

# *Theory for Core-Collapse Supernova Explosions*

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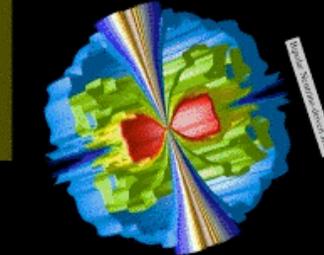
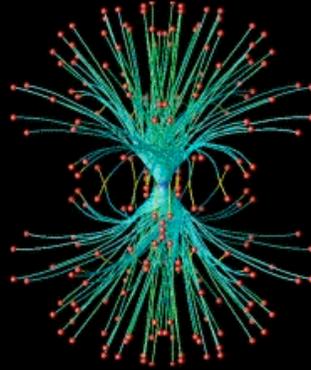
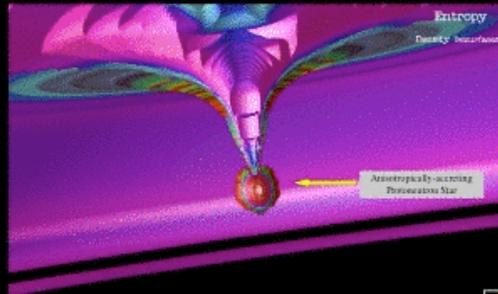
Adam Burrows, Jason Nordhaus, Christian Ott,  
Jeremiah Murphy, John Bell, Ann Almgren, Luc  
Dessart, Louis Howell, Mike Singer, Eli Livne,  
Tim Brandt



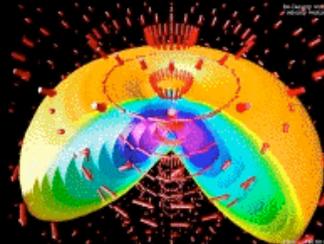
**Multi-Dimensional Core-Collapse**  
**Simulations: Explosion Mechanisms**

(A. Burrows, L. Dessart, E. Livne, C. Ott, I. Hubeny, & J. Murphy)

Core-Oscillation - Acoustic Mechanism



Accretion-Induced Collapse of a White Dwarf



2 1/2-D Multi-Group Radiation Magneto-Hydrodynamic Capability:  
**VULCAN**

Many New Simulation Results

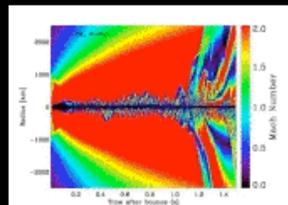
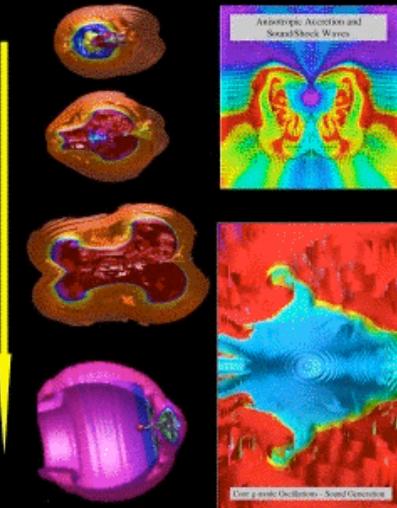
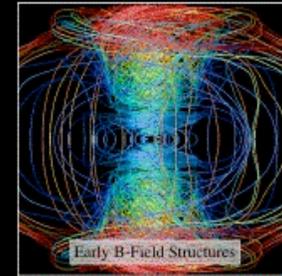
New BETHE Code Development: Multi-D Neutrino Mechanism

**BETHE: Hydro**

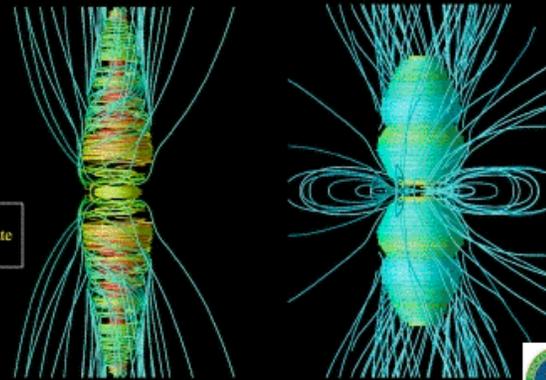
- Compatible Arbitrary-Lagrangian-Eulerian (ALE) Hydrodynamics for Unstructured Grids using the Support Operator Method
- 2nd-order in space & time
- 2nd-order bound- and sign-preserving Remap for arbitrary polygonal grids
- Arbitrary moving grid
- General EOS
- Iterative Poisson Gravity Solver
- Also discretized using Support Operator Method
- Multi-grid preconditioner, GMRES acceleration

**BETHE: Transport**

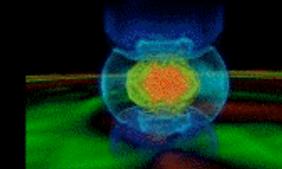
- Motivation: a need for a fast and efficient multi-D transport solver for supernovae and other astrophysical simulations
- Full transport
  - Time-dependent, implicit
  - 2 1/2 D + 2D (axisymmetric + rotation)
  - All terms up to  $O(v/c)$  included
  - Multi-group, Multi-angle
  - Anisotropic scattering
  - Isotropic scattering
  - Hubeny & Burrows 2007



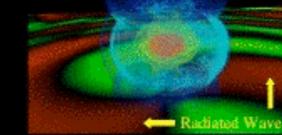
Shock and Core Oscillation to Late Explosion



Magneto-Rotational Jet Mechanism

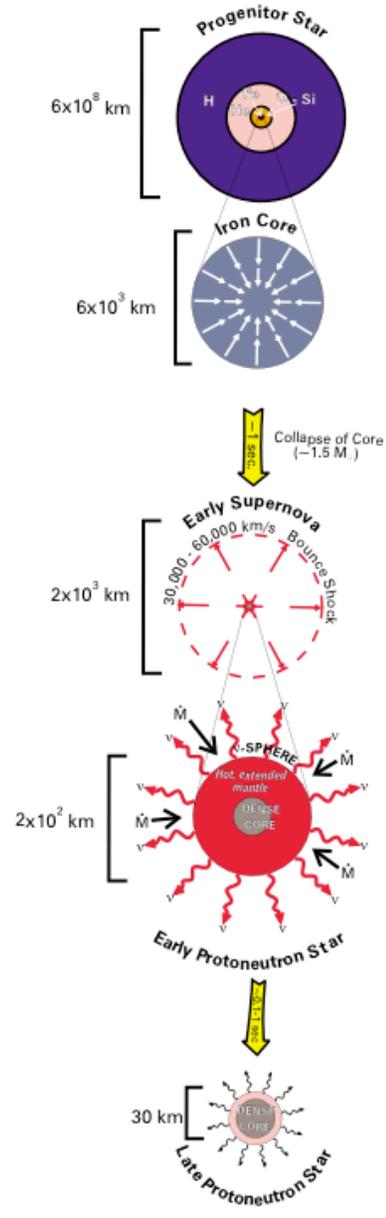


3D General-Relativistic Rotational Collapse: Gravitational Radiation



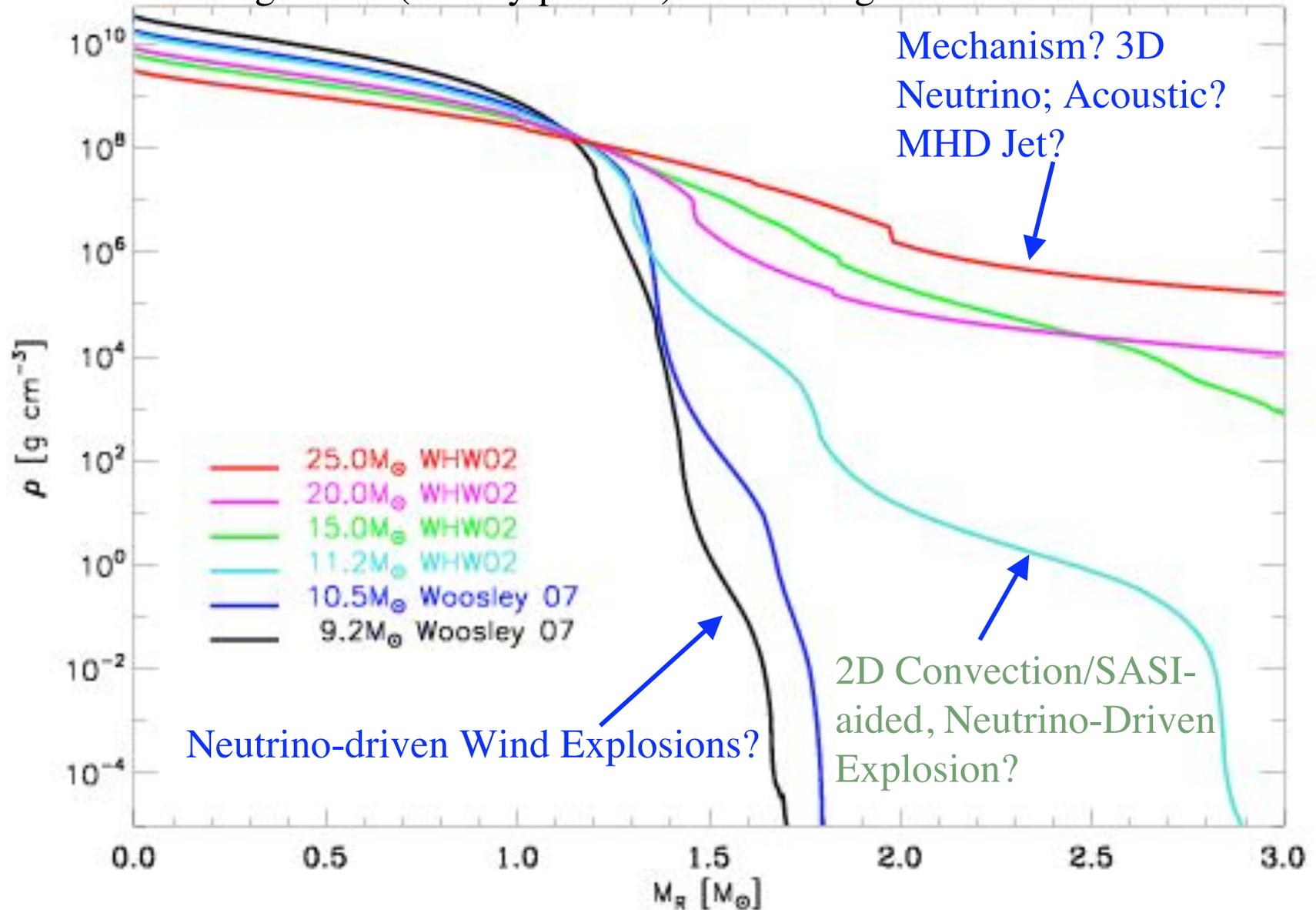
# *Some Pressing Issues in Core-Collapse Supernova Theory*

- **Mechanism of Explosion:**
  - Neutrino mechanism
  - MHD mechanism
  - Acoustic mechanism
- **Neutrino-driven Convection vs. SASI?**
- **1D vs. 2D (VULCAN) vs. 3D (CASTRO!)**
- **Pulsar Kicks** (proper motions), B-fields?
- **Blast Morphology** (Jets?)
- **Pulsar Spins?**
- **Connection with GRBs and Hypernovae?**

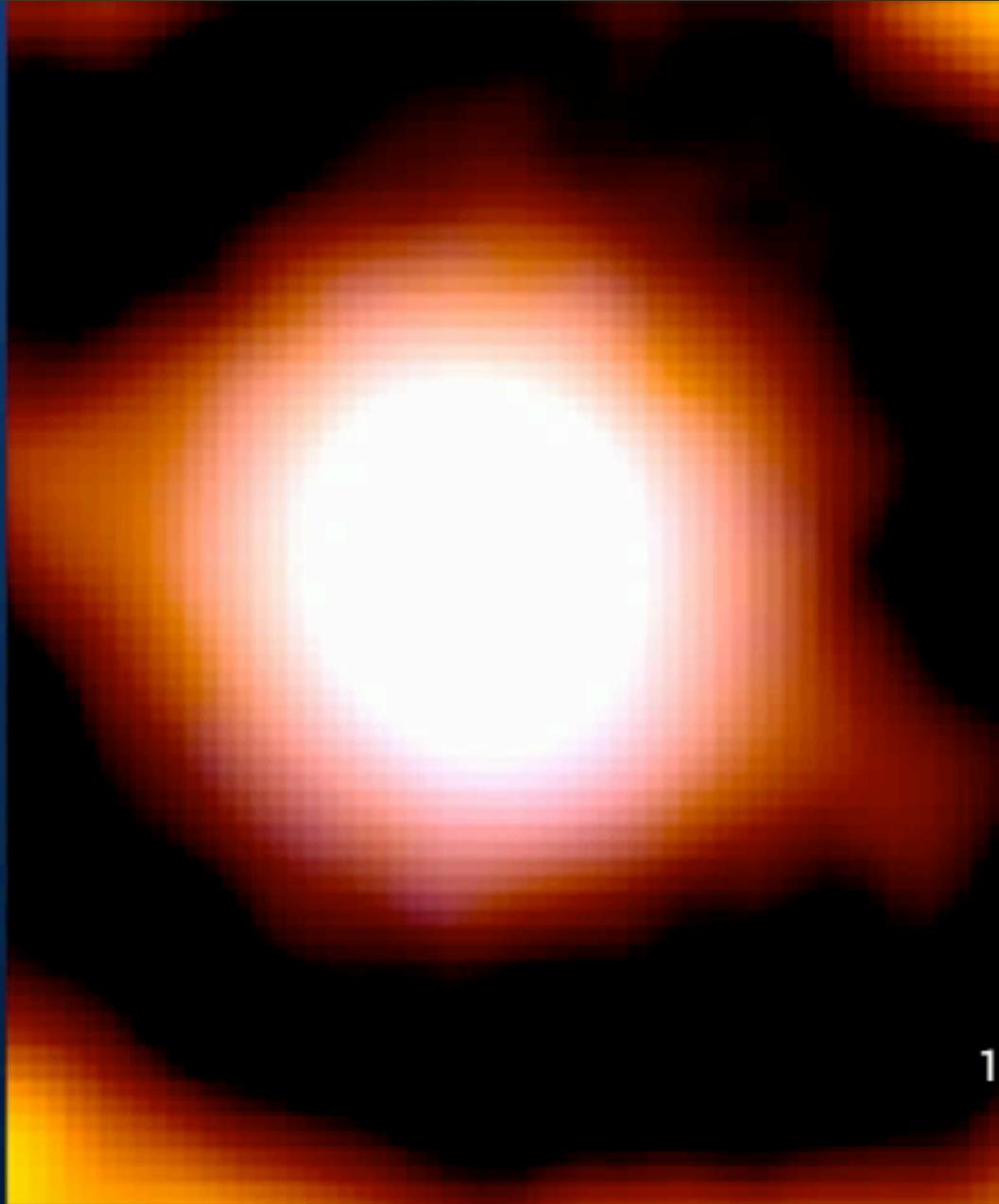


# Density Profiles of Supernova Progenitor Cores

Progenitors (density profiles) Make a Big Difference!



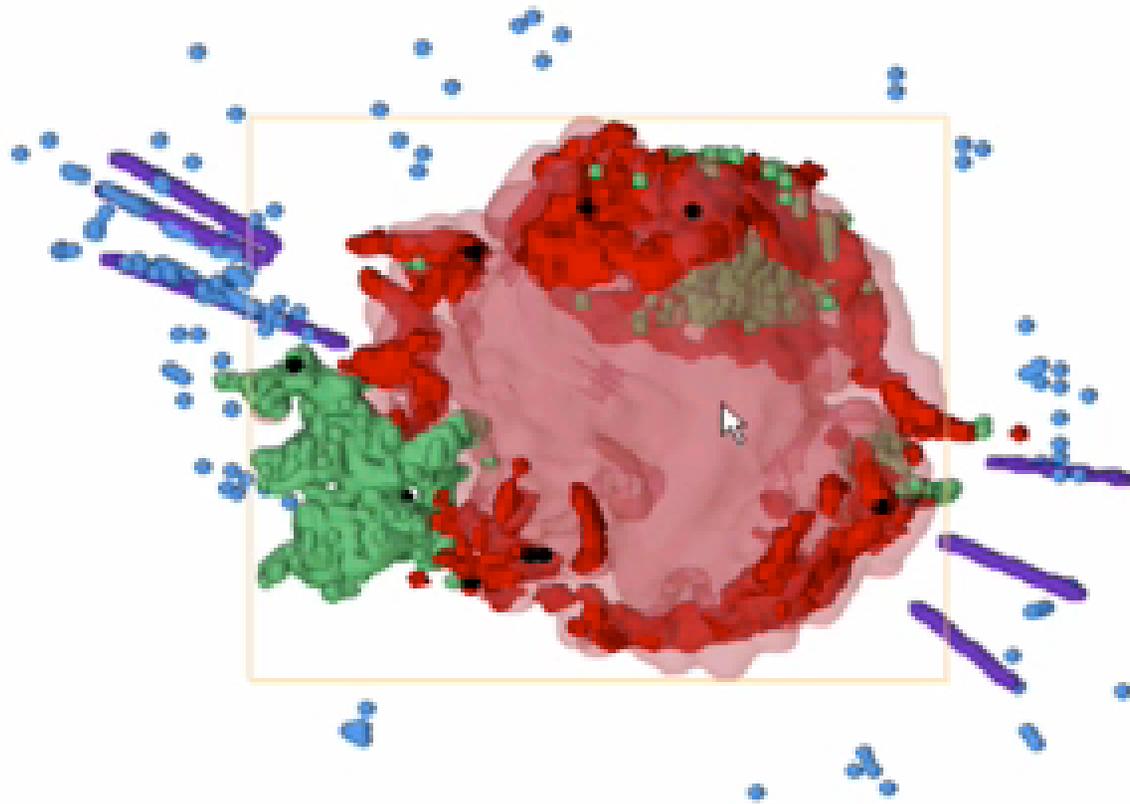
SN1987a (Pete Challis)



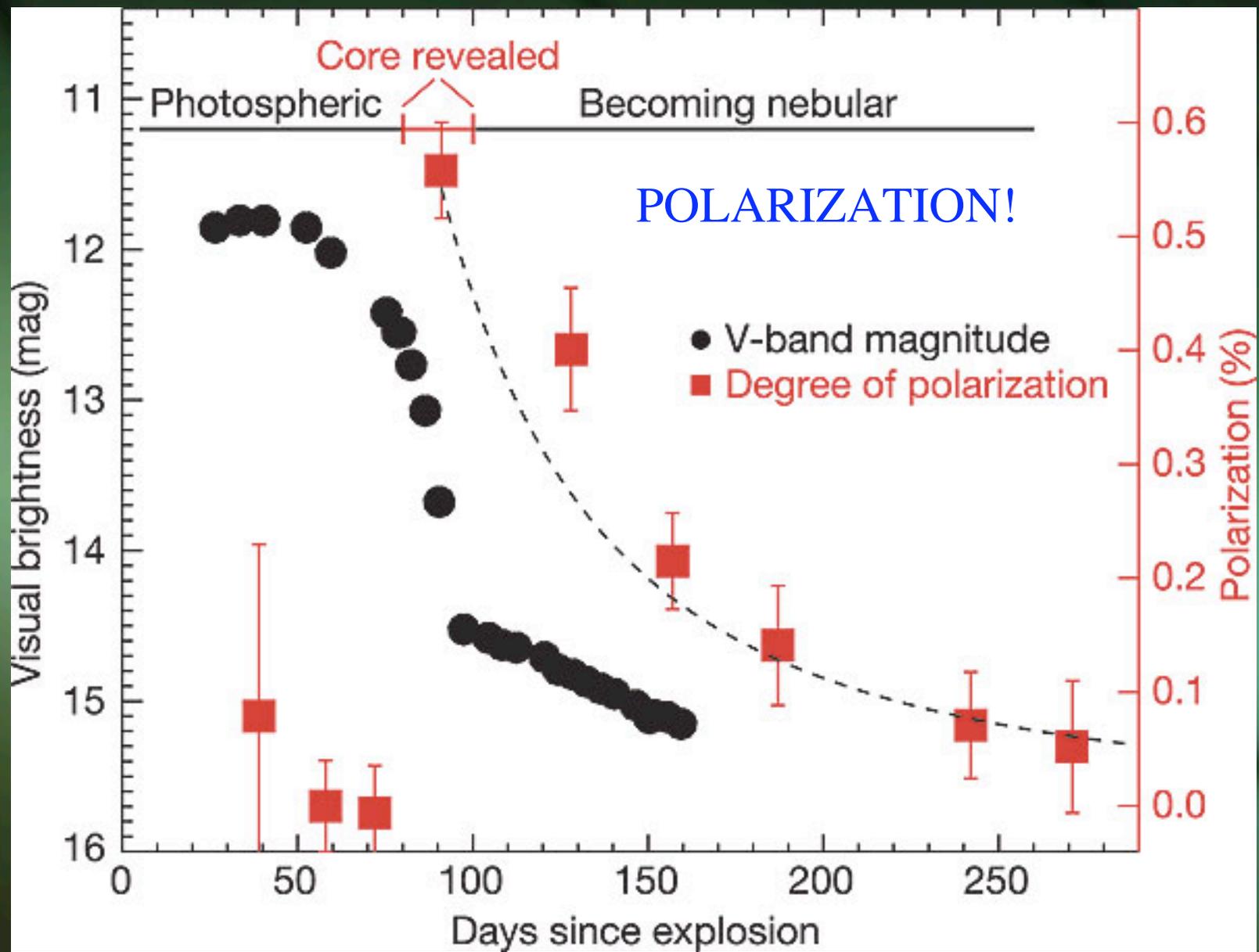
1994

# *Element Asymmetries in Cas A Remnant*

Fe  
Si



DeLaney et al. 2009



Leonard et al. 2006

# *Mechanisms of Explosion*

- Direct Hydrodynamic Mechanism: always fails?
- Neutrino-Driven Wind Mechanism,  $\sim 1D$  (Burrows 1987) Lowest-mass massive stars,  $\sim$ spherical (e.g., 8.8 solar masses, Kitaura et al. 2006, Burrows, Dessart, & Livne 2007)
- Convection/SASI-aided (Burrows et al. 1995; Blondin et al. 2003) Neutrino-Driven Wind Mechanism,  $2D$  (e.g., 11.2 solar masses, Buras et al. 2006)
- Neutrino-Driven Jet/Wind Mechanism, Rapidly rotating AIC of White Dwarf (Dessart et al. 2006)
- Acoustic Power Mechanism (after delay), all progenitors explode (Burrows et al. 2006, 2007a) (Weinberg & Quataert 2008 ?)

