

TI with conduction & turbulence

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key contributors: B Wagh, M McCourt, N Banerjee

Wagh et al. 2014, MNRAS
Banerjee & Sharma 2014, MNRAS

TI paradigm

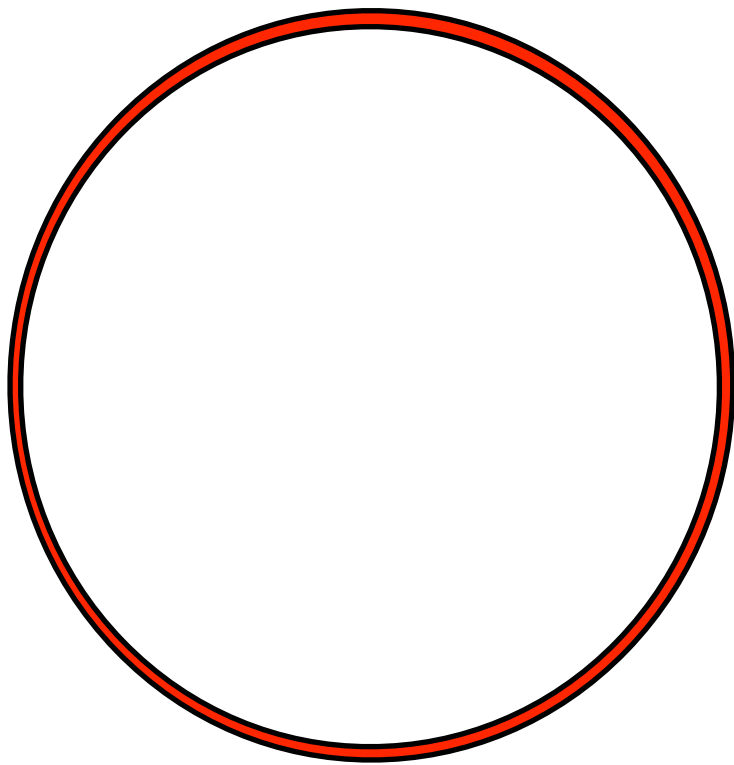
- cooling flows are absent; heating $\approx$ average cooling
- interplay of gravity & local TI in globally stable ICM
- behavior reproduced by realistic jets
- holds with anisotropic conduction
- role of turbulent heating/mixing

Toy model

heating~cooling at every radius
(must be true to some degree to prevent cooling flows)

$$q^+(r, t) = \langle n^2 \Lambda(T) \rangle$$

hydrostatic equilibrium: $dp/dr = -\rho g$
gravity due to dark matter



how far can we go with this
simple model?

“Entropy” ($K=T/n_e^{2/3}$)

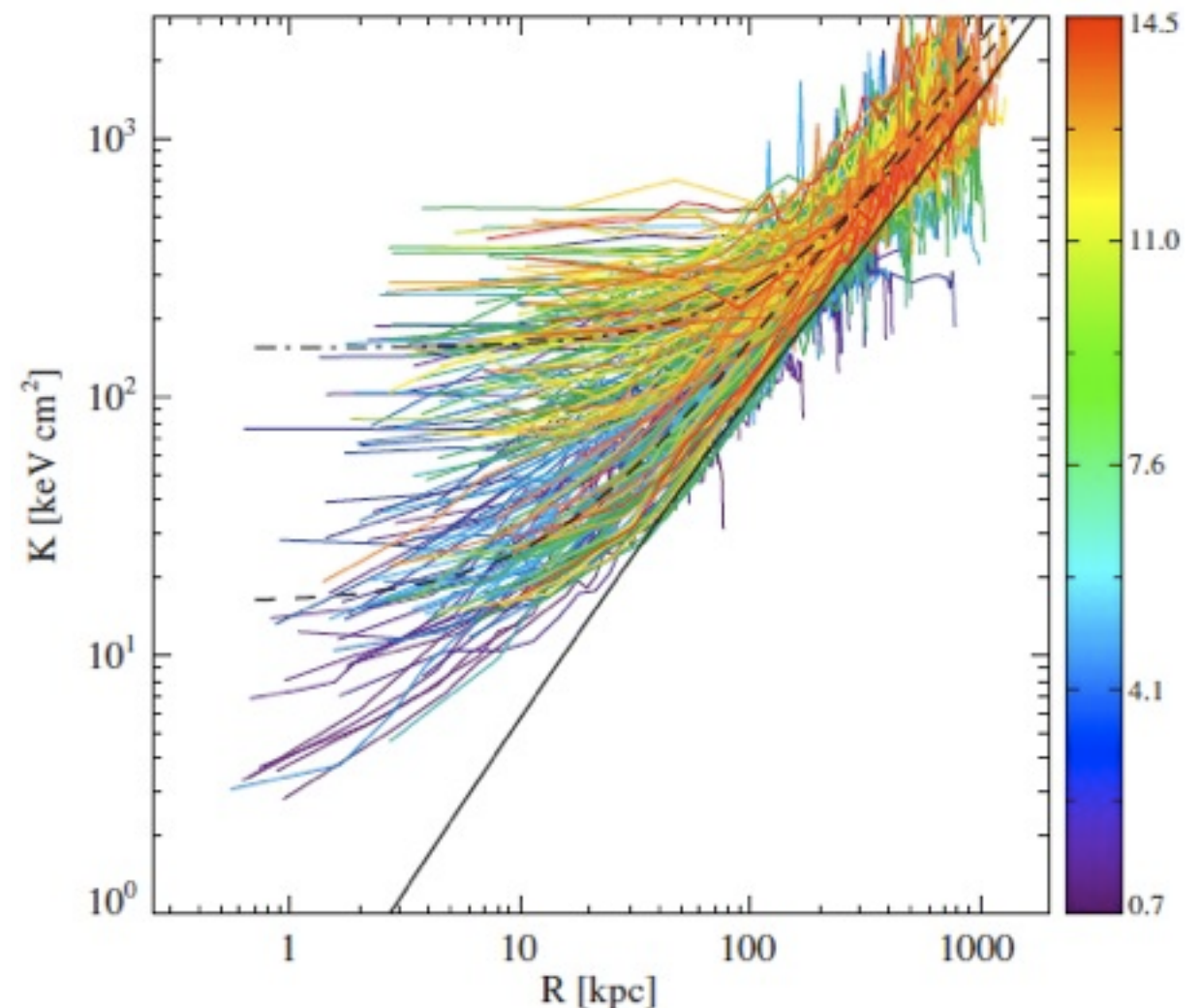
entropy tracks non-adiabatic
htg./cooling

$K(r)$: history of gas accn.

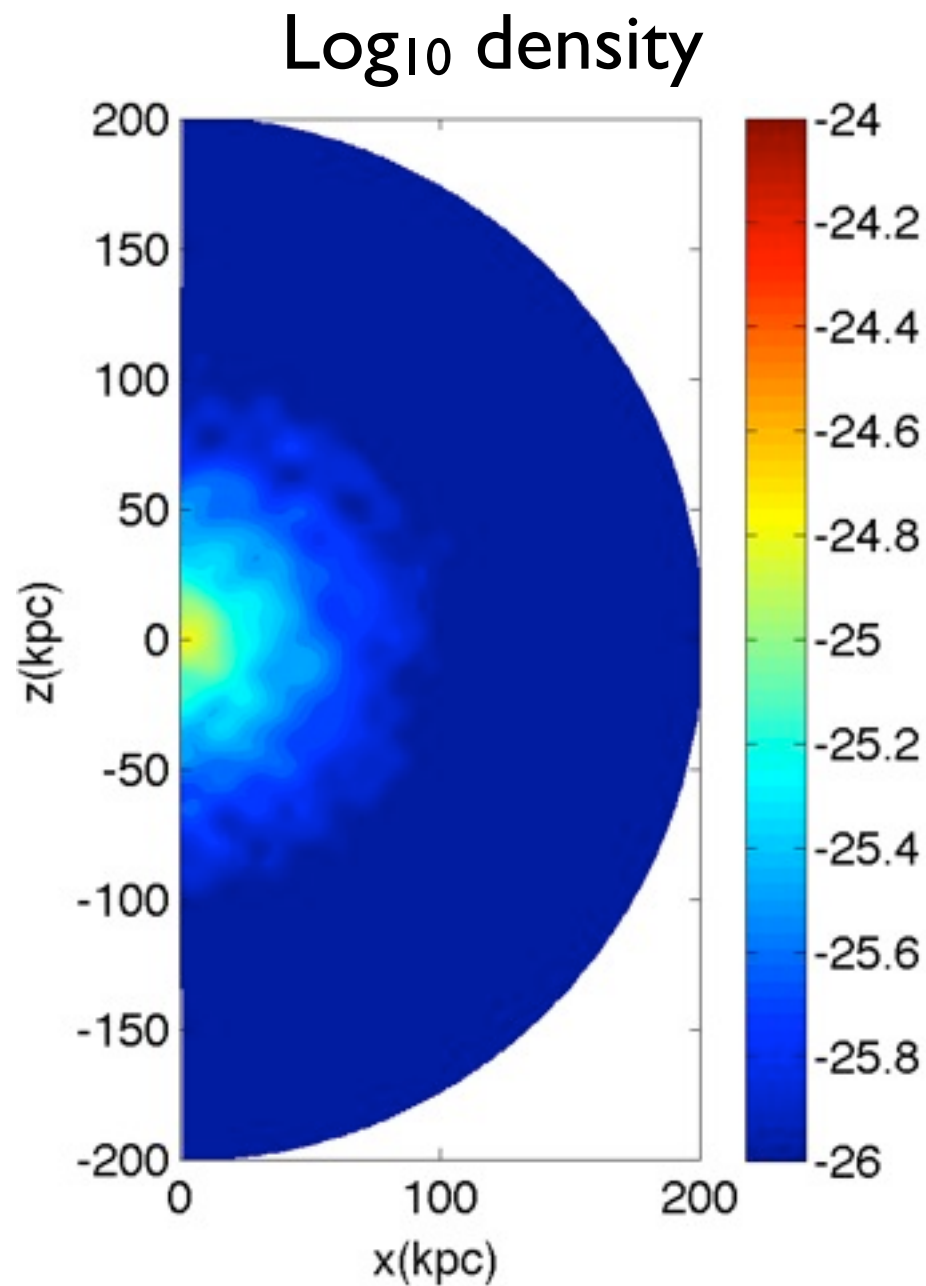
$$K(r) = K_0 + K_{100}(r/r_{100})^\alpha$$

large $K \iff$ low ICM density

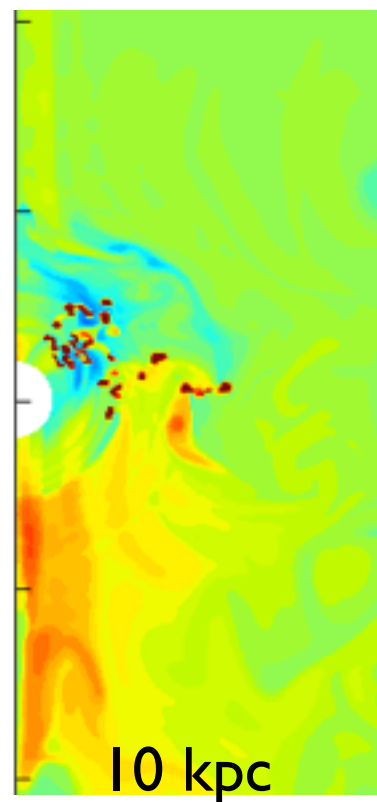
[Cavagnolo et al. 2009]



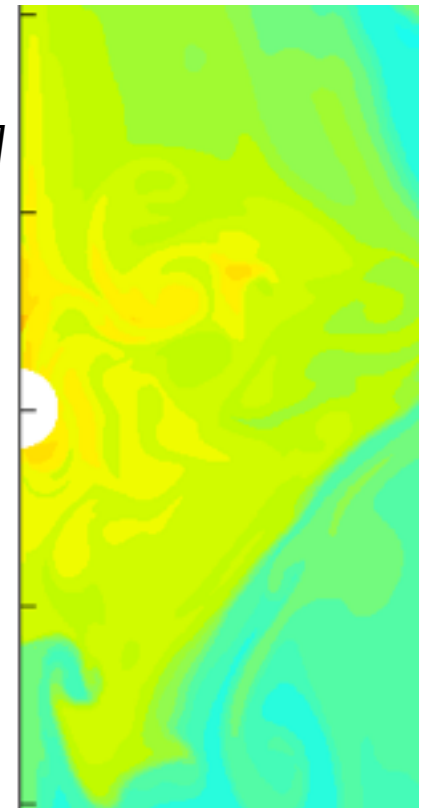
Spherical Sims. Clusters



multiphase only hot phase
if $t_{\text{cool}}/t_{\text{ff}}$ small! if $t_{\text{cool}}/t_{\text{ff}}$ big!



