

Microphysics: Electron capture rates and neutrino-nucleus cross sections

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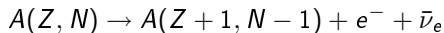


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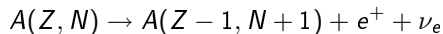
Nuclear beta decay, energetics

Q-value defined as the total kinetic energy released in the reaction

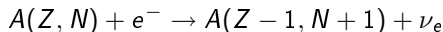
- β^- decay, $Q_{\beta^-} = M_i - M_f + E_i - E_f$



- β^+ decay, $Q_{\beta^+} = M_i - M_f + E_i - E_f - 2m_e$



- Electron capture, $Q_{\text{EC}} = M_i - M_f + E_i - E_f$



Transition rates for β decay

Fermi's golden rule:

$$\lambda = \frac{2\pi}{\hbar} \int |\mathcal{M}_{if}|^2 (2\pi\hbar)^3 \delta^{(4)}(p_f + p_e + p_\nu - p_i) \frac{d^3 p_f}{(2\pi\hbar)^3} \frac{d^3 p_e}{(2\pi\hbar)^3} \frac{d^3 p_\nu}{(2\pi\hbar)^3}$$

$$|\mathcal{M}_{if}|^2 = \frac{1}{2J_i + 1} \sum_{\text{lepton spins}} \sum_{M_i, M_f} |\langle f | \mathbf{H}_w | i \rangle|^2$$

$$\lambda = \frac{1}{2\pi\hbar^7} \int |\mathcal{M}_{if}|^2 \delta(M_f^{\text{nuc}} + E_e + E_\nu - M_i^{\text{nuc}}) p_e^2 p_\nu^2 dp_e dp_\nu \frac{d\Omega_e}{4\pi} \frac{d\Omega_\nu}{4\pi}$$

Transition rates for β decay

$$W = E_e/(m_e c^2); \quad W_0 = \frac{M_i^{\text{nuc}} - M_f^{\text{nuc}}}{m_e c^2} = \frac{Q}{m_e c^2} + 1$$

$$\lambda = \frac{m_e^5 c^4 G_V^2}{2\pi \hbar^7} \int_1^{W_0} C(W) F(Z, W) (W^2 - 1)^{1/2} W (W_0 - W)^2 dW$$

$$C(W) = \frac{1}{G_V^2} \int |\mathcal{M}_{if}|^2 \frac{d\Omega_e}{4\pi} \frac{d\Omega_\nu}{4\pi}$$

$F(Z, W)$ Fermi function, accounts for distortion of the electron (positron) wave function due to Coulomb effects. We need to compute shape factor,

$$C(W) = \frac{1}{G_V^2} \int \frac{1}{2J_i + 1} \sum_{\text{lepton spins}} \sum_{M_i, M_f} |\langle f | \mathbf{H}_W | i \rangle|^2 \frac{d\Omega_e}{4\pi} \frac{d\Omega_\nu}{4\pi}$$

between states: $|i\rangle = |J_i M_i; T_i T_{z_i}\rangle$; $|f\rangle = |J_f M_f; T_f T_{z_f}; e^-; \bar{\nu}\rangle$

Current-Current interaction:

$$\mathbf{H}_w = \frac{G_V}{\sqrt{2}} \int d^3r \mathcal{J}^\mu(\mathbf{r}) j_\mu(\mathbf{r})$$

$$\langle f | \mathbf{H}_w | i \rangle = \frac{G_V}{\sqrt{2}} \int d^3r \langle J_f M_f; T_f T_{z_f}; e, \nu | j_\mu \mathcal{J}^\mu | J_i M_i; T_i T_{z_i} \rangle$$

Assuming plane waves for electron and neutrino:

$$\langle e; \nu | j_\mu | 0 \rangle = e^{-i(\mathbf{p}_e + \mathbf{p}_\nu) \cdot \mathbf{r}} \bar{u} \gamma_\mu (1 - \gamma_5) v$$

$$\langle f | \mathbf{H}_w | i \rangle = \frac{G_V}{\sqrt{2}} l_\mu \int d^3r e^{-i\mathbf{q} \cdot \mathbf{r}} \langle J_f M_f; T_f T_{z_f} | \mathcal{J}^\mu | J_i M_i; T_i T_{z_i} \rangle$$

$$l_\mu = \bar{u} \gamma_\mu (1 - \gamma_5) v$$

Non-relativistic reduction

Assuming one nucleon participates in the decay and that we can use the free current (impulse approximation):

$$\langle f | \mathbf{H}_w | i \rangle = \frac{G_V}{\sqrt{2}} l_\mu \int d^3 r e^{-i\mathbf{q}\cdot\mathbf{r}} \bar{\psi}_f \gamma^\mu (1 + g_A \gamma_5) \mathbf{t}_\pm \psi_i$$

$$\psi = \begin{pmatrix} 1 \\ \frac{\boldsymbol{\sigma}\cdot\mathbf{p}}{E+M} \end{pmatrix} \phi \rightarrow \begin{pmatrix} \phi \\ 0 \end{pmatrix}$$

$$\langle f | \mathbf{H}_w | i \rangle = \frac{G_V}{\sqrt{2}} \int d^3 r e^{-i\mathbf{q}\cdot\mathbf{r}} \phi_f (l_0 \mathbf{1} + g_A \mathbf{l} \cdot \boldsymbol{\sigma}) \mathbf{t}_\pm \phi_i$$