# *Mechanisms of Explosion* *(cont.)*

- Convection/SASI-aided Neutrino mechanism? Nuclear-burning aided?? Inelastic scattering?? (Mezzacappa et al. 2006; Marek & Janka 2009; Bruenn et al. 2009; Murphy & Burrows 2008)
- MHD Jet Explosions - requires rapid rotation (e.g., Burrows et al. 2007b)
- The Key feature of almost all mechanisms is the Breaking of Spherical Symmetry (and simultaneous accretion during early explosion)

## *Multi-D: Simultaneous Explosion and Accretion is the Key?*

- **Neutrino Mechanism:** Anisotropic  $l=1$  explosion --> lower ram pressure at head, larger neutrino heating region, while accretion elsewhere maintains neutrino luminosity to drive the explosion (2D vs. 3D?)
- **MHD-Rapid rotation:** Explosion along poles, accretion of free rotational energy at equator (engine)
- **Acoustic Mechanism:** Explosion in one direction, accretion funnels from another, powering oscillation to maintain acoustic power

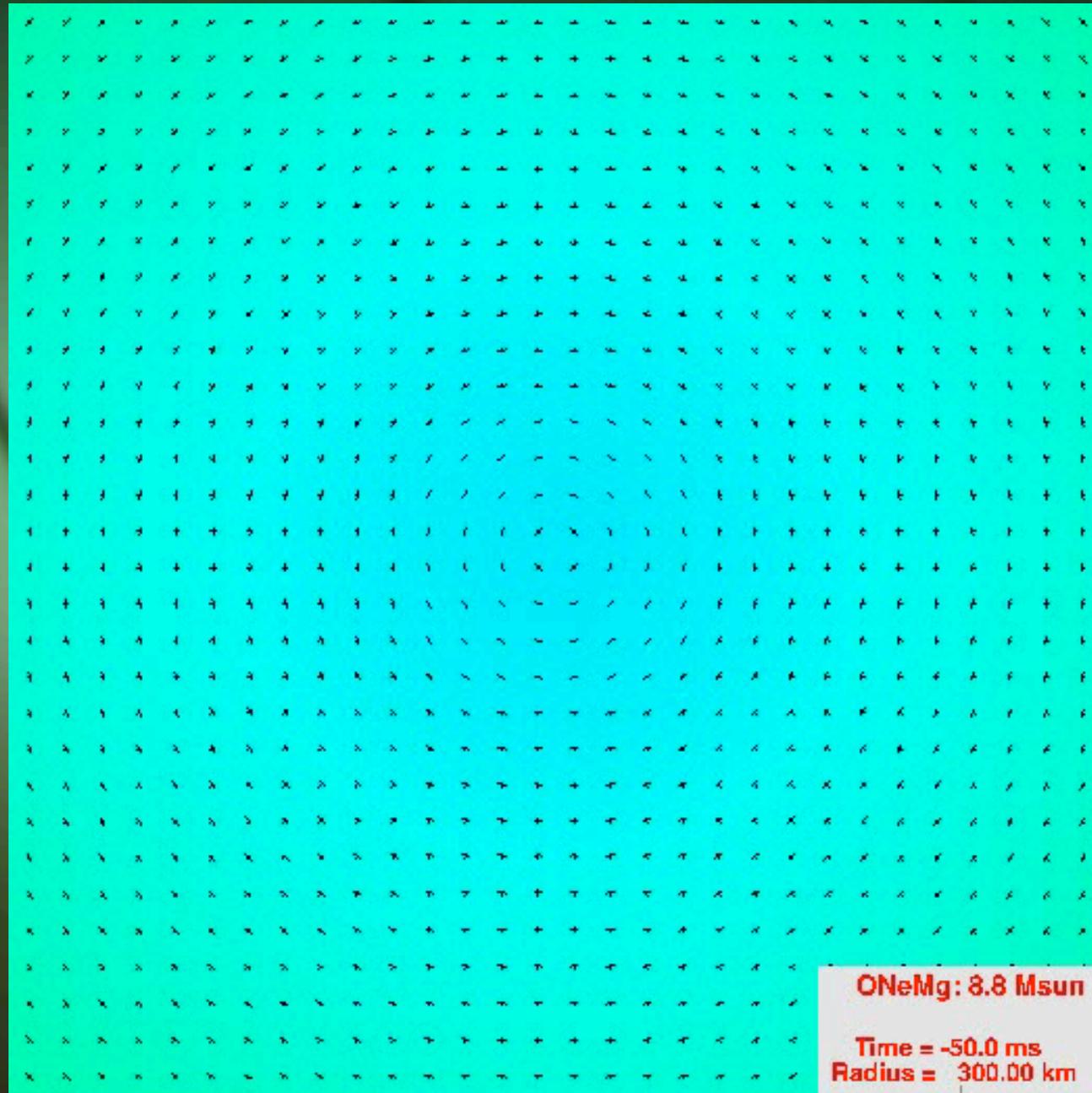
*Neutrino-Driven Wind  
Explosions: Low Mass  
Progenitors*

## 8.8-Solar mass Progenitor of Nomoto: Neutrino-driven Wind Explosion

First shown  
by Kitaura et  
al. 2006

Burrows,  
Dessart, &  
Livne 2007;

Burrows  
1987



NOTE  
WIND  
THAT  
FOLLOWS

ONeMg: 8.8 Msun

Time = -50.0 ms  
Radius = 300.00 km

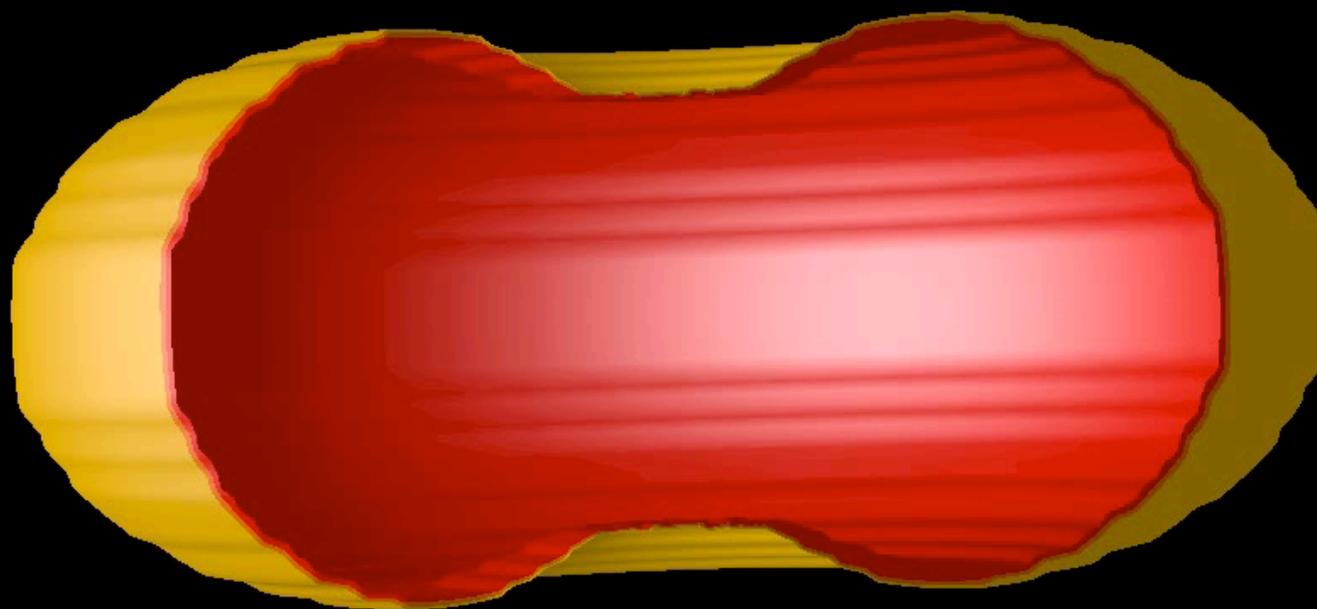
*Accretion-Induced  
Collapse of  
O-Ne-Mg White Dwarfs*

Dessart, Burrows, Ott, Livne, Yoon, & Langer 2006

Rapid Rotation!

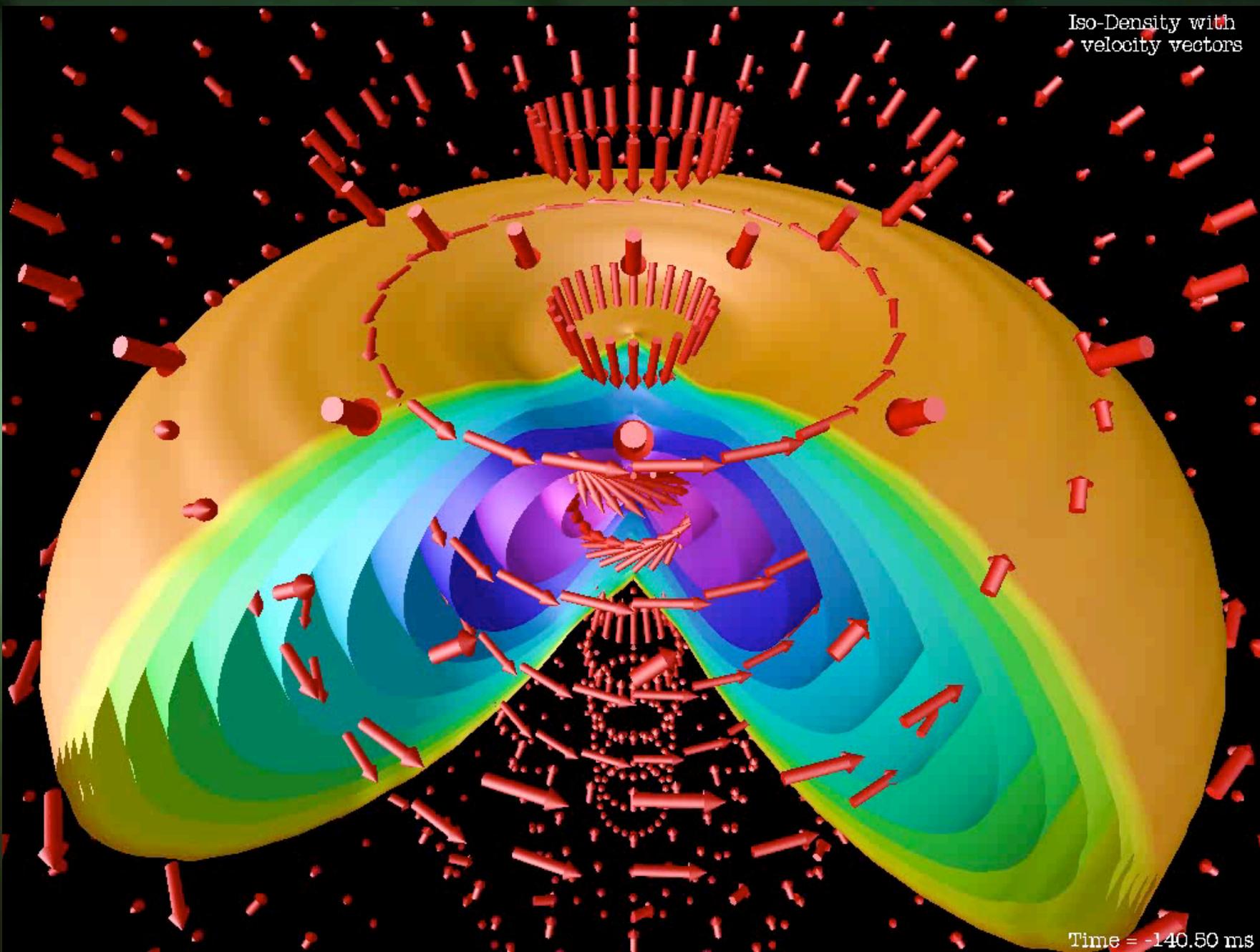
AIC: 1.92 solar masses:

Entropy

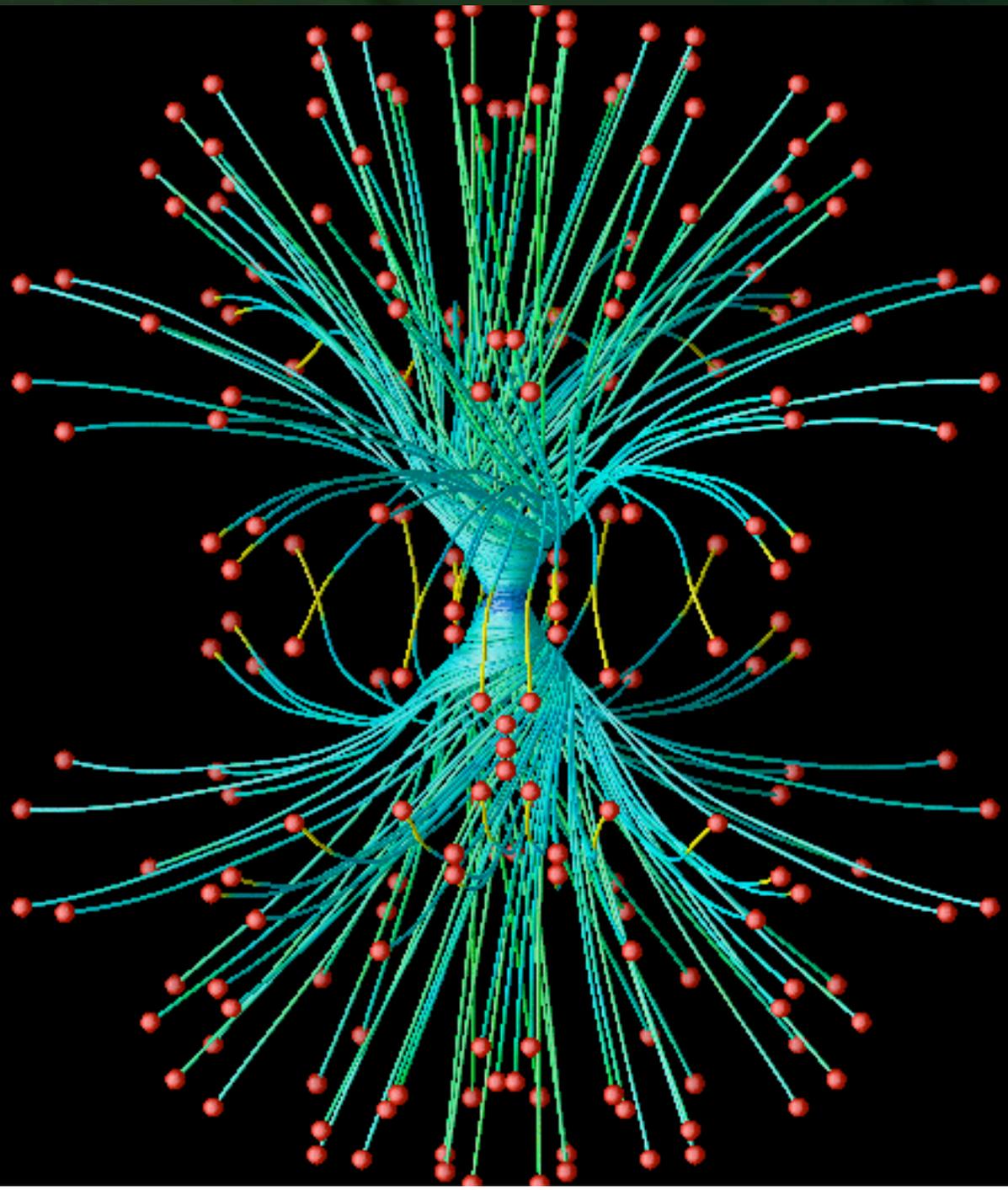


$t = -67.00$  ms

Iso-Density with  
velocity vectors

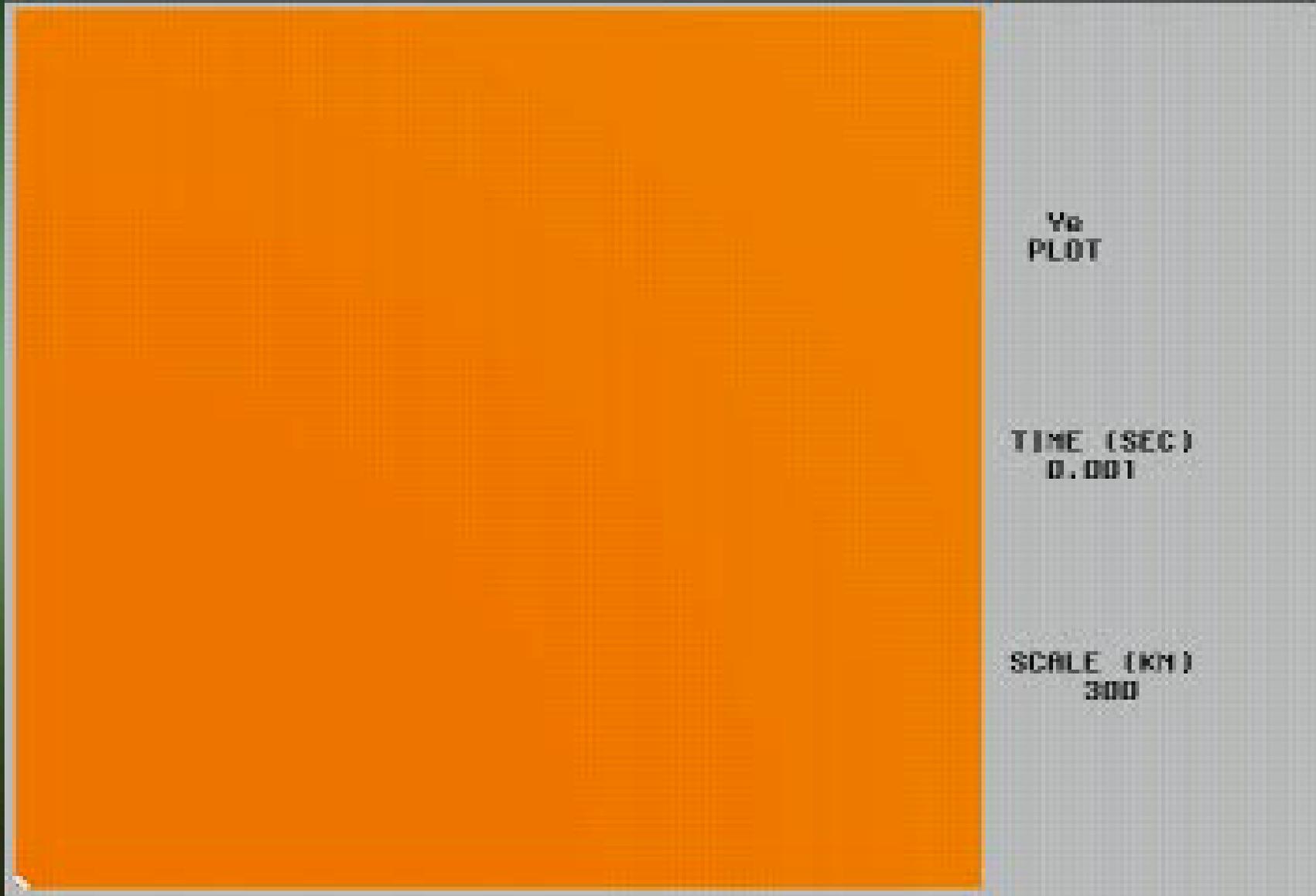


Time = -140.50 ms



*2D Radiation-Hydro  
Simulations  
of Massive-star Core  
Collapse*

BURROWS, HAYES, & FRYXELL (1995)



