

# A Density Dependent nucleon-nucleon interaction for the HD-EOS

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## Computing:

BEN (ECT\*)  
WIGLAF (UNITN)  
SISSA, LLNL, CINECA



# Punchline

We do not know enough on the nucleon-nucleon (ant three nucleon) interaction to reliably make prediction on the equation of state...

# "Standard" Monte Carlo methods : VMC & GFMC

## Green's Function Monte Carlo

Project the ground state using the standard propagator:

$$\psi(R, t) = e^{-(H-E_T)t} \psi(R, 0)$$

$$\psi(R, t) = \int dR' G(R, R', t) \psi(R', 0)$$

Approximate with a finite sum of eigenstates of the position ("walkers")

the propagator can be broken in the usual way using the Trotter-Suzuki formula:

Diffuses the walker



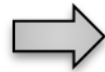
Weights the walker, and produces zero, one or more copies

# Auxiliary Field Diffusion Monte Carlo (AFDMC)

## Hubbard Stratonovich transform

↖  
Approx. order  $\Delta\tau$

2 body  
operators



$\int$  Auxiliary  
Field  $x$  + 1 body  
operator

**AFDMC = DMC + HS-transform**

### Other issues:

- ✓ Sign problem "treated" with Fixed-Phase approximation.
- ✓ Wave functions simplified to a central Jastrow (no operatorial dependence) times an antisymmetrized product of spinors.

[ Schmidt & Fantoni, PLB 446, 99 (1999) ]

[ Fantoni, Sarsa, Schmidt, Prog. Part. Nuc. Phys. 44 (2000) ]

[ Gandolfi et al, PRL 99, 022507, (2007) ]

## Equation of state of neutron matter at high density

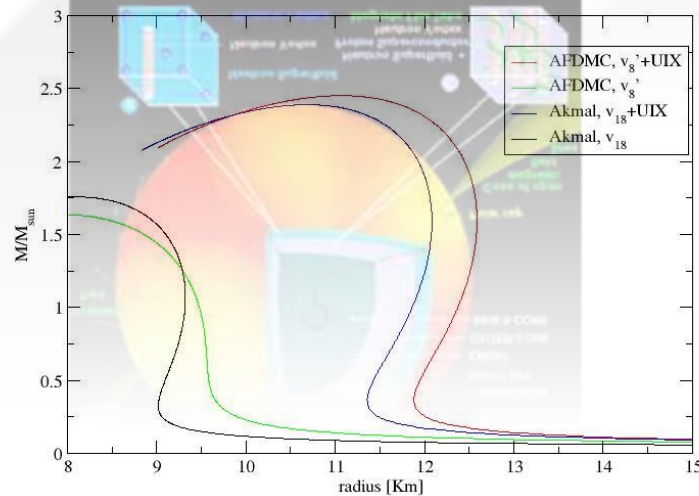
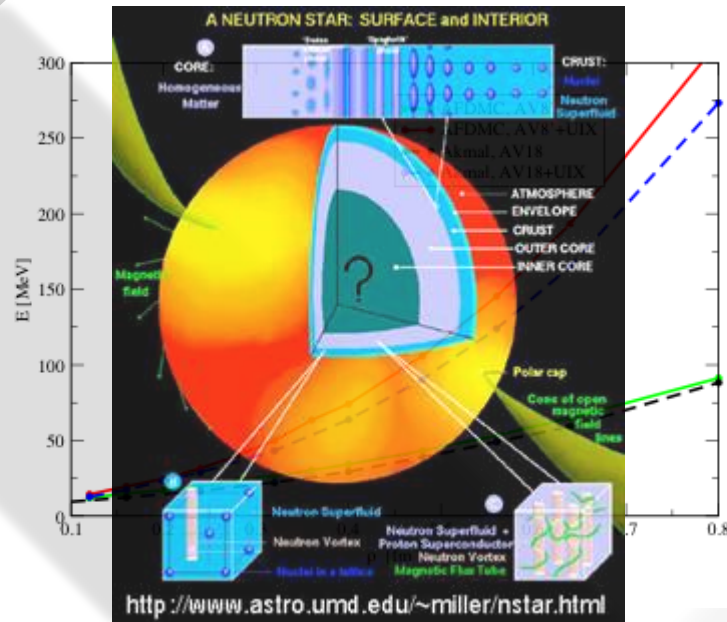
We revised the computations made on Neutron Matter to check the effect of the use of the fixed-phase approximation.

Results are *more stable*, and some of the issues that were not cleared in the previous AFDMC work are now under control.

