

Multi-gauge-boson production at hadron colliders



Standard Model @ LHC 2012

Copenhagen – April 2012

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Definition:

- 1 a : many : multiple : much <*multi-valent*>
 - b : more than two <*multi-lateral*>
 - c : more than one <*multi-parous*> <*multi-billion*>
-
- 2 : many times over <*multi-millionaire*>

Origin:

Latin, from *multus* much, many

[Merriam-Webster online dictionary]

Definition:

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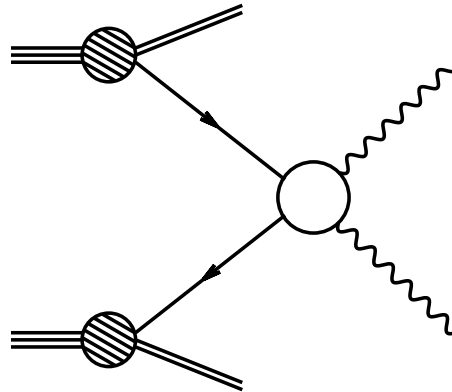
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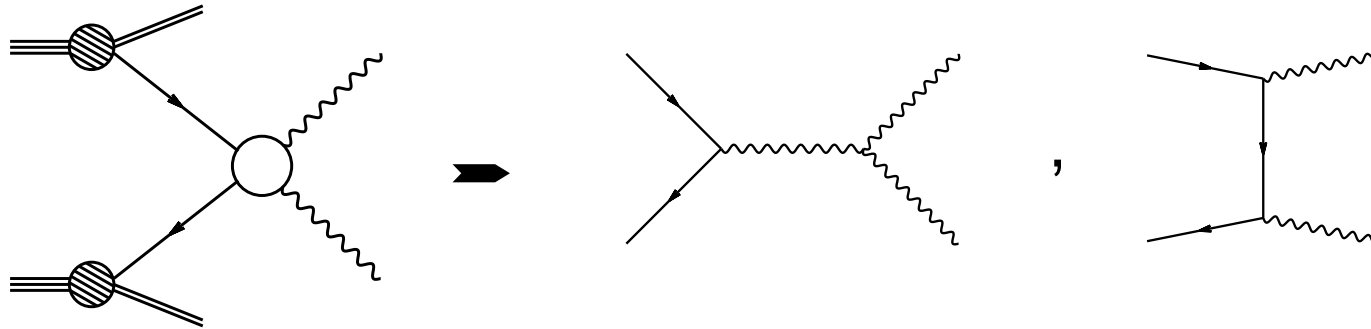
gauge-boson pair production



probe non-Abelian structure of the SM at high energies:

- ❖ (anomalous) **triple-gauge-boson couplings**
- ❖ dynamics of **longitudinal massive gauge bosons**

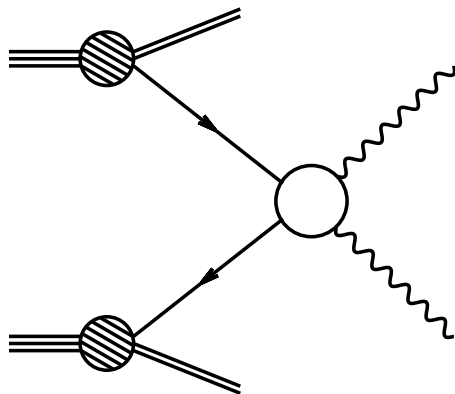
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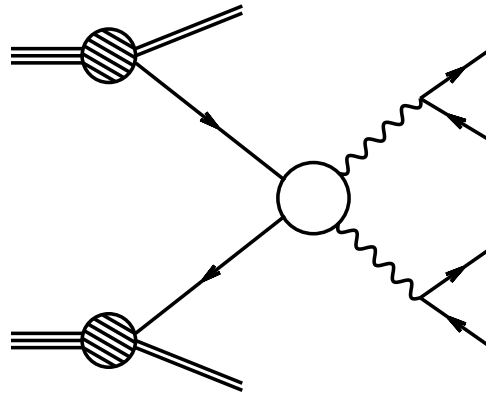
gauge-boson pair production



$pp \rightarrow VV \rightarrow 4f$
constitutes important class of
background processes to:

- ❖ the **Higgs search** in the mode $pp \rightarrow H \rightarrow VV \rightarrow 4f$
- ❖ **new physics searches** with leptons+ \cancel{E}_T signatures
(e.g. SUSY-particle pair production)

gauge-boson pair production

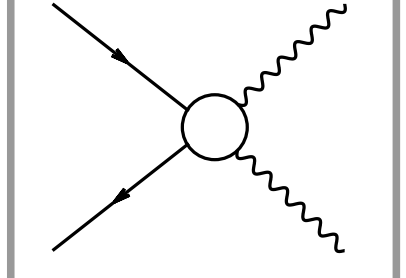


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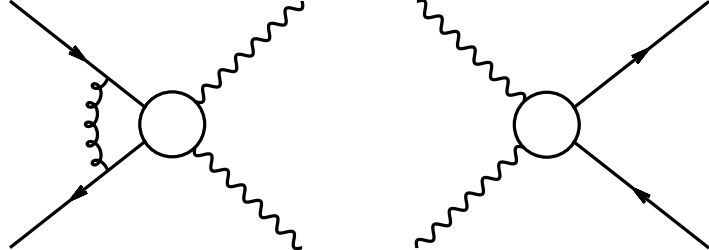
gauge-boson pair production @ NLO QCD

leading order contributions:

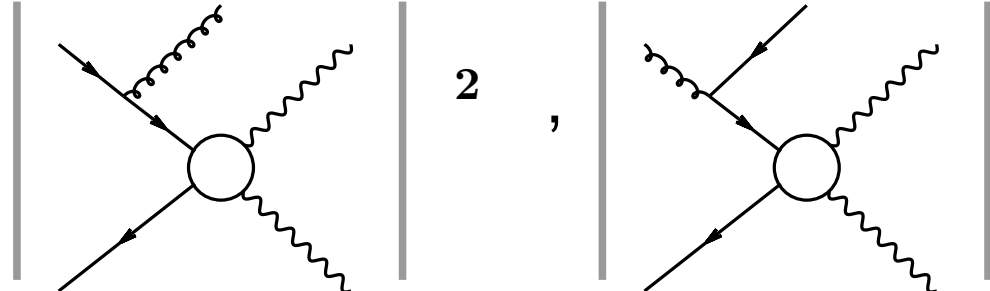
$$|\mathcal{M}_0|^2 = \left| \begin{array}{c} \text{---} \nearrow \\ \text{---} \searrow \\ \text{---} \nearrow \\ \text{---} \searrow \end{array} \right|_2$$


next-to-leading order QCD corrections:

virtual: $\mathcal{M}_V \mathcal{M}_0^* =$



real: $|\mathcal{M}_R|^2 = \left| \begin{array}{c} \text{---} \nearrow \\ \text{---} \searrow \\ \text{---} \nearrow \\ \text{---} \searrow \end{array} \right|_2, \left| \begin{array}{c} \text{---} \nearrow \\ \text{---} \searrow \\ \text{---} \nearrow \\ \text{---} \searrow \end{array} \right|_2$



gauge-boson pair production @ NLO QCD

$$h_1 h_2 \rightarrow ZZ:$$

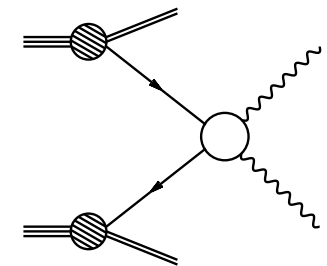
Ohnemus, Owens (1991) / Mele, Nason, Ridolfi (1991)

$$h_1 h_2 \rightarrow W^\pm Z:$$

Ohnemus (1991) / Frixione, Nason, Ridolfi (1992)

$$h_1 h_2 \rightarrow W^+ W^-:$$

Ohnemus (1991) / Frixione (1993)



