

Electroweak Baryogenesis after LHC8

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What NExT?
Southampton – November 27, 2013

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 - ✓ expansion of Universe;
 - ✓ EW phase transition.

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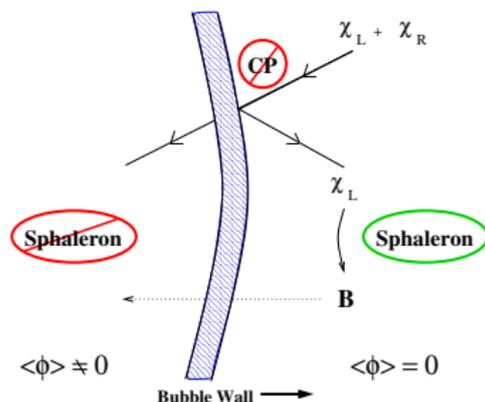
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- ▶ If $T > T^*$ after EW phase transition, the generated asymmetry is washed out.
- ▶ Successful baryogenesis requires a strong first order phase transition:

$$\frac{v_c}{T_c} \gtrsim 1.$$



Morrissey, Ramsey-Musolf
[arXiv:1206.2942]

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 - ▶ 2HDM.

EWBG in the MSSM

MSSM Higgs sector \Rightarrow two $SU(2)_L$ scalar doublets Φ_1, Φ_2 :

$$\Phi_i = \begin{pmatrix} \varphi_i^+ \\ h_i + i\eta_i \end{pmatrix}.$$

$$V_{\text{tree}}^{\text{MSSM}} = -\mu_1^2 \Phi_1^\dagger \Phi_1 - \mu_2^2 \Phi_2^\dagger \Phi_2 - \frac{\mu^2}{2} (\Phi_1^\dagger \Phi_2 + H.c.) + \\ + \frac{g^2 + g'^2}{8} (\Phi_1^\dagger \Phi_1 - \Phi_2^\dagger \Phi_2)^2 + \frac{g^2}{2} |\Phi_1^\dagger \Phi_2|^2.$$

EW minimum: $\langle \Phi_1 \rangle = \begin{pmatrix} 0 \\ v \cos \beta \end{pmatrix}, \quad \langle \Phi_2 \rangle = \begin{pmatrix} 0 \\ v \sin \beta \end{pmatrix}.$

Mass eigenstates: $\underbrace{G^0, G^\pm}_{\text{Goldstone bosons}} + \underbrace{h^0, H^0, A^0, H^\pm}_{\text{physical Higgs states}}.$

EWBG in MSSM (?)

- ▶ New scalars increase strength of phase transition \Rightarrow light stop scenario (LSS): $80 \text{ GeV} \lesssim m_{\tilde{t}_R} \lesssim 120 \text{ GeV}$.
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- ▶ This scenario allows for rather definite predictions on SM Higgs production and branching ratios, with **severe tension with experimental data!** [Curtin, Jaiswal, Meade, arXiv:1203.2932]
- ▶ Could be alleviated if light neutralino has mass $\lesssim 60 \text{ GeV}$.
[Carena, Nardini, Quiros, Wagner, arXiv:1207.6330]

2HDM

- ▶ Two-Higgs-doublet models are the minimal SM extension able to account for BAU.
- ▶ Generalization of the MSSM Higgs sector.
- ▶ Extra heavy bosons (h^0 , H^0 , A^0 , H^\pm) may strengthen the EW phase transition.
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- ▶ But what happens in the general case?

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- ▶ General fermionic couplings:

$$\mathcal{L}_{\text{Yukawa}} = -\bar{Q}_L (\Gamma_1 \Phi_1 + \Gamma_2 \Phi_2) n_R + \dots$$

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- ▶ Avoid this with \mathbb{Z}_2 symmetry: $\Phi_1 \rightarrow -\Phi_1$, $\Phi_2 \rightarrow \Phi_2$.

	u_R	d_R	e_R
Type I	+	+	+
Type II	+	-	-
Type X	+	+	-
Type Y	+	-	+

Only top-quark is significant for phase transition.

Then models differ only in phenomenological constraints on their parameter space. These come mainly from B -physics, so

Type I \sim Type X,
Type II \sim Type Y.

