

# Modelling the Impact Parameter Dependence of the nPDFs With EKS98 and EPS09 Parametrizations

Spaatind 2012

Ilkka Helenius

In collaboration with

Kari J. Eskola, Heli Honkanen, and Carlos Salgado

University of Jyväskylä  
Department of Physics

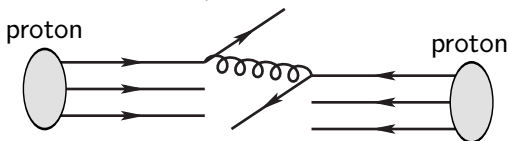
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# Parton Distribution Functions

- Hard interactions in hadronic collisions happens between partons (quarks and gluons)



- ⇒ Requires parton distribution functions (PDFs)  $f_{i/N}(x, Q^2)$
- Determined from experimental data+DGLAP (e.g. CTEQ)
  - Heavy ion collisions: protons (and neutrons) bound to nucleus  
⇒ Nuclear PDFs (nPDFs)

$$f_{i/A}(x, Q^2) = R_{i/A}(x, Q^2) \cdot f_{i/N}(x, Q^2)$$

- Nuclear modification  $R_{i/A}(x, Q^2)$  from global analysis
  - EKS98 (LO DGLAP evolution) [*Eur.Phys.J.*, C9:61-68, 1999]
  - EPS09 (LO, NLO DGLAP evolution, with uncertainties) [*JHEP*, 04:065, 2009]

# Hard Processes in Heavy Ion Collisions

The hard cross section for given centrality class in  $A + B$  collisions

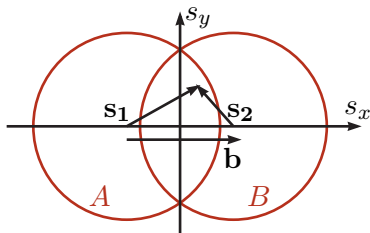
$$d\sigma^{AB \rightarrow k+X} = \sum_{i,j} \int_{b_1}^{b_2} d^2\mathbf{b} T_{AB}(\mathbf{b}) f_{i/A} \otimes f_{j/B} \otimes d\hat{\sigma}^{ij \rightarrow k+X} \quad (1)$$

## Nuclear overlap function

Amount of the interacting matter at impact parameter  $\mathbf{b}$ .

$$T_{AB}(\mathbf{b}) = \int d^2\mathbf{s} T_A(\mathbf{s}_1) T_B(\mathbf{s}_2),$$

where  $\mathbf{s}_1 = \mathbf{s} + \mathbf{b}/2$  and  $\mathbf{s}_2 = \mathbf{s} - \mathbf{b}/2$ .



# Nuclear Thickness Function

Amount of nuclear matter in beam direction

## Thickness function

Woods-Saxon density profile:

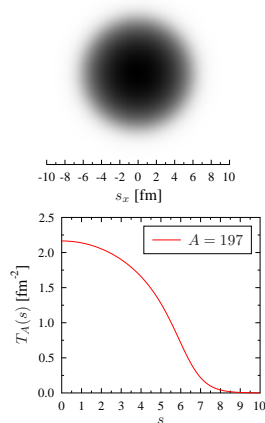
$$T_A(\mathbf{s}) = \int_{-\infty}^{\infty} dz \frac{n_0}{1 + \exp\left[\frac{\sqrt{\mathbf{s}^2 + z^2} - R_A}{d}\right]}$$

$$d = 0.54 \text{ fm}$$

$$R_A = 1.12A^{1/3} - 0.86A^{-1/3} \text{ fm}$$

$$n_0 = \frac{3}{4} \frac{A}{\pi R_A^3} \frac{1}{\left(1 + \left(\frac{\pi d}{R_A}\right)^2\right)}$$

$$A = \int d^2\mathbf{s} T_A(\mathbf{s})$$



# Framework

## Nuclear modification with spatial dependence

- We replace

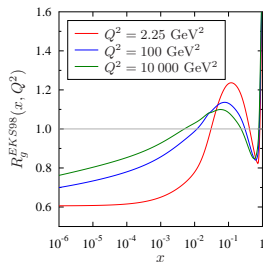
$$R_{i/A}(x, Q^2) \rightarrow r_{i/A}(x, Q^2, \mathbf{s}),$$

where  $\mathbf{s}$  is the transverse position of the nucleon

- Definition

$$R_A(x, Q^2) = \frac{1}{A} \int d^2\mathbf{s} T_A(\mathbf{s}) r_A(x, Q^2, \mathbf{s}),$$

where  $R_A(x, Q^2)$  from EKS98 or EPS09



# Fitting Procedure

Assumption: spatial dependence of the form

$$r_A(x, Q^2, s) = 1 + c_1(x, Q^2)[T_A(s)] + c_2(x, Q^2)[T_A(s)]^2 \\ + c_3(x, Q^2)[T_A(s)]^3 + c_4(x, Q^2)[T_A(s)]^4$$

