JETS IN A QUARK-GLUON PLASMA

Konrad Tywoniuk



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Large time domain for pQCD: $\frac{1}{\sqrt{s}} < t < \frac{\sqrt{s}}{\Lambda_{\text{OCD}}^2}$

QCD COHERENCE IN VACUUM

[Dokshitzer, Fadin, Khoze, Troyan, Lipatov, Bassetto, Mueller, Ciafaloni, Marchesini....]

 $\propto \frac{d\omega_i}{\omega_i} \frac{d\theta_i}{\theta_i} \Theta \left(\theta_{i-1} - \theta_i\right)$



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- soft & collinear divergences
- interferences ⇒ angular ordering

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EXPERIMENTAL EVIDENCE





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$$\kappa^{i} = k^{i} - xp^{i}$$



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1

$$\omega \frac{dN^{\text{vac}}}{d^3k} = \frac{\alpha_s}{(2\pi)^2 \omega^2} \left(Q_q^2 \mathcal{R}_{\text{coh}} + (Q_q + Q_{\bar{q}})^2 \mathcal{J} \right)$$

 $\mathcal{R}_{\rm coh} = \mathcal{R}_q + \mathcal{R}_{\bar{q}} - 2\mathcal{J}$





Fundamental building block of the QCD cascade!

$$\langle dN_q \rangle_{\varphi} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta} \Theta(\cos\theta - \cos\theta_{q\bar{q}})$$

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Q2 (easier): how will the antenna radiation pattern look like in medium?



CMS Experiment at LHC, CERN Data recorded: Mon Nov 8 11:30:53 2010 CEST Run/Event: 150431 / 630470 Lumi section: 173

HOW DOES A JET LOOK LIKE IN A NUCLEUS-NUCLEUS COLLISION?



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I) large energy loss of leading particle



II) soft gluons at large angles



Energy loss:
$$\Delta E \simeq \frac{\alpha_s C_R}{2\pi} \hat{q} L^2$$

Broadening: $k_{\perp}^2 \simeq \hat{q} L \propto \frac{\Delta E}{L}$



Baier, Dokshitzer, Mueller, Peigne, Schiff (1997-2001), Zakharov (1996), Wiedemann (2000), Gyulassy, Levai, Vitev (2001-2002)

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emitted off a **single emitter**



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wdl∕dwdĸ²

-0.1

10^2

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gluon interaction \Rightarrow k₁-broadening



 $\omega/\omega_{e}=0.4$

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- transport parameter: $\hat{q} = m_D^2 / \lambda$



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10-1

0

10-2

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- energy loss distribution: $P(\Delta E)$
- need more emitters to see coherence!





Mehtar-Tani, Salgado, KT PRL 106 (2011) 122002 Mehtar-Tani, Salgado, KT arXiv:1102.4317 [hep-ph]

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- medium is modeled as a classical background field



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$$J_q(x) = g U_p(x^+, 0) \,\delta^{(3)}(\vec{x} - \frac{p}{E}t) \Theta(t) \,Q_q \qquad J \equiv J_q + J_{\bar{q}}$$

Classical Yang-Mills eq: $[D_{\mu}, F^{\mu\nu}] = J^{\nu}$, $[D_{\mu}, J^{\mu}] = 0$

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Classical Yang-Mills eq: $[D_{\mu}, F^{\mu\nu}] = J^{\nu}$, $[D_{\mu}, J^{\mu}] = 0$ Linear response: $\Box A^{i} - 2ig [A^{-}_{med}, \partial^{+}A^{i}] = -\frac{\partial^{i}}{\partial^{+}}J^{+} + J^{i}$

Gelis, Mehtar-Tani (2005), Mehtar-Tani (2007)

ANTENNA IN MEDIUM

Y. Mehtar-Tani, KT arXiv:1105.1346 [hep-ph] C.A. Salgado,Y. Mehtar-Tani, KT, in preparation E. lancu, J. Casalderrey-Solana arXiv:1105.1760 [hep-ph]

