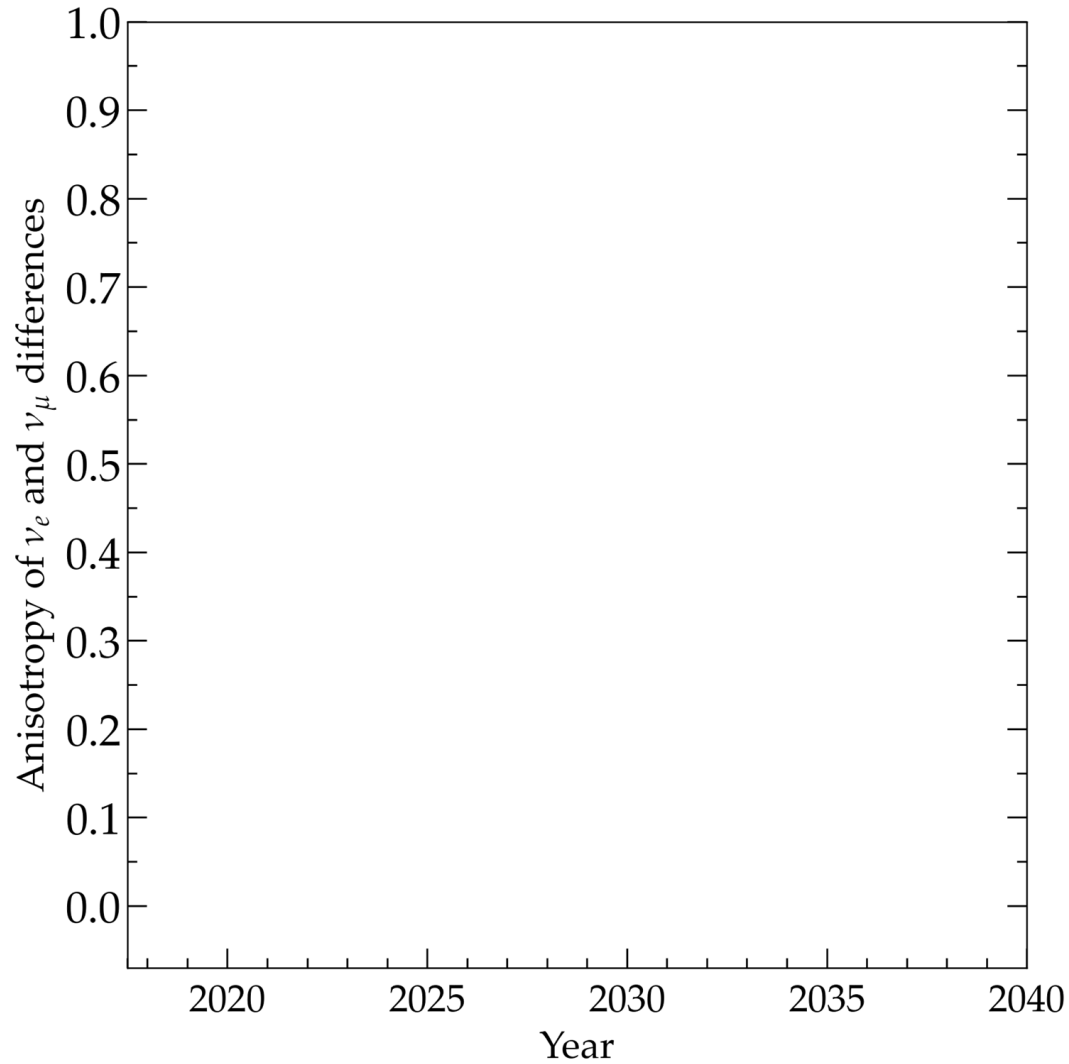


“We don’t expect different anisotropies in flavour ratios”



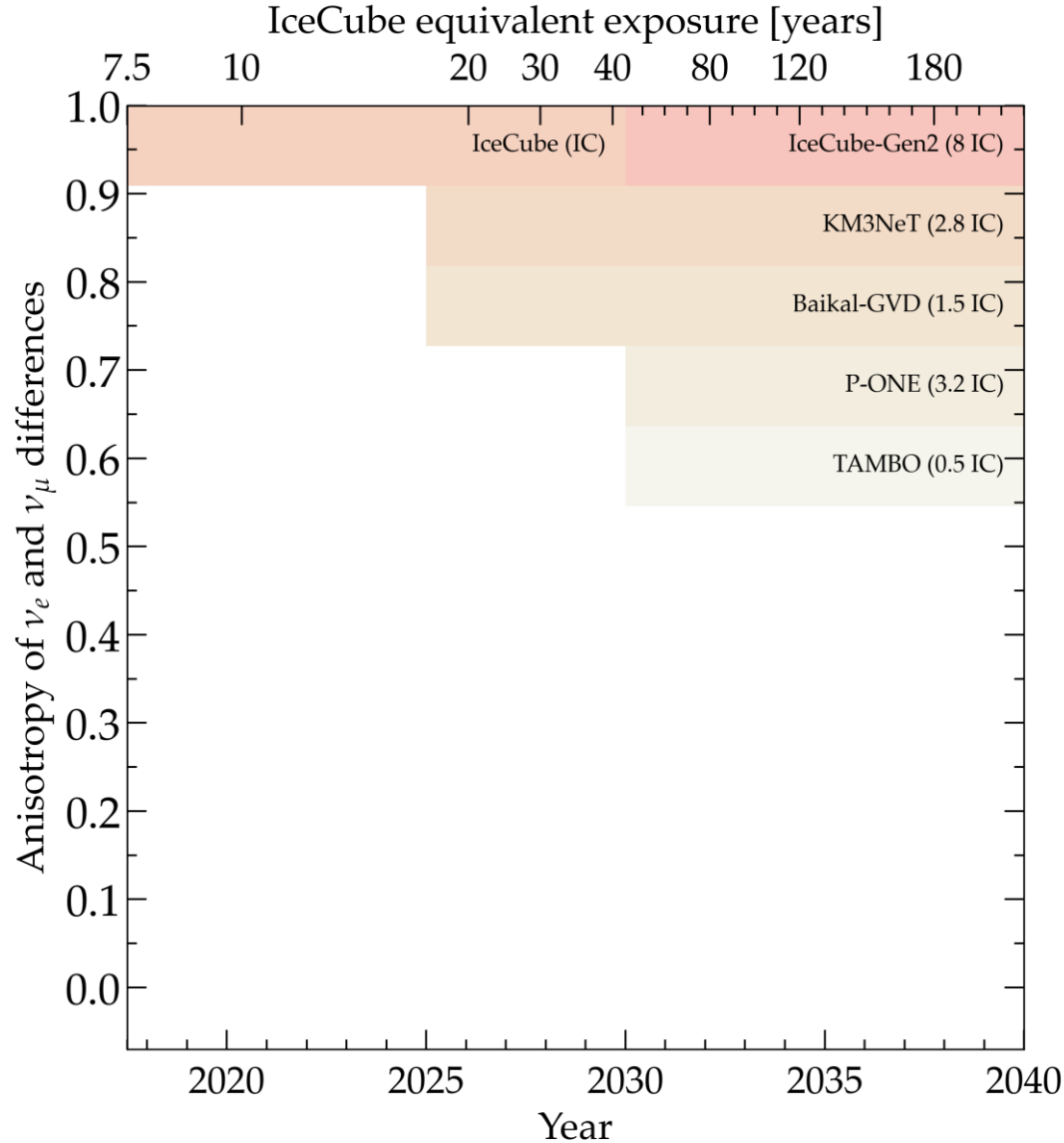
Currently large uncertainties—compatible with isotropy at  $1\sigma$ .

# How well can we constrain isotropy over time?





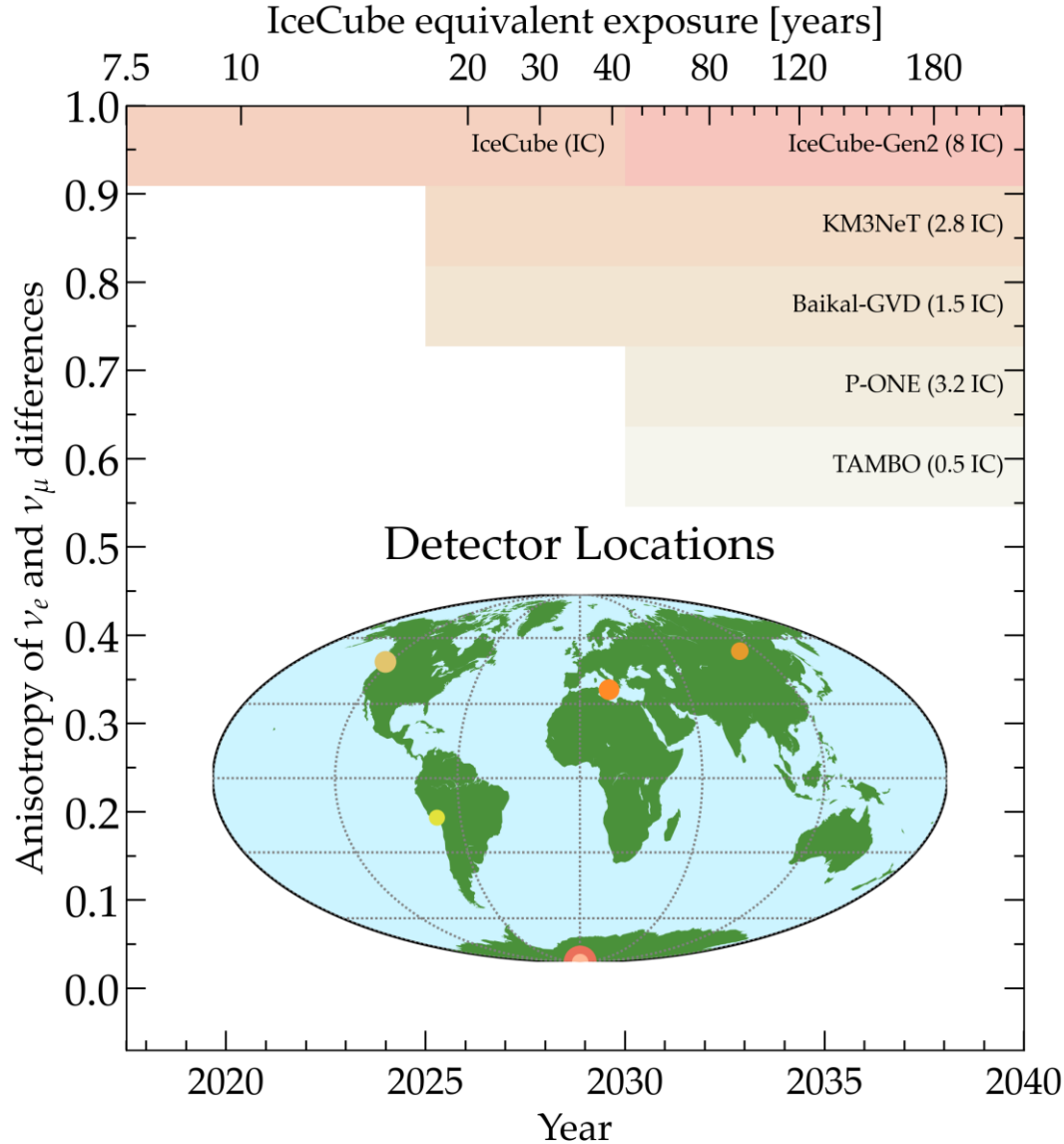
# How well can we constrain isotropy over time?