- ▶ For simplicity, consider CP conserving case only.

$$\begin{aligned}
 V_{\text{tree}}(\Phi_1, \Phi_2) = & -\mu_1^2 \Phi_1^\dagger \Phi_1 - \mu_2^2 \Phi_2^\dagger \Phi_2 - \frac{\mu^2}{2} (\Phi_1^\dagger \Phi_2 + H.c.) + \\
 & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \\
 & + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} \left[(\Phi_1^\dagger \Phi_2)^2 + H.c. \right].
 \end{aligned}$$

- ▶ EW minimum: $\langle \Phi_1 \rangle = \begin{pmatrix} 0 \\ v \cos \beta \end{pmatrix}$, $\langle \Phi_2 \rangle = \begin{pmatrix} 0 \\ v \sin \beta \end{pmatrix}$.

- ▶ Physical parameters:

- ▶ $v \approx 174$ GeV and $M \equiv \frac{\mu}{\sqrt{\sin(2\beta)}}$.
- ▶ Masses: $m_{h^0}, m_{H^0}, m_{A^0}, m_{H^\pm}$.
- ▶ β is the mixing angle between (G^+, H^+) and (G^0, A^0) .
- ▶ Likewise, α is the mixing angle between (h^0, H^0) .
It is here defined such that $\alpha = \beta \iff h^0 = h_{SM}$.

$$V = V_{\text{tree}} + V_{CW} + V_{CT} + V_T.$$

► Fix $m_{h^0} = 125$ GeV

$$0.4 \leq \tan \beta \leq 10,$$

$$-\frac{\pi}{2} < \alpha \leq \frac{\pi}{2},$$

$$0 \text{ GeV} \leq \mu \leq 1 \text{ TeV},$$

$$100 \text{ GeV} \leq m_{A^0}, m_{H^\pm} \leq 1 \text{ TeV},$$

$$150 \text{ GeV} \leq m_{H^0} \leq 1 \text{ TeV}.$$

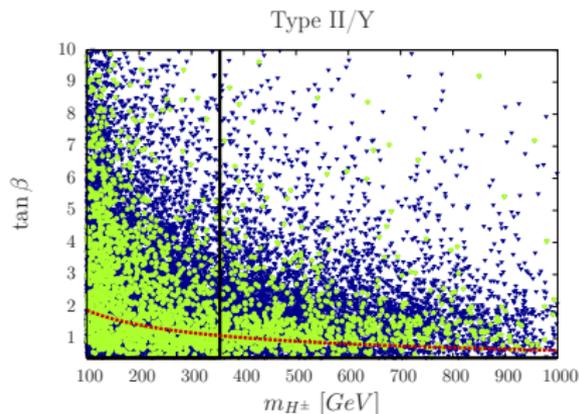
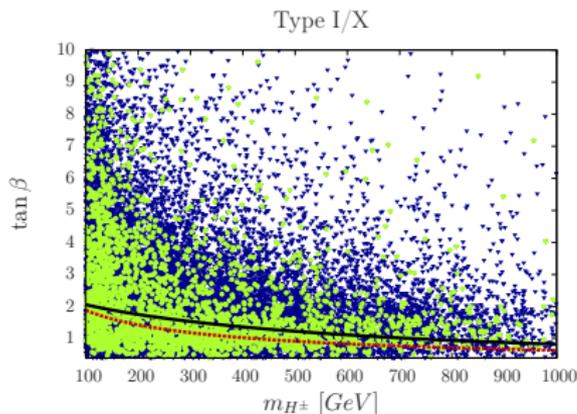
► Constraints:

► EW precision: $\rho - 1 \approx 0$;

► $\lambda_i < 4\pi$;

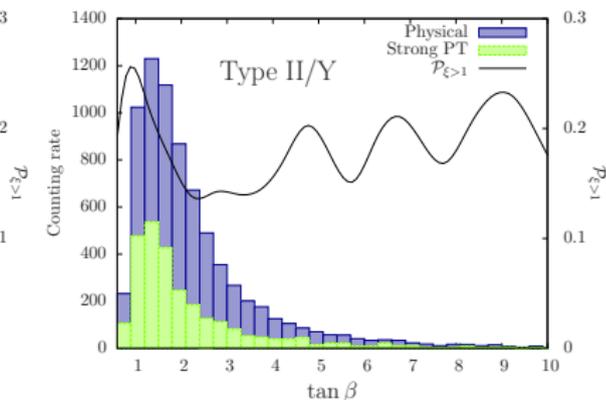
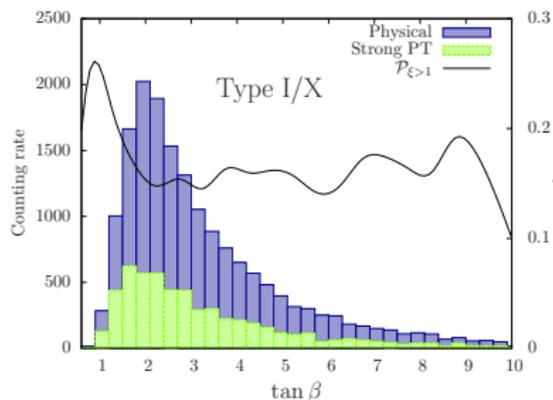
► metastability;

