



Classification of ESSnuSB WC Near Detector Events Using Graph Neural Networks

ν_{μ} - and ν_e -events for neutrino oscillation studies

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Outline

- Neutrino Physics
- Experiment and Motivation

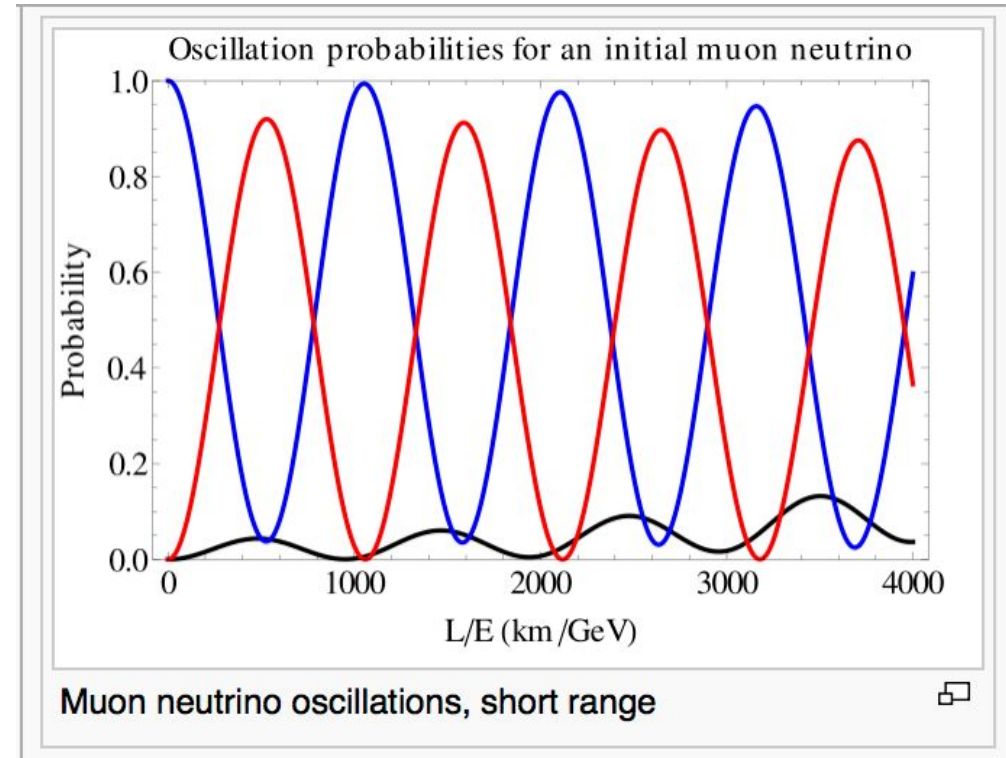
- Performance on Charged Lepton Simulations
- Performance on Full Neutrino Simulations
- Investigation of Performance Differences

Neutrino Physics

Neutrino Physics

- Neutrinos **oscillate!**

■ ν_{μ}
■ ν_{τ}
■ ν_e



Neutrino Physics

$$\begin{aligned}
 P_{\nu_\mu \rightarrow \nu_e (\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} &\simeq 4s_{23}^2 s_{13}^2 \frac{1}{(1-r_A)^2} \sin^2 \frac{(1-r_A)\Delta L}{2} \\
 &+ 8J_r \frac{r_\Delta}{r_A(1-r_A)} \cos\left(\delta_{CP} - \frac{\Delta L}{2}\right) \sin \frac{r_A \Delta L}{2} \sin \frac{(1-r_A)\Delta L}{2} \\
 &+ 4c_{23}^2 c_{12}^2 s_{12}^2 \left(\frac{r_\Delta}{r_A}\right)^2 \sin^2 \frac{r_A \Delta L}{2}
 \end{aligned}$$

$$J_r \equiv c_{12}s_{12}c_{23}s_{23}s_{13}, \Delta \equiv \frac{\Delta m_{31}^2}{2E_\nu}, r_A \equiv \frac{a}{\Delta m_{31}^2}, r_\Delta \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2}, a = 2\sqrt{2}G_F N_e E_\nu$$

Neutrino Physics

$$P_{\nu_\mu \rightarrow \nu_e}(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \simeq 4s_{23}^2 s_{13}^2 \frac{1}{(1-r_A)^2} \sin^2 \frac{(1-r_A)\Delta L}{2}$$

“atmospheric”

$$+8J_r \frac{r_\Delta}{r_A(1-r_A)} \cos\left(\delta_{CP} - \frac{\Delta L}{2}\right) \sin \frac{r_A \Delta L}{2} \sin \frac{(1-r_A)\Delta L}{2}$$

“interference”

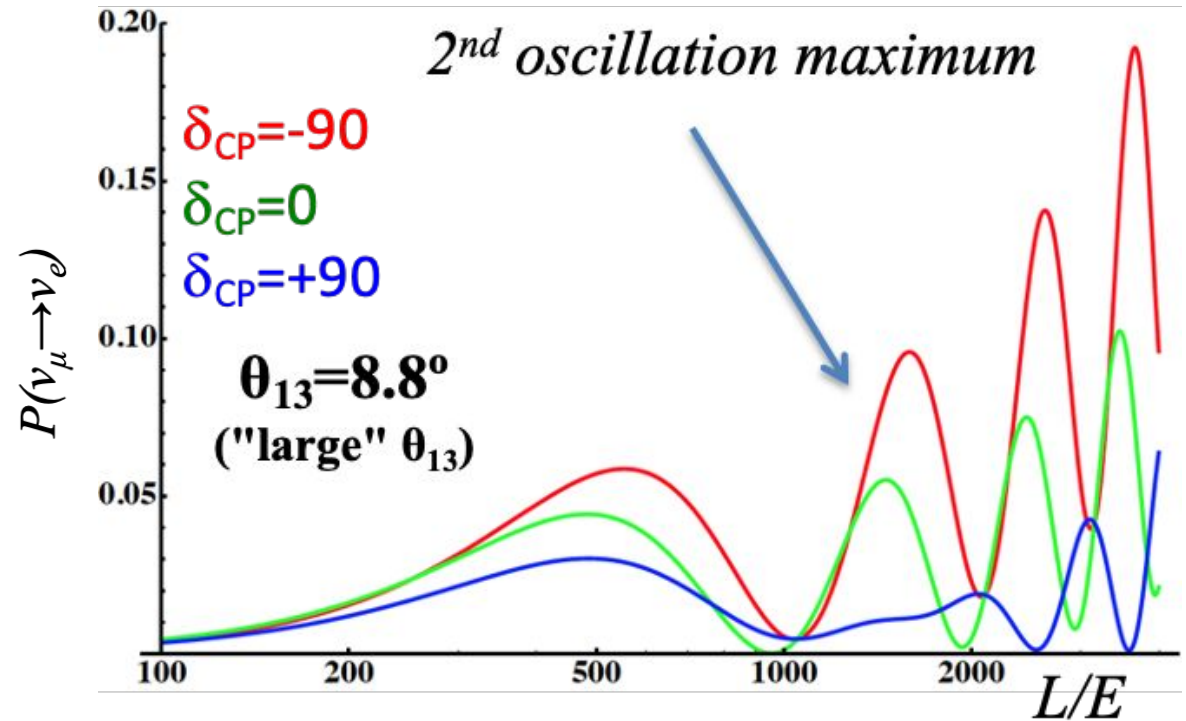
$$+4c_{23}^2 c_{12}^2 s_{12}^2 \left(\frac{r_\Delta}{r_A}\right)^2 \sin^2 \frac{r_A \Delta L}{2}$$

“solar”

$$J_r \equiv c_{12} s_{12} c_{23} s_{23} s_{13}, \Delta \equiv \frac{\Delta m_{31}^2}{2E_\nu}, r_A \equiv \frac{a}{\Delta m_{31}^2}, r_\Delta \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2}, a = 2\sqrt{2}G_F N_e E_\nu$$

Neutrino Physics

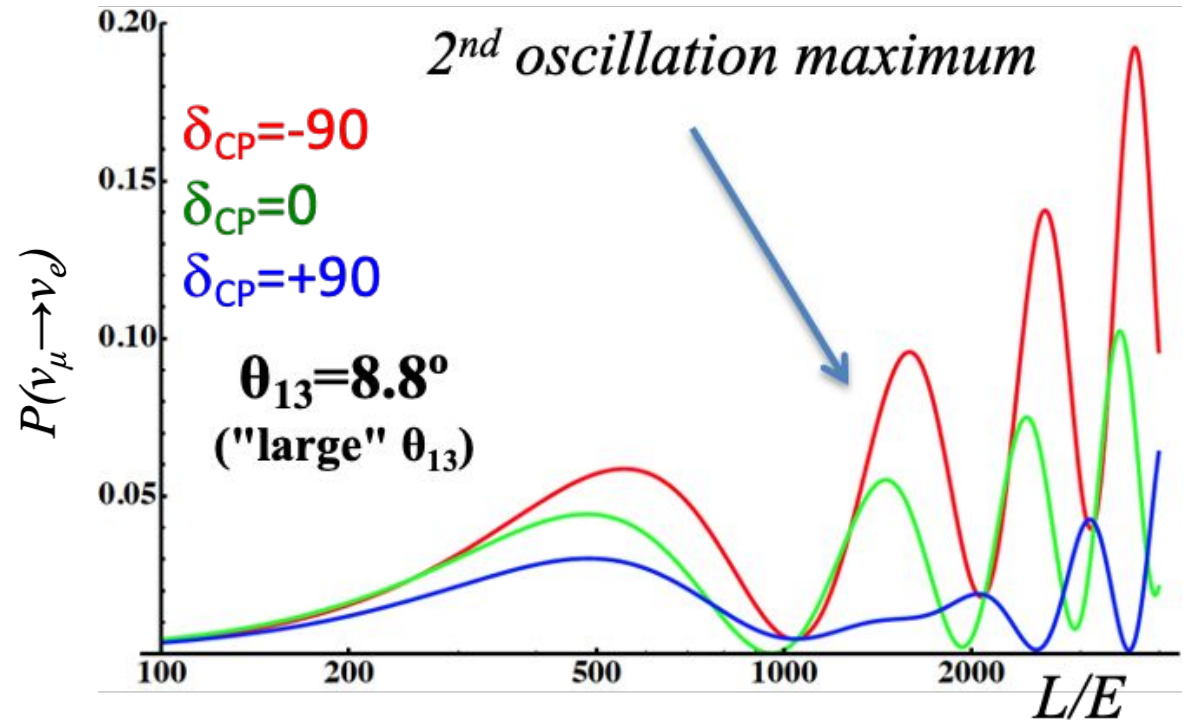
1st oscillation max: $A=0.3\sin\delta_{\text{CP}}$
2nd oscillation max: $A=0.75\sin\delta_{\text{CP}}$



[M. Dracos, NuFact2022](#)

Neutrino Physics

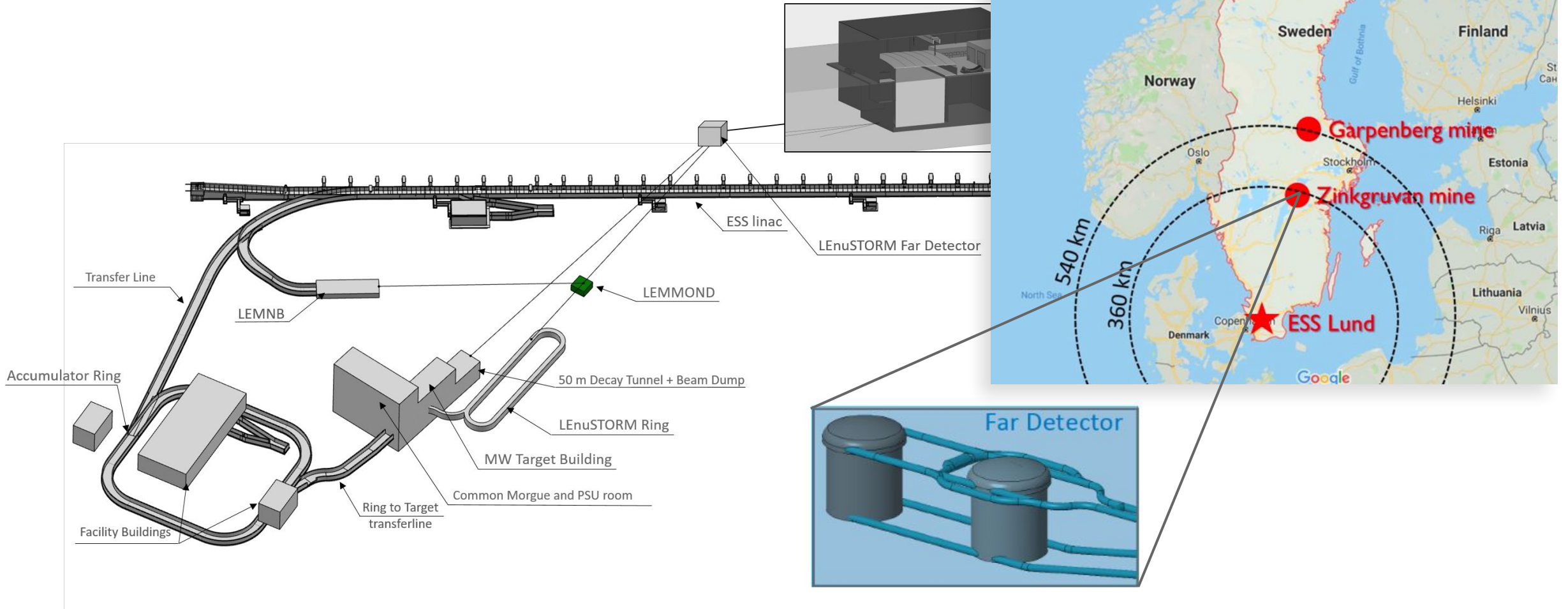
- Greater sensitivity to δ_{CP} at the second oscillation peak
- Within reach with the 5 MW proton beam produced at ESS



[M. Dracos, NuFact2022](#)

Experiment and Motivation

ESSnuSB - Detectors



Luckily, you are already Cherenkov detector experts!