Generalization to A particles:

$$\mathbf{H}_w = \frac{G_V}{\sqrt{2}} \sum_{k=1}^A e^{-i\mathbf{q}\cdot\mathbf{r}_k} (l_0 \mathbf{1}^k + g_A \mathbf{l} \cdot \boldsymbol{\sigma}^k) \mathbf{t}_\pm^k$$

$$H_w = \frac{G_V}{\sqrt{2}} \sum_{k=1}^A e^{-i\mathbf{q}\cdot\mathbf{r}_k} (l_0 \mathbf{1}^k + g_A \mathbf{l} \cdot \boldsymbol{\sigma}^k) t_{\pm}^k$$

$$e^{-i\mathbf{q}\cdot\mathbf{r}} = \sum_l \sqrt{4\pi(2l+1)} (-i)^l j_l(qr) Y_{l0}(\theta, \varphi)$$

$$j_l(qr) \approx \frac{(qr)^l}{(2l+1)!!}$$

- Zero order: Allowed transitions (Fermi, Gamow-Teller)
- Higher orders: Forbidden transitions.

$$\lambda = \frac{\ln 2}{K} \int_1^{W_0} C(W) F(Z, W) (W^2 - 1)^{1/2} W (W_0 - W)^2 dW$$

For allowed transitions: $C(W) = B(F) + B(GT)$,

$$\lambda = \frac{\ln 2}{t_{1/2}} = \frac{\ln 2}{K} [B(F) + B(GT)] f(Z, W_0)$$

$$ft_{1/2} = \frac{K}{B(F) + B(GT)}, \quad K = 6144.4 \pm 1.6 \text{ s}$$

$$B(F) = \frac{1}{2J_i + 1} \sum_{M_i, M_f} |\langle J_f M_f; T_f T_{z_f} | \sum_{k=1}^A \mathbf{t}_{\pm}^k | J_i M_i; T_i T_{z_i} \rangle|^2$$

$$B(F) = [T_i(T_i + 1) - T_{z_i}(T_{z_i} \pm 1)] \delta_{J_i, J_f} \delta_{T_i, T_f} \delta_{T_{z_f}, T_{z_i} \pm 1}$$

Energetics (Isobaric Analog State):

$$E_{\text{IAS}} = Q_{\beta} + \text{sign}(T_{z_i}) [E_C(Z + 1) - E_C(Z) - (m_n - m_H)]$$

Selection rule:

$$\Delta J = 0 \quad \Delta T = 0 \quad \pi_i = \pi_f$$

Sum rule (sum over all the final states):

$$S(F) = S_-(F) - S_+(F) = 2T_{z_i} = (N - Z)$$

Gamow-Teller Transitions

$$B(GT) = \frac{g_A^2}{2J_i + 1} \sum_{m, M_i, M_f} |\langle J_f M_f; T_f T_{z_f} | \sum_{k=1}^A \sigma_m^k t_{\pm}^k | J_i M_i; T_i T_{z_i} \rangle|^2$$

$$B(GT) = \frac{g_A^2}{2J_i + 1} |\langle J_f; T_f T_{z_f} || \sum_{k=1}^A \sigma^k t_{\pm}^k || J_i; T_i T_{z_i} \rangle|^2$$

$$g_A = -1.2720 \pm 0.0018$$

Selection rule:

$$\Delta J = 0, 1 \quad (\text{no } J_i = 0 \rightarrow J_f = 0) \quad \Delta T = 0, 1 \quad \pi_i = \pi_f$$

Ikeda sum rule:

$$S(GT) = S_-(GT) - S_+(GT) = 3(N - Z)$$

β^- decay $|J_i; T, T\rangle$

- Final state $|J_f; T - 1, T - 1\rangle$

$$B(GT) = \frac{2g_A^2}{2J_i + 1} \frac{|\langle J_f; T - 1 || \sum_{k=1}^A \sigma^k t^k || J_i; T \rangle|^2}{2T + 1}$$

- Final state $|J_f; T, T - 1\rangle$

$$B(GT) = \frac{2g_A^2}{2J_i + 1} \frac{|\langle J_f; T || \sum_{k=1}^A \sigma^k t^k || J_i; T \rangle|^2}{(2T + 1)(T + 1)}$$

- Final state $|J_f; T + 1, T - 1\rangle$

$$B(GT) = \frac{2g_A^2}{2J_i + 1} \frac{|\langle J_f; T + 1 || \sum_{k=1}^A \sigma^k t^k || J_i; T \rangle|^2}{(2T + 1)(T + 1)(2T + 3)}$$

Forbidden Transitions

Involve operators $r^l Y_{lm}$ and $r^l [Y_{lm} \otimes \sigma]^K$

Selection rules

Decay type	ΔJ	ΔT	$\Delta \pi$	$\log ft$
Superallowed	$0^+ \rightarrow 0^+$	0	no	3.1–3.6
Allowed	0,1	0,1	no	2.9–10
First forbidden	0,1,2	0,1	yes	5–19
Second forbidden	1,2,3	0,1	no	10–18
Third forbidden	2,3,4	0,1	yes	17–22
Fourth forbidden	3,4,5	0,1	no	22–24

Fermi's golden rule:

$$\sigma = \frac{2\pi}{\hbar v_e} \int |\mathcal{M}_{if}|^2 (2\pi\hbar)^3 \delta^{(4)}(p_f + p_\nu - p_i - p_e) \frac{d^3 p_f}{(2\pi\hbar)^3} \frac{d^3 p_\nu}{(2\pi\hbar)^3}$$

$$\sigma_{i,f}(E_e) = \frac{G_V^2}{2\pi\hbar^4} F(Z, E_e) [B(F) + B(GT)] p_\nu^2$$