► $B^0 - \bar{B}^0$ (red/dashed) and $\bar{B} \rightarrow X_s \gamma$ (black/full).



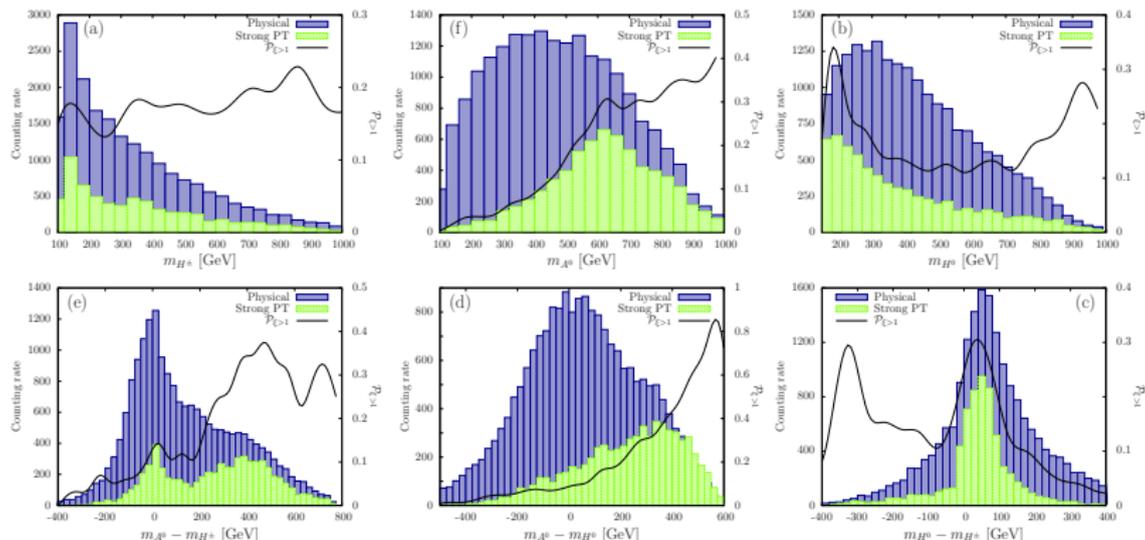
Type II/Y: $m_{H^\pm} \geq 360$ GeV [Hermann et al., arXiv:1208.2788].

Results: $\tan \beta$



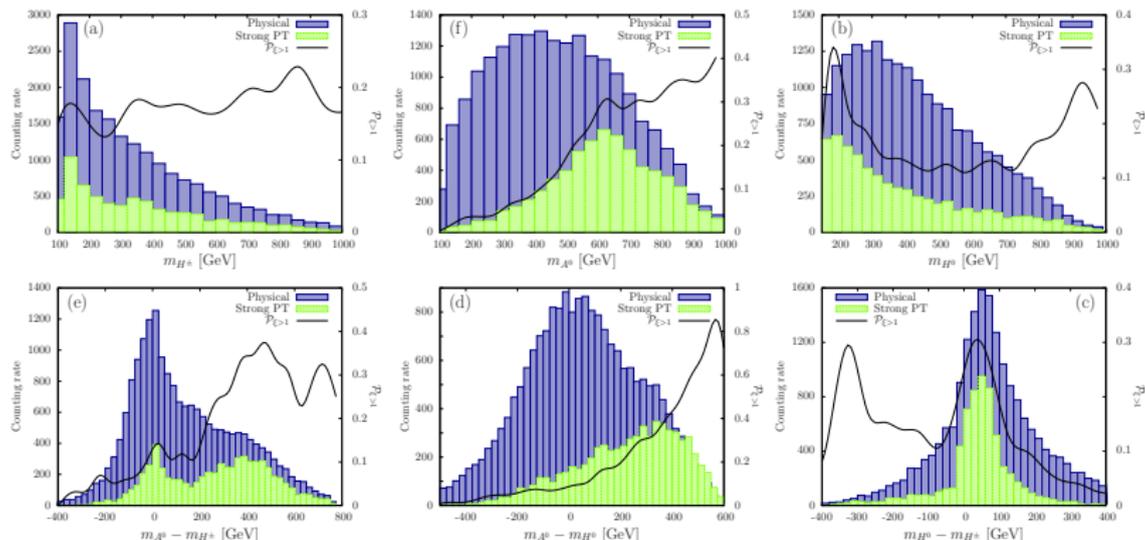
Preference for $\tan \beta \lesssim 3$ is excellent for baryogenesis, since $n_B \sim (\tan \beta)^{-2}$.