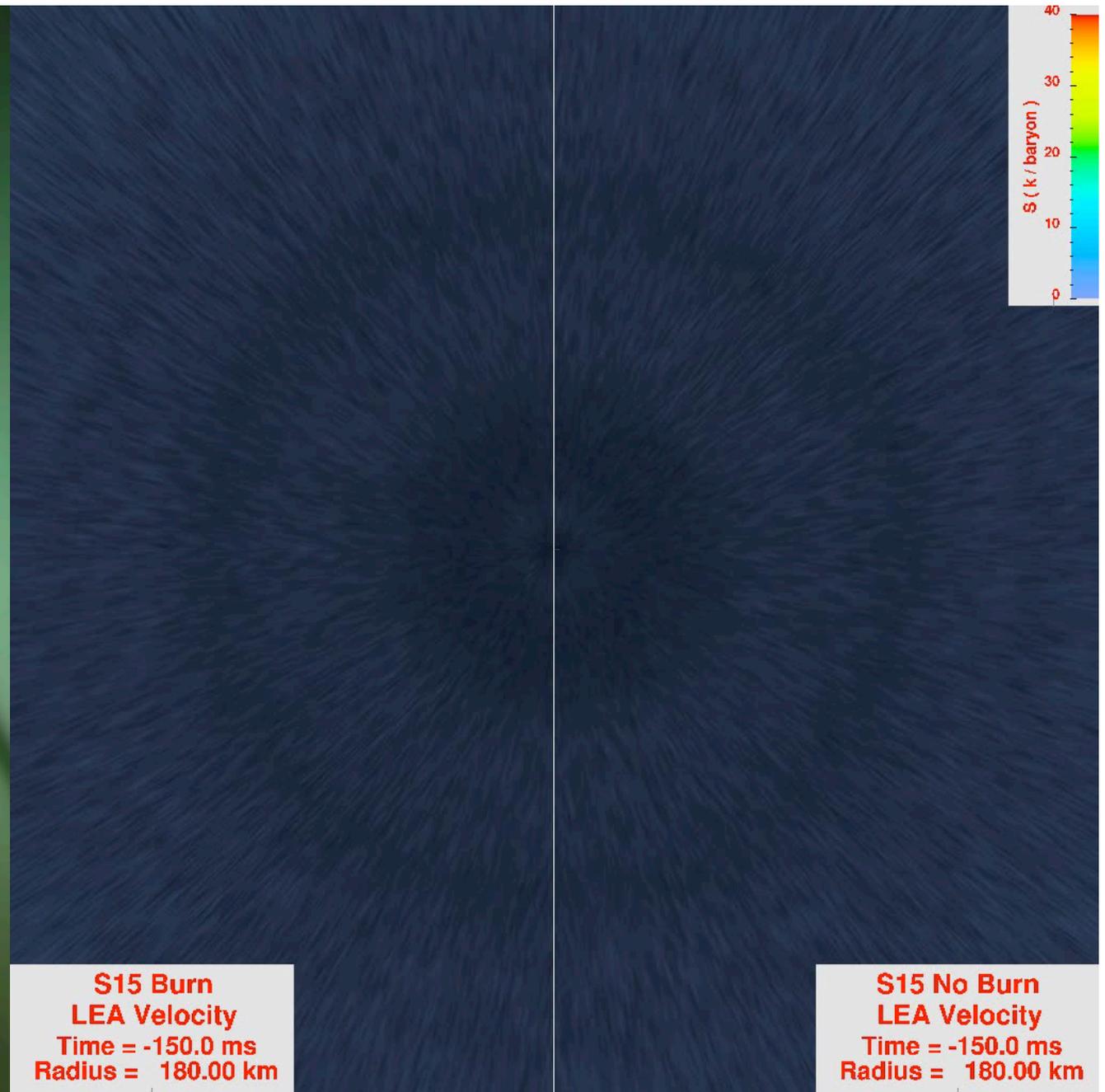
Neutrino-driven Convection (on a 90° wedge); Terminal PNS wind

## *VULCAN/2D Multi-Group, Multi-Angle, Time-dependent Boltzmann/Hydro (6D)*

- Only code with multi-D transport used in supernova theory
- Arbitrary Lagrangian-Eulerian (ALE); remapping
- 6 - dimensional (1(time) + 2(space) + 2(angles) + 1(energy-group))
- Moving Mesh, Arbitrary Grid; Core motion (kicks?)
- 2D multi-group, multi-angle,  $S_n$  (~150 angles), time-dependent, implicit transport (still slow)
- 2D MGFLD, rotating version (quite fast)
- Poisson gravity solver
- Axially-symmetric; Rotation
- MHD version ("2.5D") -  $\text{div } \mathbf{B} = 0$  to machine accuracy; torques
- Flux-conservative; smooth matching to diffusion limit
- Parallelized in energy groups; almost perfect parallelism
- Livne, Burrows et al. (2004,2007a)
- Burrows et al. (2006,2007b), Ott et al. (2005,2008); Dessart et al. 2005ab,2006

# Neutrino-driven Convection-SASI in 2D

$\nu$ -driven  
convection  
dominates (e.g.,  
see Fernandez and  
Thompson 2009)

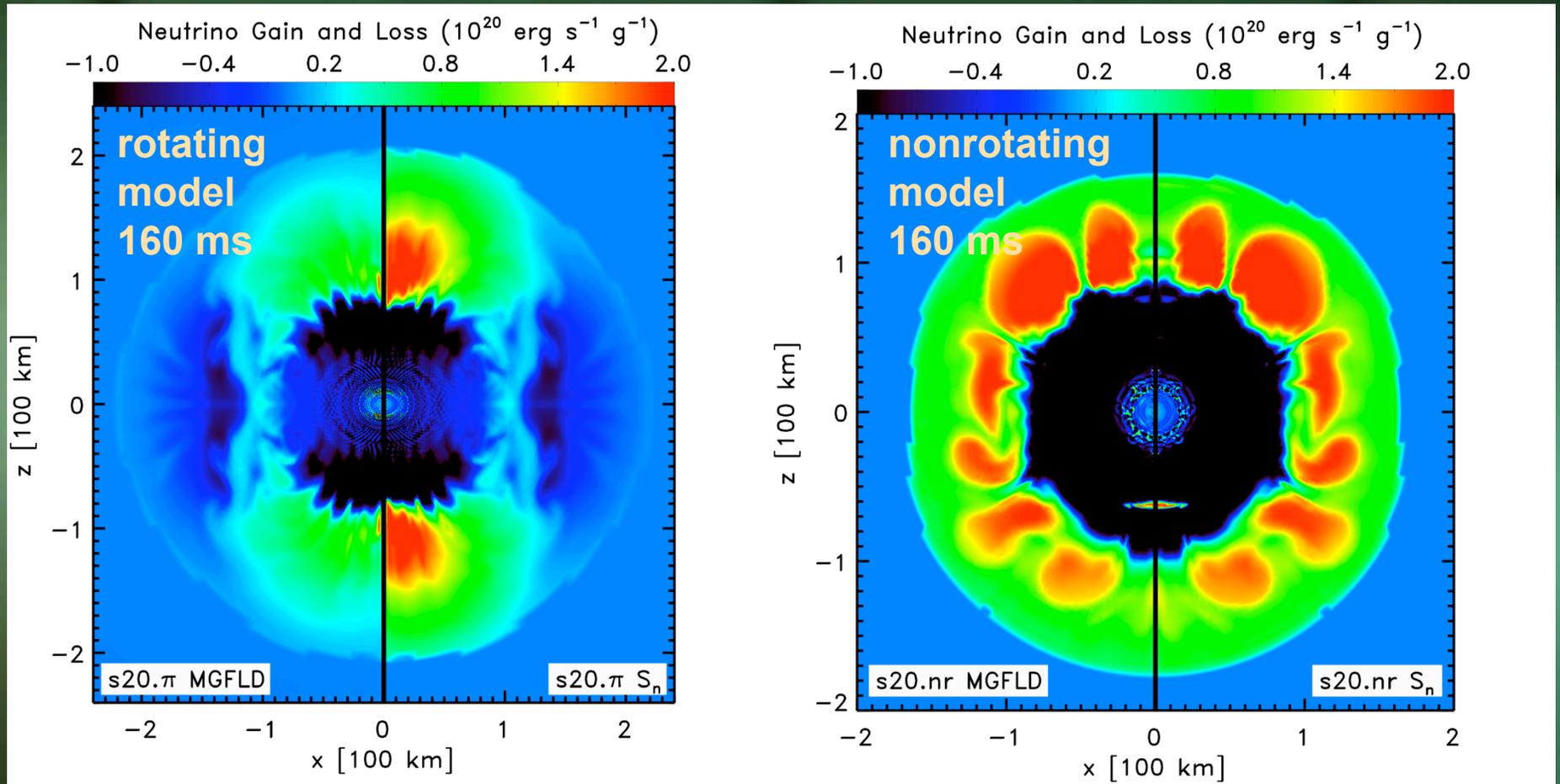


With and Without Burning

*Multi-Angle, Multi-  
group, Time-  
Dependent Transport  
in 2D SN Simulations*

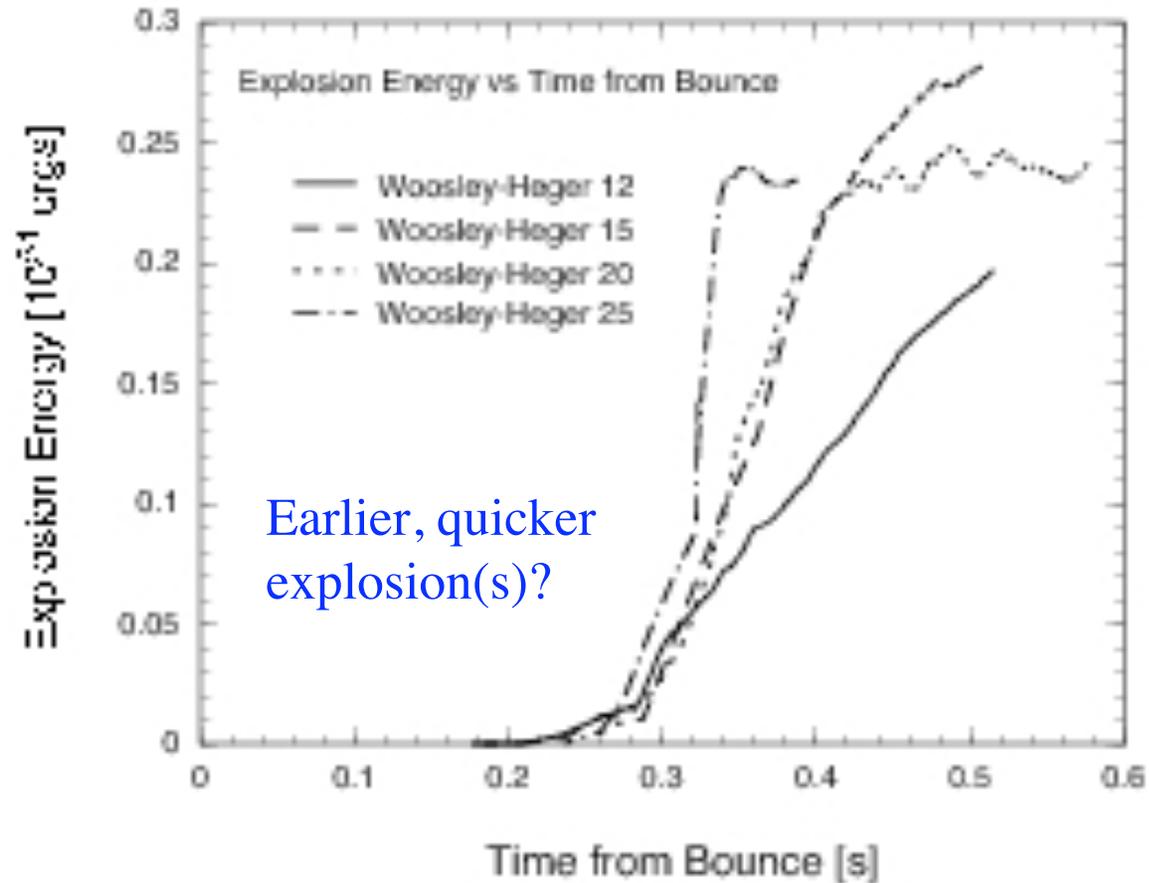
Ott et al. 2008

# Neutrino Energy Deposition



- s20.nr: Little difference between MGFLD and  $S_n$  at 160 ms after bounce.
- s20. $\pi$ : Large (factor  $\sim 3$ ) polar differences in specific heating rates.
  - (only  $\approx 2\%$  difference;  $S_n$  gain  $<$  MGFLD gain!)

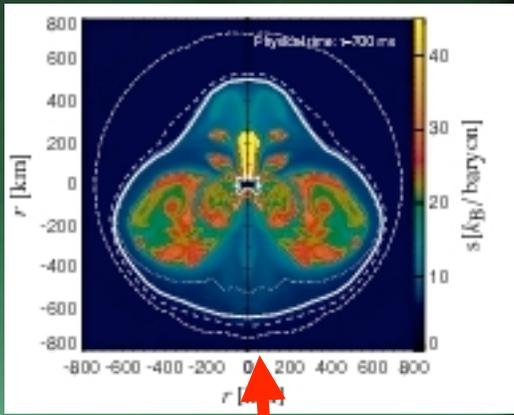
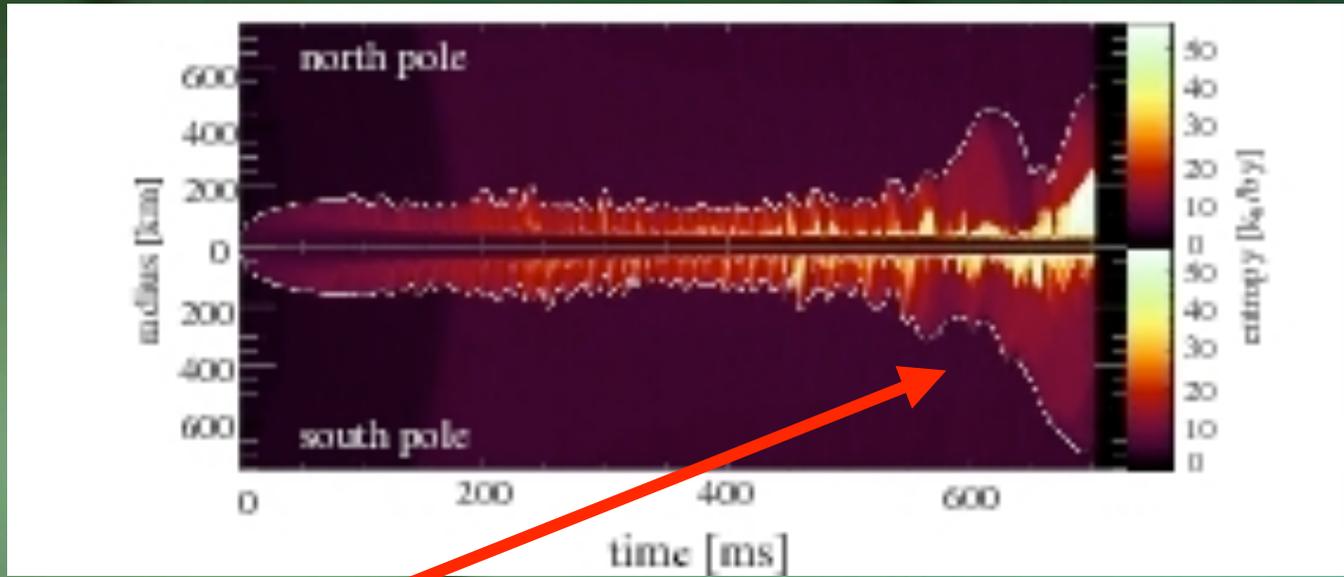
Bruenn, Mezzacappa et al. 2009 with soft EOS, 1D “ray-by-ray” transport, 2D Hydro:



What is the difference?, What's new? Inelastic scattering?!, nuclear burning? ...

FIGURE 3. Explosion energies as a function of post-bounce time.

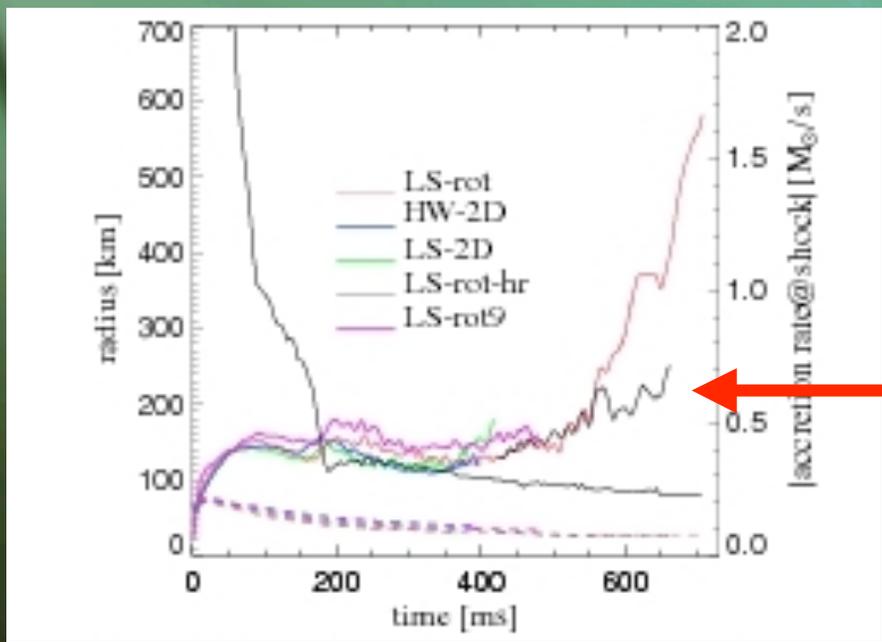
Marek & Janka 2009: 15 solar-mass model with soft (180 MeV) EOS, 1D  
 “ray-by-ray” transport, 2D hydro:



Long delay, weak explosion (?)