**Important: no  $A$  dependence in fit parameters  $c_i(x, Q^2)$ !**

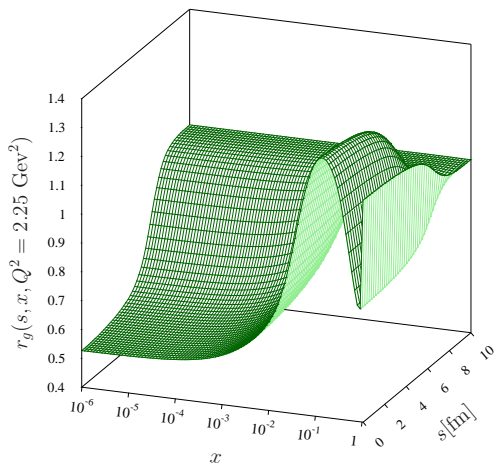
Parameters  $c_i(x, Q^2)$  obtained by minimizing the  $\chi^2$ . For EKS98s:

$$\chi^2(x, Q^2) = \sum_A \left[ \frac{R_A(x, Q^2) - \frac{1}{A} \int d^2s T_A(s) r_A(x, Q^2, s)}{R_A(x, Q^2) - 1} \right]^2,$$

where  $A = 16, 20, 24, \dots, 300$ .

# Spatial Dependence of Nuclear Modification for Au

$$r^{EKS98s}(x, Q^2, s) = 1 + \sum_{i=1}^4 c_i(x, Q^2) [T_A(s)]^i$$



## Observations

- The shape in  $x$  is similar to EKS98
- Effects are slightly stronger in small  $s$  compared to EKS98
- Nuclear effects die out when  $s > R_A$



# Nuclear Modification Factor $R_{AA}$

## Nuclear Modification Factor

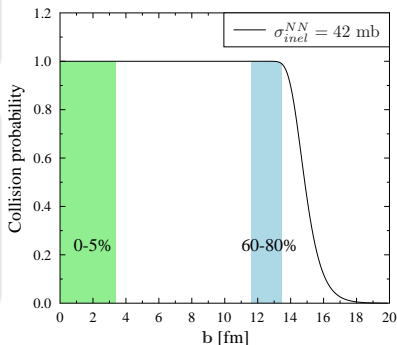
$$R_{AA} = \frac{\left\langle \frac{d^2 N_{AA}}{dp_T dy} \right\rangle_{b_1, b_2}}{\frac{\langle N_{bin} \rangle_{b_1, b_2}}{\sigma_{inel}^{NN}} \frac{d^2 \sigma_{pp}}{dp_T dy}}$$

## The central-to-peripheral ratio

$$R_{CP} = \frac{\left\langle \frac{d^2 N_{AA}}{dp_T dy} \right\rangle \frac{1}{\langle N_{bin} \rangle} (central)}{\left\langle \frac{d^2 N_{AA}}{dp_T dy} \right\rangle \frac{1}{\langle N_{bin} \rangle} (peripheral)}$$

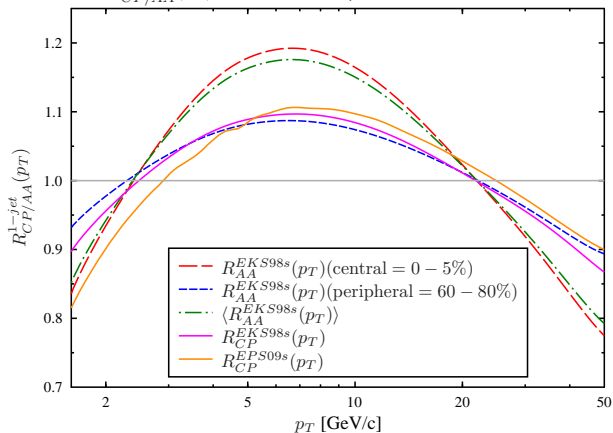
- Centrality classes from optical glauber model