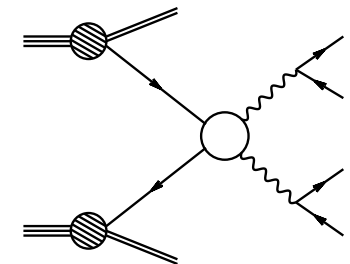
including leptonic decays:

analytical expressions:

Dixon, Kunszt, Signer (1998) / Baur, Han, Ohnemus (1996)

implementation in public code MCFM:

Campbell, Ellis (1999)



gauge-boson pair production @ NLO QCD

$$pp \rightarrow W^+(\rightarrow e^+\nu_e)W^-(\rightarrow \mu^-\bar{\nu}_\mu)$$

\sqrt{s} [TeV] and cuts	σ^{LO} [fb]	σ^{NLO} [fb]	K -factor
7 (basic)	144	249	1.73
7 (Higgs)	7.14	15.19	2.13
14 (basic)	296	566	1.91
14 (Higgs)	13.7	34.7	2.53

numbers taken from MCFM: *Campbell, Ellis, Williams (2011)*

gauge-boson pair production @ NLO QCD

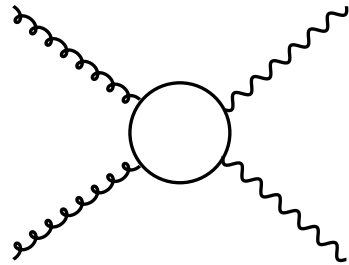
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- ❖ size of NLO-QCD corrections is large and cut-dependent
- ❖ not expected from variation of central scale

$$M_W/2 \leq \mu_f \leq 2M_W \text{ at LO } (\leftarrow \text{qg channels})$$

gauge-boson pair production – loop contributions



gluon-induced contributions
first occur at one-loop level

considered first by

Dicus, Kao, Repko (1987); Glover, van der Bij (1989)

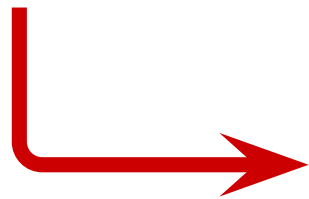
phenomenological study for the LHC:

Dührssen, Jakobs, van der Bij, Marquard (2005)

inclusion of off-shell effects and heavy-quark loops:

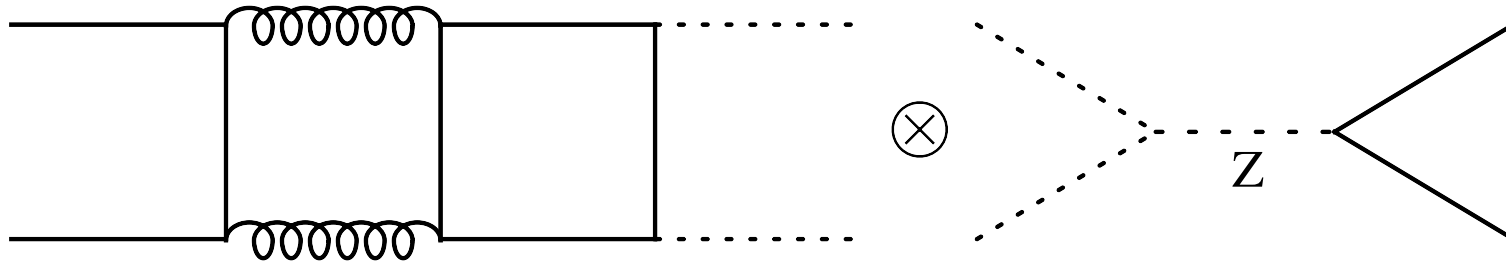
Binoth, Ciccolini, Kauer, Krämer (2005,2006);

Binoth, Kauer, Mertsch (2008)



impact depends on cuts;
can be large

gauge-boson pair production @ NNLO QCD



only small parts of the NNLO-QCD contributions
have been computed:

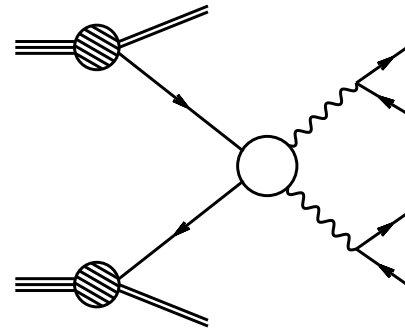
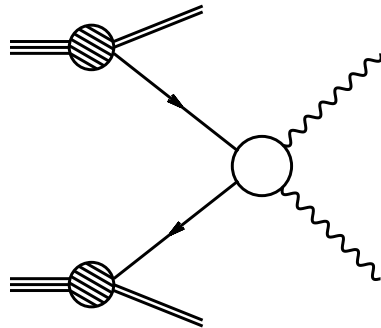
✓ two-loop and one-loop-squared virtual
QCD corrections in $q\bar{q}$ annihilation
in the high-energy limit (all invariants $\gg M_W^2$)

Chachamis, Czakon, Eiras (2008)

✗ no recent updates in the literature

gauge-boson pair production & parton showers

NLO-QCD calculations matched with multi-purpose parton-shower programs `PYTHIA`, `HERWIG`, `SHERPA`



MC@NLO :

Frixione, Webber (2002)

POWHEG :

Nason, Ridolfi (2006)

POWHEG in HERWIG++ :

Hamilton (2010)

POWHEG in SHERPA :

Höche, Krauss, Schönherr, Siegert (2010)