Current Framework

Charged Lepton Simulations

WCSIM
<https://github.com/WCSim/WCSim>

Neutrino Interaction Simulations

GENIE
Generator. Nucl. Instrum. Meth. A 614:87–104, 2010

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LLH Based Reconstruction

fiTQun
J. Phys.: Conf. Ser. 888 012066, 2017

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Challenges

- Likelihood reconstruction takes ~1 min/event
- To explore different detector proposals, fast reconstruction is crucial

Why Do We Need GNN Reconstruction?

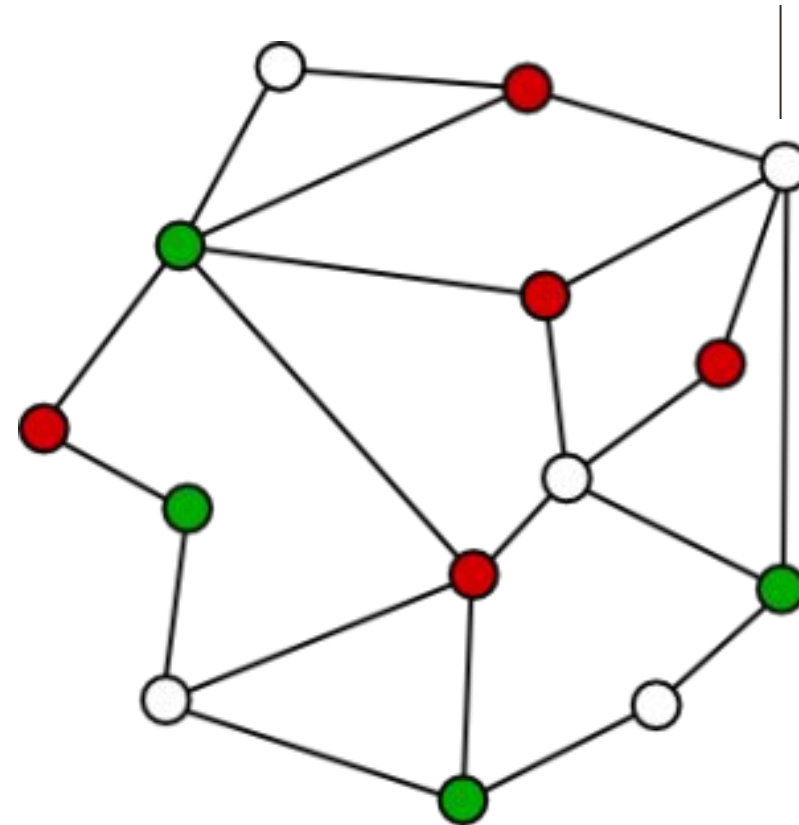
- **Fast and reliable** event reconstruction enables testing of different detector layouts
- LLH-based methods are accurate, but reconstruction is **slow**
- ML methods are **fast once trained**, GNNs are well suited for sparse events with irregular geometry
- Multiple reconstruction methods provide a way to **cross check and find systematic errors**

Setup

Graph Neural Networks (GNNs)

- Based on graph theory
- Each graph is a neutrino event
- Each data point is a node
- A node has features like xyz, time, charge
- Suited for non-euclidian data

Node = Data point
In our case a DOM hit



Graph Neural Networks - Framework



GraphNeT - Graph Neural Networks for Neutrino Telescopes

<https://github.com/graphnet-team/graphnet>

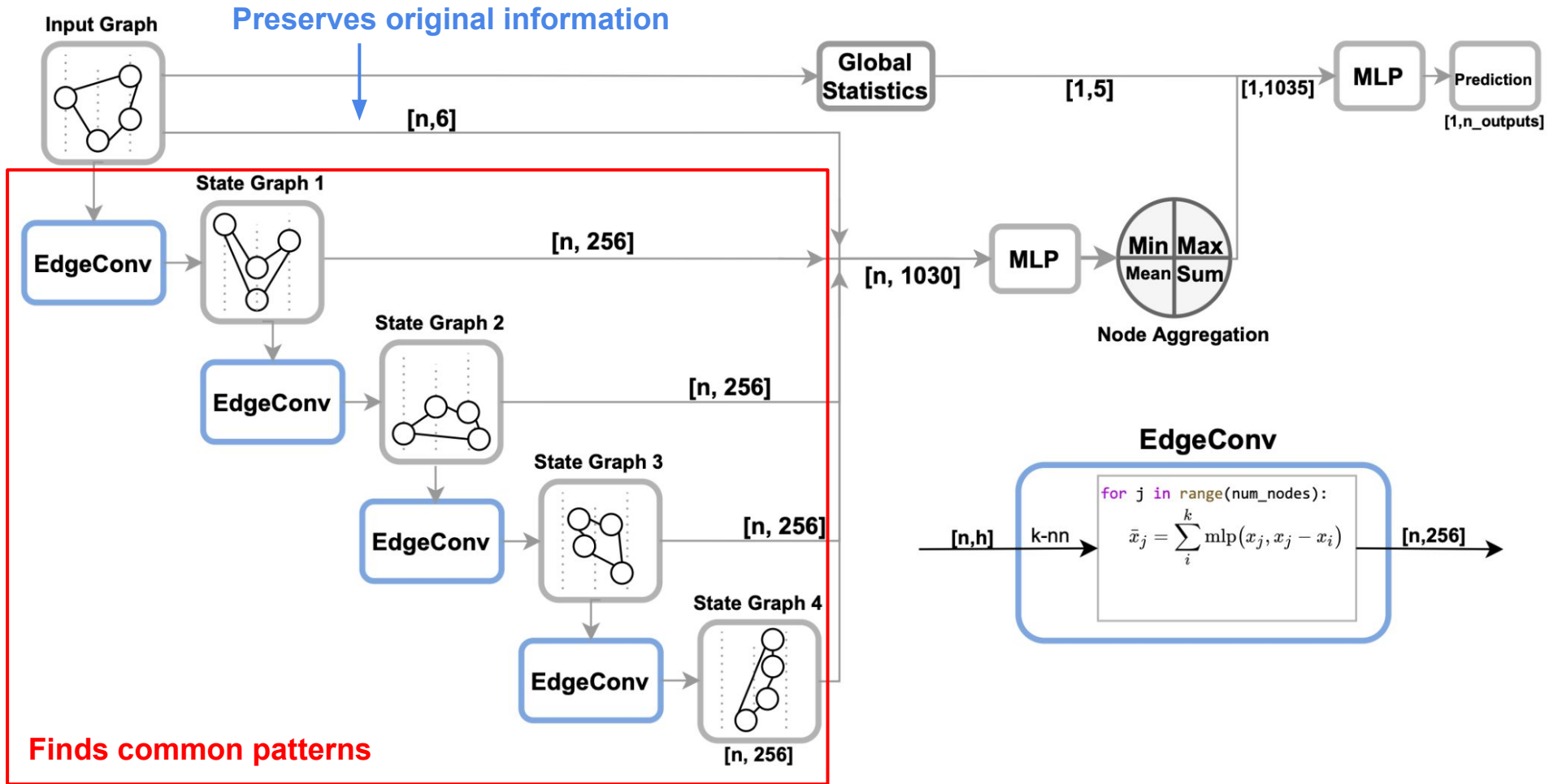
See plenary talk by Rasmus on Monday



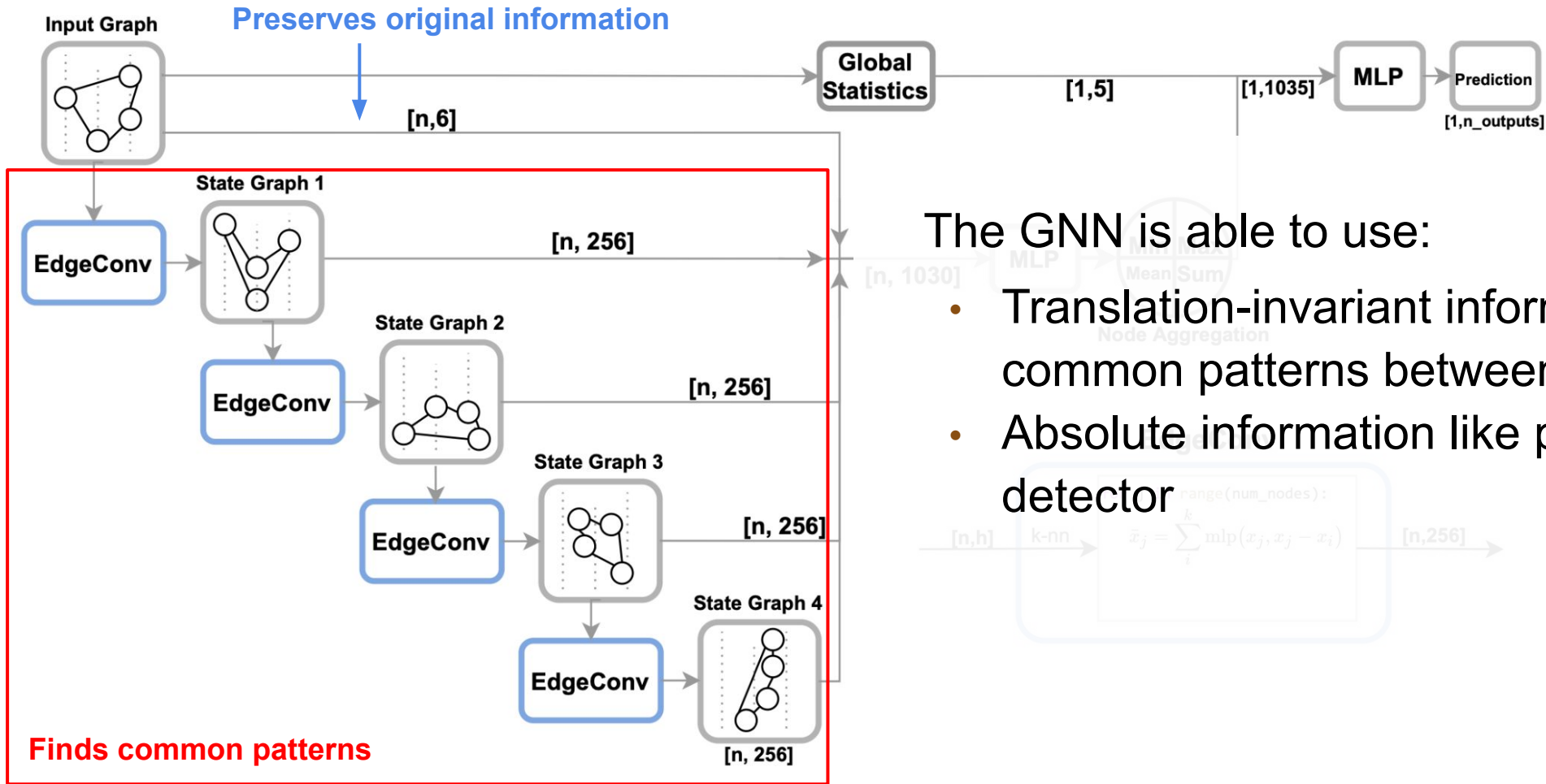
Pytorch Geometric - GNN framework for Pytorch