Multiple scattering \Rightarrow effective propagators:

$$\mathcal{J} = \operatorname{Re}\left\{\int_{0}^{\infty} dy'^{+} \int_{0}^{y'^{+}} dy^{+} \left(1 - \Delta_{\operatorname{med}}(y^{+}, 0)\right)\right\}$$



$$\times \int d^2 \boldsymbol{z} \exp\left[-i\bar{\boldsymbol{\kappa}} \cdot \boldsymbol{z} - \frac{1}{2} \int_{y'^+}^{\infty} d\xi \, n(\xi) \sigma(\boldsymbol{z}) + i\frac{k^+}{2} \delta \boldsymbol{n}^2 y^+\right] \qquad |\delta n| \simeq \theta_{q\bar{q}}$$

$$\times \left(\boldsymbol{\partial}_{y} - ik^{+} \, \delta \boldsymbol{n} \right) \cdot \boldsymbol{\partial}_{z} \, \mathcal{K}(y^{\prime +}, \boldsymbol{z}; \, y^{+}, \boldsymbol{y} \, | k^{+}) \big|_{\boldsymbol{y} = \delta \boldsymbol{n} y^{+}} \right\} + \text{sym.}$$

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 + sym.

Describes Brownian motion through medium potential...

$$\mathcal{K}\left(y^{\prime+}, \boldsymbol{z}; y^{+}, \boldsymbol{y} | k^{+}\right) = \int \mathcal{D}[\boldsymbol{r}] \exp\left[\int_{y^{+}}^{y^{\prime+}} d\xi \left(i\frac{k^{+}}{2}\dot{\boldsymbol{r}}^{2}(\xi)\right) \cdot \frac{1}{2}n(\xi)\sigma(\boldsymbol{r})\right)\right]$$
$$\sigma(\mathbf{r}) = 2\alpha_{S}C_{A} \int \frac{d^{2}\mathbf{q}}{(2\pi)^{2}} \mathcal{V}^{2}(\mathbf{q}) \left[1 - \cos(\mathbf{r} \cdot \mathbf{q})\right]$$

The opacity expansion

[Baier, Dokshitzer, Mueller, Peigne, Schiff, Wiedemann]

Propagation and interaction is encoded in the path integral:

$$\mathcal{K}\left(y^{\prime+}, \boldsymbol{z}; y^{+}, \boldsymbol{y} | k^{+}\right) = \int \mathcal{D}[\boldsymbol{r}] \exp\left[\int_{y^{+}}^{y^{\prime+}} d\xi \left(i\frac{k^{+}}{2}\dot{\boldsymbol{r}}^{2}(\xi) - \frac{1}{2}n(\xi)\sigma(\boldsymbol{r})\right)\right]$$

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Expansion in terms of $n(\xi)\sigma(r) \Rightarrow$ the medium opacity:

$$\mathcal{K}(\mathbf{r}, y_l; \mathbf{\bar{r}}, \bar{y}_l) = \mathcal{K}_0(\mathbf{r}, y_l; \mathbf{\bar{r}}, \bar{y}_l)$$

$$- \int_{z}^{z'} d\xi \, n(\xi) \, \int d\boldsymbol{\rho} \, \mathcal{K}_0(\mathbf{r}, y_l; \boldsymbol{\rho}, \xi) \, \frac{1}{2} \, \sigma(\boldsymbol{\rho}) \, \mathcal{K}_0(\boldsymbol{\rho}, \xi; \mathbf{\bar{r}}, \bar{y}_l)$$

$$+ \int_{z}^{z'} d\xi_1 \, n(\xi_1) \, \int_{\xi_1}^{z'} d\xi_2 \, n(\xi_2) \, \int d\boldsymbol{\rho}_1 \, d\boldsymbol{\rho}_2 \, \mathcal{K}_0(\mathbf{r}, y_l; \boldsymbol{\rho}_1, \xi_1)$$

$$\times \frac{1}{2} \, \sigma(\boldsymbol{\rho}_1) \, \mathcal{K}(\boldsymbol{\rho}_1, \xi_1; \boldsymbol{\rho}_2, \xi_2) \, \frac{1}{2} \, \sigma(\boldsymbol{\rho}_2) \, \mathcal{K}_0(\boldsymbol{\rho}_2, \xi_2; \mathbf{\bar{r}}, \bar{y}_l) \,. \quad (6.2)$$
MODELING THE MEDIUM