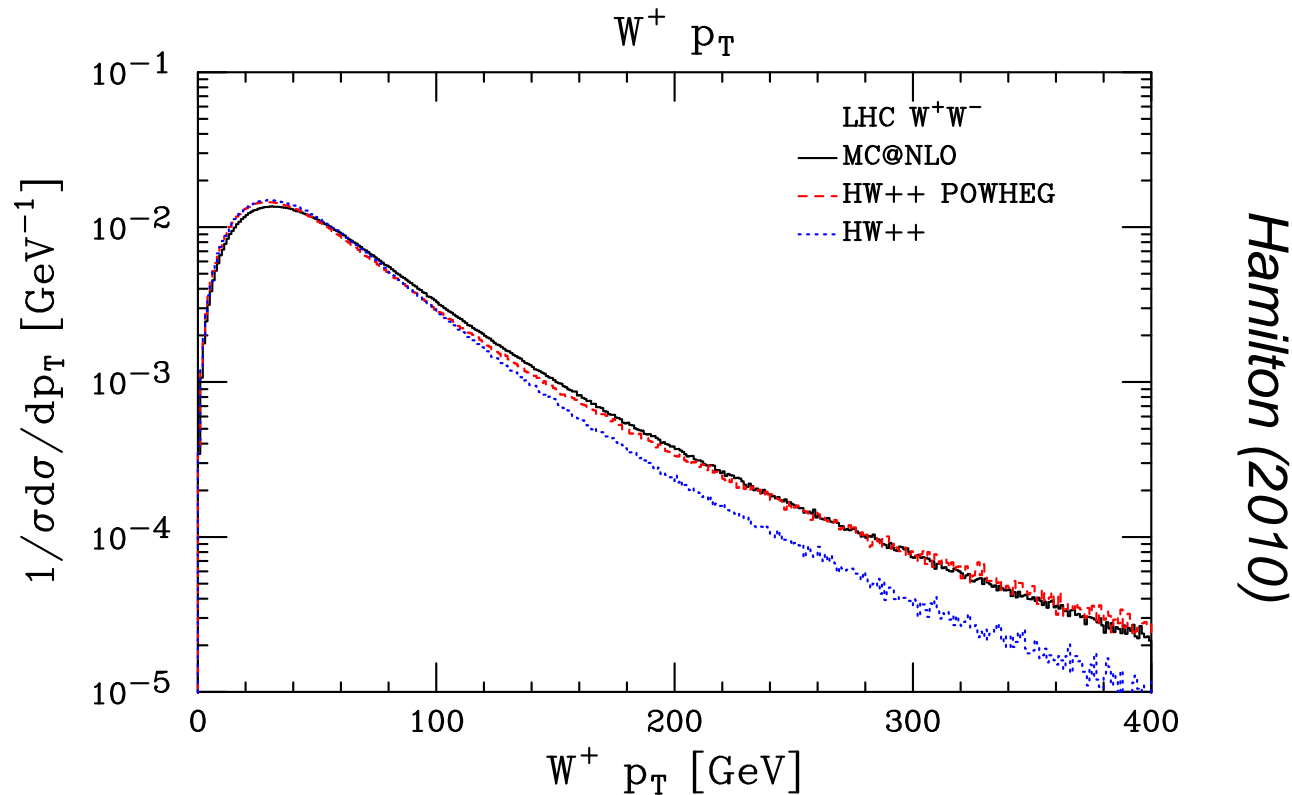
POWHEG-BOX :

Melia, Nason, Röntsch, Zanderighi (2011)

aMC@NLO :

Frederix et al. (2011)

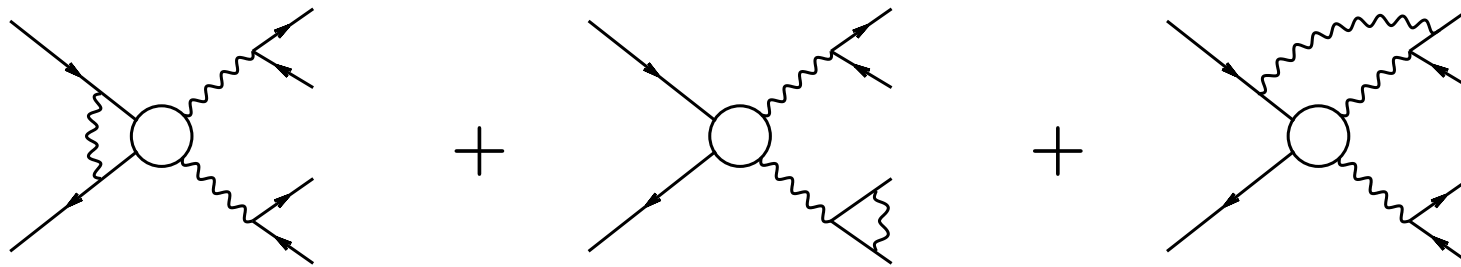
gauge-boson pair production & parton showers



- ❖ high- p_T tails: NLO+PS deviate from LO+PS results ($\leftarrow qg$)
- ❖ mostly: agreement between different NLO+PS simulations
- ❖ deviations between MC@NLO and POWHEG
in distributions sensitive to extra jet emission

gauge-boson pair production @ NLO EW

$pp \rightarrow VV \rightarrow 4 \text{ leptons}$: $\mathcal{O}(\alpha)$ corrections
more **challenging** than QCD corrections:



→ employ **approximations**:

- retain only universal logarithms that are large at high energies
- double pole approximation for gauge bosons

Accomando, Denner, Pozzorini, Kaiser (2001-2004)

gauge-boson pair production @ NLO EW

most general contribution to Lagrangian for WWV interaction, compatible with C and P conservation:

$$\mathcal{L}_{WWV} = g_{WWV} \left[ig_1^V (W_{\mu\nu}^* W^\mu V^\nu - W_{\mu\nu} W^{*\mu} V^\nu) + i\kappa^V W_\mu^* W_\nu V^{\mu\nu} + i\frac{\lambda^V}{M_W^2} W_{\rho\mu}^* W_\nu^\mu V^{\nu\rho} \right]$$

supplied by form factors to tame unitarity violations at high energies:

$$\Delta g \rightarrow \frac{\Delta g}{(1 + M_{VV}^2/\Lambda^2)^2}$$

maximum deviation from SM allowed by LEP bounds:

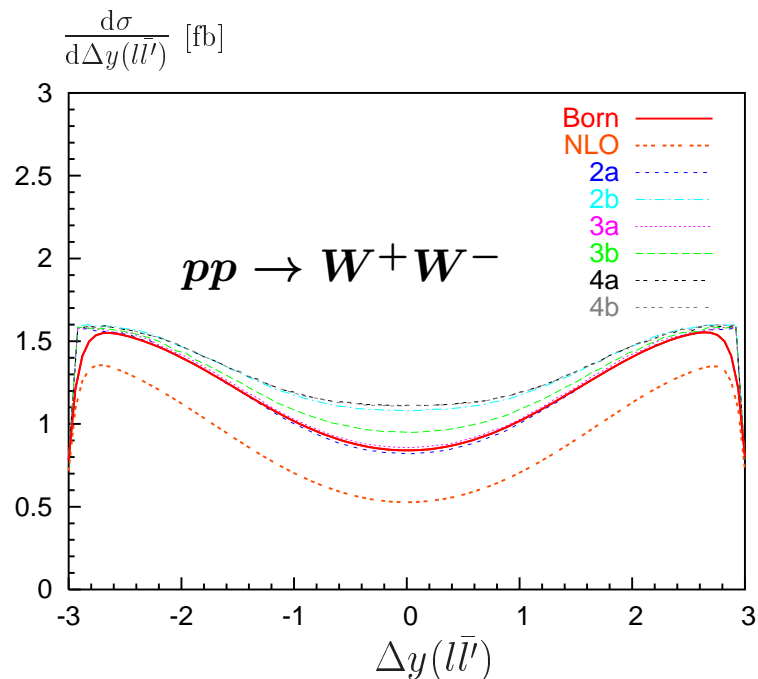
$$g_1^Z = -0.027, \quad \Delta\kappa^\gamma = -0.112, \quad \Delta\lambda^Z = \Delta\lambda^\gamma = -0.044$$

$$(\text{SM: } g_1^V = \kappa^V = 1 \text{ and } \lambda^V = 0)$$

gauge-boson pair production @ NLO EW

parameterize new physics by anomalous triple gauge boson couplings λ , $\Delta\kappa_\gamma$, Δg_1^Z