Model architecture: **DynEdge**

Graph Neural Networks - Architecture



Graph Neural Networks - Architecture



The GNN is able to use:

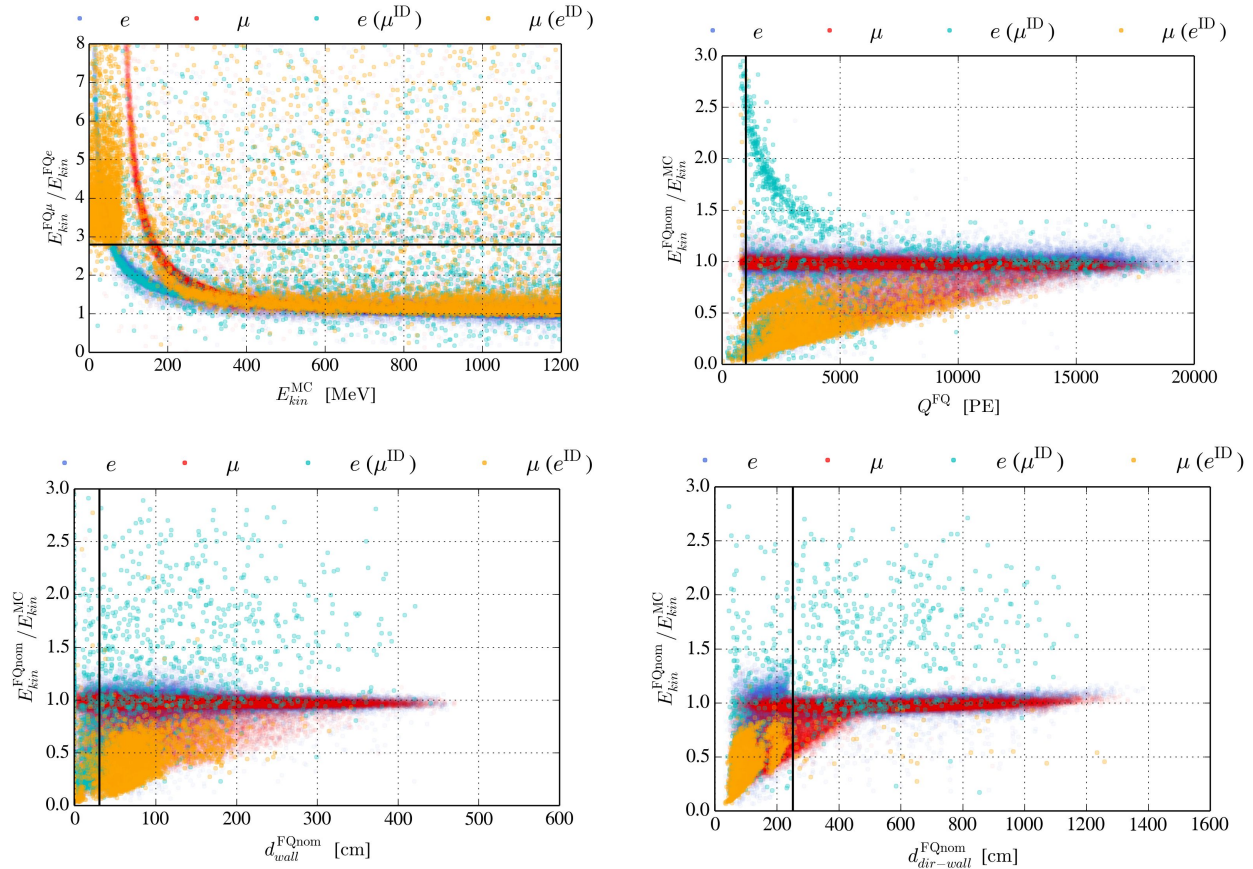
- Translation-invariant information about common patterns between events
- Absolute information like position in the detector

$$\bar{x}_j = \sum_{i \in \text{range}(\text{num_nodes})} \text{mlp}(x_j, x_j - x_i)$$

Data Processing and Performance Measures

Data processing

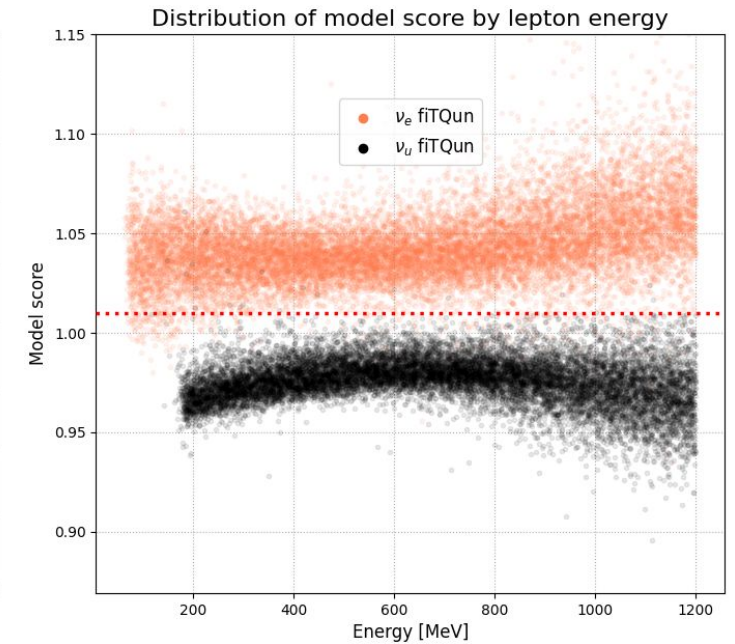
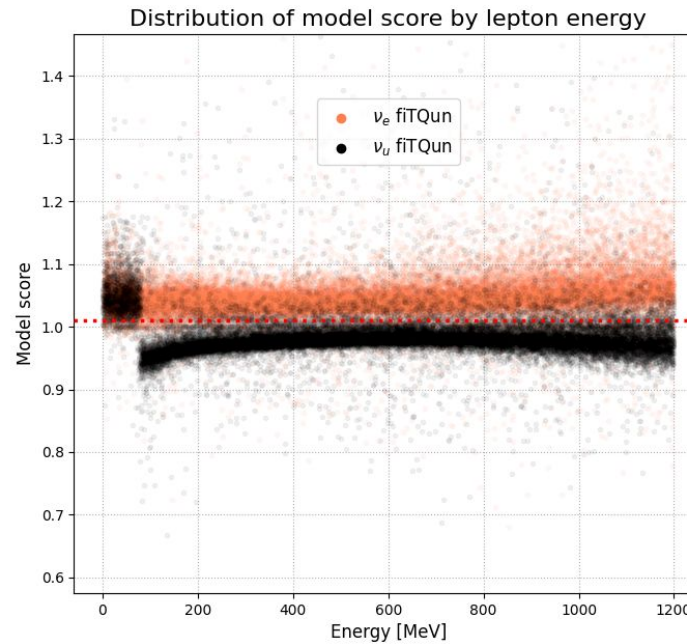
- Cuts based on reconstructed variables
- Removes events that are hard to classify
- Reduces events by a factor ~ 2



The European Spallation Source neutrino Super Beam Conceptual Design Report

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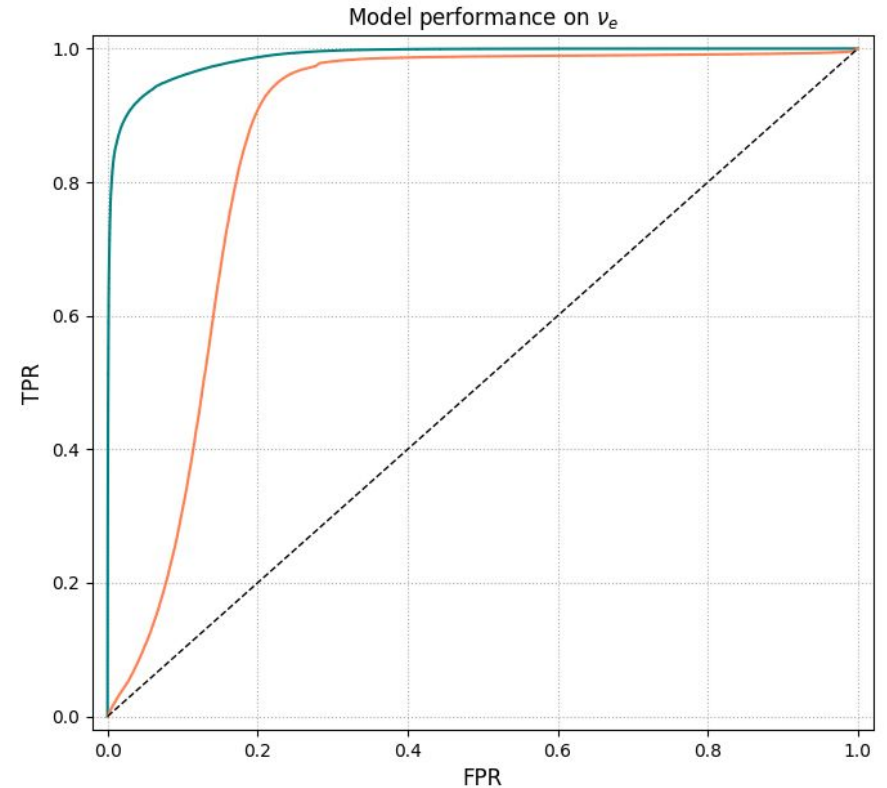


Event Classification - Performance Measures

False Positive Rate

Due to the beam composition, we select samples that have:

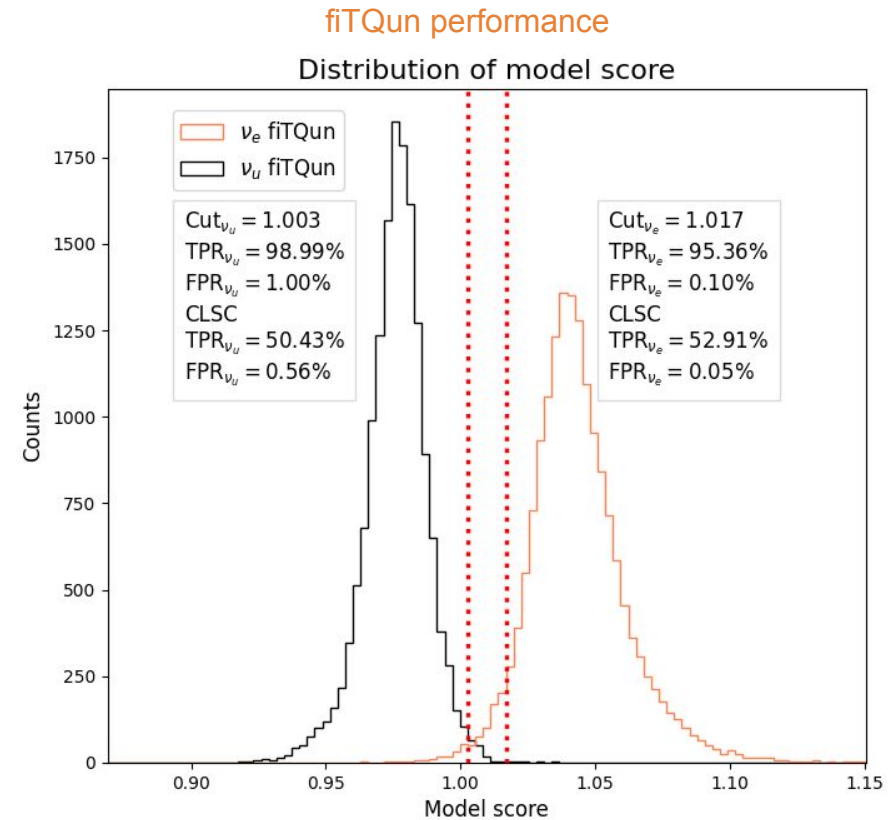
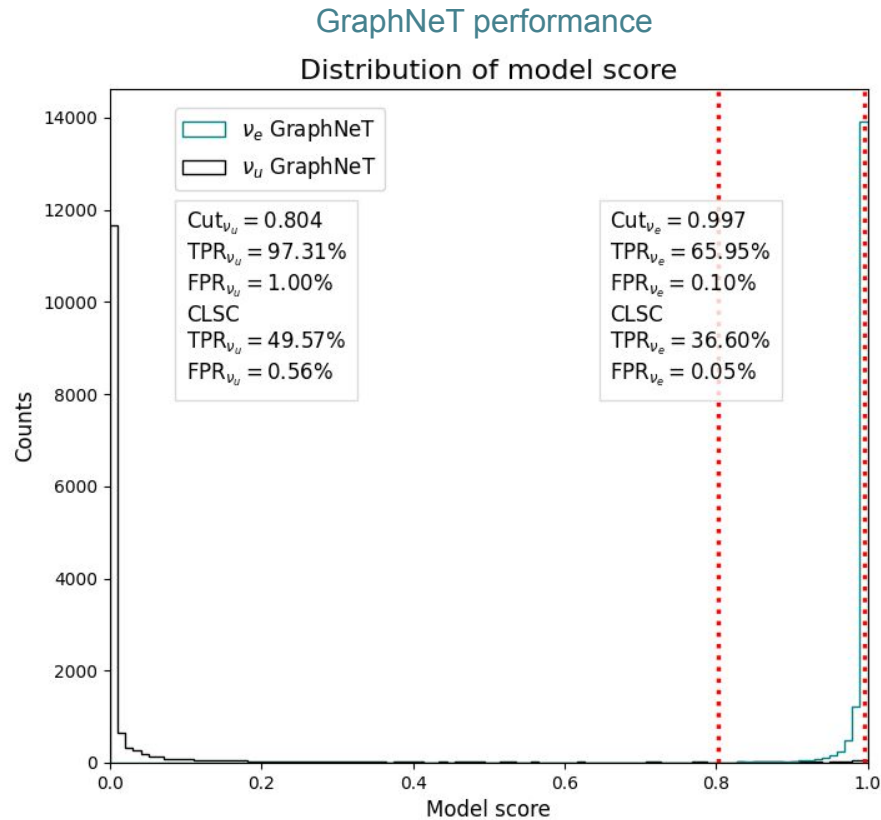
- **1 % FPR** for muon neutrinos
- **0.1 % FPR** for electron neutrinos