## More detectors – better:

- Statistics
- Angular resolution (KM3NeT)
- Sky coverage

# How well can we constrain isotropy over time?

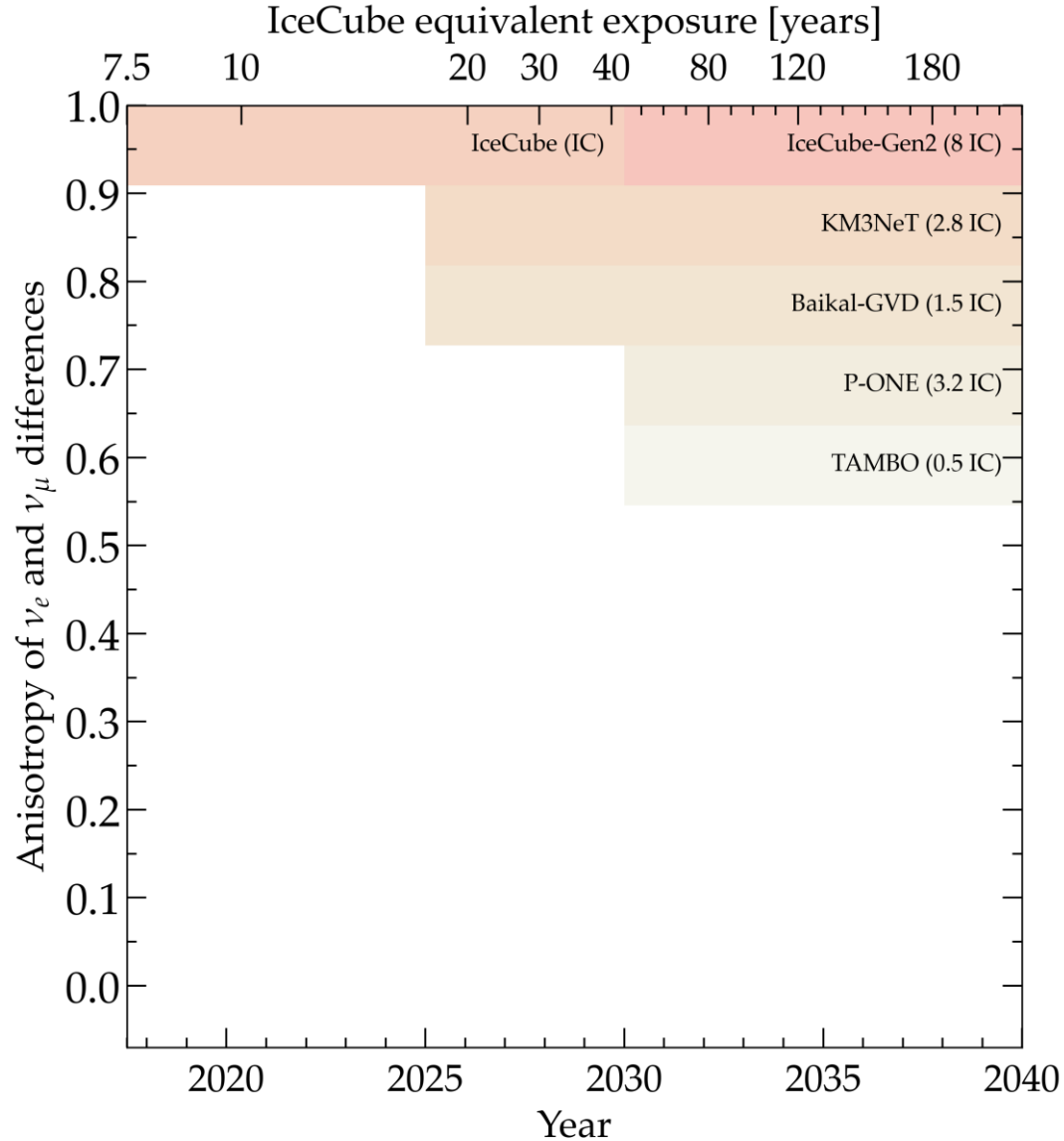


## More detectors – better:

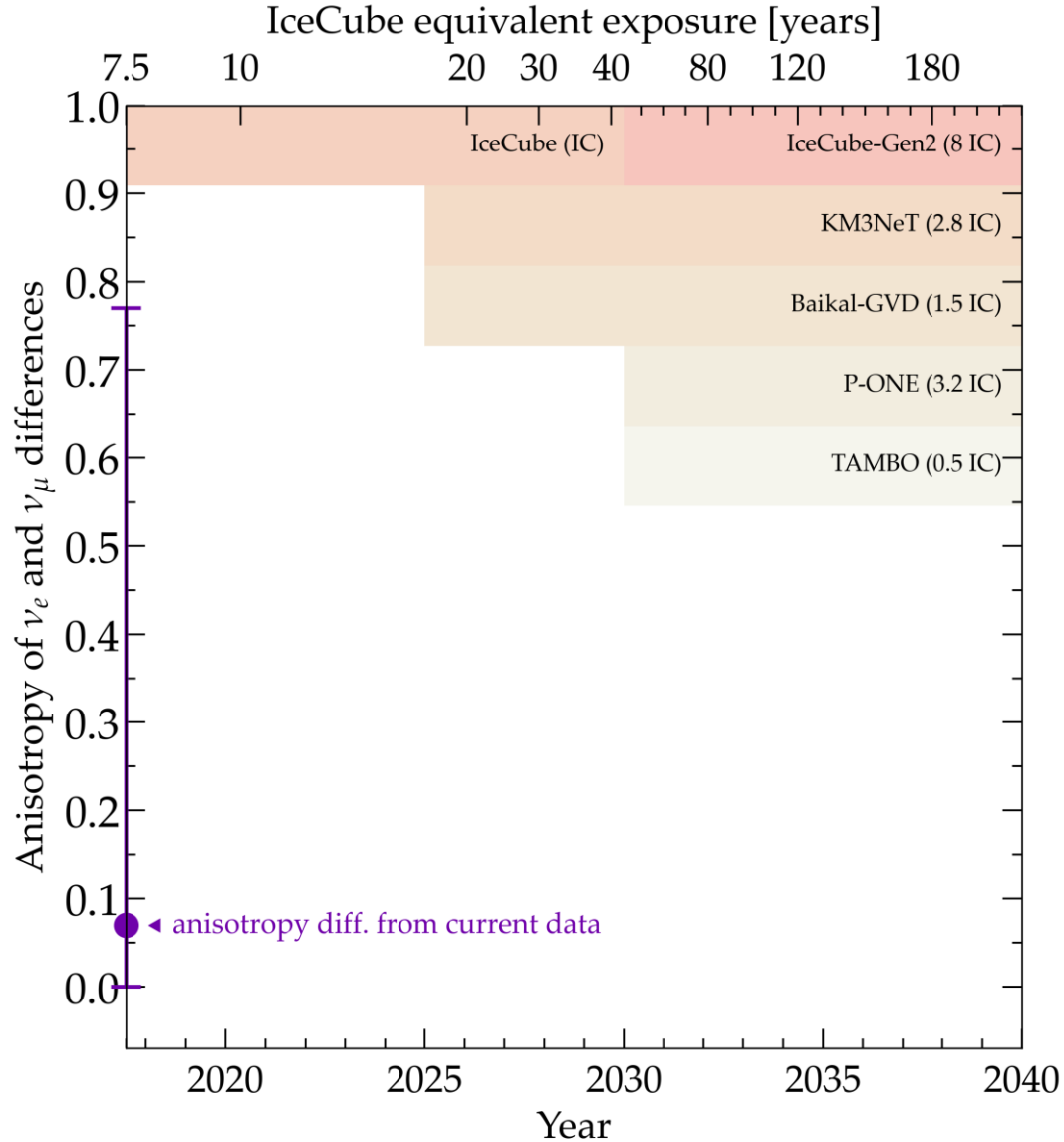
- Statistics
- Angular resolution (KM3NeT)
- Sky coverage

- IceCube (current)
- KM3NeT (2025)
- Baikal-GVD (2025)
- IceCube Gen2 (2030)
- P-ONE (2030)
- TAMBO (2030)

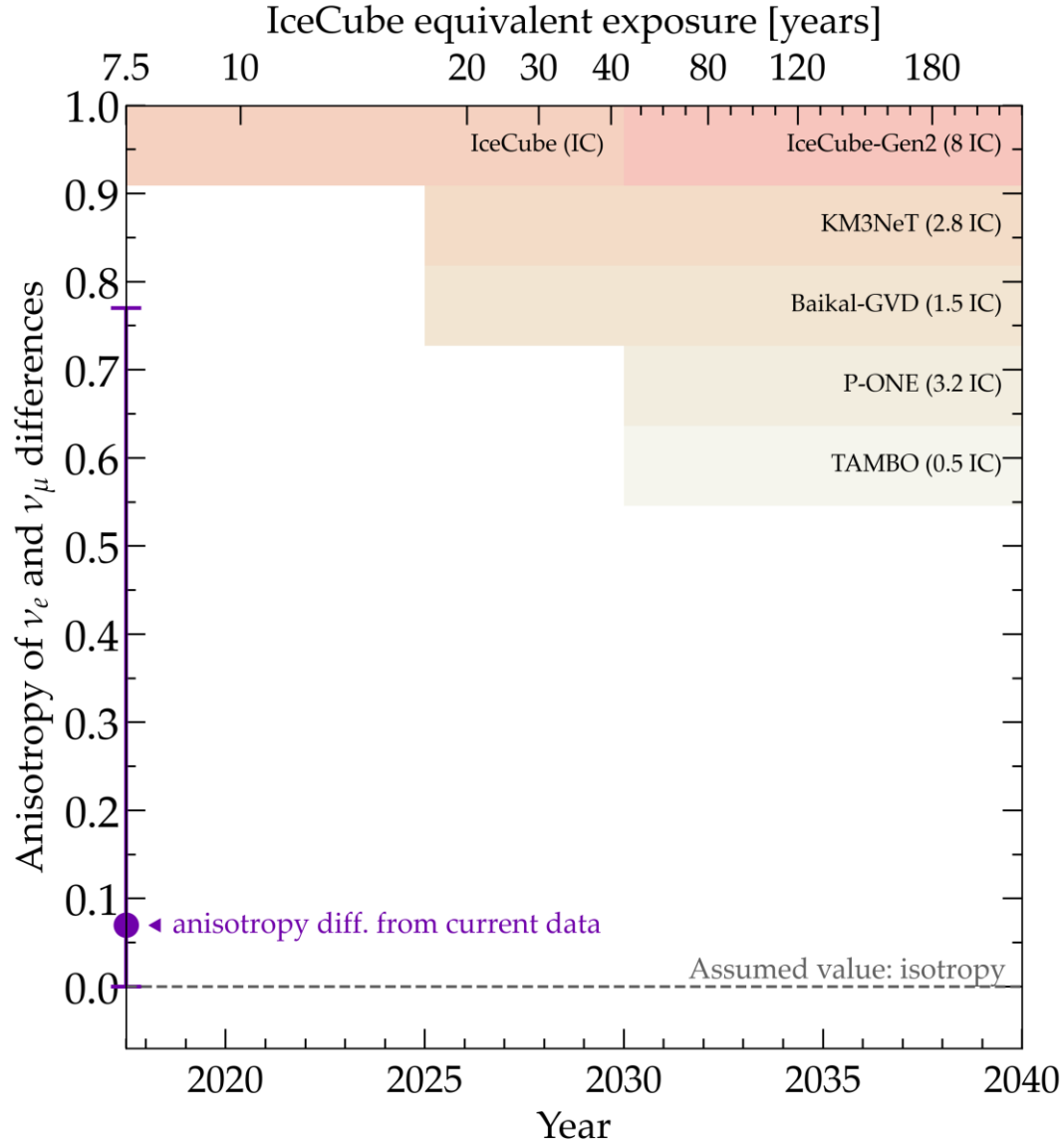
# How well can we constrain isotropy over time?