[Sharma et al. 2012]



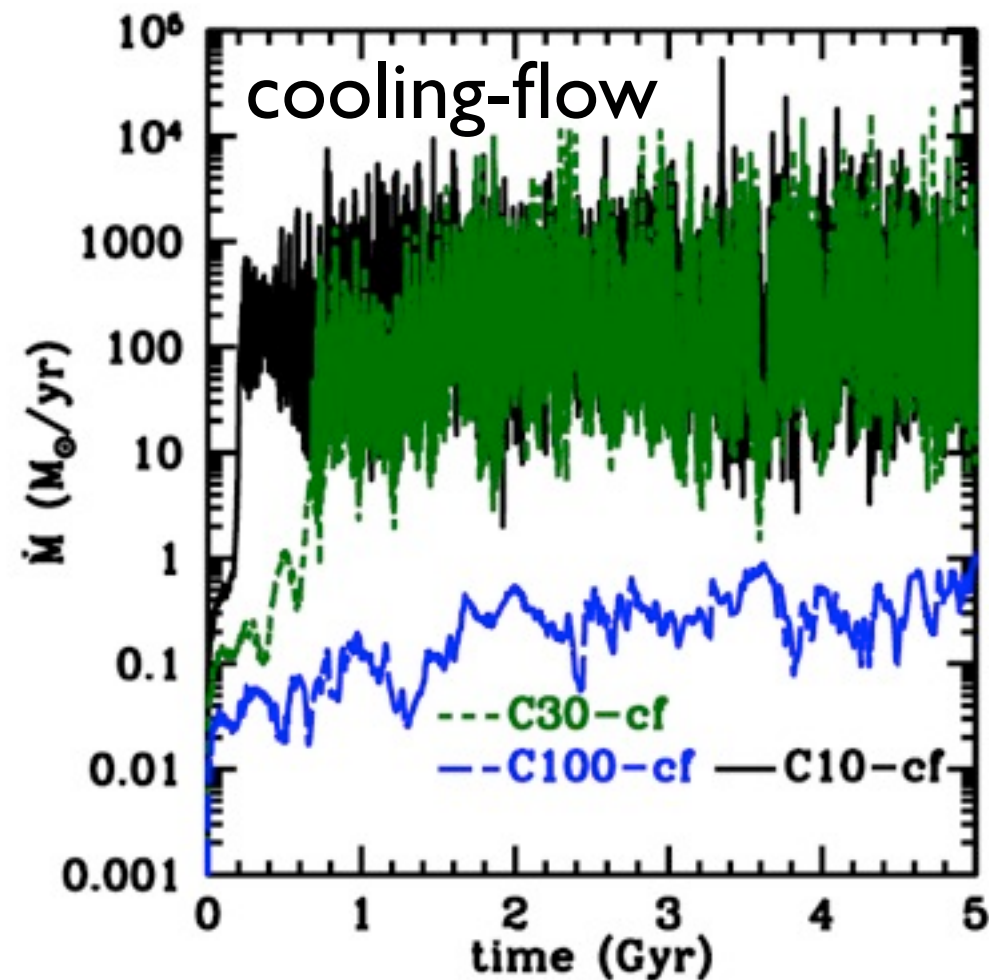
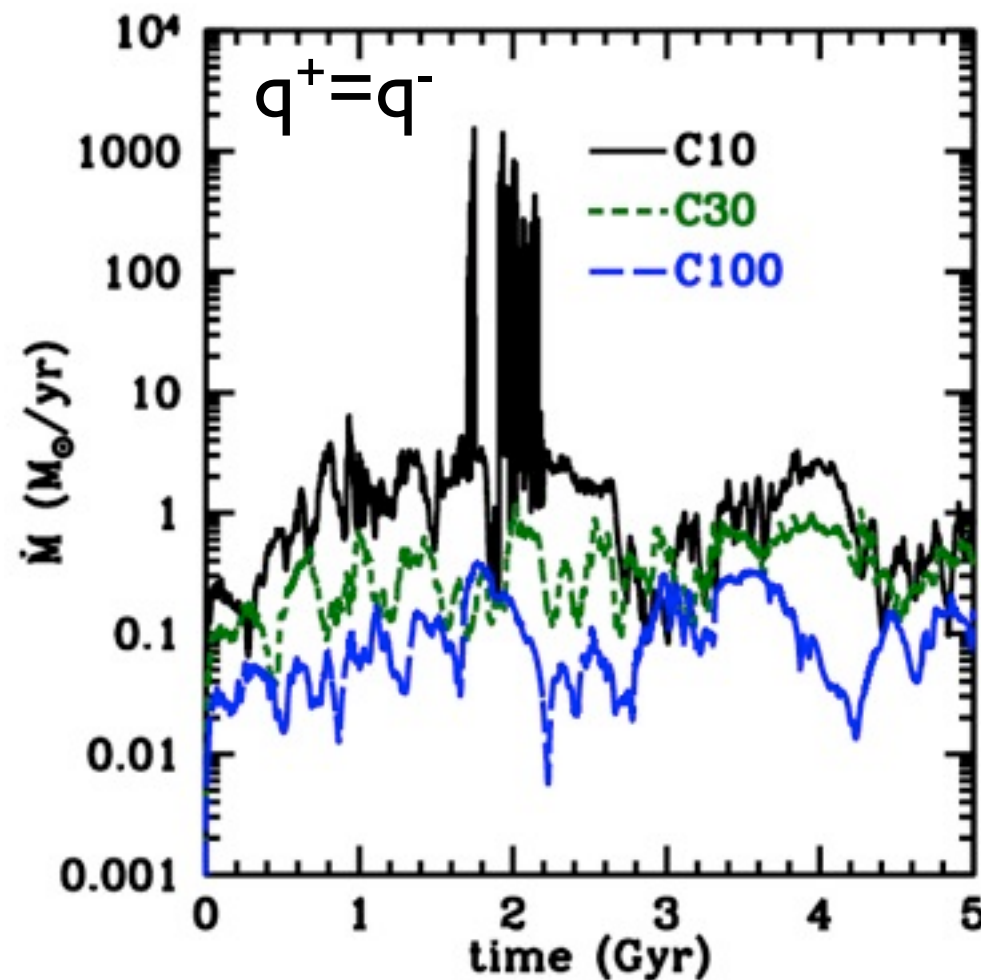
cool filaments when $t_{\text{TI}}/t_{\text{ff}} < 10$
spherical compression is quantitatively imp.

need to understand this from analytic/phenomenological calculations

$q^+ = q^- \Rightarrow$ small dM/dt
as observed

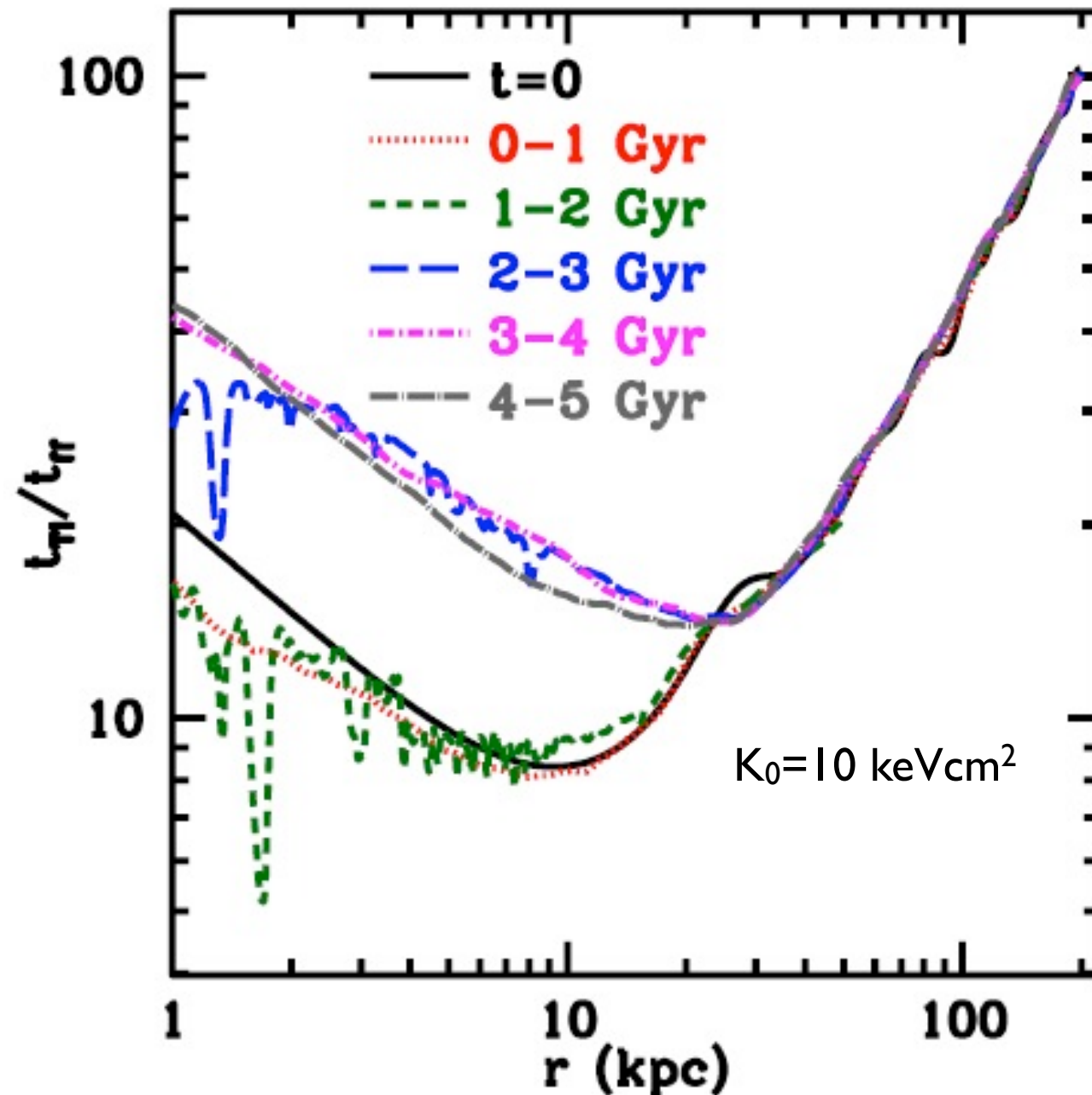
$\varepsilon \sim 10^{-3}$

[Sharma et al. 2012]



