



*3D Rad-hydro simulations to  
solve supernova problem*

*But to understand the  
simulations, we need to  
parameterize neutrino-transport*



*Critical Conditions for Successful  
Neutrino-Driven Explosions*

*A Model for the Gravitational Wave  
Emission*

by

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# Thank you...

Adam Burrows

Randy LeVeque

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Luc Dessart

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Casey Meakin

Princeton U.

Applied Math., UW

Caltech / (NBI, Copenhagen)

OAMP (Marseille, Fr.)

Steward, U.A.

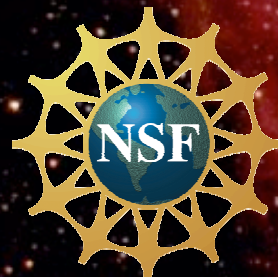
CNRS, Fr.

LANL

LANL

LANL

U. Arizona



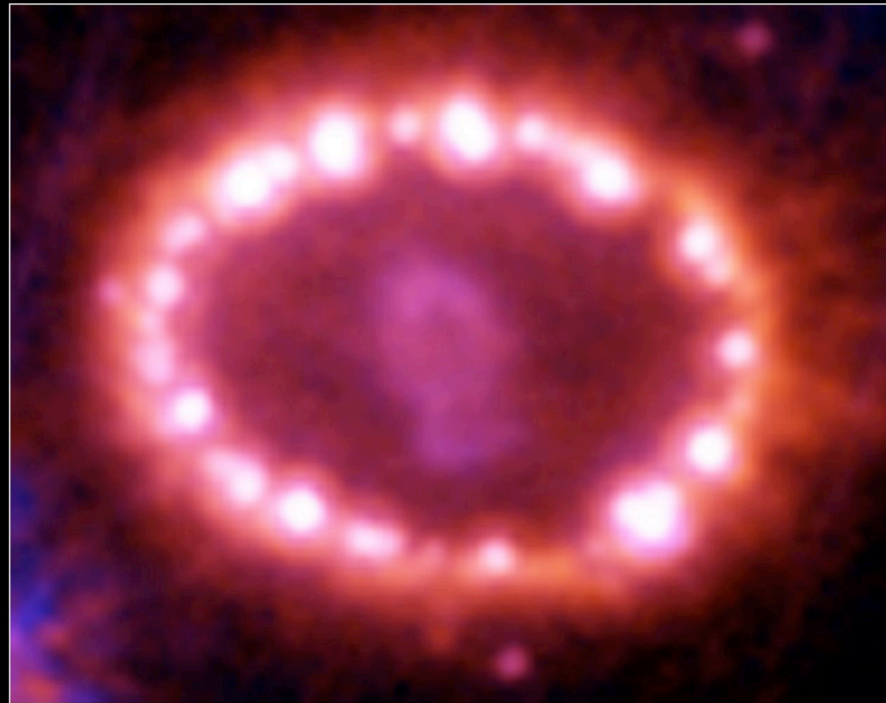
AAPF

*Core*

*A*

*ova:*

*al*



**Supernova 1987A • November 28, 2003**  
**Hubble Space Telescope • ACS**

NASA and R. Kirshner (Harvard-Smithsonian Center for Astrophysics)

STScI-PRC04-09a

# *1D simulations (Rad-hydro)*

Wilson '85

Bethe & Wilson '85

Liebendoerfer et al. '01

Rampp & Janka '02

Buras et al. '03

Thompson et al. '03

Liebendoer et al. '05

Kitaura et al. '06

Burrows et al. '07

} Neutrino mechanism suggested

} **No Explosions**

(Except lowest masses)

*Relax 1D assumption?*



*Neutrino Mechanism:*

- Neutrino-heated convection
- Standing Accretion Shock Instability (SASI)
- Explosions? maybe

*Magnetic Jets:*

- Only for very rapid rotations

*Acoustic Mechanism:*

- Explosions but caveats.



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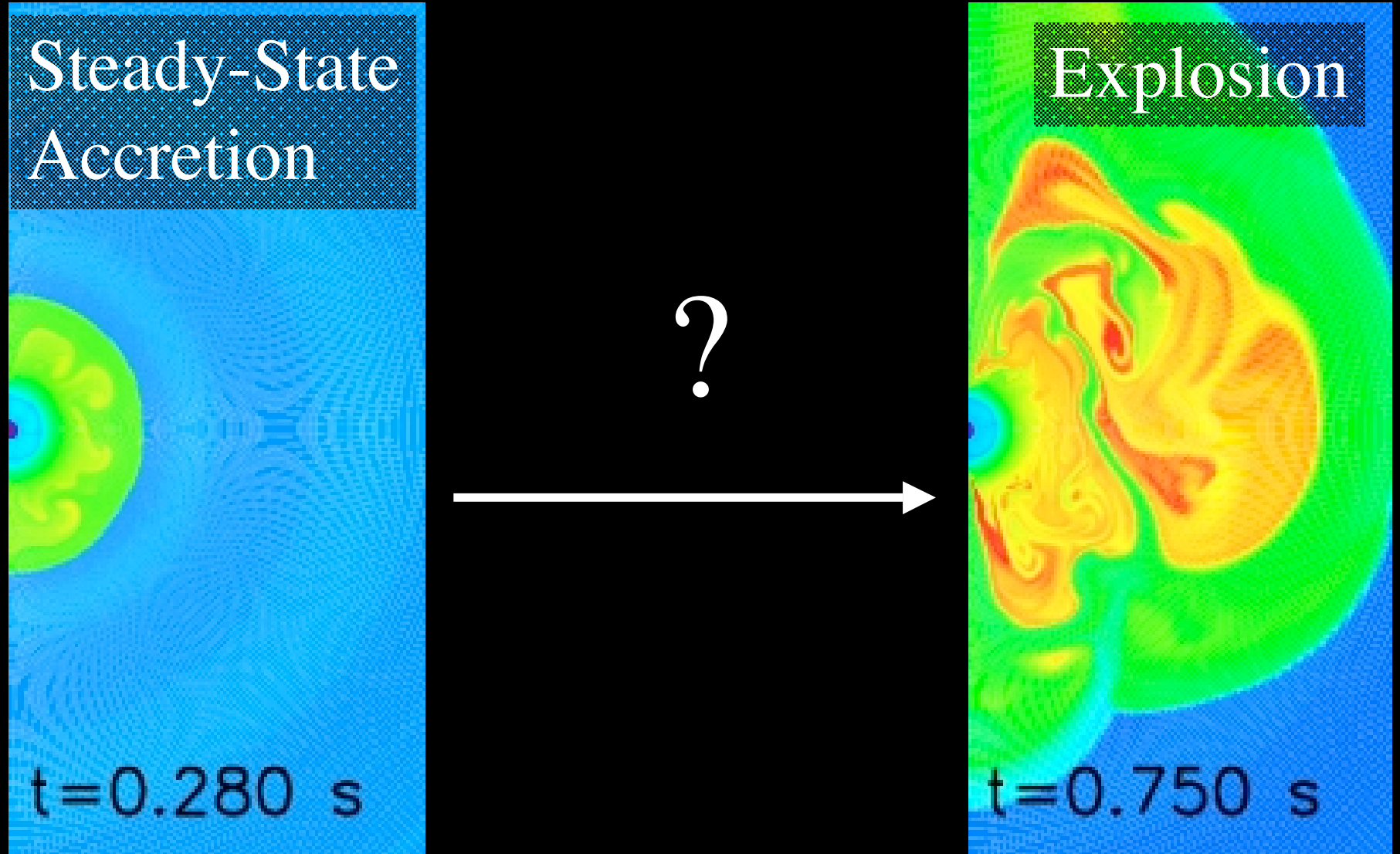


0 ms

Note...

- Stalled shock
- Begins 1D, but...
- Convection
- Standing Accretion Shock Instability (SASI)

