

**TBA**

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***Heavy Ions: Experiment Confront Theory***

Niels Bohr Institute (Copenhagen)  
November 7-9, 2011

# **NNPDF for the LHC**

**and a couple of comments on Nuclear (NN)PDFs**

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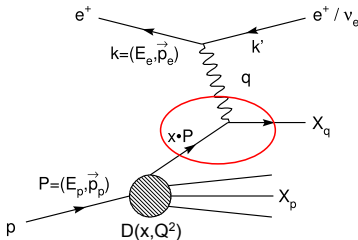
***Heavy Ions: Experiment Confront Theory***

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# What are Parton Distribution Functions?

- Consider a process with one hadron in the initial state



- According to the **Factorization Theorem** we can write the cross section as

$$d\sigma = \sum_a \int_0^1 \frac{d\xi}{\xi} D_a(\xi, \mu^2) d\hat{\sigma}_a \left( \frac{x}{\xi}, \frac{\hat{s}}{\mu^2}, \alpha_s(\mu^2) \right) + \mathcal{O} \left( \frac{1}{Q^p} \right)$$



# What are Parton Distribution Functions?

- The **absolute value** of PDFs at a given  $x$  and  $Q^2$  **cannot be computed** in QCD Perturbation Theory  
(Lattice? In principle yes, but ...)
- ... but the **scale dependence** is governed by **DGLAP** evolution equations

$$\frac{\partial}{\ln Q^2} q^{NS}(\xi, Q^2) = P^{NS}(\xi, \alpha_s) \otimes q^{NS}(\xi, Q^2)$$
$$\frac{\partial}{\ln Q^2} \begin{pmatrix} \Sigma \\ g \end{pmatrix}(\xi, Q^2) = \begin{pmatrix} P_{qq} & P_{qg} \\ P_{gq} & P_{gg} \end{pmatrix}(\xi, \alpha_s) \otimes \begin{pmatrix} \Sigma \\ g \end{pmatrix}(\xi, Q^2)$$

- ... and the **splitting functions**  $P$  can be computed in PT and are known up to **NNLO**

[**LO** - Dokshitzer; Gribov, Lipatov; Altarelli, Parisi; 1977]

[**NLO** - Floratos, Ross, Sachrajda; Gonzalez-Arroyo, Lopez, Yndurain; Curci, Furmanski, Petronzio, 1981]

[**NNLO** - Moch, Vermaseren, Vogt; 2004]



# Problem

Faithful estimation of errors on PDFs

- Single quantity: **1- $\sigma$  error**
- Multiple quantities: **1- $\sigma$  contours**
- Function: need an **"error band" in the space of functions**  
(i.e. the probability density  $\mathcal{P}[f]$  in the space of functions  $f(x)$ )

**Expectation values are Functional integrals**

$$\langle \mathcal{F}[f(x)] \rangle = \int \mathcal{D}f \mathcal{F}[f(x)] \mathcal{P}[f(x)]$$



# Problem

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**Expectation values** are **Functional integrals**

$$\langle \mathcal{F}[f(x)] \rangle = \int \mathcal{D}f \mathcal{F}[f(x)] \mathcal{P}[f(x)]$$

**Determine a function from a finite set of data points**



# Solution

## Standard Approach

- Introduce a simple functional form with enough free parameters

$$q(x, Q^2) = x^\alpha (1 - x)^\beta P(x; \lambda_1, \dots, \lambda_n).$$

- Fit parameters minimizing  $\chi^2$ .



# Solution

## Standard Approach

- Introduce a simple functional form with enough free parameters

$$q(x, Q^2) = x^\alpha (1 - x)^\beta P(x; \lambda_1, \dots, \lambda_n).$$

- Fit parameters minimizing  $\chi^2$ .

## Open problems:

- **Error propagation** from data to parameters and from parameters to observables is **not trivial**.
- **Theoretical bias** due to the chosen **parametrization** is difficult to assess.



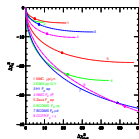


# Shortcomings of the Standard approach

What is the meaning of a one- $\sigma$  uncertainty?

- Standard  $\Delta\chi^2 = 1$  criterion is **too restrictive** to account for large discrepancies among experiments in a **global fit**.