$$p_{AA}^{inel}(b) = 1 - e^{-T_{AA}(\mathbf{b})\sigma_{inel}^{NN}}$$



# 1-jet Central-to-Peripheral Ratio for RHIC

$R_{CP/AA}^{1-jet}(p_T)$  for Au+Au at  $\sqrt{s} = 200$  GeV and  $y = 0$



## Observations

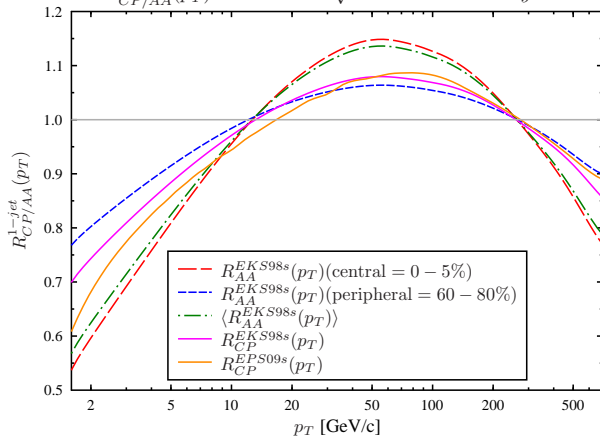
$$R_{AA}(central) \approx \langle R_{AA} \rangle$$

$$R_{AA}(peripheral) \neq 1$$

$$R_{CP} \neq \langle R_{AA} \rangle$$

# 1-jet Central-to-Peripheral Ratio for LHC

$R_{CP/AA}^{1-jet}(p_T)$  for Pb+Pb at  $\sqrt{s} = 2760$  GeV and  $y = 0$



## Observations

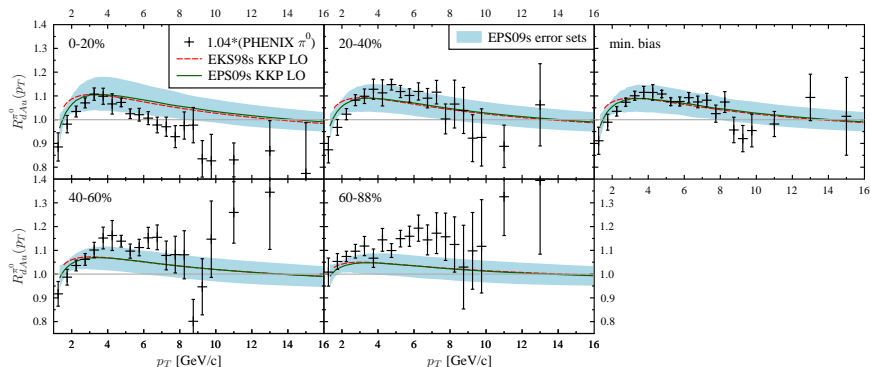
$$R_{AA}(central) \approx \langle R_{AA} \rangle$$

$$R_{AA}(peripheral) \neq 1$$

$$R_{CP} \neq \langle R_{AA} \rangle$$

# Pions in d+Au collisions at RHIC

$R_{dAu}$  for  $\pi^0$ 's in different centrality classes at  $\sqrt{s} = 200$  GeV,  $\eta = 0$   
 Data: PHENIX ( $|\eta| < 0.5$ ) [*Phys. Rev. Lett.* 98, 172302, 2007]



More centrality dependent data is needed (p+Pb at LHC?)

# Summary

## We have

- Developed a model for spatial dependence of nuclear modification based on
  - the  $A$  dependence of the EKS98/EPS09 (= data!)
  - the nuclear thickness function  $T_A(s)$
- Program to calculate  $r_A(x, Q^2, \mathbf{s})$
- Calculated  $R_{AA}^{1-jet}$ ,  $R_{CP}^{1-jet}$  and  $R_{dAu}^{\pi^0}$  in LO

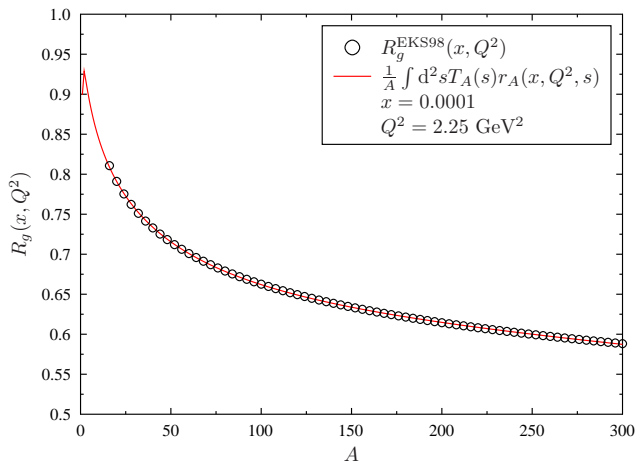
## We will

- Calculate also NLO ratios
- Make the codes for  $r_A(x, Q^2, \mathbf{s})$  calculation public (EKS98s and EPS09s)
  - ⇒ Nuclear modifications of any hard process in different centrality classes can now be computed consistently with EKS98/EPS09!