Charged Lepton Performance

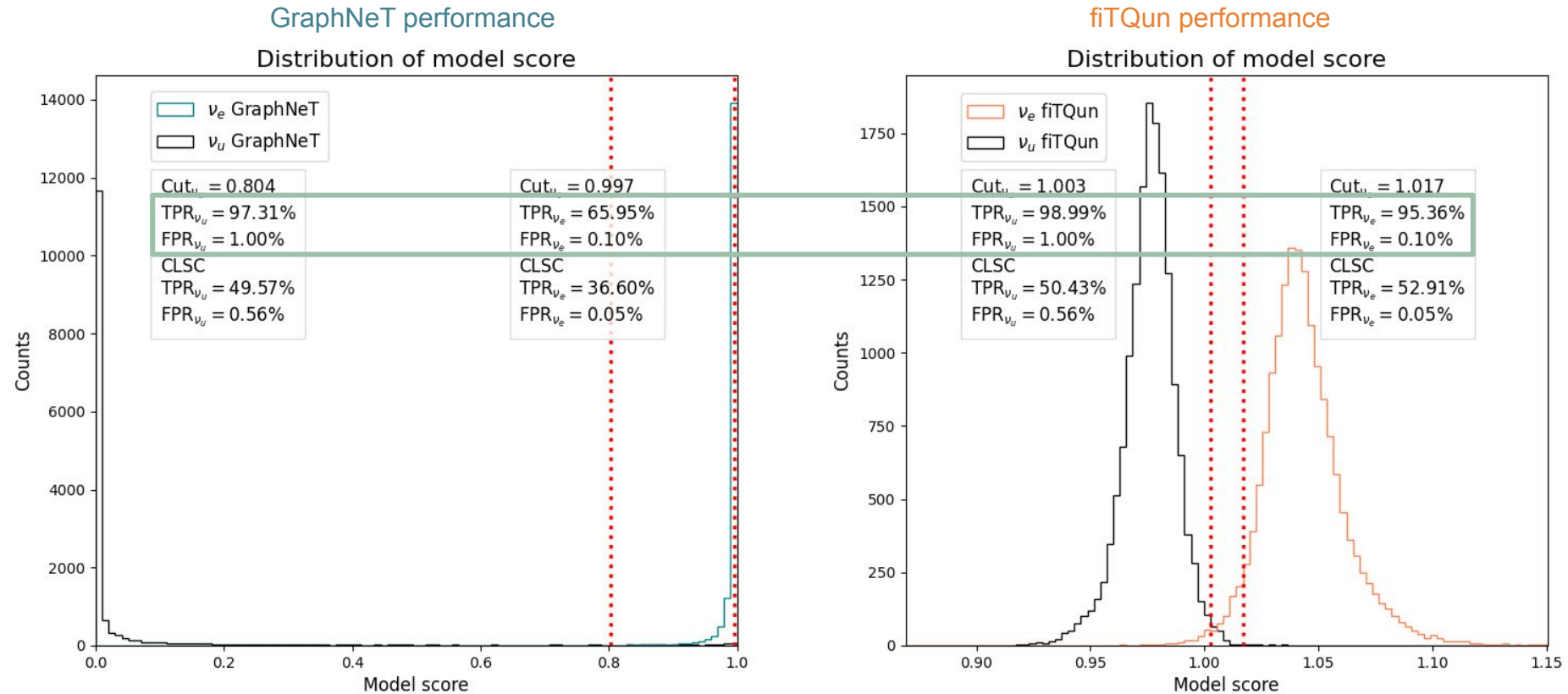
Event Classification - GraphNeT vs. fiTQun

Charged lepton simulations - with cuts



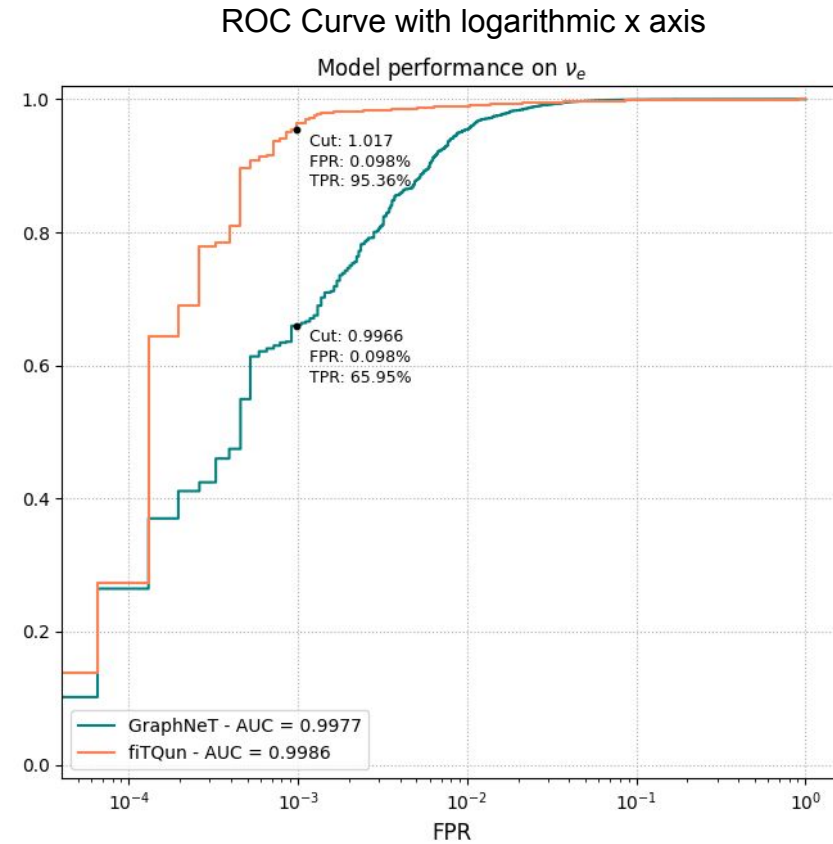
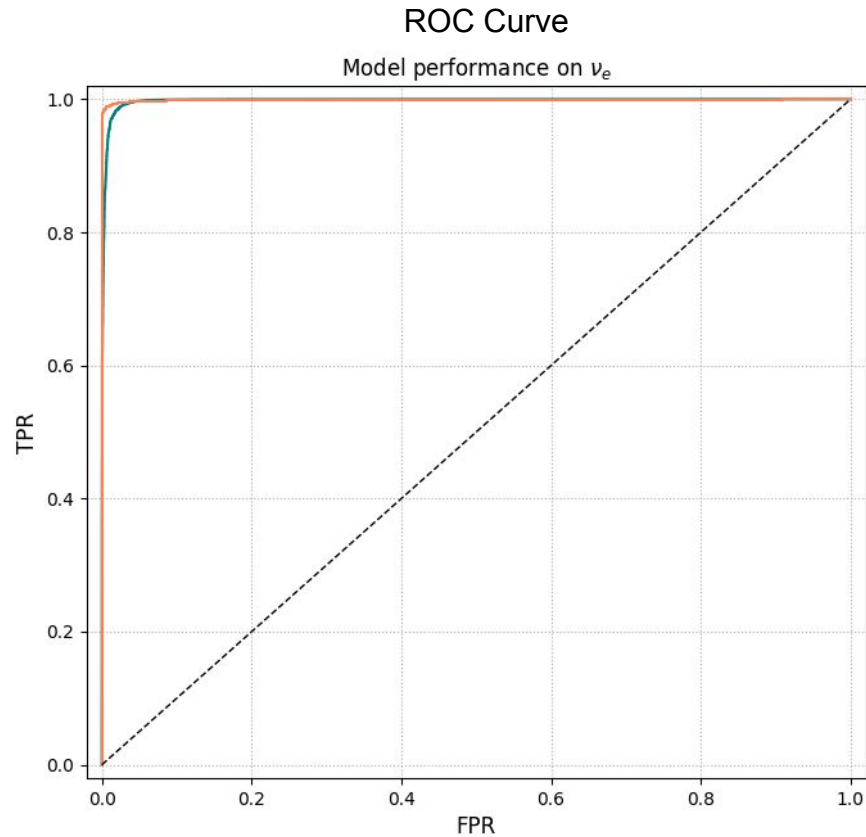
Event Classification - GraphNeT vs. fiTQun

Charged lepton simulations - with cuts



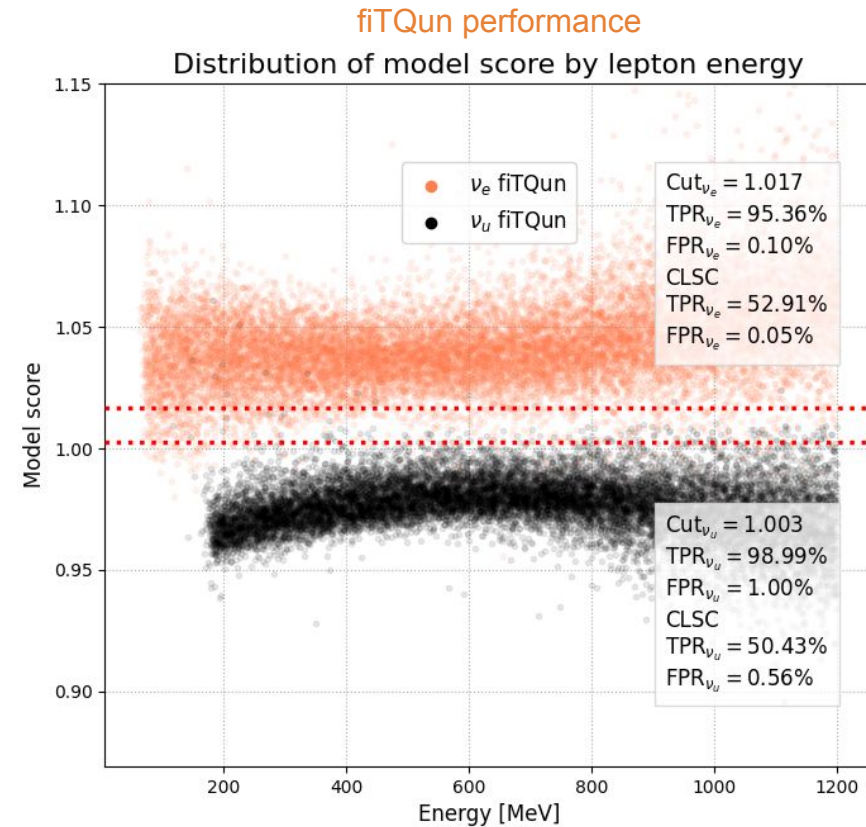
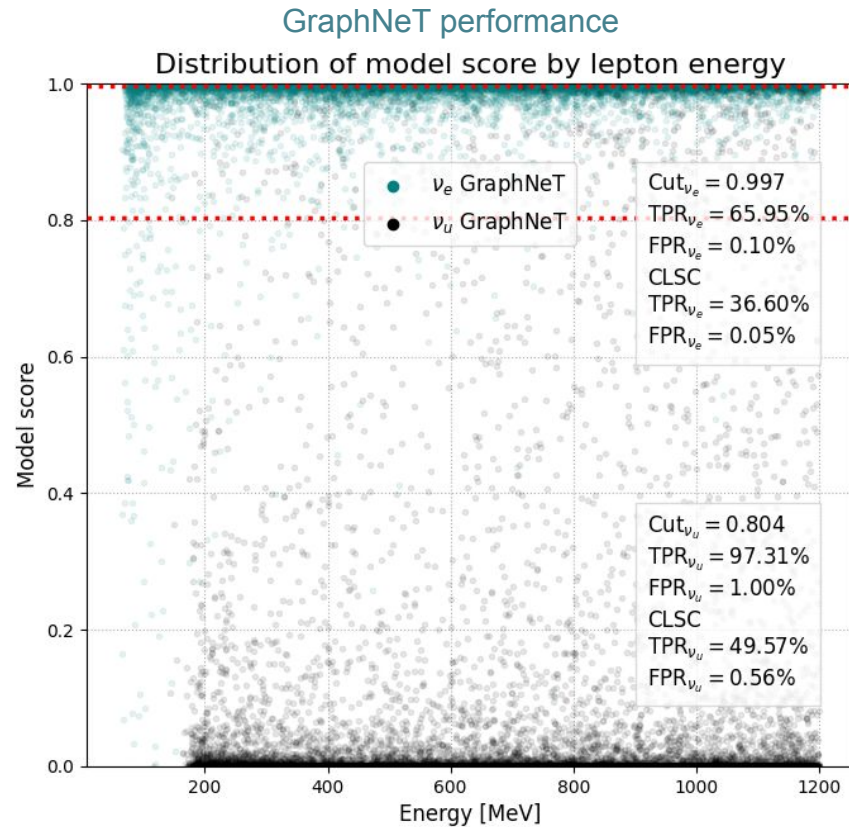
Event Classification - GraphNeT vs. fiTQun