[Collins & Pumplin, 2001]

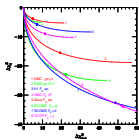


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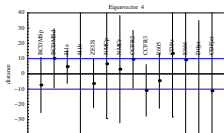
- Standard  $\Delta\chi^2 = 1$  criterion is **too restrictive** to account for large discrepancies among experiments in a **global fit**.

[Collins & Pumplin, 2001]



- Introduce a **TOLERANCE** criterion, i.e. take the envelope of uncertainties of experiments to determine the  $\Delta\chi^2$  to use for the global fit (CTEQ).

[Tung et al., 2006]

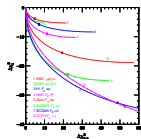


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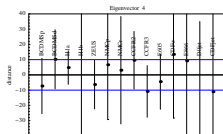
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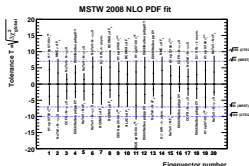
- Introduce a **TOLERANCE** criterion, i.e. take the envelope of uncertainties of experiments to determine the  $\Delta\chi^2$  to use for the global fit (CTEQ).

[Tung et al., 2006]



- Make it **DYNAMICAL**, i.e. determine  $\Delta\chi^2$  separately for each hessian eigenvector (MSTW).

[Thorne et. al, 2008]

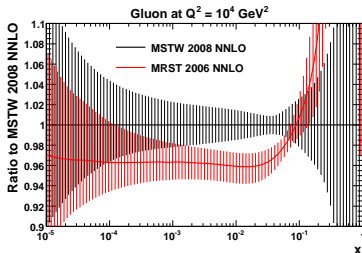


# Shortcomings of the standard approach

What determines PDF uncertainties?

- **Uncertainties** in standard fits often **increase when adding data** (i.e. when adding information) even if they are compatible with the old data.
- **Reason:** need change the parametrization in order to accomodate the new data.

Smaller high- $x$  gluon (and slightly smaller  $\alpha_S$ ) results in larger small- $x$  gluon – now shown at NNLO.



Larger small- $x$  uncertainty due to extra free parameter.

[R. Thorne, PDF4LHC]

# THE NNPDF METHODOLOGY

[R. D. Ball, V. Bertone, F. Cerutti, L. Del Debbio, S. Forte, J. I. Latorre, A. Piccione, J. Rojo, M. Ubiali and AG]



# NNPDF Methodology

## Main Ingredients

- **Monte Carlo** determination of errors
  - No need to rely on linear propagation of errors
  - Possibility to test for the impact of non gaussianly distributed errors
  - Possibility to test for non-gaussian behaviour in fitted PDFs  
( $1 - \sigma$  vs. 68% CL)
- **Neural Networks**
  - Provide an **unbiased** parametrization
- **Stopping based on Cross-Validation**
  - Ensures proper fitting avoiding overlearning



# NNPDF Methodology

... in a Nutshell

- Generate  $N_{rep}$  **Monte-Carlo replicas** of the experimental data (sampling of the probability density in the space of data)
- Fit a set of Parton Distribution Functions on each replica (sampling of the probability density in the space of PDFs)
- **Expectation values** for observables are **Monte Carlo integrals**

$$\langle \mathcal{F}[f_i(x, Q^2)] \rangle = \frac{1}{N_{rep}} \sum_{k=1}^{N_{rep}} \mathcal{F}\left(f_i^{(net)(k)}(x, Q^2)\right)$$

... the same is true for errors, correlations, etc.



# NNPDF Methodology

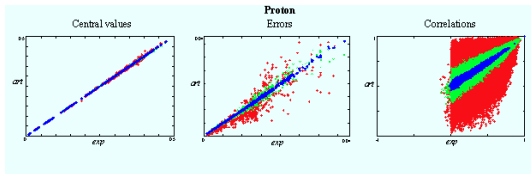
## Monte Carlo replicas generation

- **Generate** artificial data according to distribution

$$O_i^{(art)(k)} = (1 + r_N^{(k)} \sigma_N) \left[ O_i^{(exp)} + \sum_{p=1}^{N_{sys}} r_p^{(k)} \sigma_{i,p} + r_{i,s}^{(k)} \sigma_s^i \right]$$

where  $r_i$  are univariate (gaussianly distributed) random numbers

- **Validate** Monte Carlo replicas against experimental data (statistical estimators, faithful representation of errors, convergence rate increasing  $N_{rep}$ )



- $\mathcal{O}(1000)$  replicas needed to reproduce correlations to percent accuracy