$dM/dt \sim 0.01 dM/dt \text{ CF, as observed}$

Self-Adjustment of ICM

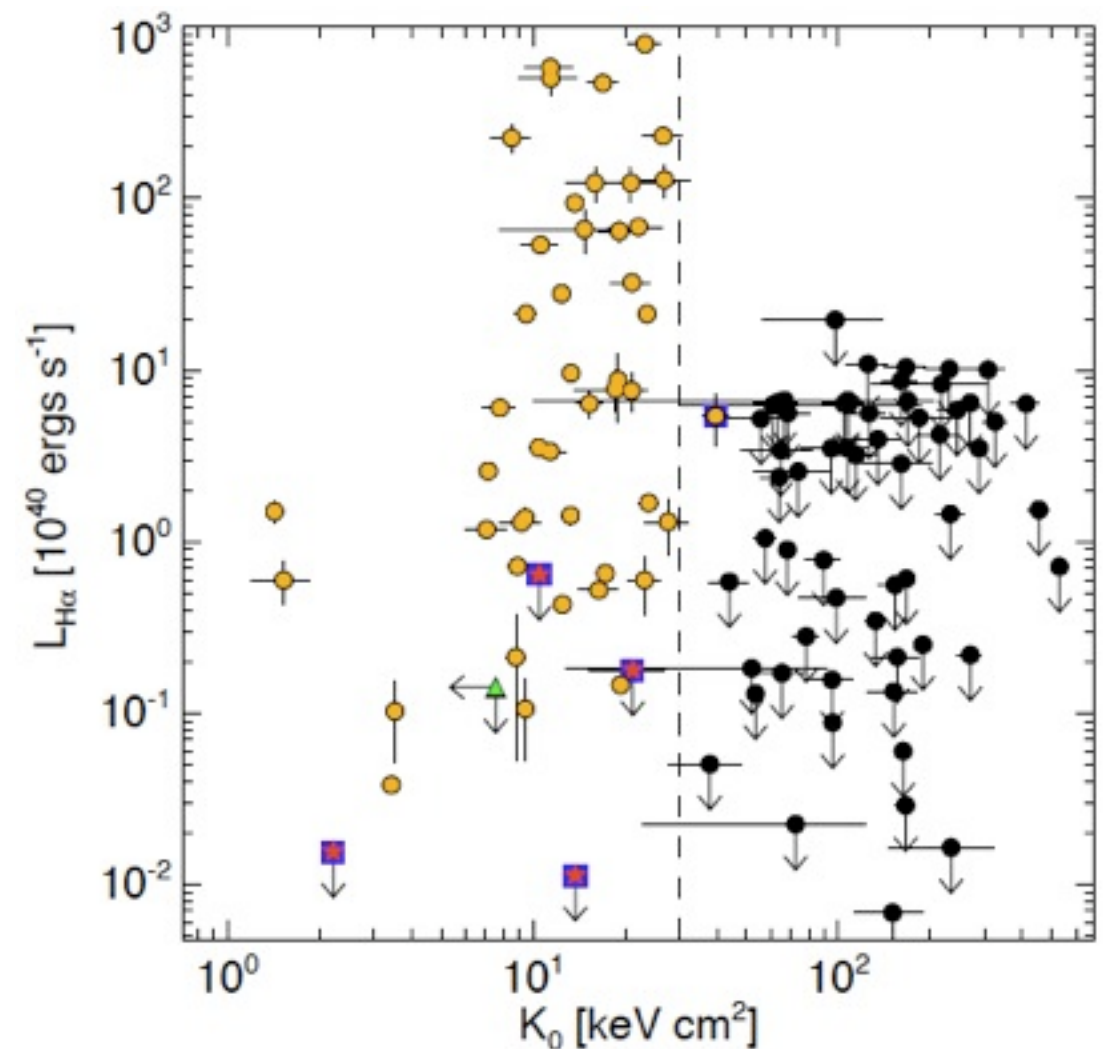
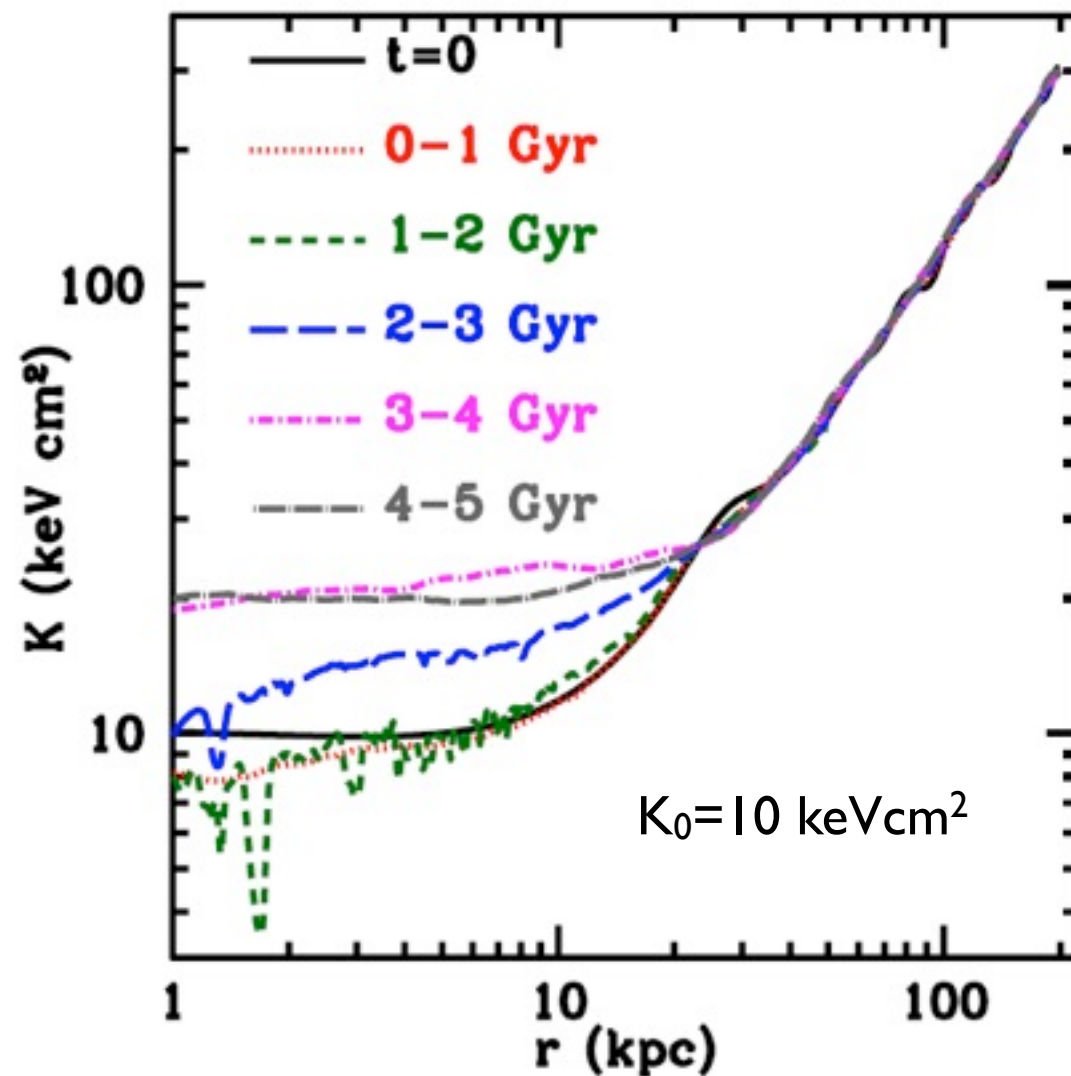


mass dropout if $t_{Tl}/t_{ff} < 10$
CC clusters at $t_{Tl}/t_{ff} \sim 10$

even if we start w. much
lower K_0 or t_{Tl}/t_{ff}

Self-Adjustment of ICM

[Cavagnolo et al. 2008]



$$t_{\text{cool}}/t_{\text{ff}} \approx 10$$

CC/NCC division corresponds to
our $t_{\text{cool}}/t_{\text{ff}}$ criterion!

Core vs. halo mass

[Sharma et al. 2012]

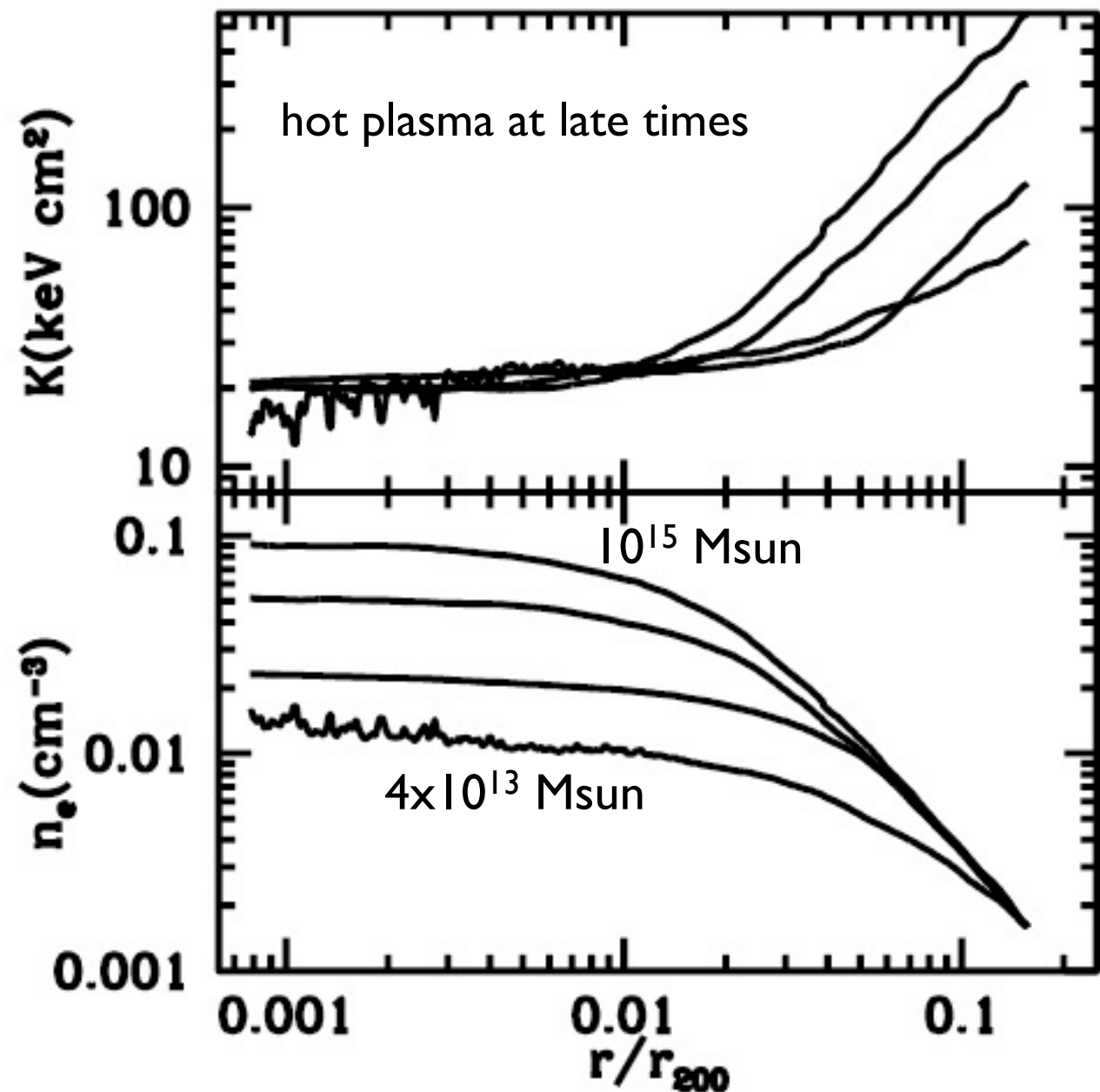
$$t_{\text{cool}} \sim T/n\Lambda \sim T^{1/2}/n$$

