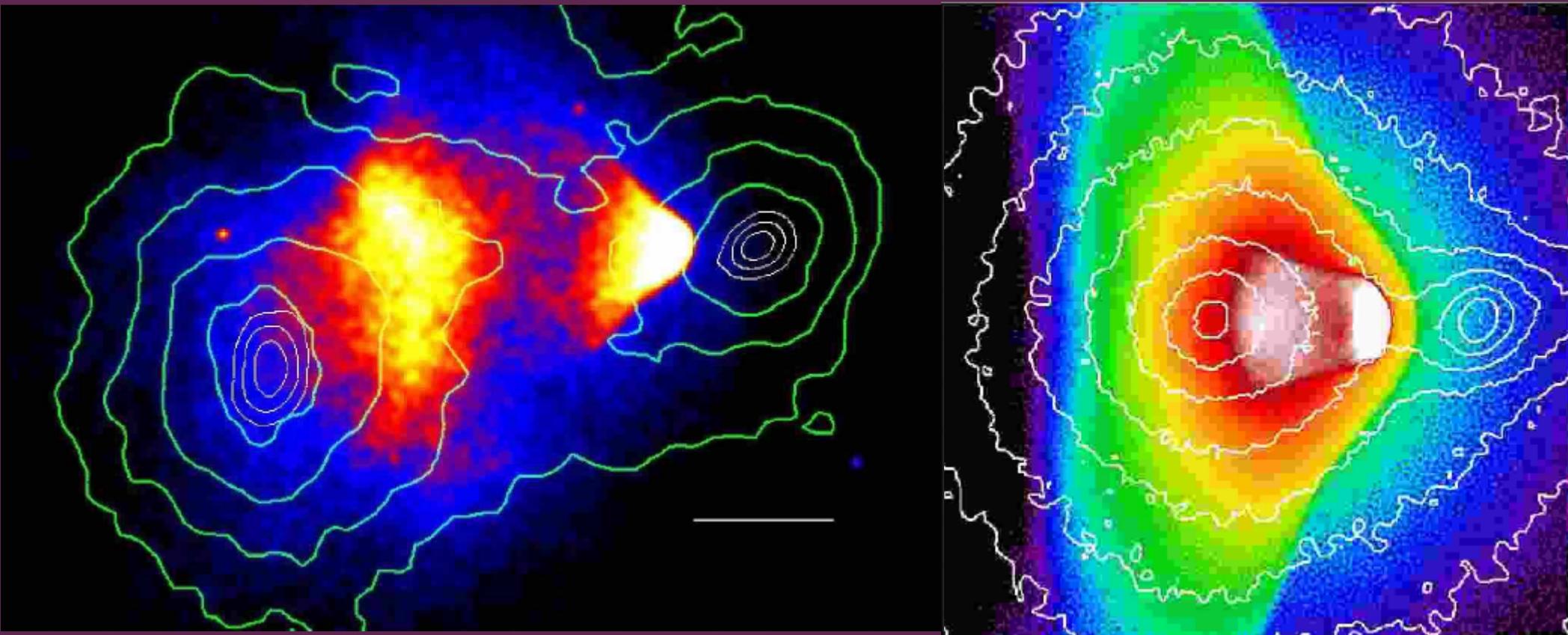
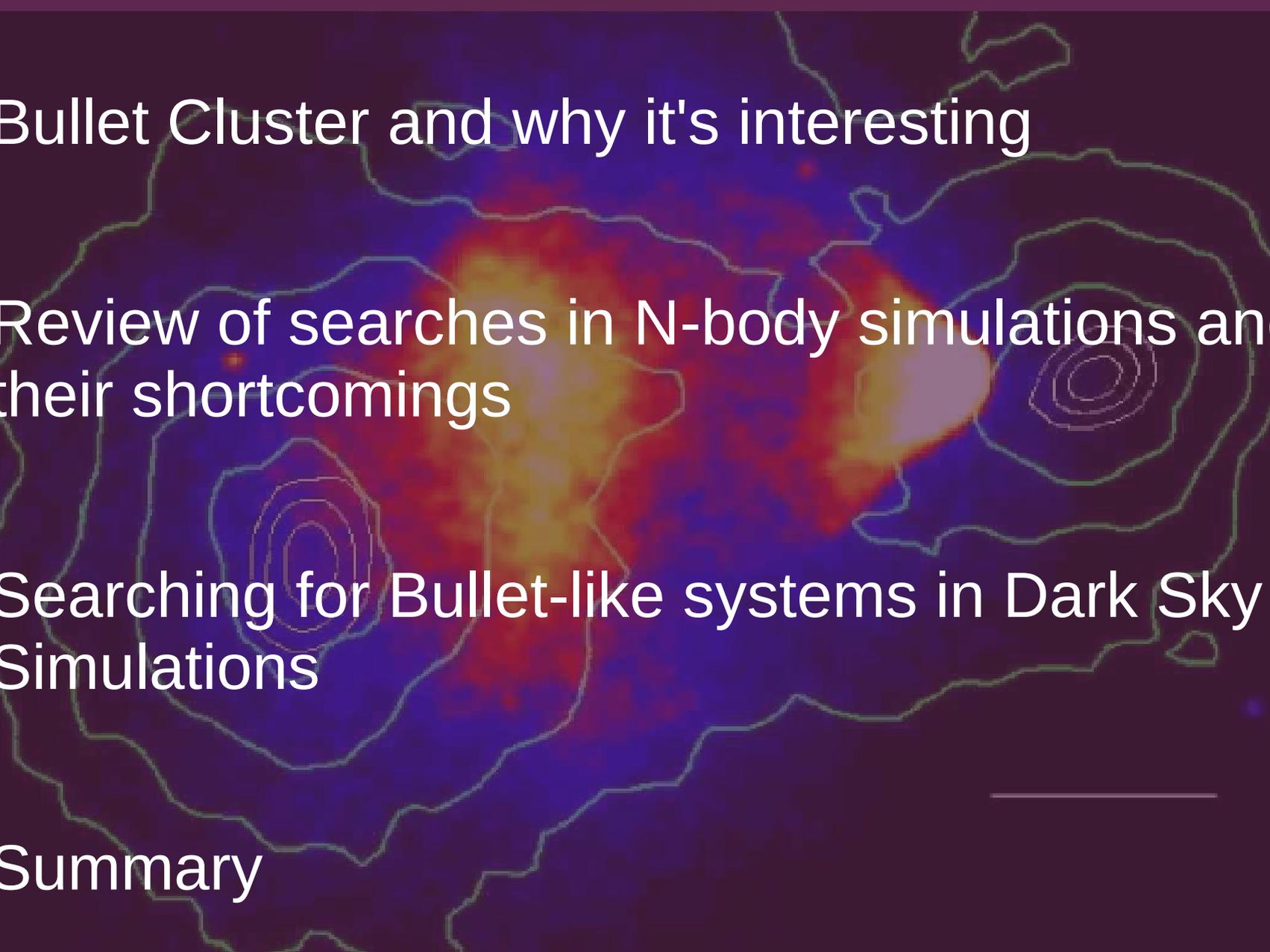


How rare is the Bullet Cluster

David Kraljic, University of Oxford
Copenhagen, August 2014



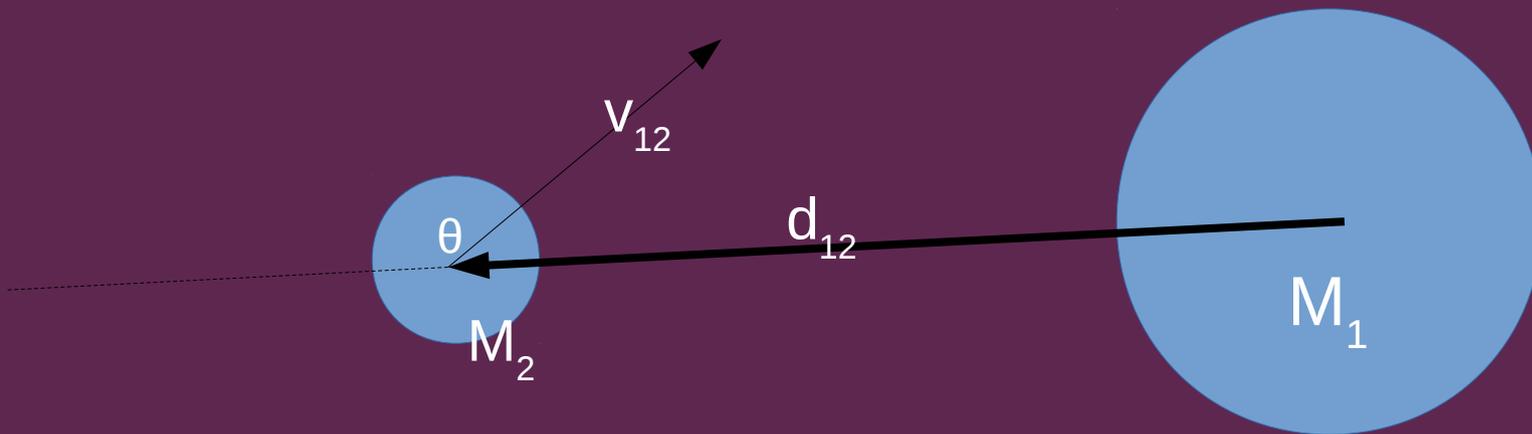
- 
- Bullet Cluster and why it's interesting
 - Review of searches in N-body simulations and their shortcomings
 - Searching for Bullet-like systems in Dark Sky Simulations
 - Summary

The Bullet Cluster system

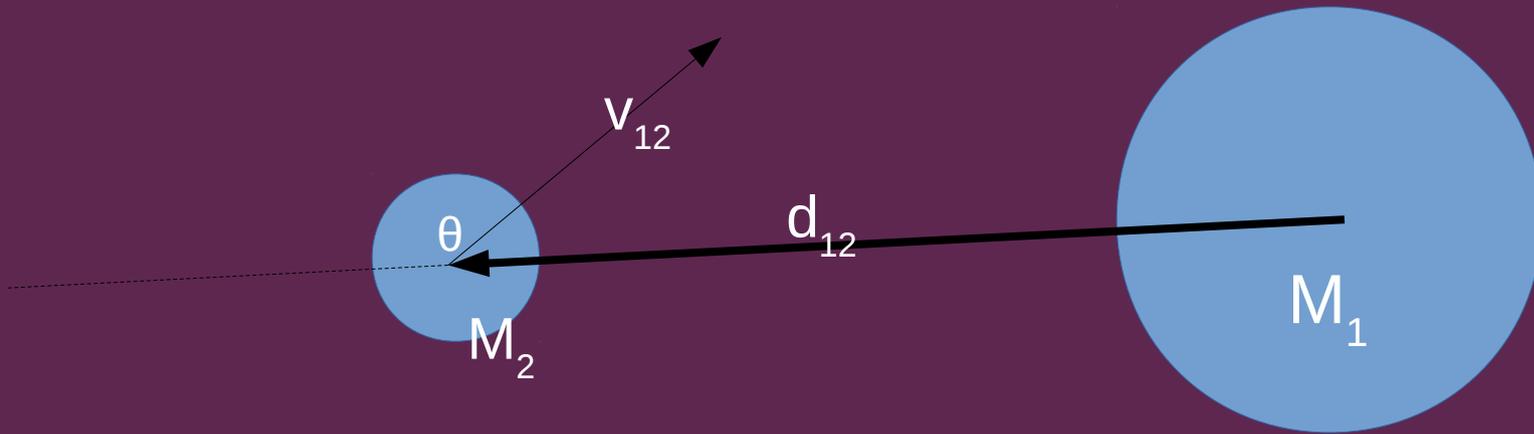
- Observed at $z \sim 0.3$
- Separated by 0.7 Mpc
- Masses $M_1 \sim 1.5 \cdot 10^{15} M_{\text{SUN}}$ and $M_2 \sim 1.5 \cdot 10^{14} M_{\text{SUN}}$
- Collision head-on and perpendicular to the line of sight
- Shock front velocity ~ 4700 km/s but relative velocity in hydrodynamical simulations smaller
- motivation = is such a system likely/consistent in LCDM
- Estimates of probabilities ranging from 10^{-11} (Lee&Komatsu 2010) to 1% (Hayashi&White 2006) !



A simple picture



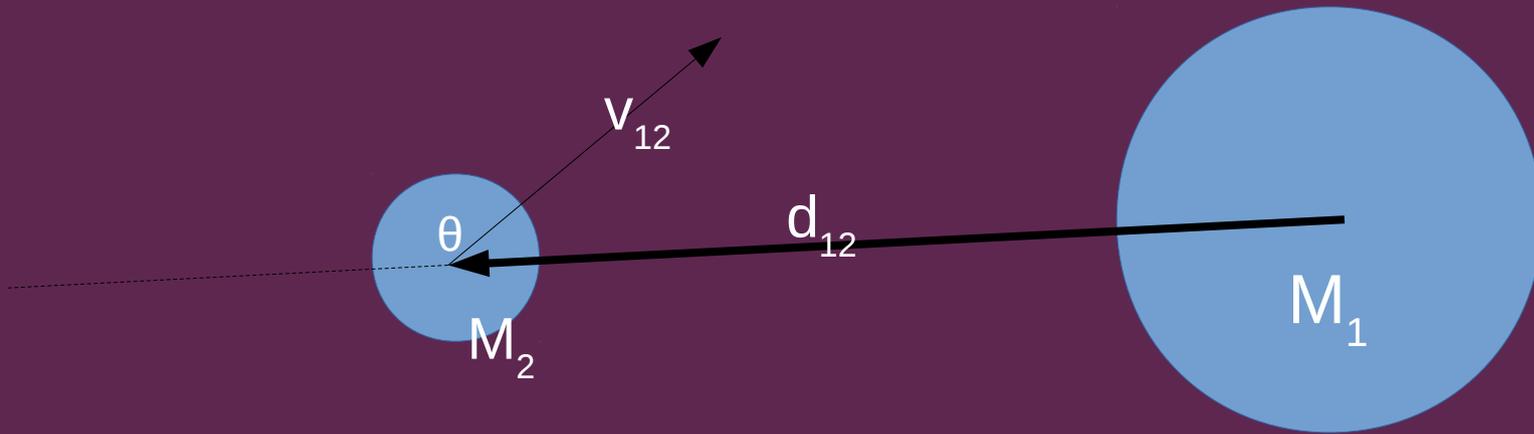
A simple picture



Masses frequently combined into $\langle M \rangle$, the arithmetic mean

Velocity looked at in the comoving or real space

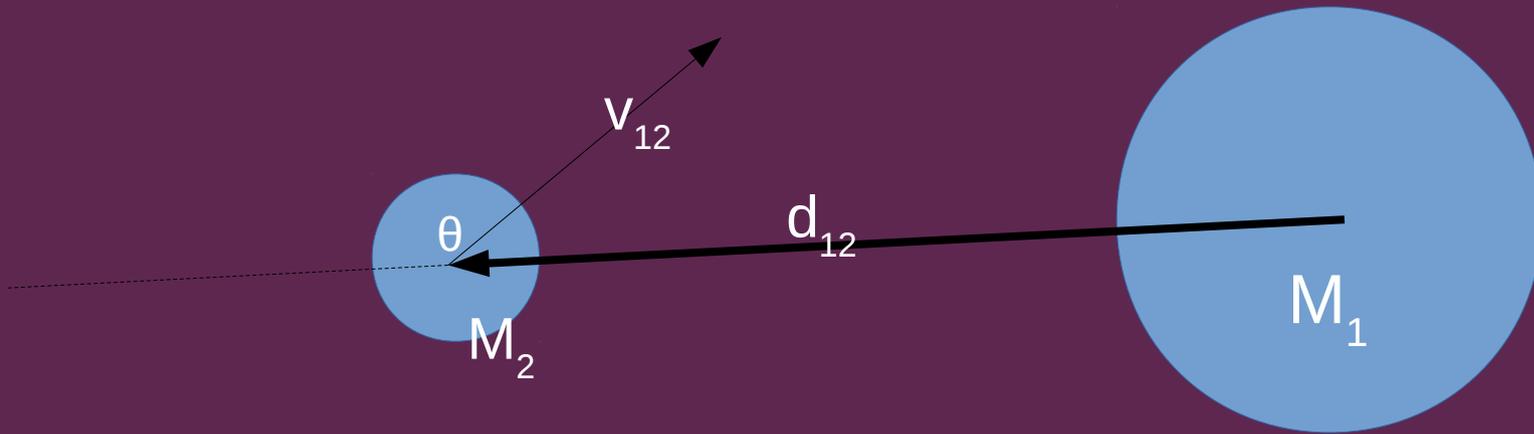
A simple picture



Masses frequently combined into $\langle M \rangle$, the arithmetic mean

Velocity looked at in the comoving or real space

A simple picture

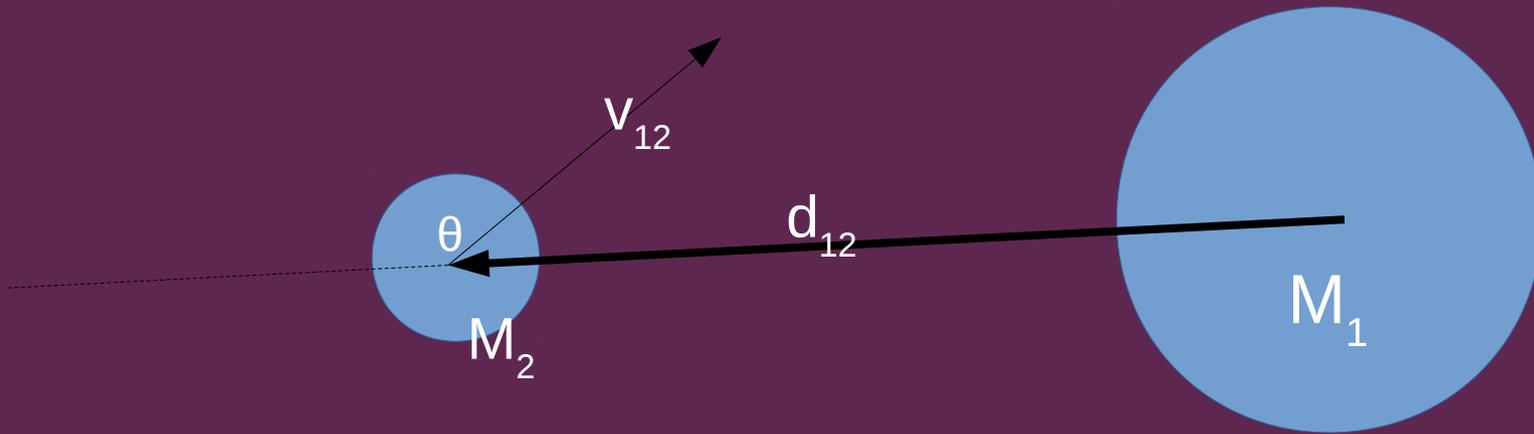


Masses frequently combined into $\langle M \rangle$, the arithmetic mean

Velocity looked at in the comoving or real space

Given certain masses, separation, angles interested in the probability that the relative velocity exceeds a certain number
e.g. $P(v_{12} > 3000 \text{ km/s}; \langle M \rangle > 10^{14} M_{\text{SUN}}/h; d_{12} < 10 \text{ Mpc}/h; \cos(\theta) < -0.9)$