Charged lepton simulations - with cuts (electron neutrino events)



Event Classification - GraphNeT vs. fiTQun

Charged lepton simulations - with cuts



Event Classification - GraphNeT vs. fiTQun

Charged lepton simulations - with cuts

- For pure charged lepton simulations with filtering of difficult events, the GNN is on par with the fiTQun LLH method.

However:

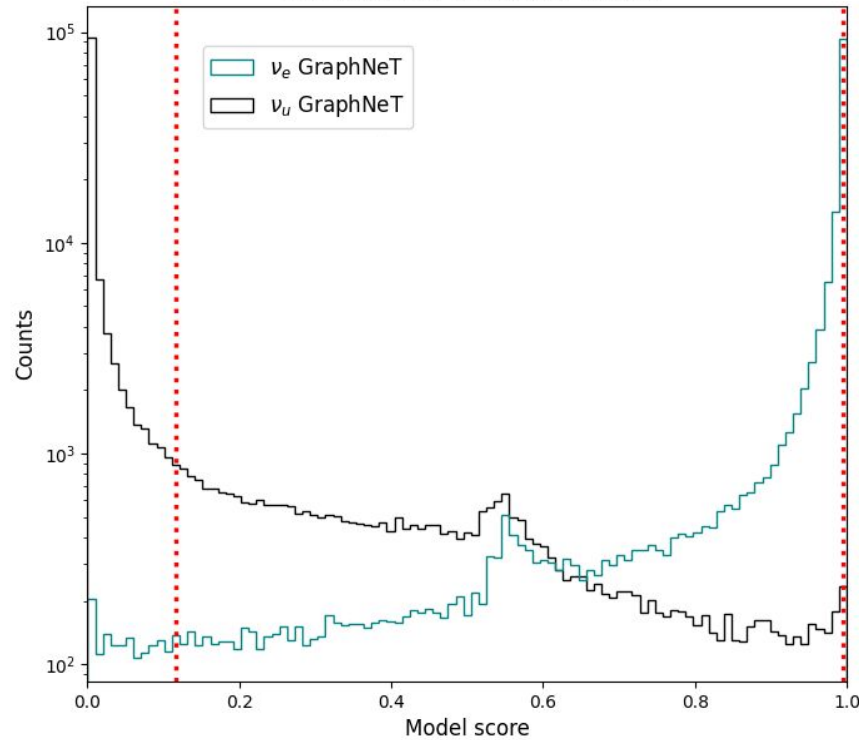
- Event filter relies on fiTQun reconstructed variables
- Full neutrino events can contain more than single charged leptons (pions, double-decays etc.)

Neutrino Event Performance

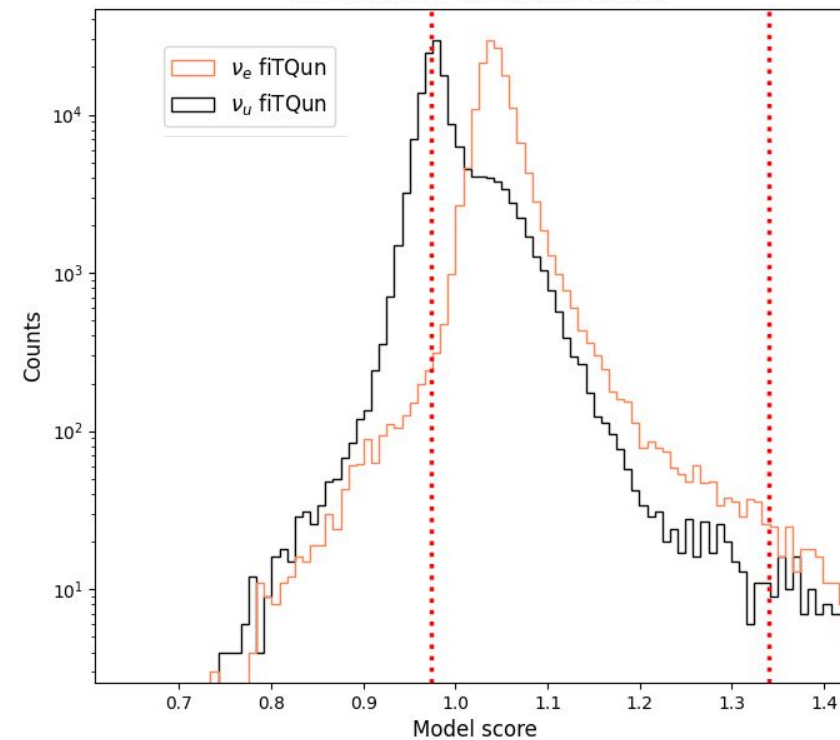
Event Classification - GraphNeT vs. fiTQun

Neutrino event simulations - without data cut

GraphNeT performance with logarithmic x axis
Distribution of model score

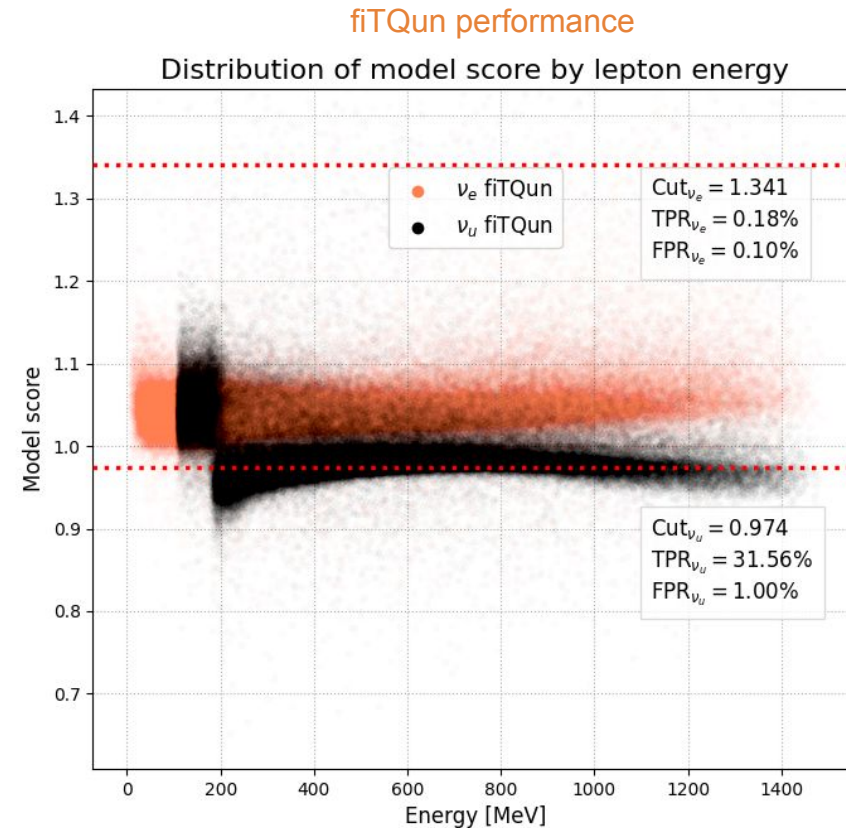
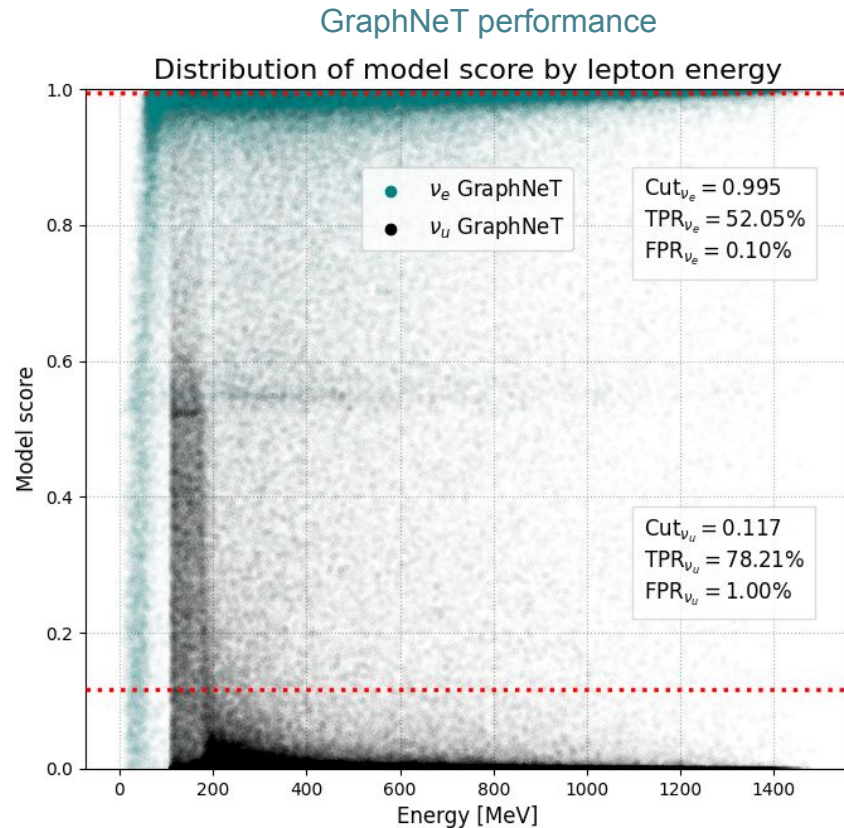