Higher-resolution, stiffer EOS - don't explode??

GR?

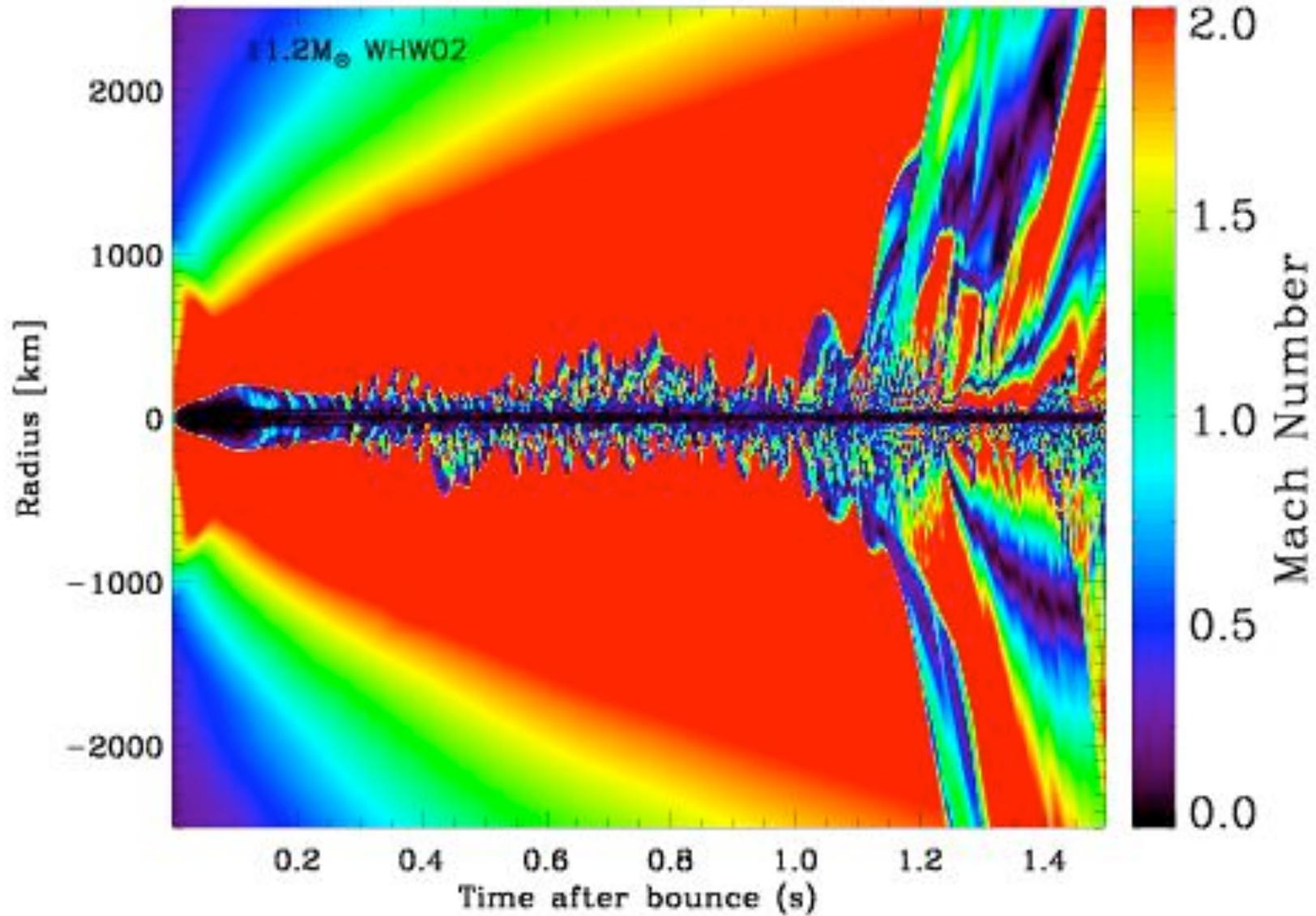


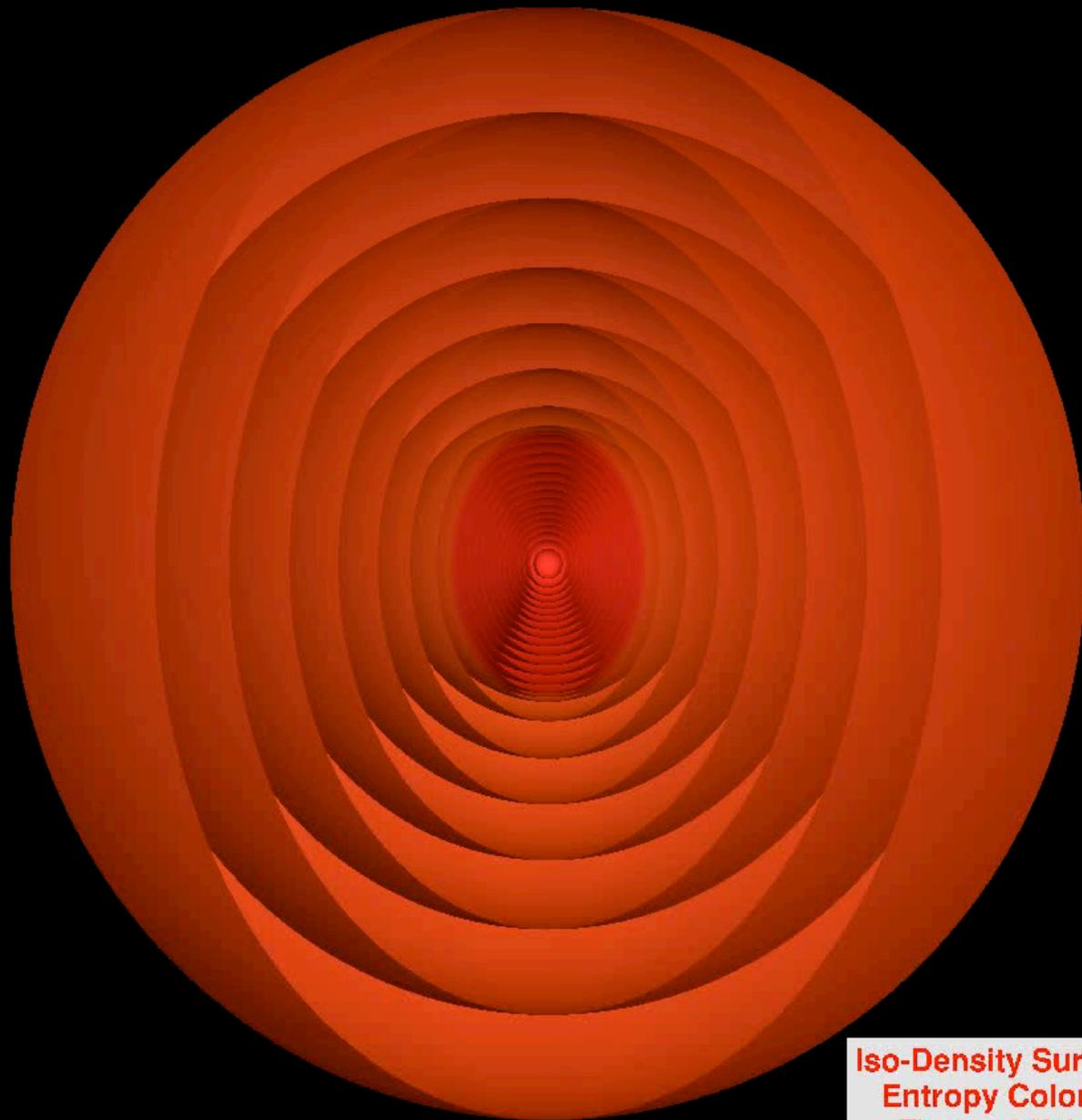
$R_{\text{shock}}$  to ~600 km

Higher-resolution. Smaller radius

*Core Oscillation/Acoustic  
Power Mechanism*

# Mach Number along axis versus Time





**Iso-Density Surfaces**  
**Entropy Coloring**  
Time = -140.0 ms  
Radius = 6000.00 km

## *Limitations of the VULCAN/2D Simulations*

- Doppler shift terms not included in transport
- Inelastic redistribution not included (though subdominant), though could be
- Not GR, no approximate correction
- No good development path to 3D
- Re Acoustic mechanism: Weinberg & Quataert ?

## *Limitations of the ORNL Simulations*

- Transport in 1D (“ray-by-ray”): Not Multi-D
- Soft (180 MeV) Nuclear EOS (but measurements?)
- Energy conservation to only  $\sim 0.5$  Bethes
- Core must stay at grid center (kicks?, acoustic mechanism?)
- Role of Nuclear Burning at Shock?
- Large Stalled Shock Radius ?

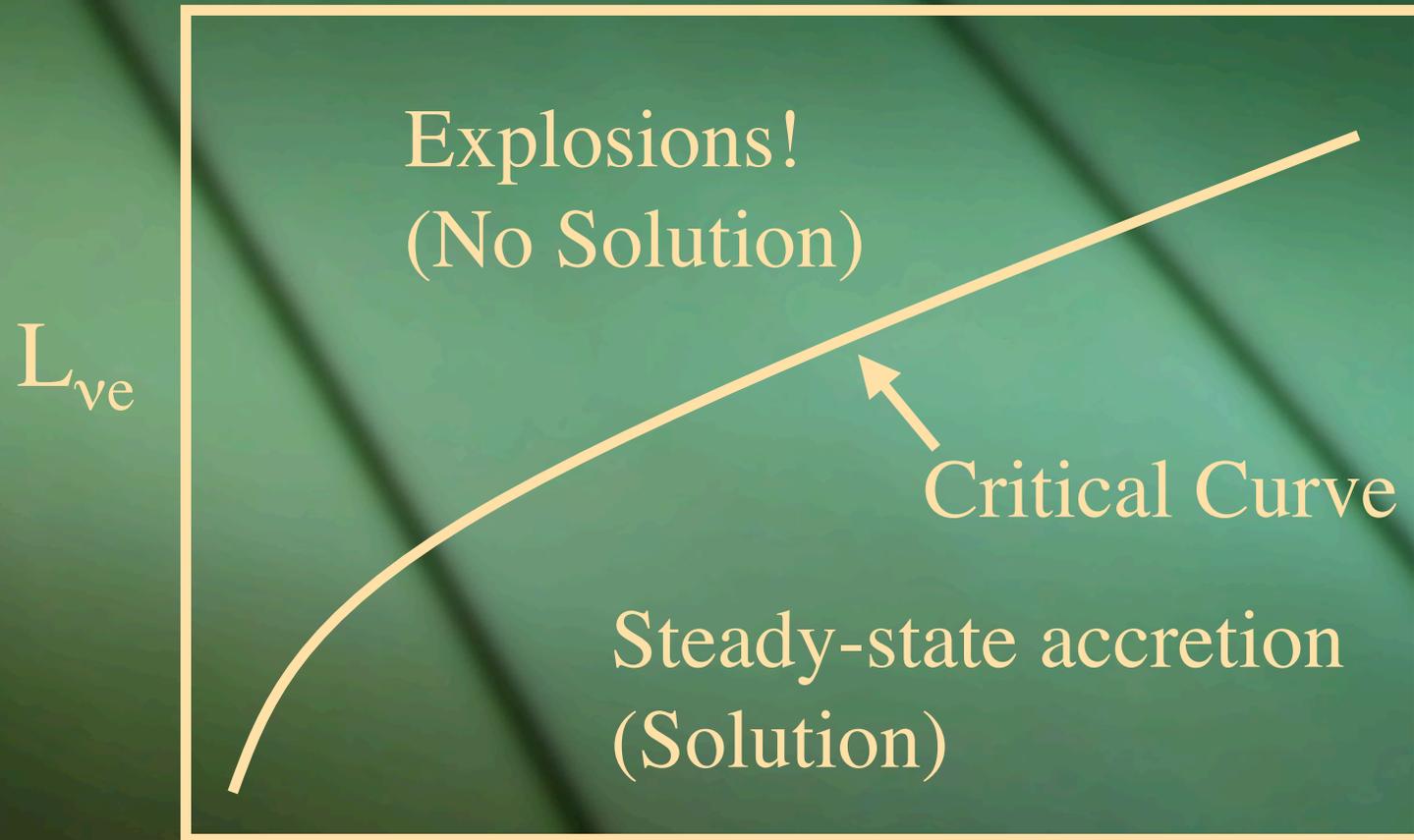
## *Limitations of the MPIA Simulations*

- Transport in 1D (“ray-by-ray”): Not Multi-D
- Soft (180 MeV) Nuclear EOS (but measurements?)
- Core must stay at grid center (kicks?, acoustic mechanism?)
- (ORNL and MPIA 15-solar-mass explosion simulations very discrepant)

*2D Radiation-Hydro  
Simulations*

*Verdict: Marginal,  
Ambiguous, at best  
(but 3D....?)*

Burrows & Goshy '93; **Murphy & Burrows 2008**  
**Critical Condition** for Neutrino Mechanism:  
Dimension-dependent



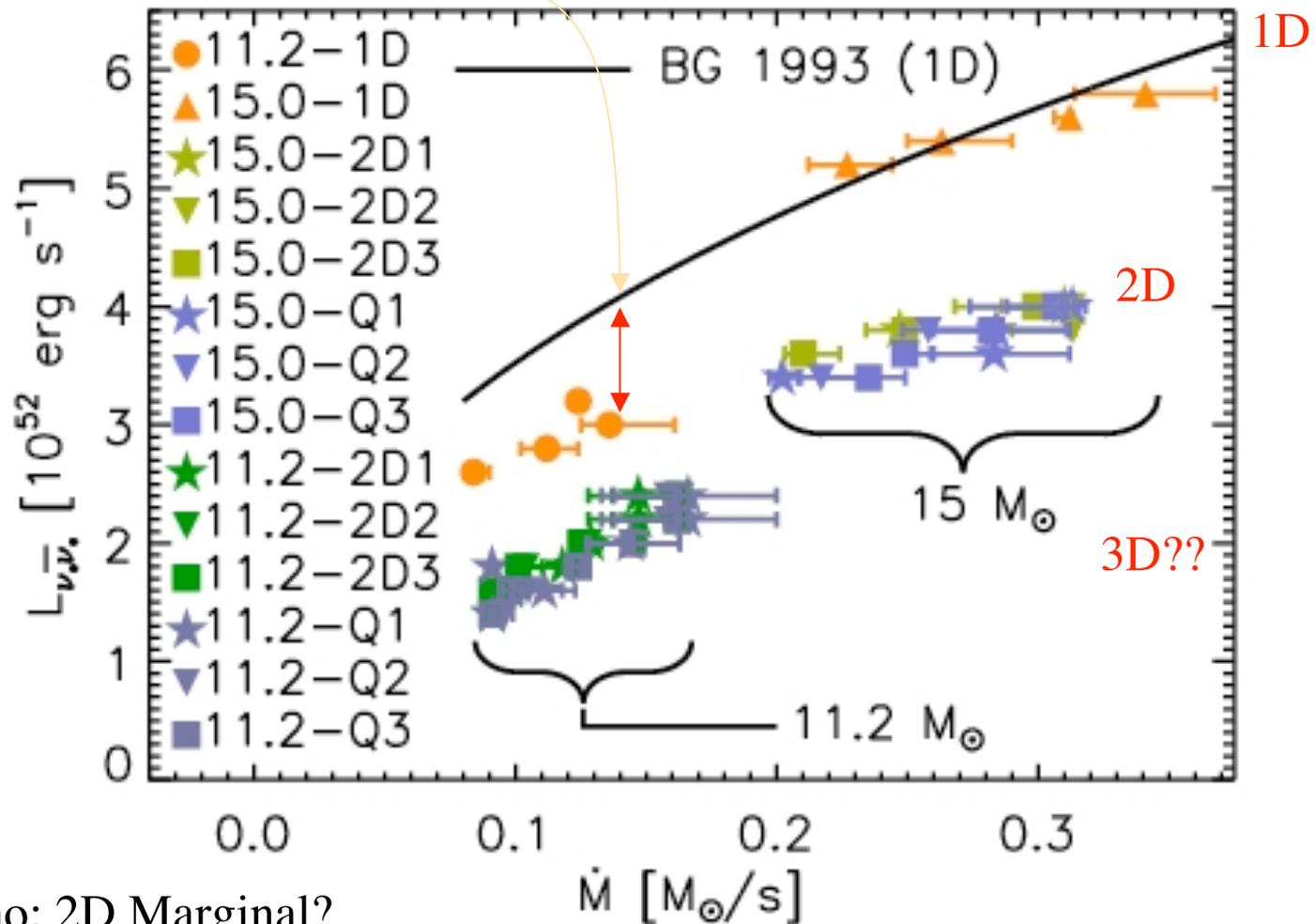
$\dot{M}$

$L_{\nu}$  vs. Accretion Rate Parameter Study

*How do the critical luminosities differ between 1D and 2D?*

# Critical Curve for Neutrino Mechanism: 1D versus 2D

Different mass cores



See Jeremiah's poster!