A simple picture



Masses frequently combined into $\langle M \rangle$, the arithmetic mean

Velocity looked at in the comoving or real space

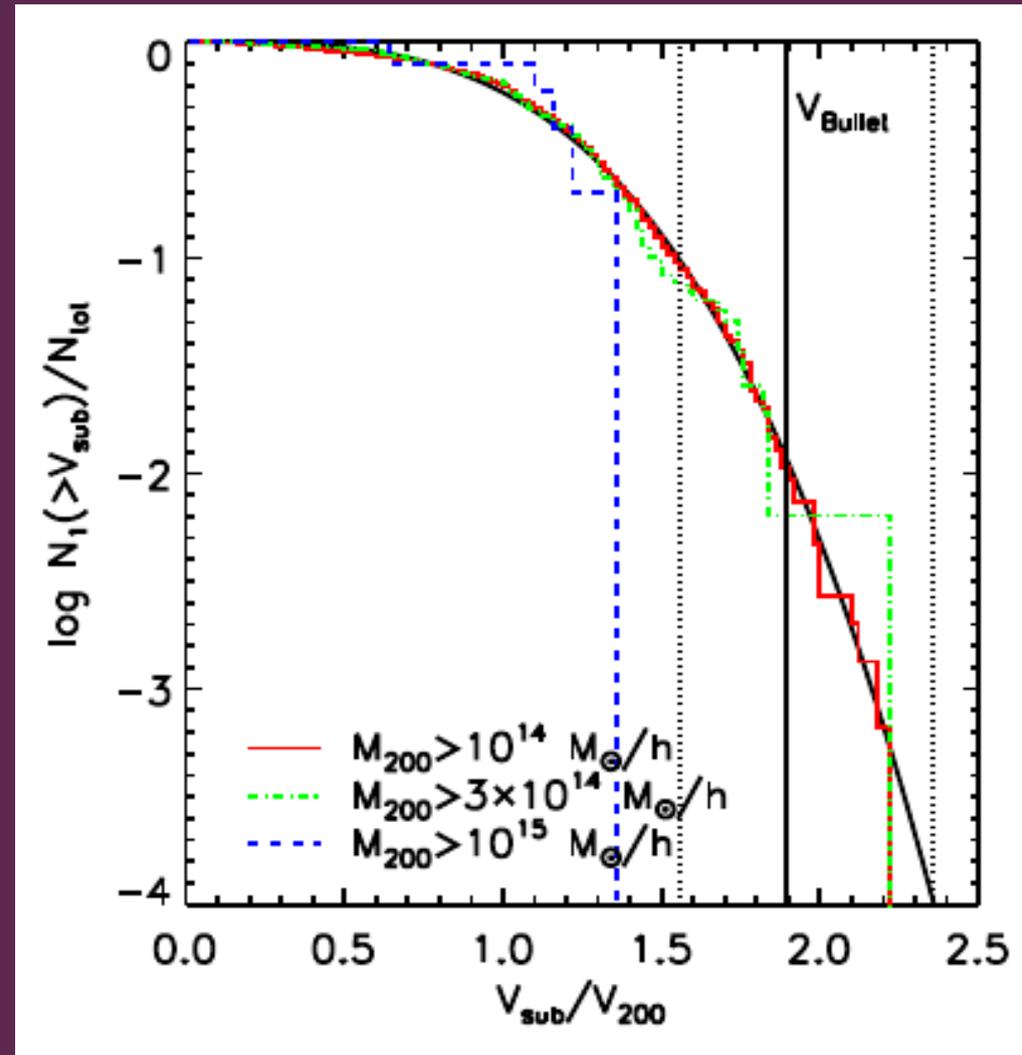
Given certain masses, separation, angles interested in the probability that the relative velocity exceeds a certain number
e.g. $P(v_{12} > 3000 \text{ km/s}; \langle M \rangle > 10^{14} M_{\text{SUN}}/h; d_{12} < 10 \text{ Mpc}/h; \cos(\theta) < -0.9)$

Initial conditions to reproduce the collision

- From non-cosmological hydrodynamical simulations
 - Springel & Farrar (2007) $d_{12} \sim 3.4\text{Mpc}$ and $v_{12} \sim 2060\text{km/s}$
 - Mastropietro & Burkert (2008) $d_{12} \sim 5\text{Mpc}$ and $v_{12} \sim 3000\text{km/s}$ at $z \sim 0.5$
- Ideal for N-body simulations because the clusters are well separated (configuration space based halofinders have difficulties resolving the 'actual' collision at $z=0.3$)

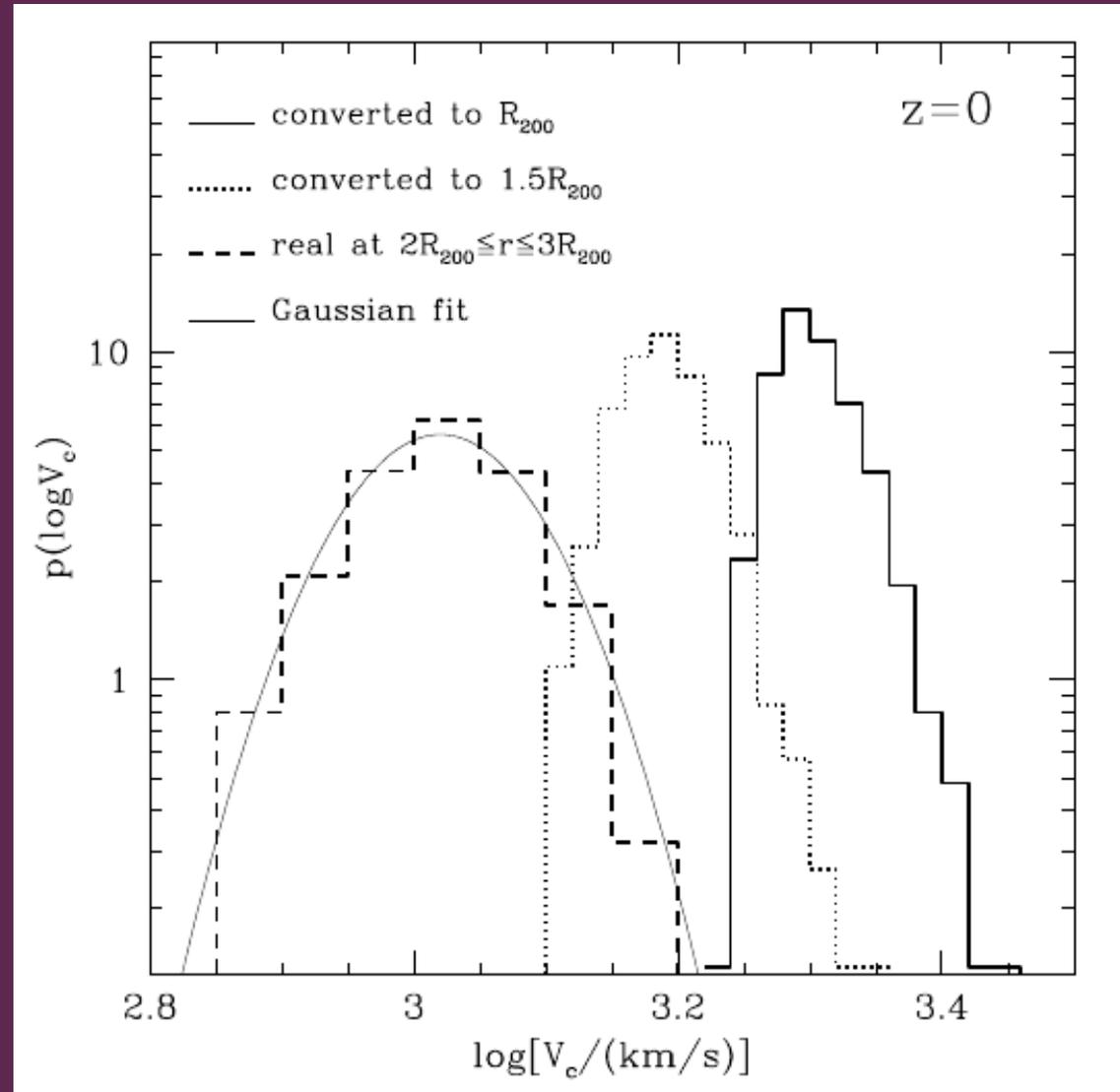
Millenium Run: Hayashi&White (2006)

- MR: 500Mpc/h box
 - Not many extreme objects in terms of mass
- Looked for a subcluster moving away with at least 4500km/s (shock front velocity) separated by at least 0.7Mpc at $z\sim 0.3$
- Had to extrapolate to get pdf-s for host halo mass $> 10^{14} M_{\text{SUN}} / h$
- Probable within LCDM (1%) but uncertain to 2 orders of magnitude dependent on the velocity cut



Lee & Komatsu (2010)

- Used MICE (3Gpc/h box with 2048^3 particles)
- Reapplied FoF to clusters to find subclusters
- Probability of finding M&B(2008) initial conditions at $z=0$ is $\sim 10^{-11}$ determined by Gaussian interpolation \Rightarrow Improbable in LCDM



Thompson & Nagamine (2012)

- Examined the effect of the box size and resolution in N-body sims. on the pairwise velocity distribution of DM halos
- Better resolution and bigger box extend the tail of the pairwise velocity pdf

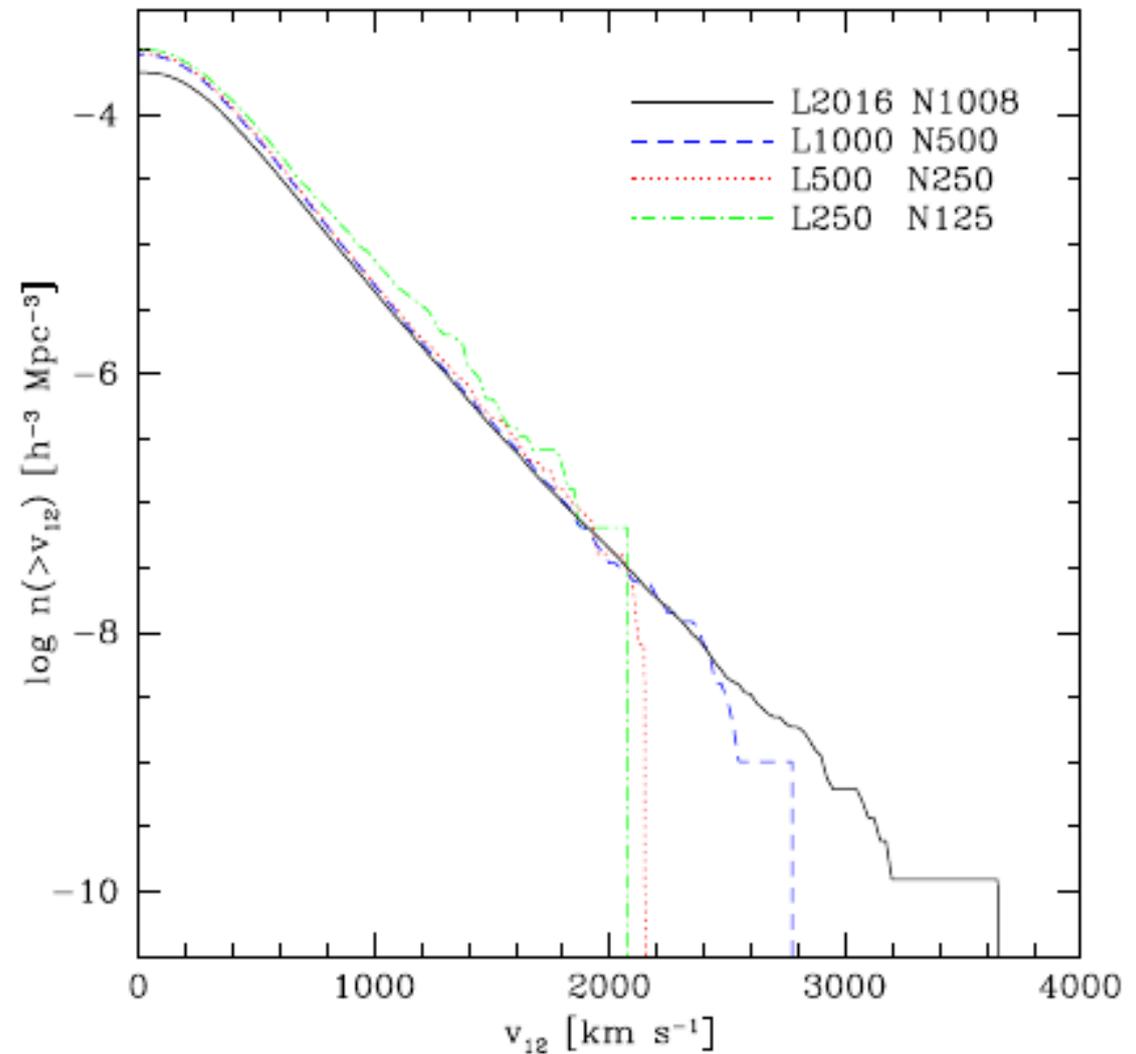


Figure 7. Cumulative v_{12} function of DM halos at $z=0$. This figure shows how increasing the box size increases the number of high- v_{12} pairs, extending the tail of the distribution.

Thompson & Nagamine (2012)

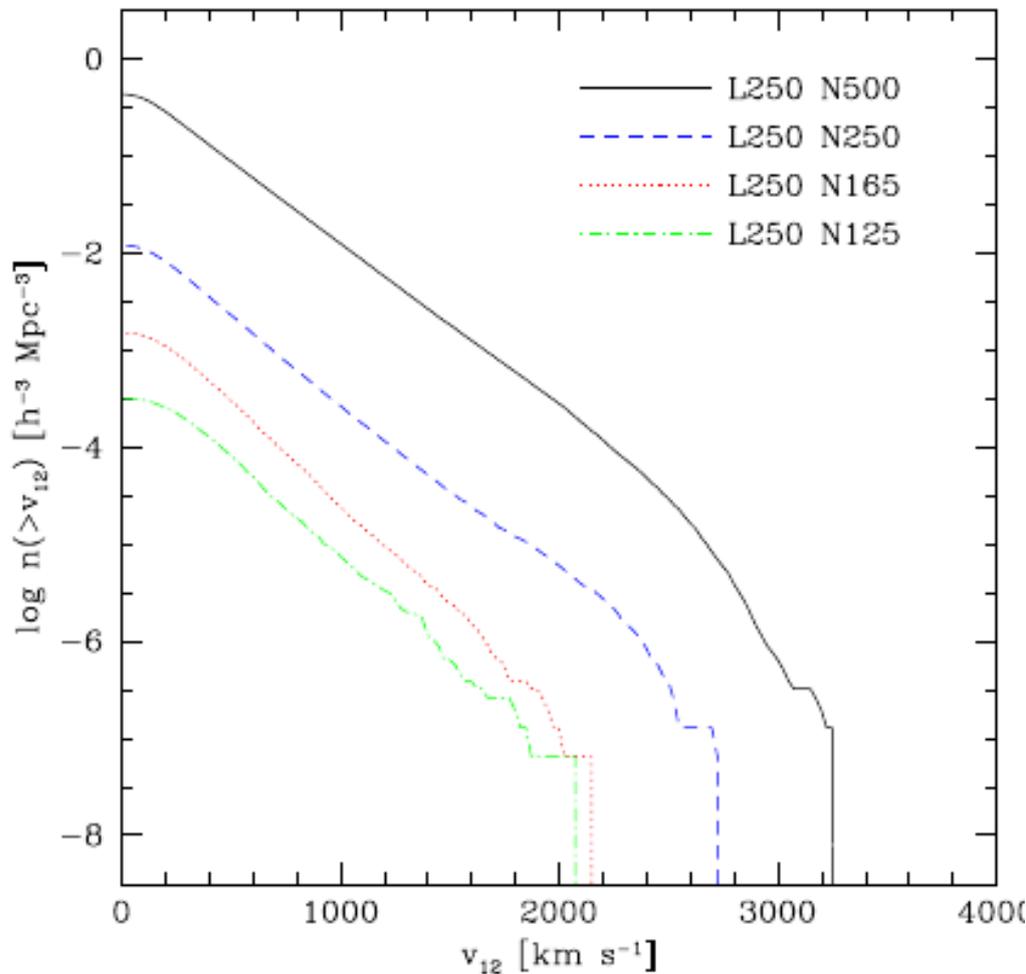
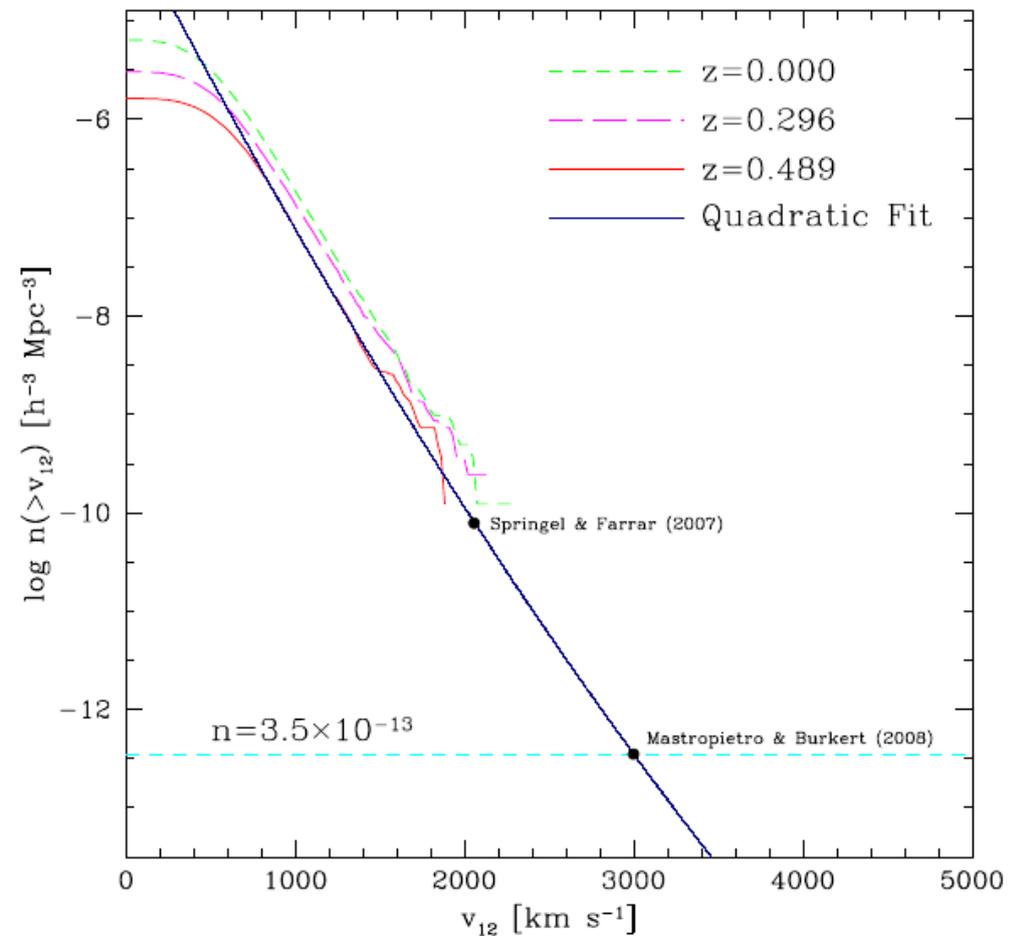


Figure 8. Cumulative v_{12} function of DM halos at $z=0$. This figure shows the resolution effect. As the resolution increases, the normalization of the distribution increases due to a larger number of lower mass halos with higher velocities.