Accomando, Kaiser (2005)



Scenario	λ	Δg_1^Z	$\Delta\kappa_\gamma$
Born/NLO EW	0	0	0
2a/2b	0	± 0.02	0
3a/3b	0	0	± 0.04
4a/4b	± 0.02	0	0



EW corrections can fake anomalous triple-gauge boson couplings

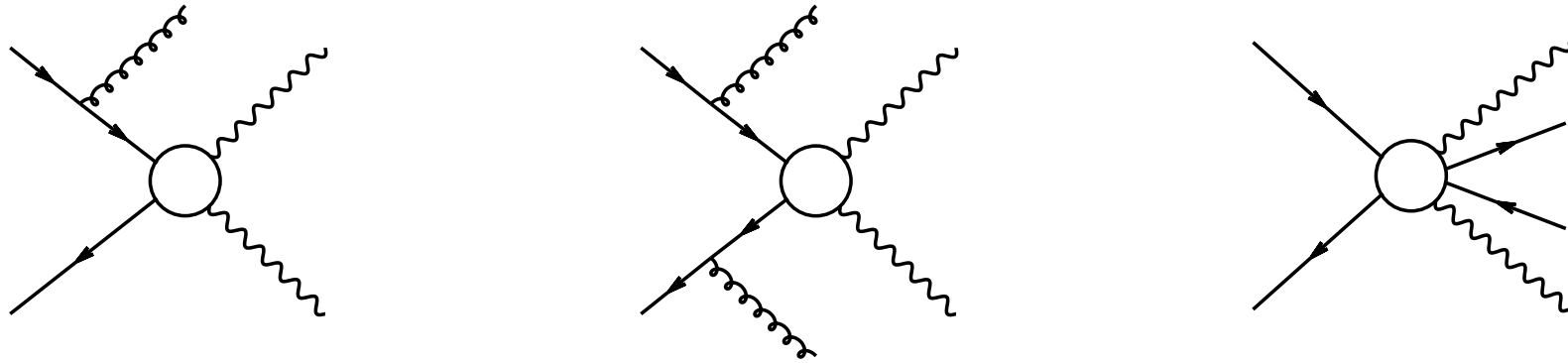
gauge-boson pair production @ NNLL EW

one- and two-loop **electroweak corrections** in
next-to-next-to-leading logarithmic approximation
in **high-energy limit**

Kühn, Metzler, Penin, Uccirati (2011)

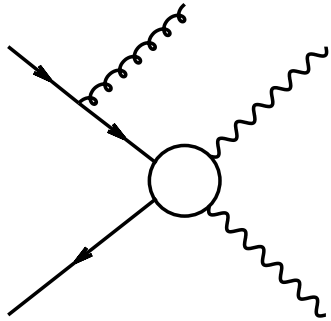
- ➡ maximal effect in distributions 60% (1-loop) and 20% (2-loop)
(partial compensation between
one- and two-loop contributions)

gauge-boson pairs in association with jets



- ❖ large fraction of V -pair events at the LHC exhibits additional jet activity
→ precise knowledge of $VV + \text{jets}$ processes needed for:
 - extraction of EW **gauge-boson couplings**
 - **search for Higgs** bosons in GF and VBF $H \rightarrow VV$ channels
 - search for various scenarios of **new physics**
- ❖ important test ground for multi-particle calculations at NLO-QCD

gauge-boson pairs in association with one jet



$pp \rightarrow WWj$ (without/with leptonic decays):

Dittmaier, Kallweit, Uwer (2007);

Campbell, Ellis, Zanderighi (2007) → MCFM

$pp \rightarrow ZZj$ (no decays):

Binoth, Gleisberg, Karg, Kauer, Sanguinetti (2010)

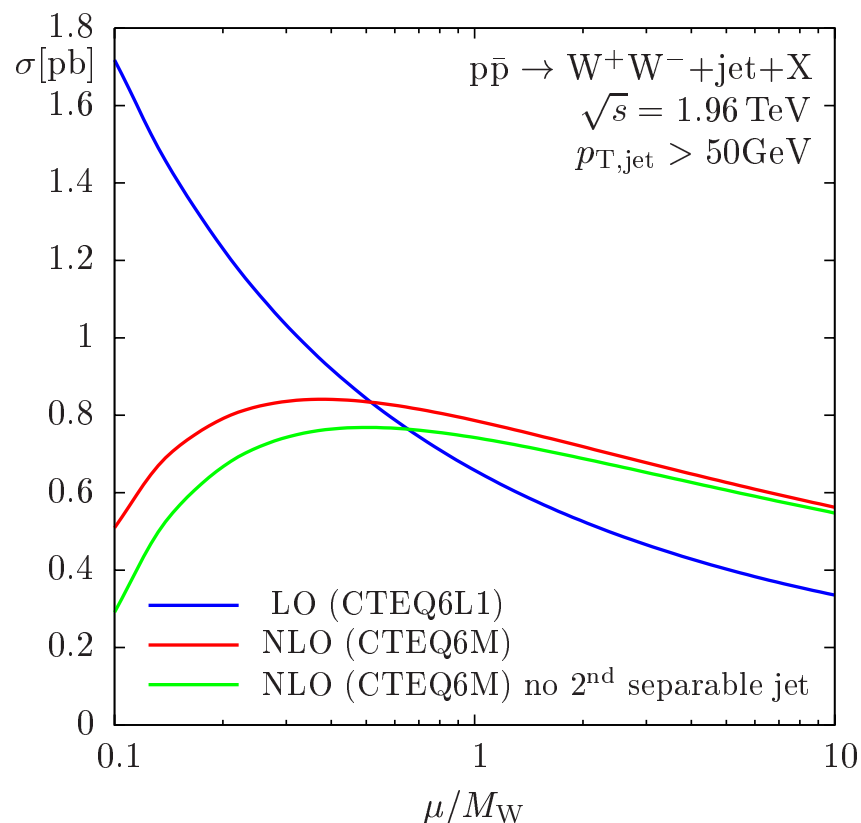
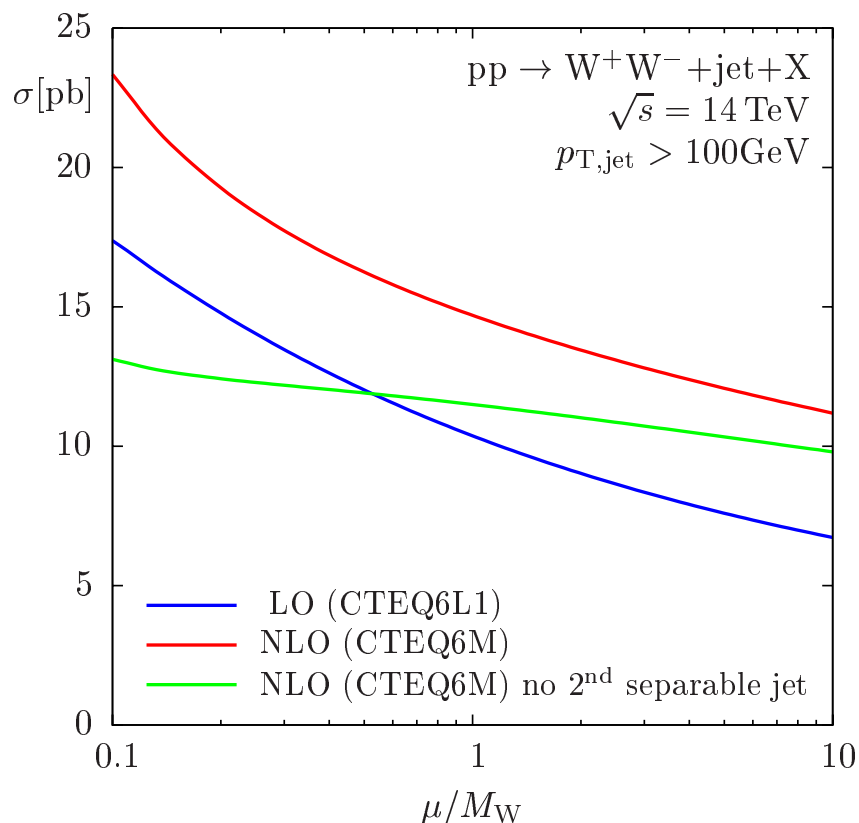
$pp \rightarrow WZj$ (including leptonic decays):