cooling more imp. for lower
mass halos

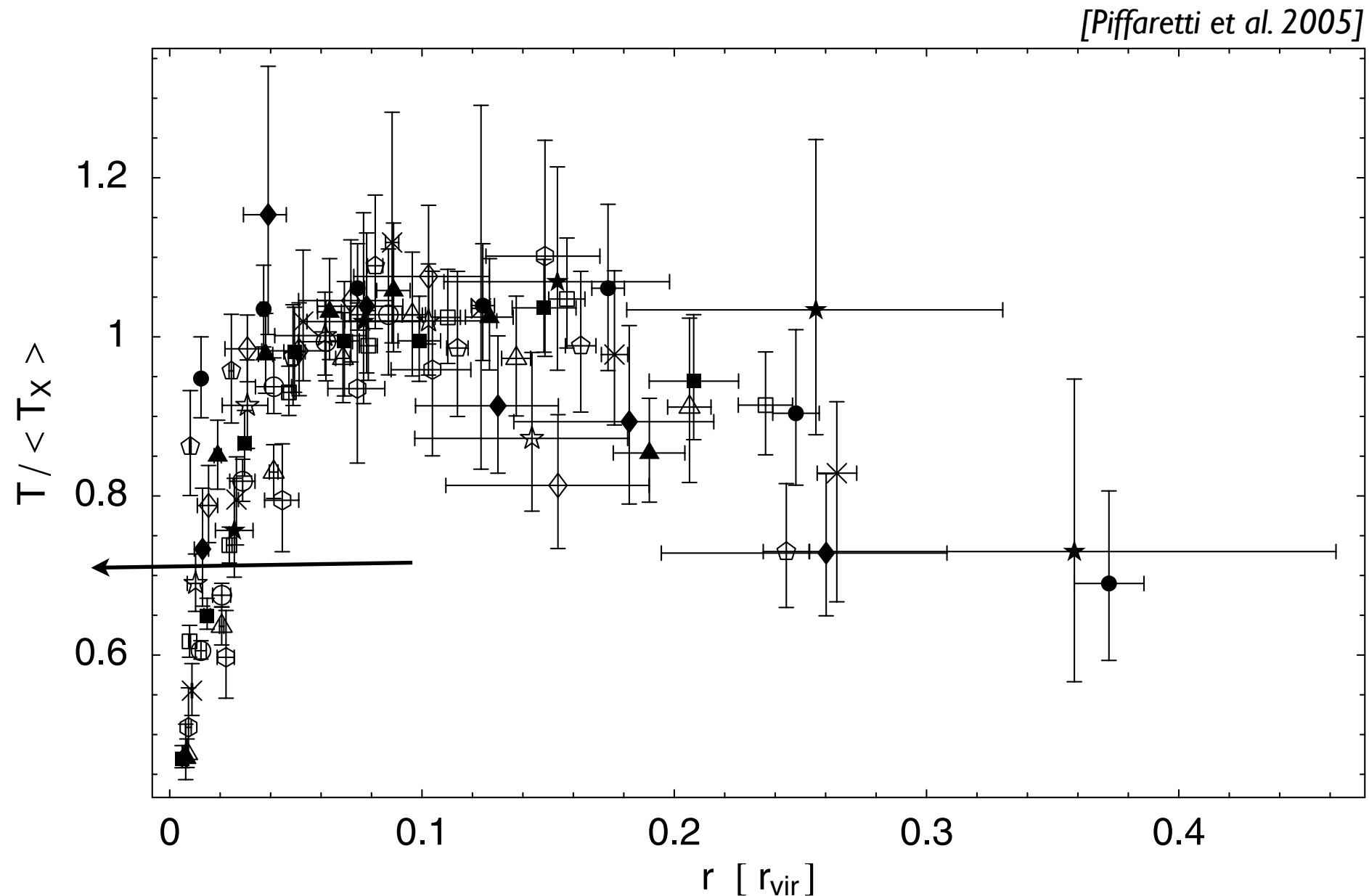
bigger & lower density cores
for groups vs. clusters

entropy almost the same for
diff. halos => smaller halos
overheated => steepening of
 L_X - T_X reln.

$$t_{\text{cool}}/t_{\text{ff}} < 10$$



Effects of Conduction

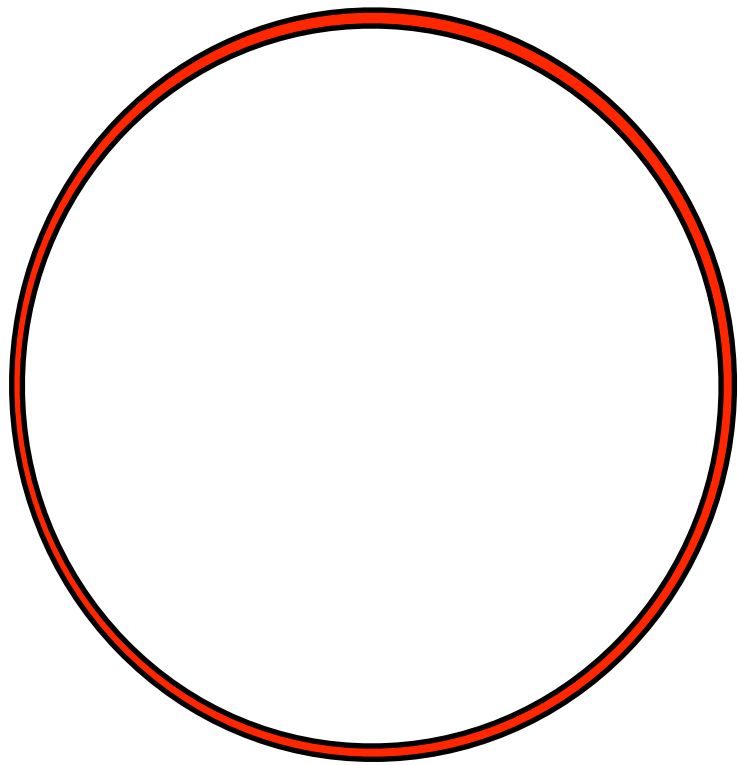


thermal conduction can, in principle, bring in heat from larger radii

Problems w. conduction

- globally unstable
- HBI shuts of conduction
- still can play a key role in energetics
- numerics: no MPI code for implicitly doing aniso. conduction

Conduction & cold gas



generalize the simple toy model but accounting
conductive heating in energetics

$$q^+(r, t) = \langle n^2 \Lambda(T) \rangle + \nabla \cdot \vec{q}$$

How do isotropic & anisotropic conduction change the picture?

in addition to $t_{\text{cool}}/t_{\text{ff}}$, conduction is expected to suppress TI

Why conduction in core?

[Voit et al. 2008]

$$\lambda_F \equiv \left[\frac{T\kappa(T)}{n^2\Lambda(T)} \right]^{1/2} = 4 \text{ kpc} \left[\frac{K}{10 \text{ keV cm}^2} \right]^{3/2} f_c^{1/2}.$$

Field length, below which conduction prevents local TI

expect *isotropic* conduction to prevent condensation
when Field length > core size; not so for *anisotropic*

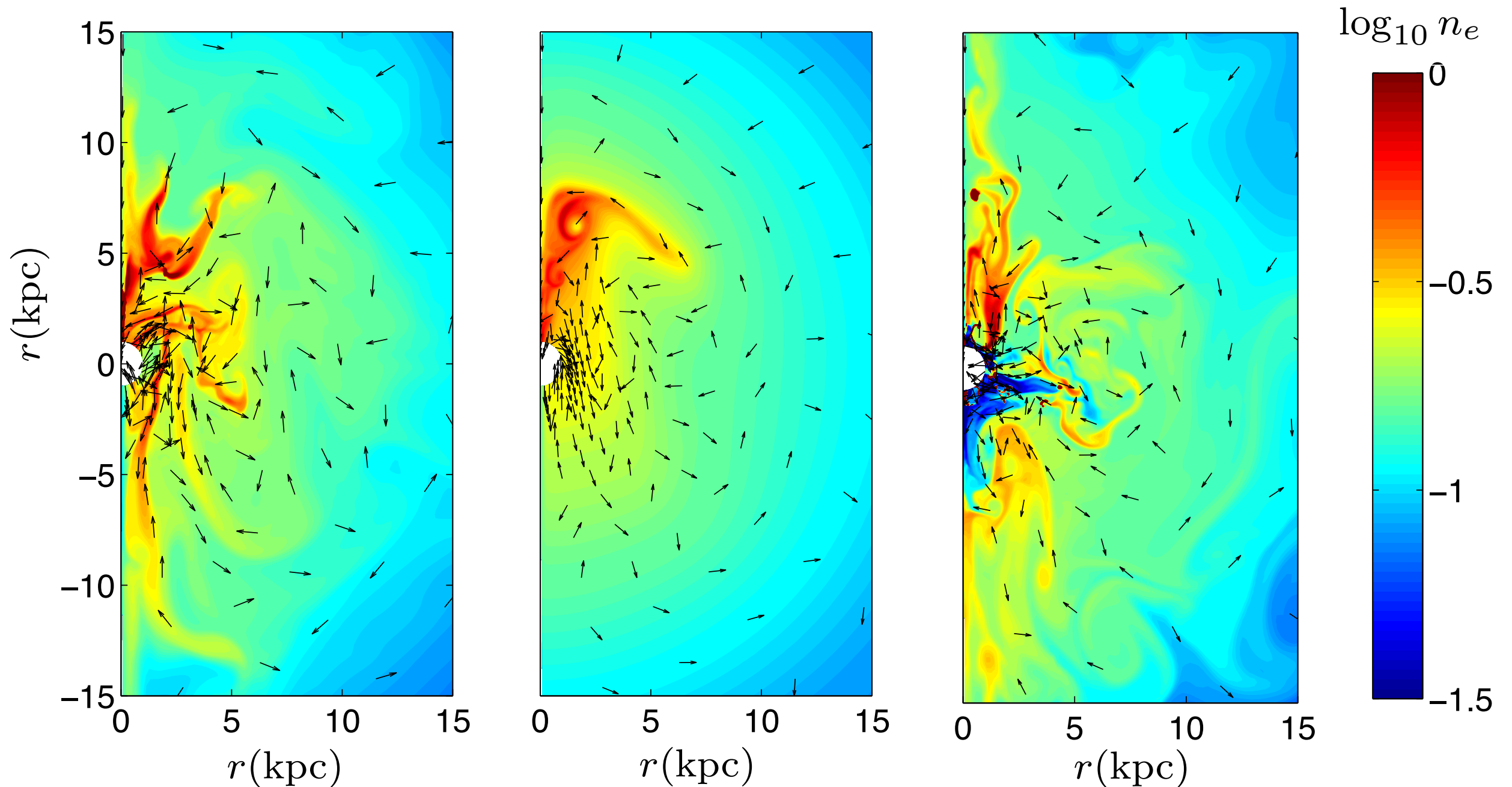
Morphology

[Wagh et al. 2014]

aniso. cond.

iso. cond.