Estimate $P(v_{12} > 3000 \text{ km/s}) \sim 10^{-8}$

To find Bullet-like system need $L=4.5 \text{ Gpc/h}$ with 500^3 particles per $(\text{Gpc/h})^3$

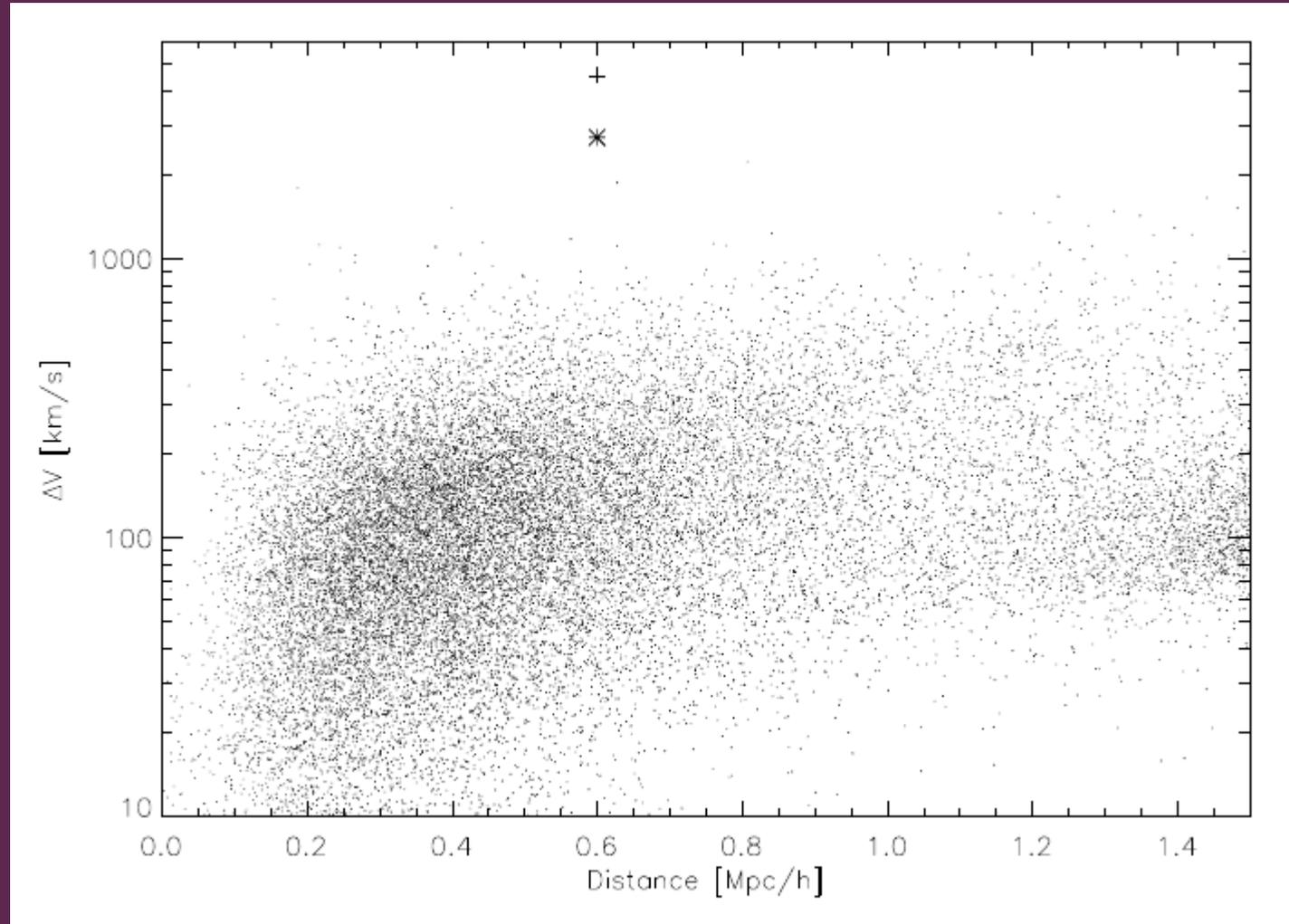
Watson et al. (2013/14) using
Jubilee

Watson et al. (2013/14) using Jubilee

- v1: “perhaps implying a tension with LCDM”
- v2: “we find that ... Bullet cluster exists in the far-tail in the distribution ”
- Used config. Space halofinders → breakdown at short distances

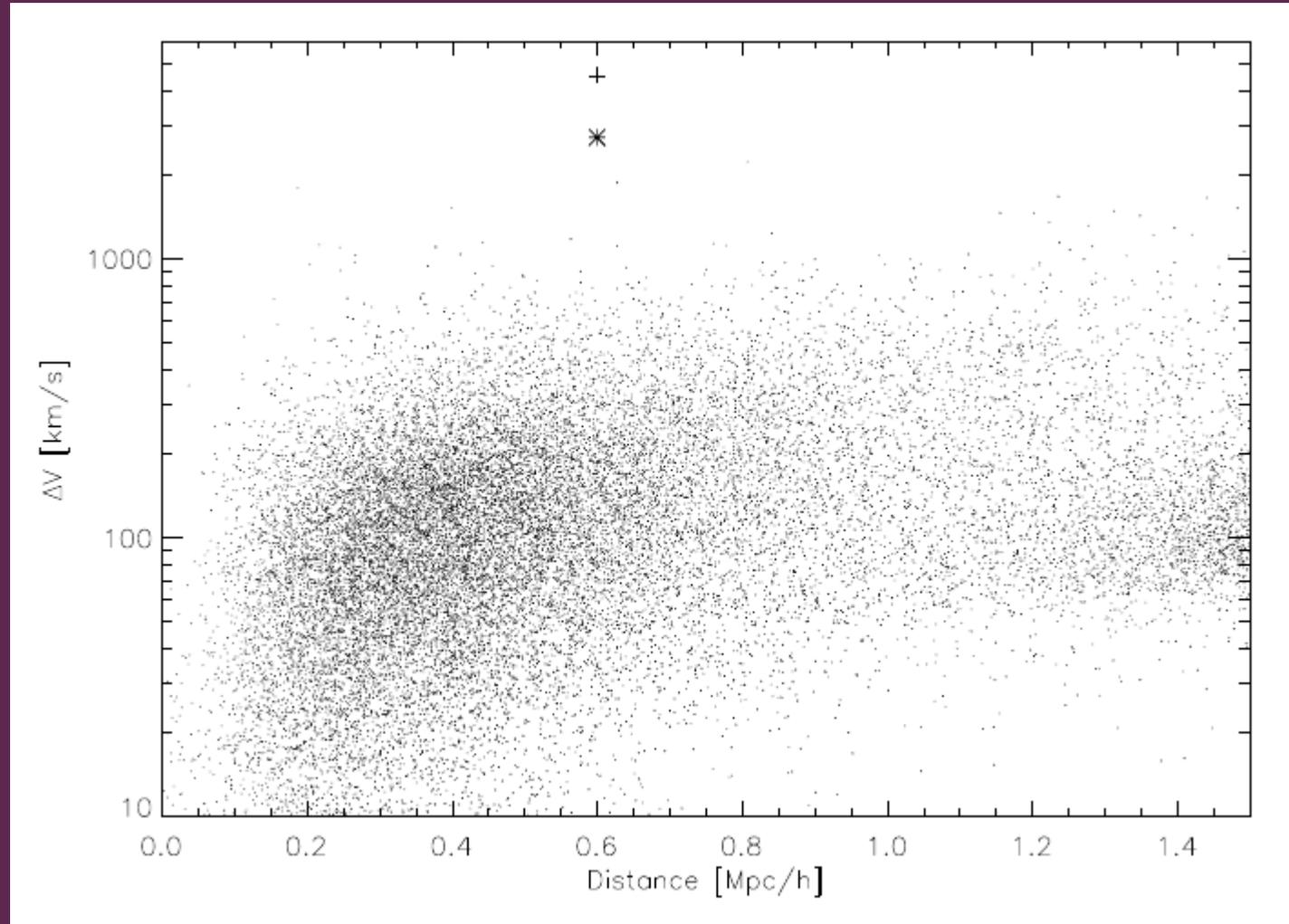
Watson et al. (2013/14) using Jubilee

- v1: “perhaps implying a tension with LCDM”
- v2: “we find that ... Bullet cluster exists in the far-tail in the distribution ”
- Used config. Space halofinders → breakdown at short distances



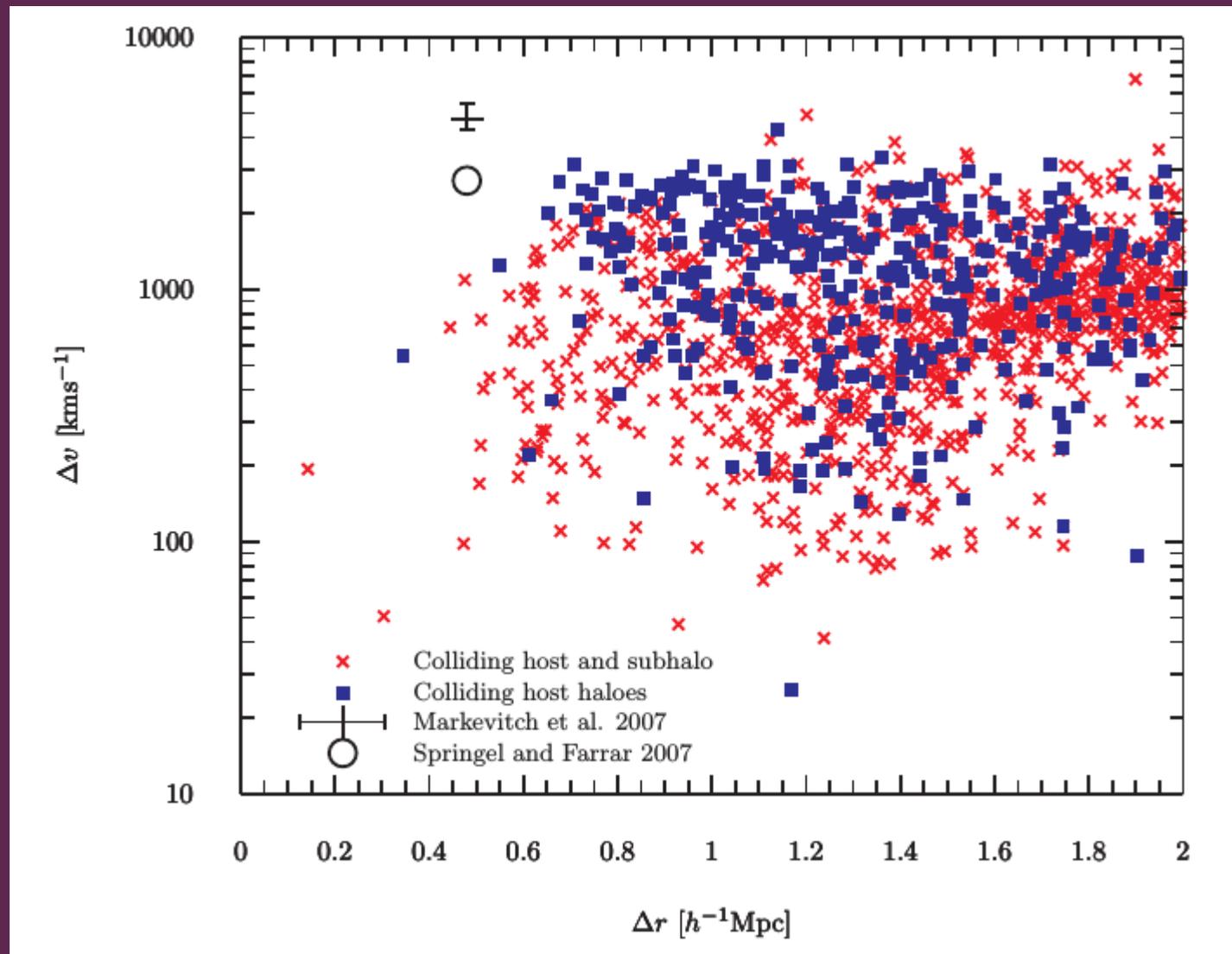
Watson et al. (2013/14) using Jubilee

- v1: “perhaps implying a tension with LCDM”
- v2: “we find that ... Bullet cluster exists in the far-tail in the distribution ”
- Used config. Space halofinders → breakdown at short distances



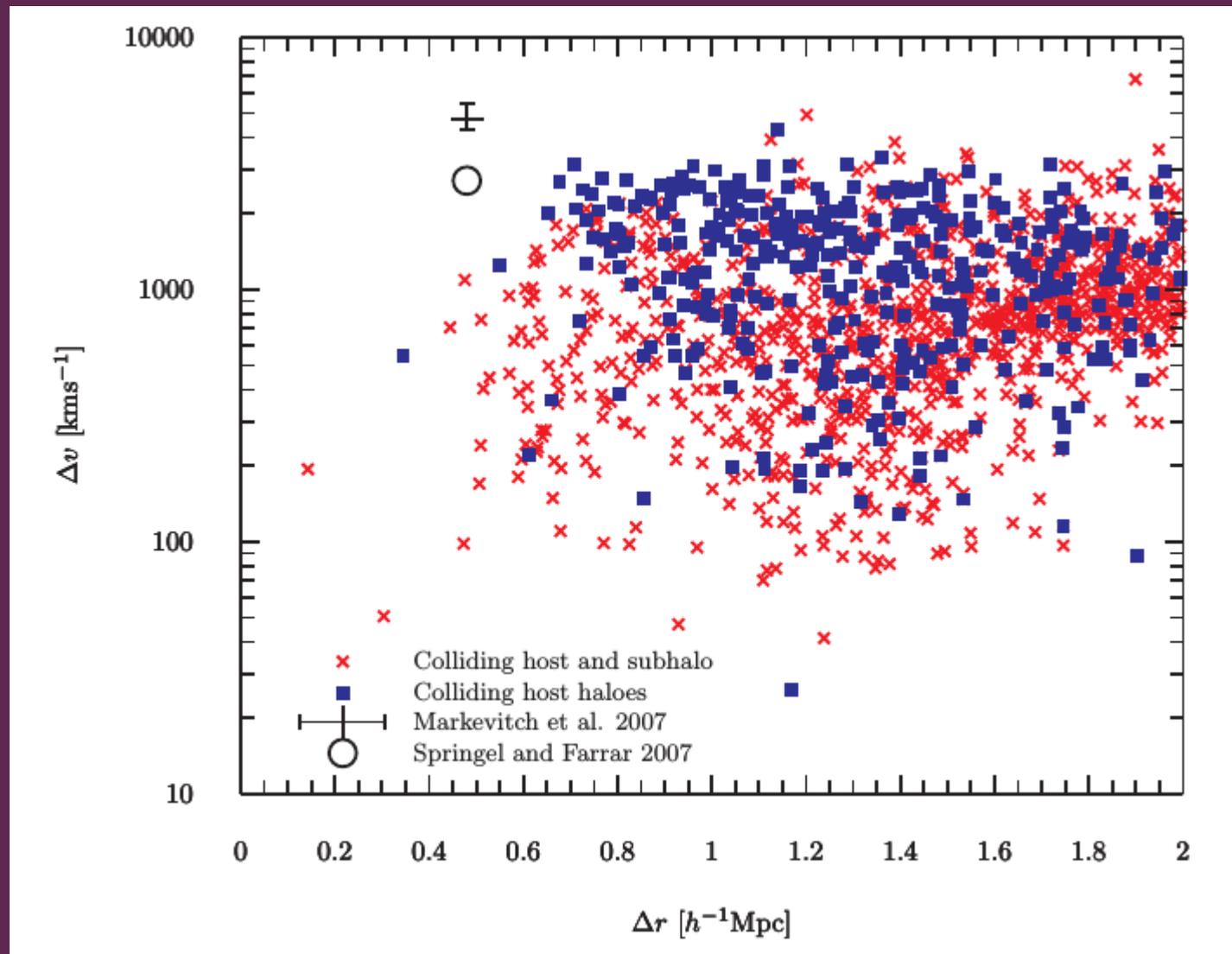
Watson et al. (2013/14) using Jubilee

- v1: “perhaps implying a tension with LCDM”
- v2: “we find that ... Bullet cluster exists in the far-tail in the distribution ”
- Used config. Space halofinders → breakdown at short distances



Watson et al. (2013/14) using Jubilee

- v1: “perhaps implying a tension with LCDM”
- v2: “we find that ... Bullet cluster exists in the far-tail in the distribution ”
- Used config. Space halofinders → breakdown at short distances



Bouillot et al. (2014)

- DEUS-FUR (box length 21Gpc/h but poor resolution)

Bouillot et al. (2014)

- DEUS-FUR (box length 21Gpc/h but poor resolution)

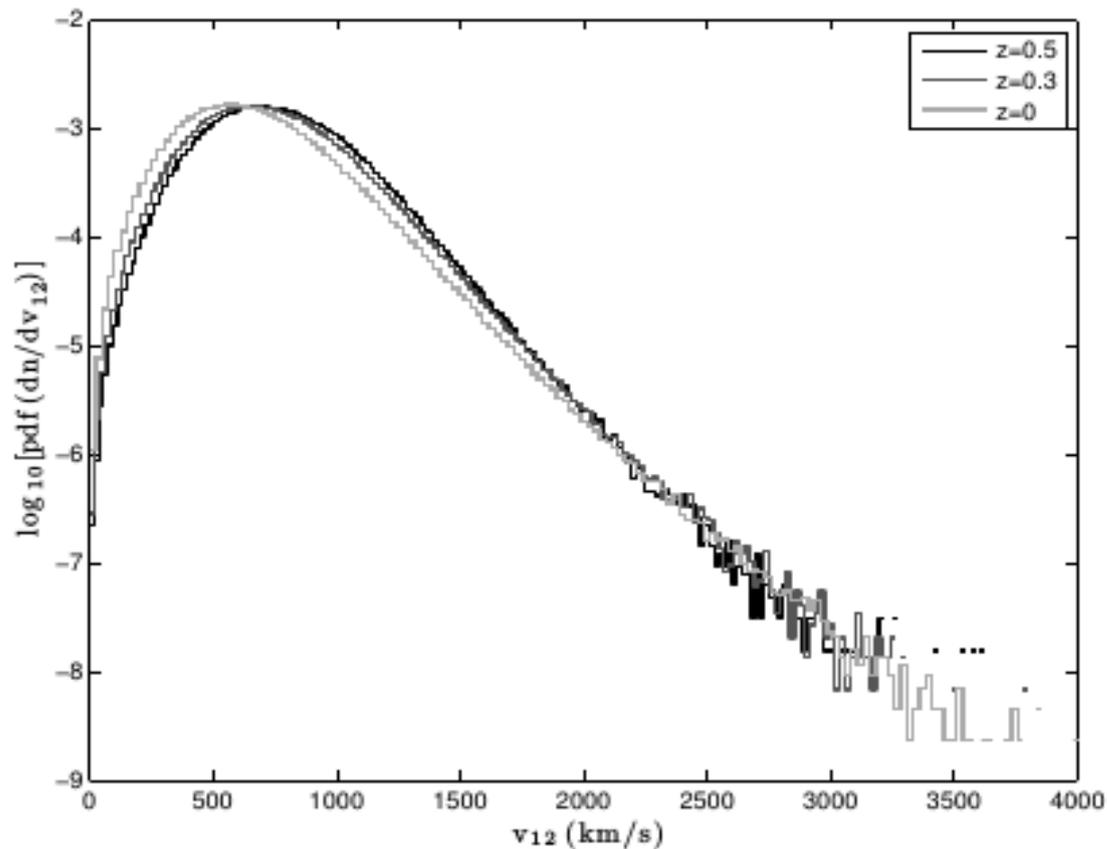


Figure 4. Redshift evolution of the probability density function of the pairwise velocity for FoF($b=0.15$) halo pairs from the DEUS-FUR Λ CDM-W7 simulation with distance separation $d_{12} < 10 h^{-1}$ Mpc at $z = 0.5$ (black), $z = 0.3$ (grey) and $z = 0$ (light grey) respectively.