fiTQun performance with logarithmic x axis
Distribution of model score



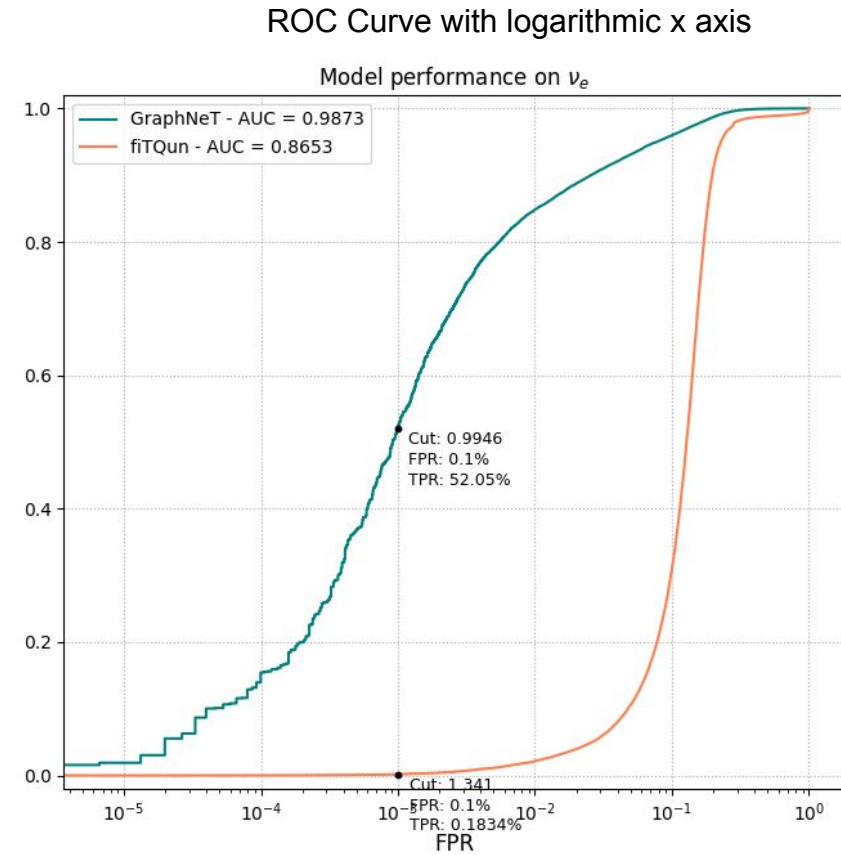
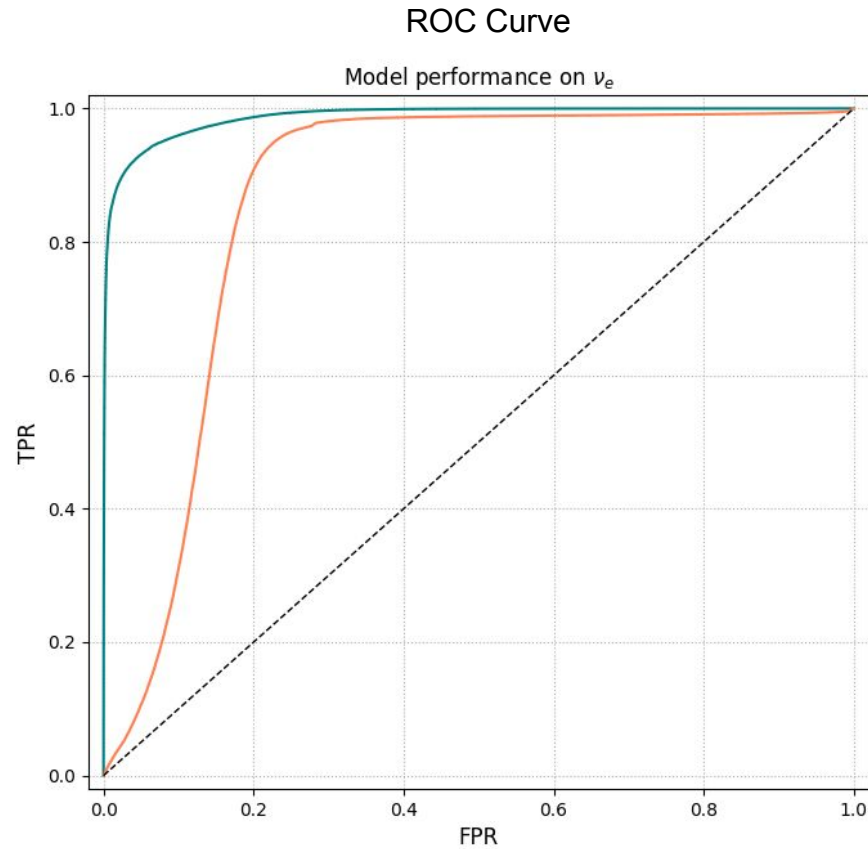
Event Classification - GraphNeT vs. fiTQun

Neutrino event simulations - without data cut



Event Classification - GraphNeT vs. fiTQun

Neutrino event simulations - without data cut (electron neutrino events)



Event Classification - GraphNeT vs. fiTQun

Neutrino event simulations - without data cut

- The GNN has acceptable performance even on the full events
- Using the GNN, the data cuts can be made obsolete

Further investigations

- Look at performance differences on an event basis
- Make a GNN-filter for good/bad events

Event Classification - GraphNeT vs. fiTQun

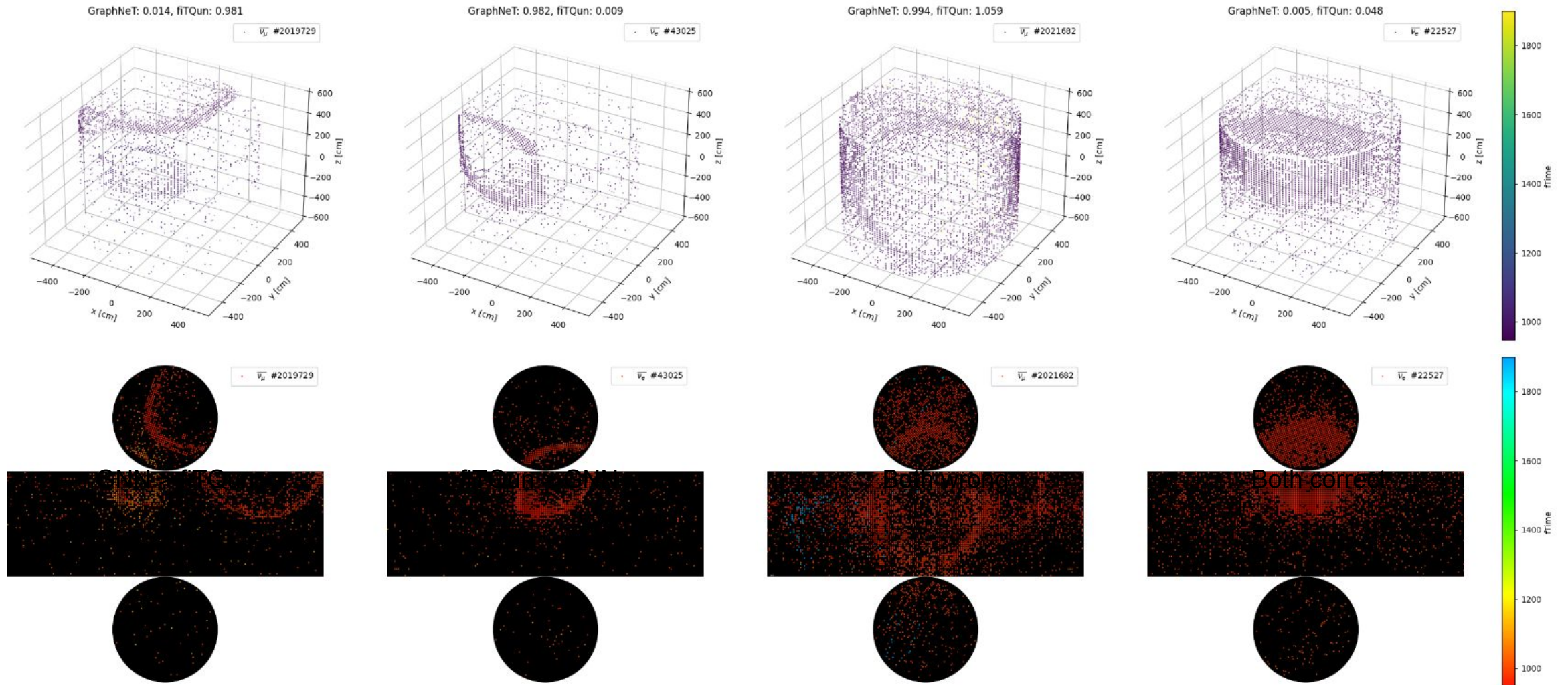
Neutrino event simulations - without data cut

Data extraction	$\sim 10^{-4}$ mins/event
Training	$\sim 10^{-3}$ mins/event
Reconstruction	$\sim 10^{-4}$ mins/event
fiTQun Reconstruction	~ 1 min/event
Improvement	10^3 (w/ training) / 10^4 (w/o training)

Performance Investigations

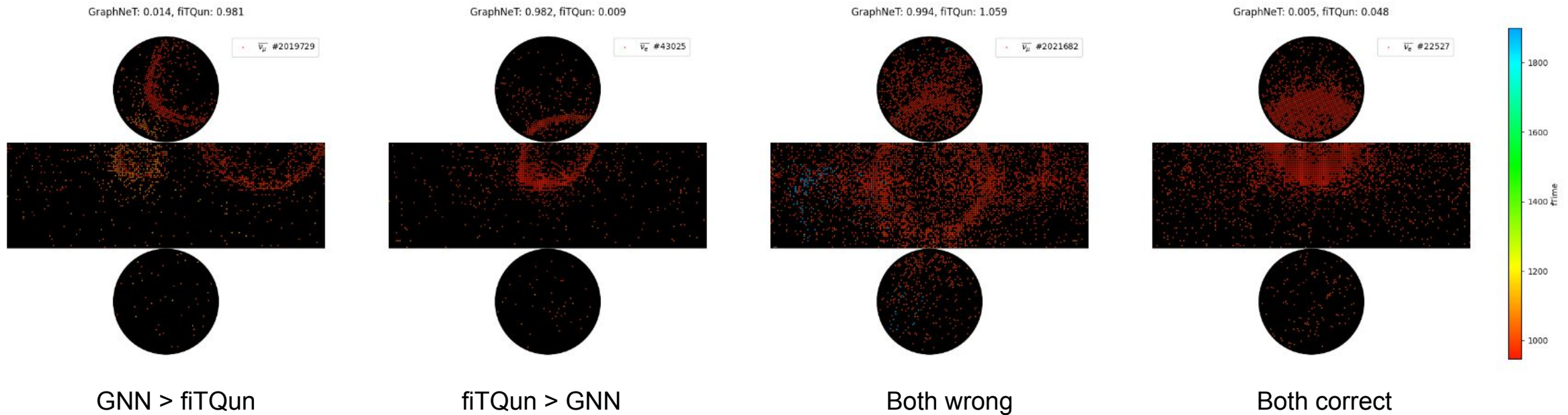
Factors impacting performance - multiple charged lepton signatures