# *Fundamental Question of Core-Collapse Theory*



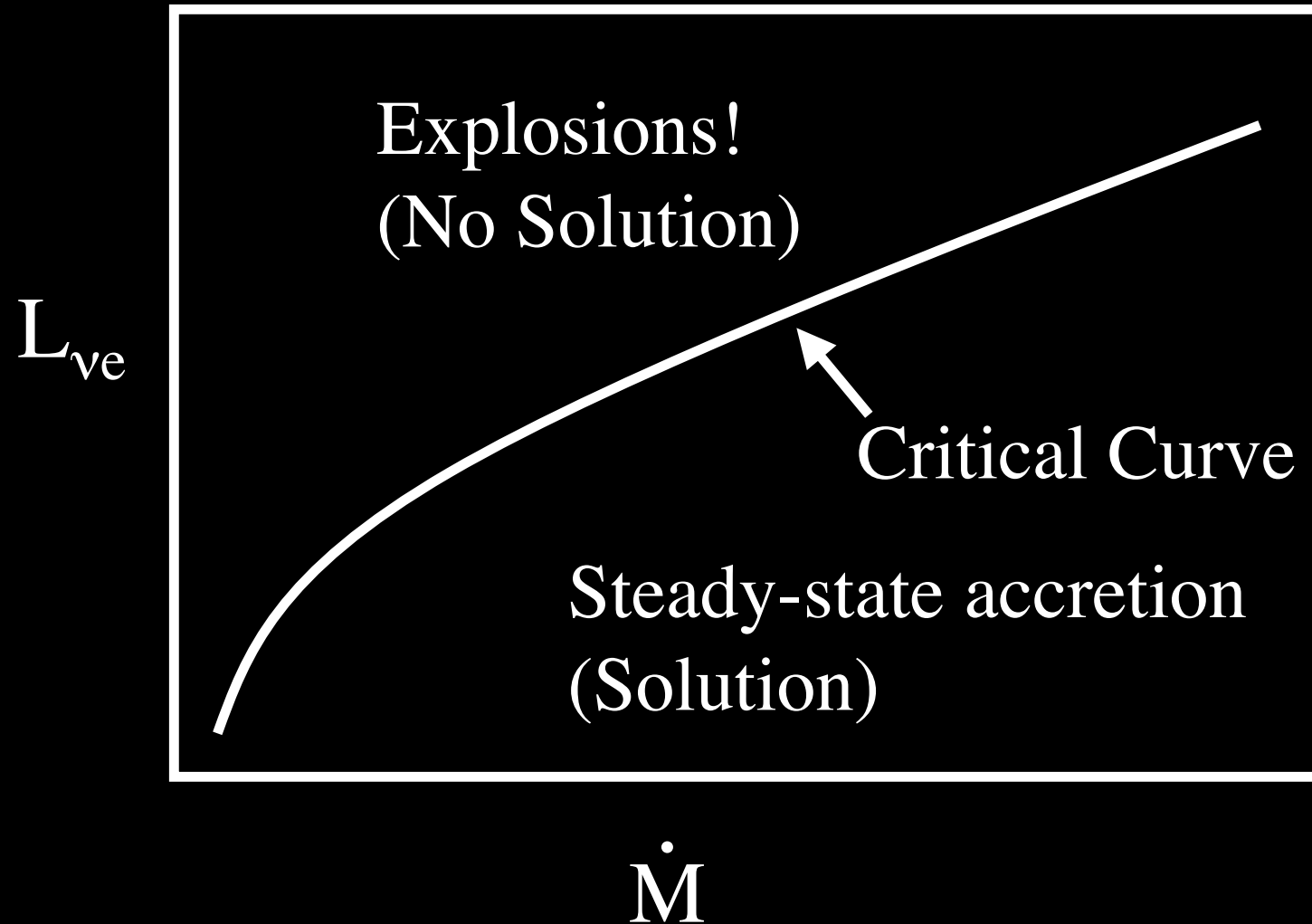
*And why is it easier to explode  
in 2D compared to 1D?*

Murphy & Burrows '08

## *Two Paths to the Solution*

- Detailed 3D radiation-hydrodynamic simulations (“Accurate” energies, NS masses, nucleo., etc.)
- Parameterizations that capture essential physics (Tease out fundamental mechanisms)

Burrows & Goshy '93  
Steady-state solution (ODE)



# Conditions for Explosions by the Neutrino Mechanism

Murphy & Burrows, 2008

## Parameter Study

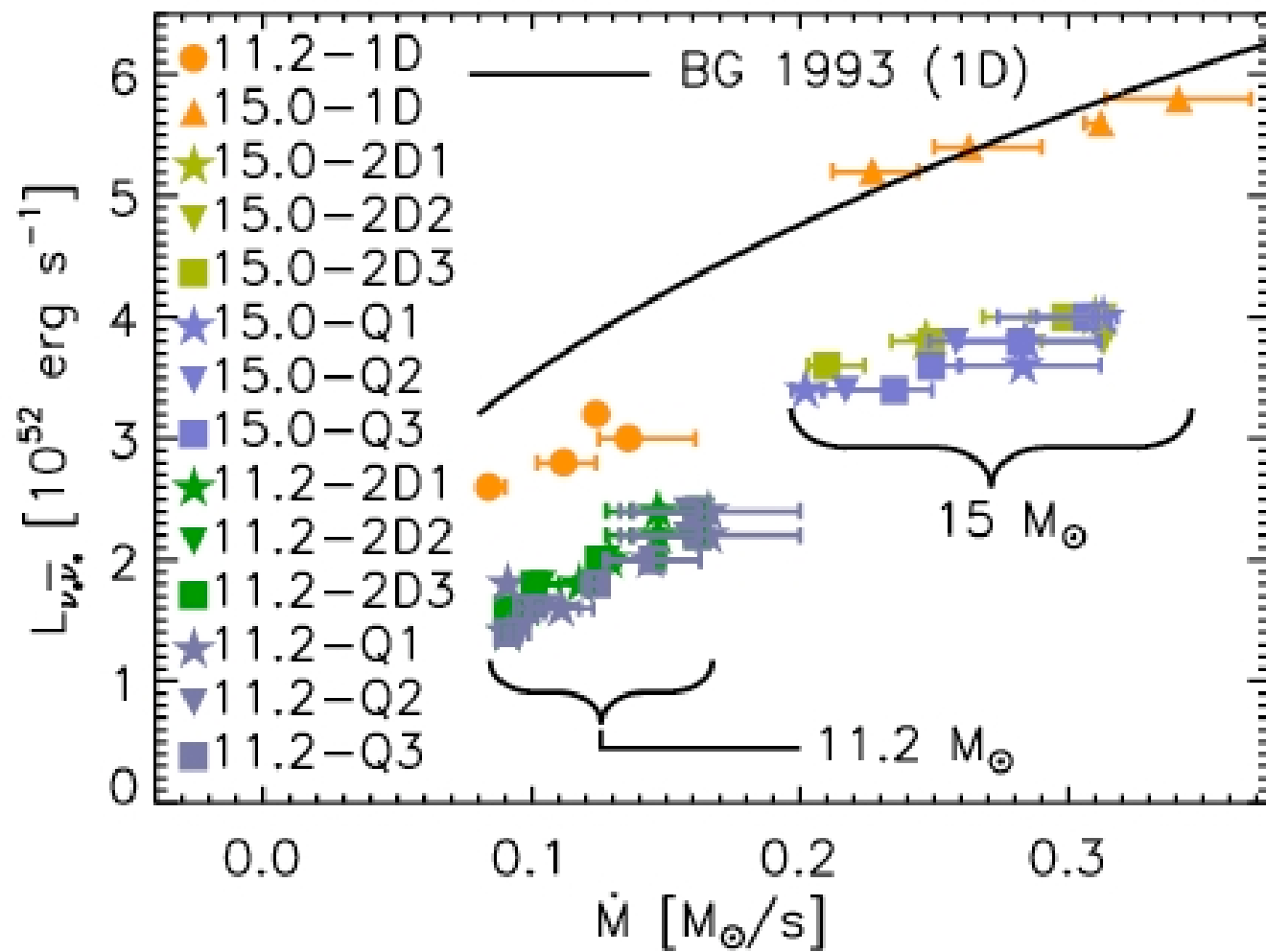
- Neutrino Luminosity (Local heating and cooling)
- 1D, 2D (90° and 180°)
- 11.2 and 15  $M_{\odot}$  (range of accretion rates)
- Resolution
- ~100 simulations

# Is a critical luminosity relevant in hydrodynamic simulations?

- 1D
- 2D Convection and SASI?

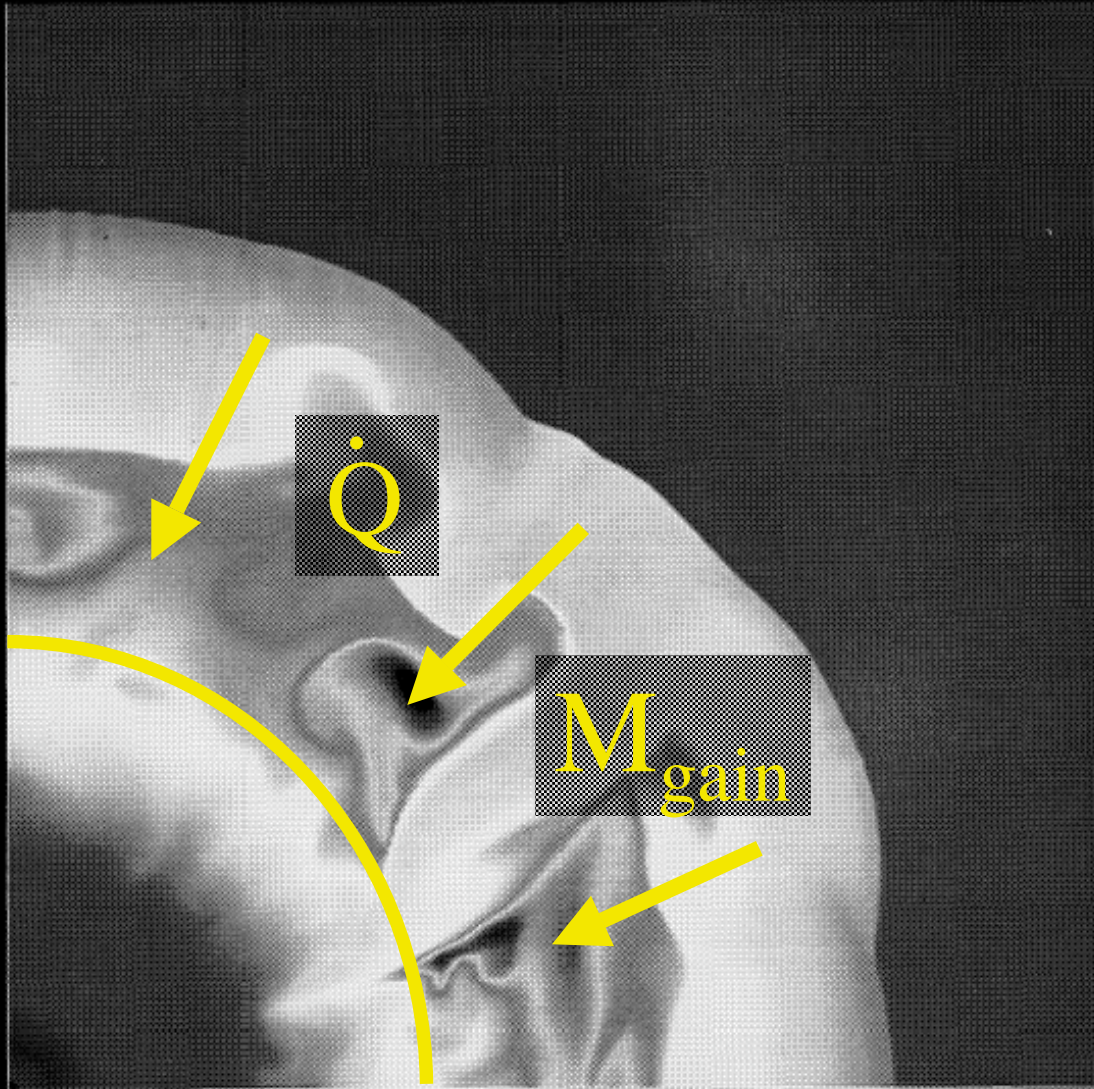
How do the critical luminosities  
differ between 1D and 2D?