Bouillot et al. (2014)

- DEUS-FUR (box length 21Gpc/h but poor resolution)

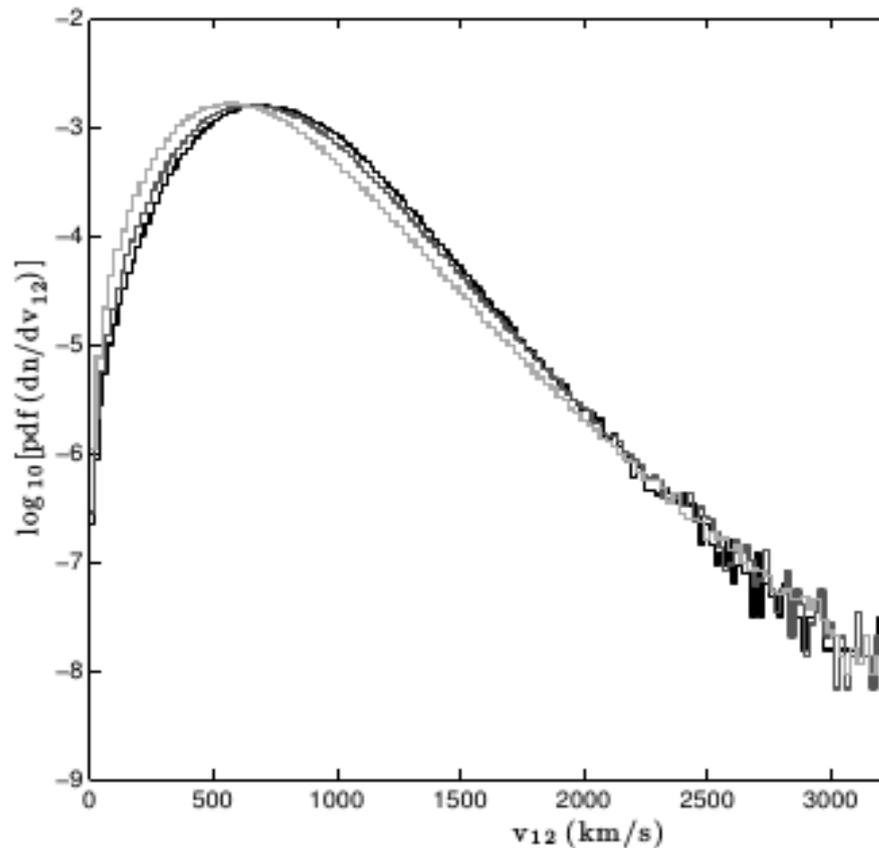


Figure 4. Redshift evolution of the probability density function of pairwise velocity for FoF($b=0.15$) halo pairs from the DEUS-FUR simulation with distance separation $d_{12} < 10 h^{-1}$ Mpc at $z = 0.3$ (grey) and $z = 0$ (light grey) respectively.

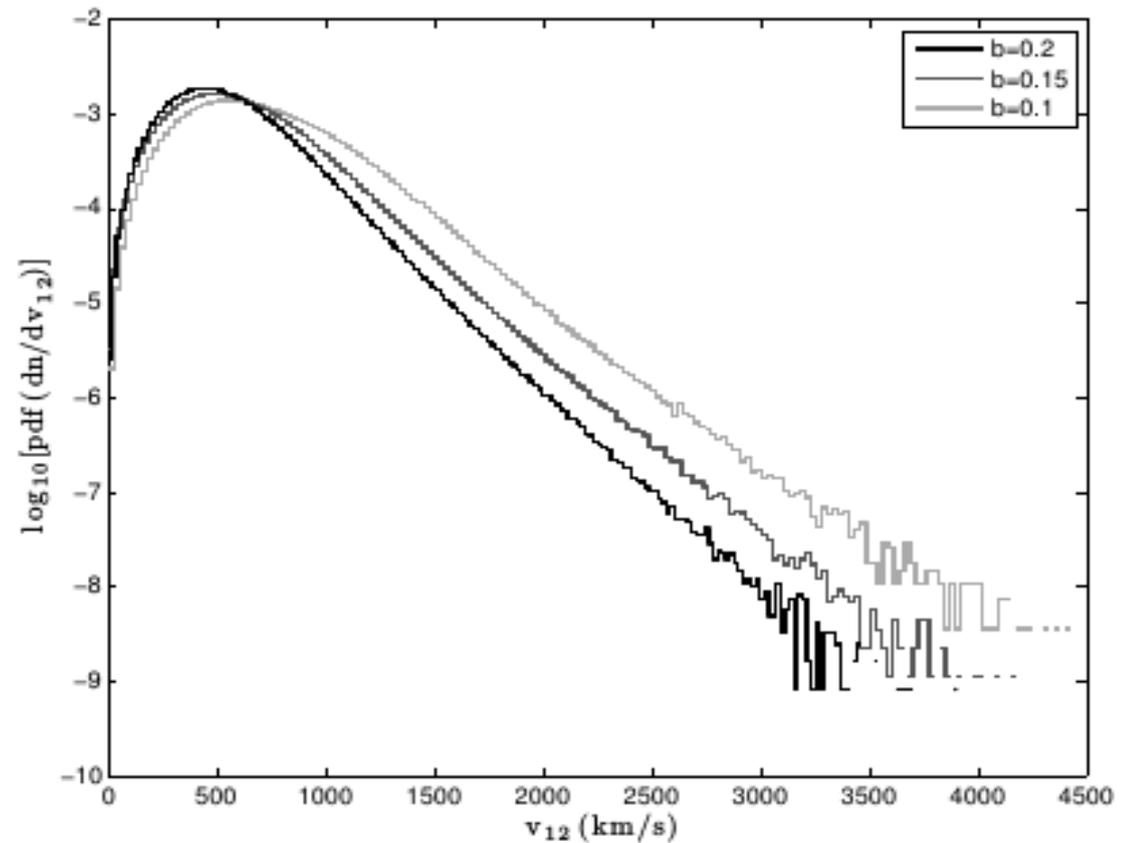


Figure 2. Probability density function of the pairwise velocity from the DEUS-FUR Λ CDM-W7 simulation at $z = 0$ for pairs with separation $d_{12} < 15 h^{-1}$ Mpc detected assuming linking-length values $b = 0.1$ (light grey), $b = 0.15$ (grey) and $b = 0.2$ (black) respectively.

Bouillot et al. (2014)

- DEUS-FUR (box length 21Gpc/h but poor resolution)

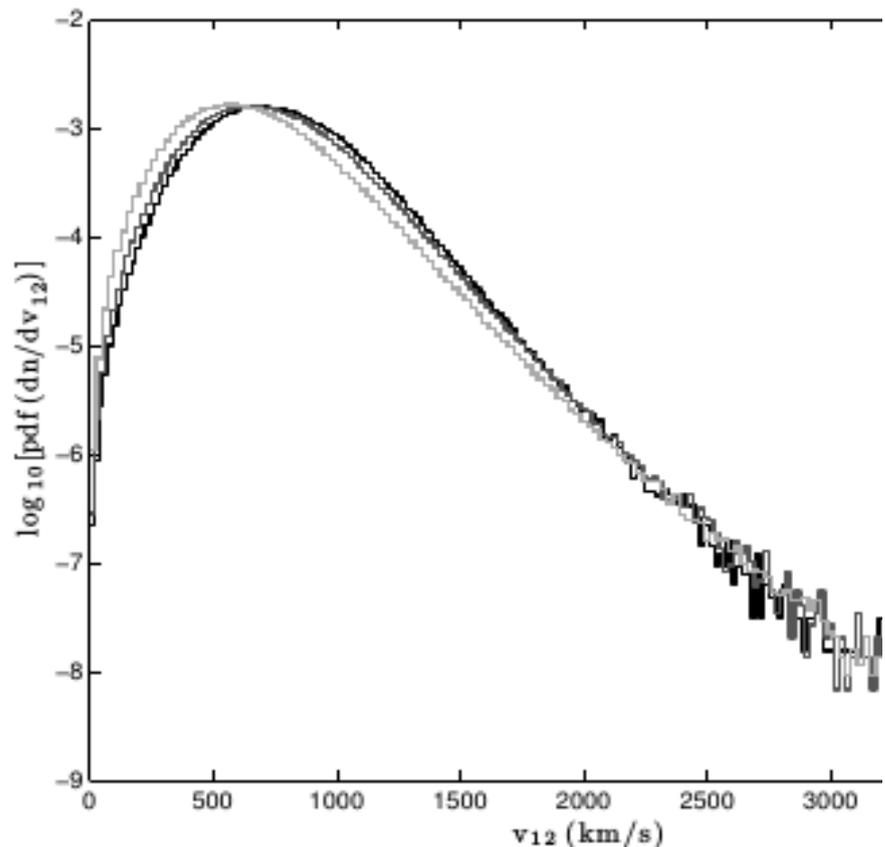


Figure 4. Redshift evolution of the probability density function of pairwise velocity for FoF($b=0.15$) halo pairs from the DEUS-FUR simulation with distance separation $d_{12} < 10 h^{-1}$ Mpc at $z = 0.3$ (grey) and $z = 0$ (light grey) respectively.

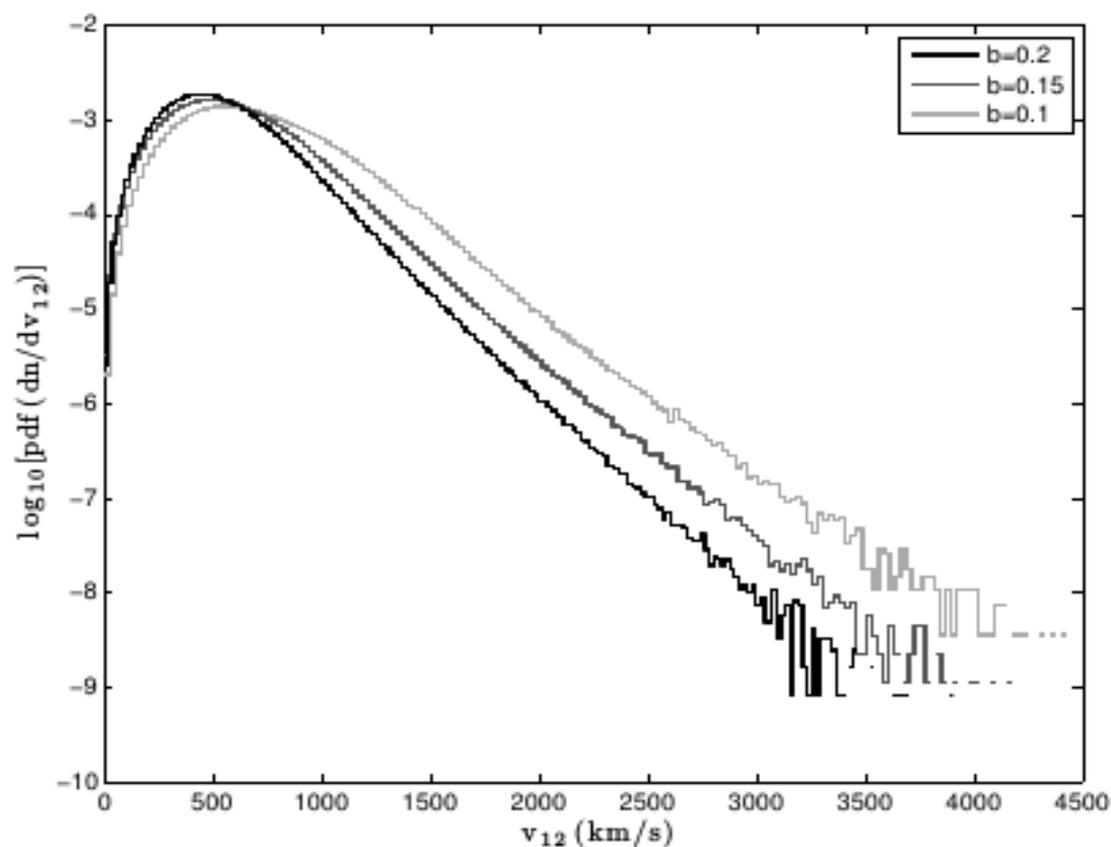
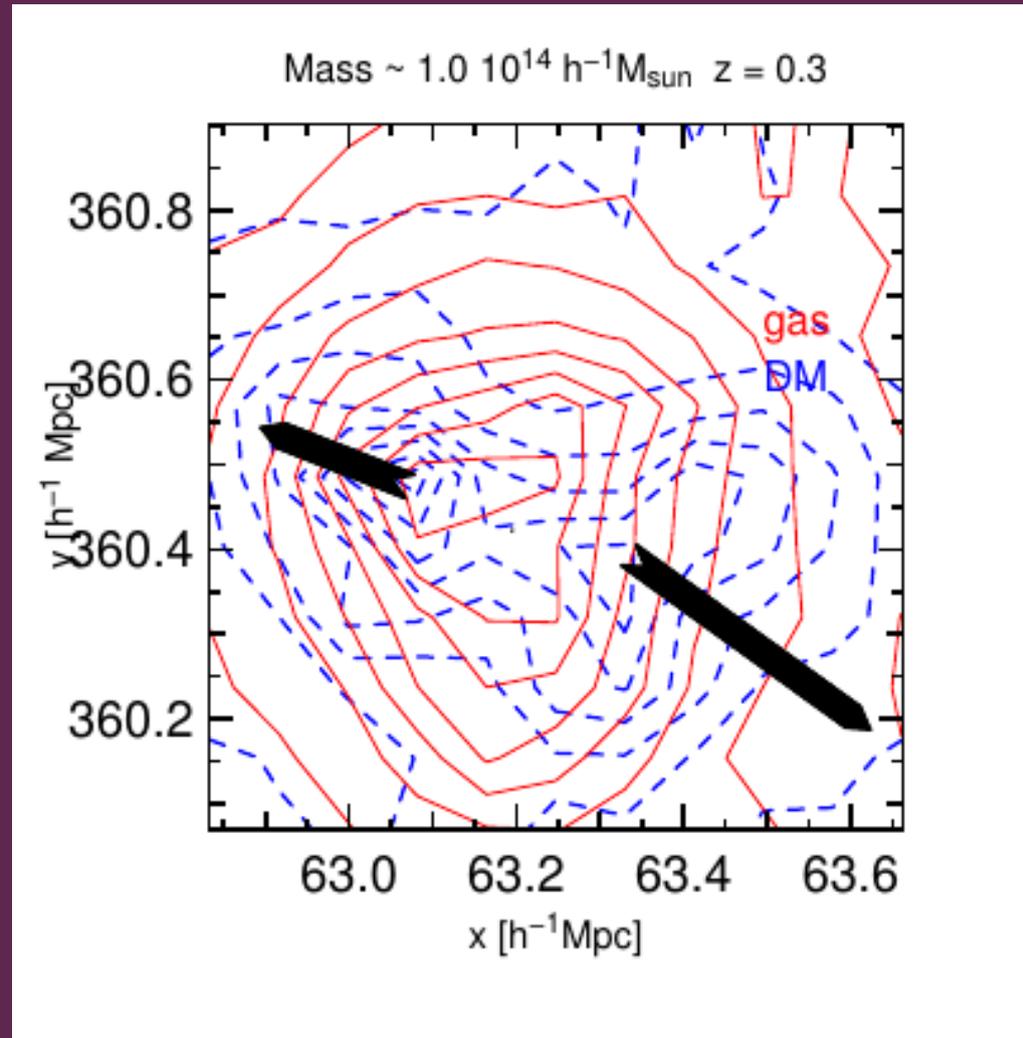


Figure 2. Probability density function of the pairwise velocity from the DEUS-FUR Λ CDM-W7 simulation at $z = 0$ for pairs with separation $d_{12} < 15 h^{-1}$ Mpc detected assuming linking-length values $b = 0.1$ (light grey), $b = 0.15$ (grey) and $b = 0.2$ (black) respectively.

Estimate $P(v_{12} > 3000 \text{ km/s}) \sim 6 \cdot 10^{-6}$ in LCDM (using $b=0.15$)

Other approaches

- Forero-Romero et al. (2010) looking at 2D projected displacement between DM and gas in MareNostrum simulations → find Bullet-like configurations in 1-2% of cases



- Most of the inconsistency arises from inadequate size of the N-Body simulation, so the tail of the distribution needs to be extrapolated → Bigger boxes and better resolution needed
- Lots of arbitrariness → the dependence on the cuts in the parameters must be explored in more detail

- Most of the inconsistency arises from inadequate size of the N-Body simulation, so the tail of the distribution needs to be extrapolated → Bigger boxes and better resolution needed
- Lots of arbitrariness → the dependence on the cuts in the parameters must be explored in more detail

Dark Sky Simulations, Skillman et al. (July 2014)

Dark Sky Simulations, Skillman et al. (July 2014)

- $L=8\text{Gpc}/h$ with 1280^3 particles per $(\text{Gpc}/h)^3$
 - Compare with Jubilee ($L=6\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$), MICE ($L=3\text{ Gpc}/h$ with 666^3 particles per $(\text{Gpc}/h)^3$), Thom.&Nag.(2008) ($L=2\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$)
- Phase space based Halo-finder (ROCKSTAR)
 - Previous studies used FoF with LL $b=0.2$ or $b=0.15$
- Currently output only at $z=0$

Dark Sky Simulations, Skillman et al. (July 2014)

- $L=8\text{Gpc}/h$ with 1280^3 particles per $(\text{Gpc}/h)^3$
 - Compare with Jubilee ($L=6\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$), MICE ($L=3\text{ Gpc}/h$ with 666^3 particles per $(\text{Gpc}/h)^3$), Thom.&Nag.(2008) ($L=2\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$)
- Phase space based Halo-finder (ROCKSTAR)
 - Previous studies used FoF with LL $b=0.2$ or $b=0.15$
- Currently output only at $z=0$

Dark Sky Simulations, Skillman et al. (July 2014)

- $L=8\text{Gpc}/h$ with 1280^3 particles per $(\text{Gpc}/h)^3$
 - Compare with Jubilee ($L=6\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$), MICE ($L=3\text{ Gpc}/h$ with 666^3 particles per $(\text{Gpc}/h)^3$), Thom.&Nag.(2008) ($L=2\text{ Gpc}/h$ with 1000^3 particles per $(\text{Gpc}/h)^3$)
- Phase space based Halo-finder (ROCKSTAR)
 - Previous studies used FoF with LL $b=0.2$ or $b=0.15$
- Currently output only at $z=0$

Bound system?

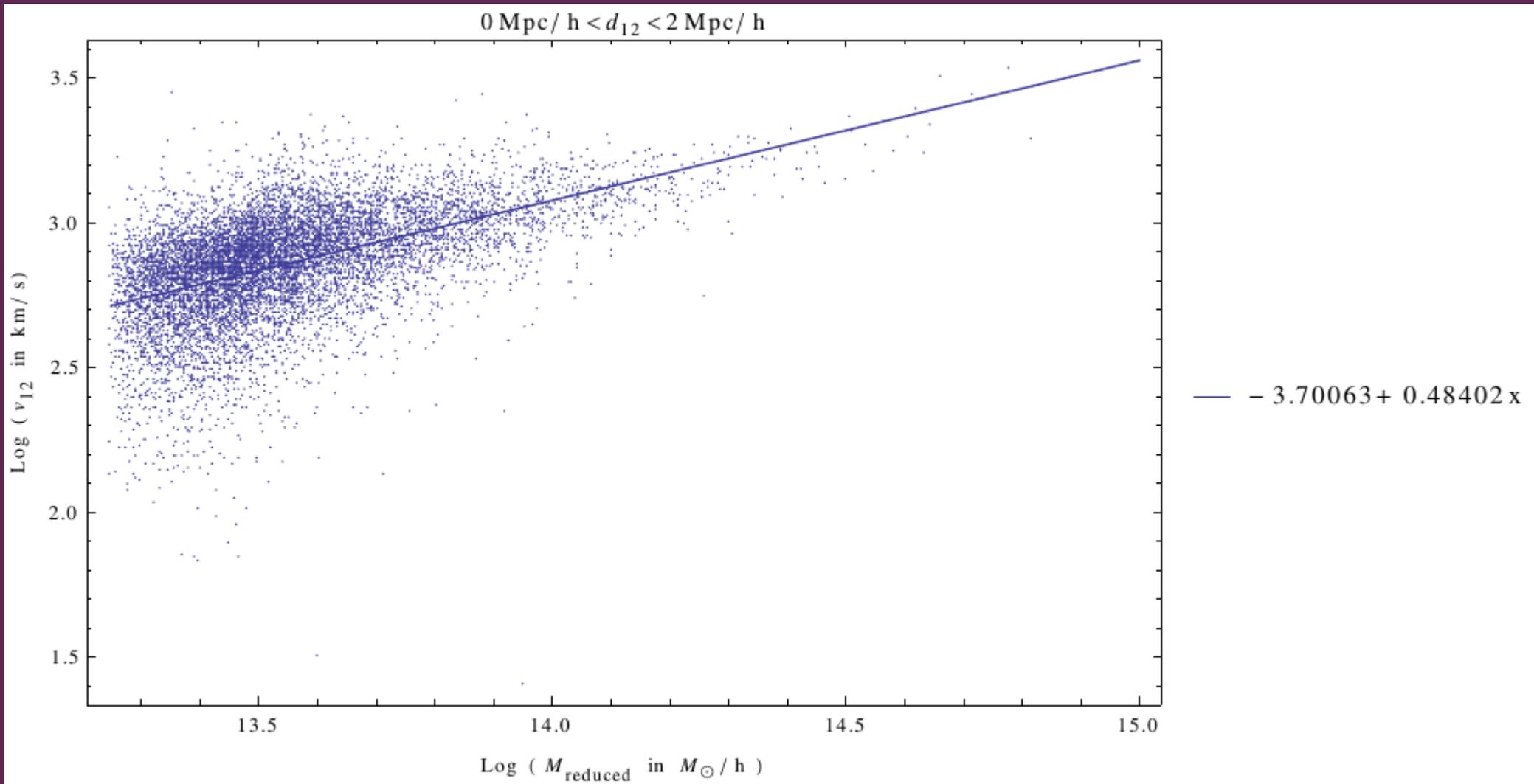
For a gravitationally bound system
expect the scaling to be $v_{12} \sim M^{1/2}$

Prelim.