Backup

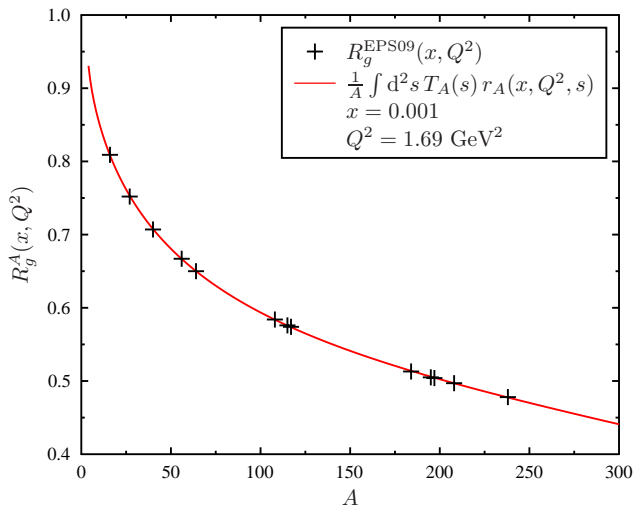
# Fit Outcome

Example fit: gluon modification from EKS98



# Fit Outcome

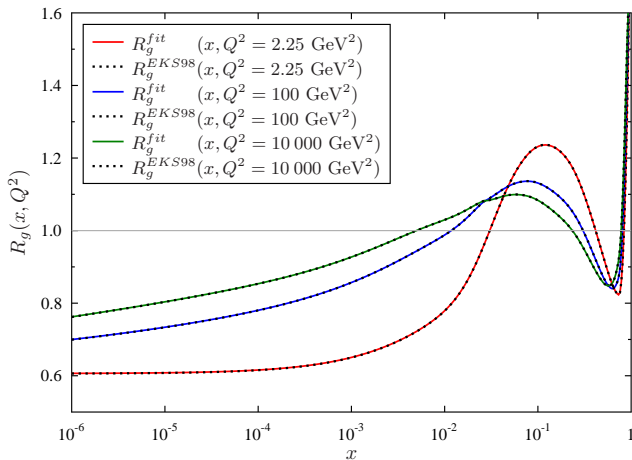
Example fit: gluon modification from EPS09



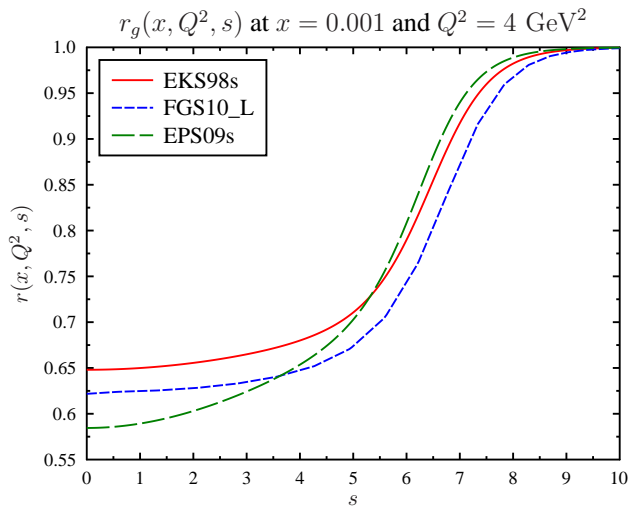


# Fitted $R(x, Q^2)$ vs. old $R(x, Q^2)$

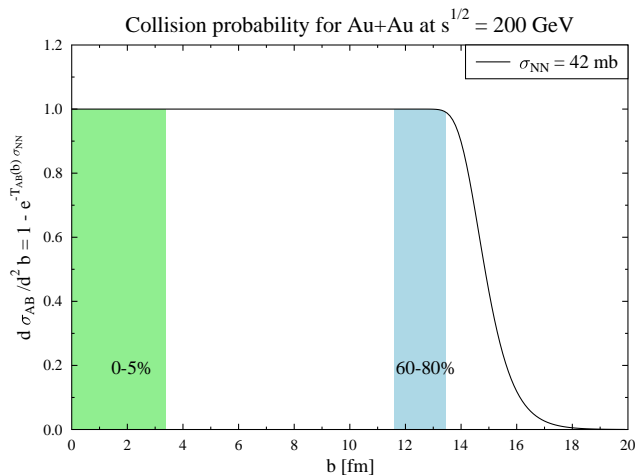
$$R^{fit}(x, Q^2) = \frac{1}{A} \int d^2\mathbf{s} T_A(s) \left[ 1 + \sum_{i=1}^4 c_i(x, Q^2) [T_A(s)]^i \right]$$