Why is critical luminosity of 2D  
simulations  $\sim 70\%$  of 1D?

# *Conditions during Explosion*



$$\tau_{adv} = \frac{\Delta r_{gain}}{v_r}$$

$$\tau_q = \frac{E}{\dot{Q}}$$

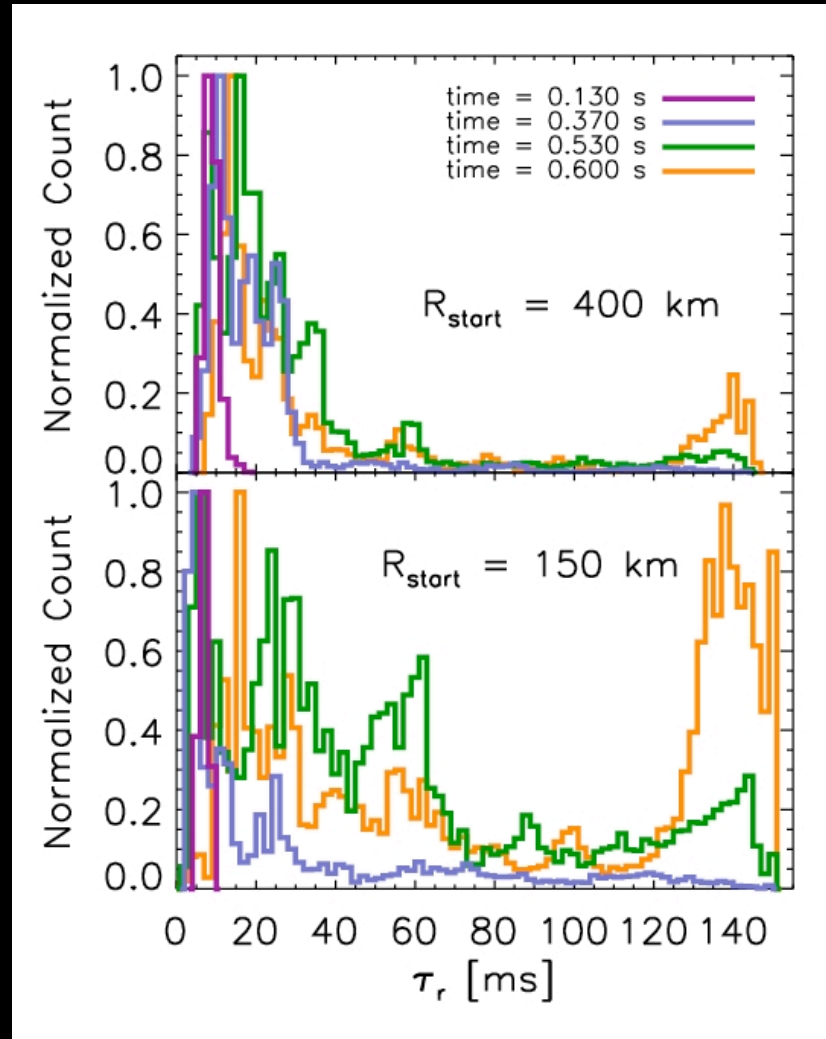
$$\frac{\tau_{adv}}{\tau_q} \gg 1$$

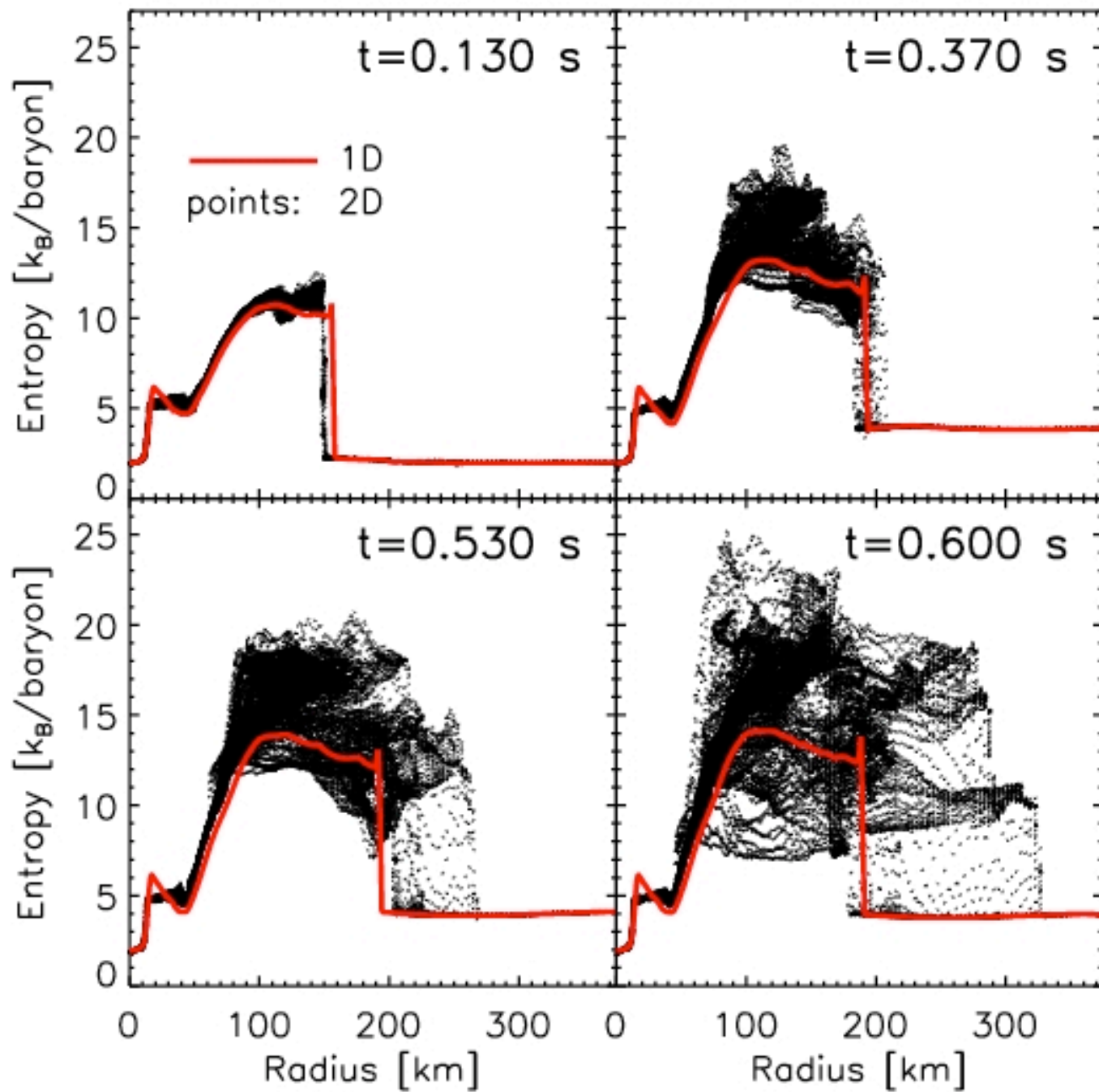
1D  $\rightarrow$  one time

2D  $\rightarrow$  distribution of times

More heating?