Bound system?

For a gravitationally bound system
expect the scaling to be $v_{12} \sim M^{1/2}$

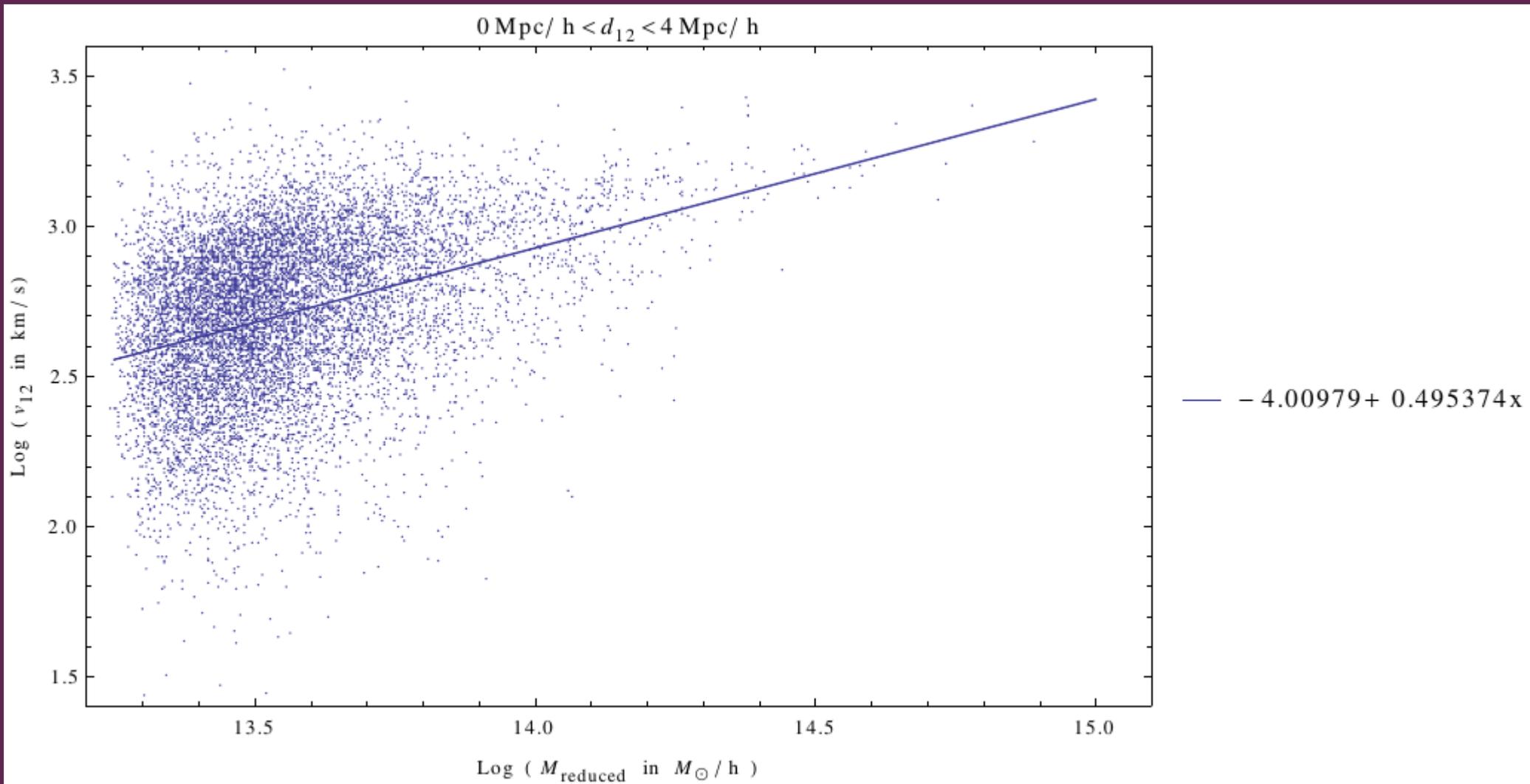
Prelim.



Bound system?

For a gravitationally bound system
expect the scaling to be $v_{12} \sim M^{1/2}$

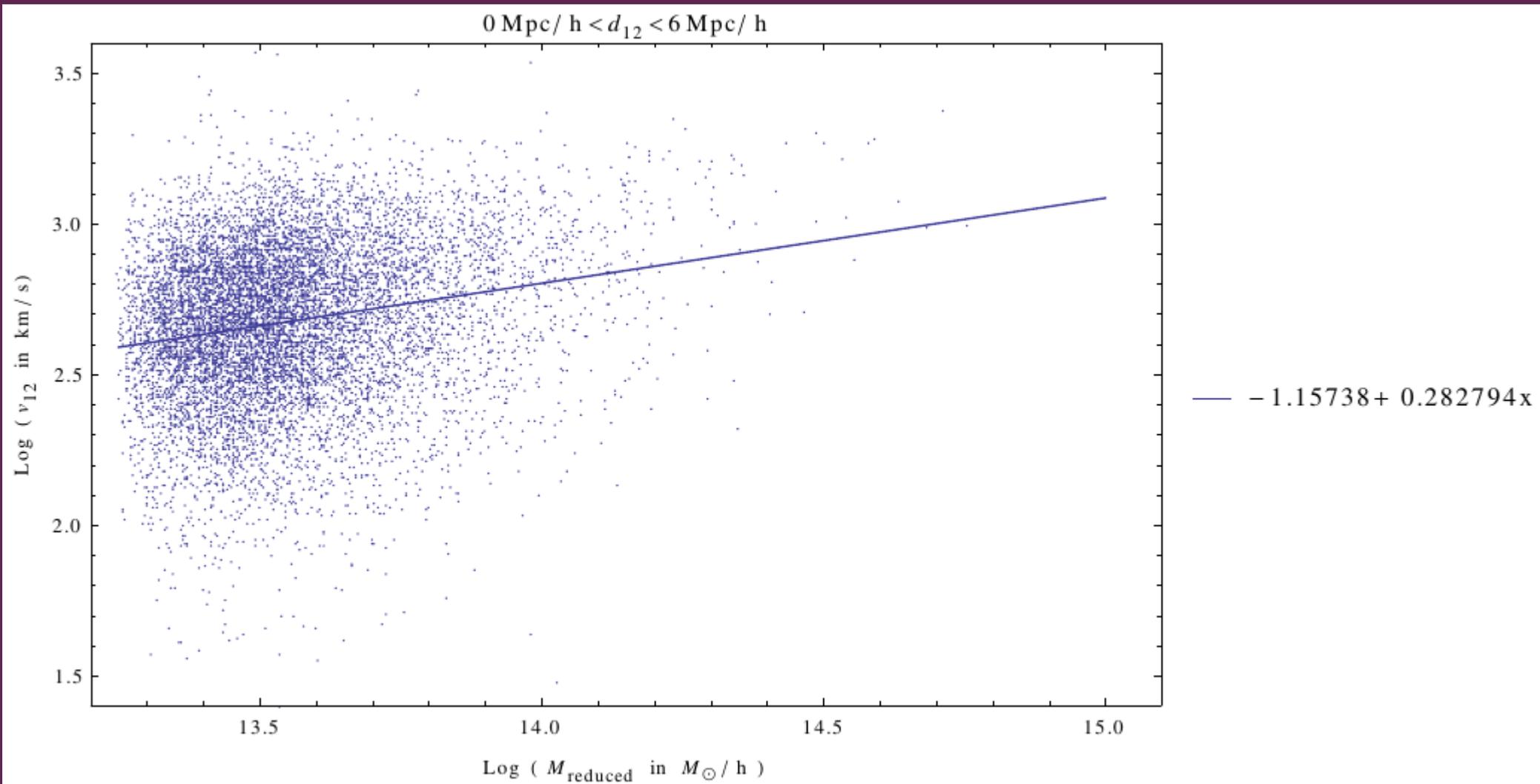
Prelim.



Bound system?

For a gravitationally bound system
expect the scaling to be $v_{12} \sim M^{1/2}$

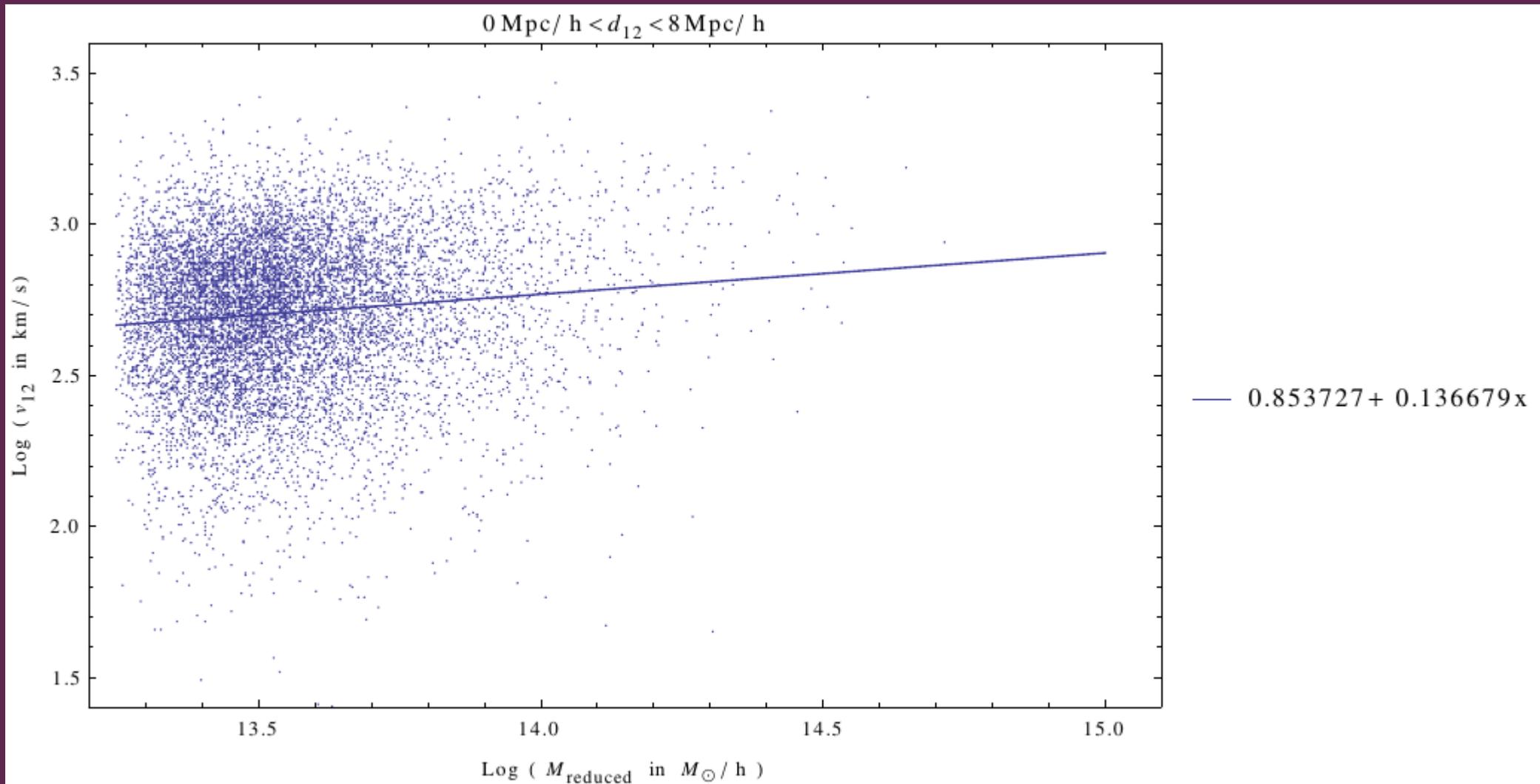
Prelim.



Bound system?

For a gravitationally bound system
expect the scaling to be $v_{12} \sim M^{1/2}$

Prelim.

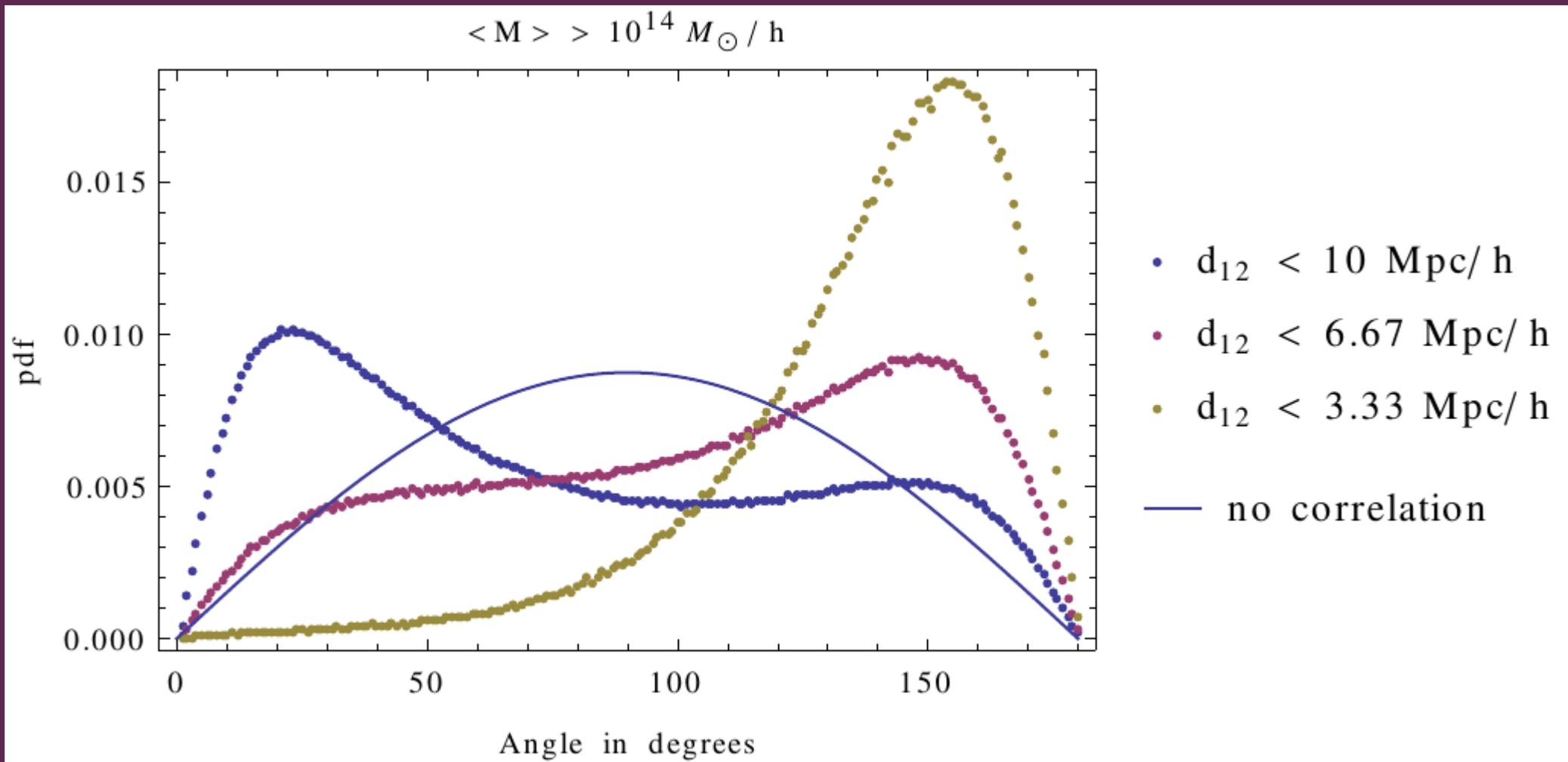


Collisional angle dependence on distance

For smaller distances we expect the halos to deviate from the Hubble flow (0°) and become more likely to be in a head-on collision (180°)

Collisional angle dependence on distance

For smaller distances we expect the halos to deviate from the Hubble flow (0°) and become more likely to be in a head-on collision (180°)



Collisional angle dependence on pairwise velocity

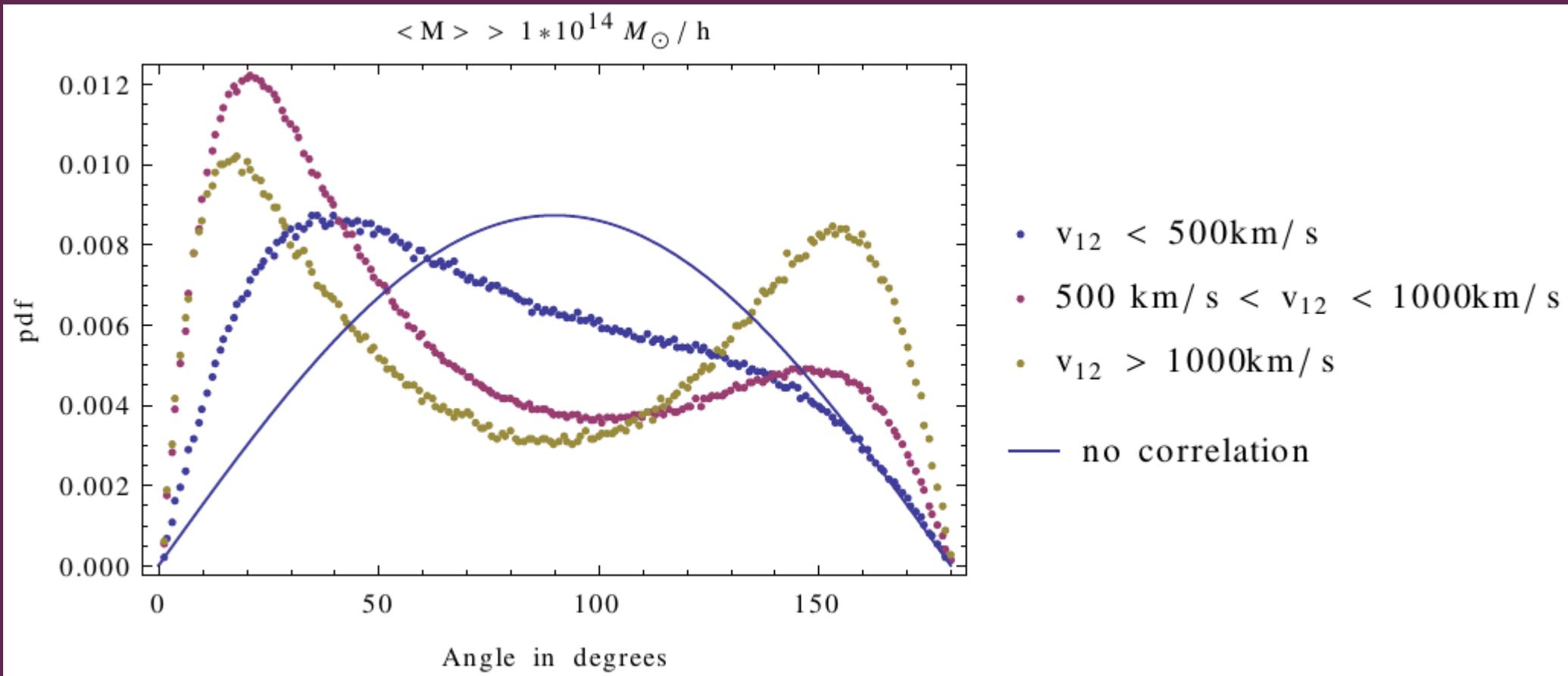
High pairwise relative velocities are not from the Hubble flow and originate from the attractive force and are expected to be more head-on

Prelim.