Campanario, Englert, Kallweit,

Spannowsky, Zeppenfeld (2010) → vbfnl0

- ❖ NLO-QCD **corrections** can be as **large** as 70%
- ❖ significant reduction of scale uncertainty at NLO-QCD
- ❖ effect of NLO-QCD corrections enhanced by cuts typical for Higgs search

gauge-boson pairs in association with jets



Dittmaier, Kallweit, Uwer (2009)

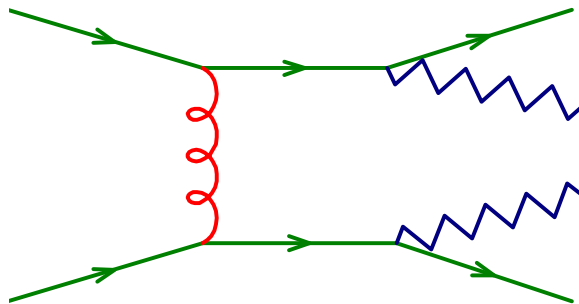
QCD corrections to x-sec can be reduced by **veto on extra jet**,
 but: perturbative stability of differential distributions can suffer

gauge-boson pairs in association with two jets

QCD-induced production

W^+W^+jj & W^+W^-jj :

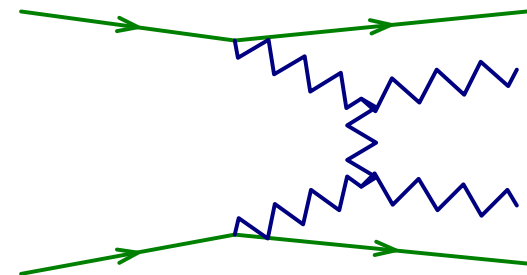
Melia, Melnikov, Rontsch, Zanderighi
(2010-2011)



EW production

all $VVjj$ channels:

Bozzi, Oleari, Zeppenfeld, B.J.
(2006-2009)

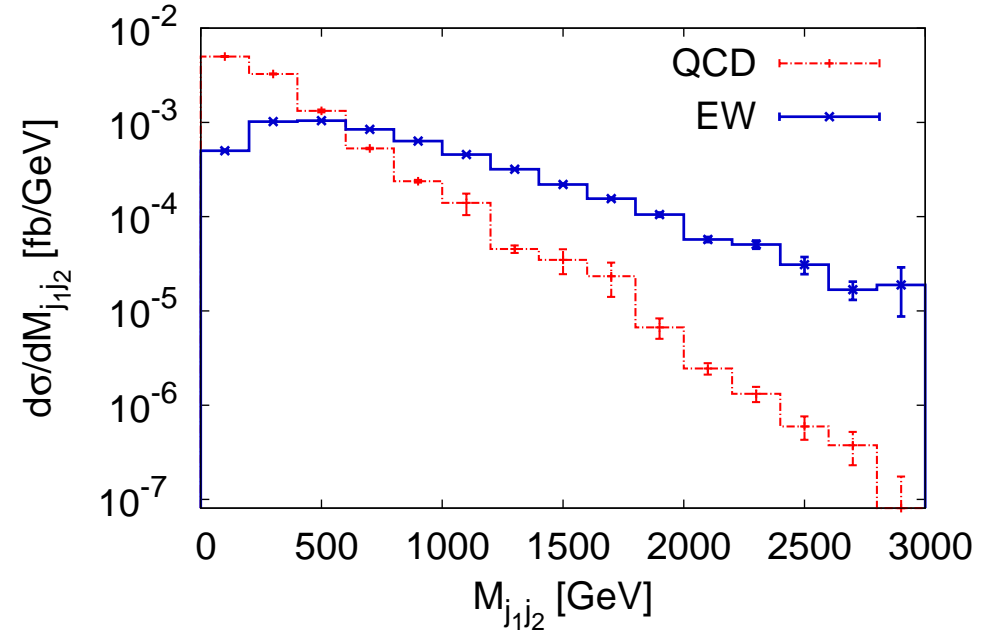
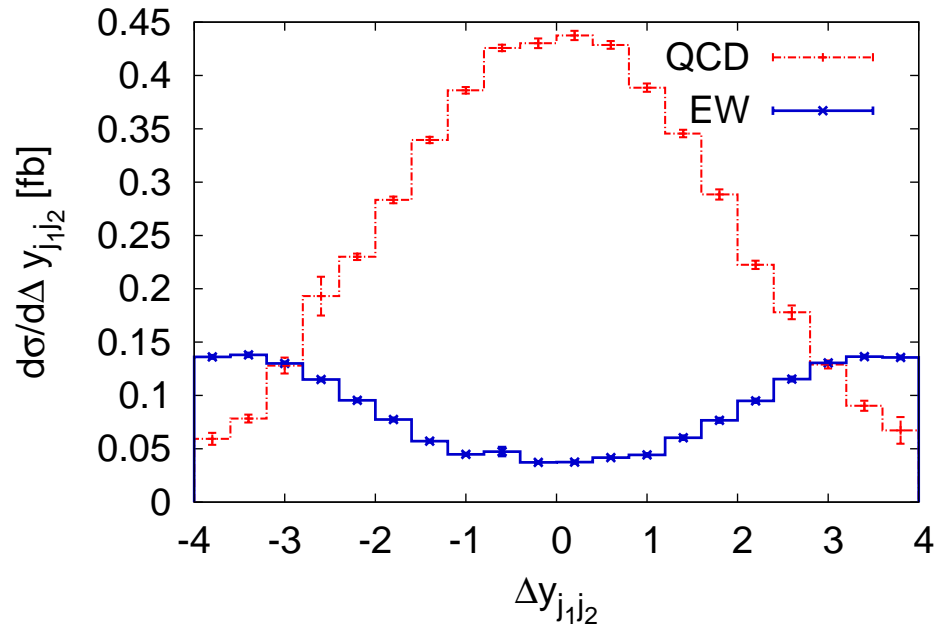