# Neural Networks

... a suitable basis of functions

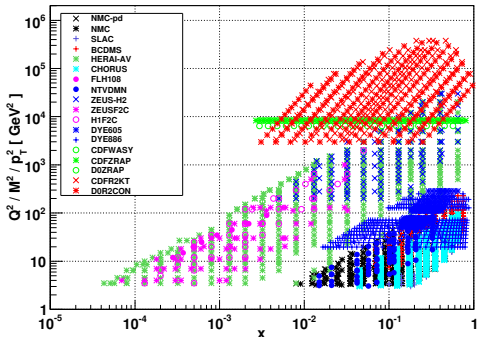
- We use **Neural Networks** as **functions** to represent **PDFs at the starting scale**
  - They provide a parametrization which is **redundant** and **robust** against variations
- We employ **Multilayer Feed-Forward** Neural Networks trained using a **Genetic Algorithm**
  - Very efficient for complex parameter spaces
  - Reduces the probability of being trapped in local minima
- Stopping of the fit for each replica is determined by **cross-validation** method
  - Ensures proper proper fitting avoiding overlearning



# NNPDF2.1

A family of global fits ...

NNPDF2.1 dataset



**3338** data points (NLO fit)  
(3330 - LO and 3445 - NNLO)

[R. D. Ball et. al, arXiv:1101.1300] - NLO  
[R. D. Ball et. al, arXiv:1107.2652] - LO/NNLO

OBS	Data set
<b>Deep Inelastic Scattering</b>	
$F_2^d / F_2^p$	NMC-pd
$F_2^p$	NMC, SLAC, BCDMS
$F_2^d$	SLAC, BCDMS
$\sigma_{NC}^{\pm}$	HERA-I, ZEUS (HERA-II)
$\sigma_{CC}^{\pm}$	HERA-I, ZEUS (HERA-II)
$F_L$	H1
$\sigma_{\nu}, \sigma_{\bar{\nu}}$	CHORUS
dimuon prod.	NuTeV
$F_2^c$	ZEUS, H1

<b>Drell-Yan &amp; Vector Boson prod.</b>	
$d\sigma^{DY} / dM^2 dy$	E605
$d\sigma^{DY} / dM^2 dx_F$	E866
W asymm.	CDF
Z rap. distr.	D0/CDF

<b>Inclusive jet prod.</b>	
Incl. $\sigma^{(jet)}$	CDF ( $k_T$ ) - Run II
Incl. $\sigma^{(jet)}$	D0 (cone) - Run II



# NNPDF2.1

... based on the NNPDF Methodology

## Parton Distributions Combination

## NN architecture

Singlet ( $\Sigma(x)$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Gluon ( $g(x)$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Total valence ( $V(x) \equiv u_V(x) + d_V(x)$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Non-singlet triplet ( $T_3(x)$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Sea asymmetry ( $\Delta_S(x) \equiv \bar{d}(x) - \bar{u}(x)$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Total Strangeness ( $s^+(x) \equiv (s(x) + \bar{s}(x))/2$ )	$\Rightarrow$	2-5-3-1 (37 pars)
Strange valence ( $s^-(x) \equiv (s(x) - \bar{s}(x))/2$ )	$\Rightarrow$	2-5-3-1 (37 pars)

**259** parameters

Standard fits have  $\sim 25$  parameters in total

**No change in the parametrization** since NNPDF1.2 ... despite substantial **enlargement of the dataset.**



# NNPDF2.1

... including Heavy Flavour contributions (FONLL)

- We adopt the **FONLL** General Mass-Variable Flavour Number Scheme

[M. Cacciari, M. Greco and P. Nason, (1998)]

[S. Forte, P. Nason E. Laenen and J. Rojo, (2010)]