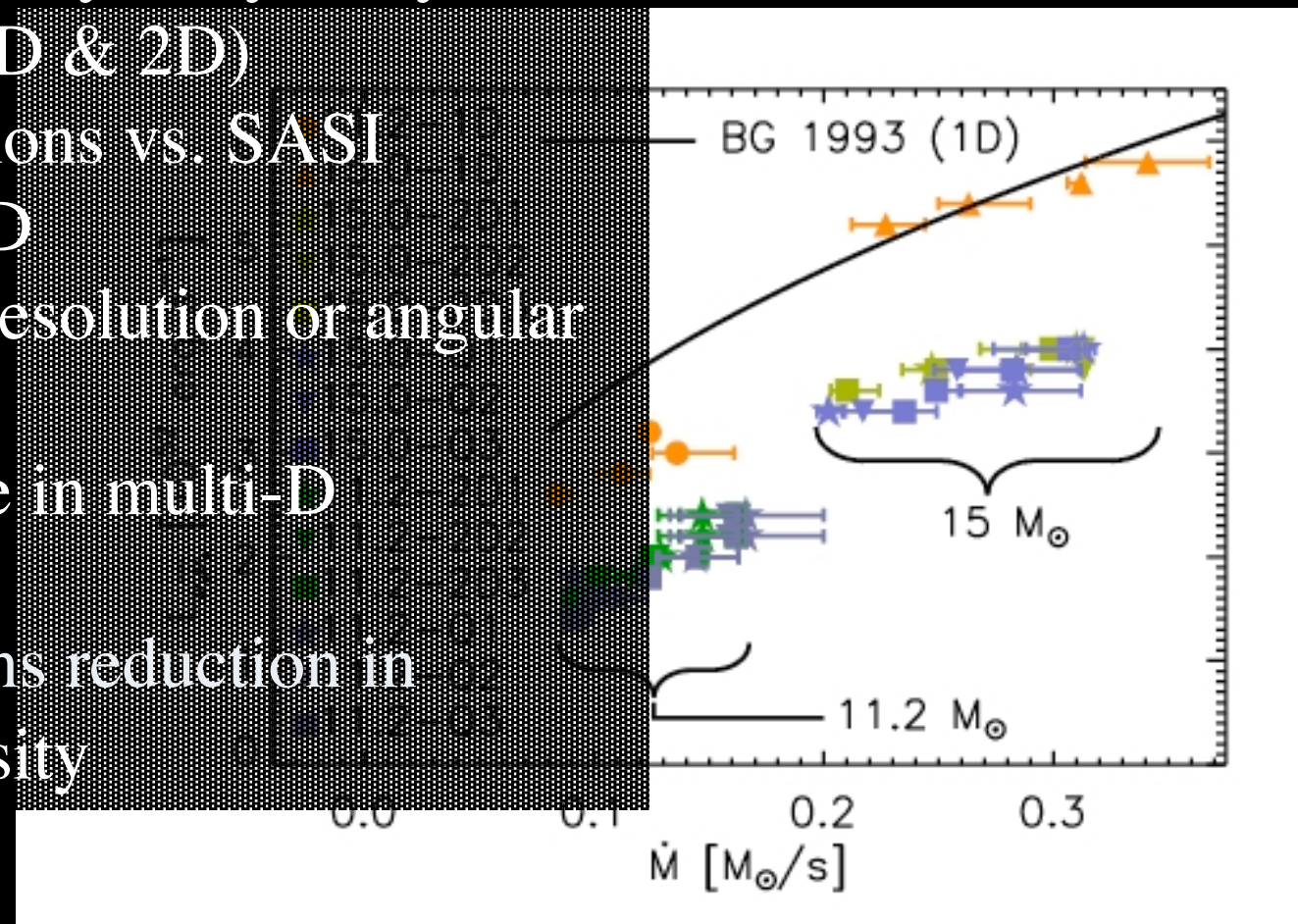
$$\Delta S \propto \frac{\dot{Q}}{T}$$





# Conclusions

- Critical luminosity in hydrodynamic simulations (1D & 2D)
- Radial oscillations vs. SASI
- 2D  $\sim 70\%$  of 1D
- Insensitive to resolution or angular domain
- Residence time in multi-D simulations
- Long  $\tau_r$  explains reduction in critical luminosity





*A Model for Gravitational Wave  
Emission from Neutrino-Driven  
Explosions*

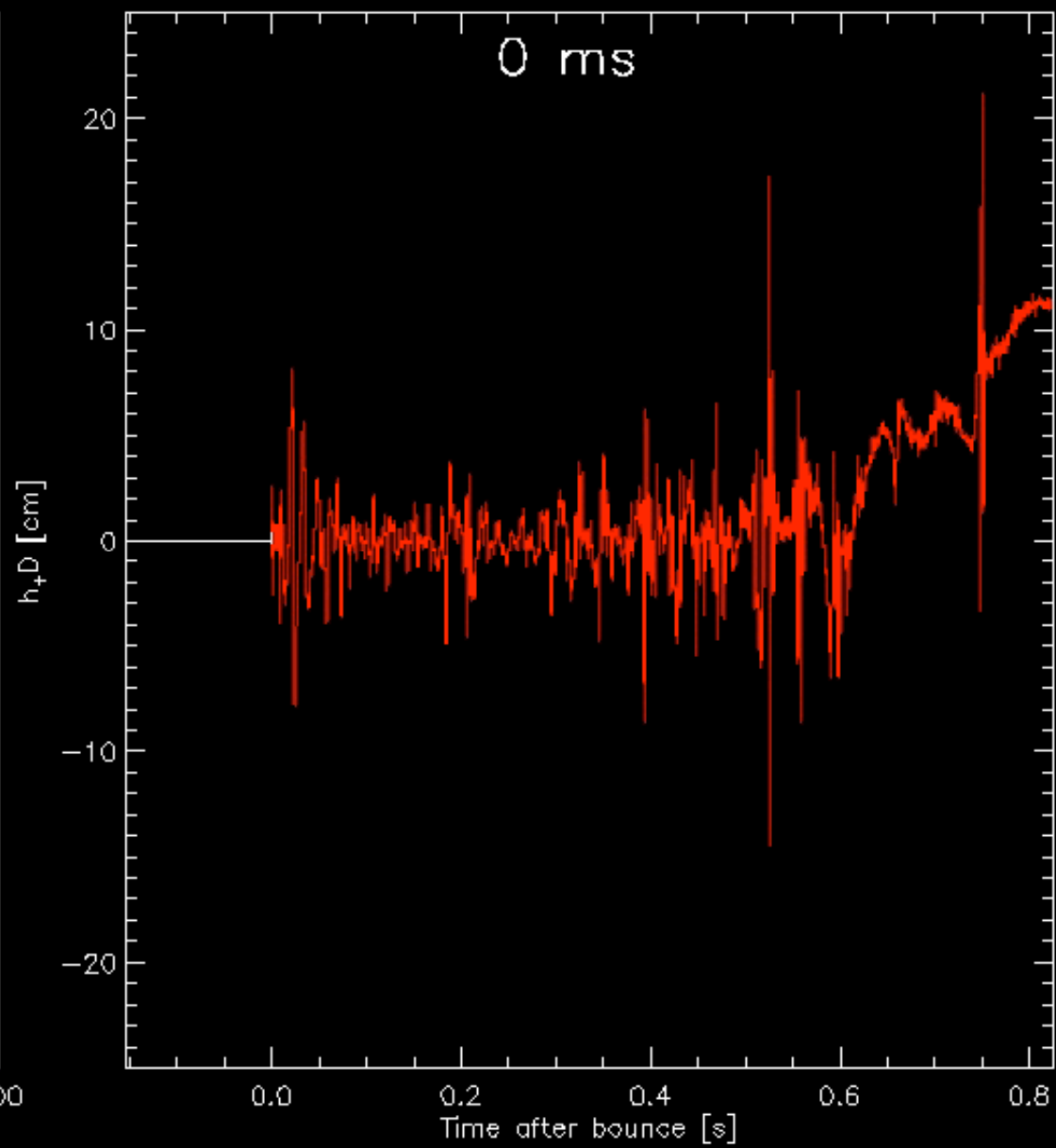
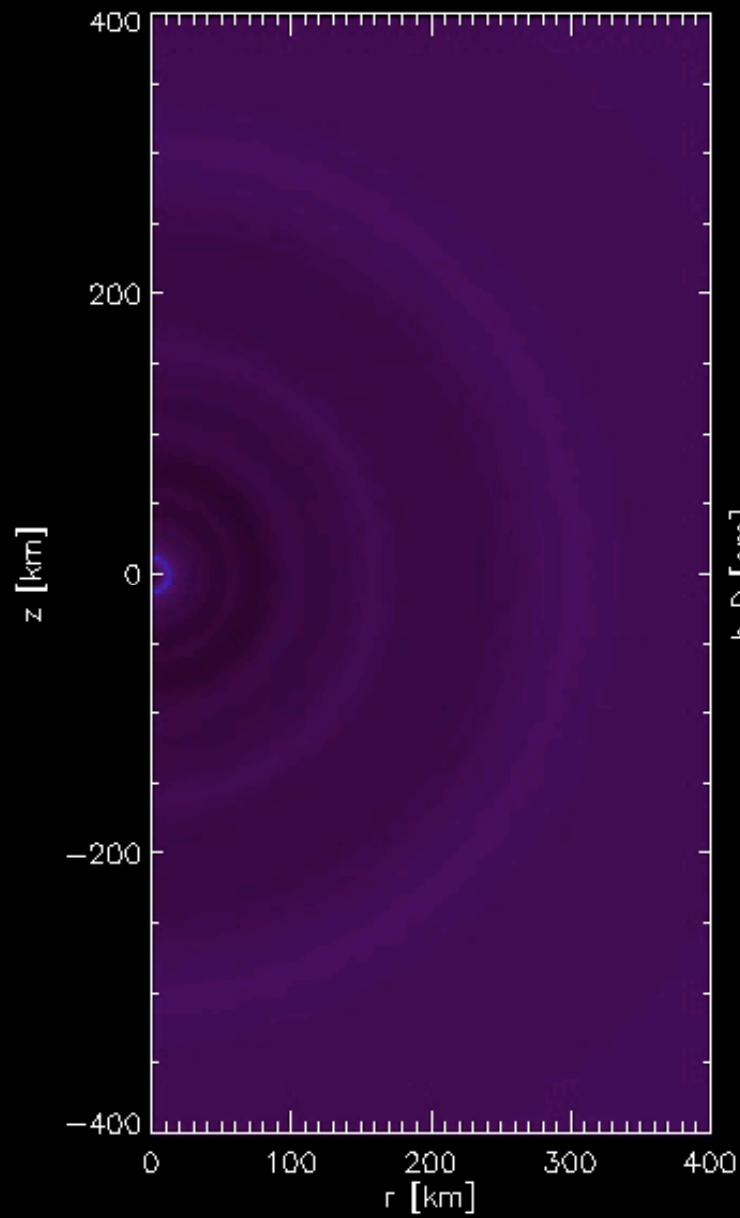
Murphy, Ott, & Burrows '09