Collisional angle dependence on pairwise velocity

High pairwise relative velocities are not from the Hubble flow and originate from the attractive force and are expected to be more head-on

Prelim.



Collisional angle dependence on mass

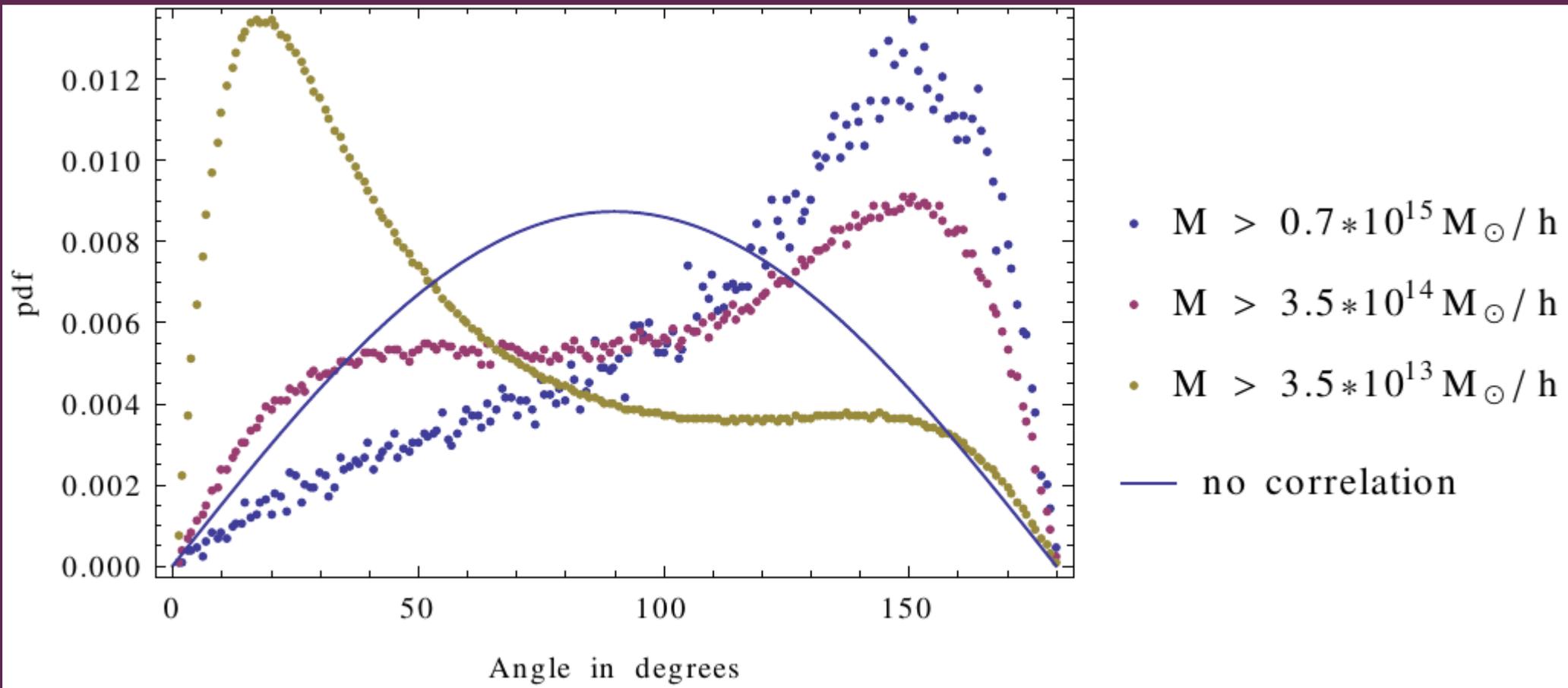
For a fixed distance we expect the more massive halos to attract gravitationally more and therefore have a larger probability for a head-on collision

Prelim.

Collisional angle dependence on mass

For a fixed distance we expect the more massive halos to attract gravitationally more and therefore have a larger probability for a head-on collision

Prelim.



Mass vs pairwise velocity

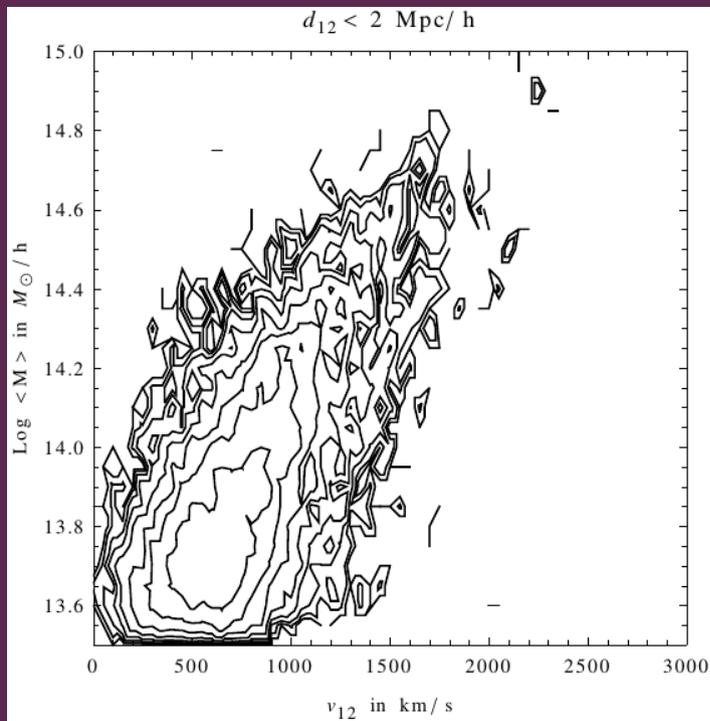
Pairs of halos consist of two populations with different M vs v_{12} distribution determined by the relative distance d_{12}

Prelim.

Mass vs pairwise velocity

Pairs of halos consist of two populations with different M vs v_{12} distribution determined by the relative distance d_{12}

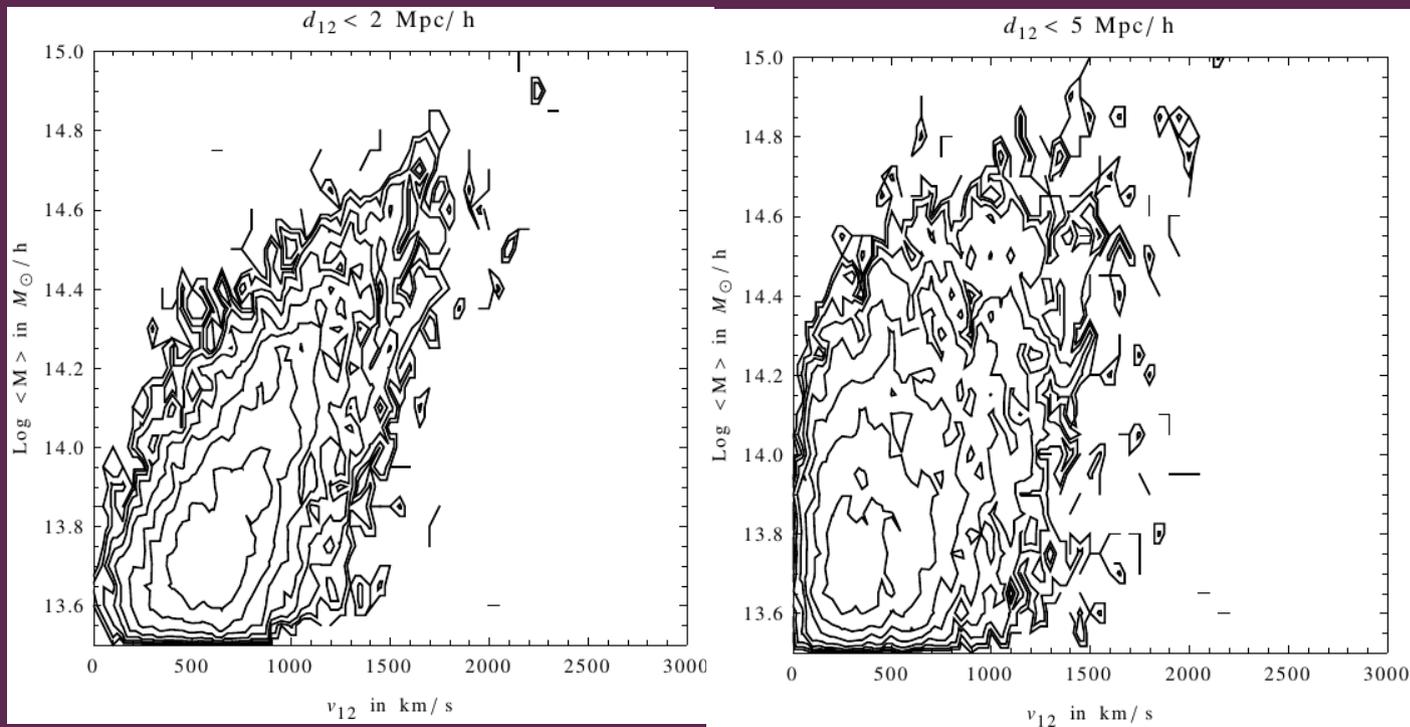
Prelim.



Mass vs pairwise velocity

Pairs of halos consist of two populations with different M vs v_{12} distribution determined by the relative distance d_{12}

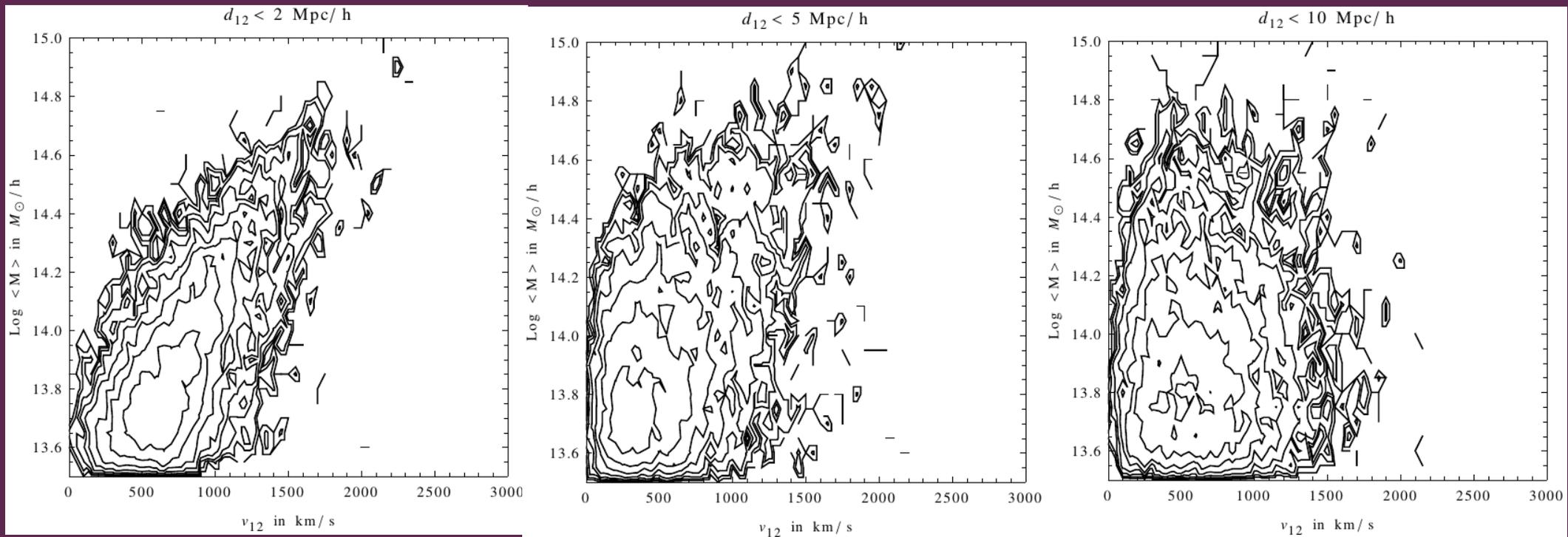
Prelim.



Mass vs pairwise velocity

Pairs of halos consist of two populations with different M vs v_{12} distribution determined by the relative distance d_{12}

Prelim.

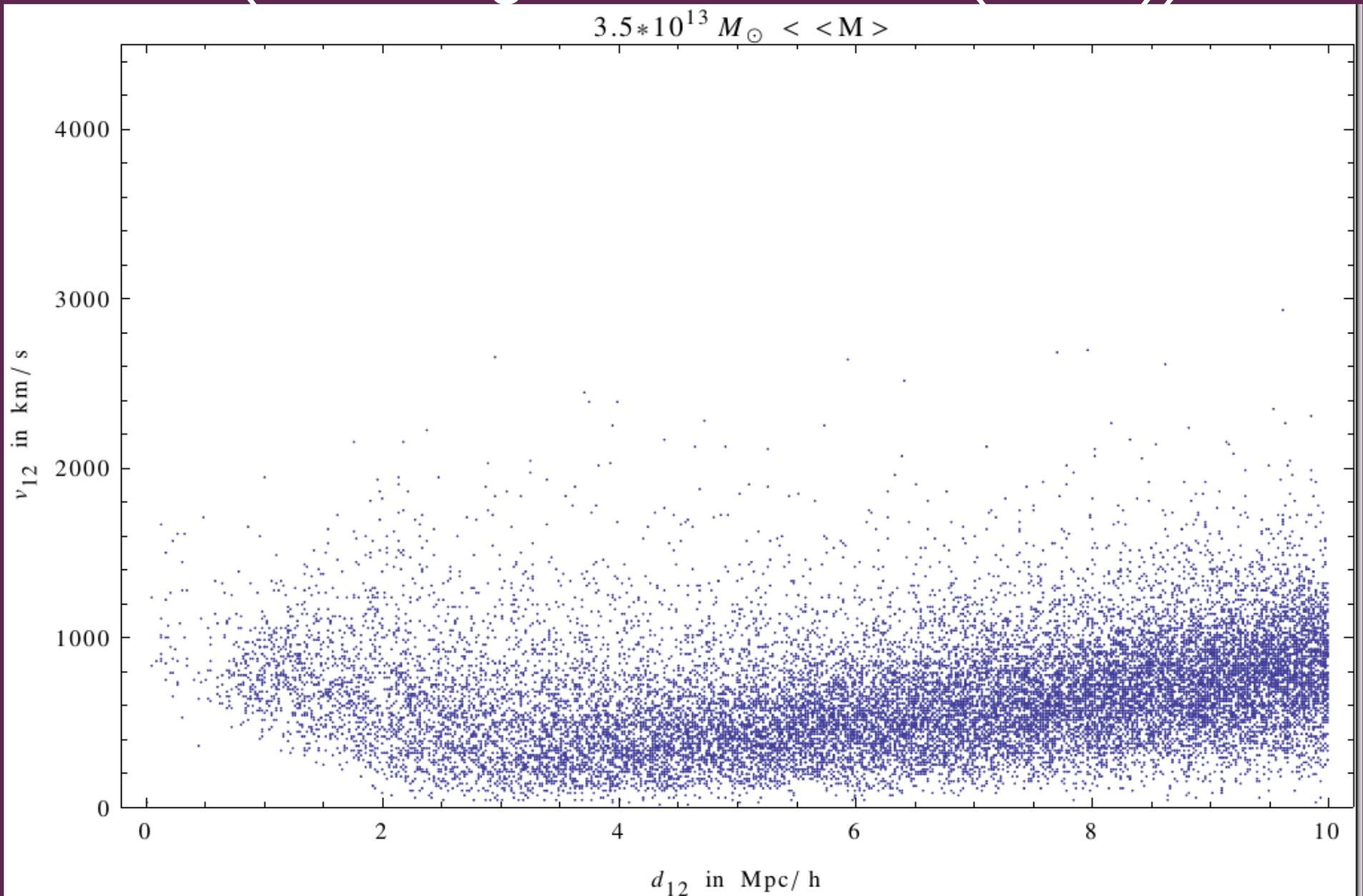


Relative velocity vs relative distance (following Watson et al. (2013))

Prelim.

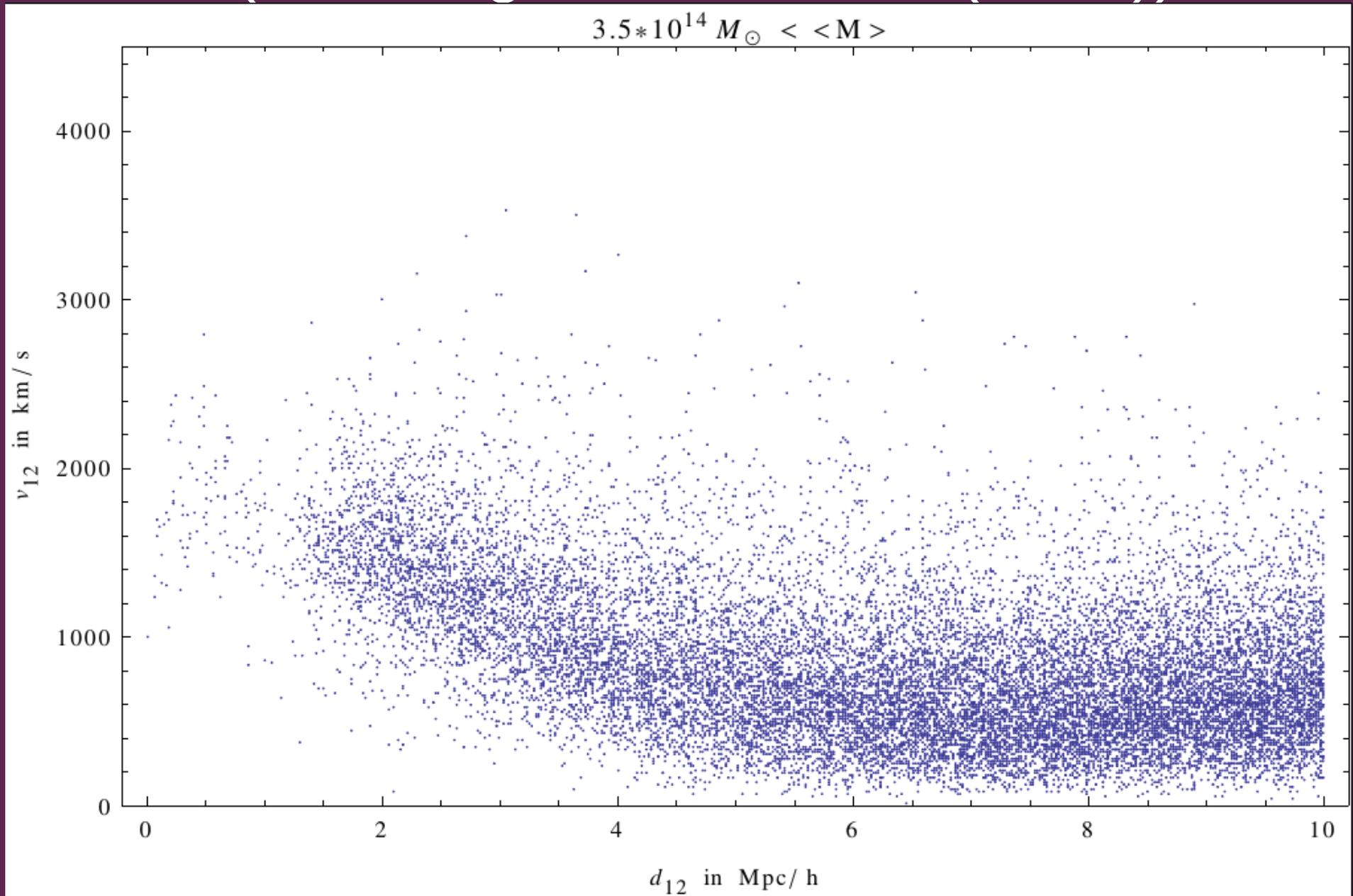
Relative velocity vs relative distance (following Watson et al. (2013))

Prelim.