# Comparison of the spatial dependence



# Centrality Classes for RHIC



# Numerical Calculation of $T_A(s)$

## Thickness function

- Woods-Saxon density profile:

$$T_A(s) = \int_0^\infty dz \frac{2n_0}{1 + \exp\left[\frac{\sqrt{s^2 + z^2} - R_A}{d}\right]}$$

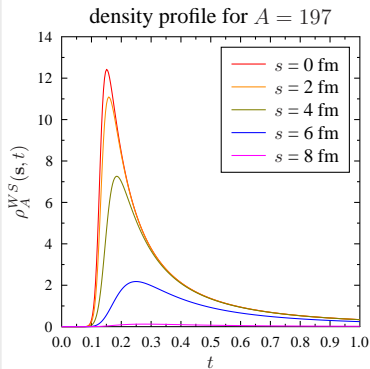
Needs numerical integration

- Change of variable as  $z = \frac{1-t}{t}$  gives

$$T_A(s) = \int_0^1 dt \frac{2n_0}{t^2 \left\{ 1 + \exp\left[\frac{\sqrt{s^2 + \left(\frac{1-t}{t}\right)^2} - R_A}{d}\right] \right\}}$$

- Singularity at  $t = 0$  is ok, because

$$\lim_{t \rightarrow 0} \rho^{WS}(t) = 0$$



# A-dependent modification

## Thickness function

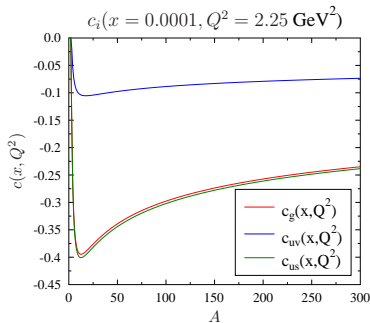
- If the Modification of the form

$$r_A(x, Q^2, s) = 1 + c(x, Q^2)[T_A(s)]$$

[Phys.Rev., C61:044904, 2000]

- The parameter  $c(x, Q^2)$  from the normalization condition

$$c(x, Q^2) = \frac{A(R_i^A(x, Q^2) - 1)}{\int d^2\mathbf{s} [T_A(\mathbf{s})]^2}$$



$$\frac{c_g^{208}(x, Q^2)}{c_g^{12}(x, Q^2)} = 0.65$$

⇒ Strong  $A$  dependence of  $c(x, Q^2)$ !

The  $s$  dependence not entirely decomposed from  $c(x, Q^2)$ .

# Central-to-Peripheral Ratio $R_{CP}^{1-jet}$

- The 1-jet distribution for a centrality class with  $b \in [b_1, b_2]$  can be calculated from

$$\left\langle \frac{d^2 N_{AA}^{1-jet}}{dp_T dy} \right\rangle_{b_1, b_2} = \frac{\int_{b_1}^{b_2} d^2 b \frac{d^2 N_{AA}^{1-jet}(b)}{dp_T dy}}{\int_{b_1}^{b_2} d^2 b p_{AA}^{inel}(b)}$$

- $p_{AA}^{inel}(b) = 1 - e^{-T_{AA}(\mathbf{b})\sigma_{inel}^{NN}}$  (optical Glauber model)

## Parameters from Optical Glauber Model

	<i>central</i> = 0 – 5%			<i>peripheral</i> = 60 – 80%		
	$b_1$ [fm]	$b_2$ [fm]	$\langle N_{bin} \rangle$	$b_1$ [fm]	$b_2$ [fm]	$\langle N_{bin} \rangle$
RHIC	0.0	3.355	1083	11.62	13.42	15.11
LHC	0.0	3.478	1772	12.05	13.91	19.08

- RHIC:  $\sigma_{inel}^{NN} = 42$  mb
- LHC:  $\sigma_{inel}^{NN} = 64$  mb