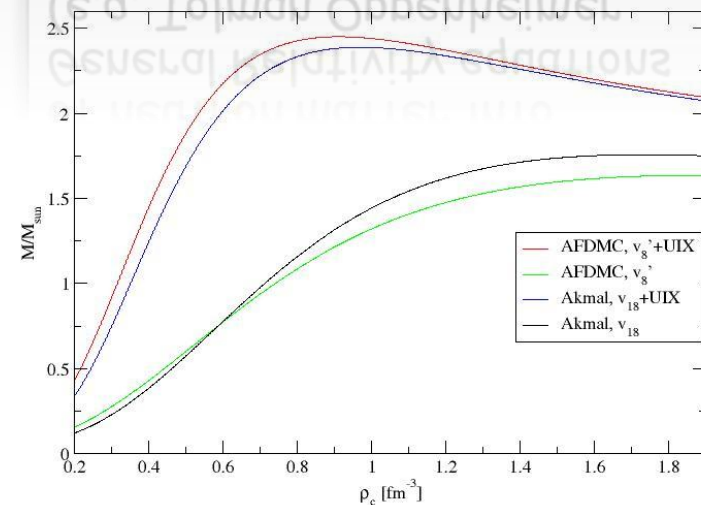
In particular the ***energy per nucleon*** computed with the AV8' potential in PNM with  $A=14$  neutrons in a periodic box is now ***17.586(6)MeV***, which compares very well with the GFMC-UC calculations of J. Carlson et al. which give ***17.00(27)MeV***. The previous published AFDMC result was ***20.32(6)MeV***.

The functions in the Jastrowfactor are taken as the scalar components of the FHNC/SOC correlation operator which minimizes the energy per particle of SNM at saturation density  $r_0=0.16 \text{ fm}^{-3}$ . The antisymmetric product  $A$  is a Slater determinant of *plane waves*.

# Equation of state of neutron matter



Plugging the equation of state of neutron matter into General Relativity equations (e.g. Tolman Oppenheimer Volkov equation), it is possible to make predictions about the structure of compact stars!



# Density dependent potential

Following Lagaris and Pandharipande (*Nucl. Phys. A359, 349 (1981)*), it is possible to redefine the interaction with density dependent parameters:

The density dependent repulsive part is a modification of the intermediate part of  $AV6'$ :

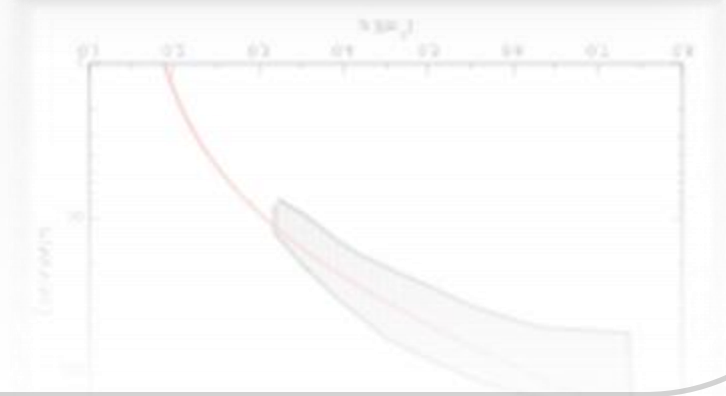
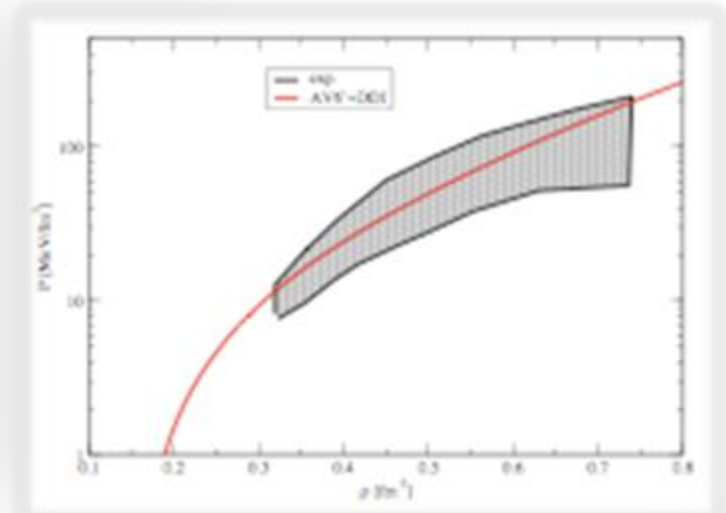
The attractive part is completely phenomenological, and it is written as:

# Density dependent potential

The parameters are fitted in order to reproduce the saturation density, the energy at the saturation density and the compressibility of symmetric nuclear matter. The values are

The equation of state of nuclear matter fitted with these values of the parameters is:

with:



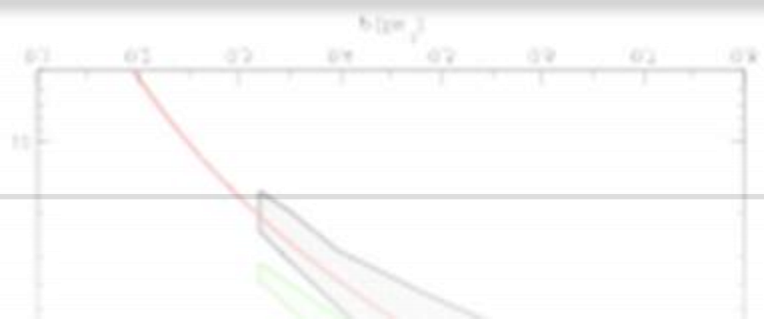
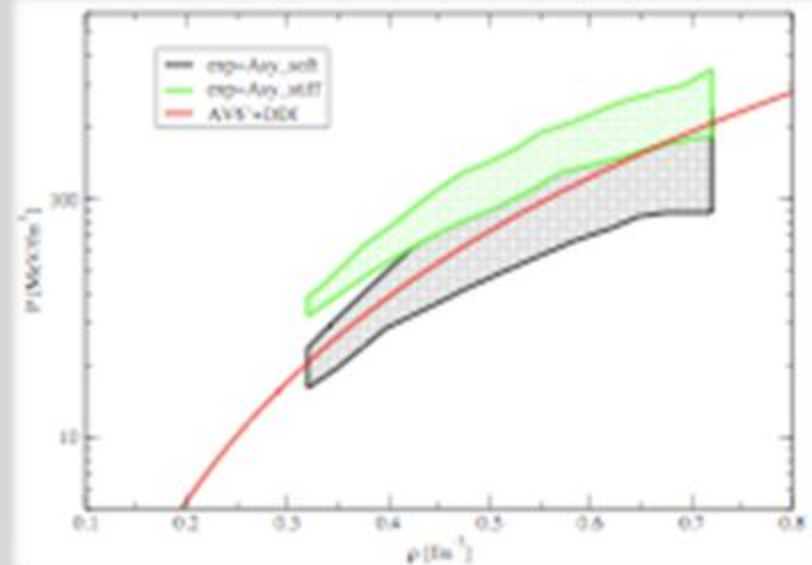


# Density dependent potential

Using the *same parameters in the Hamiltonian*, we computed the equation of state of pure neutron matter. The results are strikingly good.

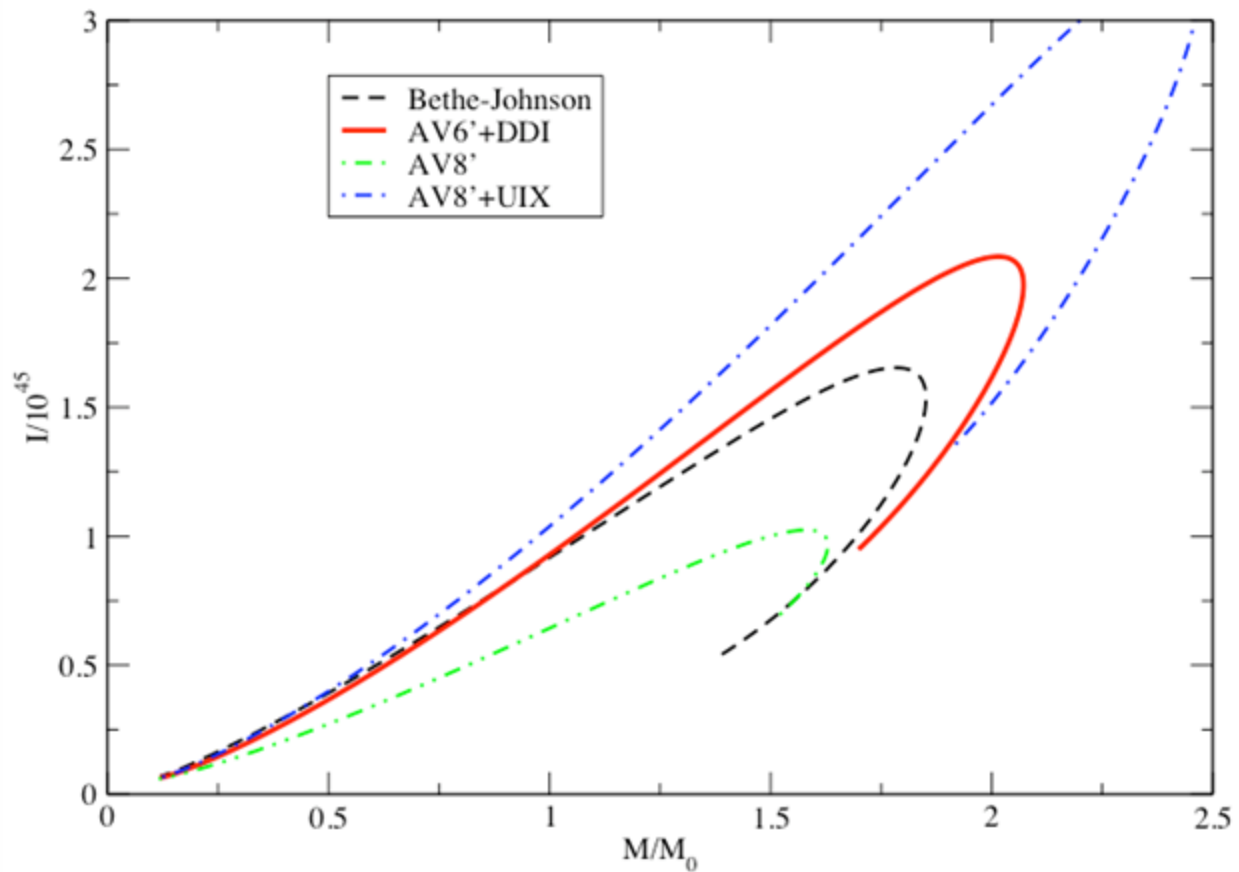
In this case the equation of state is fitted with the expression:

with:



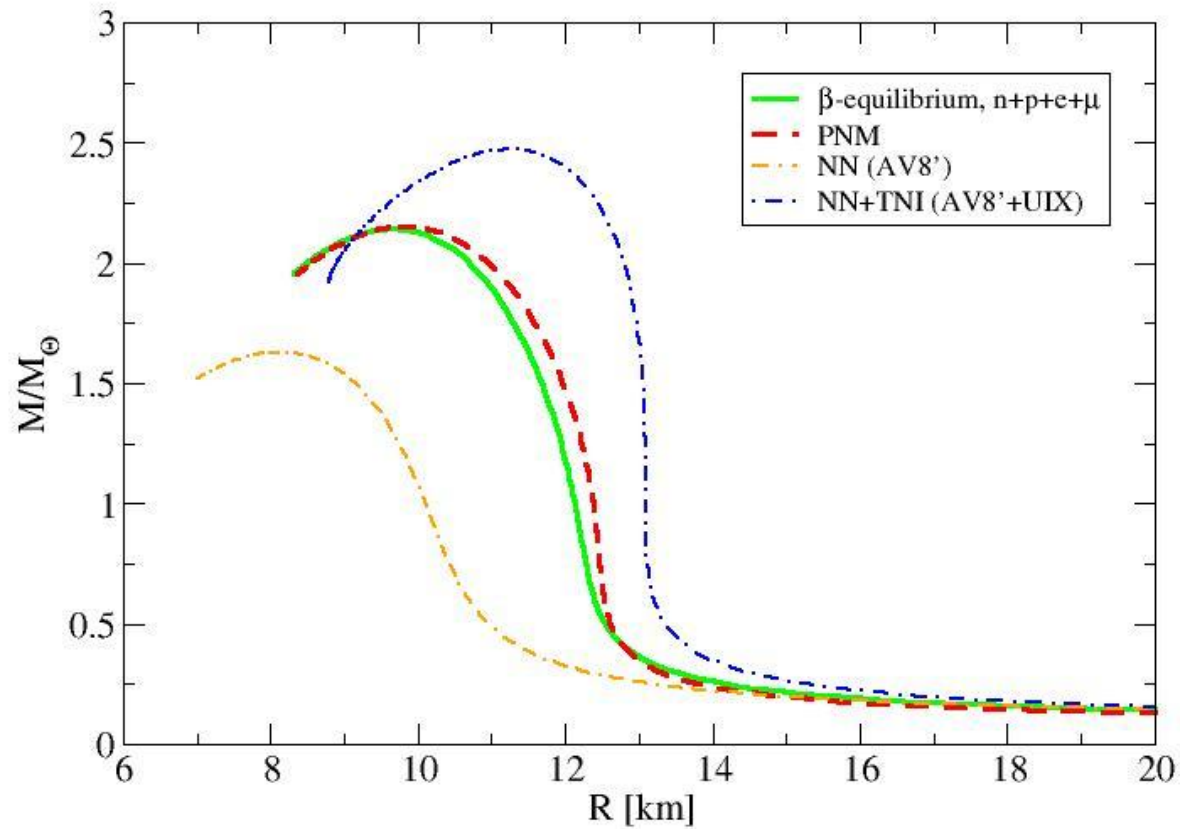
# Density dependent potential

Momentum of inertia vs. mass of the star



# Density dependent potential

Mass vs. radius of the star



# Density dependent potential