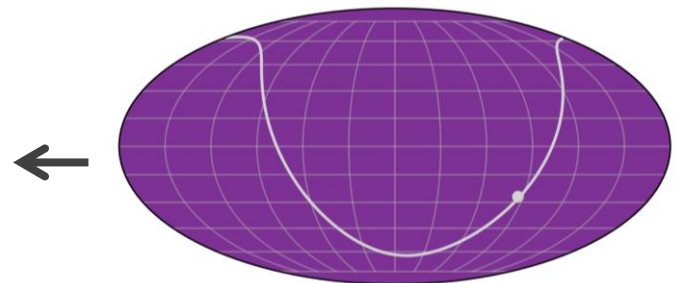
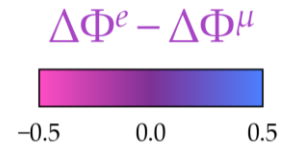
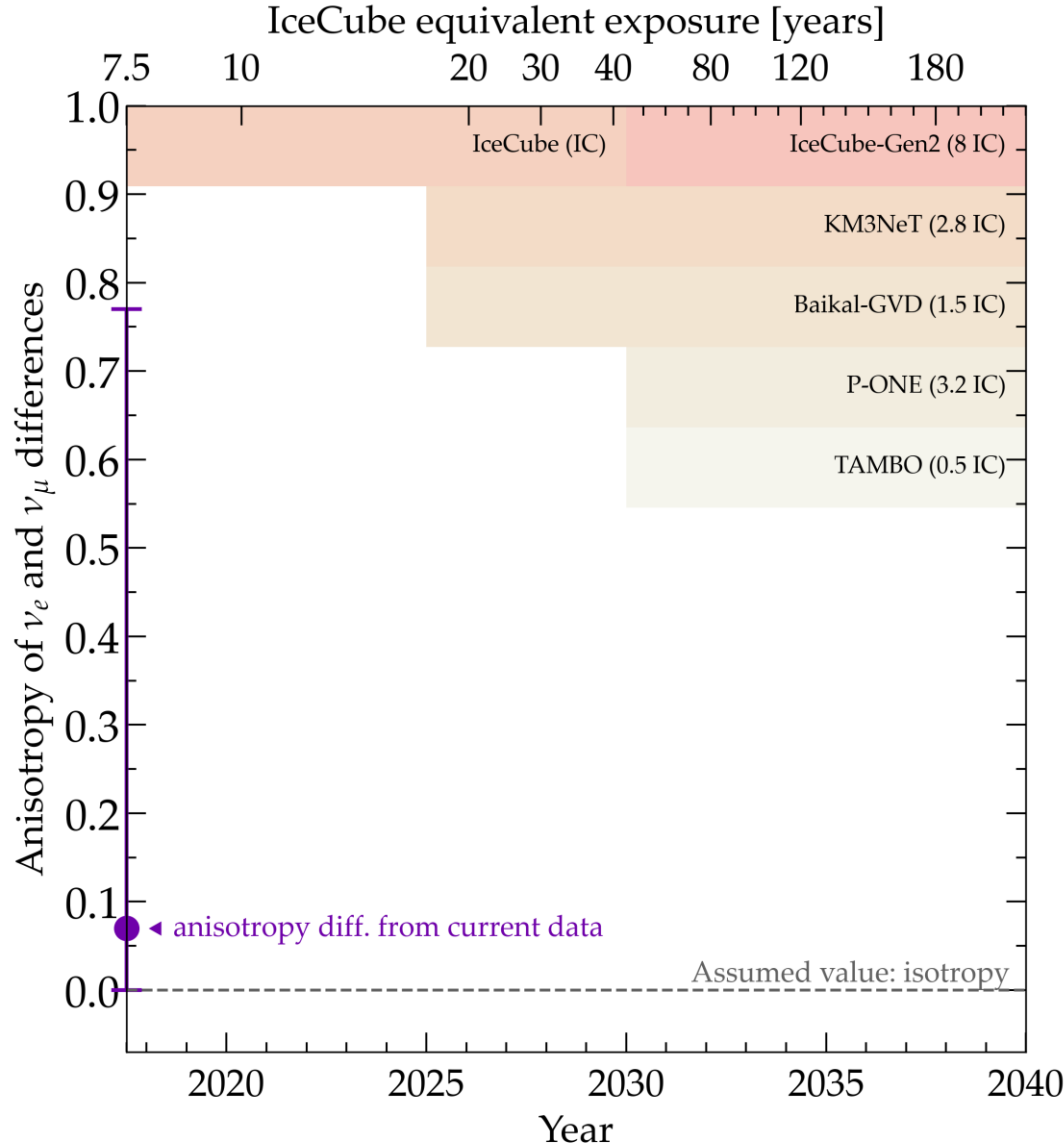
# How well can we constrain isotropy over time?



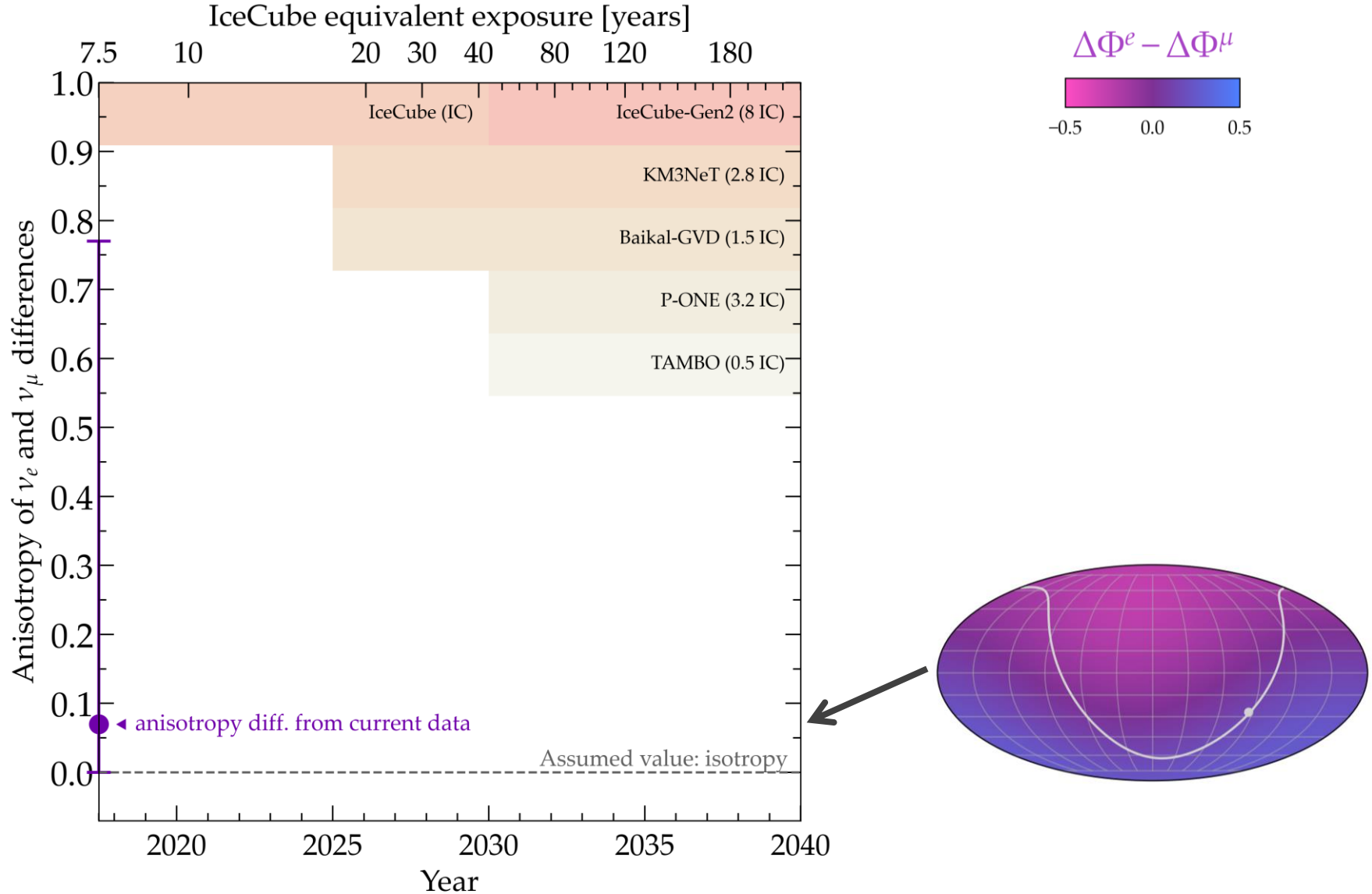
# How well can we constrain isotropy over time?



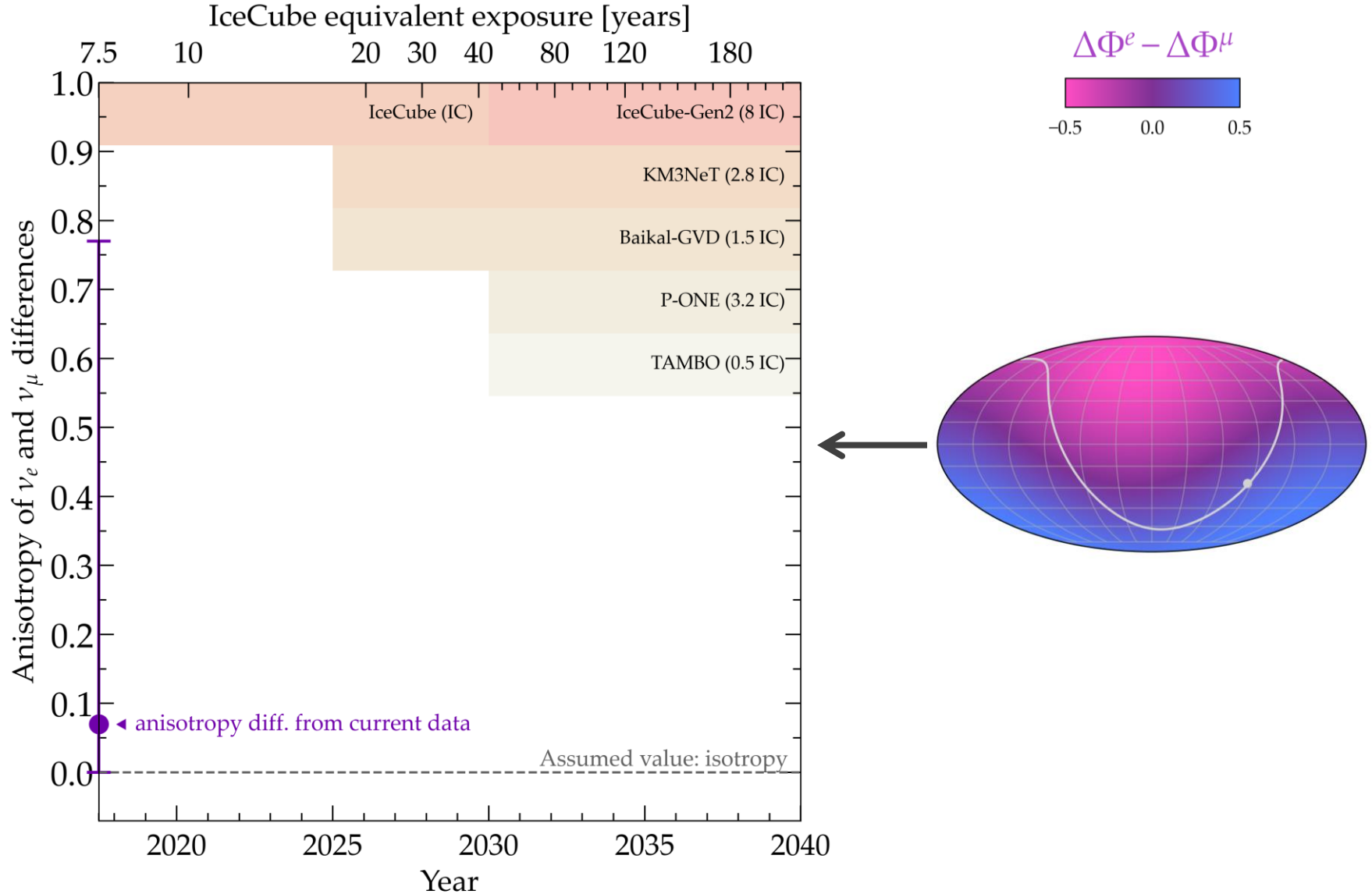
# How well can we constrain isotropy over time?