- W^+W^+jj \Rightarrow distinct signature: same-sign leptons + \cancel{E}_T + 2 jets
- W^+W^+jj \Rightarrow test ground for multiple parton interactions
- $VVjj$ \Rightarrow important backgrounds to search for

Higgs and BSM in VBF channel

$pp \rightarrow W^+W^+jj$: QCD versus EW production

Zanderighi, B.J. (2011)



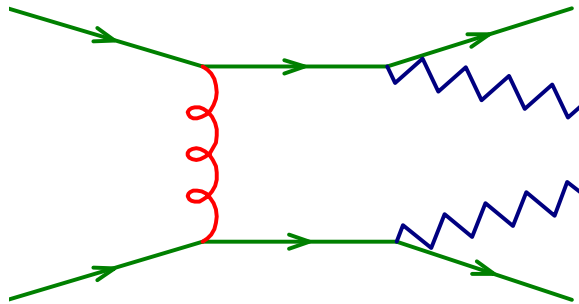
- $\sqrt{s} = 7$ TeV
- basic jet cuts only
- NLO-QCD accuracy

$pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

QCD-induced production

Melia, Melnikov, Rontsch, Zanderighi (2010);

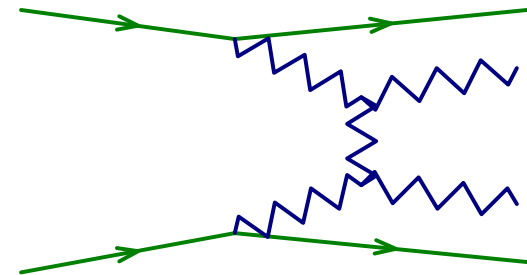
Melia, Nason, Rontsch, Zanderighi (2011)



EW production

Oleari, Zeppenfeld, B.J. (2009);

Zanderighi, B.J. (2011)



NLO results with basic jet cuts only ($p_T^{\text{tag}} > 20$ GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

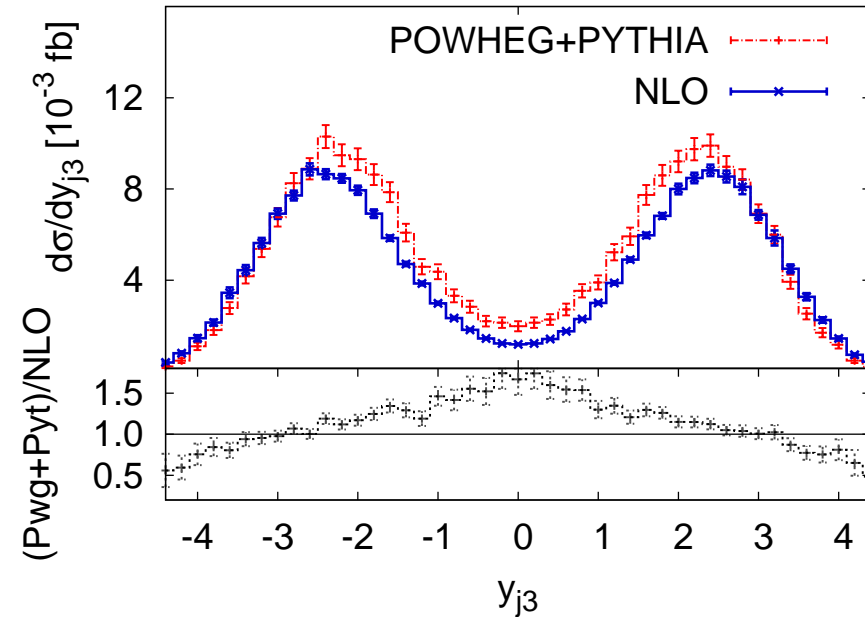
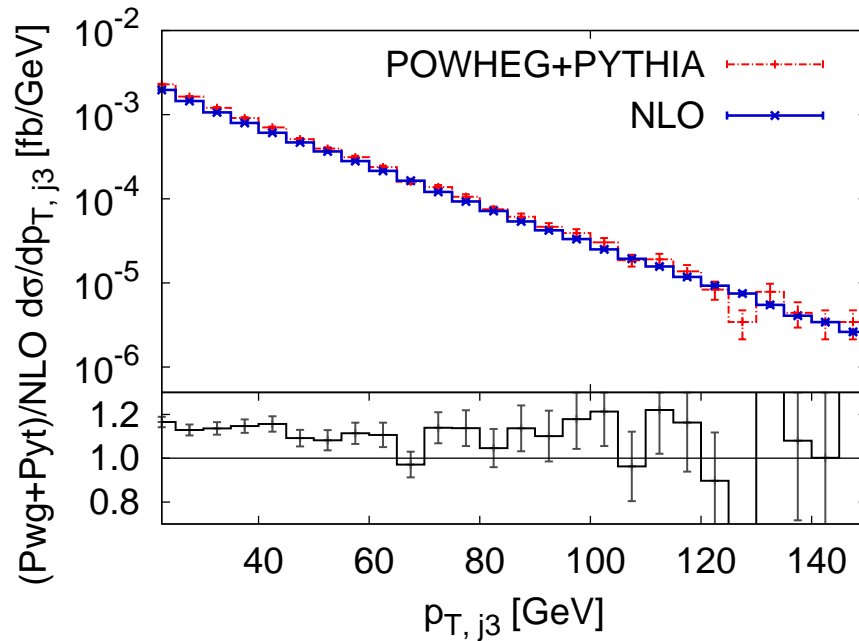
NLO results with VBF cuts:

$$\sigma_{\text{QCD}}^{\text{cuts}} = 0.0074 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{cuts}} = 0.201 \text{ fb}$$

$pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

Zanderighi, B.J. (2011)



good agreement between parton-level NLO calculation and POWHEG matched with PYTHIA for many observables