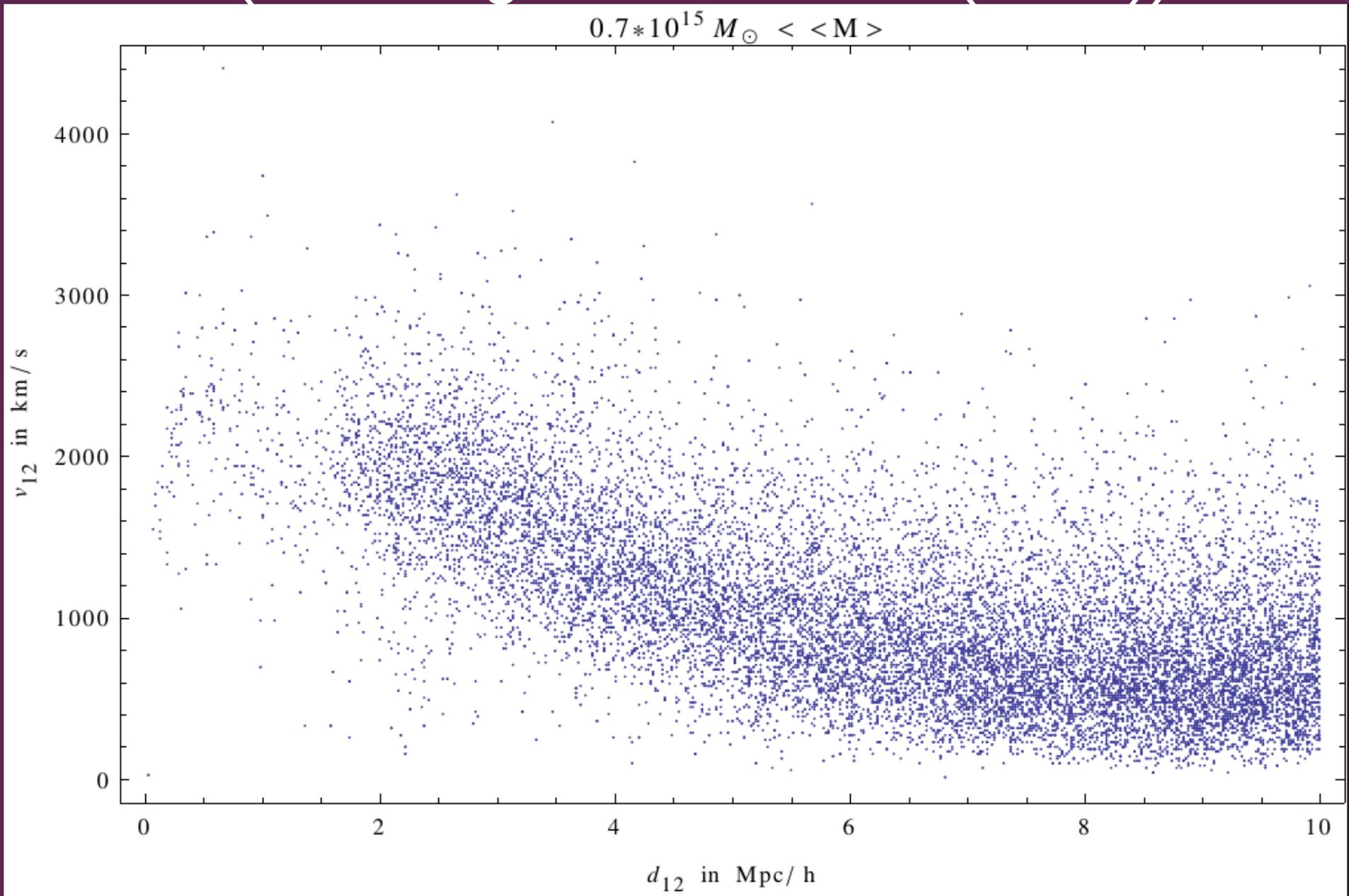
Relative velocity vs relative distance (following Watson et al. (2013))

Prelim.



Relative velocity vs relative distance (following Watson et al. (2013))

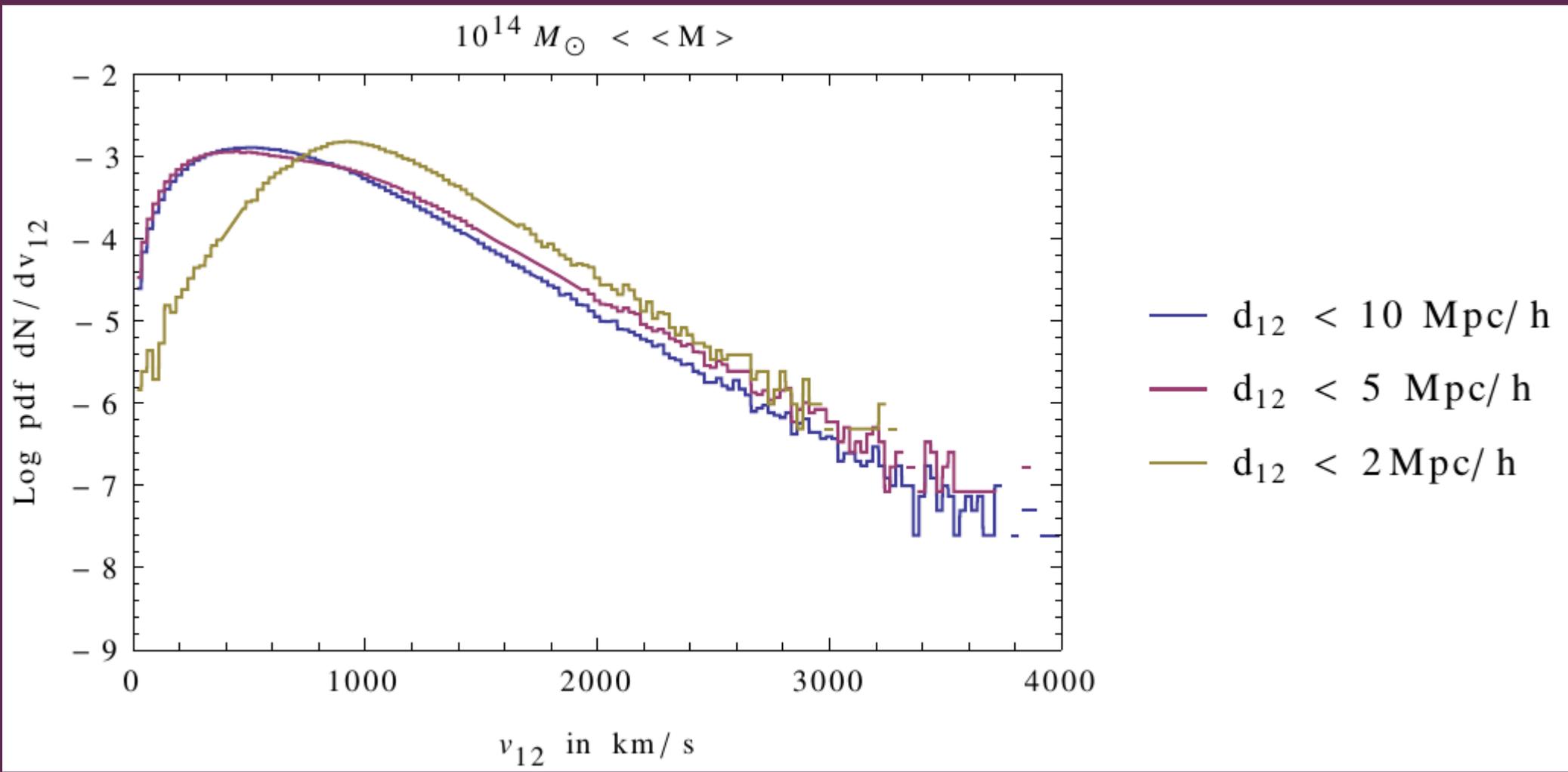
Prelim.



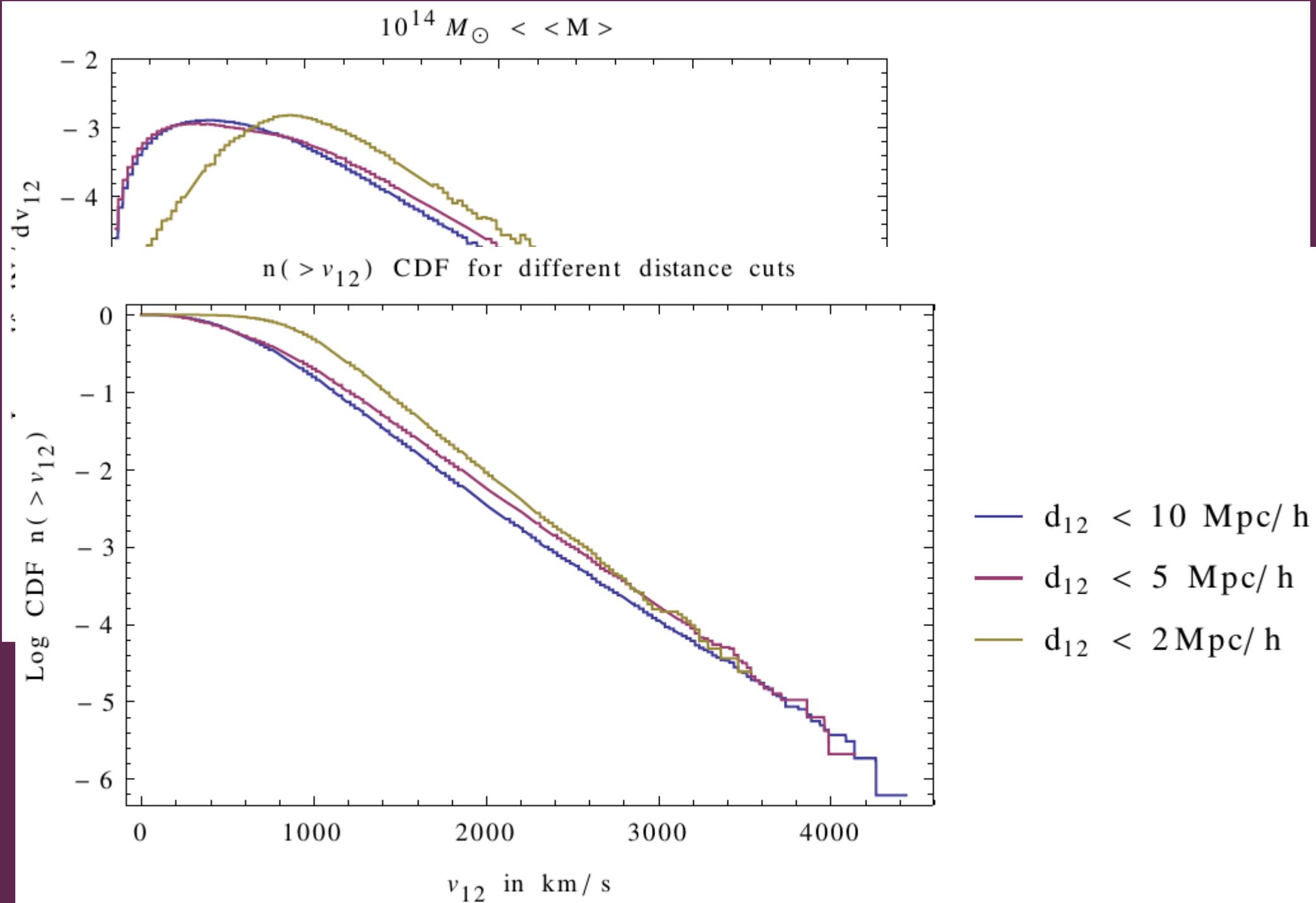
Relative velocity PDF dependence on distance cuts Prelim.



Relative velocity PDF dependence on distance cuts Prelim.



Relative velocity PDF dependence on distance cuts Prelim.



Relative velocity PDF dependence on angle cuts

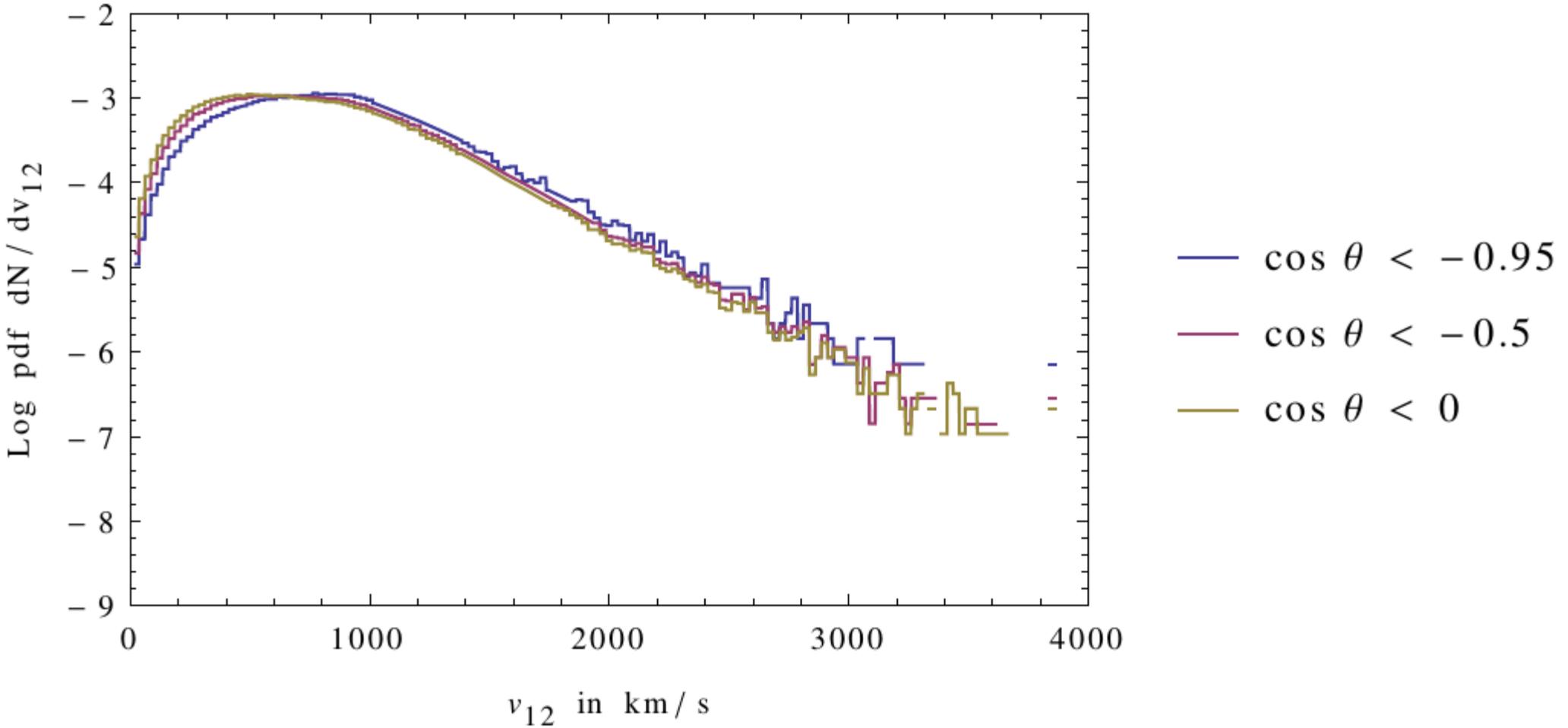
Prelim.

Relative velocity PDF dependence on angle cuts

Relative velocity PDF dependence on angle cuts

Prelim.

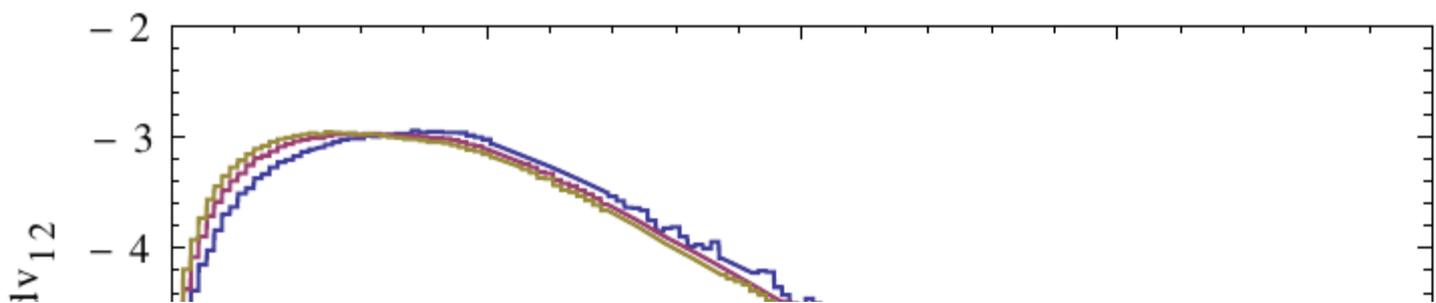
$10^{14} M_{\odot} < \langle M \rangle, d_{12} < 5 \text{ Mpc}/h$



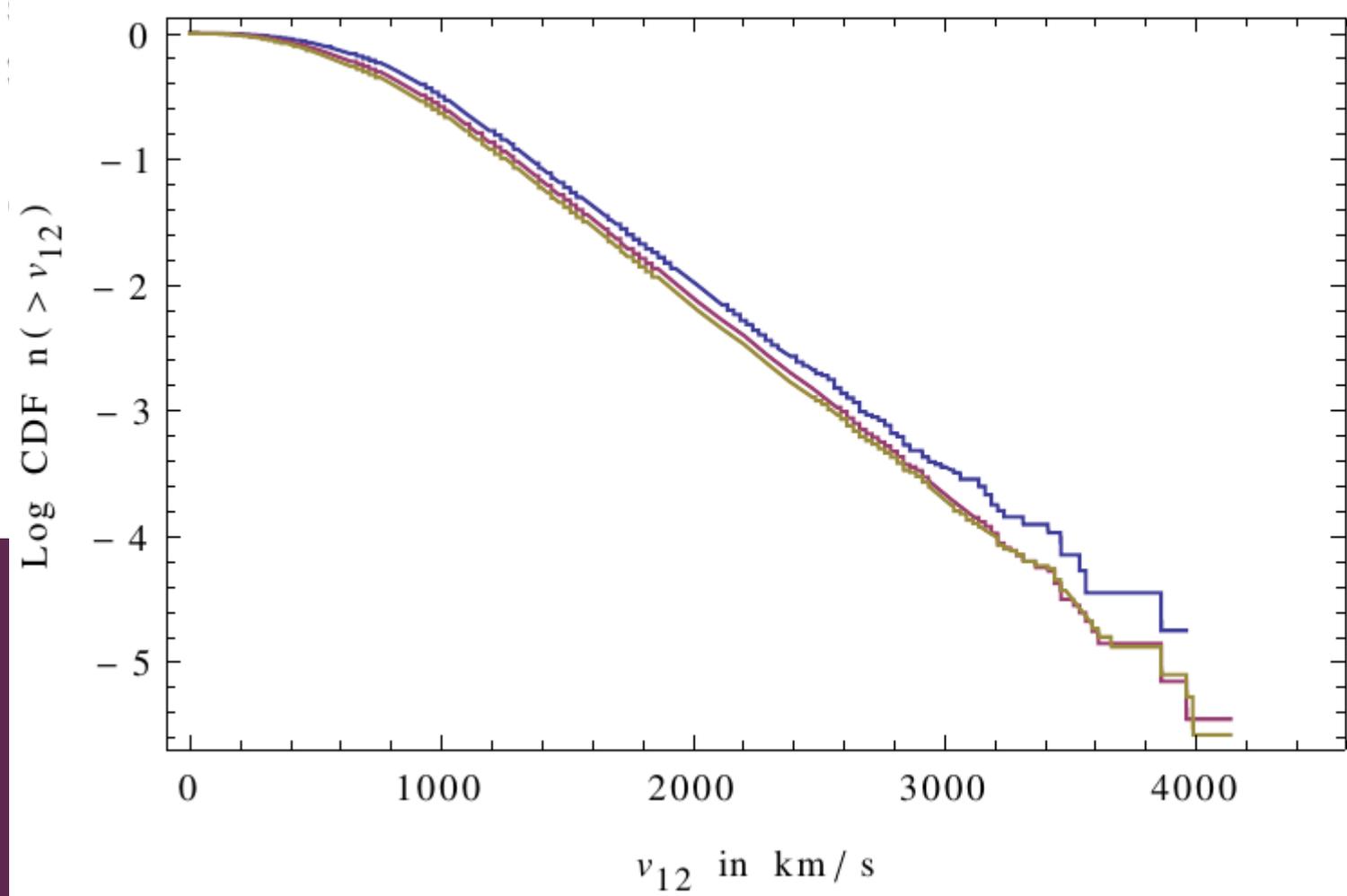
Relative velocity PDF dependence on angle cuts

Prelim.