Poisson equation:
$$-\partial_{\perp}^2 A_{\text{med}}^-(x^+, x) = \rho_{\text{med}}(x^+, x)$$

Gaussian approximation:

 $\langle \rho_{\text{med}}^{a}(x^{+}, \boldsymbol{q}) \rho_{\text{med}}^{*b}(x^{\prime +}, \boldsymbol{q}^{\prime}) \rangle = \delta^{ab} m_{D}^{2} n(x^{+}) \ \delta(x^{+} - x^{\prime +}) \ (2\pi)^{2} \delta^{(2)}(\boldsymbol{q} - \boldsymbol{q}^{\prime}) \\ \langle \mathcal{A}_{\text{med}}^{a}(x^{+}, \boldsymbol{q}) \mathcal{A}_{\text{med}}^{*b}(x^{\prime +}, \boldsymbol{q}^{\prime}) \rangle = \delta^{ab} m_{D}^{2} n(x^{+}) \ \delta(x^{+} - x^{\prime +}) \\ \times (2\pi)^{2} \delta^{(2)}(\boldsymbol{q} - \boldsymbol{q}^{\prime}) \ \mathcal{V}^{2}(\boldsymbol{q})$

- Medium is a set of static potentials with screening length m_D⁻¹
 No recoil
- Mean free path: λ

$$\mathcal{V}(\boldsymbol{q}) \;=\; rac{1}{\boldsymbol{q}^2 + m_D^2}$$

AMPLITUDE AT N=1

Describes two physical processes of a virtual parton traversing the medium:

$$\mathcal{M}^{a}_{(1)\lambda,q} = 2 i g^{2} \int \frac{d^{2} q}{(2\pi)^{2}} \int_{0}^{\infty} dx^{+} \left[T \cdot \mathcal{A}_{\mathrm{med}}(x^{+},q) \right]^{ab} Q^{b}_{q} e^{i(k^{-}-v^{-})x^{+}}$$

$$\times \left[\frac{\nu}{\nu^{2}} - L \exp\left(i\frac{\nu^{2}}{2k^{+}}x^{+}\right)\right] \cdot \epsilon_{\lambda}$$

$$\kappa^{i} = k^{i} - xp^{i}$$

$$\nu^{i} = k^{i} - q^{i} - xp^{i}$$

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$$\omega \frac{dN_q^{\text{indep}}}{d\omega \, d^2 \boldsymbol{k}} = \frac{8 \, \alpha_s C_F \, \hat{q}}{\pi} \int_{\mathcal{V}(\boldsymbol{q})} \int_0^{L^+} dx^+ \left(1 - \cos \frac{(\boldsymbol{k} - \boldsymbol{q})^2}{2k^+} x^+\right) \frac{\boldsymbol{k} \cdot \boldsymbol{q}}{\boldsymbol{k}^2 (\boldsymbol{k} - \boldsymbol{q})^2}$$

Incoherent limit:
$$\hat{q} \int_{\mathcal{V}(\boldsymbol{q})} \frac{\boldsymbol{k} \cdot \boldsymbol{q}}{\boldsymbol{k}^2 (\boldsymbol{k} - \boldsymbol{q})^2} = \frac{\hat{q}}{2} \int_{\mathcal{V}(\boldsymbol{q})} \left(-\frac{1}{\boldsymbol{k}^2} + \frac{1}{(\boldsymbol{k} - \boldsymbol{q})^2} + \boldsymbol{L}^2 \right)$$

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$$\lim_{L \to \infty} \sum_{m=0}^{N=1} \frac{d^3 \sigma^{(nas)}(m)}{d(\ln x) \, d\mathbf{k}_{\perp}} = \frac{\alpha_s}{\pi^2} \, N_C \, C_F$$

$$\times \left[(1 - w_1) H(\mathbf{k}_{\perp}) + n_0 \, L \, \int_{\mathbf{q}_1} H(\mathbf{k}_{\perp} + \mathbf{q}_{1\perp}) \right]$$

$$+ n_0 \, L \, \int_{\mathbf{q}_1} R(\mathbf{k}_{\perp}, \mathbf{q}_{1\perp}) \right] \, .$$

$$Wiedemann (2004)$$

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Probabilistic
interpretation!
Wiedemann (2000)

and the second

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two phase structures:

- "dipole" phase, involving the opening angle
- **LPM phase**, describing rescattering interference

- two vertices:
 - Lipatov vertex
 - "gluon-gluon" vertex

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two phase structures:

- "dipole" phase, involving the opening angle
- **LPM phase**, describing rescattering interference

- two vertices:
 - Lipatov vertex
 - "gluon-gluon" vertex

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$$\lim_{\omega \to 0} \boldsymbol{L} \cdot \bar{\boldsymbol{L}} = \frac{\boldsymbol{\kappa} \cdot \bar{\boldsymbol{\kappa}}}{\boldsymbol{\kappa}^2 \bar{\boldsymbol{\kappa}}^2}$$

- vacuum-like
- antiangular ordered

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SATURATION

$$\Delta_{\rm med}(\theta_{q\bar{q}},L) \equiv \frac{\hat{q}}{m_D^2} \int_0^{L^+} \mathrm{d}x^+ \left[1 - \frac{|\mathbf{r}_{\perp}| m_D x^+}{L^+} K_1\left(\frac{|\mathbf{r}_{\perp}| m_D x^+}{L^+}\right)\right]$$

Medium decoherence parameter $|r_{\perp}| = |\delta n| L^+ \simeq \theta_{q\bar{q}} L$ \Rightarrow controls the cancellation of interferences

$$\Delta_{\text{med}} \approx \frac{1}{6} \ \hat{q} L^+ r_{\perp}^2 \left[\ln \frac{1}{r_{\perp} m_D} + \text{const.} \right] \quad \blacksquare \quad \mathbf{r}_{\perp}^{-1} \gg \mathbf{m}_D$$
$$\qquad \blacksquare \quad \text{``dipole'' regime}$$

 $\Delta_{\rm med} \approx n_0 L^+ \equiv N_{\rm scat}$

• $r_{\perp}^{-1} \ll m_D$

"saturation" regime

MULTIPLE SCATTERING

Wilson line along the trajectory:

$$U_p(x^+, 0) = \mathcal{P}_+ \exp\left\{ ig \int_0^{x^+} dz^+ \left[T \cdot A^-_{\text{med}}(z^+, z^+ p_\perp / p^+) \right] \right\}$$

Only the quarks are rotated in color: $J_q^{\mu,a}(k) = -ig \frac{p^{\mu}}{p \cdot k} U_p^{ab}(L,0) Q_q^b$

$$\Delta_{\rm med} = 1 - \frac{1}{N_c^2 - 1} \langle \mathbf{Tr} \, U_p(x^+, 0) U_{\bar{p}}^{\dagger}(x^+, 0) \rangle$$



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Multiple soft scattering approximation

$$\Delta_{\mathrm{med}} \approx 1 - e^{-\frac{1}{12}\hat{q}\,\theta_{q\bar{q}}^2\,L^3}$$



q: medium transport coefficient





 $\Theta_{qar{q}}$

- $\Delta_{\text{med}} \rightarrow 0$ **Coherence**
- $\Delta_{\text{med}} \rightarrow 1$ **Decoherence**

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 $dN_{q,\gamma^*}^{\text{tot}} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{\sin\theta \ d\theta}{1 - \cos\theta} \left[\Theta(\cos\theta - \cos\theta_{q\bar{q}}) + \Delta_{\text{med}} \Theta(\cos\theta_{q\bar{q}} - \cos\theta)\right] \,.$ 12 Mehtar-Tani, Salgado, KT PRL 106 (2011) 122002 $dN_{q,\gamma^*}^{\text{tot}}\Big|_{\text{opaque}} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{\sin\theta \ d\theta}{1 - \cos\theta}.$ 8 medium-induced radiation 1) Independent emissions! vacuum radiation 2) "Memory loss" effect 2 0 0.1 0.2 0.3 0.4 0