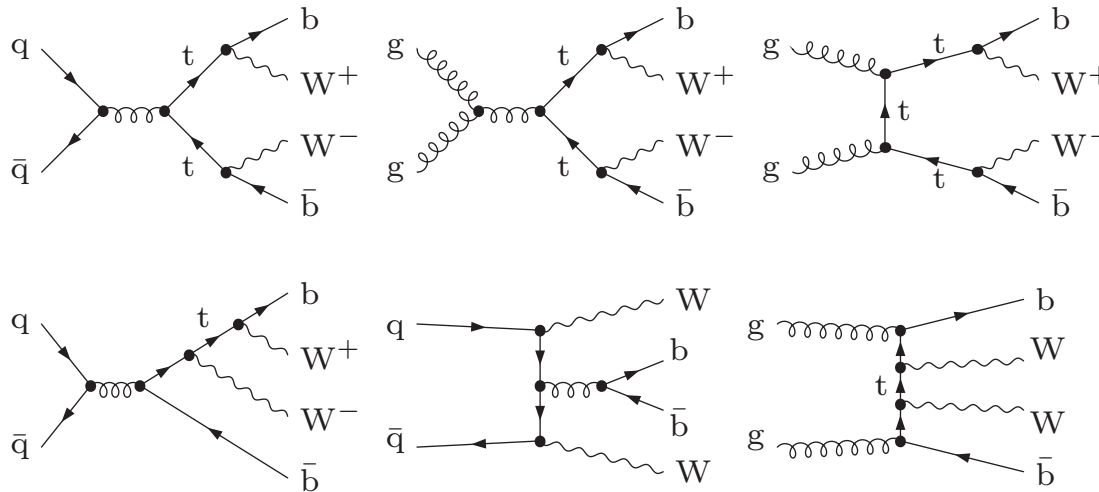
typical for VBF processes: little jet activity at central rapidities

→ exploited by **central-jet veto** techniques

note: parton-shower effects slightly enhance central jet activity

W pairs in association with bottom quarks

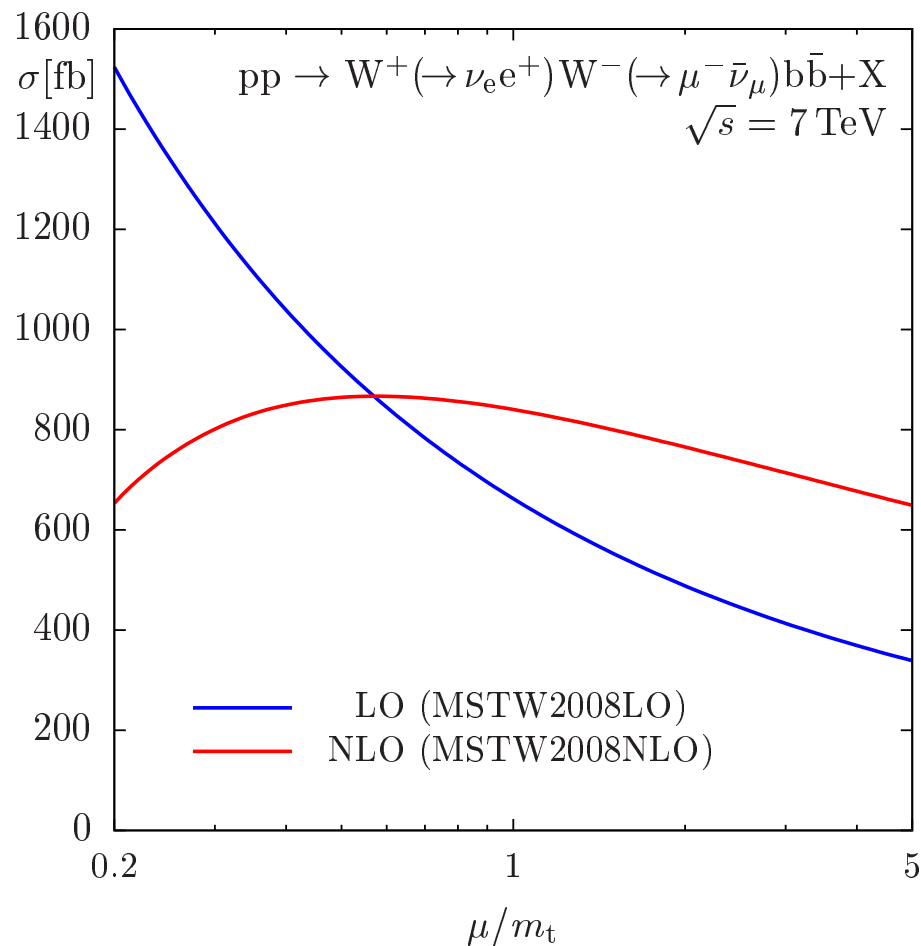
$pp \rightarrow W^+W^-b\bar{b}$... complete description of
 $pp \rightarrow t\bar{t}$ production and subsequent $t \rightarrow Wb$ decay,
 including interferences, off-shell effects, non-resonant
 backgrounds



- *Denner, Dittmaier, Kallweit, Pozzorini (2010)*
- *the HELAC group: Bevilacqua et al. (2010)*

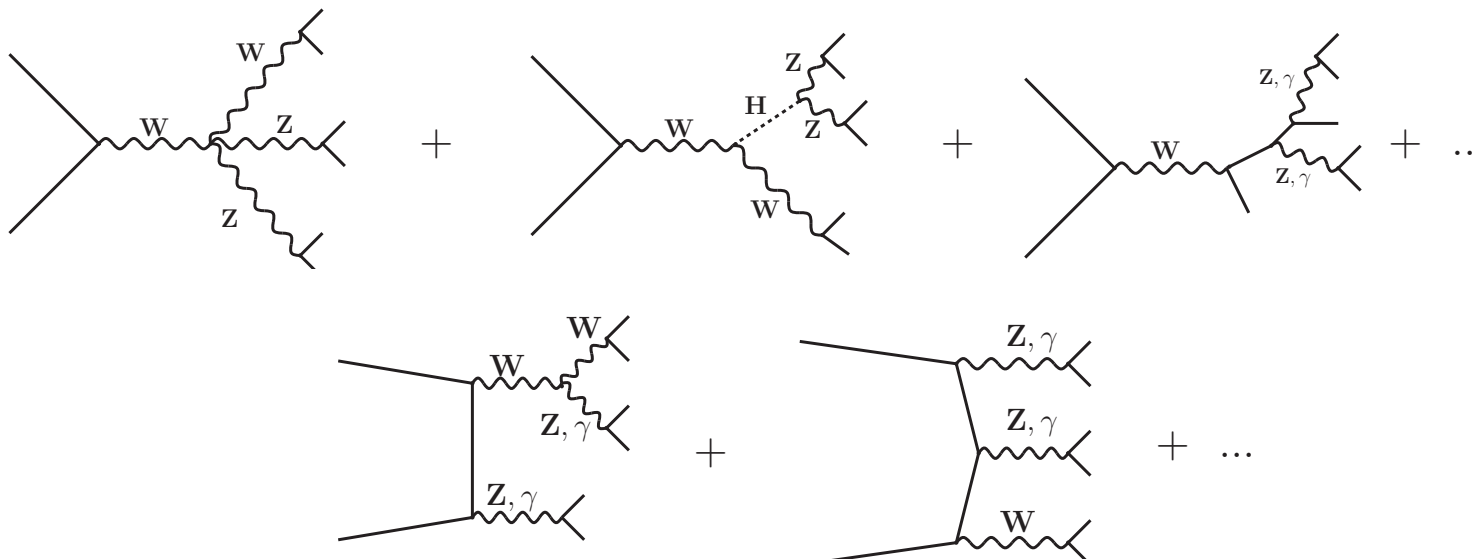
W pairs in association with bottom quarks