Neutrino event simulations - **with** data cut

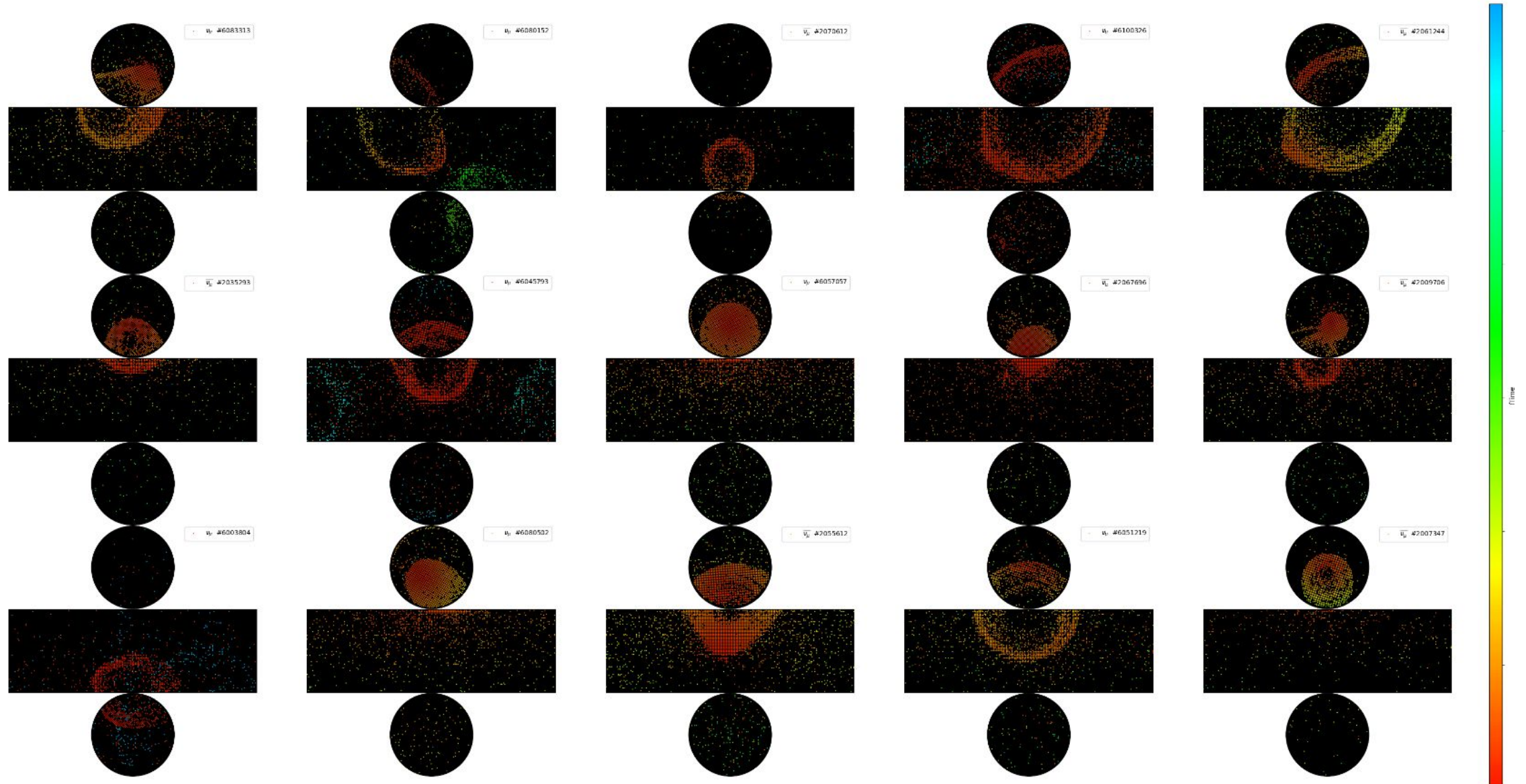


Factors impacting performance - multiple charged lepton signatures

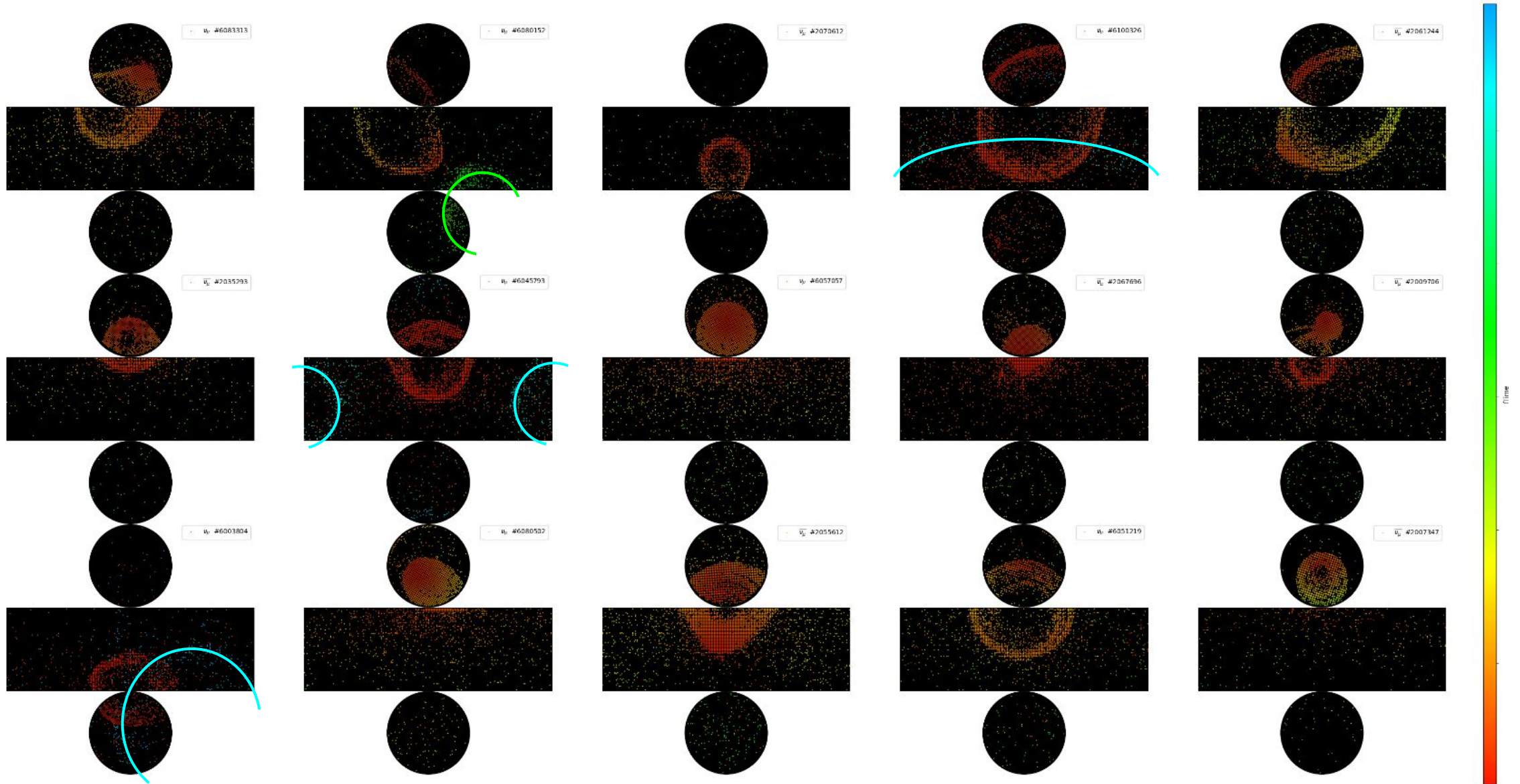
Neutrino event simulations - **with** data cut



Events for which GraphNeT performs significantly better than fiTQun



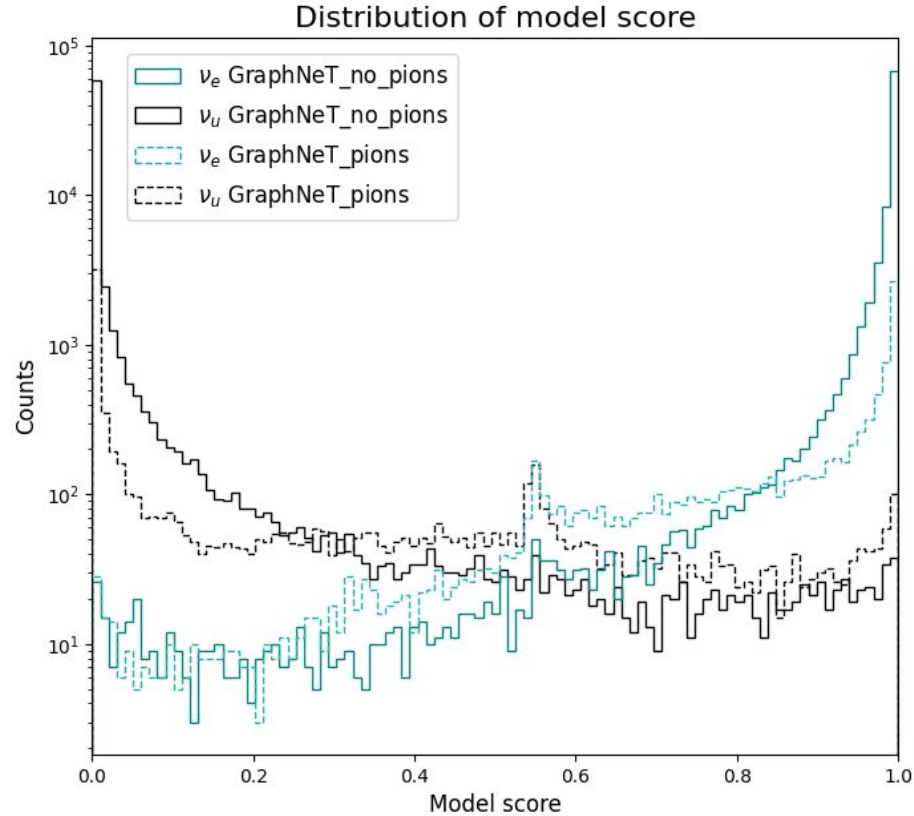
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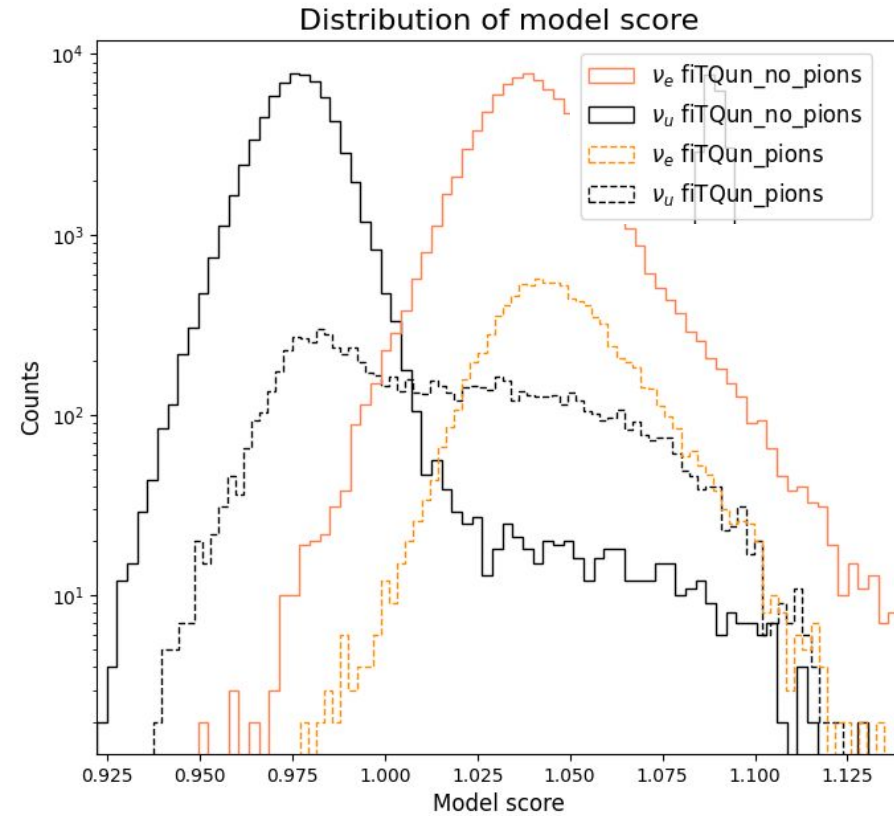
Factors impacting performance - pion creation

Neutrino event simulations - with data cut

GraphNeT performance with logarithmic x axis

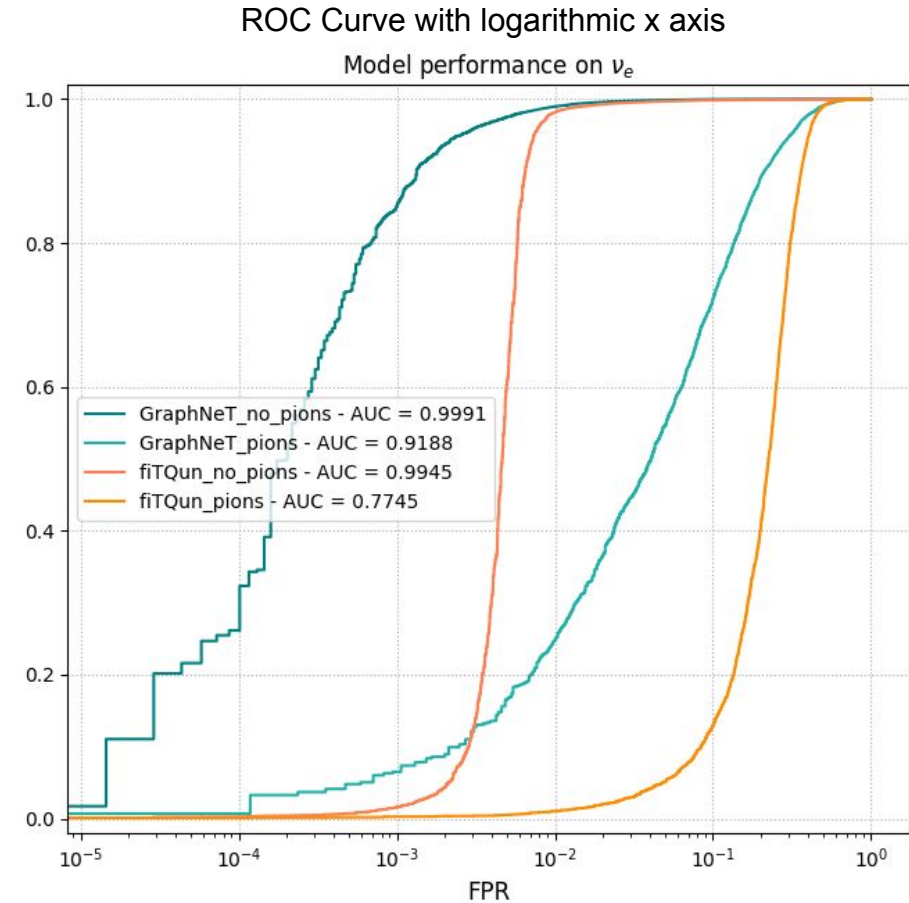
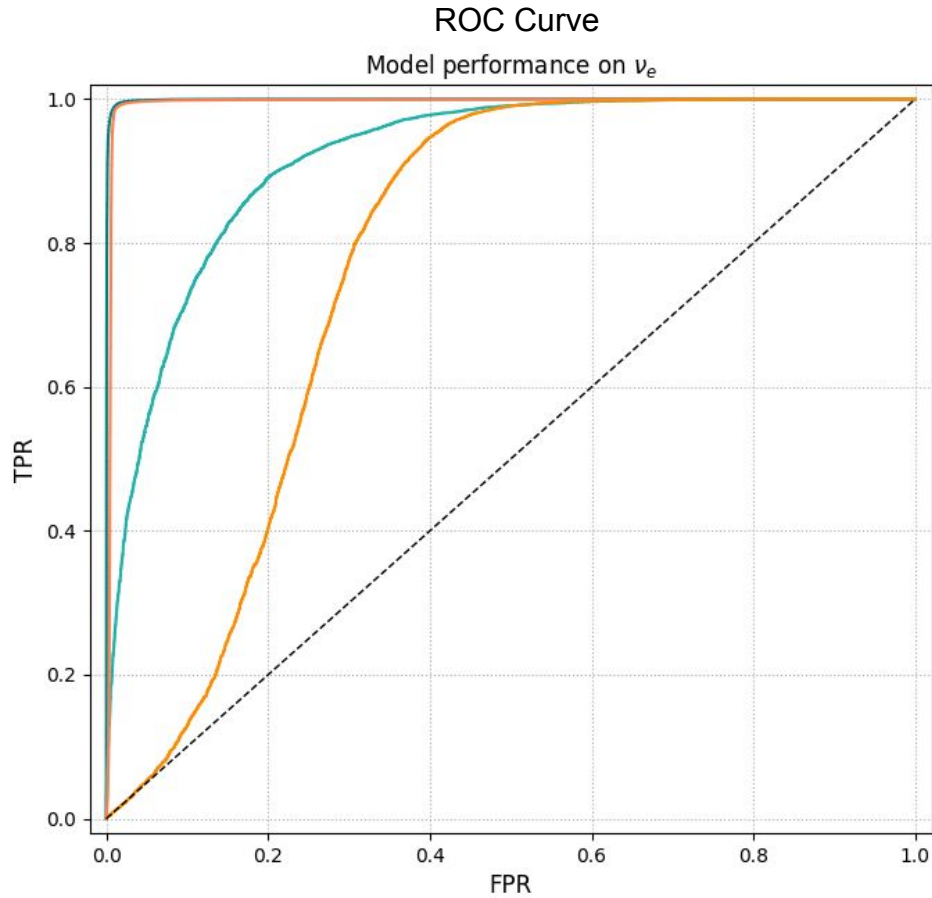