# How well can we constrain isotropy over time?

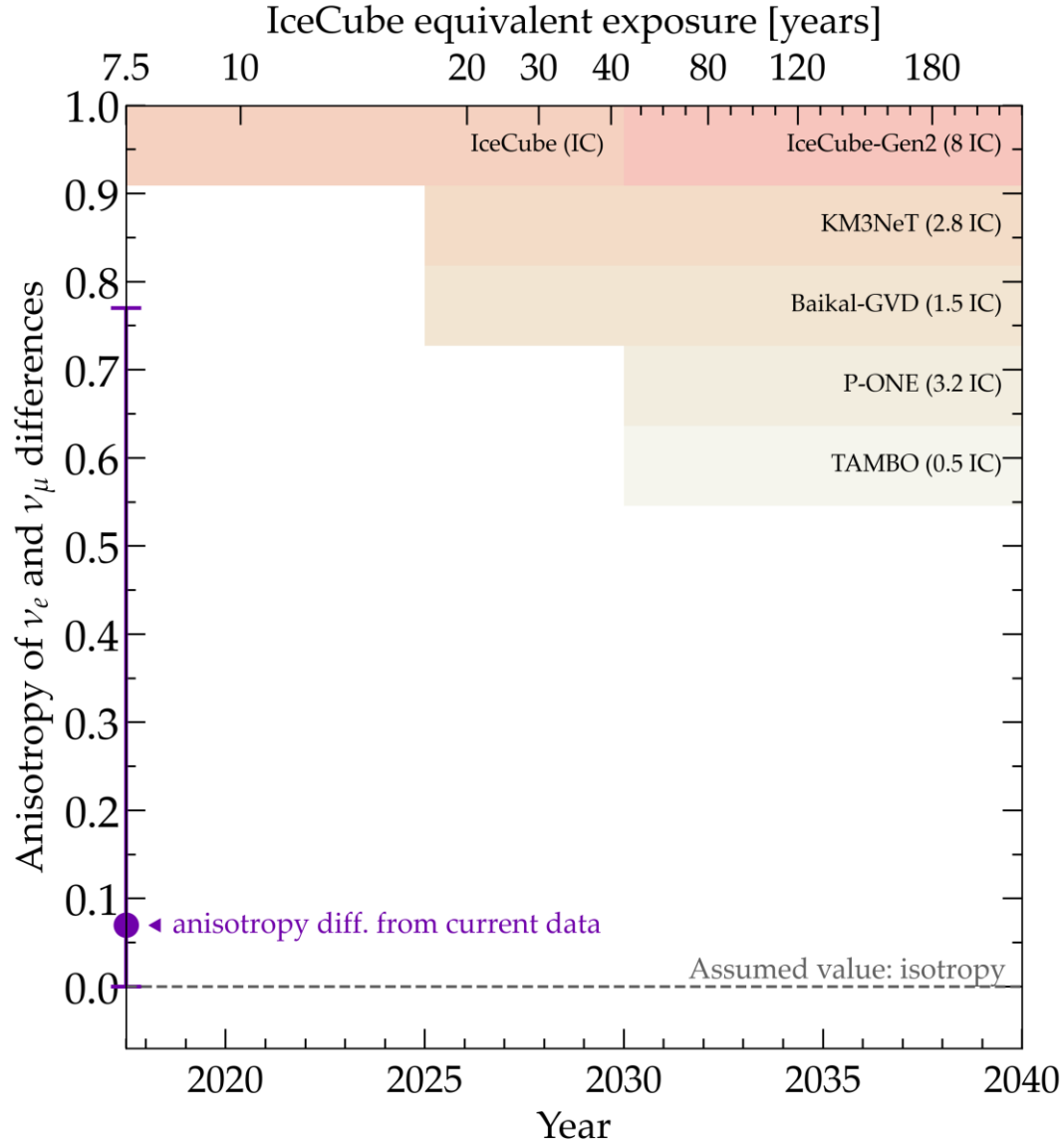


# How well can we constrain isotropy over time?

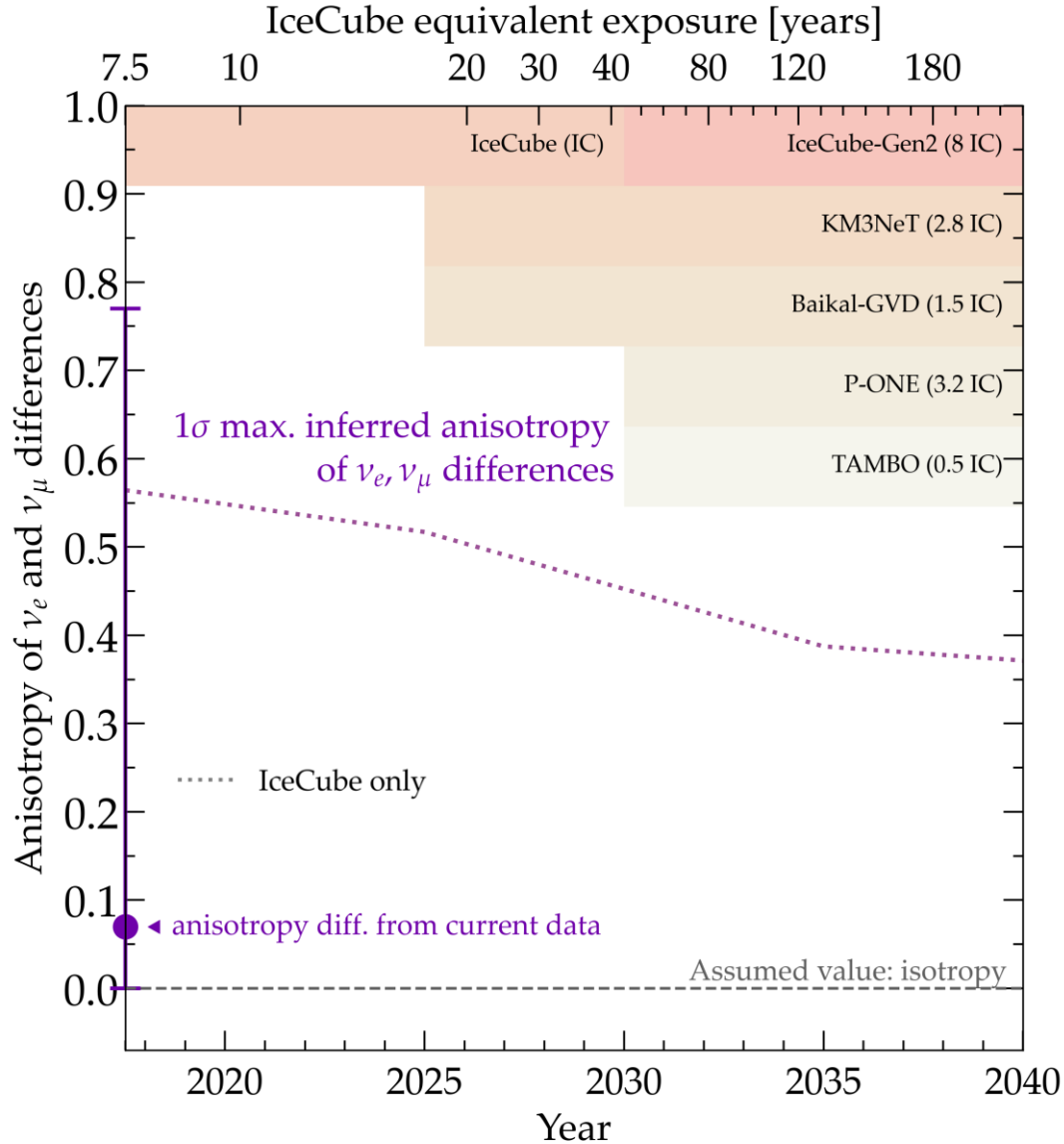




# How well can we constrain isotropy over time?



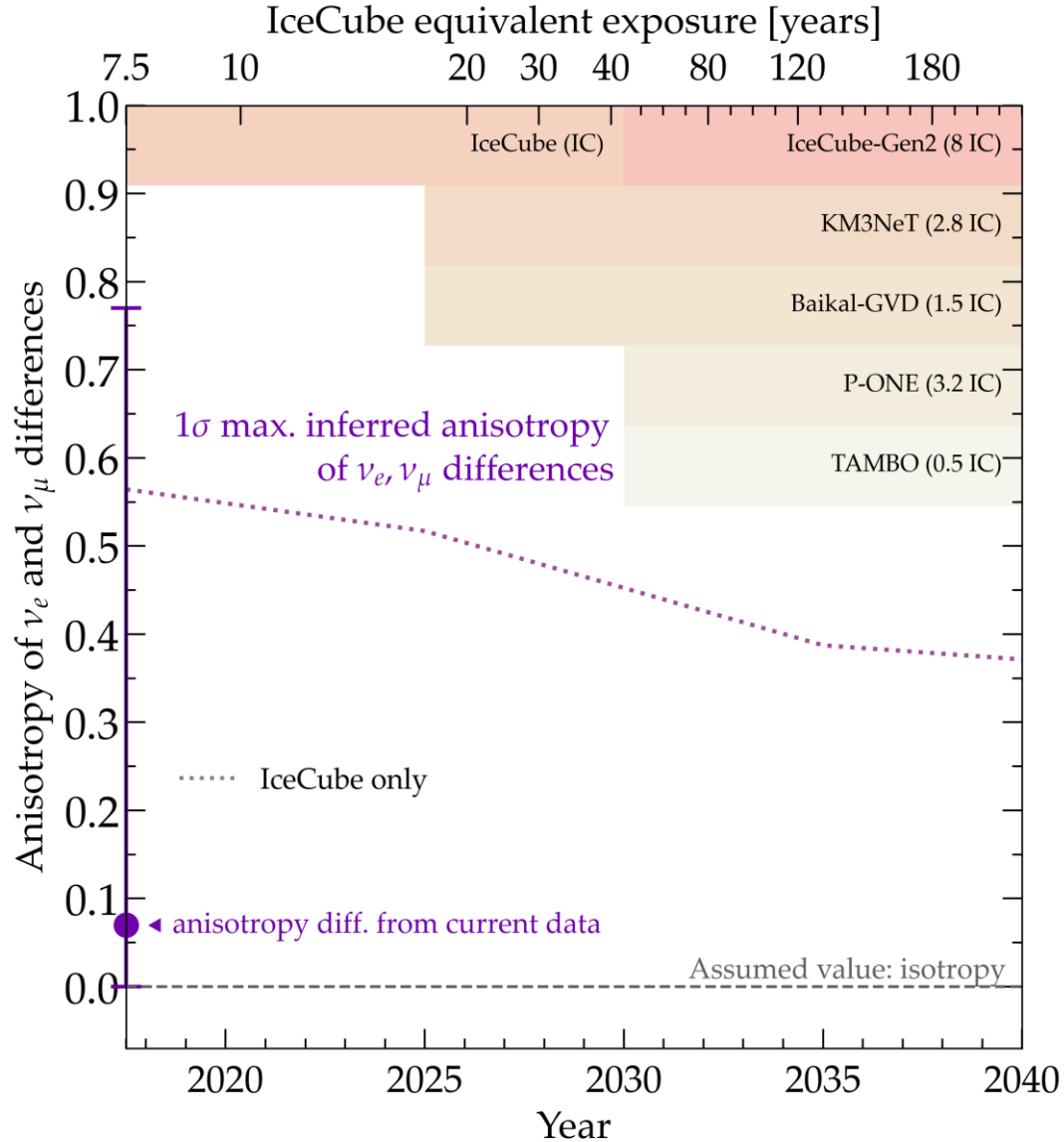
# How well can we constrain isotropy over time?