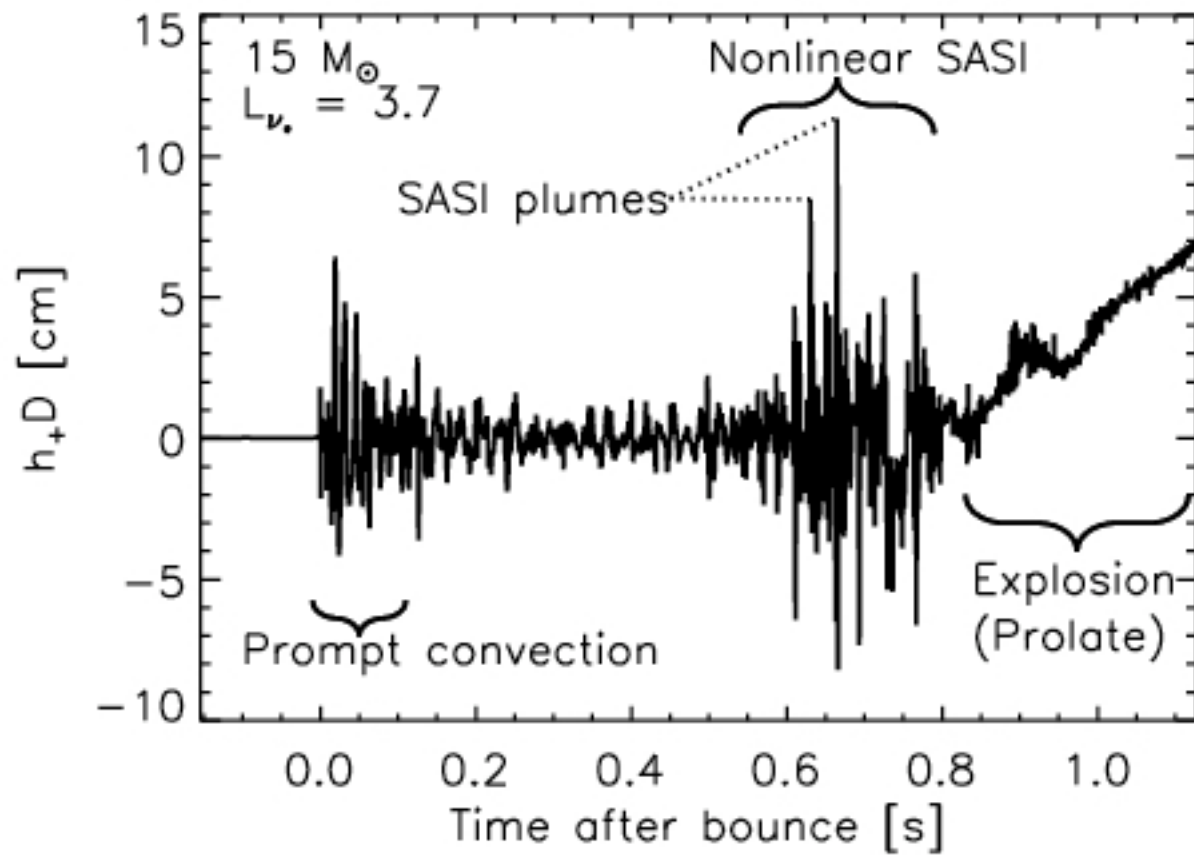
Murphy, Ott, & Burrows, 2009

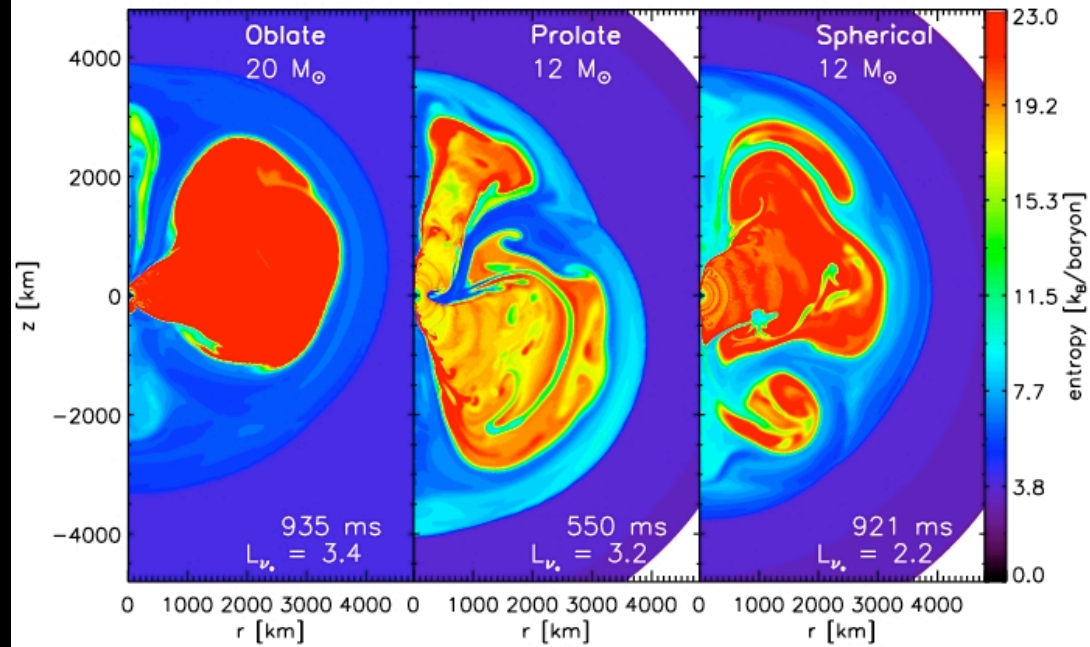
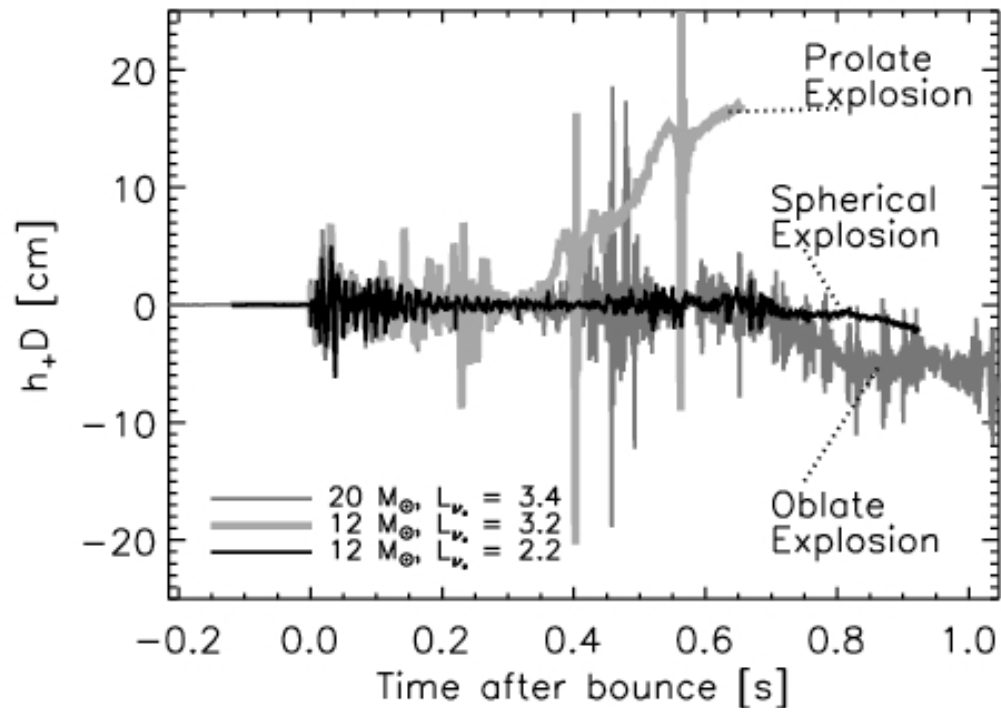
**Another Parameter Study**

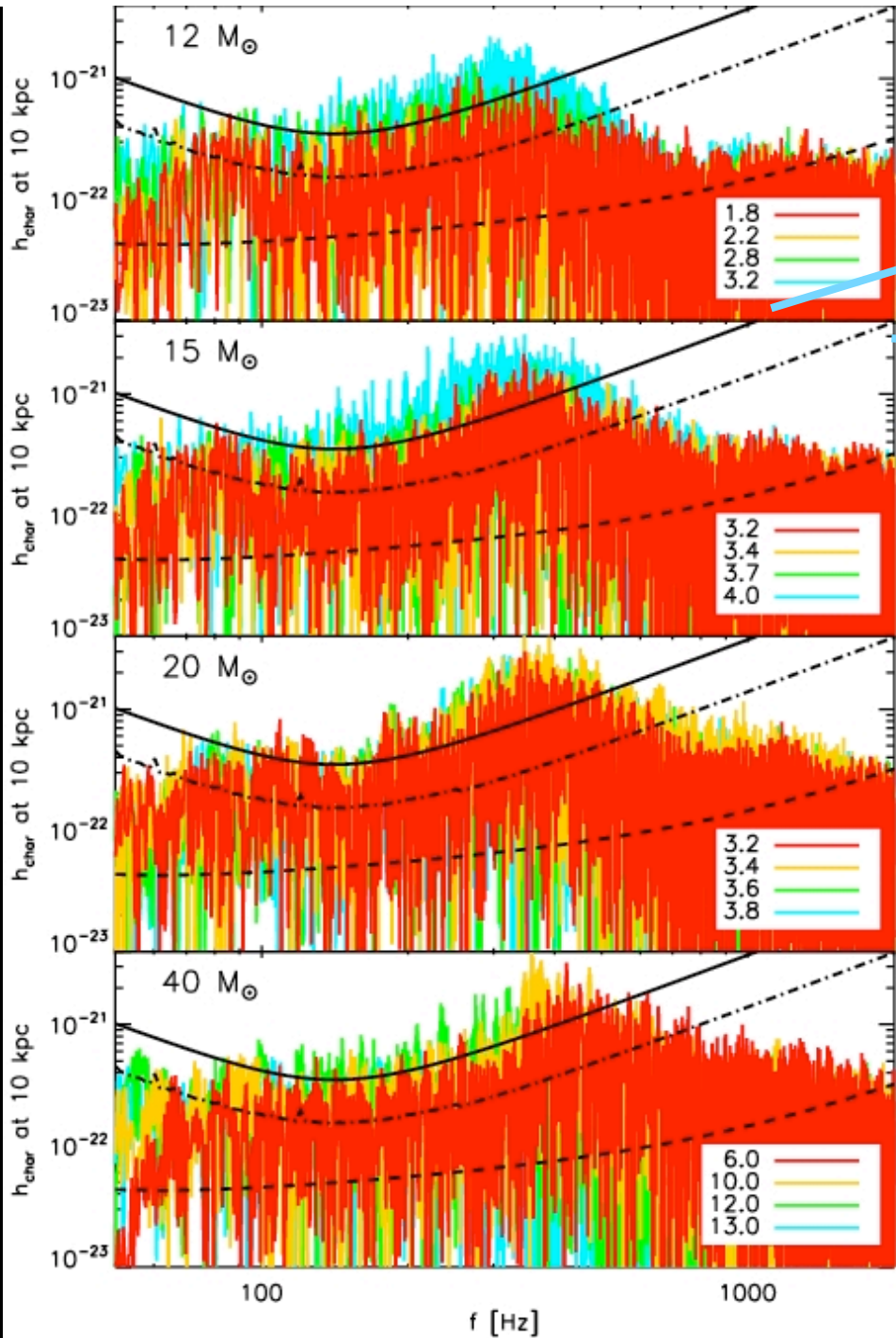
- Neutrino Luminosity (Local heating and cooling)
- 2D
- 12, 15, 20, and 40  $M_{\odot}$  (Woosley & Heger '07)