Murphy & Burrows 2008

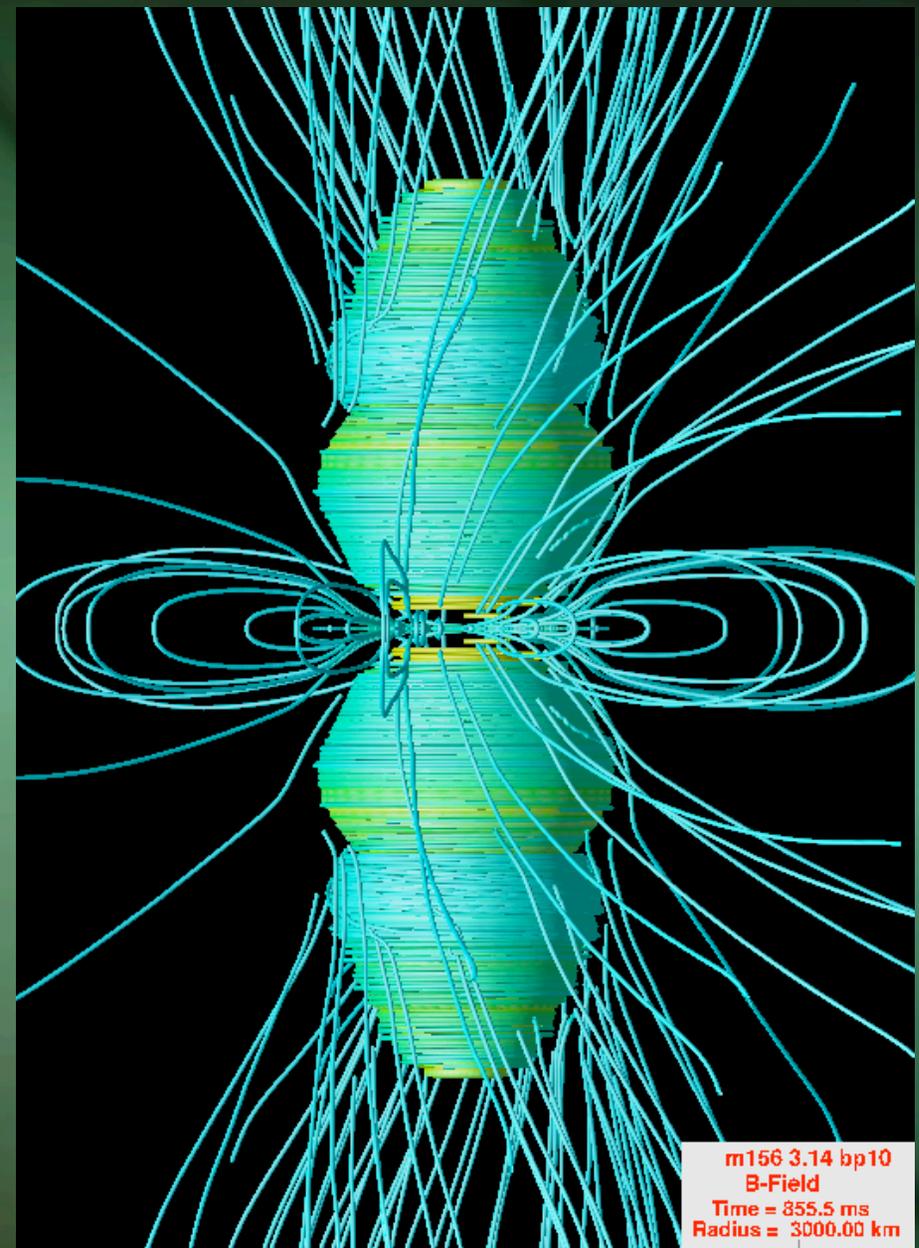
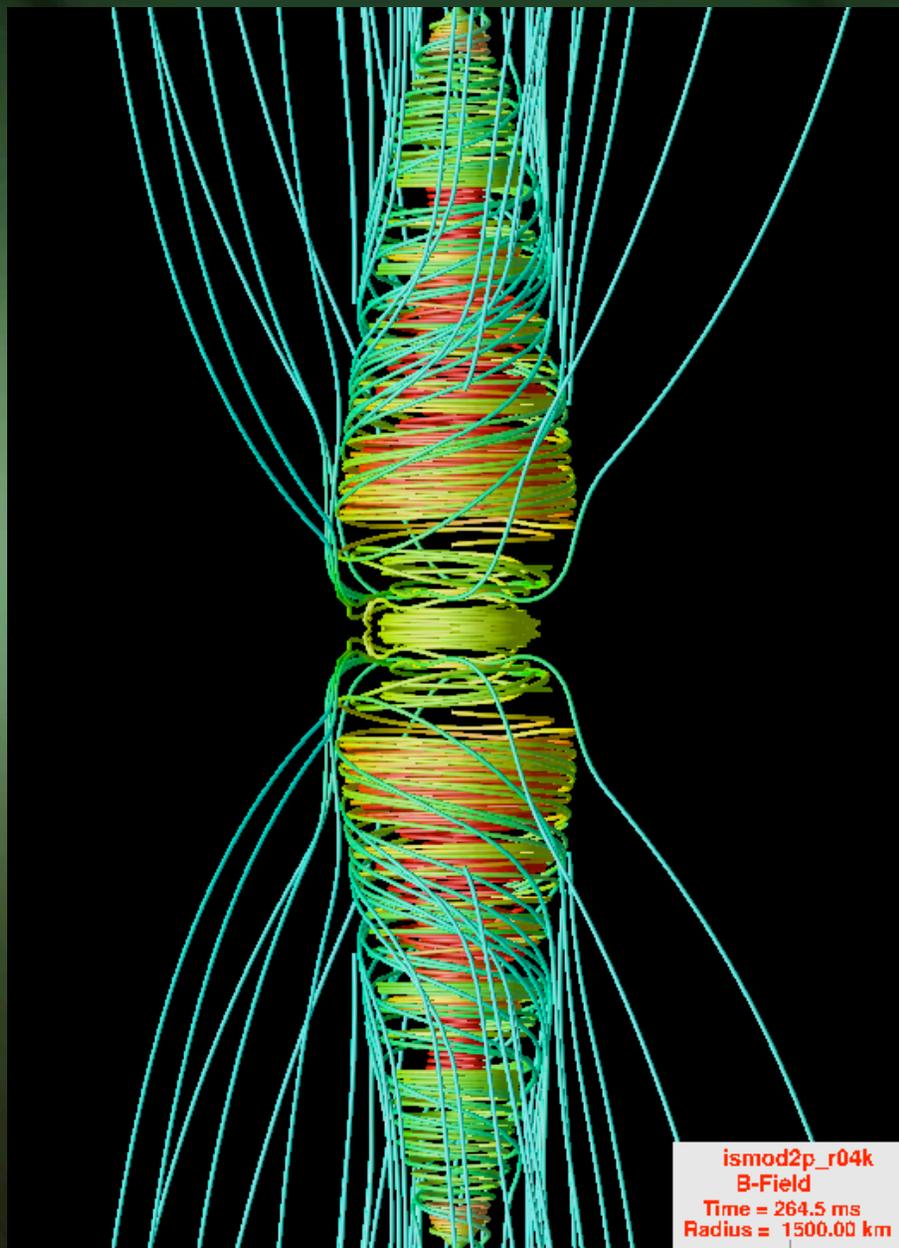
# Some Myths of Core-Collapse Theory

- “The supernova is a sensitive, 1%, phenomenon”
- “Every detail makes a difference to the viability of the mechanism”
- “The SASI is new and trumps neutrino-driven convection”
- “Neutrino-electron and neutrino-nucleon scattering is important”
- “The ‘Hot Bubble’ has an entropy of  $\sim 300$ ”
- “Details of the Nuclear EOS make a difference(?)”
- “MHD is required to explain polarization or imaged asymmetries”
- “Jets?”
- “Collapse can lead directly to a black hole”
- “ $\nu / \bar{\nu}$  annihilation to  $e^+/e^-$  pairs is an important heat source”
- “There is a puzzle with pulsar spins”
- “SASI  $l=1$  in 3D?”
- “Other groups have tested the acoustic mechanism”

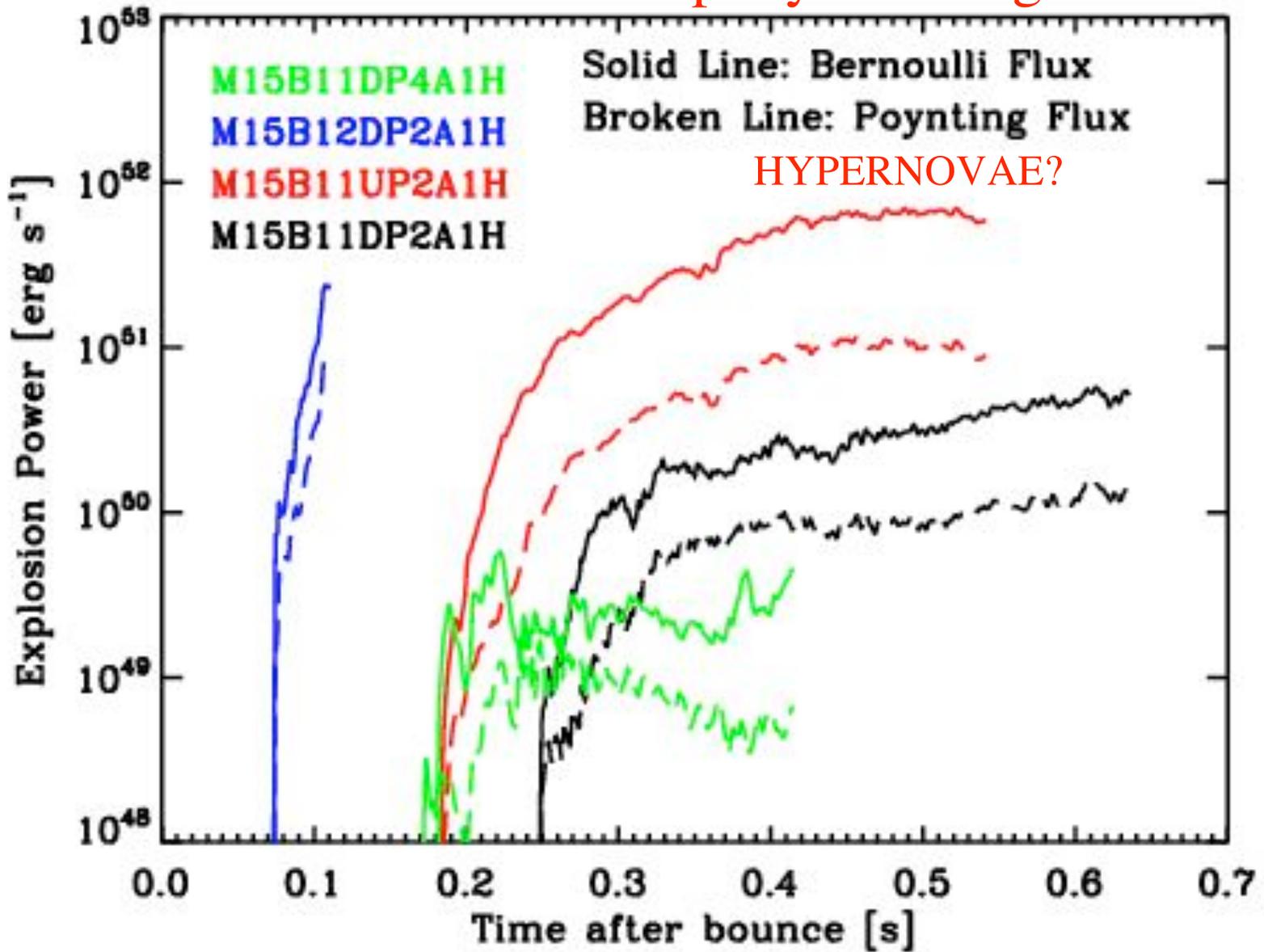
*MHD Jets and RMHD  
Simulations of Core  
Collapse: Rapid Rotation  
Required*

Burrows, Dessart, Livne, Ott, & Murphy 2007; Dessart  
et al. 2007

Rotation Winding, the MRI and B-field Stress effects

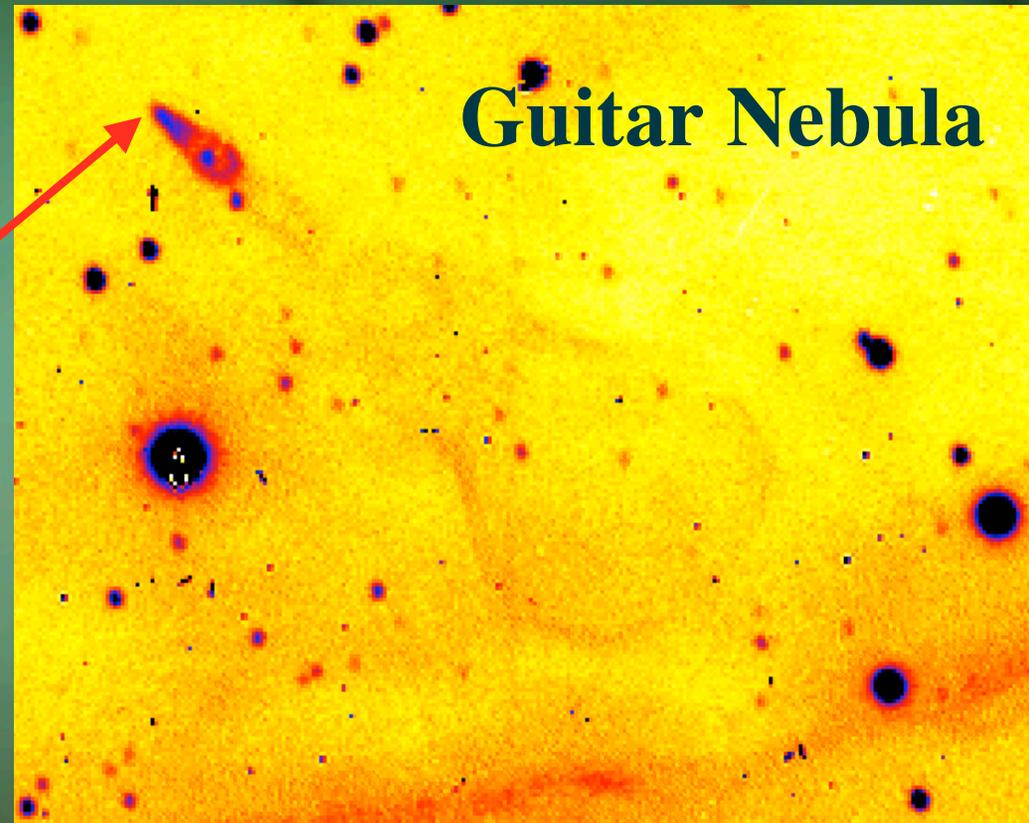


## MHD Jet Powers for Rapidly-Rotating Cores



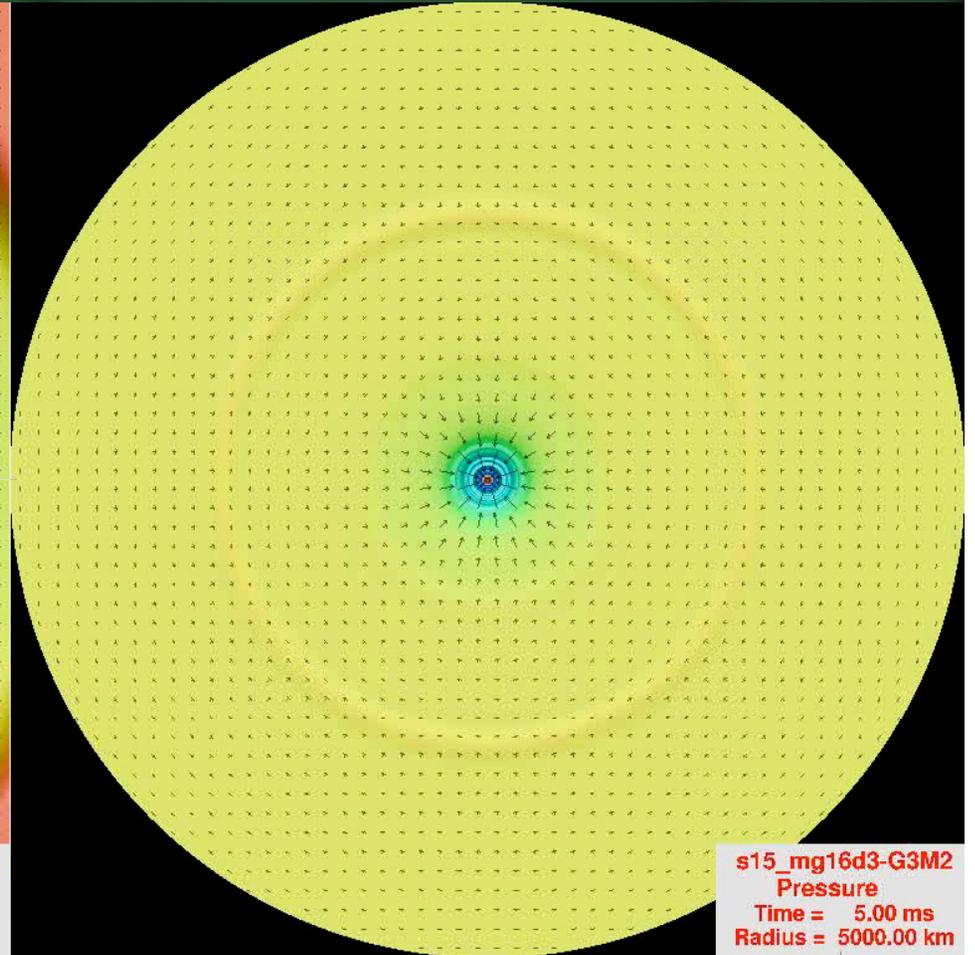
# *Pulsar Recoil: A Generic Feature*

Pulsar Kicks:  
Pulsar B2224+65  
and Bow Shock  
 $V \geq 1000 \text{ km s}^{-1}$



Cordes, Romani, Lundgren '93

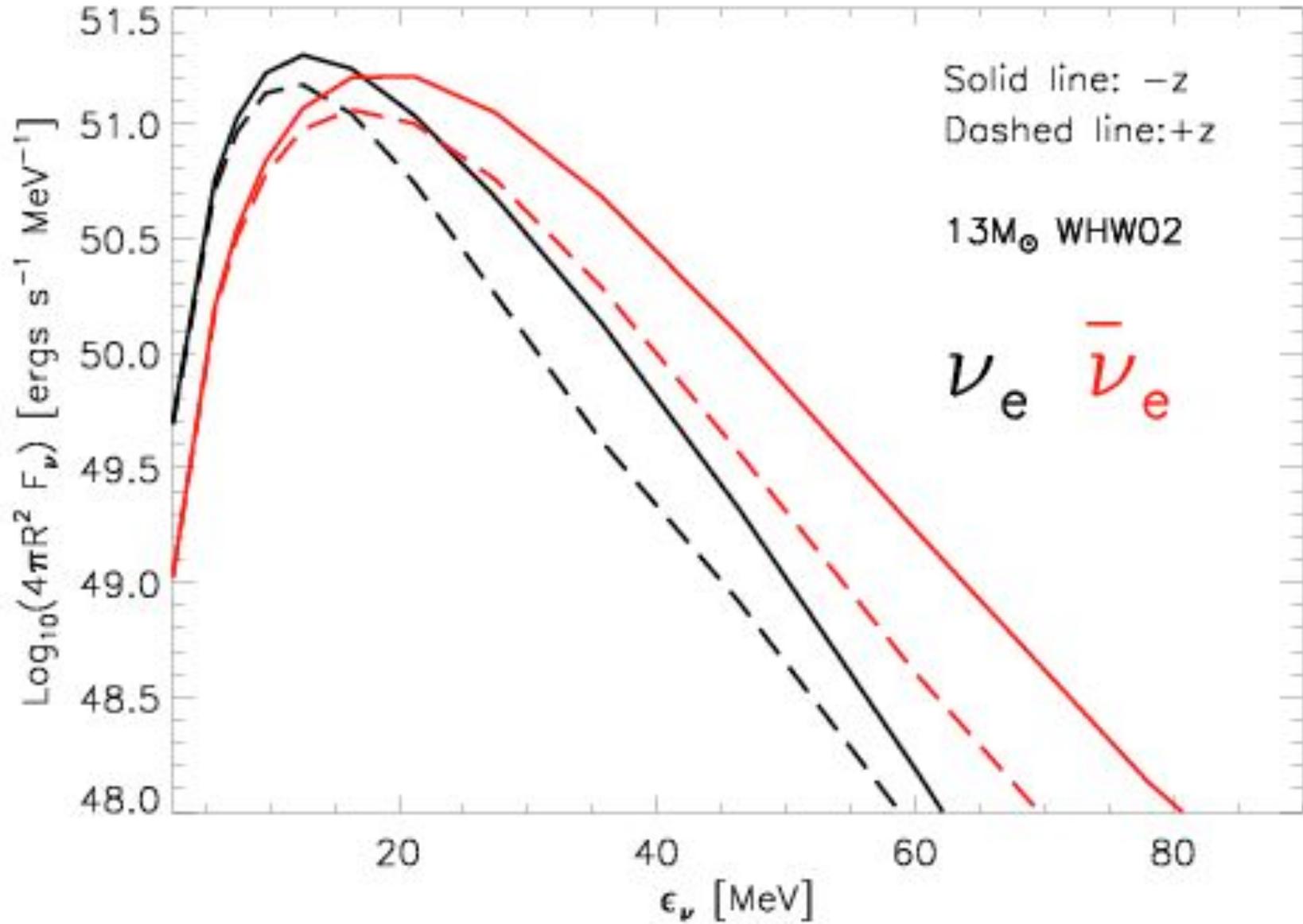
# The Origin of Pulsar Kicks in Hydrodynamic (and neutrino?) Recoil