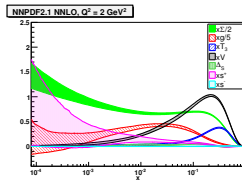
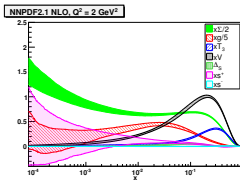
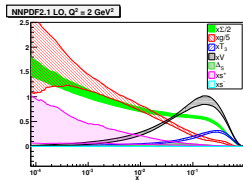
- FONLL gives a prescription to **combine FFN** (Massive) and **ZM-VFN** (Massless) computations, at any given order, **avoiding double counting**.
- With available computations three implementations of FONLL are possible:
  - **FONLL-A**:  $\mathcal{O}(\alpha_s)$  Massless +  $\mathcal{O}(\alpha_s)$  Massive - (NLO fit)
  - **FONLL-B**:  $\mathcal{O}(\alpha_s)$  Massless +  $\mathcal{O}(\alpha_s^2)$  Massive
  - **FONLL-C**:  $\mathcal{O}(\alpha_s^2)$  Massless +  $\mathcal{O}(\alpha_s^2)$  Massive - (NNLO fit)
- **Fixed Flavour Number Scheme** (3-, 4-, 5-) fits **available**.



# NNPDF2.1

... a (PDF) family portrait

- At the starting scale ( $2 \text{ GeV}^2$ ) ...

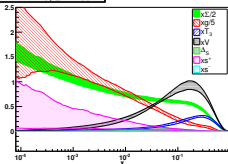


# NNPDF2.1

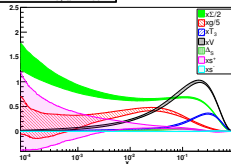
... a (PDF) family portrait

- At the starting scale ( $2 \text{ GeV}^2$ ) ...

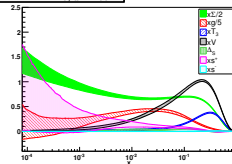
NNPDF2.1 LO,  $Q^2 = 2 \text{ GeV}^2$



NNPDF2.1 NLO,  $Q^2 = 2 \text{ GeV}^2$

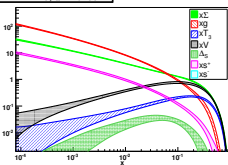


NNPDF2.1 NNLO,  $Q^2 = 2 \text{ GeV}^2$

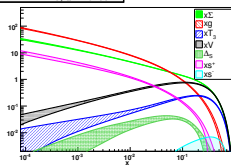


- ... and at the typical EW scale ( $100 \text{ GeV}^2$ )

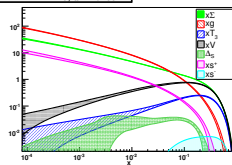
NNPDF2.1 LO,  $Q^2 = 10^4 \text{ GeV}^2$



NNPDF2.1 NLO,  $Q^2 = 10^4 \text{ GeV}^2$



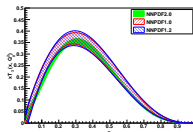
NNPDF2.1 NNLO,  $Q^2 = 10^4 \text{ GeV}^2$



# NNPDF2.1

Partons - A couple of upshots

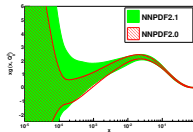
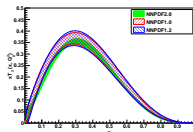
- **Reduction of uncertainties** with respect to older NNPDF sets due to **inclusion of new data**



# NNPDF2.1

Partons - A couple of upshots

- **Reduction of uncertainties** with respect to older NNPDF sets due to **inclusion of new data**
- When **uncertainties increase** we know it is **not a parametrization effect**

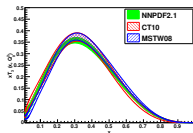
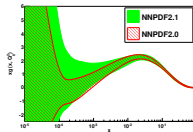
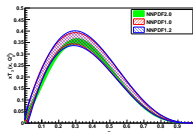




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Partons - A couple of upshots

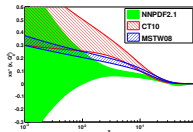
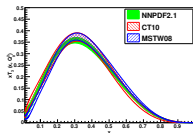
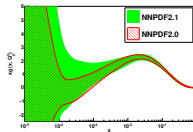
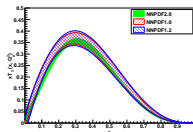
- **Reduction of uncertainties** with respect to older NNPDF sets due to **inclusion of new data**
- When **uncertainties increase** we know it is **not a parametrization effect**
- **Uncertainties** on PDFs have **size comparable** to those obtained by other groups when there are significant **constraints from data** ...



# NNPDF2.1

Partons - A couple of upshots

- **Reduction of uncertainties** with respect to older NNPDF sets due to **inclusion of new data**
- When **uncertainties increase** we know it is **not a parametrization effect**
- **Uncertainties** on PDFs have **size comparable** to those obtained by other groups when there are significant **constraints from data** ...
- ... but **no functional bias** in kinematic regions where there are little or **no experimental constraints**.