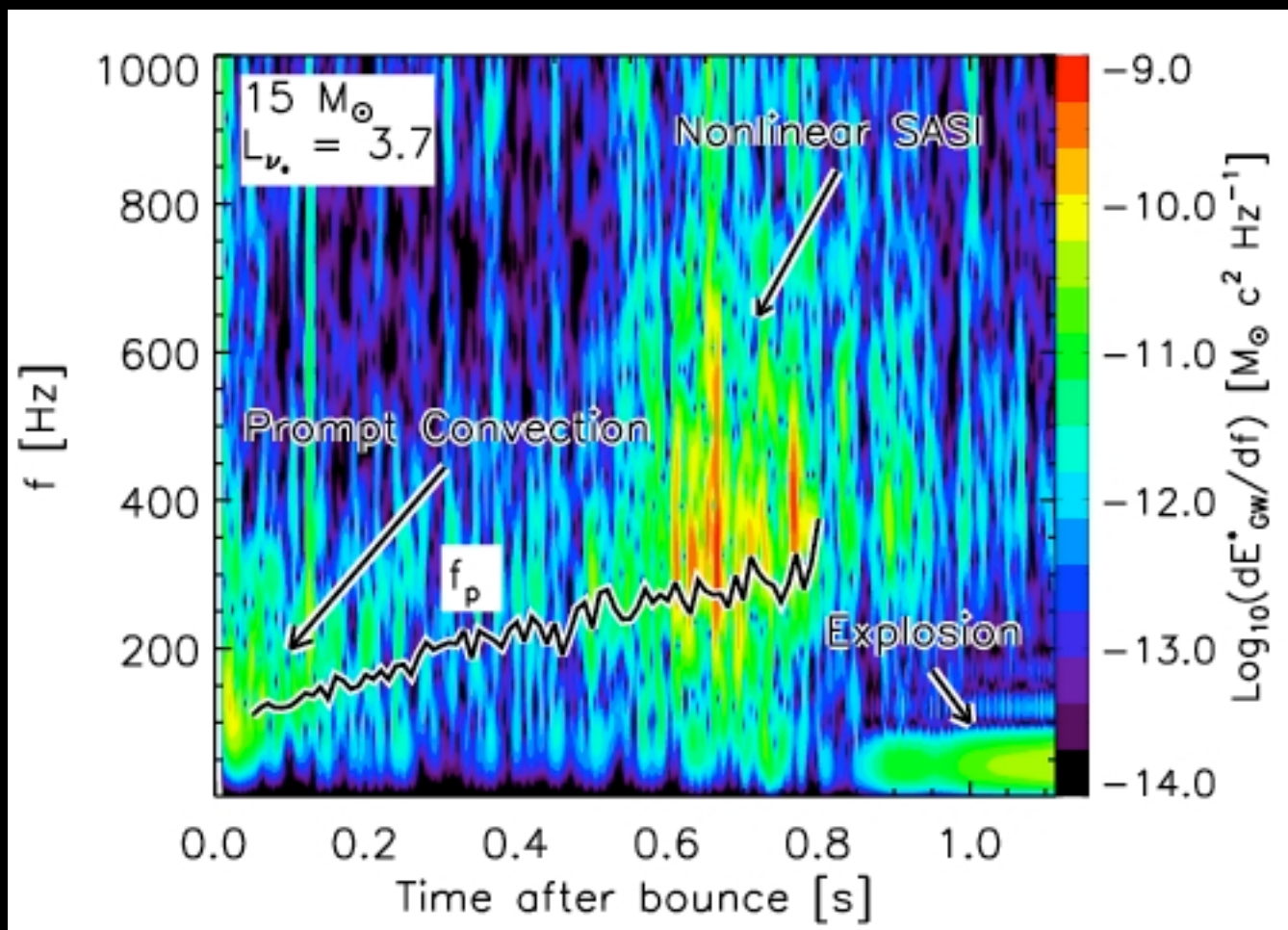




Initial LIGO

Enhanced LIGO

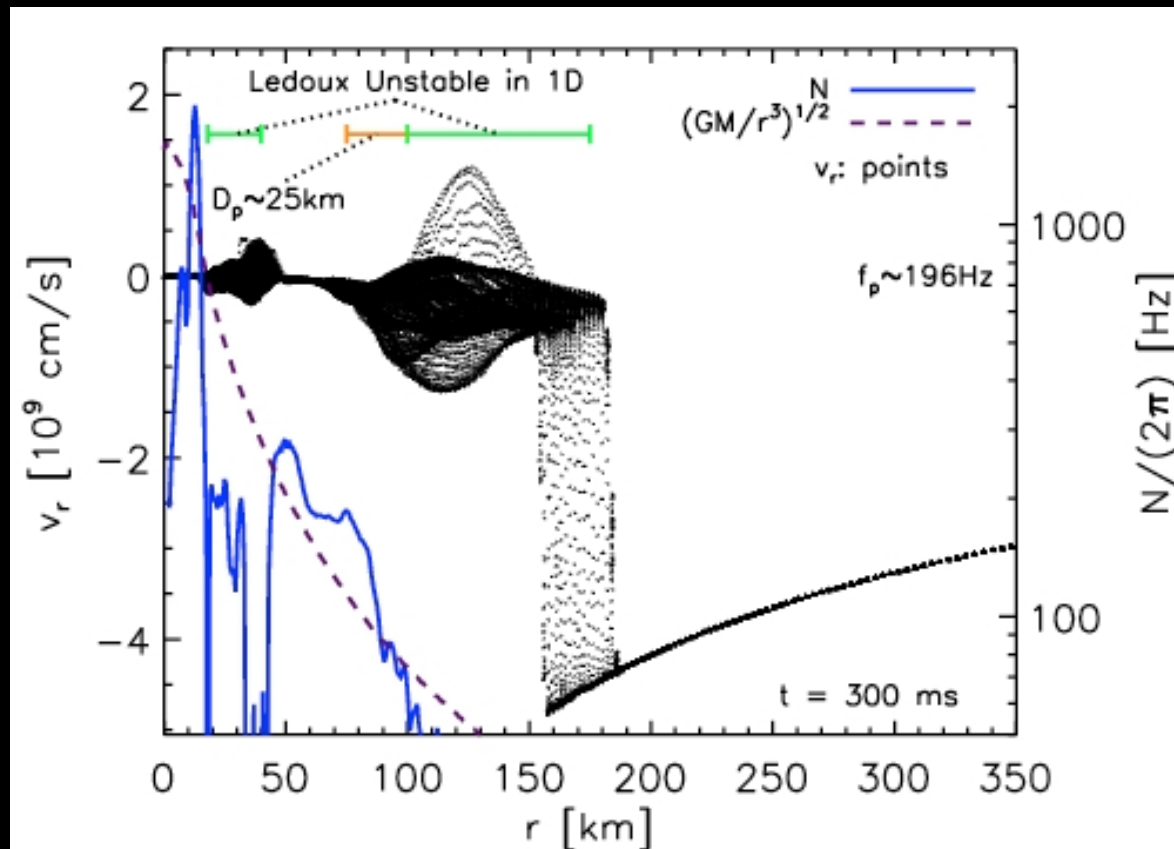
Advanced LIGO



*Characteristic GW frequencies  
and amplitudes?*

# The Model: Buoyant Impulse

$$b(r) = \int N^2 dr$$



$$R_b = \frac{\Delta b D_p}{v_p^2}$$

$$D_p \sim v_p / N$$