Acceleration  $\sim 500 \text{ km/s}^2$

Nordhaus, Burrows, & Ott 2009

## Top-Bottom Asymmetry in Neutrino Luminosity after Explosion: Kicks!



# *3D - Crucial Next Step*

**CASTRO!**

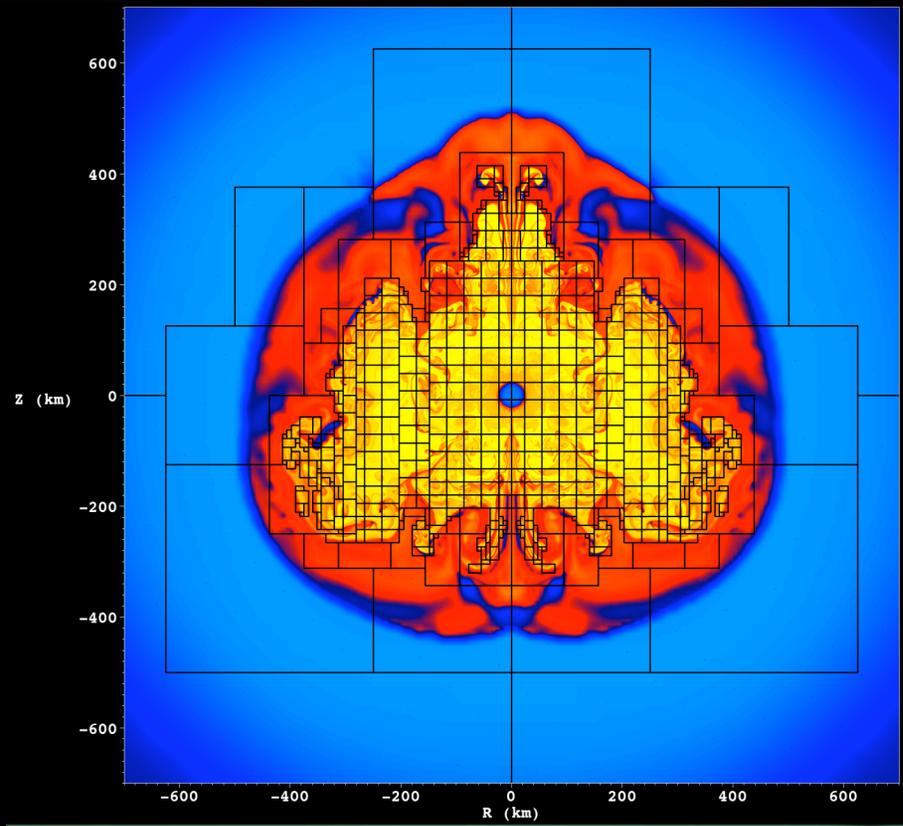
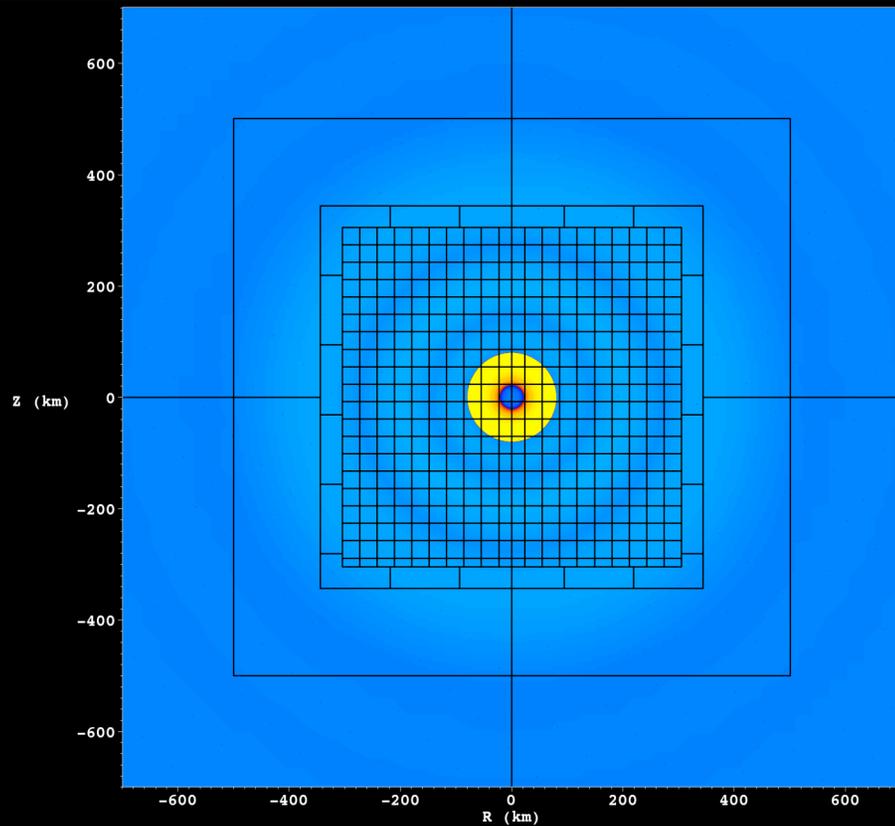
(J. Bell; A. Almgren; L. Howell; M.  
Singer; A. Burrows; J. Nordhaus)  
(Using a MGFLD variant of  
Hubeny/Burrows scheme)

See Jason Nordhaus' poster

# CASTRO - 3D AMR, Multi-Group Radiation-Hydrodynamic Supernova Code

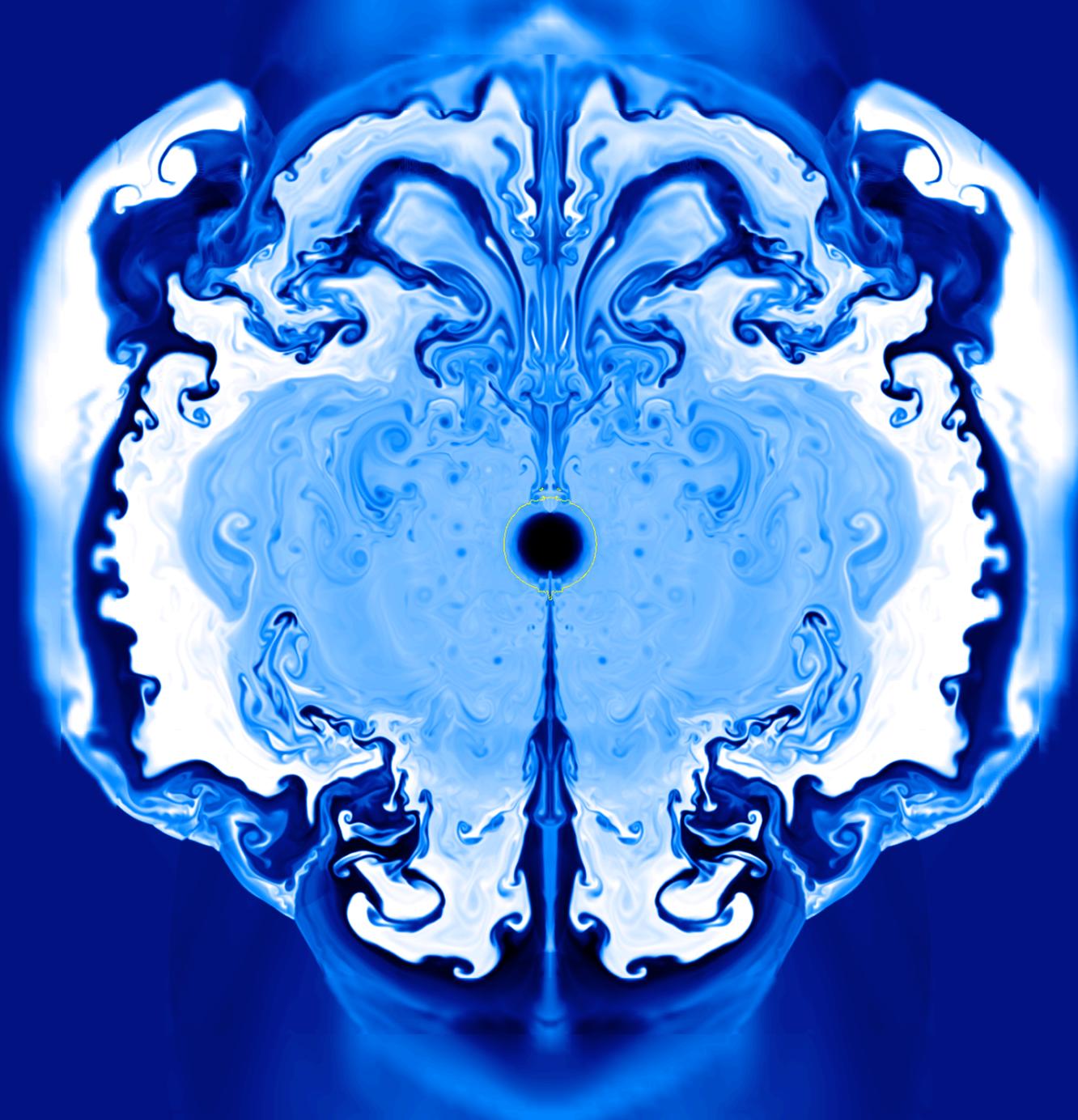
- 2nd-order, Eulerian, unsplit, compressible hydro
- PPM and piecewise-linear methodologies
- Multi-grid Poisson solver for gravity
- Multi-component advection scheme with reactions
- Adaptive Mesh Refinement (AMR) - flow control, memory management, grid generation
- Block-structured hierarchical grids
- Subcycles in time (multiple timestepping - coarse, fine)
- Sophisticated synchronization algorithm
- BoxLib software infrastructure, with functionality for serial distributed and shared memory architectures
- 1D (cartesian, cylindrical, spherical); 2D (Cartesian, cylindrical); 3D (Cartesian)
- Transport is a conservative implementation of mixed-frame method of Hubeny & Burrows (2007), with v/c terms and inelastic scattering
- Uses scalable linear solvers (e.g., hypre) with high-performance preconditioners that feature parallel multi-grid and Krylov-based iterative methods
- Developers: John Bell, Ann Almgren, Louis Howell, Mike Singer, Jason Nordhaus, Adam Burrows - LBNL, LLNL, Princeton

## Sample Block Grid Structures of CASTRO: Pre-collapse, Post-bounce

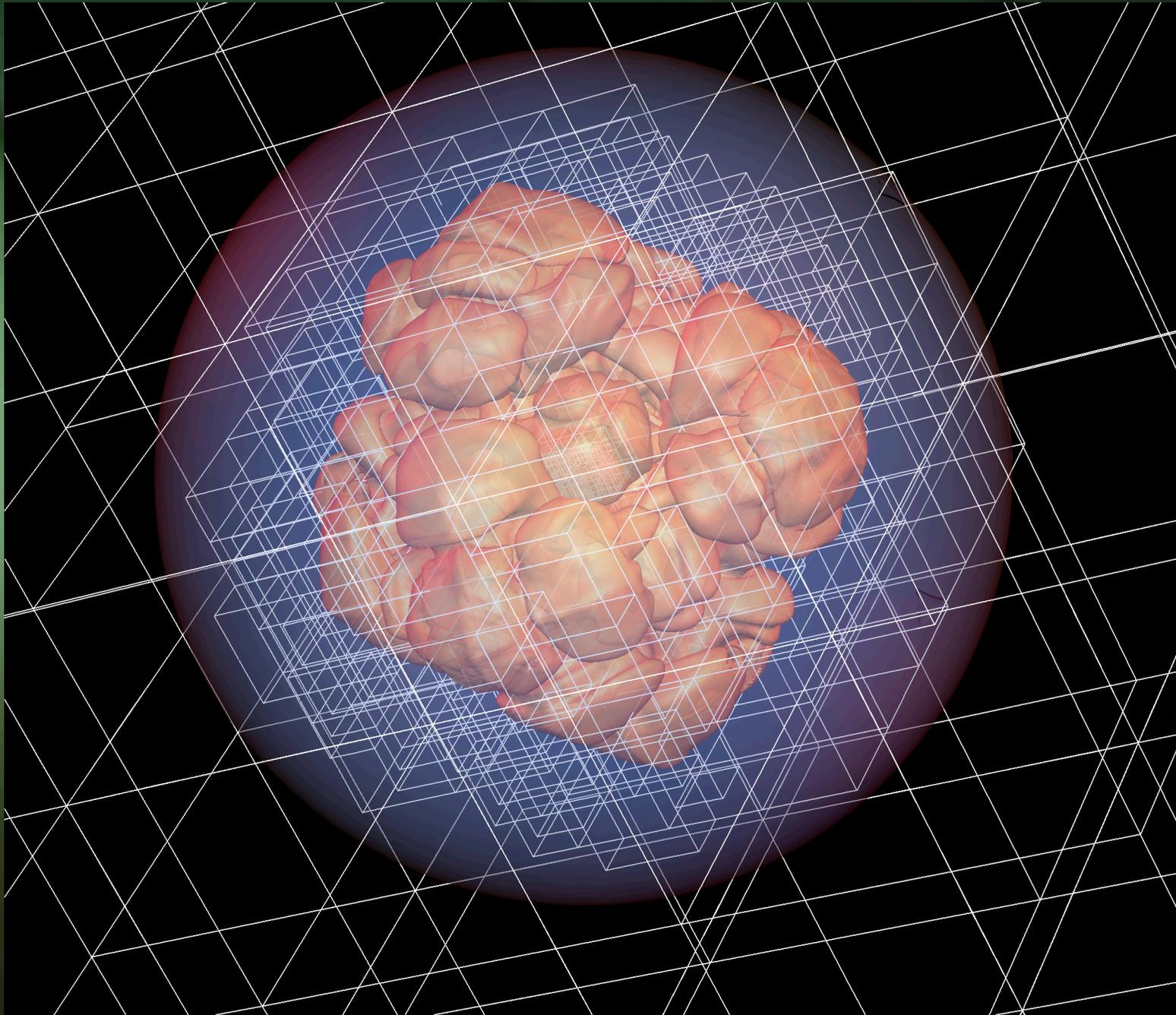


See Jason's poster!

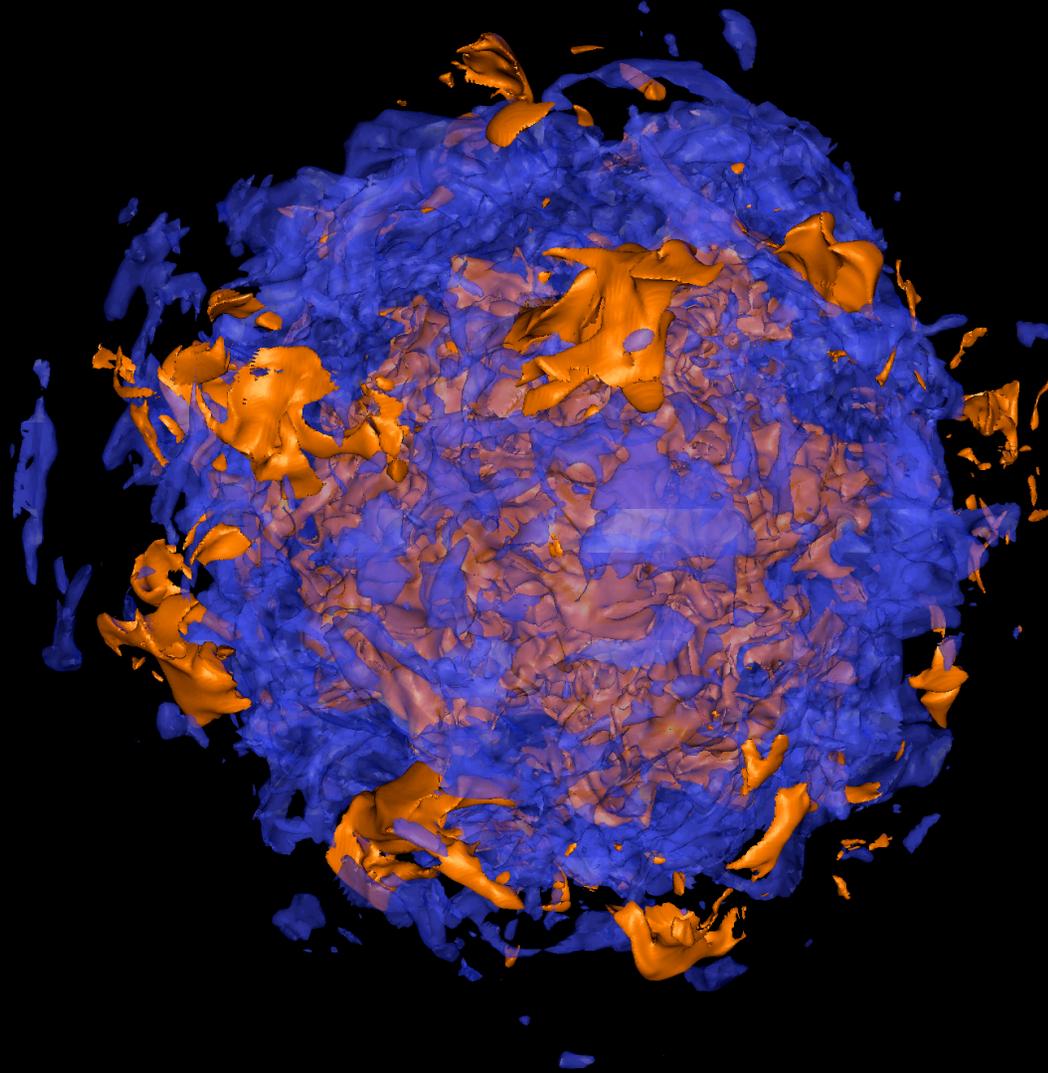
2D:



## CASTRO 3D AMR Mesh: Explosion Model



# CASTRO 3D AMR No-Explosion Model



# Entropy:

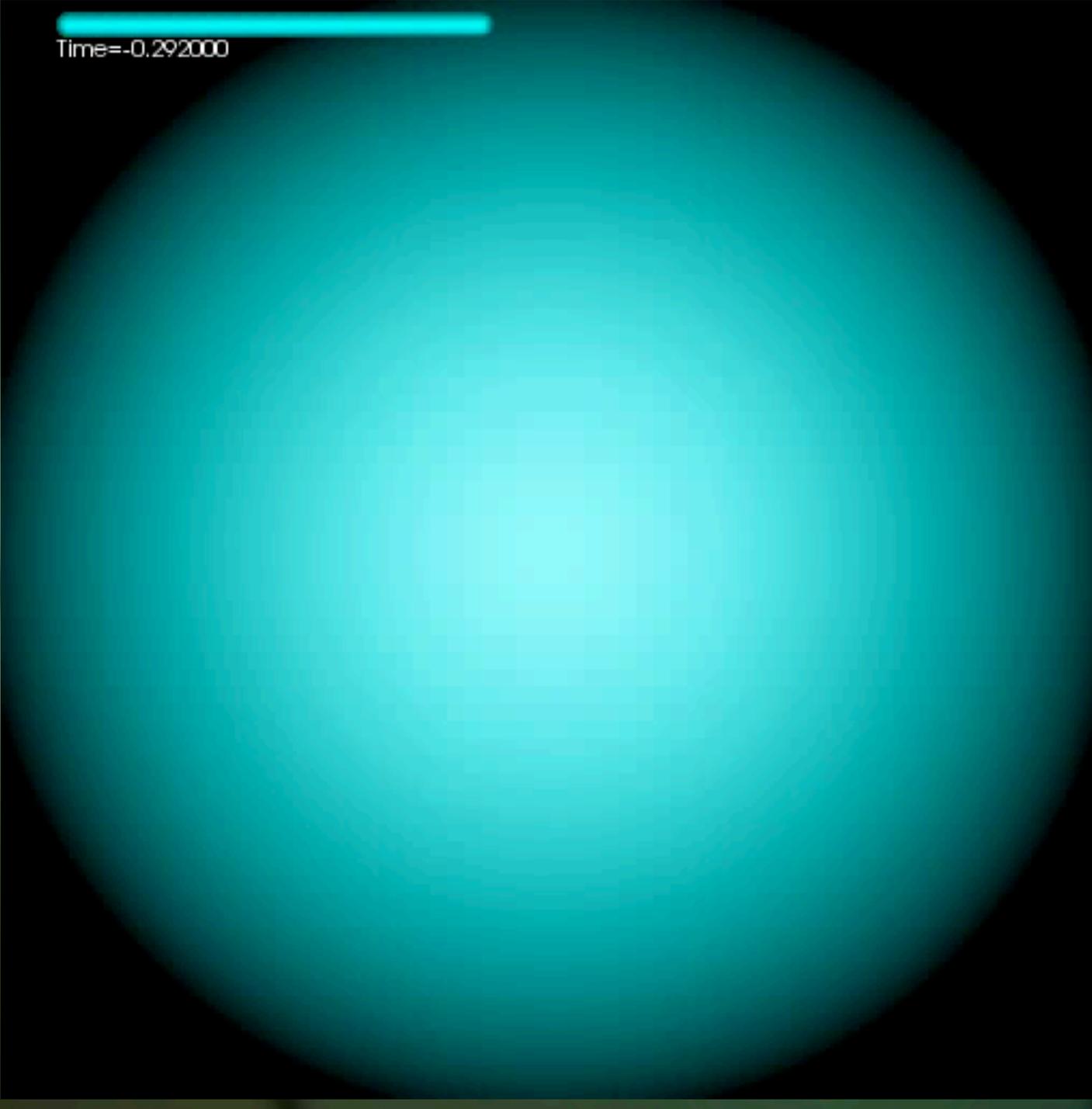
CASTRO 3D  
AMR Core-  
Collapse -- No  
Explosion  
Model