Results: Masses



m_{H^\pm} hardly influences the phase transition.

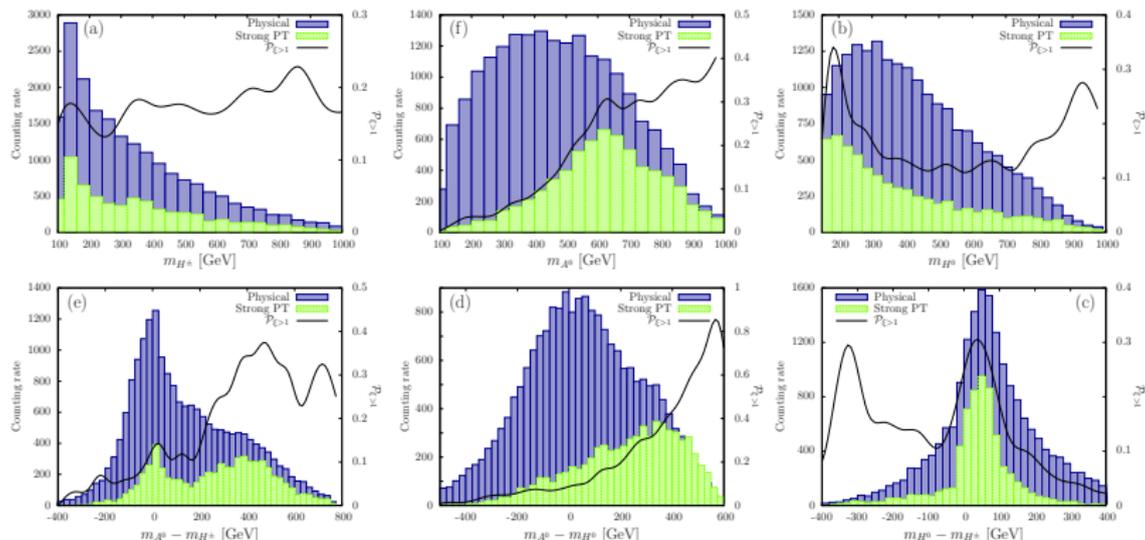
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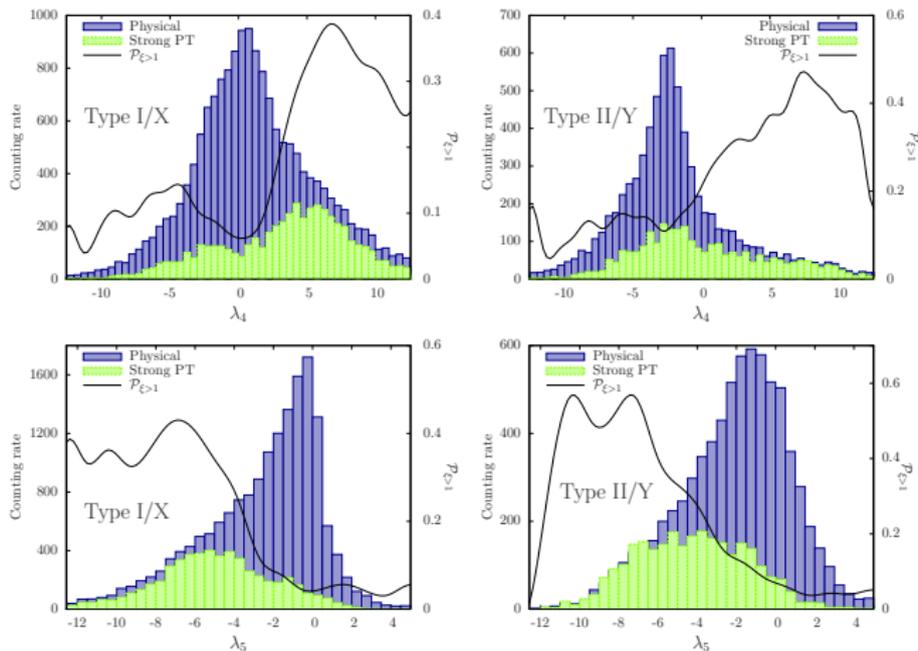
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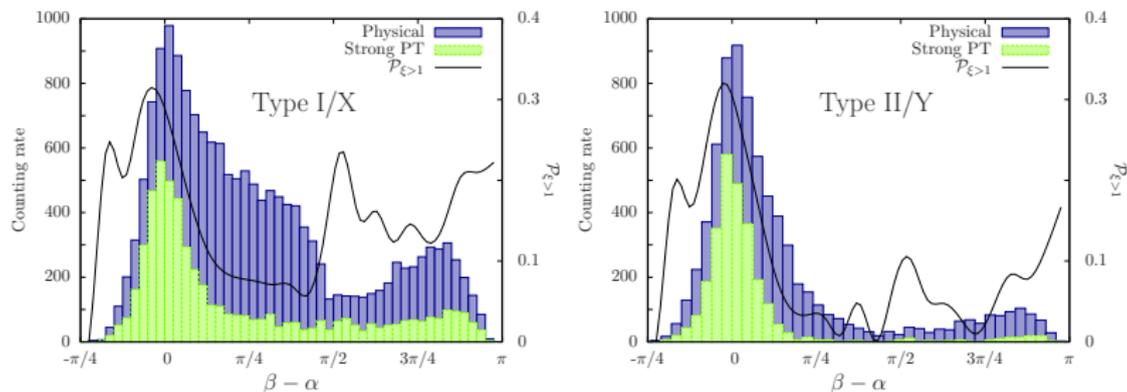
Strong PTs also prefer hierarchy $m_{A^0} > m_{H^0} \gtrsim m_{H^\pm}$.