## Improvement by 2040:

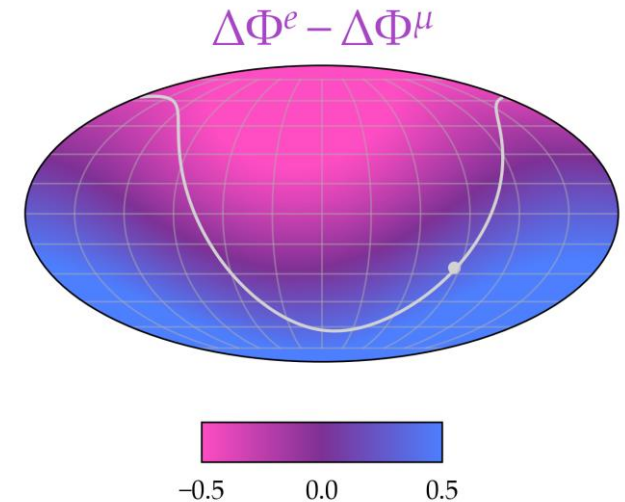
- IC only: 25%

# How well can we constrain isotropy over time?

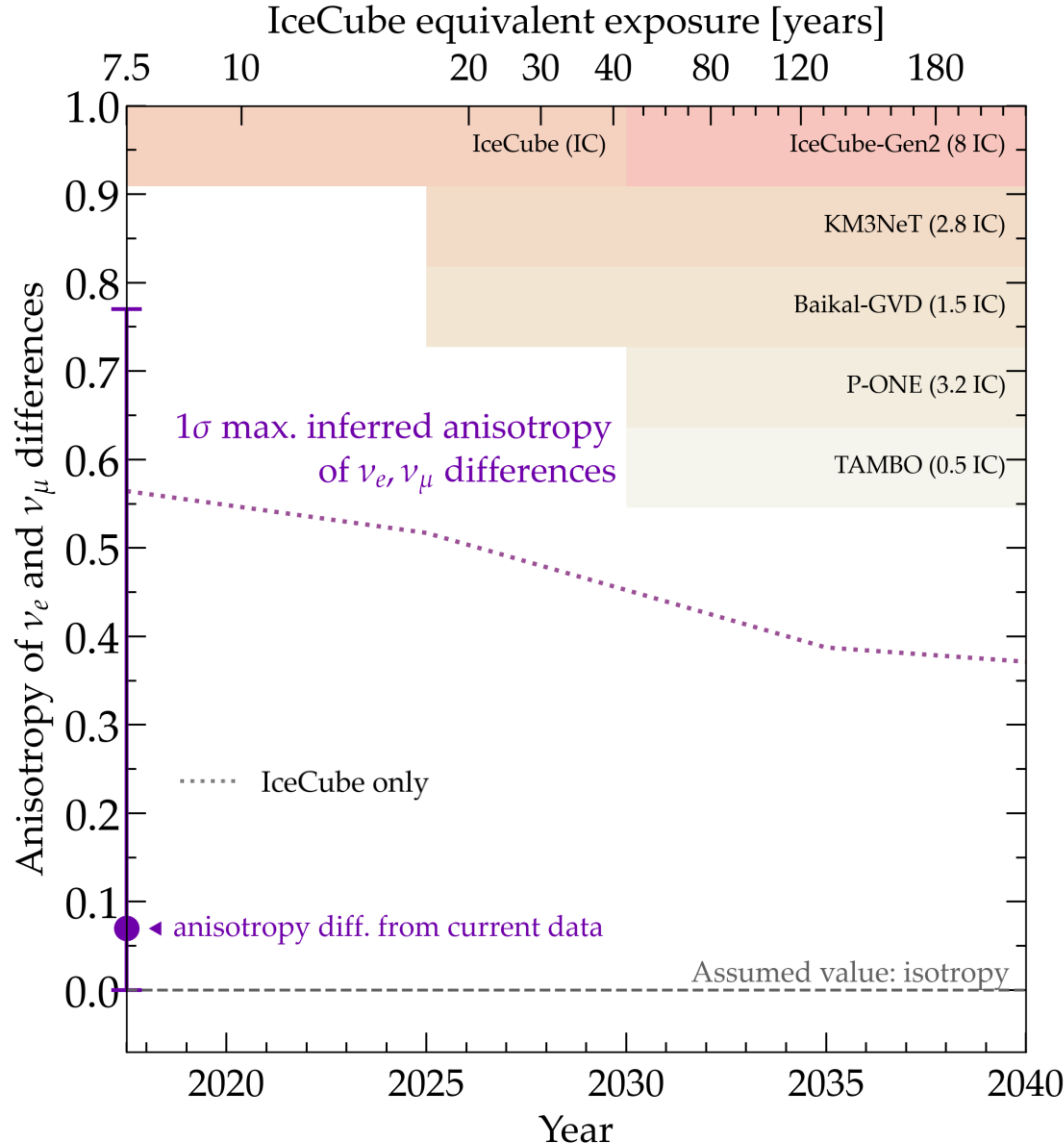


## Improvement by 2040:

- IC only: 25%

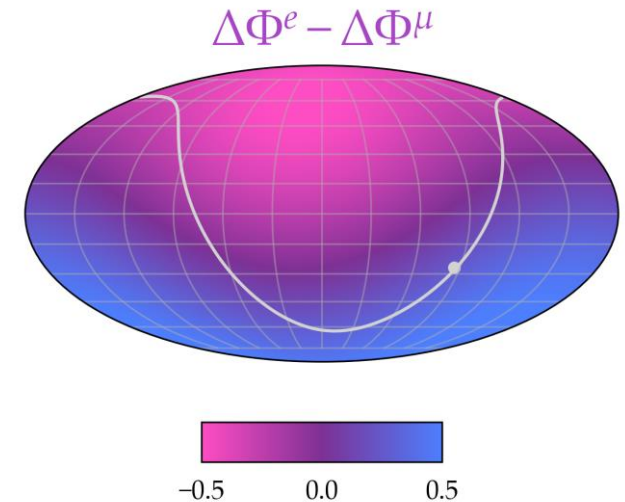


# How well can we constrain isotropy over time?

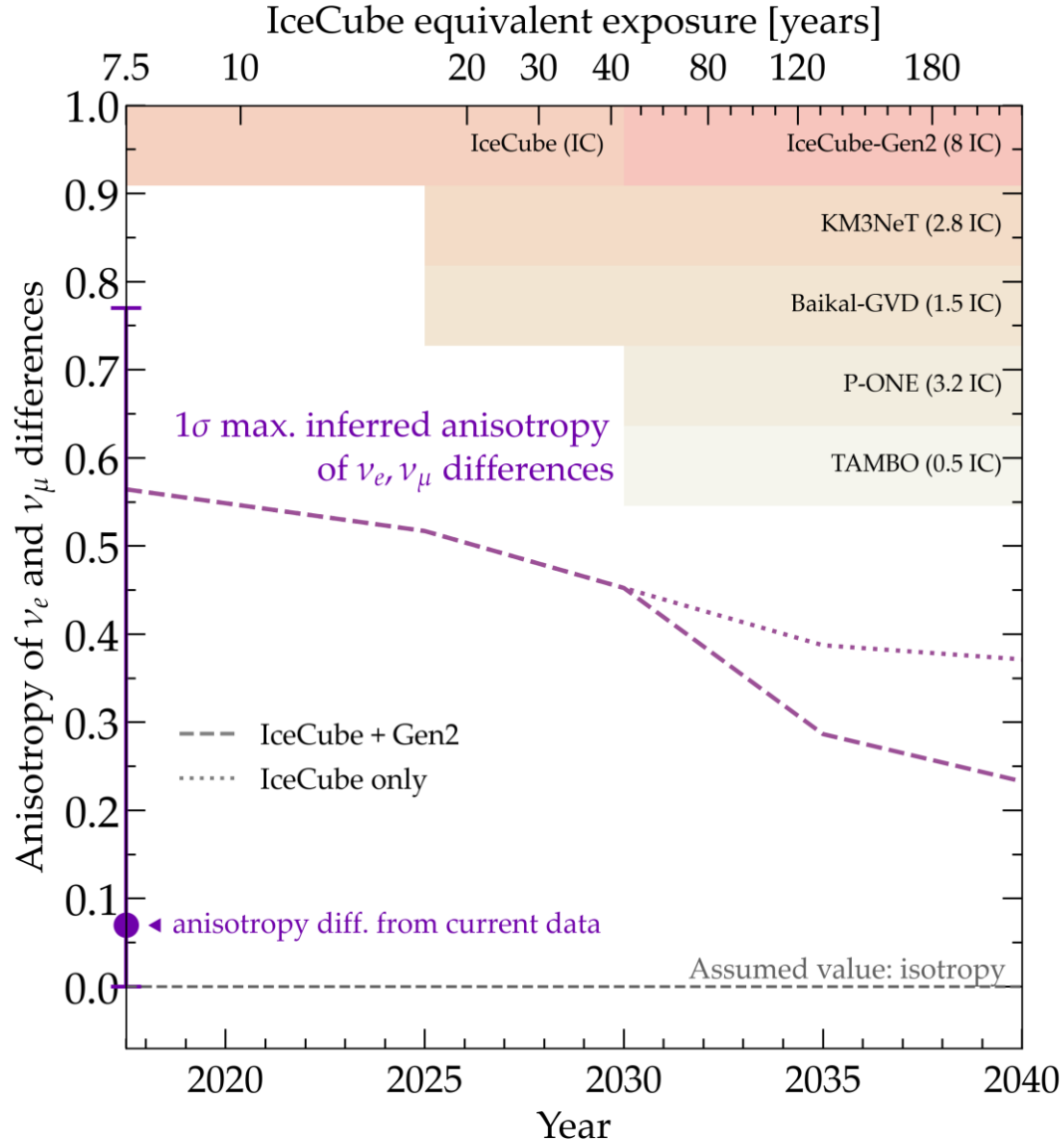


## Improvement by 2040:

- IC only: 25%

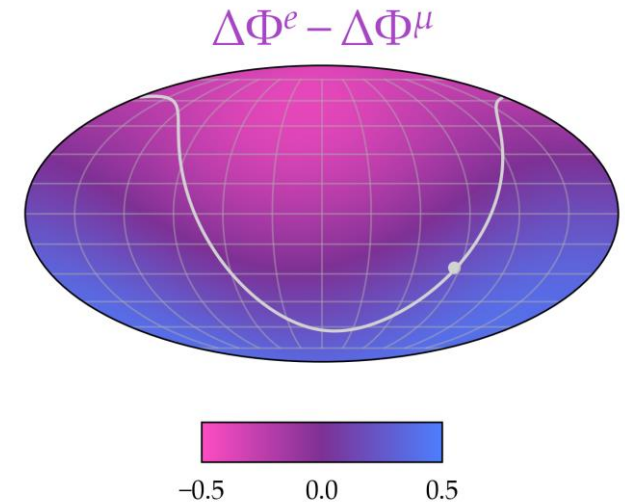


# How well can we constrain isotropy over time?

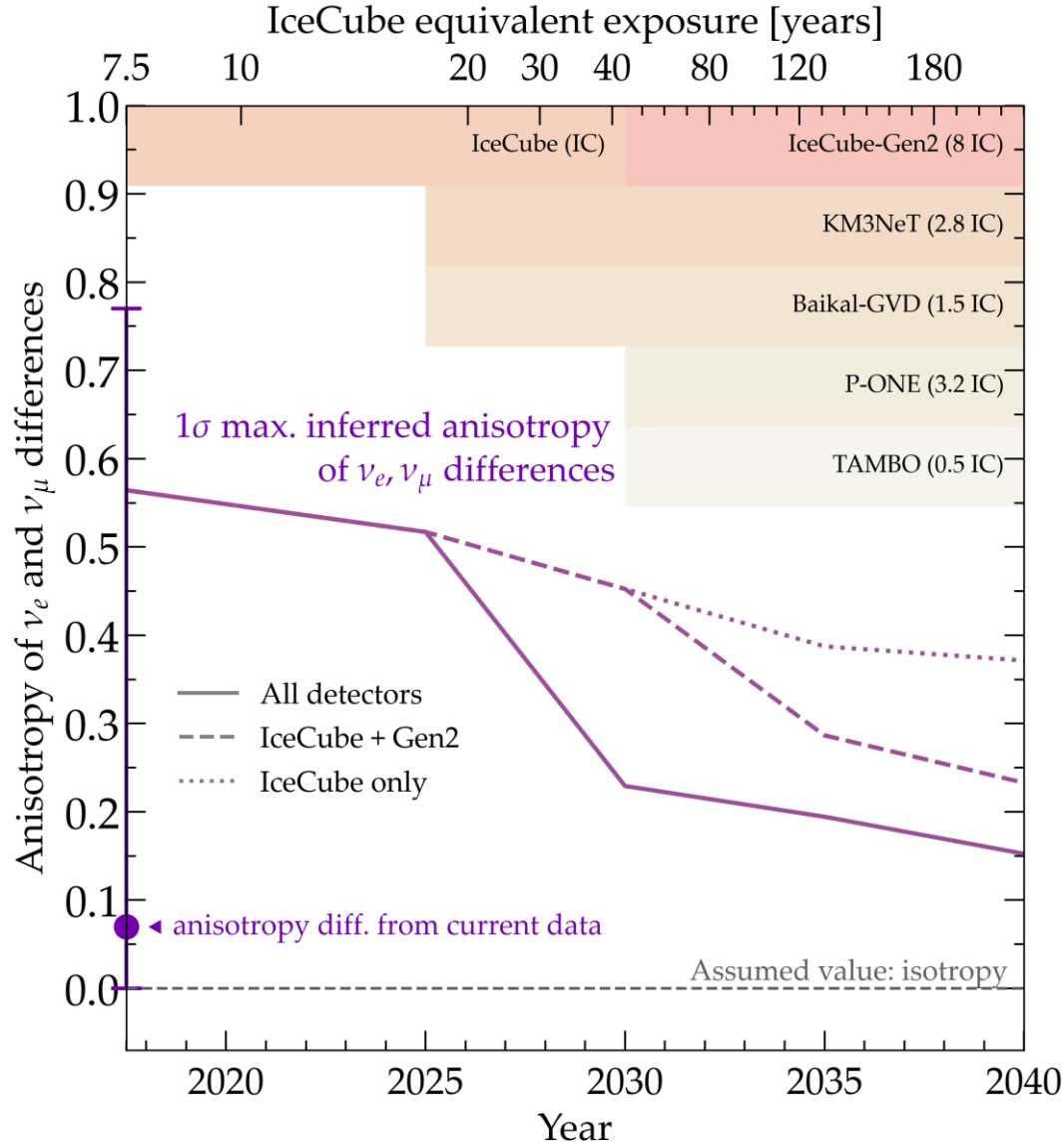