Little evidence  
of fast induced  
rotation; (see  
also Iwakami et  
al. 2009);

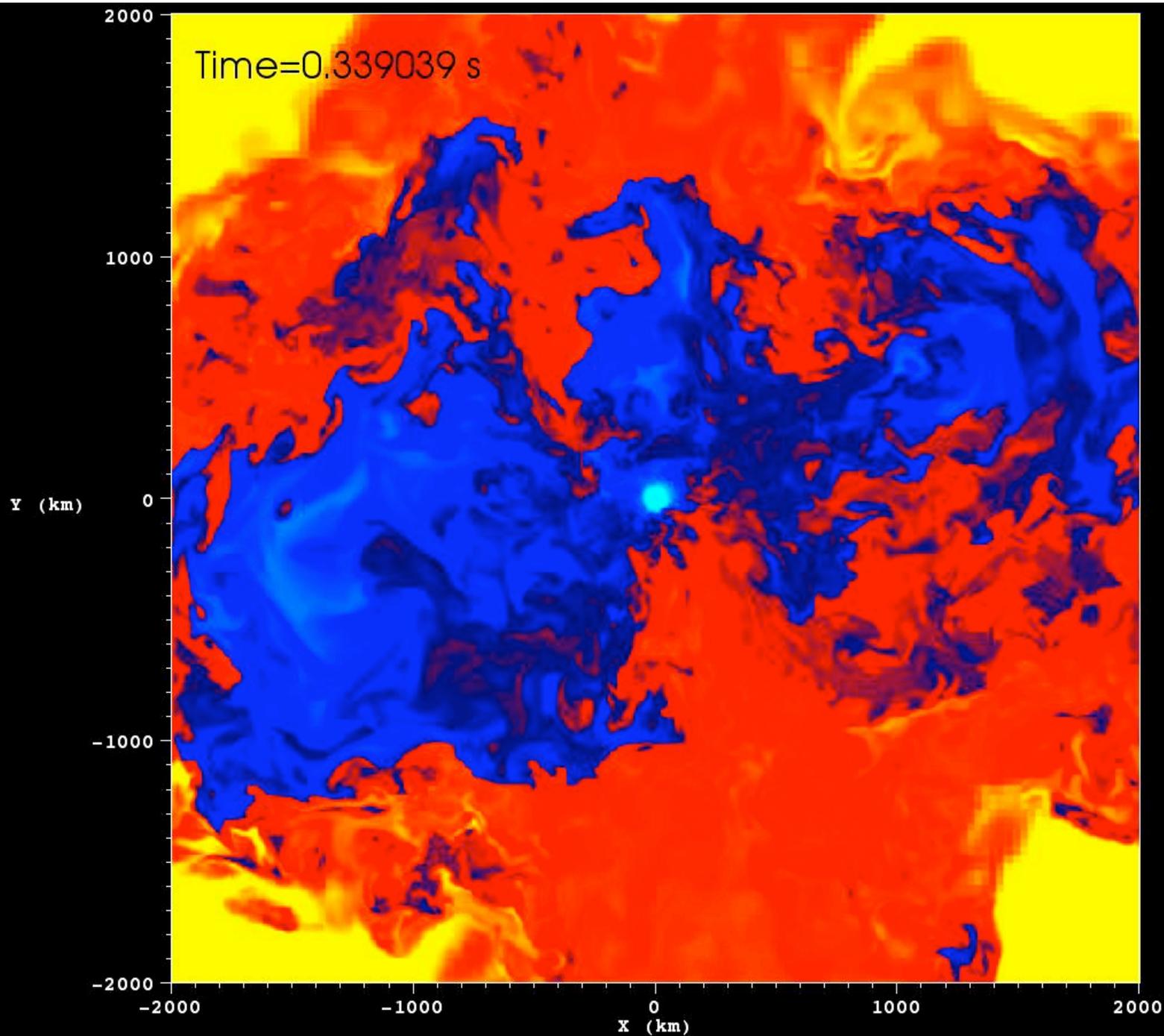
Blondin and  
Mezzacappa 2007?:

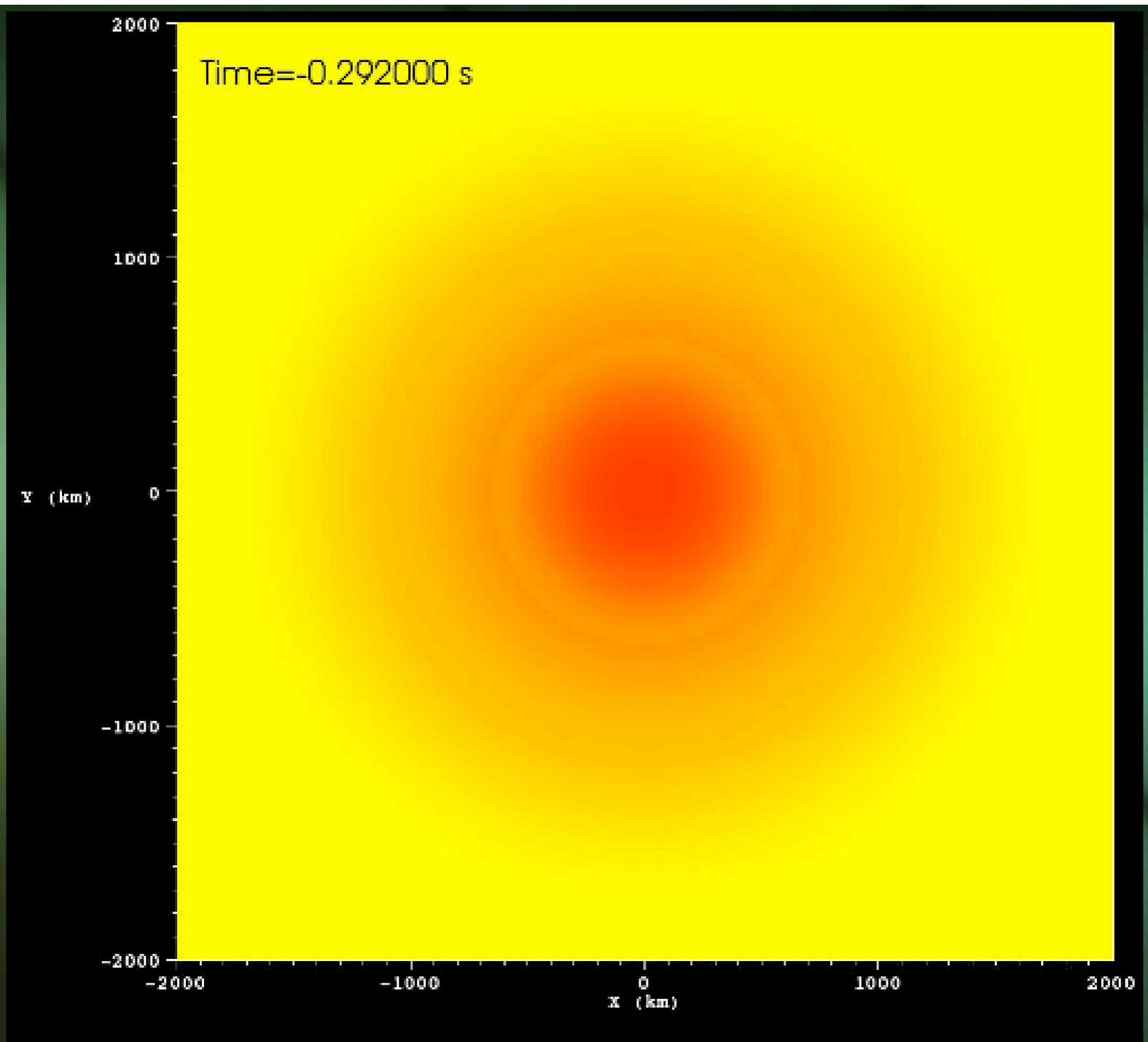
A bit of rotation  
(on the outside),  
but...

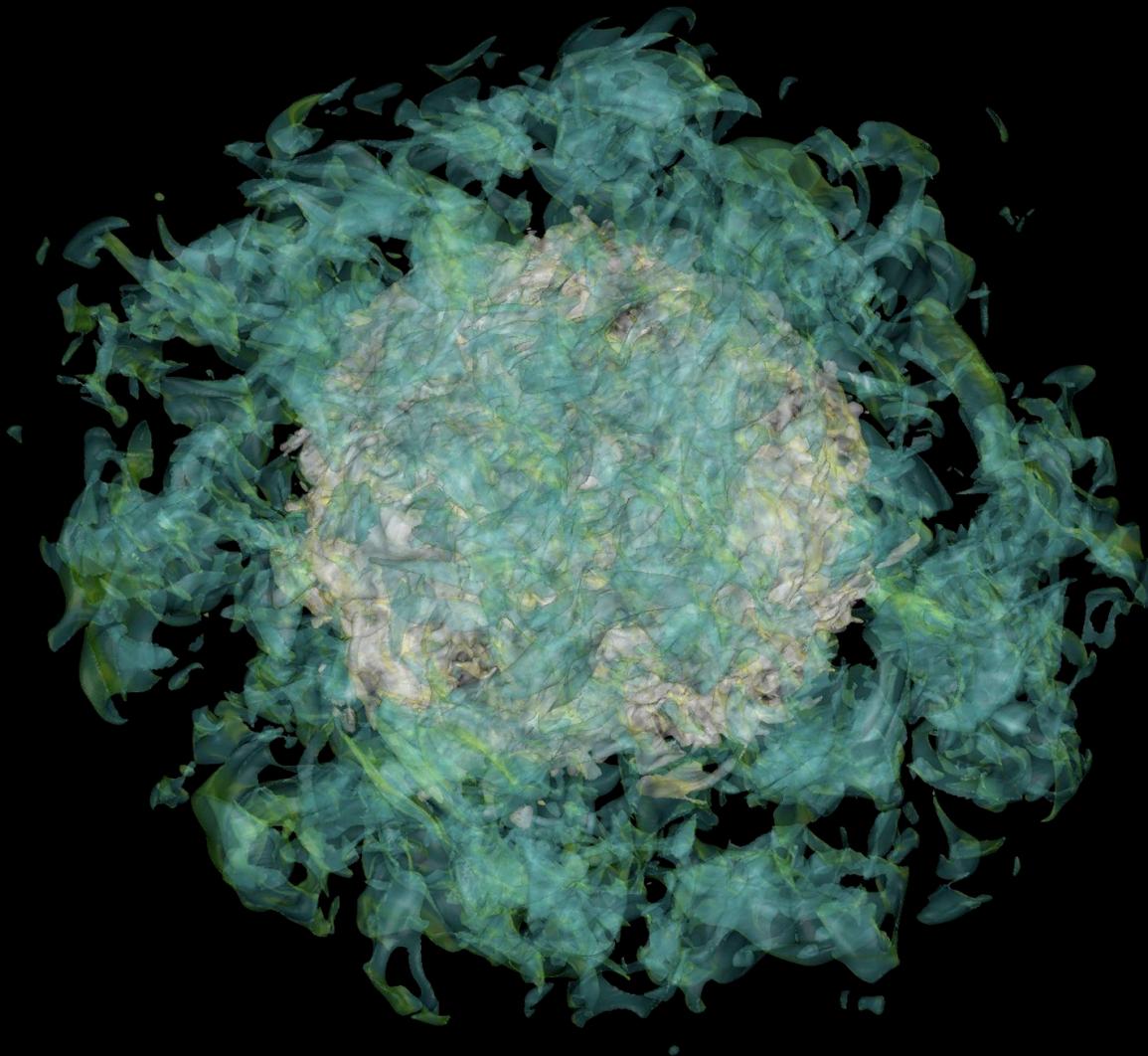
Time=-0.292000



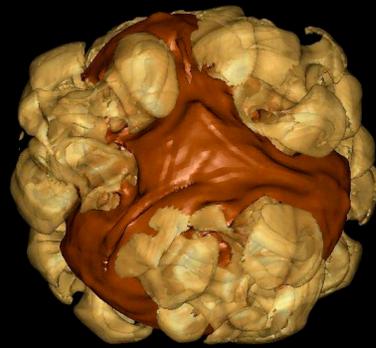
CASTRO 3D  
AMR Core-  
Collapse --  
Explosion  
Model

