Disk winds driven by MRI -some aspects and applications-

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Aug. 4th, 2014

Suzuki & Inutsuka 2009, 691, L49 Suzuki, Muto, & Inutsuka 2010, ApJ, 718, 1289 Io & Suzuki 2014, ApJ, 780, 46 Suzuki & Inutsuka 2014, 784, 121

Thanks to PC clusters(Ta lab.), HITACHI SR16000(Yukawa inst.), Cray XT4 & XC30 (NAOJ)

Turbulence in Accretion Disks

- Turbulence ⇒ Macroscopic (effective) Viscosity
 - Outward Transport of Angular Momentum
 - Inward Accretion of Matters





Unstable under

- Weak B-fields
- (inner-fast) Differential Rotation

Velikov (1959); Chandrasekhar (1960); Balbus & Hawley (1991) • Local at Midplane

Theoretical Attempts on MRI in Disks

Analytic Works

Shakura & Sunyaev 1973; Lynden-Bell & Pringle 1974; & many others

Simulations



 Local Simulations in Shearing Box: "Zoom-in" Hawley+ 1995; Matsumoto & Tajima 1995; Brandenburg+ 1995; Stone+ 1996; Sano+ 2004; Hirose+ 2009; Simon+ 2009; Davis+ 2010; Shi+ 2010 & more
 Global Simulations Machida+ 2000; Hawley 2000; Papaloizou & Nelson 2003; Machida & Matsumoto 2003; Kato+ 2004; Formang & Nelson 2006; Papalwith, 2004; Elostic 2014, 2014; Formang 2014, 2014; Lawley 2016;

Beckwith+ 2009; Flock+ 2011, 2012, 2013; Fromang+ 2011, 2013; Hawley+ 2011, 2013; Parkin & Bicknell 2013; Parkin 2014 & more

But, not so many works with B_z from the beginning.

Accretion Disk Winds

Magneto-centrifugal driven disk winds

(Coherent field lines)

(Blandford & Payne 1982; Kudoh & Śhibata 1998; Ramsey & Clarke 2011; Salmeron+ 2011)



But the mass loading mechanism to wind is necessary.

Accretion Disk Winds

Magneto-centrifugal driven disk winds

(Coherent field lines)

Gravity

(Blandford & Payne 1982; Kudoh & Śhibata 1998; Ramsey & Clarke 2011; Salmeron+ 2011)

> centrifugal force

B-field

But the mass loading mechanism to wind is necessary.



Suzuki & Inutsuka 2009 (modified)

 Turbulent-driven vertical outflows as a mass loading mechanism

Recent works: Bai & Stone 2013; Fromang+ 2013; Lesur+ 2013

Dispersal of Protoplanetary Disks

Current Major Scenario: Photo-evaporating wind

+ Accretion

Shu+ 1993; Matsuyama+ 2003; Takeuchi+ 2005; Alexander+ 2006; Ercolano+ 2009; many more



Other mechanisms

- Stellar Winds
 - Limitted contribution ?

Matsuyama et al.2009

• Significant contribution with a boundary layer ?

Schnepf et al.2014

 Disk Winds –Today's talk

• Recent Review Armitage 2011

Outline

• Simulation in Local Shearing Box

Suzuki & Inutsuka 2009; Suzuki, Muto & Inutsuka 2010

Wave activity

Local with vertical stratification

- Effect of the z box size
- Effect of a dead zone
- Preventing Type I migration
- Simulations in Global Accretion Disk

Suzuki & Inutsuka 2014

- Effect of vertical shear (differential rotation)
- Structured vertical outflows
- Radial motion of the net B_z

Assuming (locally) isothermal gas Scheme: MHD Godunov (with only *B*_⊥) (Sano+ 1999) + CMoC(Clarke 1996) + CT(Evans & Hawley 1988)

Dependence on NET B_z (ideal MHD) Stronger $B_z \Rightarrow$



- Upper panel $\alpha = \left[\delta v_{\phi} v_r - \frac{B_{\phi} B_r}{4\pi\rho} \right] / c_s^2$ (Reynolds + Maxwell stresses)
- Lower panel $C_{\rm w} \equiv \left[(\rho v_z)_{\rm surf} \right] / (\rho c_s)_{\rm mid}$