Neutrino cross sections

Charged current: $(Z, A) + \nu_e \rightarrow (Z + 1, A) + e^-$

$$\sigma_{i,f}(E_\nu) = \frac{G_V^2}{\pi} p_e E_e F(Z + 1, E_e) [B(F) + B(GT)]$$

Neutral current: $(Z, A) + \nu \rightarrow (Z, A)^* + \nu$

$$\sigma_{i,f}(E_\nu) = \frac{G_F}{\pi} (E_\nu - w)^2 B(GT_0)$$

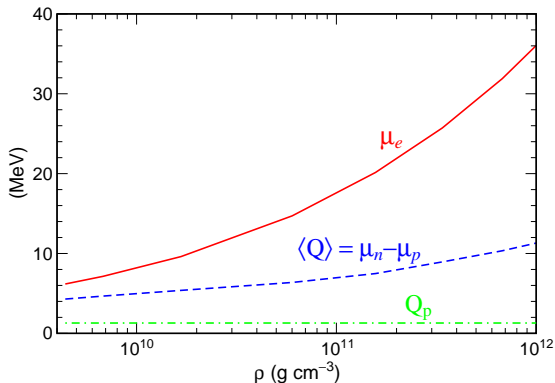
with $w = E_f - E_i$

In general, multipoles beyond allowed transitions are necessary. See Donnelly and Peccei, Phys. Repts. **50**, 1 (1979).

General considerations: Which multipoles?

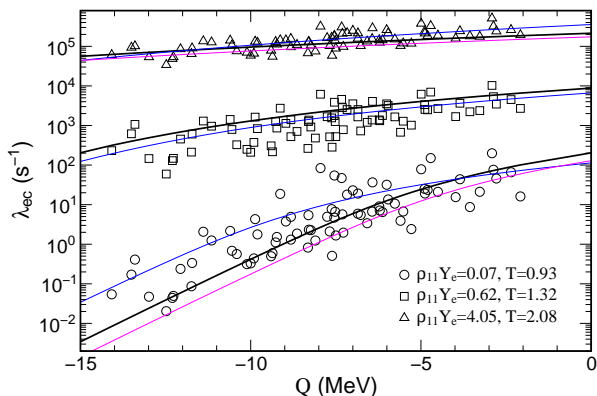
- **Multipole operators O_λ**
 - $\sim \left(\frac{qR}{\hbar c}\right)^\lambda$; $q \approx E_\nu$
 - **successively higher rank with increasing E_ν**
- **Collective nuclear excitations:**
 - $[H, O_\lambda] \neq 0 \rightarrow$ **strength is fragmented**
 - **centroid $E_{coll}^\lambda \sim \lambda \hbar \omega \sim \lambda \frac{41}{A^{1/3}} \text{MeV}$**
- **Phase space:**
 - $\sim p_{lep} E_{lep} \rightarrow$ **high E_{lep} preferred**
 - **average nuclear excitation $\bar{\omega}$ lags behind with increasing E_ν**
 - **if $E_\nu \gg \bar{\omega}$, σ sensitive to **total** strength**

Electron capture: energetics during collapse



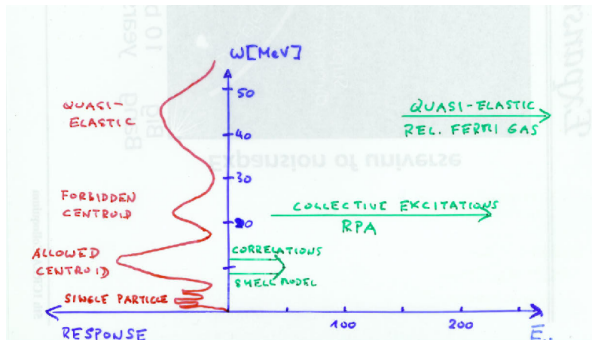
capture rate becomes less dependent on details of GT distribution with increasing density (chem. potential); for $\rho_{11} > \sim 1$, it depends essentially only on total strength and centroid

Example: electron capture at high electron energy



Assumption: capture proceeds by a single transition ($E_f - E_i = \text{const}$) with a constant strength

Remarks about response: Which models?

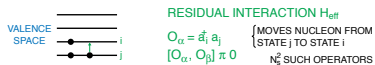


INTERACTING

SHELL MODEL



EXTERNAL SPACE (ALWAYS EMPTY)



CORE (ALWAYS OCCUPIED)

HAMILTONIAN

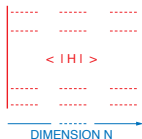
$$H = \epsilon O - \frac{1}{2} V O^2$$

- IF $V = 0$, H IS PURE 1-BODY, SOLVABLE
 $N_s \times N_s$ MATRIX ELEMENTS
- IF $V \neq 0$, $\phi \xrightarrow{H_{\text{eff}}} \{\text{ALL POSSIBLE } \phi\text{'s}\}$
FULL COMBINATORIAL DIMENSION

C-196-1

Diagonalization shell model.

DIAGONALIZATION APPROACH



"GIANT" MATRIX

$$N = \begin{pmatrix} N_S \\ N_{VAL}^P \end{pmatrix} \begin{pmatrix} N_S \\ N_{VAL}^N \end{pmatrix}$$
$$= 10^9 \text{ FOR } {}^{60}\text{Zn}$$

REDUCTION OF SIZE DUE TO SYMMETRIES

MODERN ALGORITHM (STRASSBOURG - MADRID)

- LANCZOS ALGORITHM
(FEW LOWEST EIGENSTATES)
- STORAGE OF ONLY H_{pp} , H_{nn} , H_{pn}
- EFFICIENT ALGORITHM TO CONSTRUCT
<.....H.....> FROM H_{pp} , H_{nn} , H_{pn}

ALL EVEN-EVEN NUCLEI IN PF-SHELL

C-1962

Shell Model Monte Carlo.

SHELL MODEL MONTE CARLO

GOAL: DETERMINE NUCLEAR PROPERTIES,
NOT ALL $\sim 10^9$ COMPONENTS OF W.F.