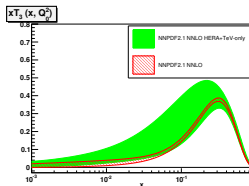
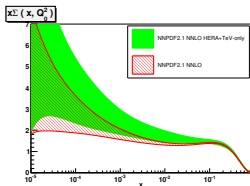
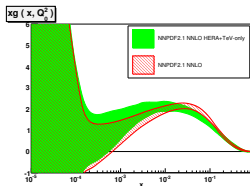


## Comparisons to LHC data

# NNPDF2.1: fits to reduced datasets

## Collider-only fit

- The (proton) fit we would love to have ...
  - Only **high energy data**: minimize effects of higher-twist contributions
  - Only **proton data**: no assumptions based on models for nuclear corrections
- Based on **HERA and Tevatron** (inclusive jets and W/Z production) data



- **LHC** (and HERA-II combined) **data are crucial** in order to improve collider-only fit



# LHC4PDFs

... the data we would love to have from the LHC

- Medium- and large- $x$  **gluon**
  - Prompt photons
  - Inclusive Jets
  - $t$ -quark distributions ( $p_{\perp}, y$ ) (?)
- **Light flavour separation** at medium- & small- $x$ 
  - Low-mass Drell-Yan
  - High-mass  $W$  production
  - $Z$  rapidity distribution
  - $W(+\text{jets})$  asymmetry
- **Strangeness & Heavy Flavours**
  - $W + c$
  - $Z + c, \gamma + c$
  - $Z + b$

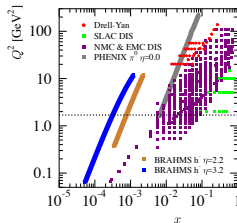
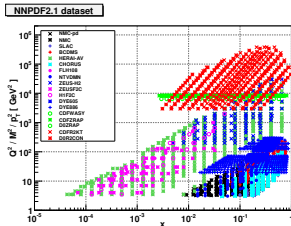


# A QUICK LOOK IN THE NUCLEAR TERRITORY



## The case for having them

- Nuclear PDFs are determined from a much more restricted dataset than proton ones



- In the standard approach to PDF extractions (used by EPS, HKN and nDS sets) uncontrolled theoretical assumption on the functional form of PDFs can be a source of large bias
- The NNPDF methodology is ideally suited to provide a reliable estimation of the uncertainties in a situation where experimental constraints are very loose

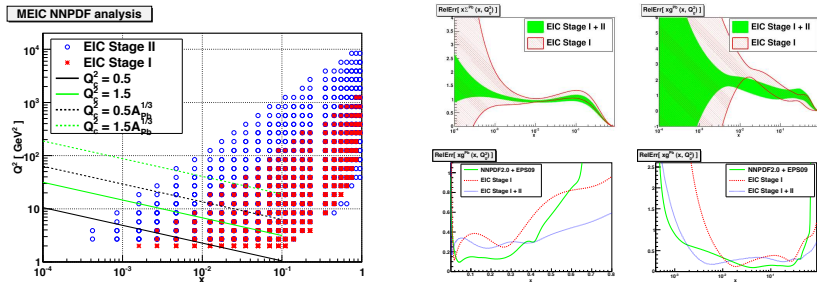


# Nuclear NNPDFs

EIC White Book - the first NNPDF steps in the nuclear territory

[A. Accardi, V. Guzey and J. Rojo, arXiv:1106.3839]

- One of the physics goal of the proposed Electron Ion Collider (EIC) is the determination of nuclear PDFs
- The NNPDF methodology has been used to extract the Singlet and gluon PDFs from a fit to simulated EIC  $e$ -Pb pseudodata





# Conclusions & Outlook

- A set of PDF with a **reliable** estimation of **uncertainties** is crucial in order to exploit the full physics potential of the LHC experiments (both for  $pp$  and  $AA$ ).
- The **NNPDF2.1** family of PDF sets fulfills the requirement of an ideal parton densities set for precision ( $pp$ ) phenomenology at the LHC
- The NNPDF Methodology is ideally suited to tackle problems that affect standard global (nuclear) fits (loose constraints from data, parametrization bias, etc.)
- ... moreover, plenty of new data will come from the LHC probing different nPDF combinations and providing more stringent constraints