(normalized disk wind mass flux)

Both $\alpha \& (\rho v_z)_w$

- are constant for weak B_z $(\beta_{z,{
 m mid}} \gtrsim 10^6)$
- increase with B_z

Suzuki, Muto, & Inutsuka 2010 see also Pessah+ 2007; Okuzumi & Hirose 2011

Poynting flux-driven disk winds



- Wind Onset: $\beta = 8\pi p/B^2 \leq 1$
- Energetics Argument
 - Energy Flux (z-direction): $v_z \left(\frac{1}{2}\rho v^2 + \rho \Phi + \frac{\gamma}{\gamma - 1}p\right)$

 $+v_z \frac{B_r^2 + B_{\phi}^2}{4\pi} - \frac{B_z}{4\pi} (v_r B_r + v_{\phi} B_{\phi})$ where, $\Phi = z^2 \Omega_0^2/2$

Poynting Flux-driven
 Both Pressure & Tension
 contribute

Suzuki & Inutsuka 2009, ApJ, 691, L49

Characteristics of Turbulence



Imbalanced with waves in the vertically stratified background.

- Transverse (≈ Alfvén) waves to both directions
 - $$\begin{split} w_{\pm} &= (v_{\perp} \mp B_{\perp} / \sqrt{4\pi\rho})/2 \\ -B_z v_{\perp} B_{\perp} / 4\pi = \rho v_{\rm A} (w_{+}^2 w_{-}^2) \\ (\text{Elsässer variables}) \end{split}$$
- Sound waves to midplane $u_{\pm} = (\delta v_z \pm c_s \delta \rho / \rho)/2$ $\delta \rho \delta v_z = \rho c_s (u_+^2 - u_-^2)$



- Vertical outflows from Injection Regions at z ≈ ±(1.5 − 2)H with β ~1−10
- Momentum flux to midlplane ⇒ Dusts Turner et al.2010

Time dependency: t - z diagrams



of B_{ϕ}

Dependence on *z* Box Size





r.

Effect of a Dead Zone

- Disk winds are not so affected by a dead zone with resistivity.
 - The mass flux slightly decreases to 1/2-1/3.

see Gressel+ (2013) & Bai (2013) for ambipolar diffusion

• Quasi-periodic inversion of B_{ϕ} . (e.g. Nishikori et al.2006)

Overall dynamics is controlled by the thin active layers near the surfaces.



Most of ionization sources from the surfaces







- $\alpha \& (\rho v_z)_w \Leftarrow \text{local simulations}$
 - turbulent viscosity: $\alpha = (v_r \delta v_{\phi} B_r B_{\phi}/4\pi\rho)/c_s^2$
 - disk wind flux from top & bottom surfaces: (pvz)w
- Initial Cond.: Min.Mass Sol.Neb. (Hayashi 1981) $\Sigma = \Sigma_0 \left(\frac{r}{1 \text{ AU}}\right)^{-3/2} \exp(-r/r_{\text{cut}})$ $(\Sigma_0 = 2400 \text{ g cm}^{-3}; r_{\text{cut}} = 50 \text{AU})$

Evolution of Surface Density



Type I Migration with Disk Winds



Put

- 0.3*M*⊕ at 0.3 AU
- 1*M*_⊕ at 1 AU

• $5M_\oplus$ at 5 AU with Tanaka+ 2002 formula

- Solid: With Disk Winds
- Dashed: Without Disk Winds

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Suzuki & Inutsuka 2009; Suzuki, Muto & Inutsuka 2010

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Global Simulations – Set-up– (1/2)

Simulation Region: Suzuki & Inutsuka 2014



- Low resolution: (*r*, θ, φ) = (1 ~ 20, ±0.5, 2π) resolved by (192,64,128) mesh points.
- High resolution:
 - $(1 \sim 20, \pm 0.5, \pi)$ by (512,128,256)
 - $(1 \sim 300, \pm 0.5, \pi)$ by (1024,128,256)
- Ideal MHD with local isothermal EoS

(⇒ next page)

- Initial Conditions
 - ~Keplerian rotation

•
$$p \propto r^{-3}$$
 & weak $B_z \propto r^{-3/2}$ ($\beta = \frac{8\pi p}{B_z^2} = 10^5$)

- Boundary Conditions
 - outgoing at $\pm \theta$
 - accretion at $r_{\rm out}$ & $r_{\rm in}$: $v_r \approx -\alpha c_{\rm s}^2/r\Omega$
- up to 2000 rotations at $r_{
 m in}$

Global Simulations –Set-up– (2/2)

Assuming locally isothermal gas Case I Case II

► cT+H.R.