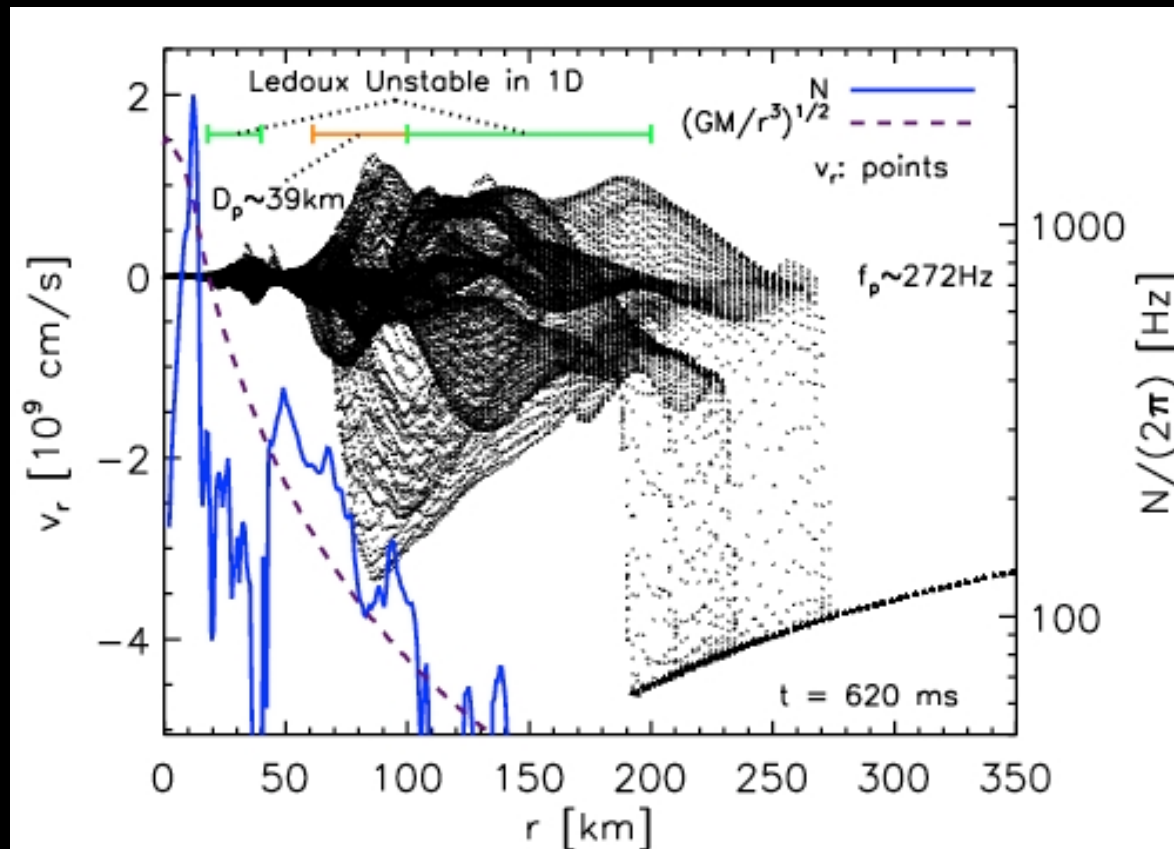
$$f_p \sim N/(2\pi)$$

$$h_+ \propto f_p v_p$$

Similar analysis for 3D convection in stellar interiors  
(Meakin & Arnett 2007, Arnett & Meakin 2009)

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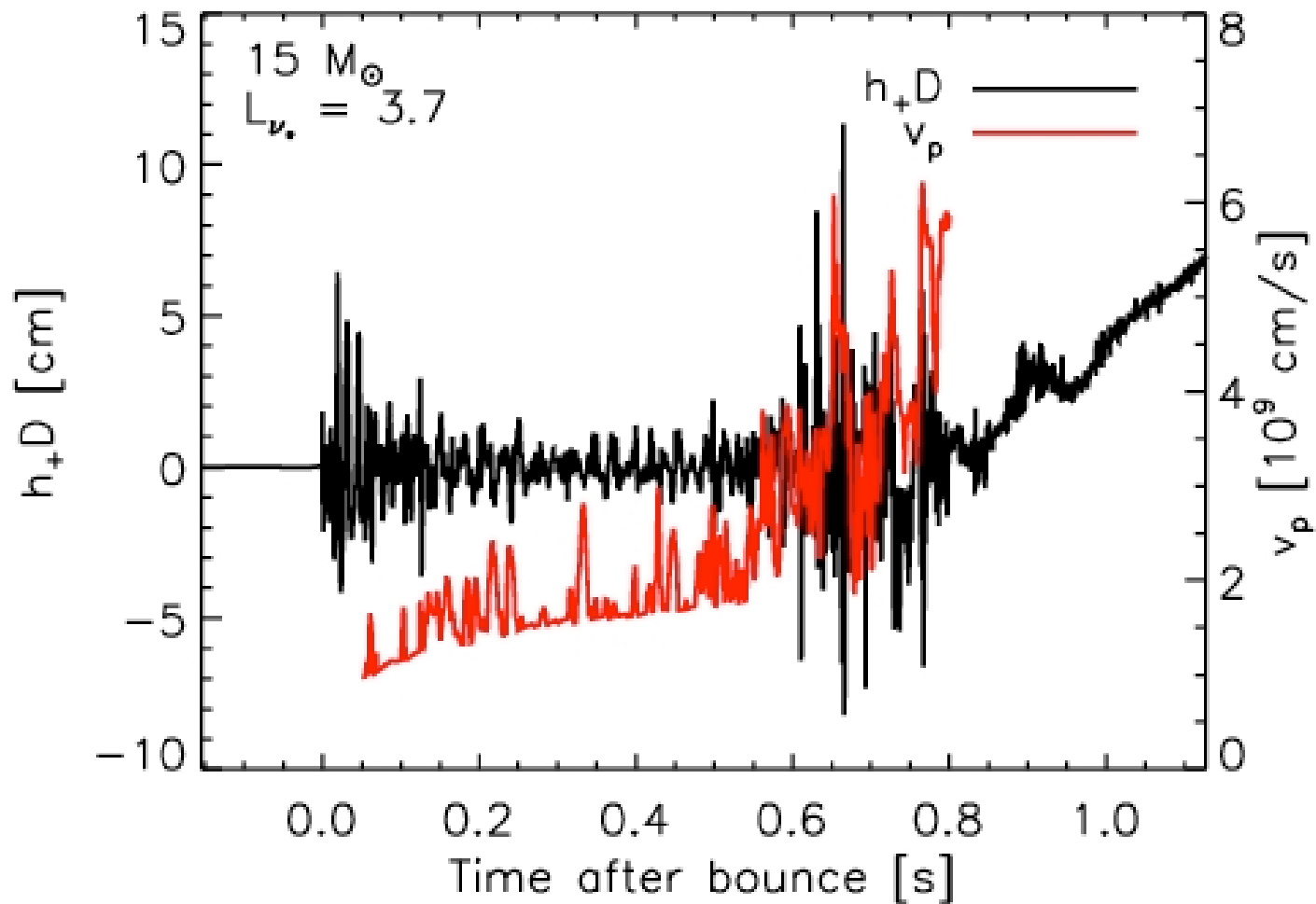
$$f_p \sim N / (2\pi)$$