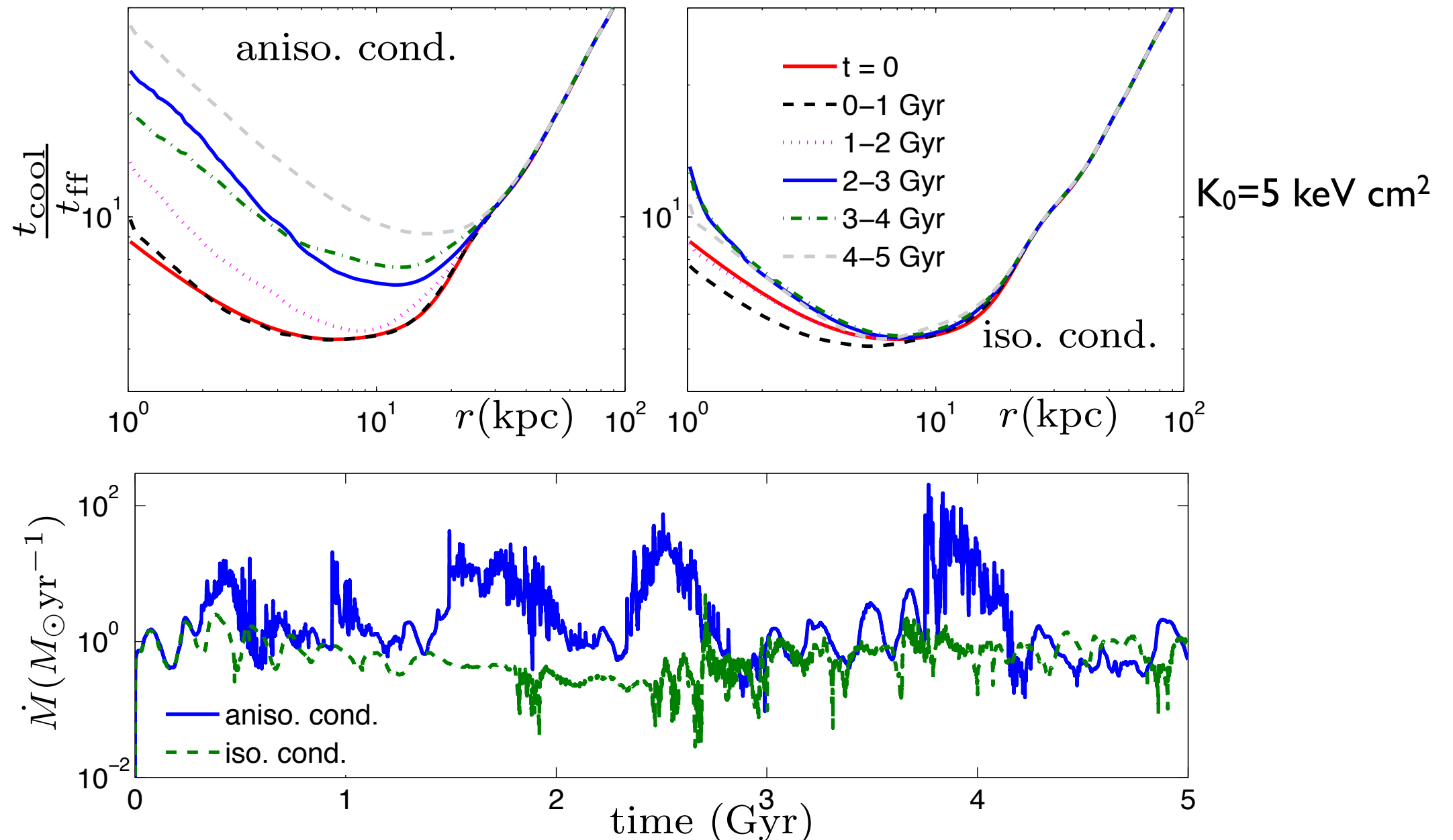
no cond.



halo mass $3.8 \times 10^{14} M_{\text{sun}}$; split monopolar $B \sim 1 \mu\text{G}$; $K_0 = 5 \text{ keV cm}^2$
sim. with aniso. conduction much closer to hydro

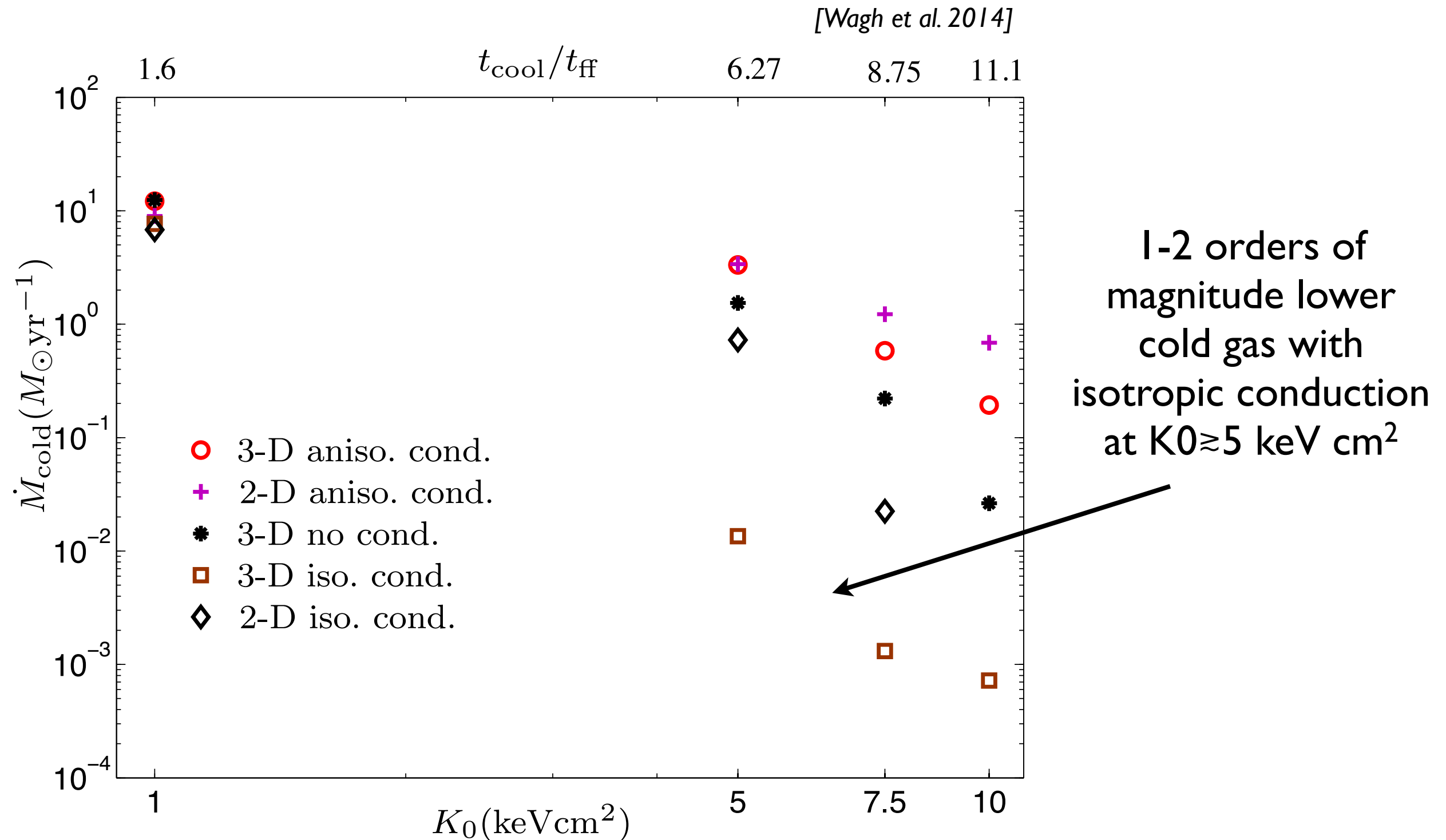
Anisotropic vs Isotropic

[Wagh et al. 2014]

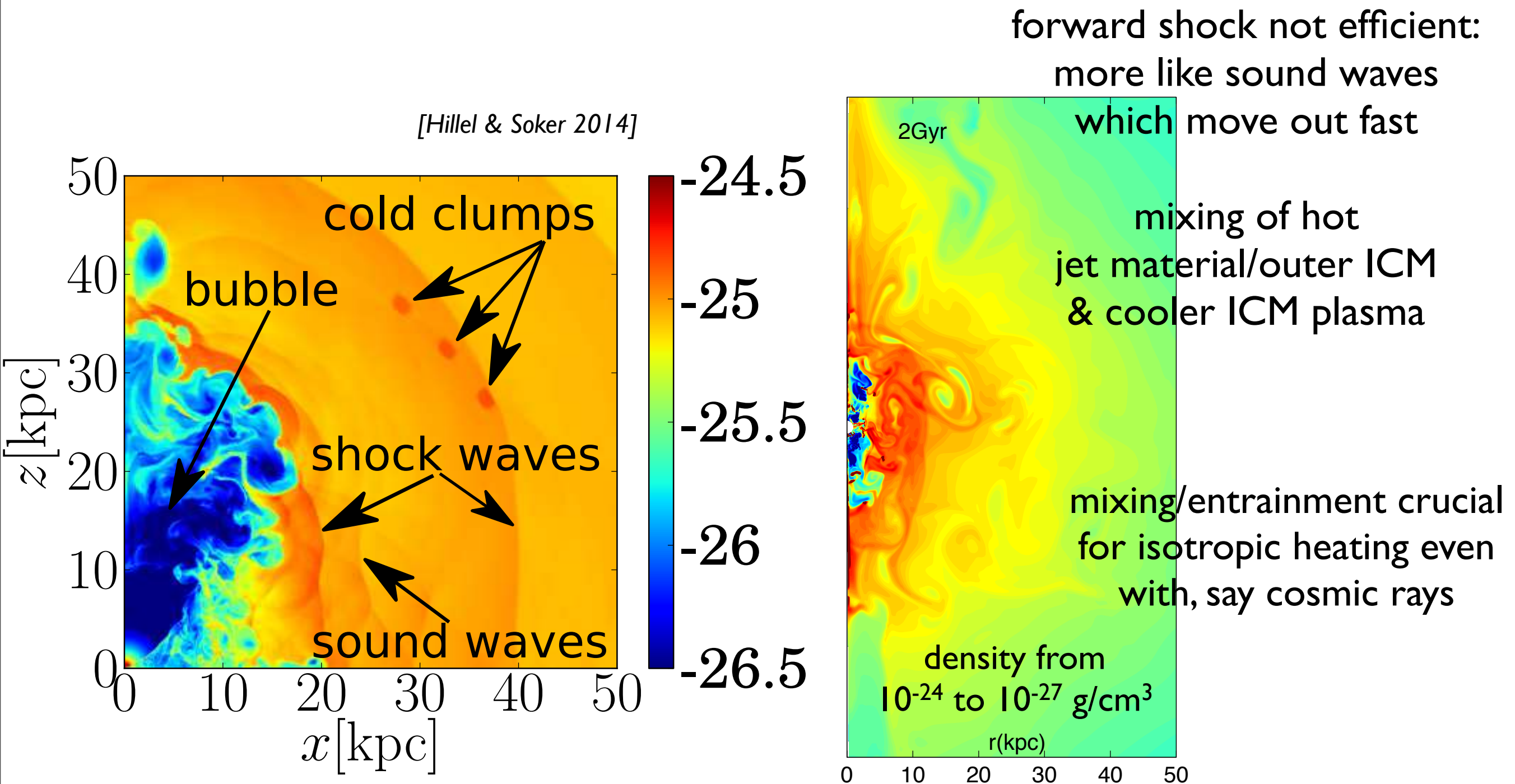


much smaller cold gas condenses with isotropic conduction
because of suppression of TI by conduction
difference is more pronounced for massive clusters