• T = const. $\Rightarrow \frac{\partial \Omega}{\partial z} = 0$ (good for MRI studies) $H/R \propto R^{1/2}$

> (not good for disk winds) No Vertical Shear

• $T \propto r^{-1}$ $\Rightarrow \frac{\partial \Omega}{\partial z} \neq 0$ (not good for MRI studies) H/R = const.(z < 4H)(good for disk winds) Vertical Shear

▶ rT+L.R. rT+H.R.

 $\frac{d\Omega}{dz} = 0 \text{ only if } p = p(\rho)$ von Zeipel 1924; Kozlowski 1978; Takeuchi & Lin 2002; McNally & Pessah 2014

Vertical shear seems important even without **B**.(Nelson+ 2013)

- Simulations: spherical coordinates (r, θ, ϕ)
- Data Analyses: cylindrical coordinates (R, ϕ, z)

Turbulent vs. Coherent $B_R B_{\phi}$



(Not converged with resolution yet,)

- Case I (No Vertical shear): Turbulent component dominates
- Case II (Vertical shear): Coherent Maxwell stress (magnetic braking) is not negligible



Disk Winds





(Case I: insufficient vertical box size) Disk Winds in Global Simulations (Case II)

- Structured & Intermittent
- Mass flux is slightly smaller (~1/2 of that of local sh.box.)



- Accretion in small *R* and Decretion in large *R* (Lynden-Bell & Pringle 1974) by the Maxwell stress
- $\langle v_R B_z \rangle / \langle B_z \rangle$ (radial motion of net B_z) is different from that of the gas.

Radial motion of gas & net B_z (2/2)



Lobow et al.1994; Rothstein & Lovelace 2008; Guilet & Ogilvie 2012, 2013, 2014; Okuzumi et al.2014; Hubbard et al.2014

Caution: The boundary condition at the disk surfaces might affect the result.

Summary

 Vertical outflows from the injection regions at z ≈ ±(1.5 − 2)H;

Alfvénic & acoustic wave flux along z direction \Rightarrow Dynamics of solid particles

- $\rho \& v_z$ structures are affected by the *z* box size, but $\rho v_z \iff \dot{M}_{wind}$ is less affected.
- Vertical shear (differential rotation) $\Rightarrow B_r B_{\phi}$; Turbulent MRI vs. Coherent Magnetic Braking
- Layered accretion in the global ideal MHD simulations; ⟨B_z⟩ dragged inward in the surface regions (⇐ surface boundary condition??).
- Suzuki & Inutsuka 2009, ApJ, 691, L49
- Suzuki, Muto, & Inutsuka 2010, ApJ, 718, 1289
- Io & Suzuki 2014, ApJ, 780, 46
- Suzuki & Inutsuka 2014, ApJ, 784, 121

Shearing Box approximation

 Local Cartesian coordinate with co-rotating with Ω₀. (neglect curvature)