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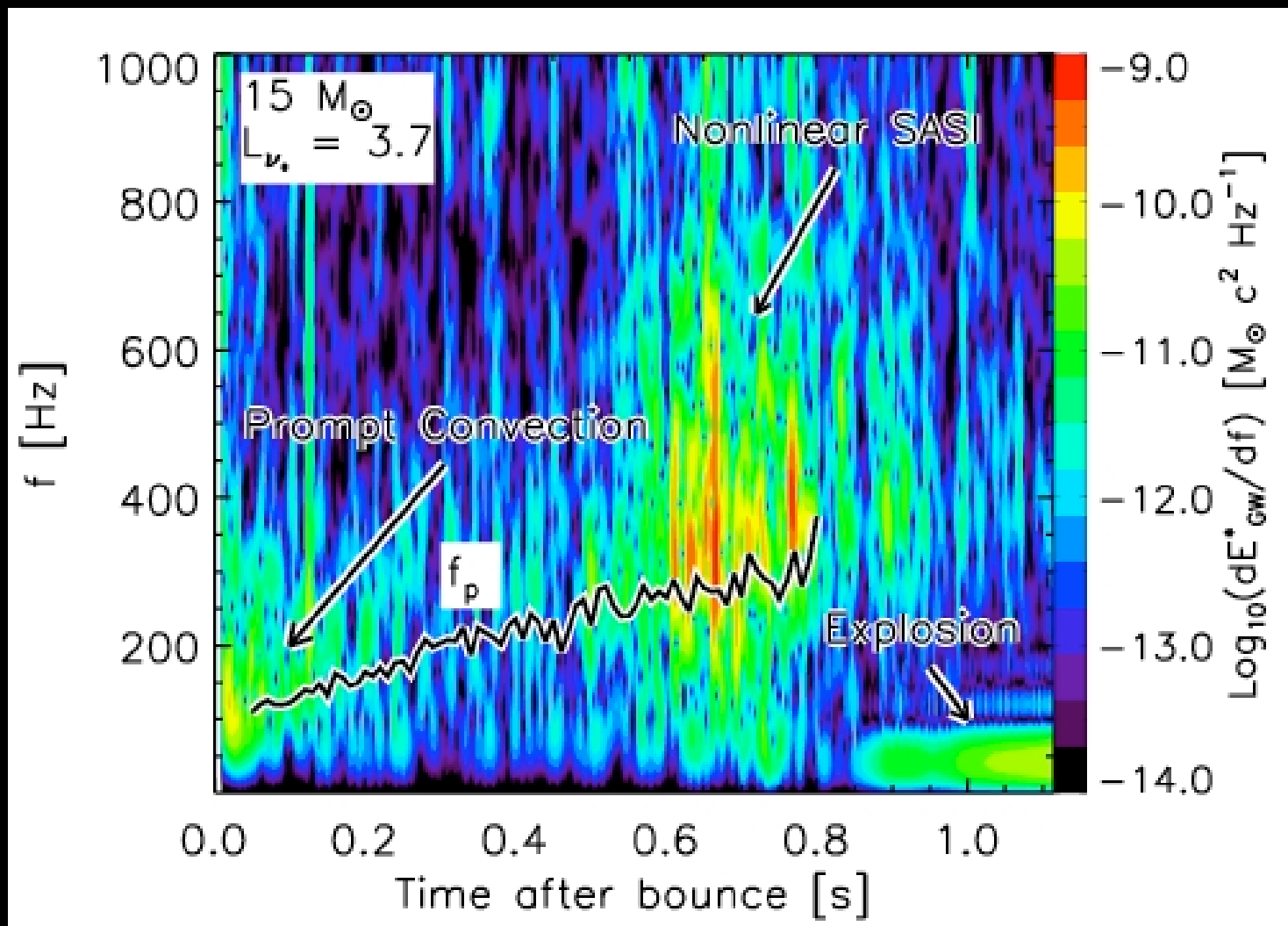
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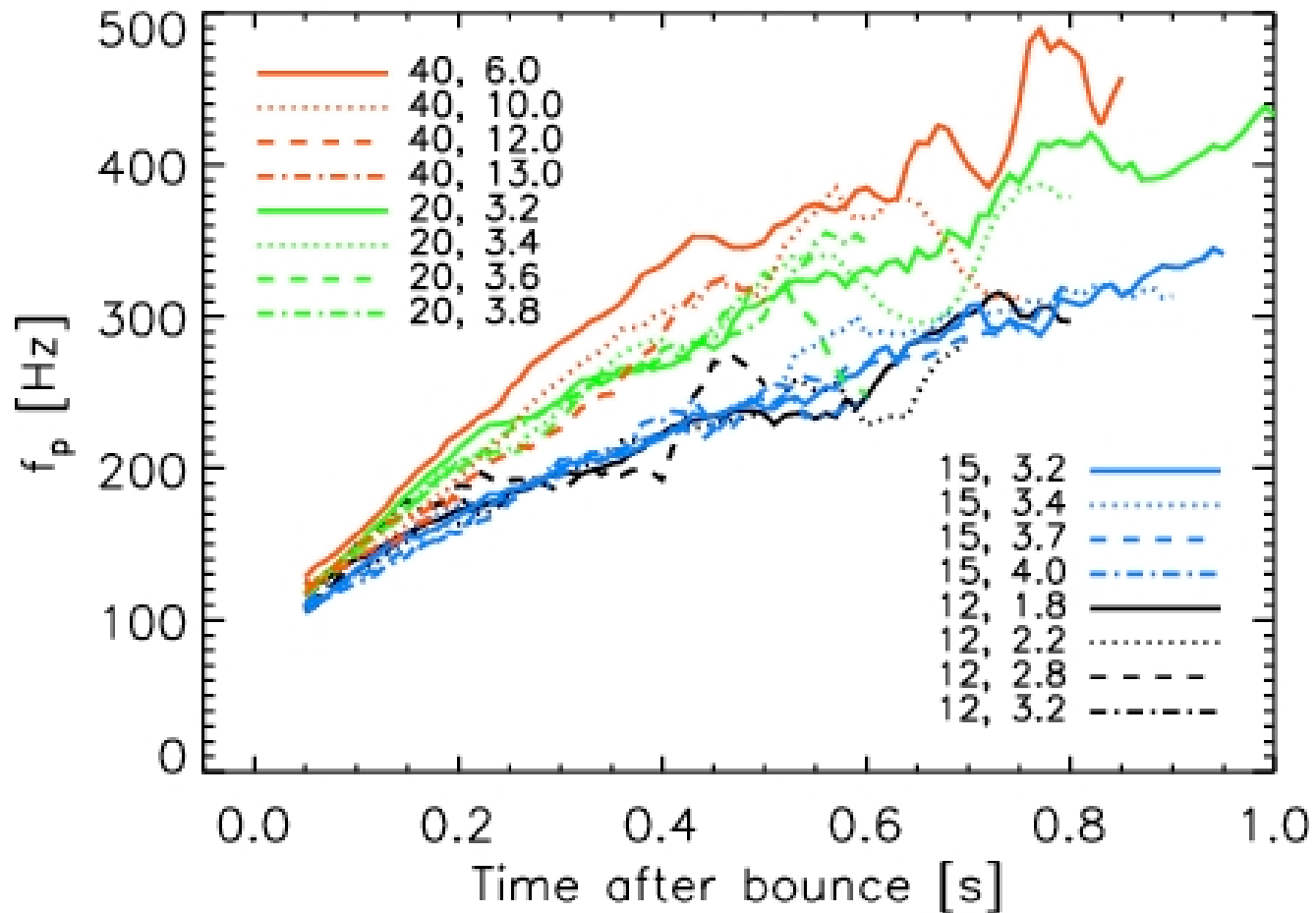
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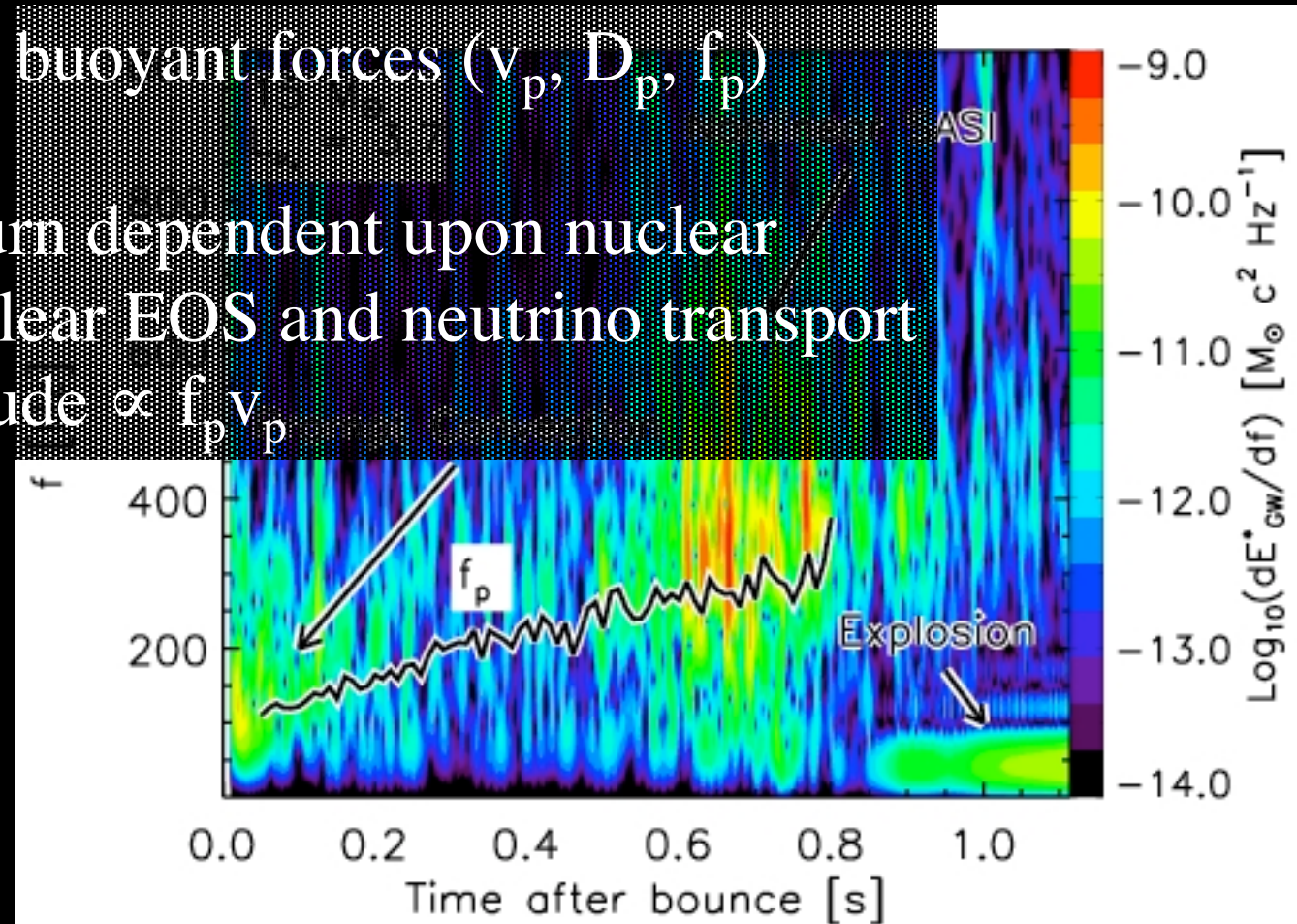


# Progenitor Mass and $\nu$ Luminosity Dependence



# Conclusions

- GW emission of asymmetric explosions
- A model for GW emission
  - Plumes and buoyant forces ( $v_p, D_p, f_p$ )
  - $f_p \propto N_{\text{turn}}$
  - $N_{\text{turn}}$  is in turn dependent upon nuclear and subnuclear EOS and neutrino transport
  - GW amplitude  $\propto f_p v_p$



# *Future Directions*

## The Condition for successful explosions

- Better approximate neutrino physics
- $L_{\text{crit}}$ ,  $\dot{M}$ , and  $M$  relation!?
  - Where does it come from?
  - relate to  $\tau_{\text{adv}}$  and  $\tau_{\text{q}}$  condition?
- Distribution of residence times?
  - long and short
  - inherent asymmetry
  - Convection & SASI in context of Accretion?
- Analytic and numerical techniques
- 3D?

*Why is it easier to explode in 2D  
compared to 1D?*

*Why is it easier to explode in 2D  
compared to 1D?*

*Because it's 2D*

*3D?*



# *3D Simulations*

Convection, SASI, & Accretion (in 3D)?

Distribution of residence times?

Lower critical luminosities?

Randy LeVeque et al.

**CLAWPACK**