fiTQun performance with logarithmic x axis



Factors impacting performance - pion creation

Neutrino event simulations - with data cut

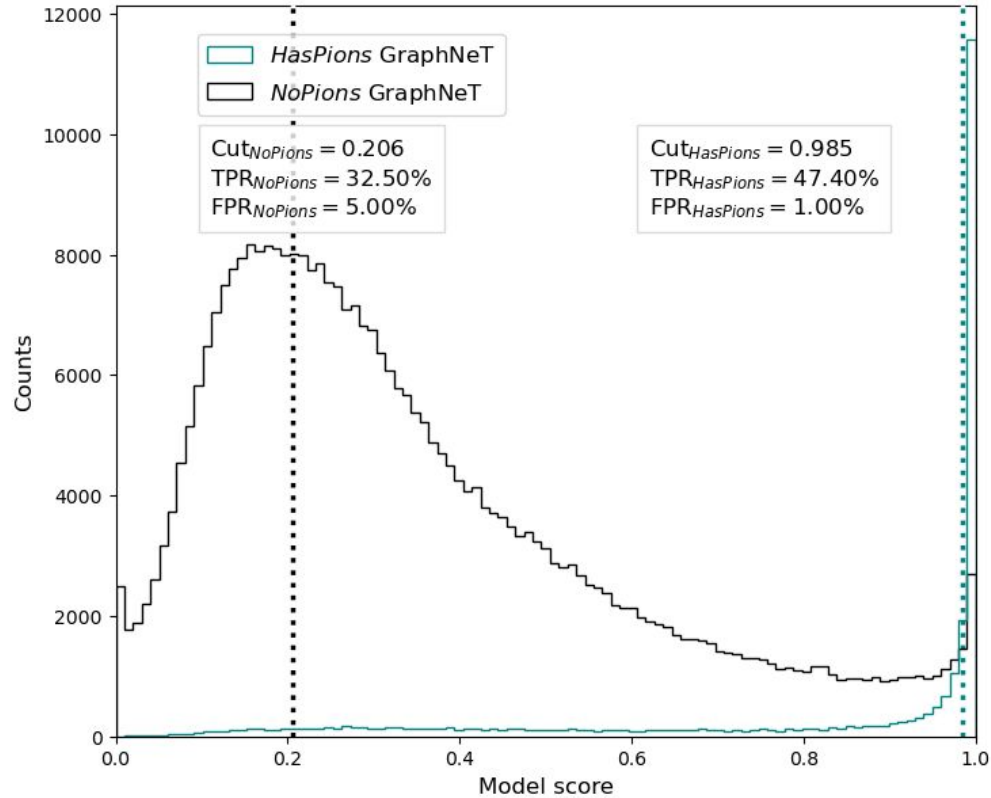


Pion production classifier

Neutrino event simulations - with data cut

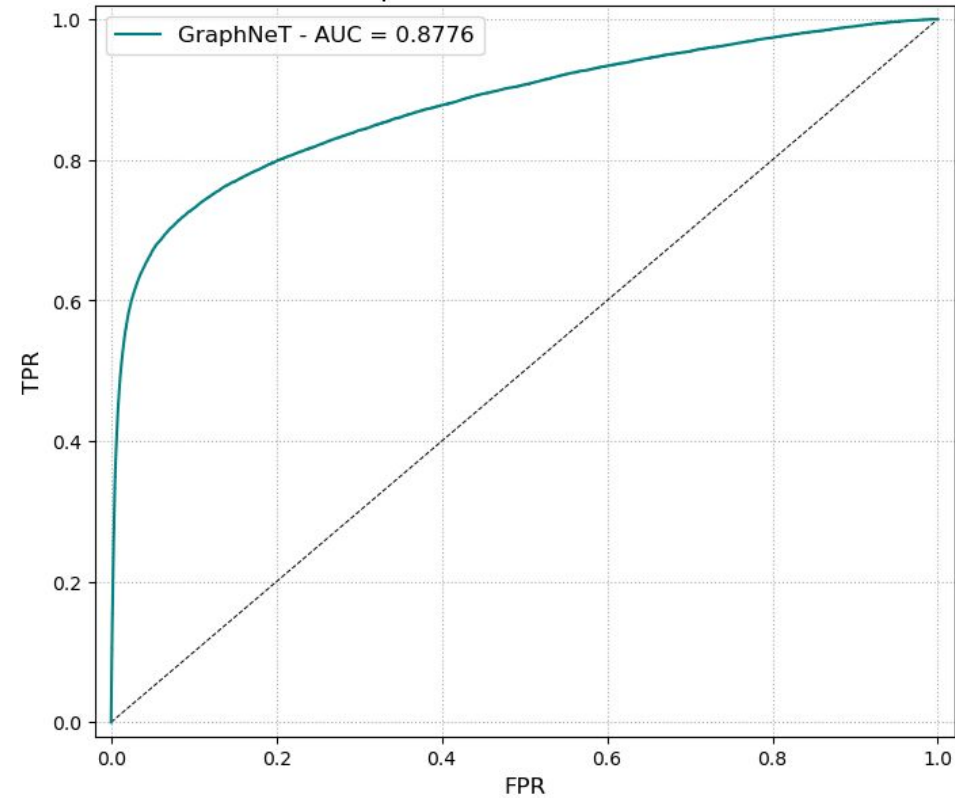
GraphNeT Performance

Distribution of model score



ROC Curve

Model performance on *HasPions*



Factors impacting performance

Neutrino event simulations - with data cut

The GNN is able to identify the characteristics of both

- Events with two Cherenkov rings due to decaying muons
- Events with pion production

Filtering these types of events and treating them separately could be beneficial

An aerial architectural rendering of a campus or urban development. The scene features a winding river in the foreground, a large circular structure with a blue logo in the center, and various buildings and green spaces. The background shows a cityscape under a hazy sky. The text "Thank you!" is overlaid in the center.

Thank you!

Additional Slides

Event Classification - Performance Measures

The neutrino beam will consist of > 98 % muon neutrinos (at the near detector)

- We can allow more electron neutrino events to be misidentified and still have a pure muon neutrino event sample



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False positive rate (FPR) is the ratio of undesired events are identified as the desired type

- Example: The FPR for **electron neutrino** events is the number of **muon neutrino** events identified as **electron neutrinos**, divided by the total number of **muon neutrino** events

Event Classification - Performance Measures

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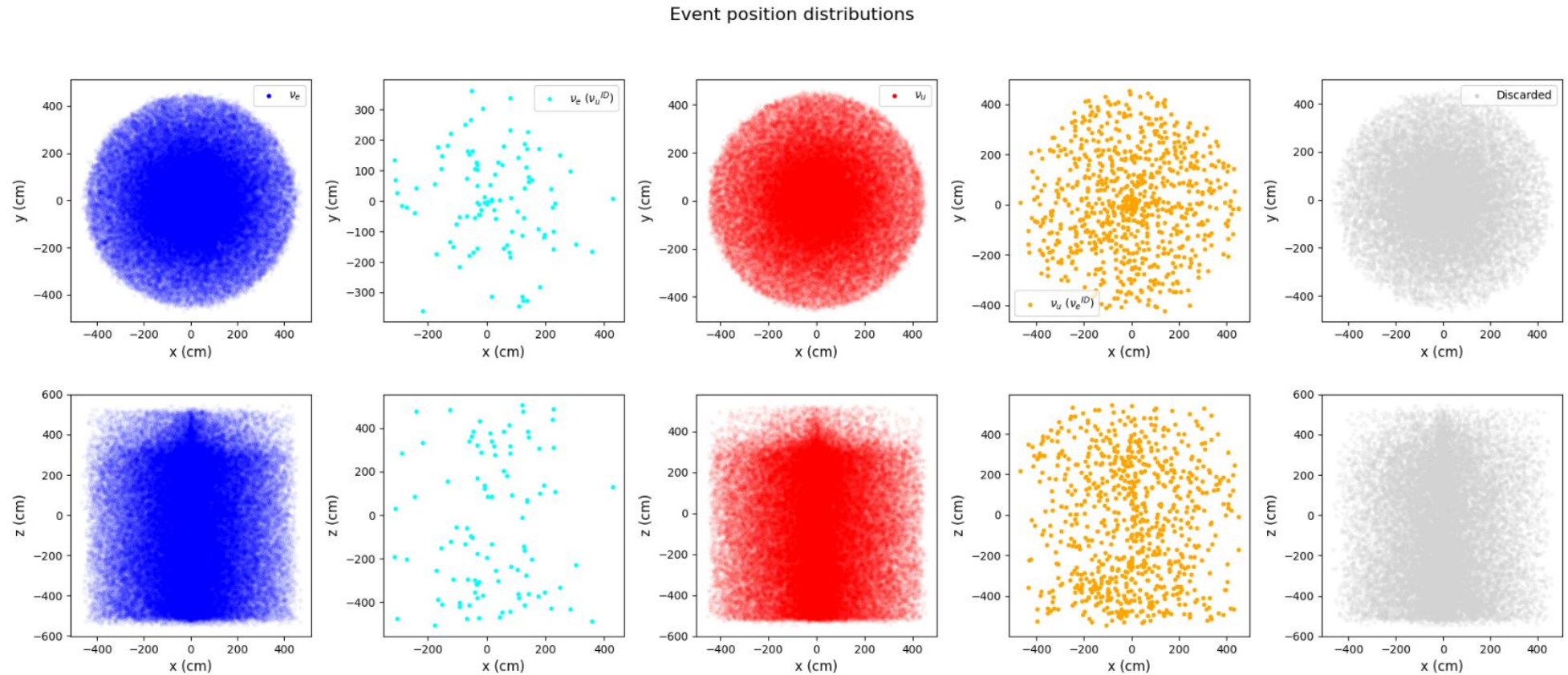
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We select samples that yield FPRs of:

- **1 % for muon neutrinos**
- **0.1 % for electron neutrinos**

Relation between interaction position and reconstruction performance

Neutrino event simulations - with data cut



Relation between interaction position and reconstruction performance

Neutrino event simulations - with data cut