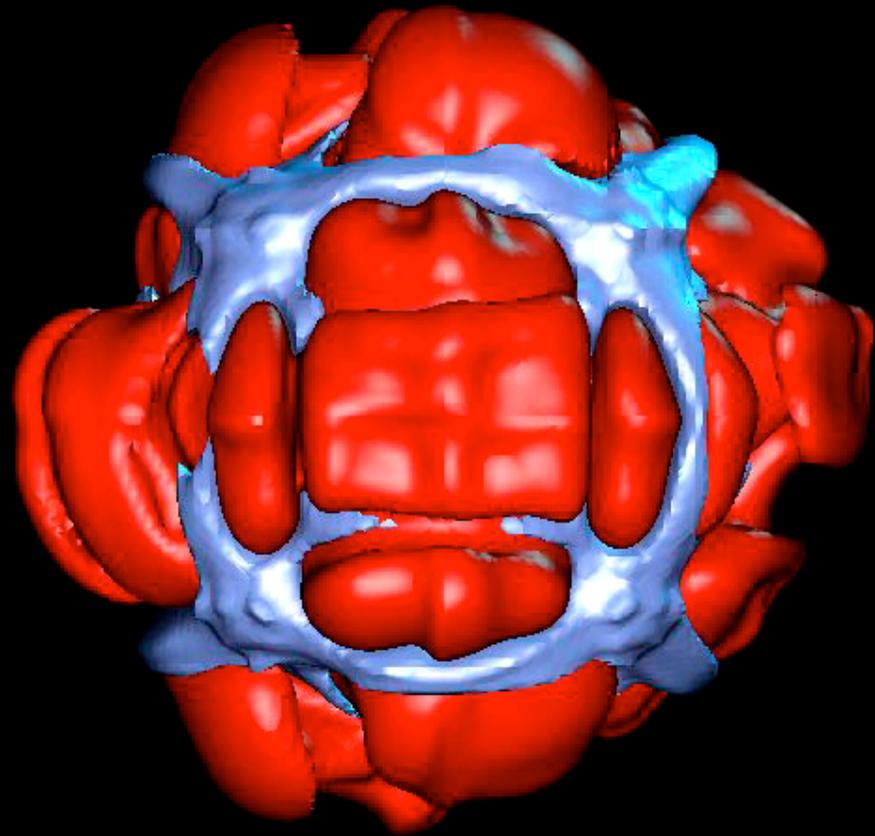


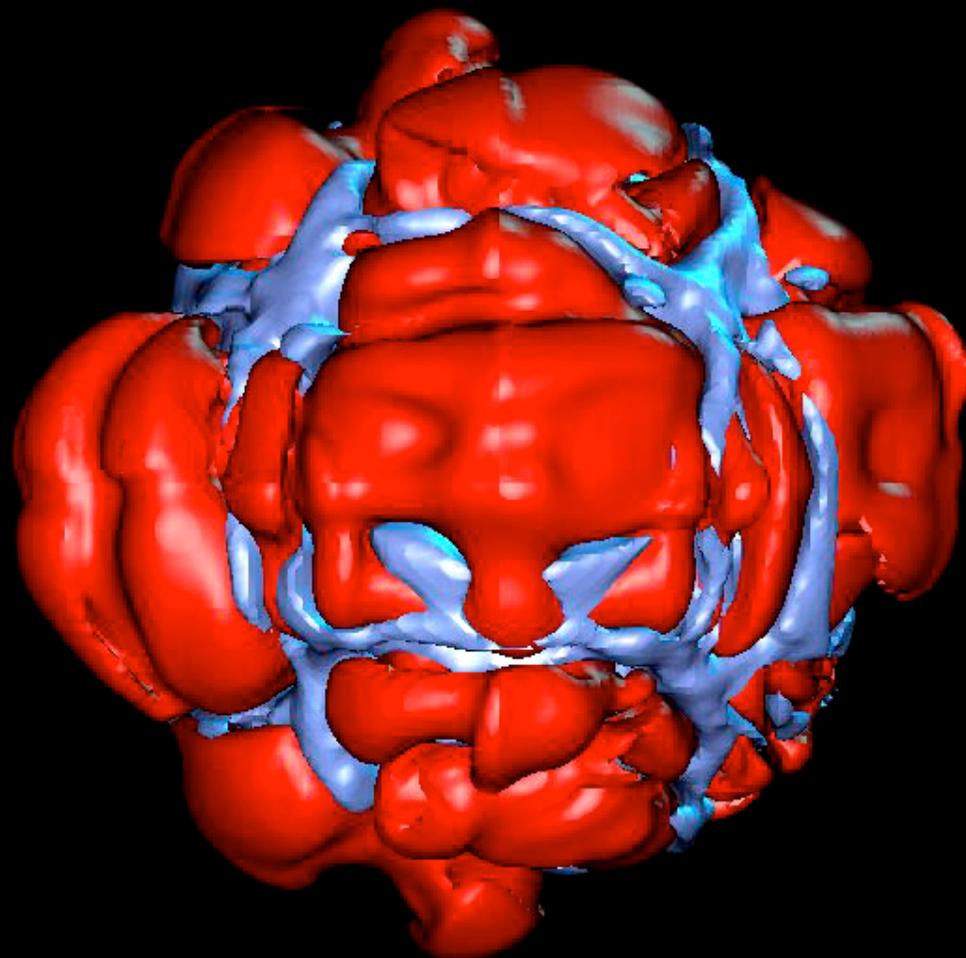




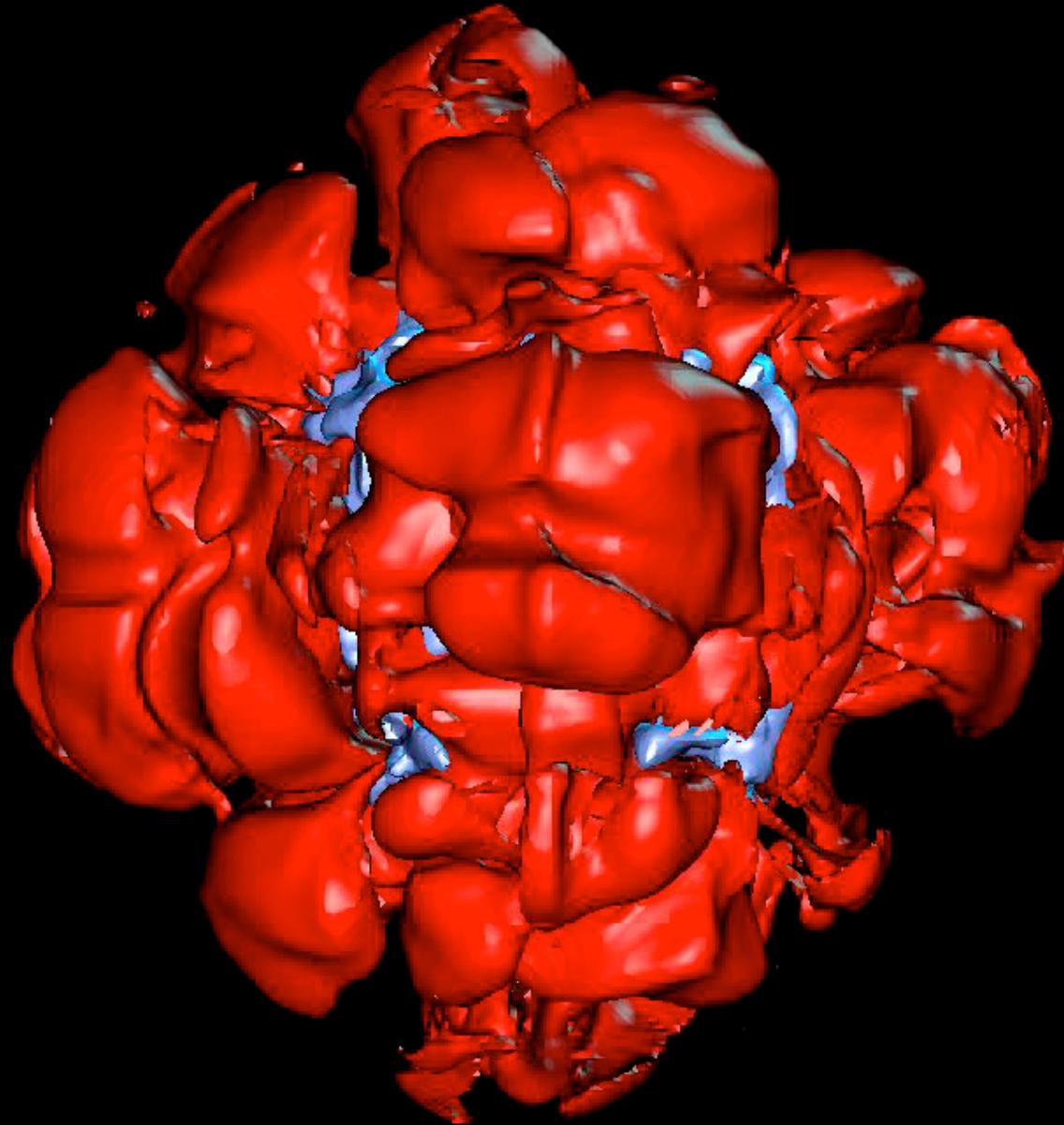
Time = 0.080587 s



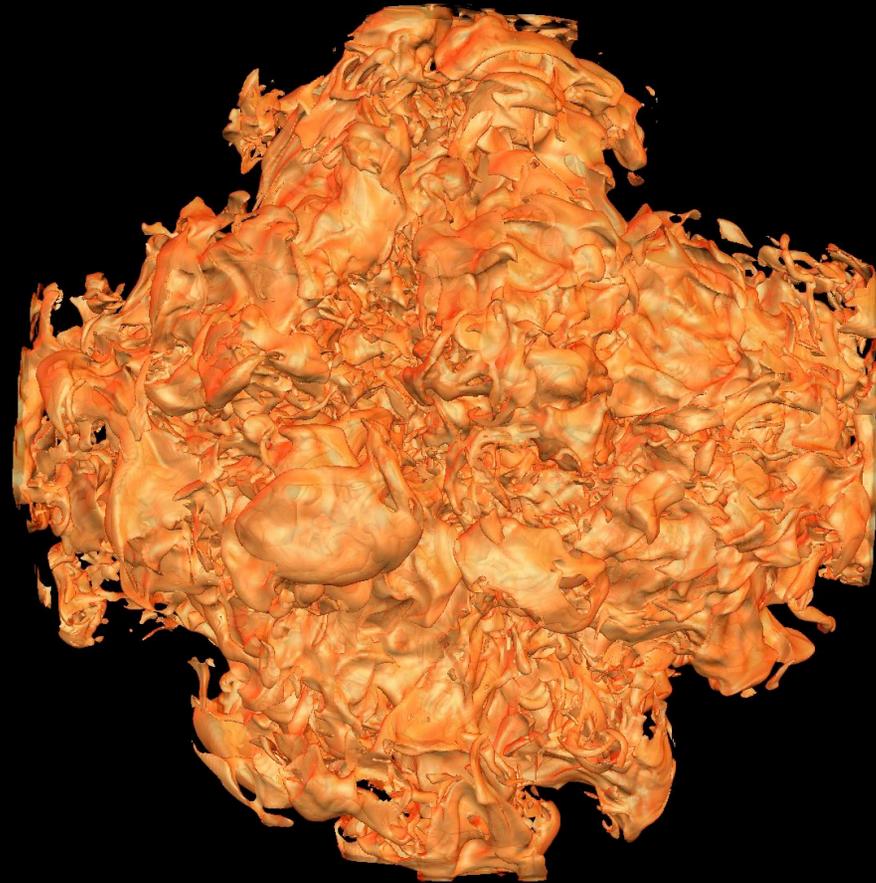




# CASTRO 3D AMR Neutrino-driven Explosion Model



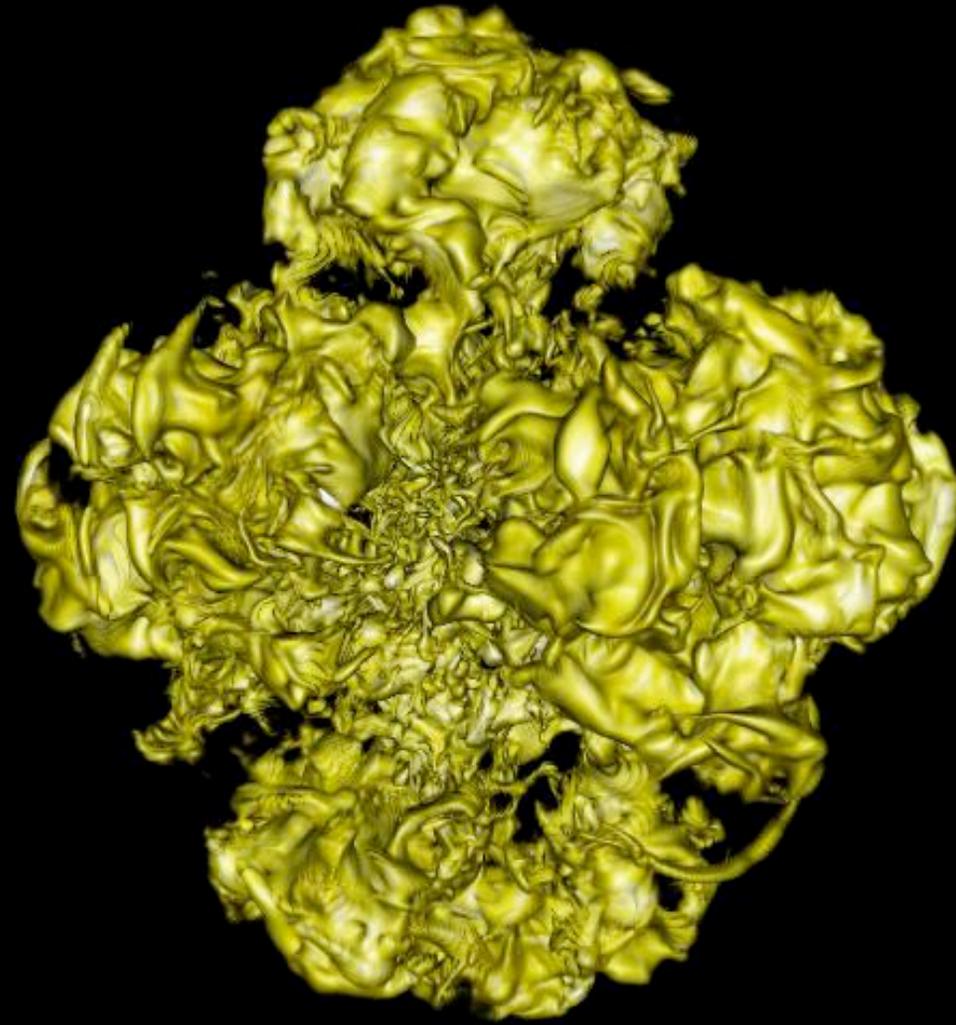
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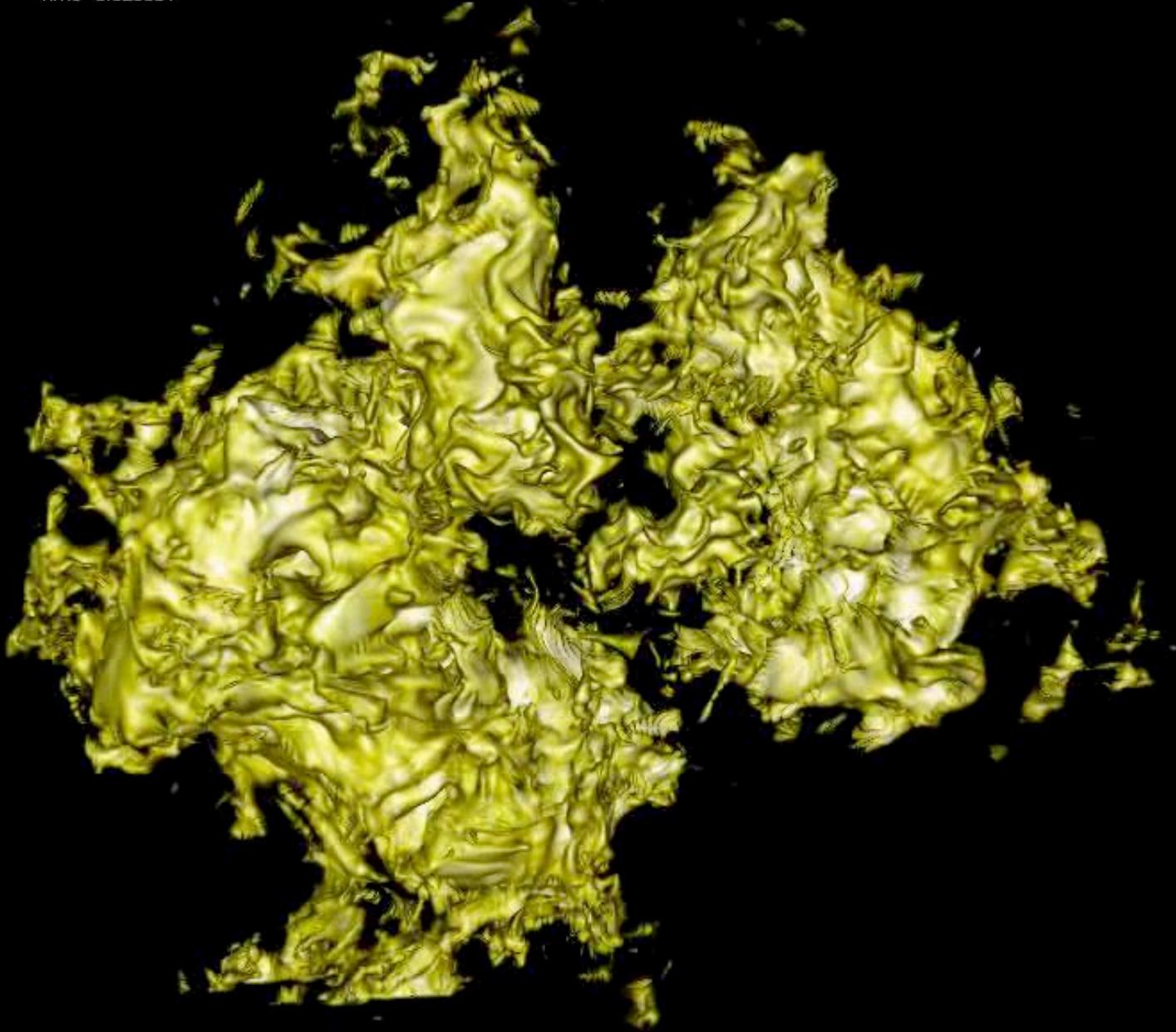
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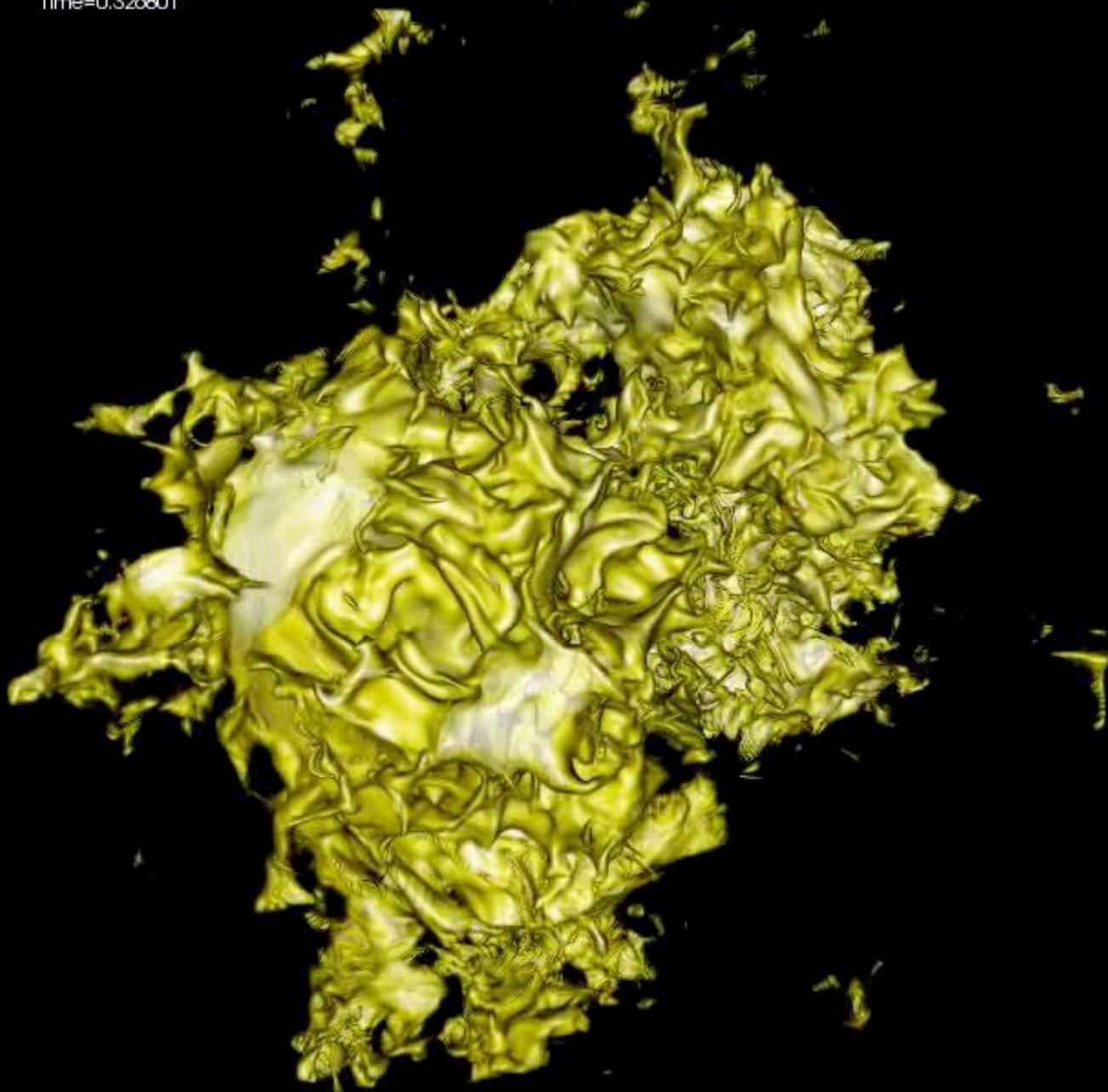
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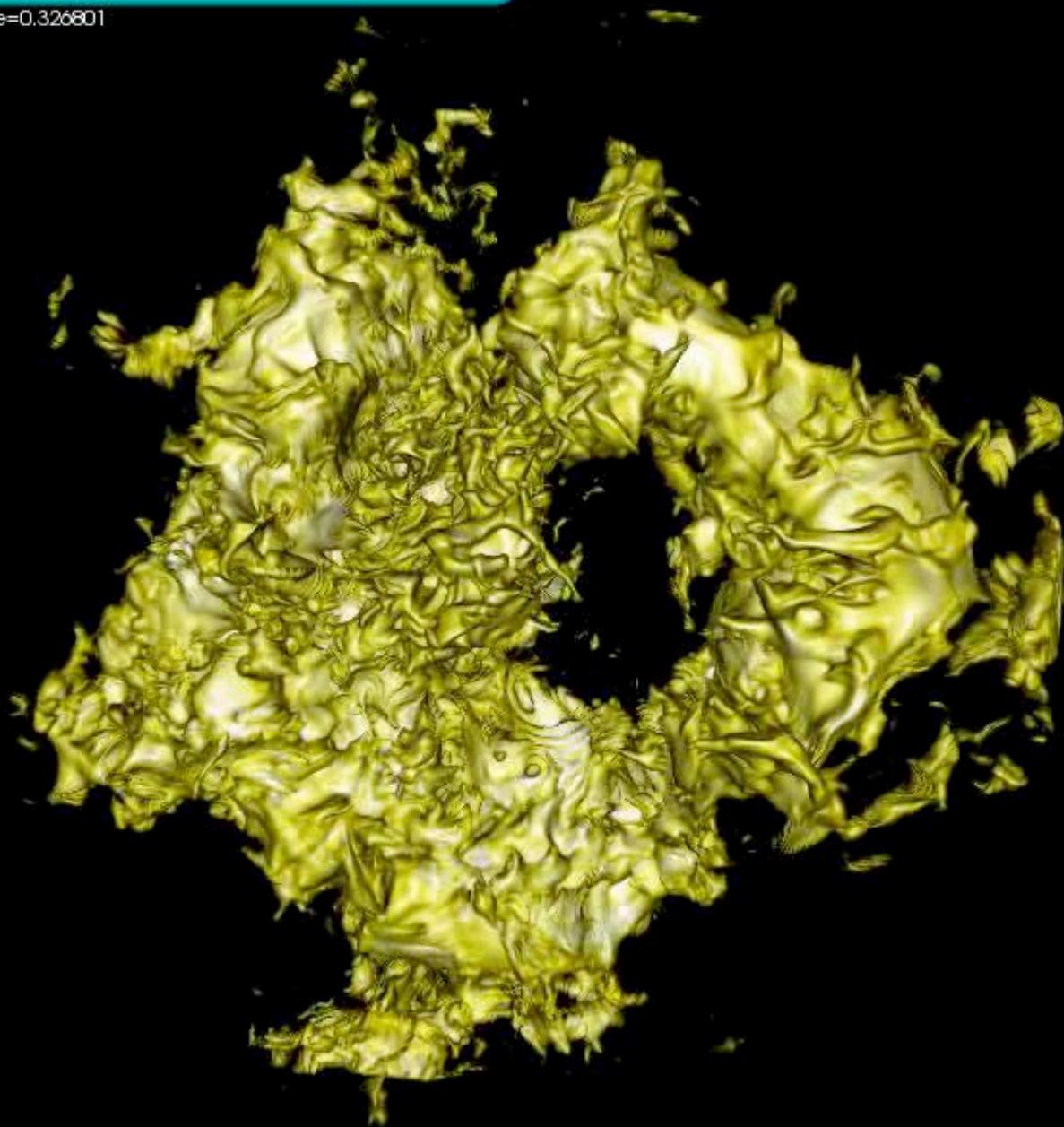
Time=0.326801



Time=0.326801



Time=0.326801



# Core-Collapse Theory: A Status Summary

- **Multi-D is Key Enabler** of explosion for all viable mechanisms
- **Progenitor** structure crucial
- Multi-D allows **simultaneous explosion and accretion** (not possible in 1D)
- Neutrino mechanism: **3D(?) > 2D > 1D - Critical condition**
- Neutrino Mechanism marginal/ambiguous in 2D; Need to go to **3D** !?
- Neutrino-driven convection > SASI
- **Pulsar Kicks** are Simple **Recoils** in Multi-D context
- **MHD explosion** models require **rapid rotation** (rare); hypernovae?  $< 2 \times 10^{52}$  ergs
- GRBs may be preceded by Non-Rel. **precursor jets** launched during PNS phase