Denner et al. (2010)



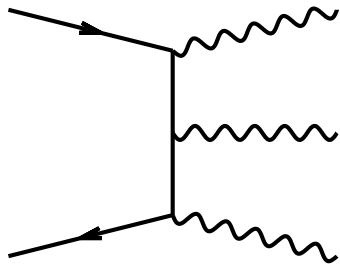
- ❖ off-shell contributions
numerically relevant
(in particular beyond LO)
- ❖ NLO-QCD corrections sizable:
Tevatron: $K^{\text{inc}} \sim 0.94$
LHC(7): $K^{\text{inc}} \sim 1.27$
- ❖ reduction of scale uncertainty
($\sim 40\% \rightarrow 9\%$)

triboson production

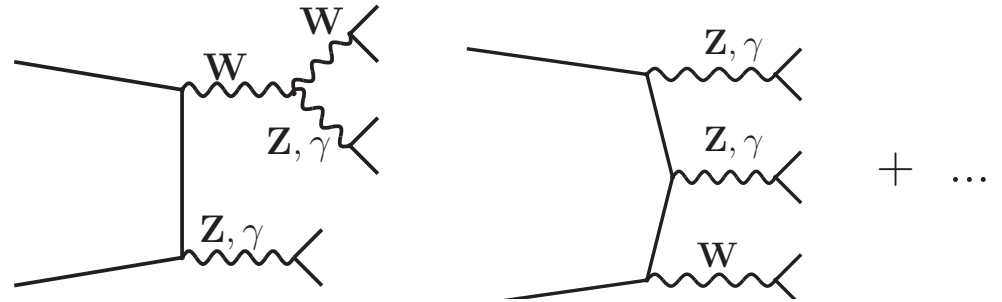


- ❖ SM background for new physics signatures with multi-leptons + \cancel{p}_T
- ❖ sensitive to (anomalous) triple and quartic gauge boson couplings
- ❖ NLO QCD corrections are large and strongly depend on observable and phase space region
(drastically underestimated by LO scale variations)

triboson production @ NLO QCD



on-shell production



including **leptonic decays**
and **off-shell effects**

$$pp \rightarrow ZZZ:$$

Lazopoulos, Melnikov, Petriello (2007)

$$pp \rightarrow WWZ:$$

Hankele, Zeppenfeld (2007)

$$pp \rightarrow VVV:$$

*Binoth, Ossola, Papadopoulos,
Pittau (2008)*

$$pp \rightarrow ZZW, WWW:$$

*Campanario, Hankele, Oleari,
Prestel, Zeppenfeld (2008)*

example: $pp \rightarrow W^+W^-Z$ with decays

LO: very mild scale dependence

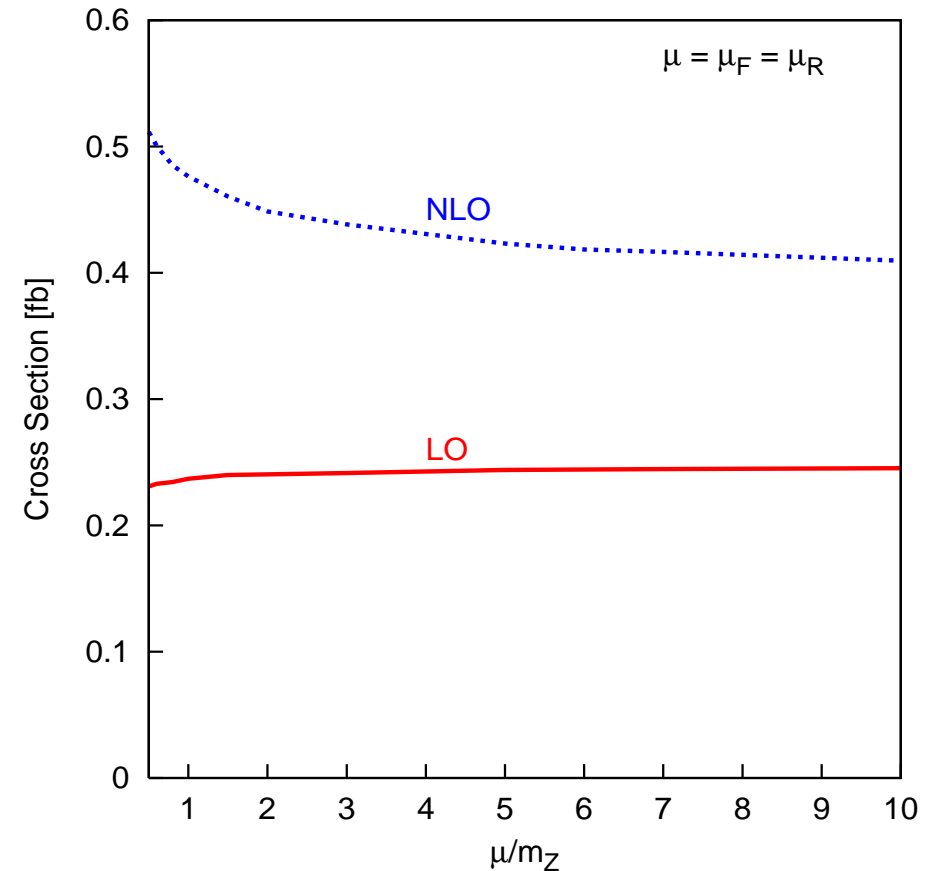
LO is $\mathcal{O}(\alpha_s^0)$,

PDFs probed in regions
with small μ_f dependence

but large QCD corrections with

$$\frac{\sigma^{NLO}}{\sigma^{LO}} \sim 1.7 \div 2.2$$

Hankele, Zeppenfeld (2007)



summary

- ❖ discussed selected processes with multiple massive weak gauge bosons at hadron colliders:

$$VV, VVj, VVjj, VVb\bar{b}, VVV$$

- ❖ provide powerful probes of the **structure of the Standard Model**

e.g. triple and quartic gauge boson couplings

- ❖ serve as important **backgrounds**

... to searches for the Higgs boson

... to searches for new physics

conclusions

impact of **radiative corrections** can be large and dependent on experimental selection criteria



- ❖ to achieve precision required by experiment:
 - consider QCD and EW corrections
 - disregard (on-shell, high-energy, ...) approximations
 - match to parton-shower programs
- ❖ calculations for selected processes advanced, several public **tools available**:
MCFM, vbfno, POWHEG-BOX, ...



disclaimer:

could only touch on the subject

▣➔ apologies for incompleteness