• $x = r - r_0$; $y \leftrightarrow \phi$ -direction

- Basic equations for Keplerian rotation ($\Omega_0 = \sqrt{GM/r^3}$) $\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0$ $\frac{\partial v_x}{\partial t} = -\frac{1}{\rho} \nabla_x (p + \frac{B^2}{8\pi}) + \frac{(B \cdot \nabla)B_x}{4\pi\rho} + 2\Omega_0 v_y + 3\Omega_0^2 x$ $\frac{\partial v_y}{\partial t} = -\frac{1}{\rho} \nabla_y (p + \frac{B^2}{8\pi}) + \frac{(B \cdot \nabla)B_y}{4\pi\rho} - 2\Omega_0 v_x$ $\frac{\partial v_z}{\partial t} = -\frac{1}{\rho} \nabla_z (p + \frac{B^2}{8\pi}) + \frac{(B \cdot \nabla)B_z}{4\pi\rho} - \Omega_0^2 z$ $\frac{\partial B}{\partial t} = \nabla \times (v \times B - \eta \nabla \times B)$ $\nabla \cdot B = 0$
- Steady-state solution
 - $B = (0, B_y, B_z) \& v = (0, -\frac{3}{2}\Omega_0 x, 0)$
 - $\rho = \rho_0 \exp(-z^2/H^2)$ $(H^2 \equiv 2c_s^2/\Omega_0^2)$: hydrostatic equilibrium

Set up

- Simulation Region : -0.5H < x < 0.5H, -2H < y < 2H, -4H < z < 4H $(N_x, N_y, N_z) = (32, 64, 256)\&(64, 128, 512)$ $(H^2 = 2c_s^2/\Omega_0^2)$
- Boundary : x: shearing, y: periodic, & z: outgoing
 - outgoing boundary ≠ 0-gradient boundary
- Initial Condition
 - Hydrostatic Equilibrium: $\rho = \rho_0 \exp(-z^2/H^2)$
 - Keplerian Rotation : $v_{y,0} = -(3/2)\Omega_0 x$
 - *B*-field : $B_{z,0}$ =const or $B_{y,0}$ =const ($\beta_0 \equiv 8\pi \rho_0 c_s^2 / B_0^2 = 10^4 - 10^7$)
 - Base Model: net B_z with $\beta_0 = 10^6$ (@midplane)
 - v perturbation: $\delta v = 0.005c_s$
- miscellaneous
 - With/Without Resistivity (*B* diffusion)
 - Isothermal Equation of State

Turbulent Viscosity

Angular Momentum Eq. :

$$\frac{\partial}{\partial t}(\rho r v_{\phi}) + \nabla \cdot r \left[\rho v_{\phi} v - \frac{B_{\phi}}{4\pi} B + \left(p + \frac{B_r^2 + B_z^2}{8\pi} \right) e_{\phi} \right] = 0$$

Assuming
$$\partial_t = \nabla_z = \nabla_\phi = 0$$

 $\frac{1}{r} \frac{\partial}{\partial r} \left[\rho r^3 \Omega v_r + r^2 \rho \left(\delta v_\phi v_r - \frac{B_\phi B_r}{4\pi\rho} \right) \right]$
 $\equiv \frac{1}{r} \frac{\partial}{\partial r} \left[\rho r^3 \Omega v_r + r^2 \rho w_{r\phi} \right] = 0,$
where $v_\phi = r\Omega + \delta v_\phi$ (Kepler rot.+perturbation)
 $w_{r\phi}$ = Reynolds stress($\delta v_\phi v_r$) + Maxwell stress($-\frac{B_\phi B_r}{4\pi\rho}$)

For accretion ($v_r < 0$), $w_{r\phi} > 0$.(Outward ang.mom. transport) Note : $w_{r\phi} \equiv \alpha c_s^2$; α is the Shakura & Sunyaev parameter.

Mass accretion rate can be estimated as follows: $\dot{M} = -2\pi r v_r \int \rho dz \approx -2\pi w_{r\phi} /\Omega \int \rho dz$

Time-averaged Vertical Structure



Face-on Views of $1/\beta$

Case I-low (250trot,in) Case II-low (1250trot,in)



Case I-high (250trot,in) Case II-high (1250trot,in)



$$\frac{1}{\langle\beta\rangle_z(t,R,\phi)} = \frac{\langle B^2\rangle_z(t,R,\phi)}{8\pi\langle p\rangle_z(t,R,\phi)}$$

- Case I: More
 Turbulent
- Case II: More
 coherent by Winding

t - z diagram of v_z at $R = 5r_{in}$



The disk winds take a rest for a while. (The intermittency is more random)

MHD Simulations

in a shearing box

• Ideal MHD with isothermal eq. of state

Suzuki & Inutsuka 2009, ApJ, 691, L49 Local with vertical stratification

- Ideal MHD with non-isothermal eq. of state
 lo & Suzuki 2014, ApJ, 780, 46 > y=1.4
- Resistive MHD with isothermal eq. of state

Suzuki, Muto, & Inutsuka 2010, 718, 1289 Dead Zone

in a global box

• Effects of large- / intermediate-scale flows on turbulent *B* field.