DECOMPOSITION

$$\mathcal{R}_{q}^{\text{med}} = 32\pi \hat{q} \int_{\mathcal{V}(\boldsymbol{q})} \int_{0}^{L^{+}} dx^{+} \left[1 - \cos\left(\frac{\boldsymbol{\nu}^{2}}{2k^{+}}x^{+}\right) \right] \frac{\boldsymbol{\nu}}{\boldsymbol{\nu}^{2}} \cdot \boldsymbol{L}$$
$$\mathcal{J}_{q}^{\text{med}} = -32\pi \hat{q} \int_{\mathcal{V}(\boldsymbol{q})} \int_{0}^{L^{+}} dx^{+} \left\{ \frac{1}{2} \left[1 - \cos\left(\frac{\boldsymbol{\nu} + \bar{\boldsymbol{\nu}}}{2} \cdot \delta \boldsymbol{n} x^{+}\right) \right] \boldsymbol{L} \cdot \bar{\boldsymbol{L}} - \left[1 - \cos\left(\frac{\boldsymbol{\nu}^{2}}{2k^{+}}x^{+}\right) \right] \frac{\bar{\boldsymbol{\nu}}}{\bar{\boldsymbol{\nu}}^{2}} \cdot \boldsymbol{L} \right\},$$

$$\omega \frac{dN_q^{\text{med}}}{d^3k} = \frac{\alpha_s C_F}{(2\pi)^2 \,\omega^2} \left(\mathcal{R}_q^{\text{med}} - \mathcal{J}_q^{\text{med}} \right)$$

- independent:
 BDMPS/GLV
- novel interferences



 $\mathcal{R}_q^{ ext{med}}$ $\mathcal{J}_q^{ ext{med}}$

 $1/\theta$











LARGE ANGLE BEHAVIOR



INSIDE THE CONE

$$\omega \frac{dN^{\text{med}}}{d^3k} = \frac{8\,\alpha_s C_F\,\hat{q}L^+}{\pi} \int_{\mathcal{V}(\boldsymbol{q})} \left(1 - \frac{\sin\Omega_q L^+}{\Omega_q L^+}\right) \left[\frac{\boldsymbol{\nu}}{\boldsymbol{\nu}^2} - \frac{k^+\delta\boldsymbol{n}}{(k^+\delta\boldsymbol{n})^2}\right] \cdot \left[\frac{\boldsymbol{\nu}}{\boldsymbol{\nu}^2} - \frac{\boldsymbol{\kappa}}{\kappa^2}\right]$$

$r_{\perp}^{-1} \gg m_D$

- this implies that ω » ω̄_c, spectrum is suppressed
 only for hard gluons in the "dipole" regime
 r_⊥⁻¹ « m_D
 - LPM phase is working
 - independent BDMPS/GLV spectrum close to the quark and antiquark
 - important in the "saturation" regime




C.A. Salgado, Y. Mehtar-Tani, KT, in preparation

SCALING BEHAVIORS



PROBABILISTIC INTERPRETATION

Incoherent limit $(L \rightarrow \infty)$ $\hat{q} \int_{\mathcal{V}(q)} \frac{\mathbf{k} \cdot \mathbf{q}}{\mathbf{k}^2 (\mathbf{k} - \mathbf{q})^2} = \frac{\hat{q}}{2} \int_{\mathcal{V}(q)} \left(-\frac{1}{\mathbf{k}^2} + \frac{1}{(\mathbf{k} - \mathbf{q})^2} + \mathbf{L}^2 \right)$

Inside the cone:

same probabilistic picture as before

conservation of probability

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 $\omega \frac{dN^{\text{med}}}{d^3 k} = \frac{8 \alpha_s C_F \hat{q}}{\pi} \int_{\mathcal{V}(q)} \int_0^{L^+} dx^+ \left[1 - \cos\left(\frac{\nu + \bar{\nu}}{2} \cdot \delta n \, x^+\right) \right] \left[L \cdot \bar{L} \right]$ Outside the cone: $\square \text{ medium induces new radiation!}$ $\square \text{ only Gunion-Bertsch, no hard component}$ $\square L^2$ $\square \text{ because no corresponding vacuum radiation!}$

CONCLUSIONS

 \star copious jets in heavy-ion collisions at the LHC * medium induces soft radiation at large angles \Rightarrow onset of decoherence \star a two scale problem: r_{\perp} vs. Q_s \Rightarrow jet probes medium, and vice versa * the radiation pattern off an antenna \Rightarrow building block for jet calculus in medium