- CONSIDER THERMAL AVERAGE IN CANONICAL
(FIXED NUMBER) ENSEMBLE

$$\langle A \rangle = \frac{\text{Tr}(e^{-\beta H} A)}{\text{Tr}(e^{-\beta H})} \quad \beta = \frac{1}{T}$$

- HUBBARD - STRATONOVICH TRANSFORMATION

2-BODY \Rightarrow MANY 1-BODY EVOLUTIONS IN
FLUCTUATING EXTERNAL FIELDS

SUPPOSE

$$e^{-\beta H} \rightarrow e^{\frac{i}{2}\beta V O^2} = \int \frac{d\sigma}{\sqrt{2\pi/\beta V}} e^{\frac{i}{2}\beta V \sigma^2} \underbrace{e^{\beta \sigma V O}}_{\text{1-BODY PROPAGATOR}}$$

HOWEVER: MANY NON-COMMUTING O's

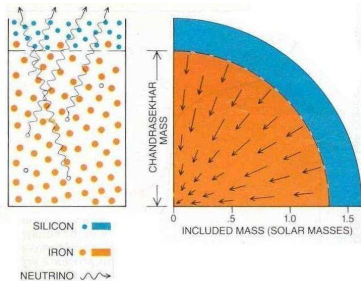
$$e^{-\beta H} = (e^{-\Delta \beta H})^{N_t} ; \quad \Delta \beta = \frac{\beta}{N_t} \text{ "TIME SLICE"}$$

- \Rightarrow SEPARATE σ -FIELDS AT EACH TIME SLICE FOR EACH O

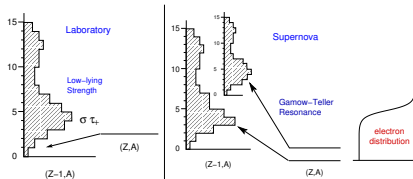
- MONTE-CARLO EVALUATION OF σ -INTEGRALS
EMBARRASSINGLY PARALLEL

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Presupernova evolution.



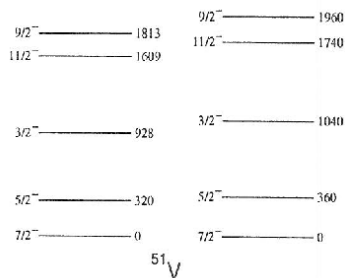
- $T = 0.1\text{--}1.0 \text{ MeV}$,
 $\rho = 10^7\text{--}10^{10} \text{ g cm}^{-3}$.
- Composition of iron group nuclei ($A=45\text{--}65$)
- The dynamical time scale set by electron captures:
$$e^- + (N, Z) \rightarrow (N + 1, Z - 1) + \nu_e$$
- Evolution decreases number of electrons (Y_e)



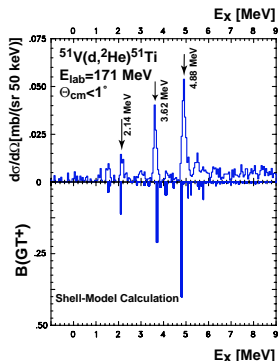
Capture rates on individual nuclei computed by Shell Model.

Gamow-Teller strength distributions

medium-mass nuclei: shell model is method of choice

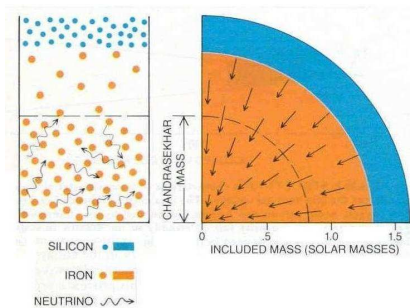


spectrum



GT distribution, KVI Groningen

Collapse phase.



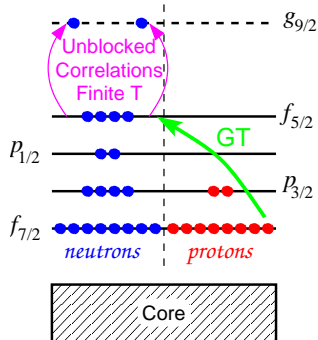
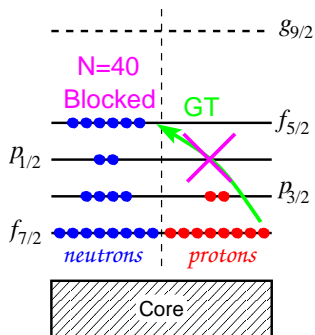
Important processes:

- $T > 1.0 \text{ MeV}$, $\rho > 10^{10} \text{ g cm}^{-3}$.
- electron capture on protons
 $e^- + p \rightarrow n + \nu_e$
- Neutrino transport (exact solution Boltzmann equation):
 $\nu + A \rightleftharpoons \nu + A$ (trapping)
 $\nu + e^- \rightleftharpoons \nu + e^-$ (thermalization)
cross sections $\sim E_\nu^2$

What is the role of electron capture on nuclei?

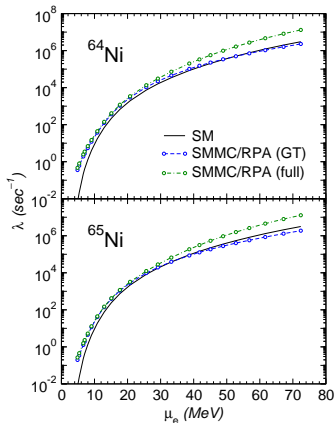


Pauli blocking of Gamow-Teller transition



- Unblocking mechanism: correlations and finite temperature
- calculation of rate in SMMC + RPA model

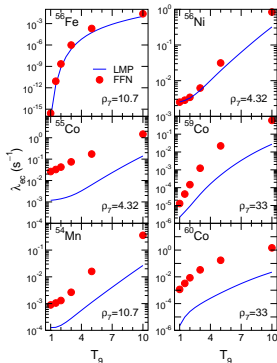
Validation of SMMC/RPA approach



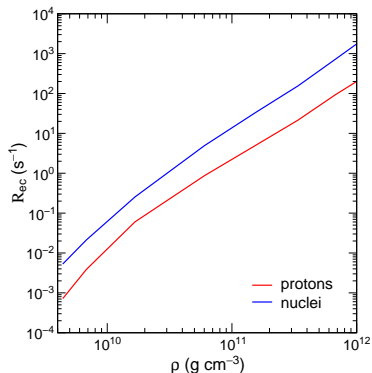
At low μ , not valid, sensitivity to GT details.