Cold gas accretion

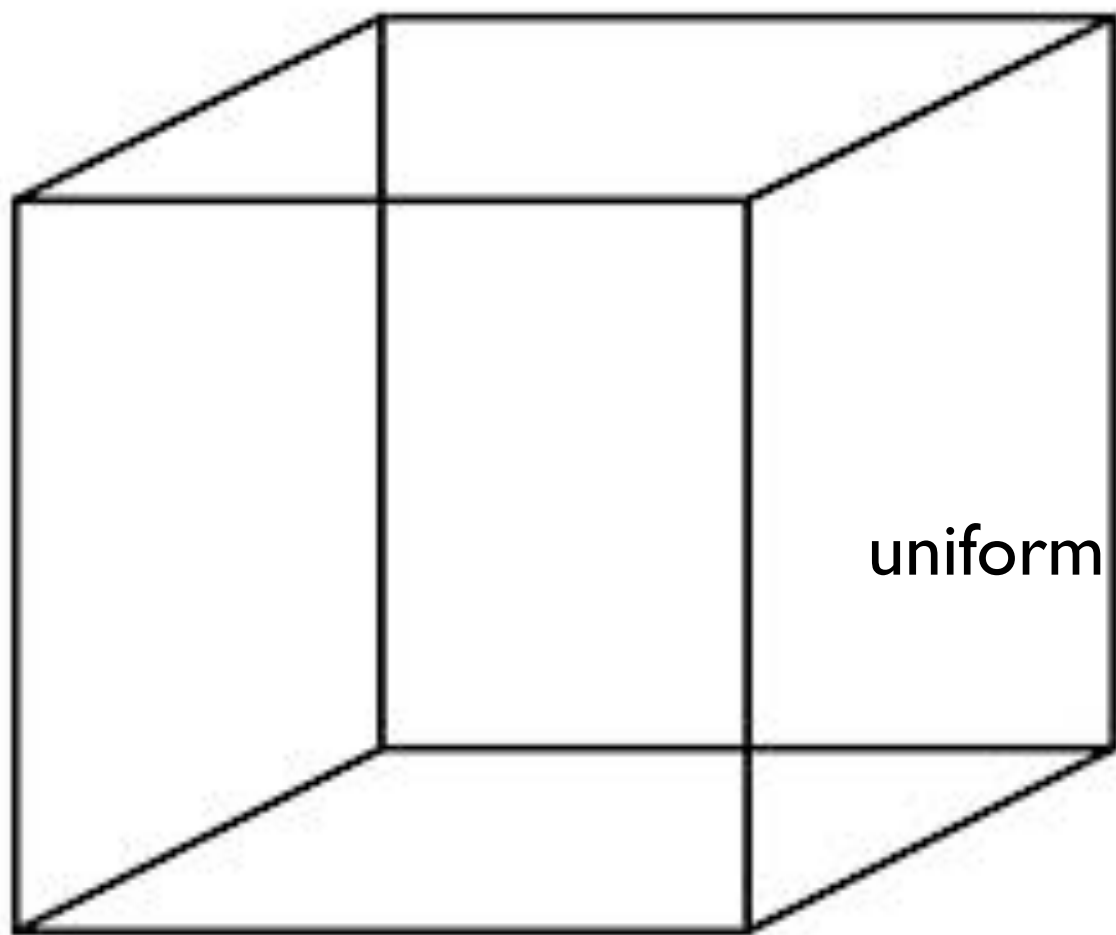


What heats cool cores?



N Experiments with Turbulent Heating/Mixing

[Banerjee & Sharma 2014]



uniform box

$$\frac{\partial(\rho \vec{v})}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v} \otimes \vec{v} + P^* I) = \vec{F},$$

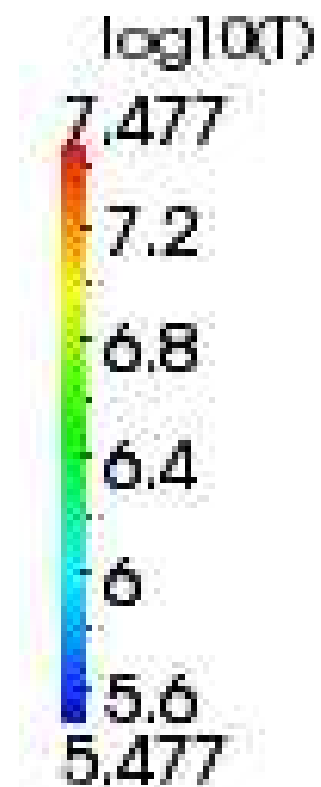
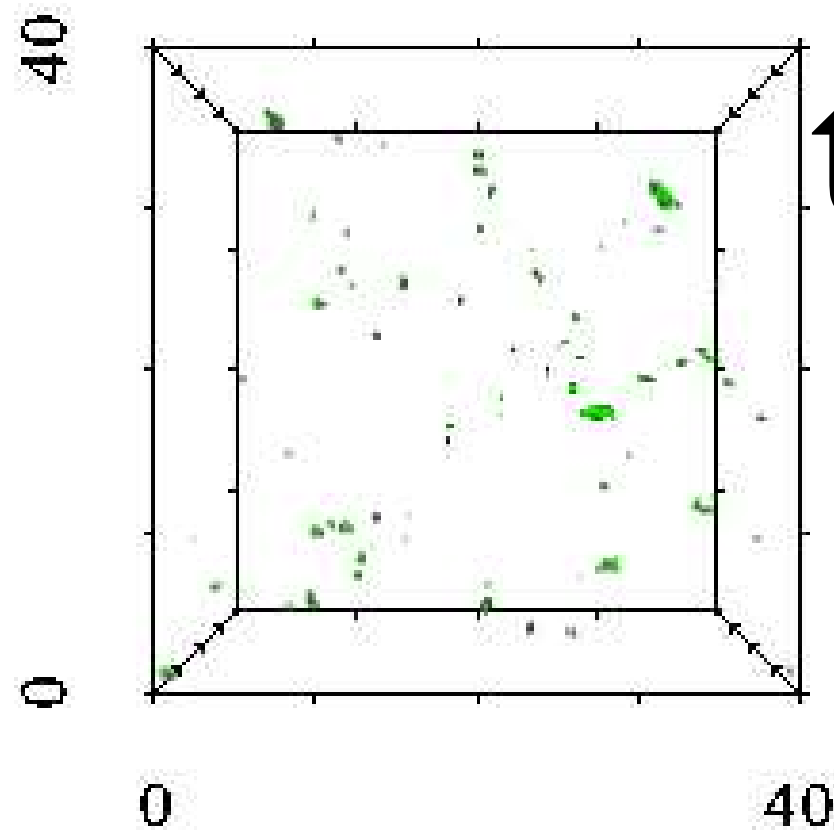
$$\frac{\partial E}{\partial t} + \vec{\nabla} \cdot \{ (E + P^*) \vec{v} + (\vec{B} \cdot \vec{v}) \vec{B} + \vec{Q} \} = \vec{F} \cdot \vec{v} - \mathcal{L},$$

$$\langle \vec{F} \cdot \vec{v} \rangle = \langle \mathcal{L} \rangle$$

turbulence driven at 10 kpc

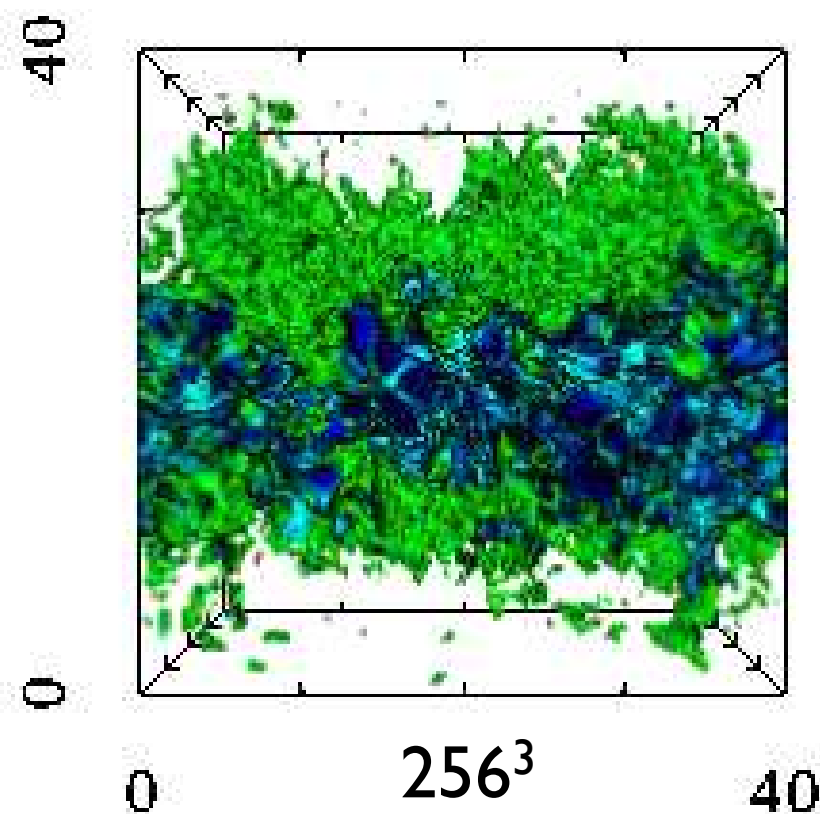
work done by turbulent force balances cooling over the box, on average
mimicking heating due to jet-induced turbulence

Multiphase gas w. turbulence



only large-enough clouds can
condense out smaller ones are
mixed faster than they can cool

$L = 10$ kpc is the driving scale



Scalings

L is the driving scale

$$\rho v_L^3 / L = 2K / t_{\text{mix,L}} \approx n^2 \Lambda = U / t_{\text{cool}}$$