## Improvement by 2040:

- IC only: 25%
- IC + Gen2: 55%

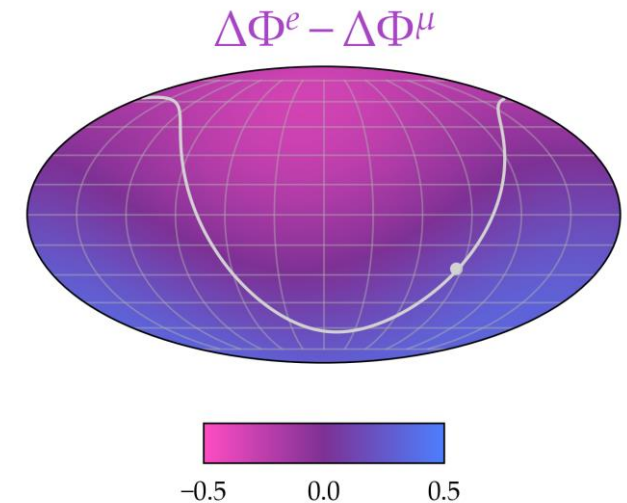


# How well can we constrain isotropy over time?

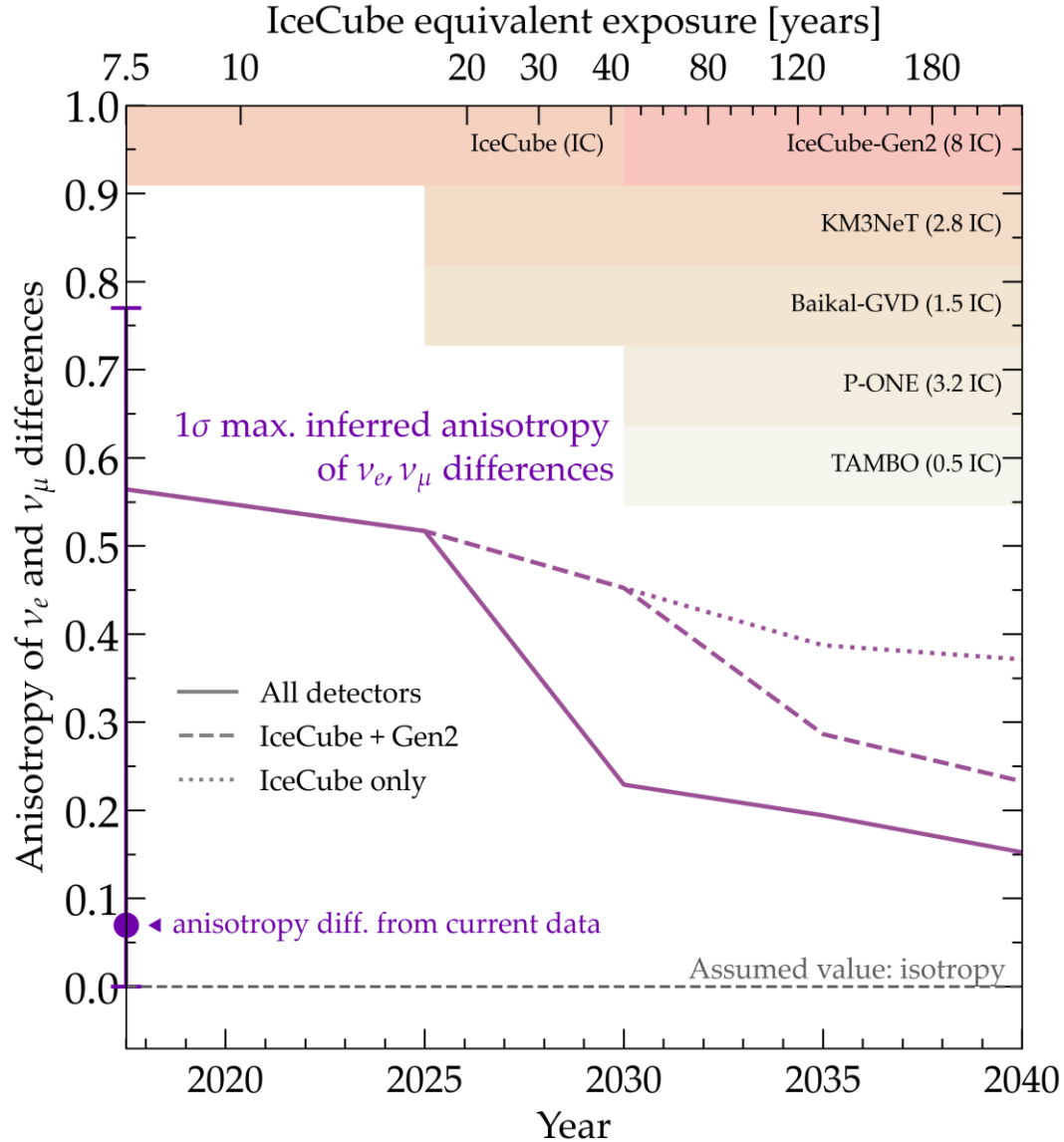


## Improvement by 2040:

- IC only: 25%
- IC + Gen2: 55%
- All detectors: 73%

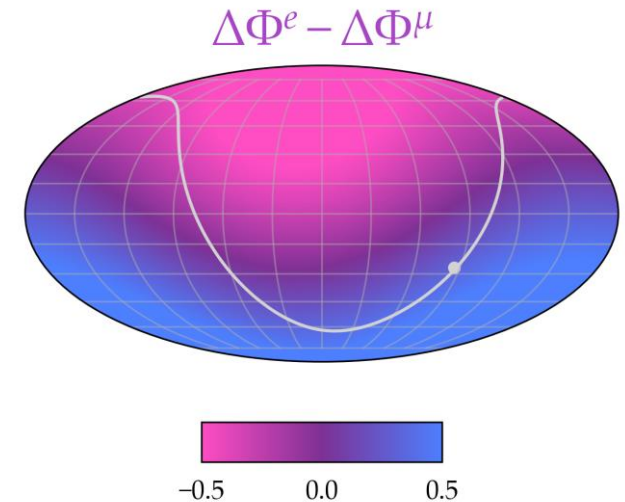


# How well can we constrain isotropy over time?

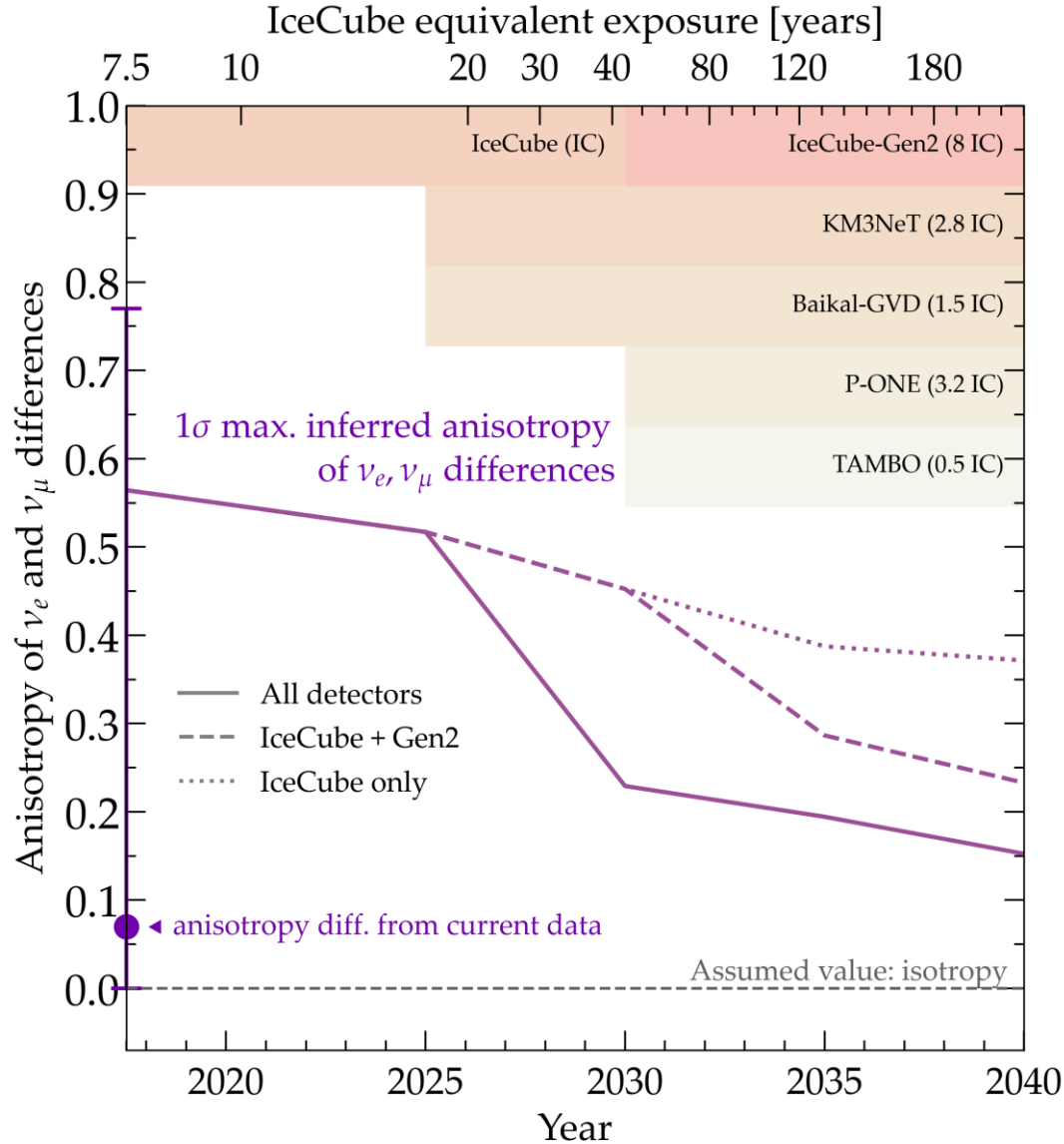


## Improvement by 2040:

- IC only: 25%
- IC + Gen2: 55%
- All detectors: 73%