At moderate μ (where we need the model), good description of rate.

How do shell-model rates compare to previous rates?



$A < 65$: SM rates smaller



$A > 65$: SM rates larger

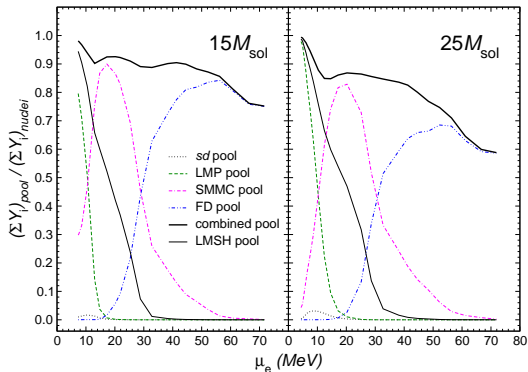
For supernova conditions there exist several tabulations for weak-interaction rates (electron and positron capture, β^\pm decay)

- **FFN**: independent particle model, supplemented by data wherever available, $A=21-60$
G.M. Fuller, W.A. Fowler, M.J. Newman, Astr. J. 252 (1982) 715; 293 (1985) 1.
- **OHMTK**: diagonalization shell model, $A=17-39$
T. Oda, M. Hino, K. Muto, M. Takahara, K. Sato, ADNDT 56 (1994) 231
- **LMP**: diagonalization shell model, supplemented by data wherever available, $A=45-65$
K. Langanke and G. Martinez-Pinedo, Nucl. Phys. A673 (2000) 481; ADNDT 79 (2001) 1
- **Pruet-Fuller**: independent particle model ($A < 80$), phase space model (electron capture, $A > 80$)
J. Pruet and G.M. Fuller, Astr. J. Suppl. 149 (2003) 189

For supernova conditions there exist several tabulations for weak-interaction rates (electron capture)

- **LMSH**: Shell Model Monte Carlo + RPA, $A=65-112$
J.M. Sampaio, thesis, Aarhus (2003); Phys. Rev. Lett. 90 (2003)
- **Nabi+Klapdor-Kleingrothaus**: QRPA
J.U. Nabi, H.V. Klapdor-Kleingrothaus, ADNDT 88 (2004) 237
- **JLMSH**: parametrized RPA model, $A>65$
A. Juodagalvis, K. Langanke, G. Martinez-Pinedo, J.M. Sampaio, R. Hix, submitted to PRC

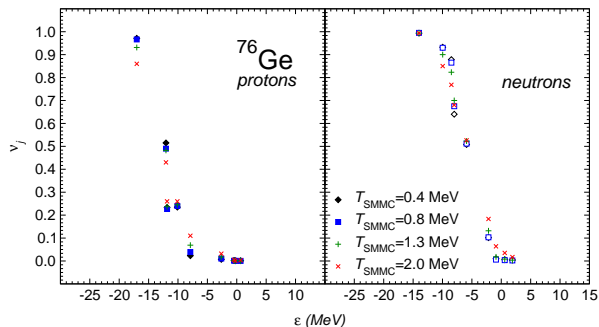
Capture rates and number of nuclei considered



Very neutronrich nuclei are missed in the pool of nuclei.

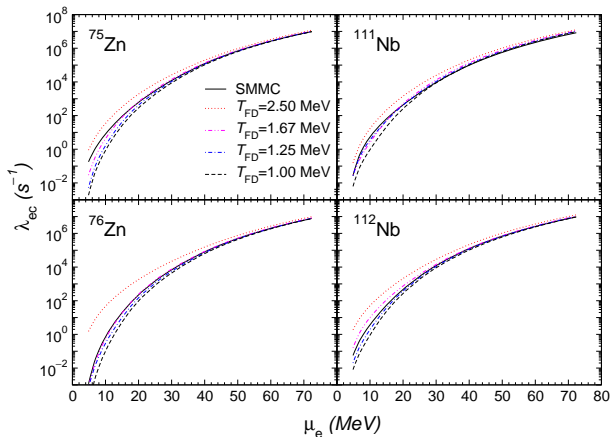
Capture gets more Pauli-blocked with increasing neutron excess.

Single-particle occupation numbers



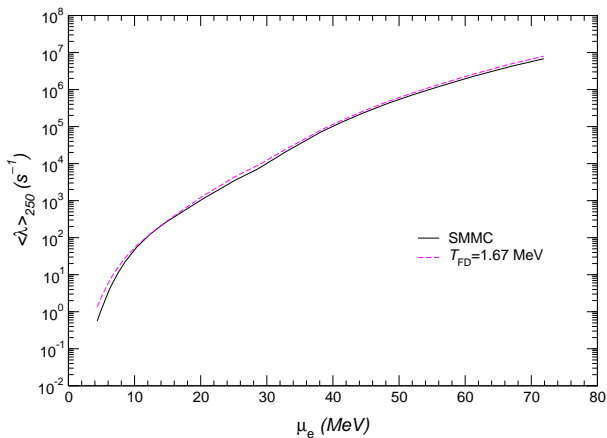
Parametrization of SMCC occupation numbers by Fermi-Dirac function with 'temperature' as fit parameter.