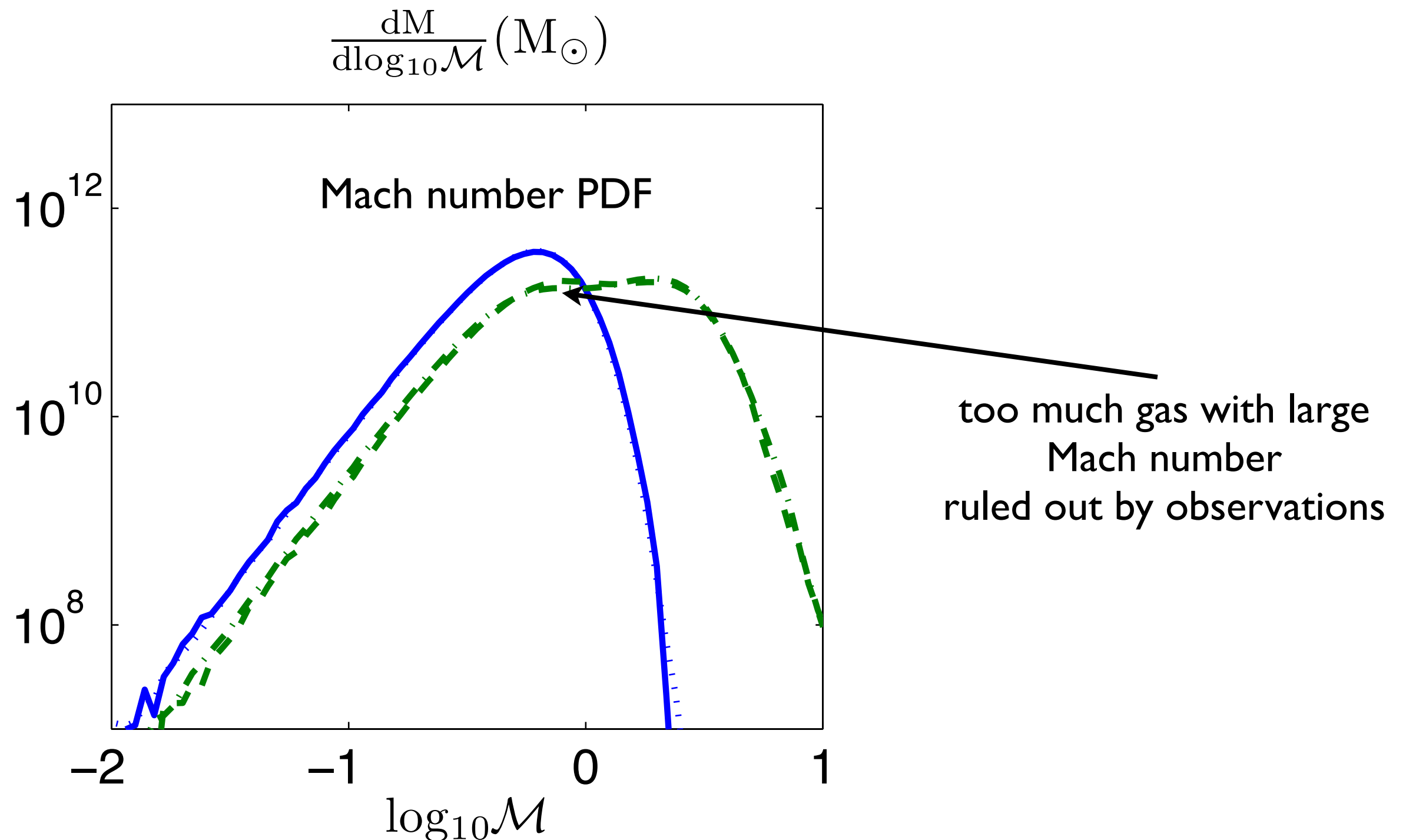
$$t_{\text{mix,L}} / t_{\text{cool}} \approx 2K / U \approx \mathcal{M}^2 \gtrsim 1 \quad \text{for condensation}$$

implies that clouds condense out at large scales
& turbulence is close to sonic; ruled out for CCs!

$2K / U \approx \mathcal{M}^2$ can be < 1 , but $t_{\text{mix,L}} < t_{\text{cool}}$ in this case

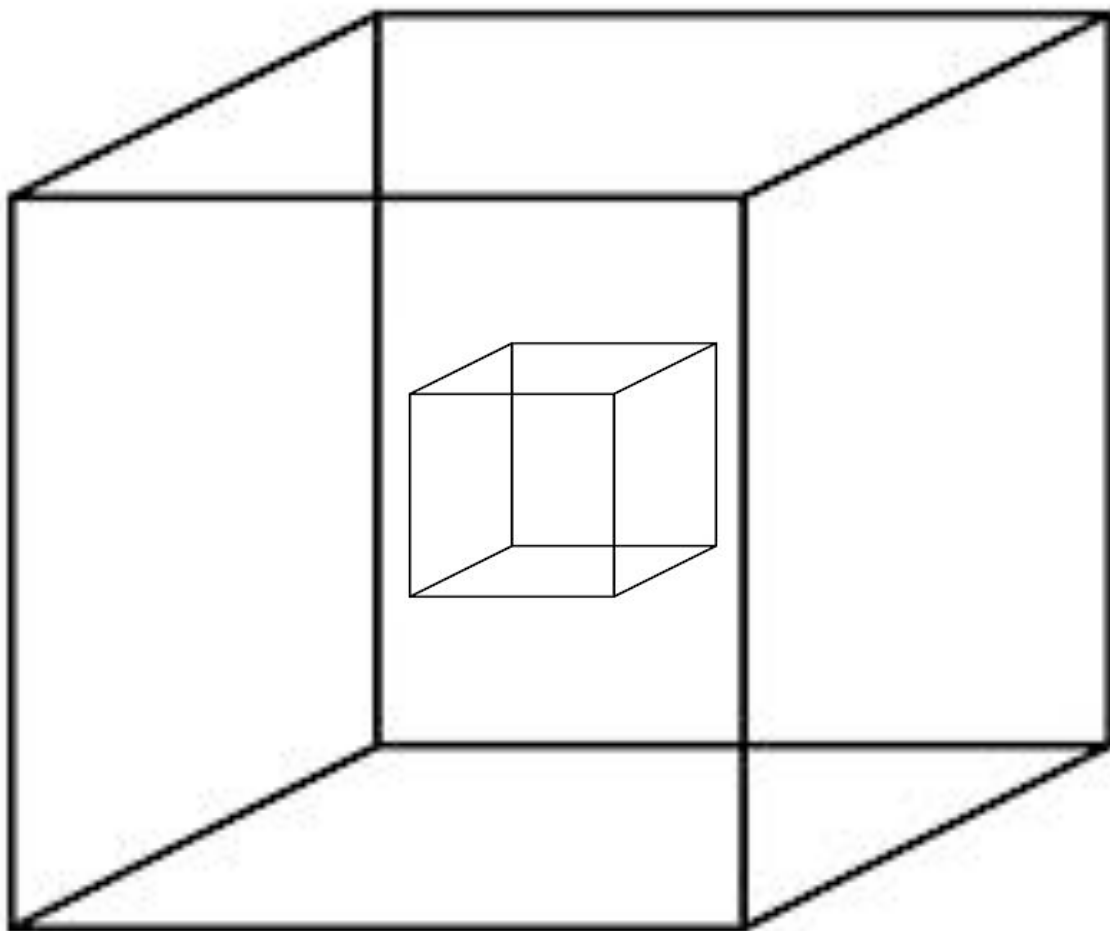
can't have condensation as seen in CCs

Turbulent htg. ruled out



Turbulent Mixing?

[Banerjee & Sharma 2014]



small box, represents the cool core

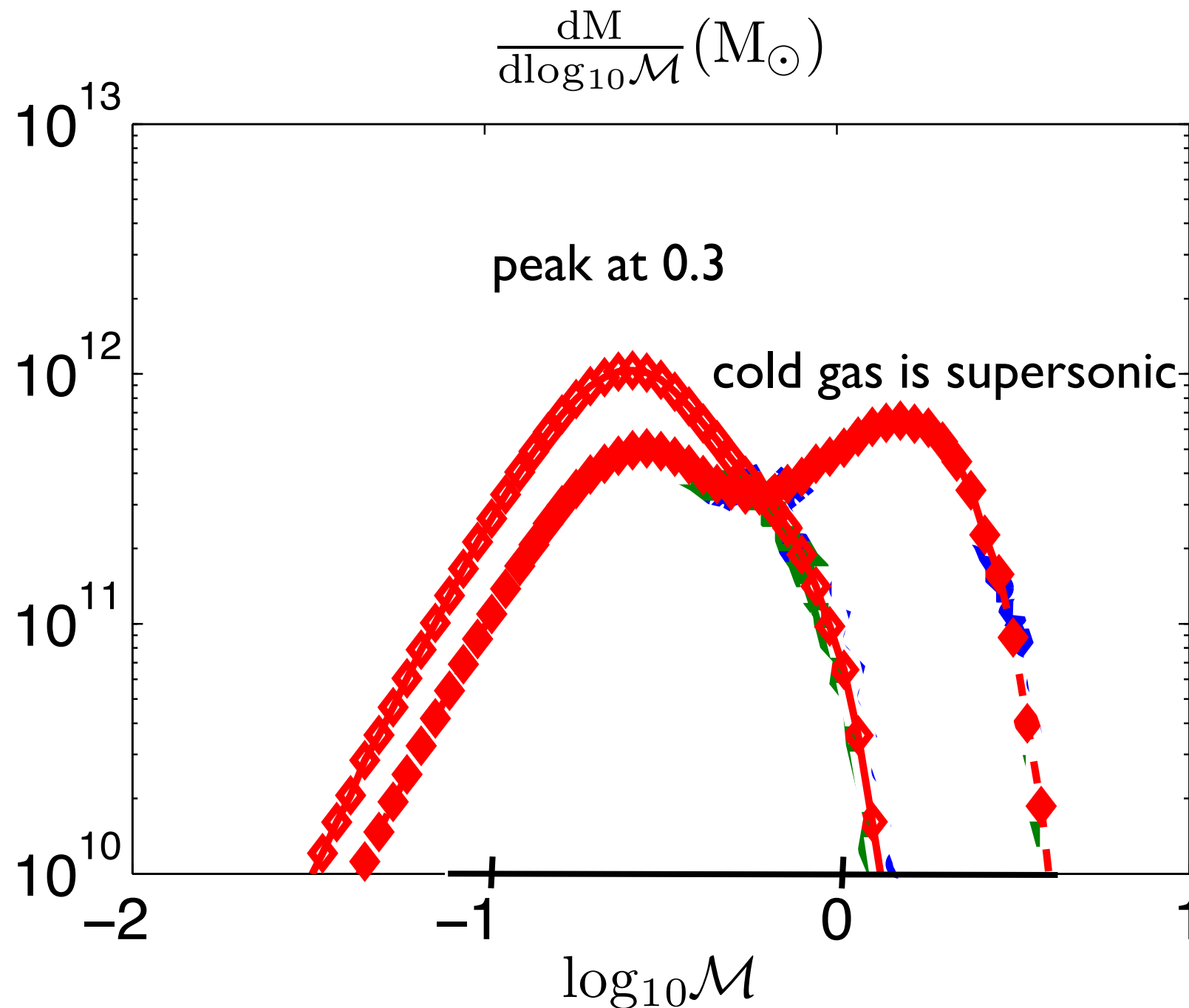
outer region is bubble material or
hotter dilute regions of ICM

turbulence mixes the hotter gas
with the denser core

$$\langle F \cdot v \rangle = \langle \mathcal{L} \rangle$$

still, but lower velocities because the dilute
outer regions have longer cooling times &
larger volume