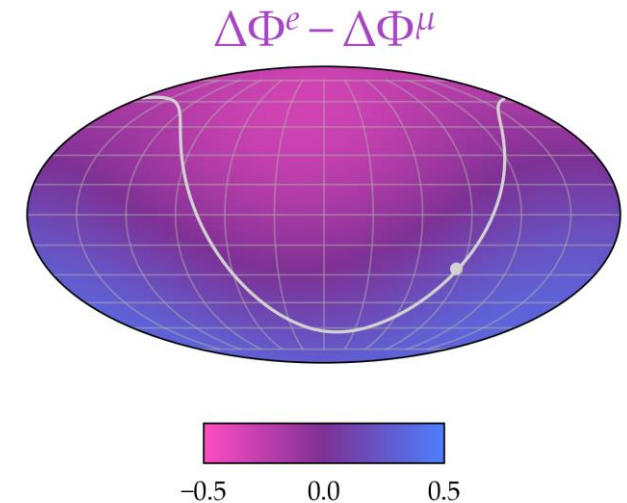


# How well can we constrain isotropy over time?



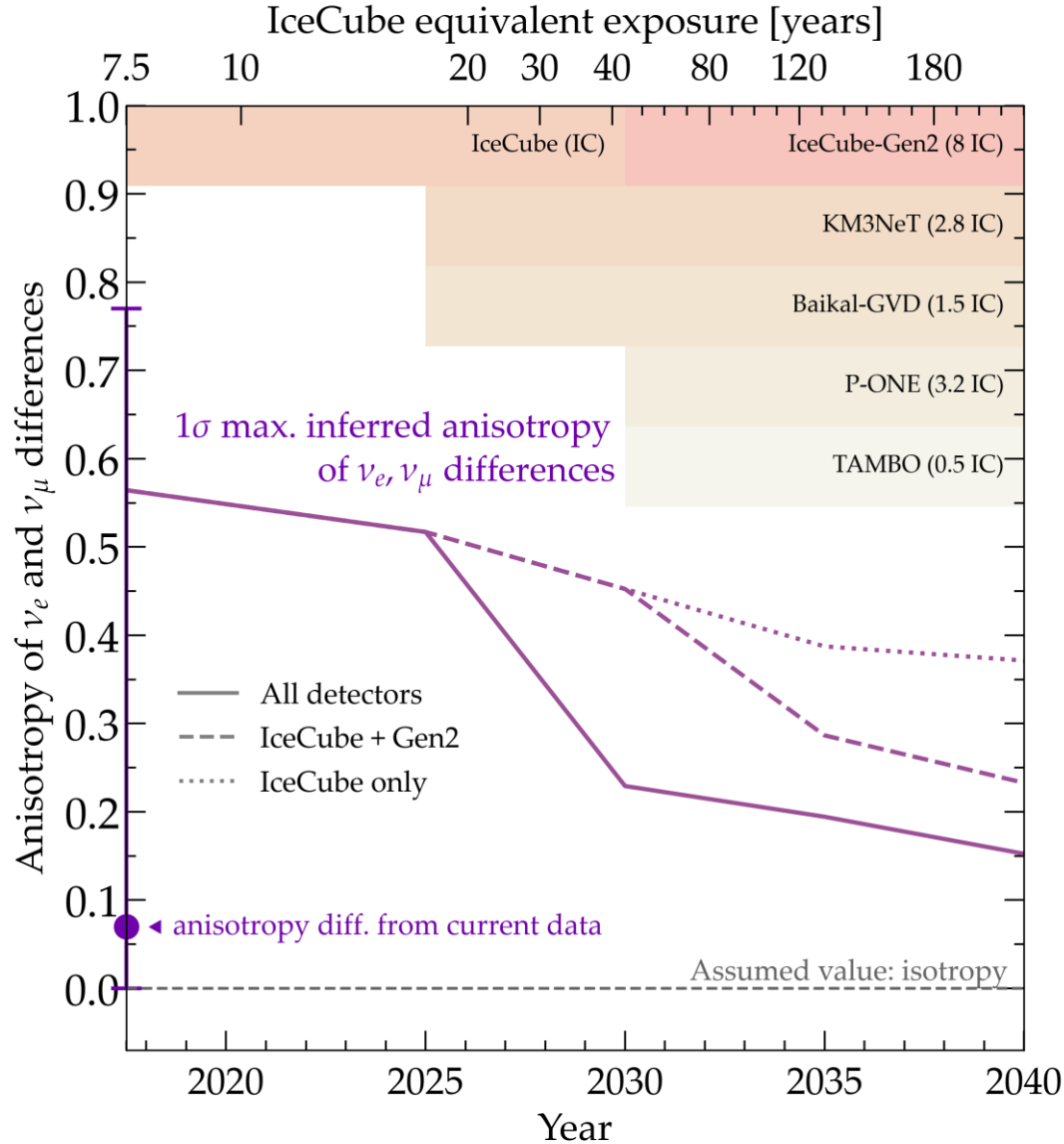
## Improvement by 2040:

- IC only: 25%
- IC + Gen2: 55%
- All detectors: 73%





# How well can we constrain isotropy over time?

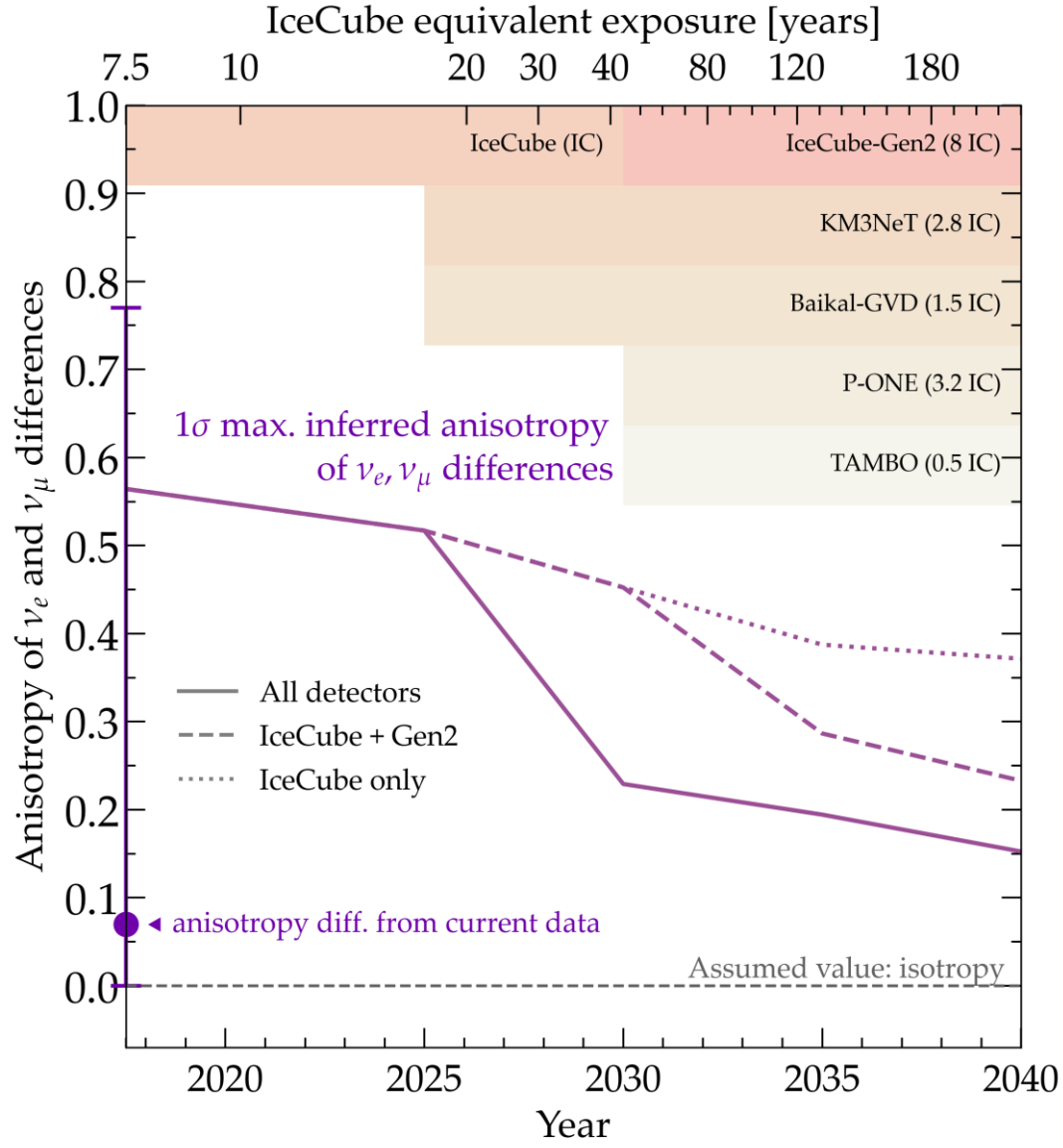


## Improvement by 2040:

- IC only: 25%
- IC + Gen2: 55%
- All detectors: 73%

Assuming IC-like sensitivity

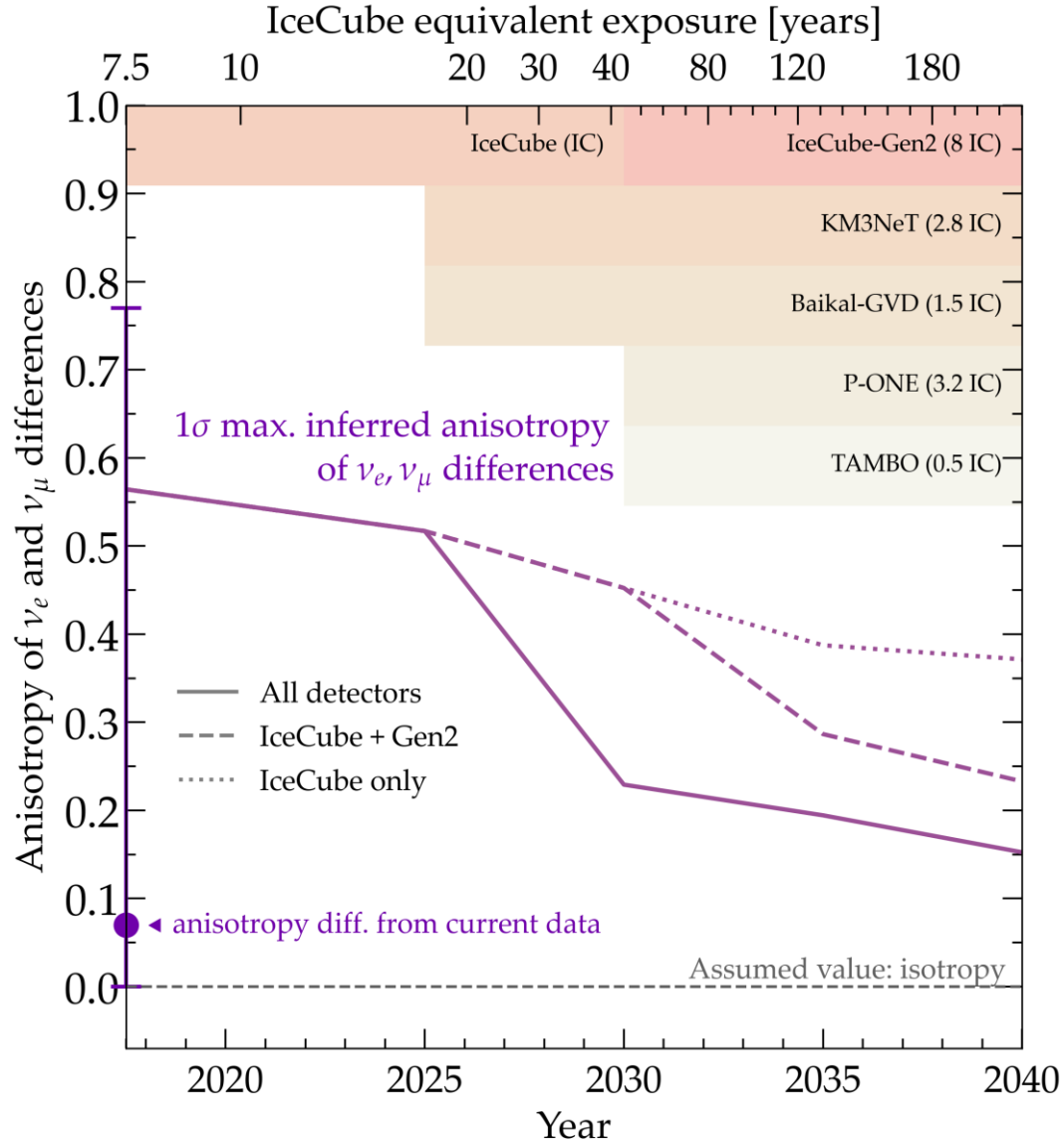
# How well can we constrain isotropy over time?