RPA with parametrized occupation numbers

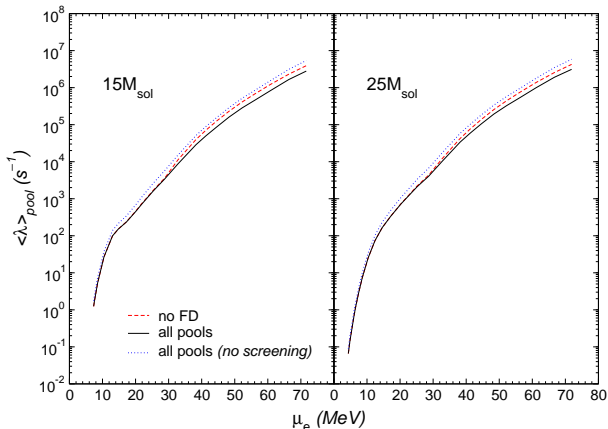


Parametrization of SMMC occupation numbers by Fermi-Dirac function with $T = 1.67$ MeV as fit parameter.

Empirical model vs SMMC/RPA approach

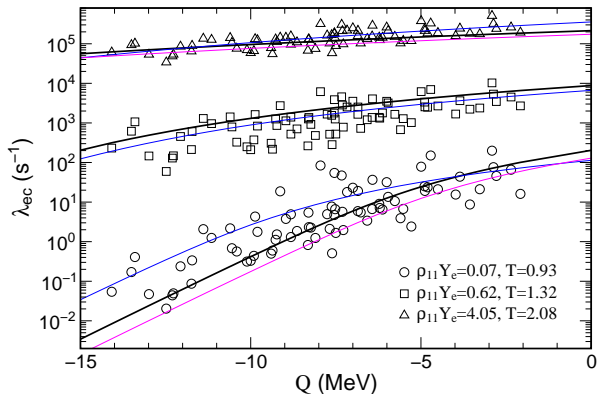


Capture rates



Screening effects: electron chemical potential slightly reduced, while effective Q-value slightly enlarged

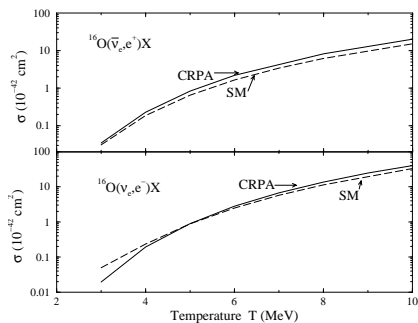
Example: electron capture at high electron energy



Assumption: capture proceeds by a single transition ($E_f - E_i = \text{const}$) with a constant strength

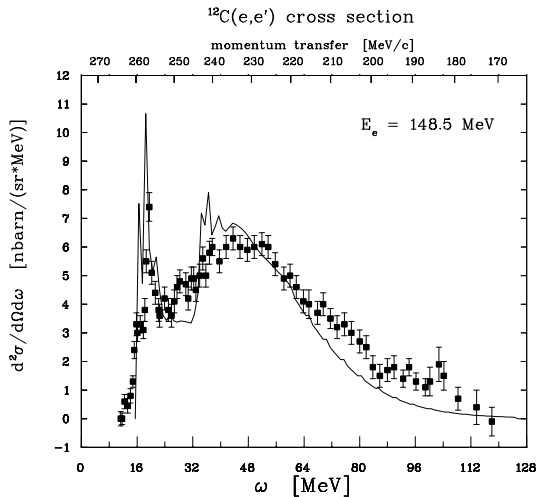
This is the assumption made by J. Pruet and G.M. Fuller in their calculation of electron capture rates for heavier ($A > 80$) nuclei.

Shell Model versus RPA.

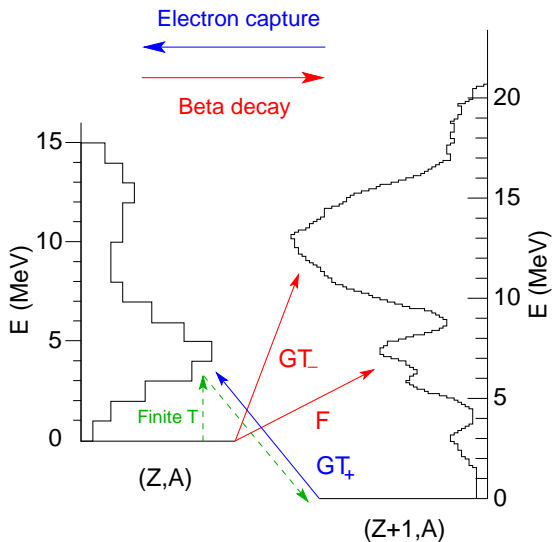


The RPA considers only (1p-1h) correlations; it is well suited to describe the centroid of giant resonances

Inelastic electron scattering: RPA description of response



Beta-decay, electron capture, charged-current



Systematics of Fermi and Gamow-Teller centroids

ESTIMATE OF CHARGED-CURRENT CROSS SECTION

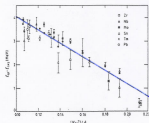
$$\sigma(E_\nu) = \frac{G_F^2 \cos^4 \theta_c}{\pi} h_e E_e F(Z+1, E_e) \left(|M_F|^2 + \left(\frac{g_A}{g_V}\right)^2 |M_{GT}|^2 \right)$$

FERMI TRANSITIONS

- $|M_F|^2 = (N-2)$ ISOBARIC ANALOG
- $E_{IAS} \approx \left(\frac{1.328 Z}{1.42 A^{1/3} + 0.78} - 1.293 \right) \text{ MeV}$

GAMOW-TELLER TRANSITIONS

- $|M_{GT}|^2 = 3(N-2)$ VERY NEUTRON RICH
IKEDA SUM RULE
- $\langle E_{GT} \rangle - \langle E_{IAS} \rangle = A + 2(N-2)$