Results: Couplings

$$\lambda_4 = \frac{1}{2v^2} (M^2 + m_{A^0}^2 - 2m_{H^\pm}^2), \quad \lambda_5 = \frac{1}{2v^2} (M^2 - m_{A^0}^2).$$

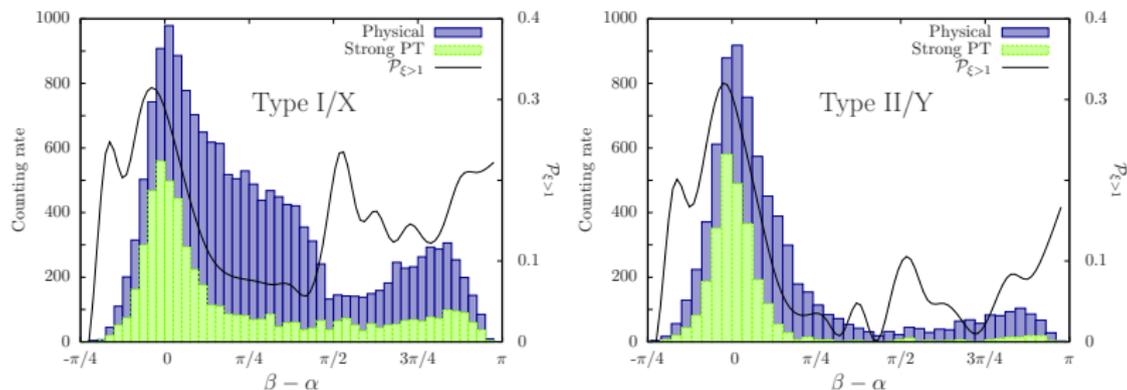


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Put another way, the observation of a SM-like h^0 constrains the parameter space of 2HDMs in favour of strong PTs.