Suzuki & Inutsuka 2014, ApJ, 784, 121



 (ρv_z) (disk wind mass flux)





Vertical Differential Rotation ?

Force Balance eqns.:

von Zeipel (1924); Kozlowski (1978)

$$-\frac{1}{\rho}\frac{\partial p}{\partial R} + R\Omega^2 - \frac{\partial \Phi}{\partial R} = 0, \qquad (1)$$

$$-\frac{1}{\rho}\frac{\partial p}{\partial z} - \frac{\partial \Phi}{\partial z} = 0, \qquad (2)$$

Ω: rot.freq.; **Φ**: External Potential Differentiating Eq. (1) with *z* and Eq. (2) with $R \Rightarrow$

$$-\frac{\partial}{\partial z}\left(\frac{1}{\rho}\frac{\partial p}{\partial R}\right) + \frac{\partial}{\partial R}\left(\frac{1}{\rho}\frac{\partial p}{\partial z}\right) + \frac{\partial}{\partial z}(R\Omega^2) = 0.$$
(3)

Globally $p = p(\rho) \Rightarrow$ the 1st and 2nd terms are canceled out:

$$\frac{\partial \Omega}{\partial z} = \mathbf{0} \tag{4}$$

c.f. Taylor-Proudman state

Non-barotropic EoS $\Rightarrow \frac{\partial \Omega}{\partial z} \neq 0$

Global Simulations –Set-up– (2/2)

Assuming locally isothermal gas Case I Case II

• T = const. $\Rightarrow \frac{\partial v_{\phi}}{\partial z} = 0$ (good for MRI studies) $H/R \propto R^{1/2}$

> (not good for disk winds) No Differential Rotation along *z* direction

> > ▶ cT+L.R. ▶ cT+H.R.

• $T \propto r^{-1}$ $\Rightarrow \frac{\partial v_{\phi}}{\partial z} \neq 0$ (not good for MRI studies) H/R = const.(z < 4H)(good for disk winds) Differential Rotation along z direction

von Zeipel 1924: Kozlowski 1978: Takeuchi & Lin 2002

- Simulations:spherical coordinates (r, θ, ϕ)
- Data Analyses: cylindrical coordinates (R, ϕ, z)

Type I Migration

Armitage 2005



Gravitational Interaction of a Planet with Gas \Rightarrow Migration of Planet by (tiny) \pm force Difference. Mostly inward migrate with :

$$\tau_{\text{mig,I}}(r) \approx 5 \times 10^4 \text{yr} \left(\frac{4.35}{2.7+1.1s}\right) \left(\frac{\Sigma(r)}{\Sigma_0}\right)^{-1} \left(\frac{M}{M_{\oplus}}\right)^{-1}$$
(Tanaka et al.2002)
Surface density is a key

Description of Time Evolution

- No Disk Winds Approach to $\exp(-r/r_{
 m s})/r.($ Lynden-Bell & Pringle 1974)
- Disk Winds
 - Mass Flux:

 $(\rho v_z)_w = C_w \rho_{mid} c_s \propto C_w \Sigma \Omega \propto \Sigma r^{-3/2}$ \propto Keplerian Frequency

- Dispersal Time (if no accretion) :
 - $\tau = \Sigma/(\rho v_z)_w \propto r^{-3/2}$ "Dynamically Evaporate" Inside-Out (controlled via τ_{dyn})
- Switching-on accretion & disk winds
 ⇒ an expanding inner hole

Disks with inner holes ⇔ Transitional Disks ?

Time Evolution of B_{ϕ} –contd.– From a viewgraph by Dr. R. Matsumoto

(Nishikori et al.2006; Machida et al.2013)



Amplification of *B*-field



MagnetoRotational Instability Parker Instability (Magnetic Boyancy)

 B_{φ} Generation by Differential Rotation

MRI: triggering MHD turbulence