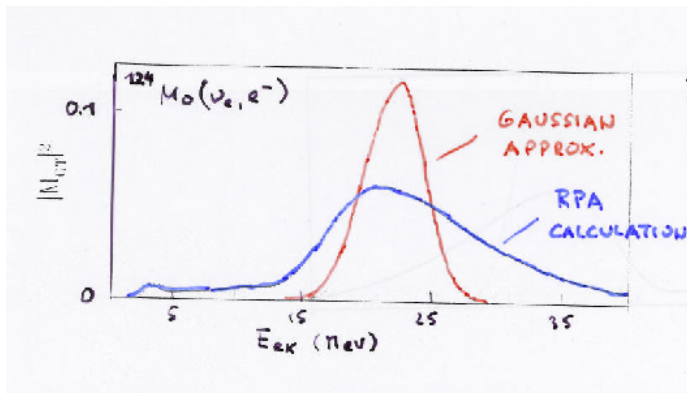


- DISTRIBUTION
 - a) δ -FUNCTION
 - b) GAUSSIAN AROUND $\langle E_{GT} \rangle$ WITH WIDTH $\sim 5 \text{ MeV}$

THE OPEN QUESTIONS :

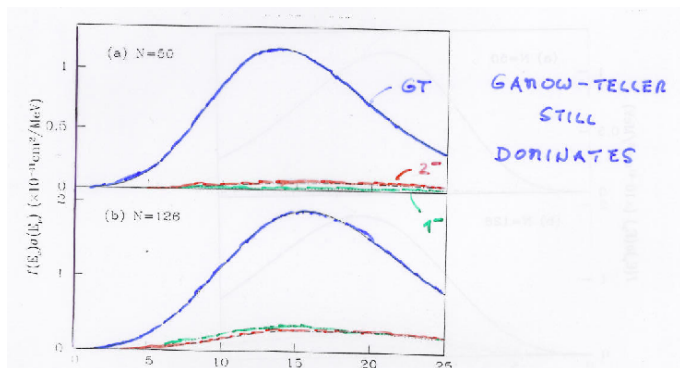
- LOW LYING GT-STRENGTH
- FORBIDDEN TRANSITIONS

How well do we know charged-current cross sections?



RPA vs simple Gaussian: \sim factor 2 (Surmann+Engel)

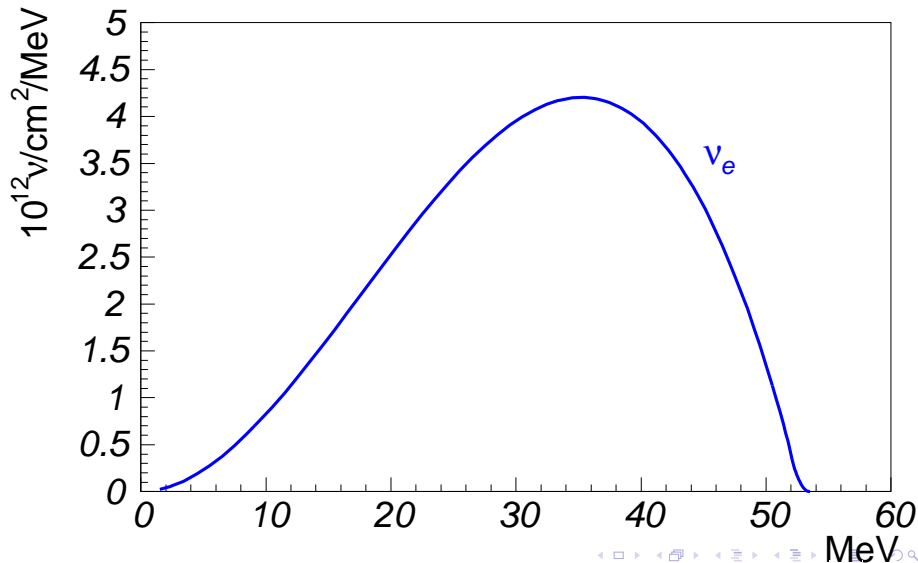
What about other multipoles?



for neutrino spectrum with $T = 4$ MeV

Influence of higher multipoles

Spectrum for muon decay: $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$

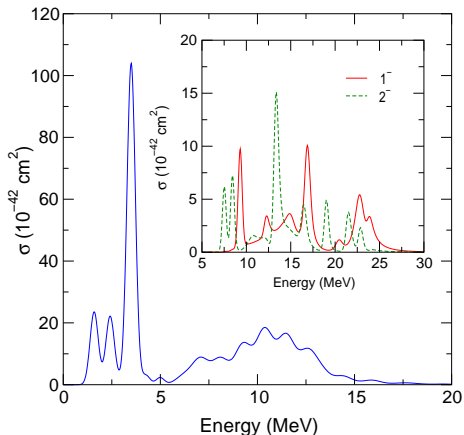


Influence of higher multipoles

$^{56}\text{Fe}(\nu_e, e^-)^{56}\text{Co}$ measured by KARMEN collaboration:

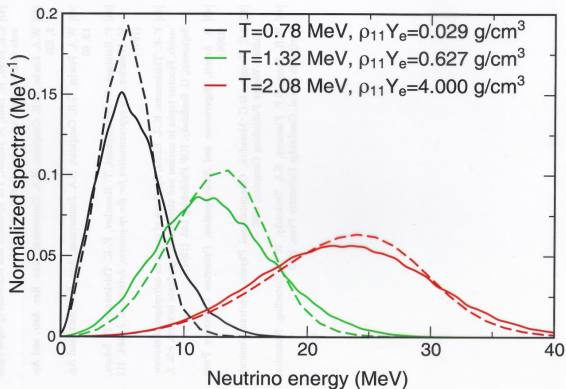
$$\sigma_{exp} = 2.56 \pm 1.08(stat) \pm 0.43(syst) \times 10^{-40} \text{ cm}^2$$