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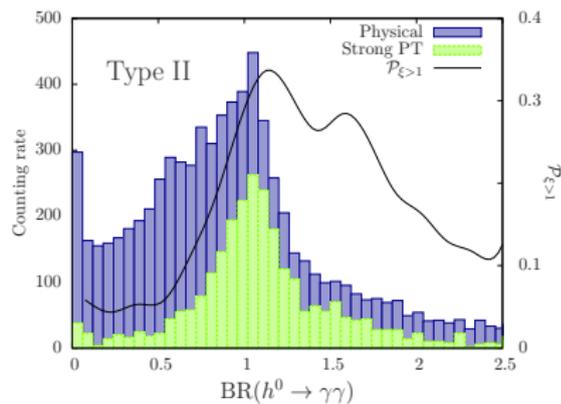
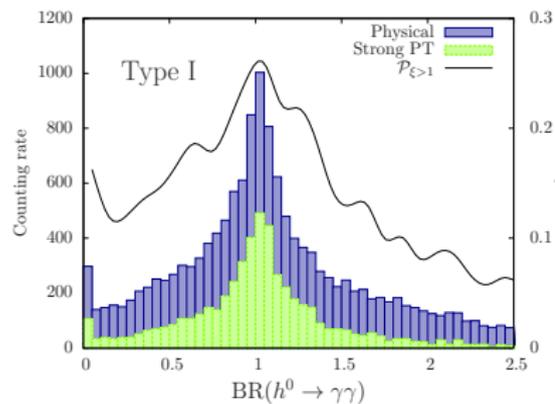
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Thank you!

Appendix – $h^0 \rightarrow \gamma\gamma$

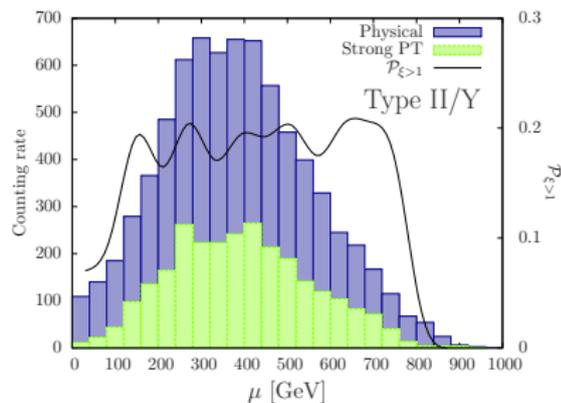
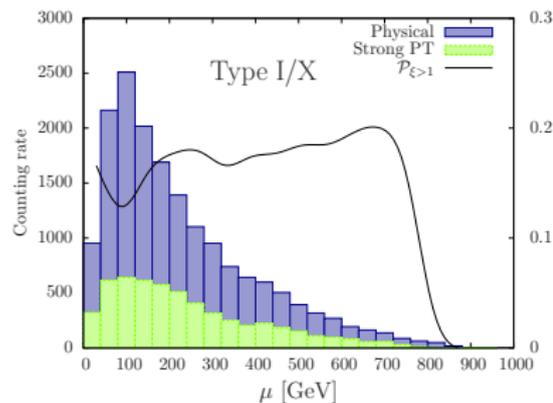


Coupling of h^0 to b and τ :

$$\text{Type I: } \frac{\sin \alpha}{\sin \beta}, \quad \text{Type II: } \frac{\cos \alpha}{\cos \beta}.$$

Appendix – μ parameter

$$V_{\text{tree}} \supset -\frac{\mu^2}{2} \left(\Phi_1^\dagger \Phi_2 + H.c. \right)$$



Type II/Y: $m_{H^\pm} \geq 360$ GeV.

Appendix

Surviving points after each step of tests:

	Total	EW precision	$\lambda_i < 4\pi$	Metastability	Strong PT
Absolute	6.3×10^6	1.2×10^6	1.4×10^5	2.6×10^4	4.3×10^3
Relative	100%	19.1%	2.3%	0.41%	0.069%

Physical fields:

$$\begin{aligned} G^+ &= \cos \beta \varphi_1^+ + \sin \beta \varphi_2^+ && \text{(charged Goldstone),} \\ H^+ &= -\sin \beta \varphi_1^+ + \cos \beta \varphi_2^+ && \text{(charged scalar),} \\ G^0 &= \cos \beta \eta_1 + \sin \beta \eta_2 && \text{(neutral Goldstone),} \\ A^0 &= -\sin \beta \eta_1 + \cos \beta \eta_2 && \text{(pseudo-scalar),} \\ h^0 &= \cos \alpha h_1 + \sin \alpha h_2 && \text{(lightest scalar),} \\ H^0 &= -\sin \alpha h_1 + \cos \alpha h_2 && \text{(heaviest scalar).} \end{aligned}$$

where

$$\Phi_i = \begin{pmatrix} \varphi_i^+ \\ h_i + i\eta_i \end{pmatrix}.$$