## How anisotropic is LIV?



# How well can we constrain isotropy over time?

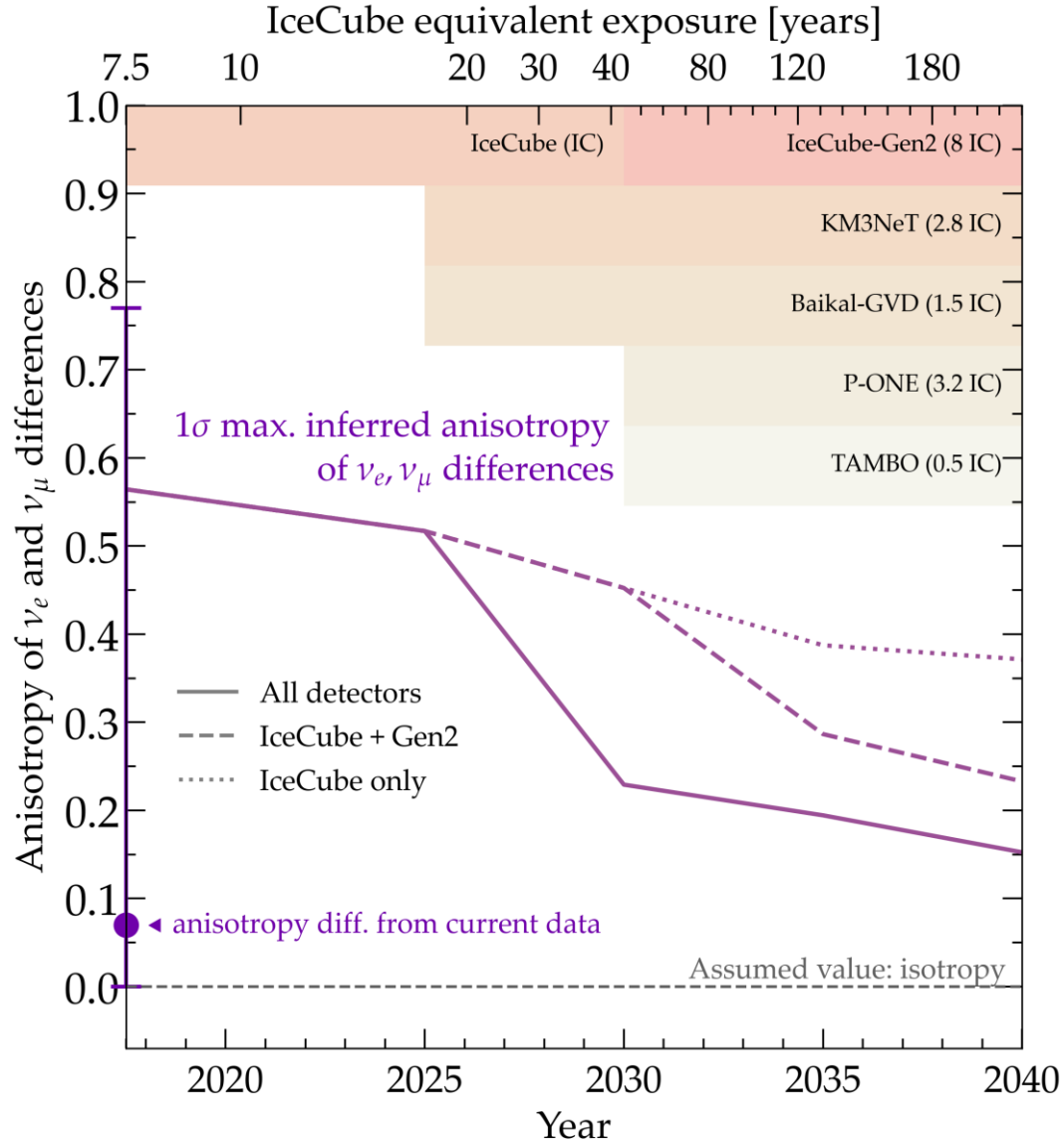


How anisotropic is LIV?

What about other BSM anisotropies?



# How well can we constrain isotropy over time?



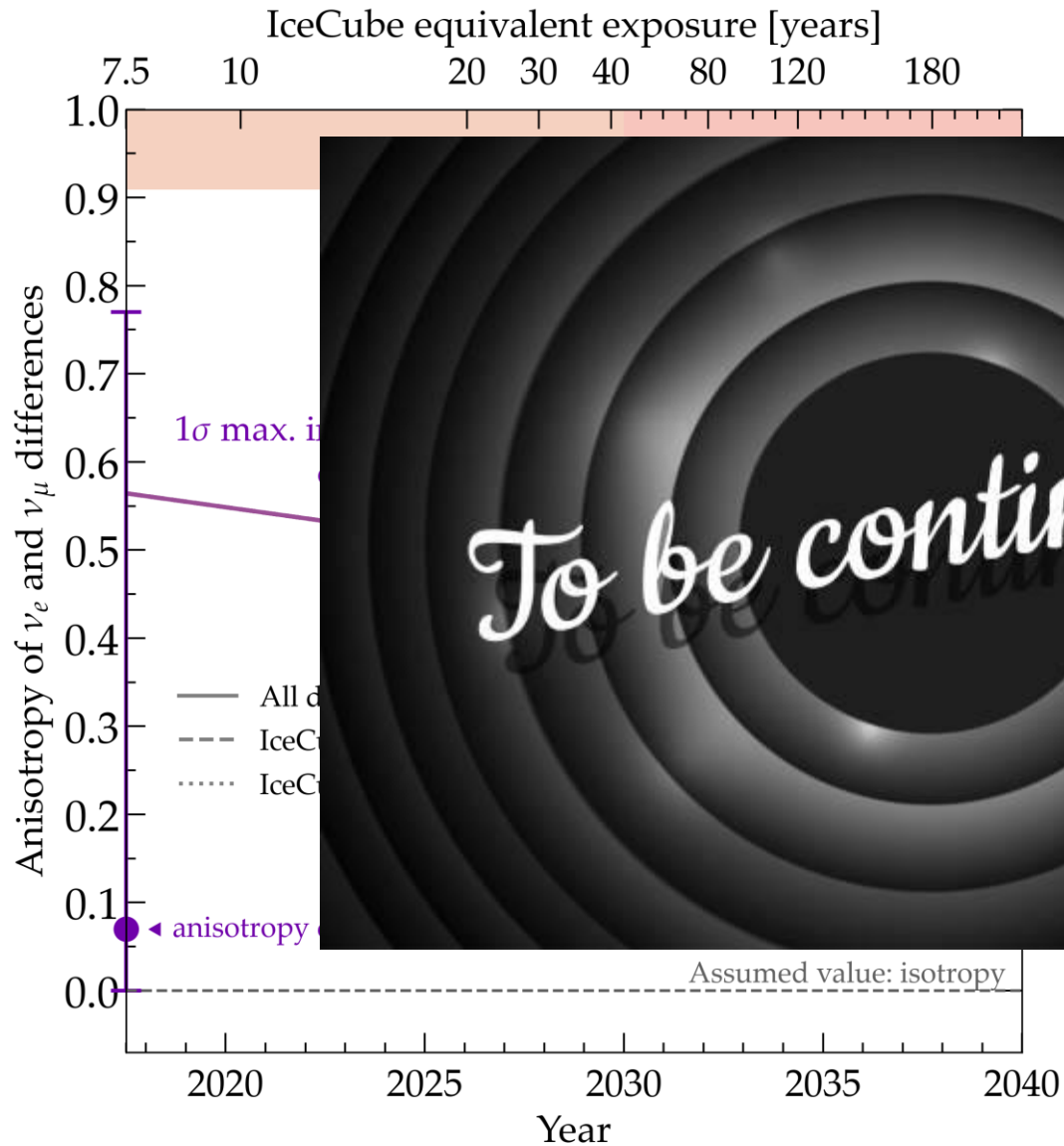
How anisotropic is LIV?

What about other BSM anisotropies?

How well can we constrain them with flavour ratios?



# How well can we constrain isotropy over time?



Is LIV?

BSM

re

with



Thanks!

Questions?



# References

- R. Abbasi *et al.* (IceCube), The IceCube high-energy starting event sample: Description and flux characterization with 7.5 years of data, Phys. Rev. D **104**, 022002 (2021), arXiv:2011.03545 [astro-ph.HE].
- IceCube Collaboration, HESE 7.5 year data release, <https://icecube.wisc.edu/data-releases/2021/12/hese-7-5-year-data/> (2021).
- Sungwook E. Hong *et al.*, Revealing the Local Cosmic Web from Galaxies by Deep Learning, Astrophys.J. **913**, 1, 76 (2021), arXiv:2008.01738 [astro-ph.CO]



“We don't expect anisotropies in flavour ratios”

$$\Delta\Phi_\alpha = \sum_{\ell>0,m} a_{\ell,m}^\alpha Y_{\ell,m}$$

Take the difference:

$$\delta a_{\ell,m}^{\alpha,\beta} = a_{\ell,m}^\alpha - a_{\ell,m}^\beta$$





# Quantifying anisotropy

$$\Delta\Phi_\alpha = \sum_{\ell>0,m} a_{\ell,m}^\alpha Y_{\ell,m}$$

The anisotropy measure (power spectrum):



# Quantifying anisotropy

$$\Delta\Phi_\alpha = \sum_{\ell>0,m} a_{\ell,m}^\alpha Y_{\ell,m}$$

The anisotropy measure (power spectrum):

$$C_\ell^\alpha = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell,m}^\alpha|^2$$



# Quantifying anisotropy

$$\Delta\Phi_\alpha = \sum_{\ell>0,m} a_{\ell,m}^\alpha Y_{\ell,m}$$

The anisotropy measure (power spectrum):

$$C_\ell^\alpha = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell,m}^\alpha|^2$$

$$\Delta C_\ell^{\alpha,\beta} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |\delta a_{\ell,m}^{\alpha,\beta}|^2$$



# How do we recover the flux?

Using Ice Cube Monte Carlo. We need:



Data



Model



Monte Carlo



Model parameters



Repetition

# How do we recover the flux?

We do:

sample parameter space



Monte Carlo re-weigh



bad fit

good fit



repeat