$$\sigma_{th} = 2.38 \times 10^{-40} \text{ cm}^2$$

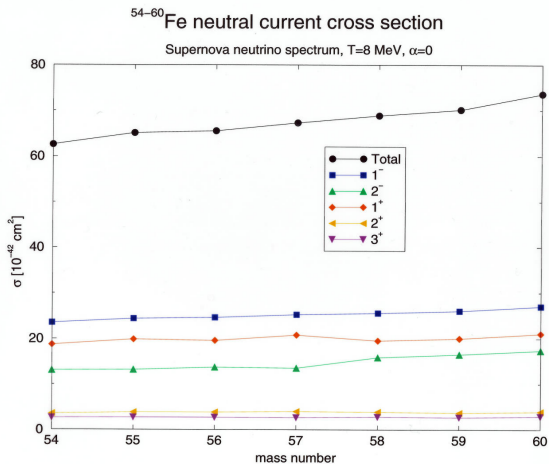


E. Kolbe, K. Langanke, G. Martinez-Pinedo, Phys. Rev. C60 (1999)

Typical supernova neutrino spectra

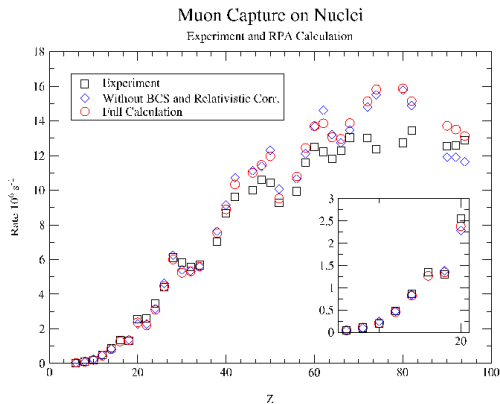


Multipole decomposition



Muon capture

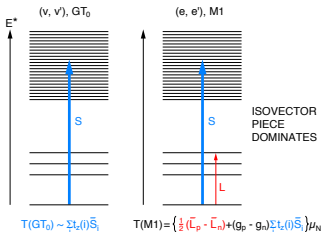
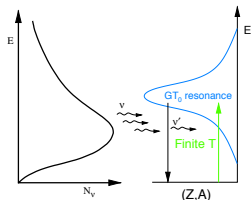
kinematics similar to capture of antineutrinos with a few 10 MeV



N.T. Zinner *et al.*, RPA calculations, submitted to Phys. Rev. C

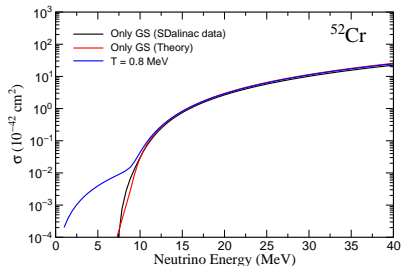
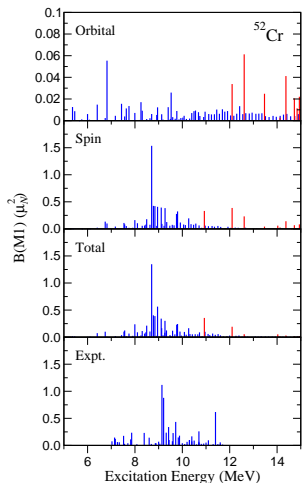
Determining inelastic neutrino-nucleus cross sections

INELASTIC NEUTRINO SCATTERING ON NUCLEI



M1 DATA YIELD GT₀ INFORMATION
IF ORBITAL PART CAN BE REMOVED

Neutrino cross sections from electron scattering

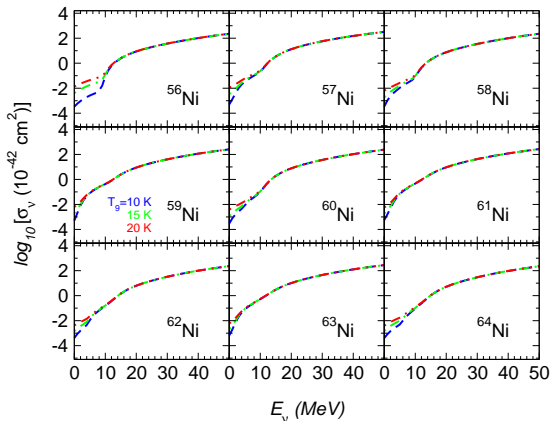


- high-precision SDalinac data
- large-scale shell model

- neutrino cross sections from (e, e') data
- validation of shell model
- G.Martinez-Pinedo, P. v. Neumann-Cosel, A. Richter

- **Fuller-Meyer**: parametrized Gamow-Teller model (Gaussian), (ν_e, e^-)
G.M. Fuller and B.S. Meyer, Astr. J. 453 (1995) 792; G. McLaughlin and G.M. Fuller, Astr. J. 455 (1995) 202
- **Borzov+Goriely**: Fermi liquid theory, (ν_e, e^-)
I. Borzov and S. Goriely, Phys. Rev. C62 (2000)035501
- **Langanke-Kolbe**: RPA, neutronrich nuclei, (ν_e, e^-) , (ν, ν')
K. Langanke and E. Kolbe, ADNDT 79 (2001) 293; 82 (2002) 191
- **Juodagalvis**: diagonalization shell model + RPA, (ν, ν') , finite T
A. Juodagalvis, K. Langanke, G. Martinez-Pinedo, W.R. Hix, D.J. Dean and J.M. Sampaio, Nucl. Phys. A747 (2005) 87

Inelastic neutrino-nucleus cross sections



- large-scale shell model (allowed transitions), finite-T effects
- random phase approximation (forbidden transitions)
- A. Juodagalvis, W.R. Hix, G. Martinez-Pinedo, J.M. Sampaio