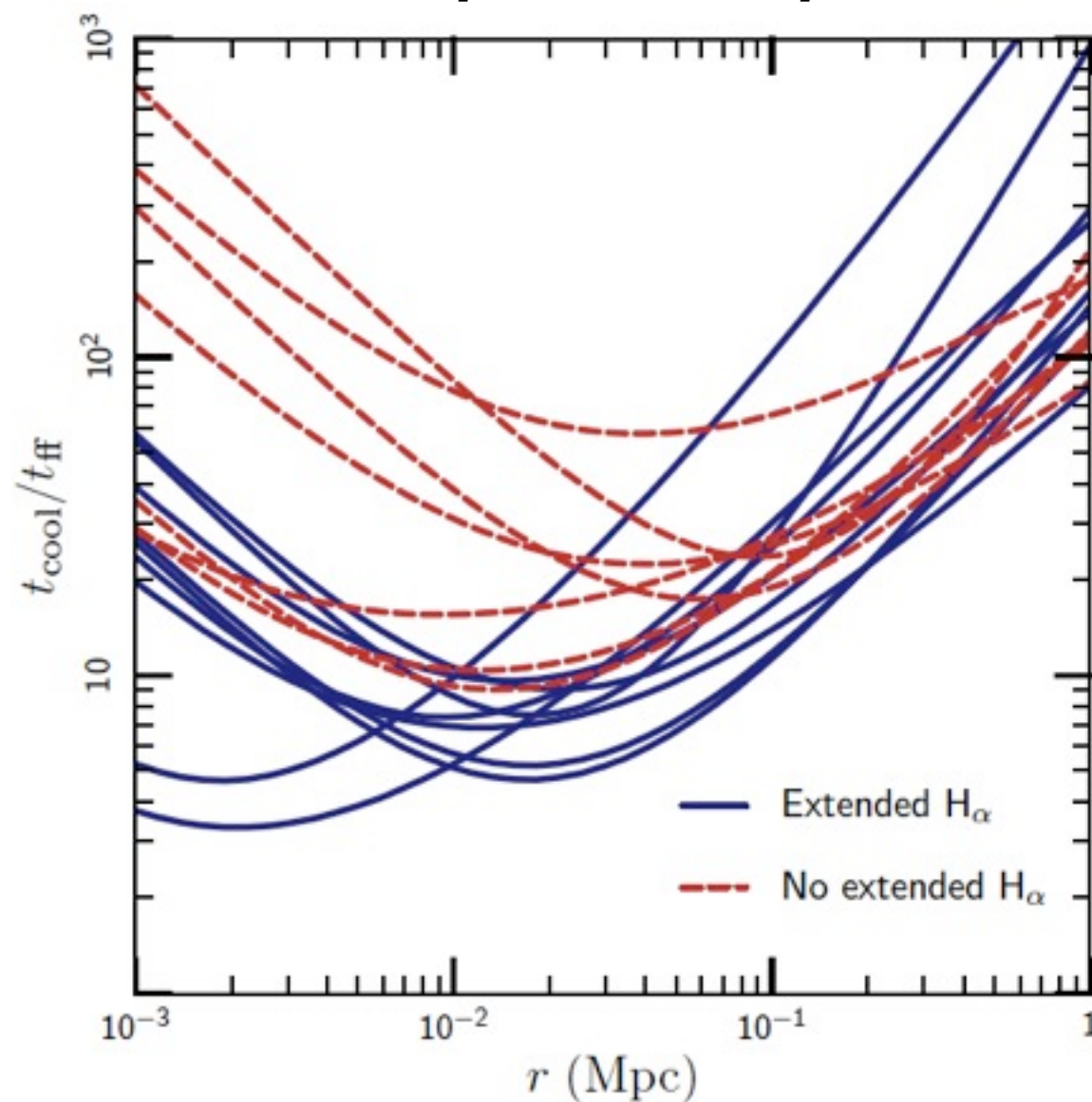
Mach no. with mixing



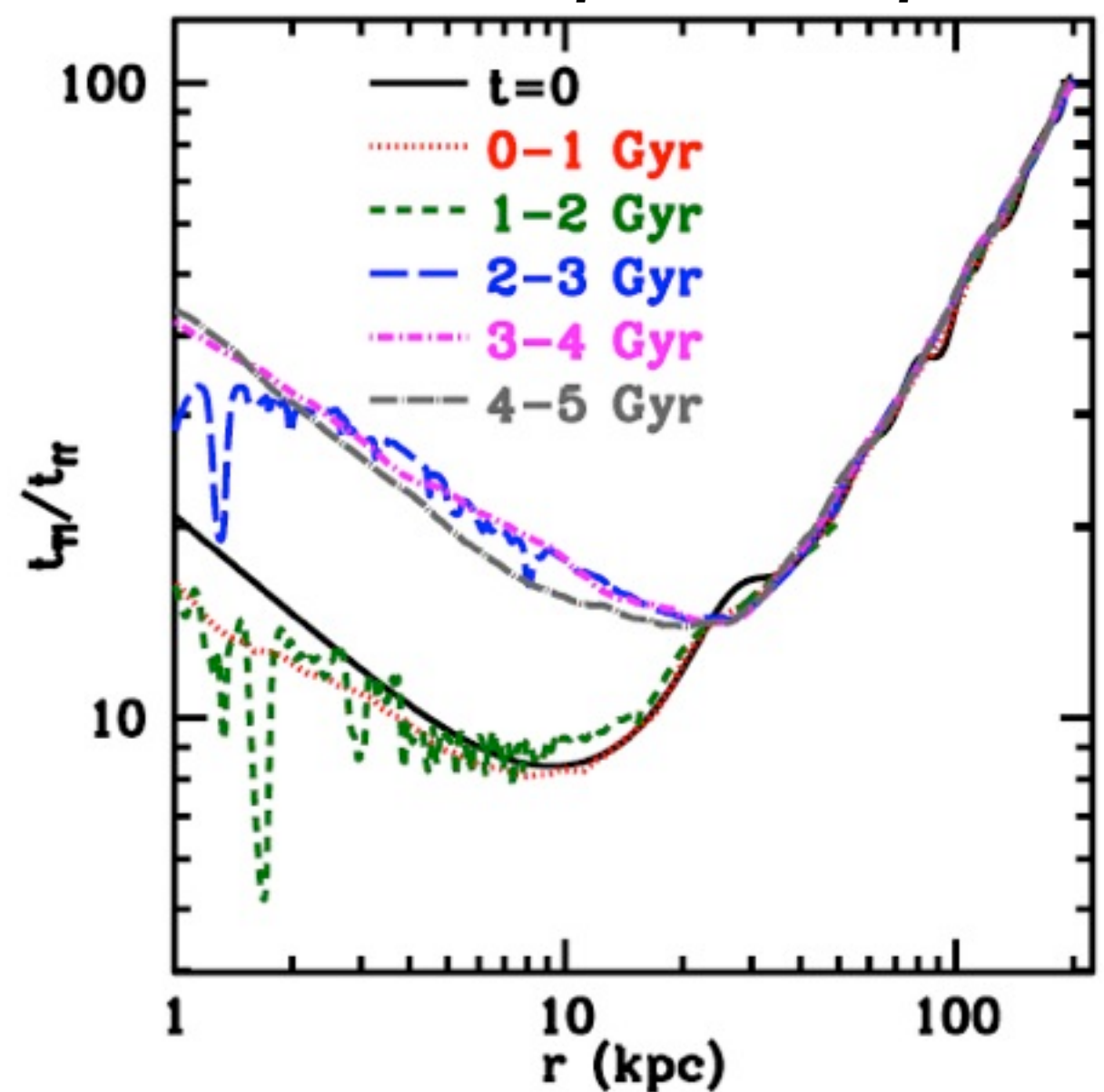
mixing gives a Mach number
consistent with observations
of cool core clusters

Data=> $t_{\text{cool}} \approx t_{\text{TI}}$

[McCourt et al. 2012]



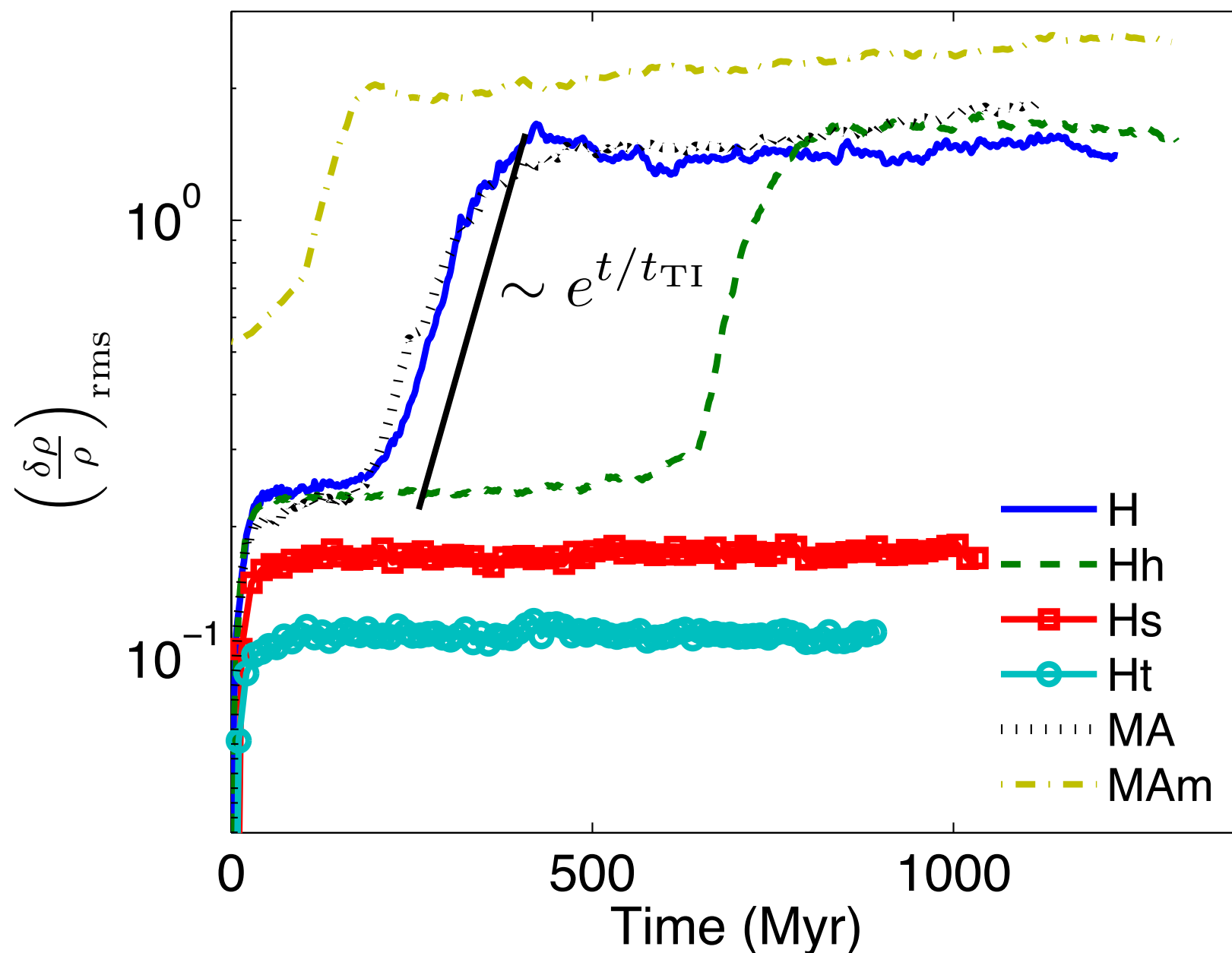
[Sharma et al. 2012]



$$q^+ \propto n^\alpha$$

$t_{\text{TI}} \approx t_{\text{cool}}$ or $\alpha \approx 0$ for observations to match idealized simulations

Measuring t_{TI}



measure the growth rate of
density perturbations

measuring growth rate gives
 t_{TI} and the density dependence
of microscopic heating

$$q^+ \propto n^\alpha$$

$\alpha \approx 0$ needed for agreement with observations

Measuring t_{TI}

Label [†]	Res.	L_x (kpc) $= L_y = L_z$	$\beta^\ddagger$	$\frac{\langle \text{heating} \rangle}{\langle \text{cooling} \rangle}$	t_{TI} range (Myr)	$\alpha^{\dagger\dagger}$ range
H*	128^3	40	...	1.0	59 to 116	−0.8 to 0.6
Hh	256^3	40	...	1.0	52 to 132	−1.2 to 0.7
Ht	128^3	40	...	1.0	...	...
Hs	128^3	20	...	1.0	...	...
Hl	128^3	80	...	1.0	100 to 117	0.3 to 0.6
Hm	128^3	80	...	1.0	66 to 87	−0.5 to 0.1
Hha	256^3	40	...	no cooling	...	...
M	128^3	40	100	1.0	67 to 69	−0.5 to −0.4
MA	128^3	40	100	1.0	73 to 93	−0.3 to 0.2
MAm	128^3	80	100	1.0	66 to 87	−0.5 to 0.1

$\alpha \approx 0$ agrees with the range observed from TI growth rate

$q^+ \propto n^\alpha$ too simplistic

Conclusions

- aniso. conduction much closer to runs without conduction
- *isotropic* conduction suppresses cold gas
- Turbulent heating is ruled out
- Turbulent mixing is viable
- $\alpha \approx 0$ for turbulent heating/mixing

Thank You!