$10^{14} M_{\odot} < \langle M \rangle, d_{12} < 5 \text{ Mpc} / h$



$n(>v_{12})$ CDF for different angle cuts



- $\cos \theta < -0.95$
- $\cos \theta < -0.5$
- $\cos \theta < 0$

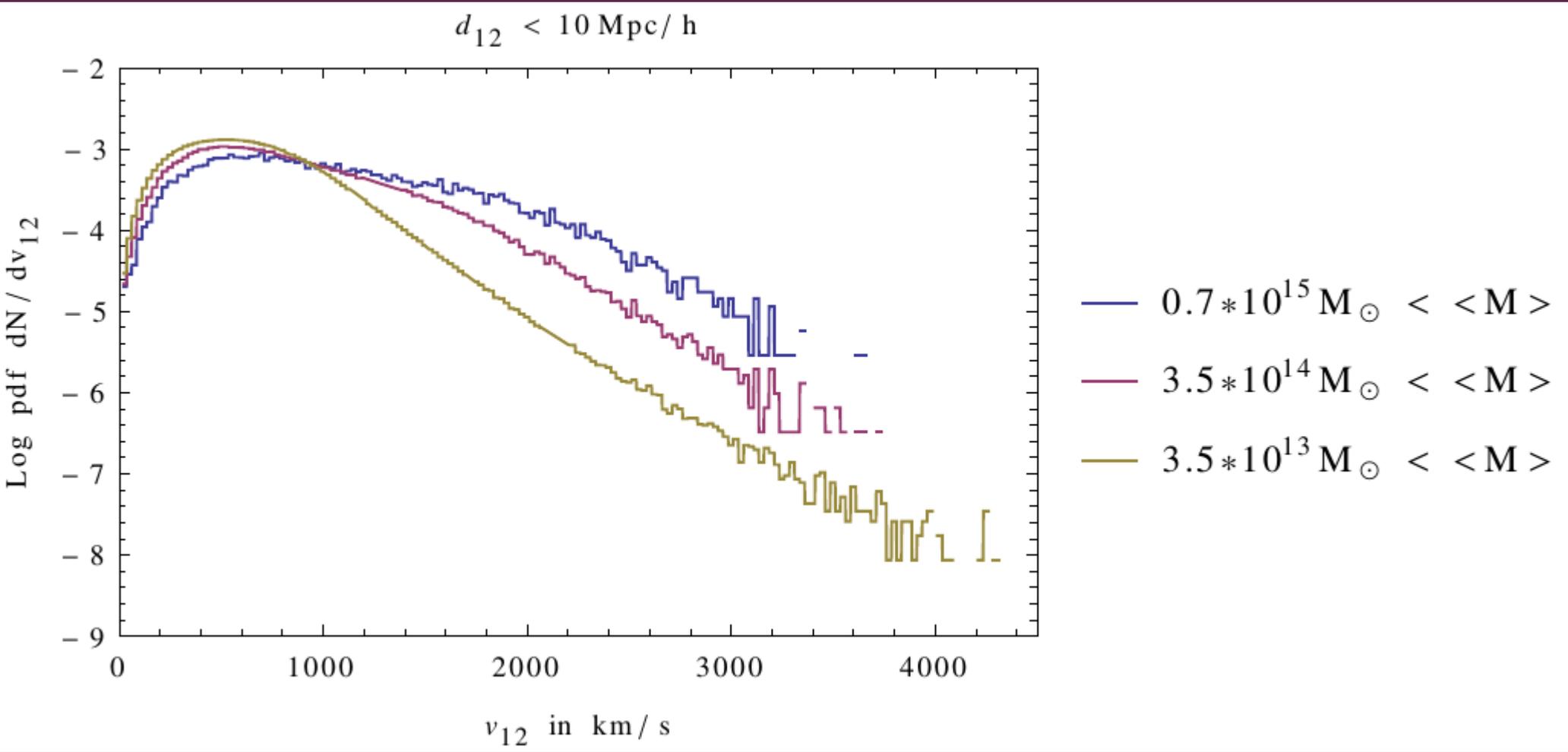
Relative velocity PDF dependence on mass cuts

Prelim.

Relative velocity PDF dependence on mass cuts

Relative velocity PDF dependence on mass cuts

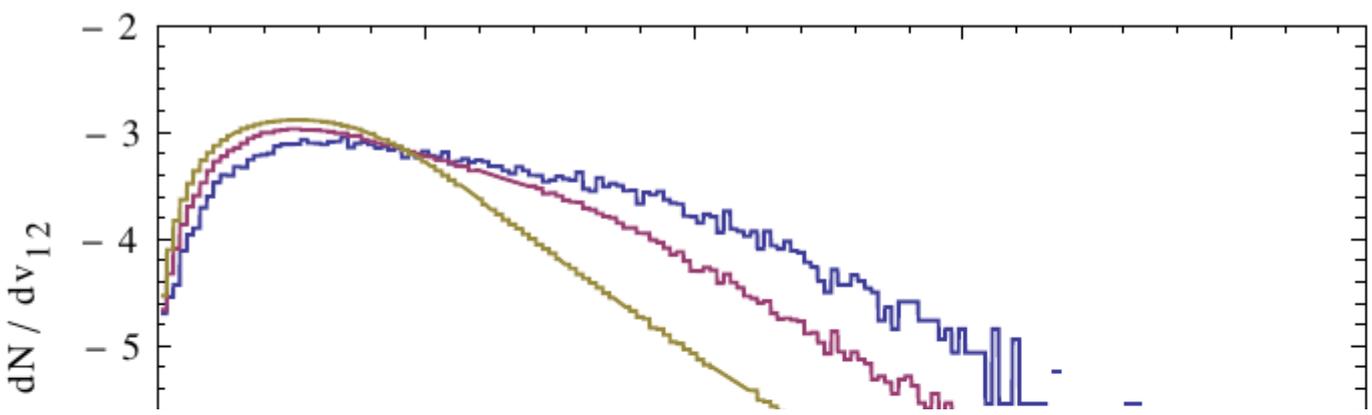
Prelim.



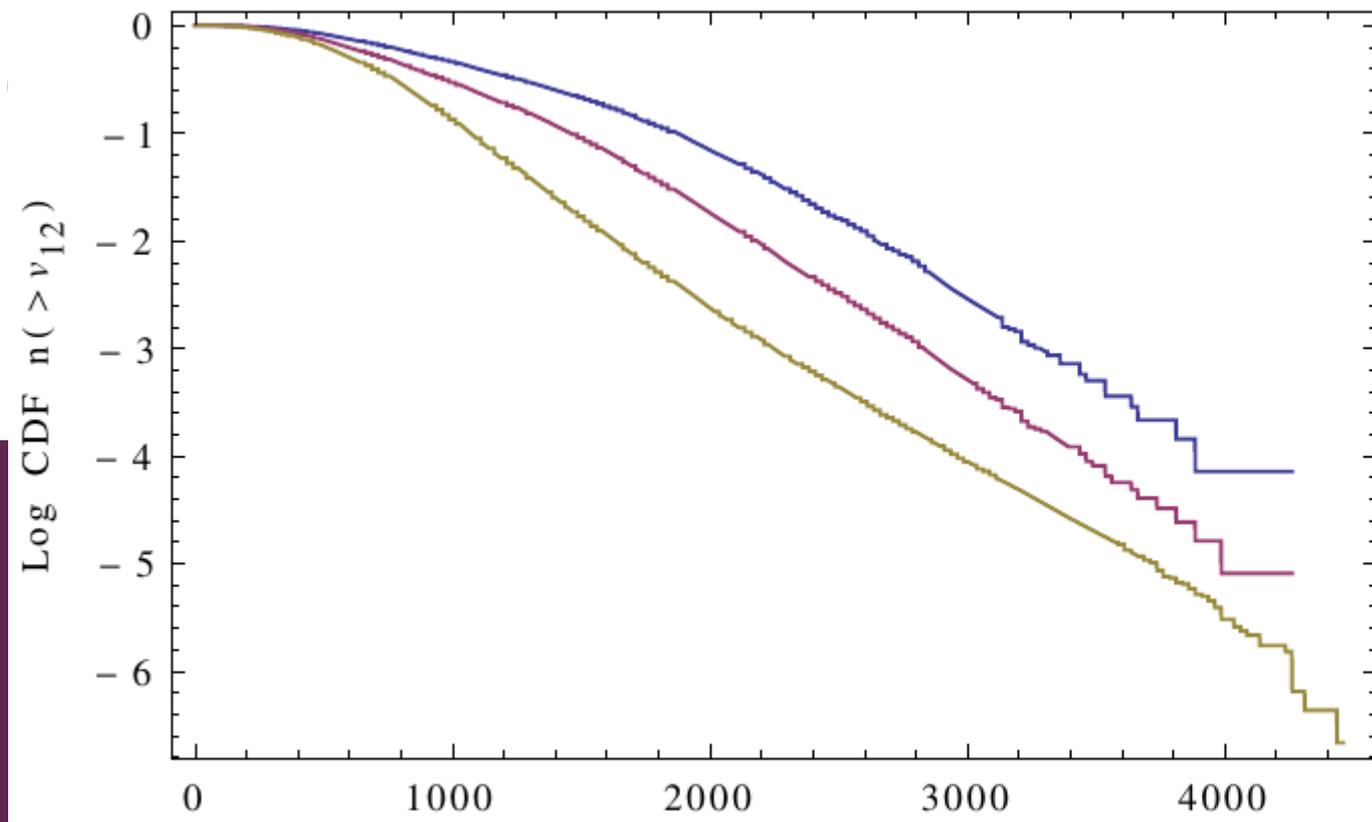
Relative velocity PDF dependence on mass cuts

Prelim.

$d_{12} < 10 \text{ Mpc}/h$



$n(>v_{12})$ CDF for different mass cuts



— $0.7 * 10^{15} M_{\odot} < <M>$

— $0.7 * 10^{15} M_{\odot} < <M>$

— $3.5 * 10^{14} M_{\odot} < <M>$

— $3.5 * 10^{13} M_{\odot} < <M>$

v_{12} in km/s

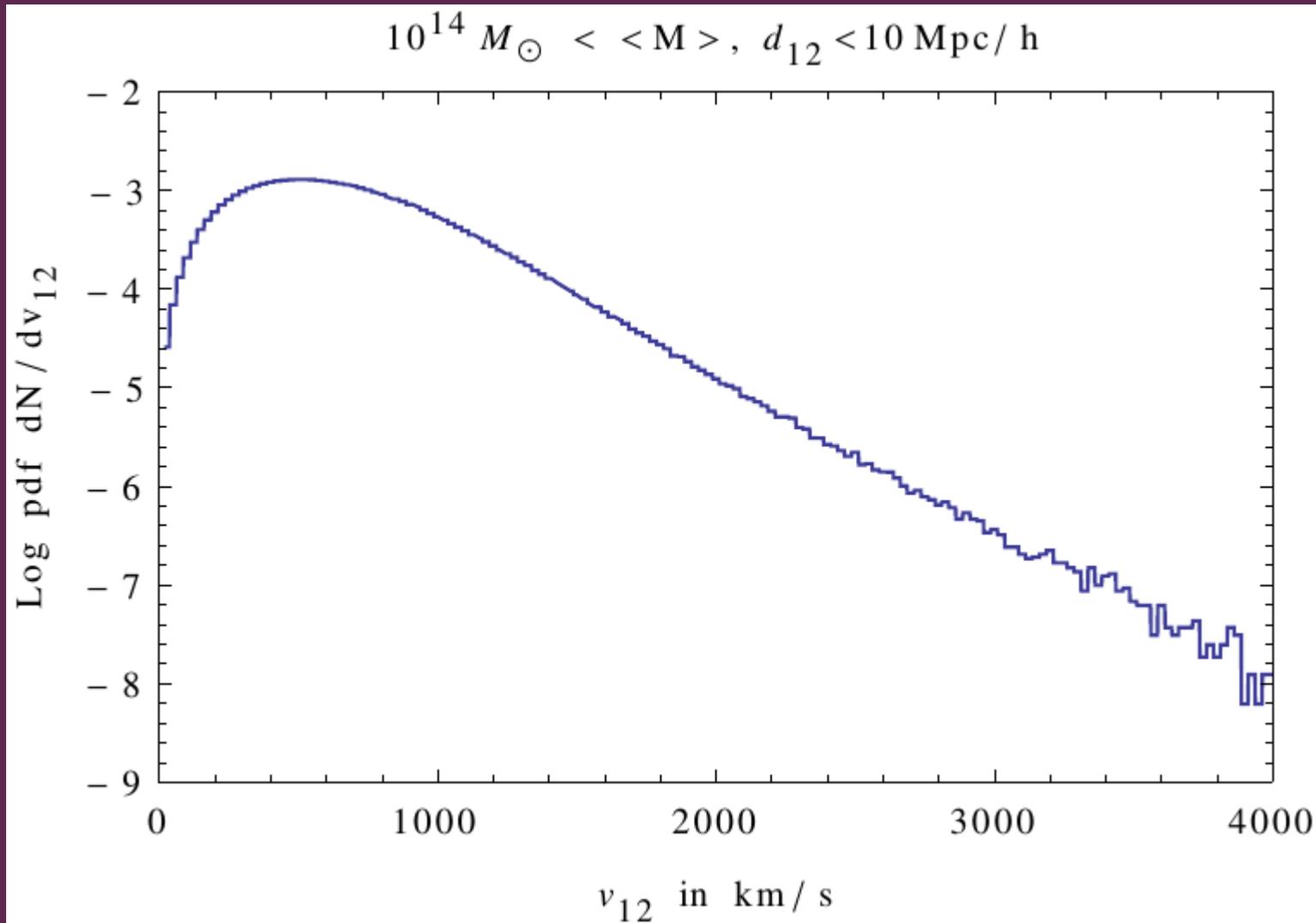
Probability of finding a bullet-like system in DS

(cuts from Thompson&Nagamine(2012) and Buillot et al. (2014) ~ M&B(2008) initial conditions)

Prelim.

Probability of finding a bullet-like system in DS

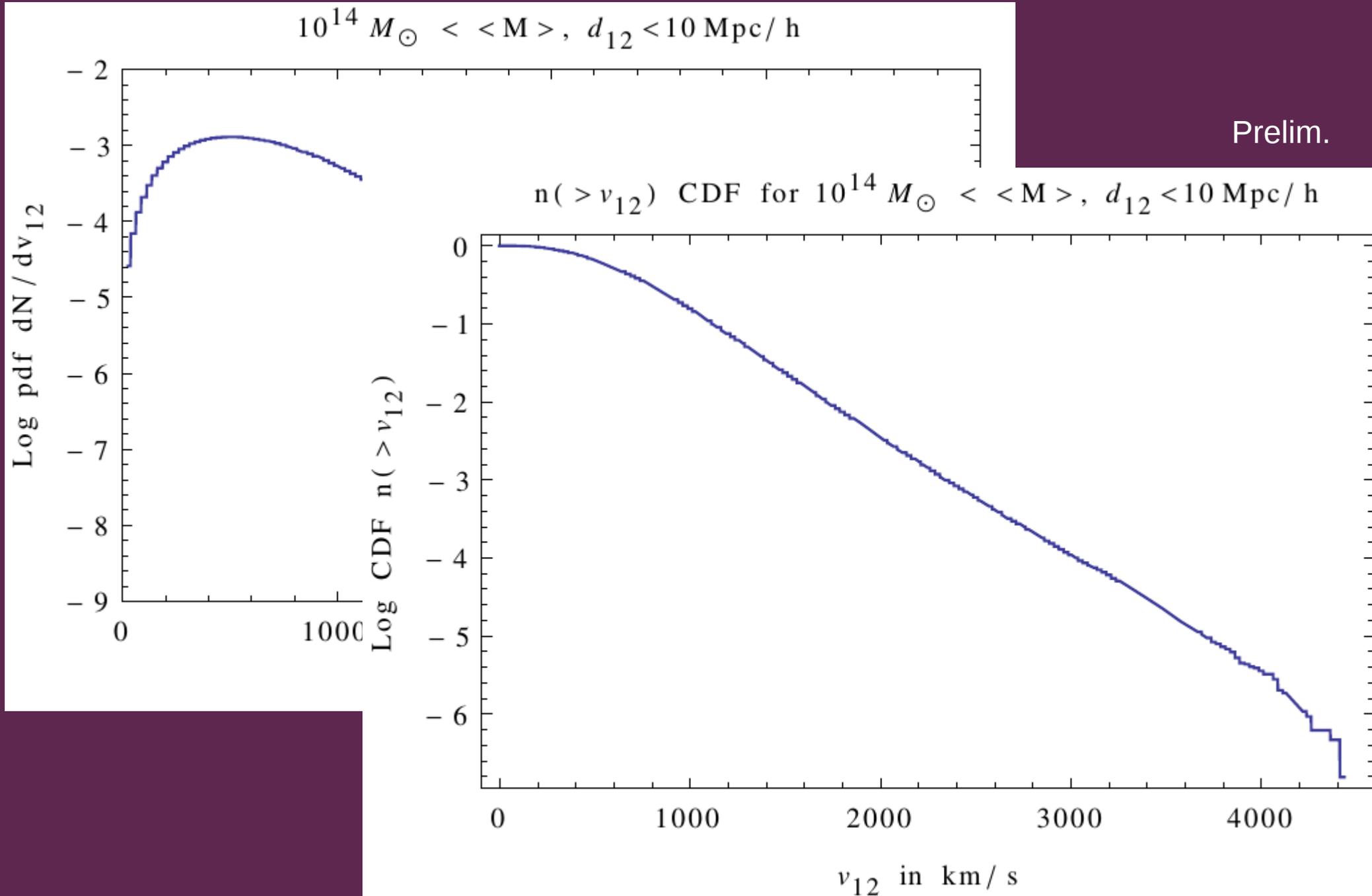
(cuts from Thompson&Nagamine(2012) and Buillot et al. (2014) ~ M&B(2008) initial conditions)



Prelim.

Probability of finding a bullet-like system in DS

(cuts from Thompson&Nagamine(2012) and Buillot et al. (2014) ~ M&B(2008) initial conditions)



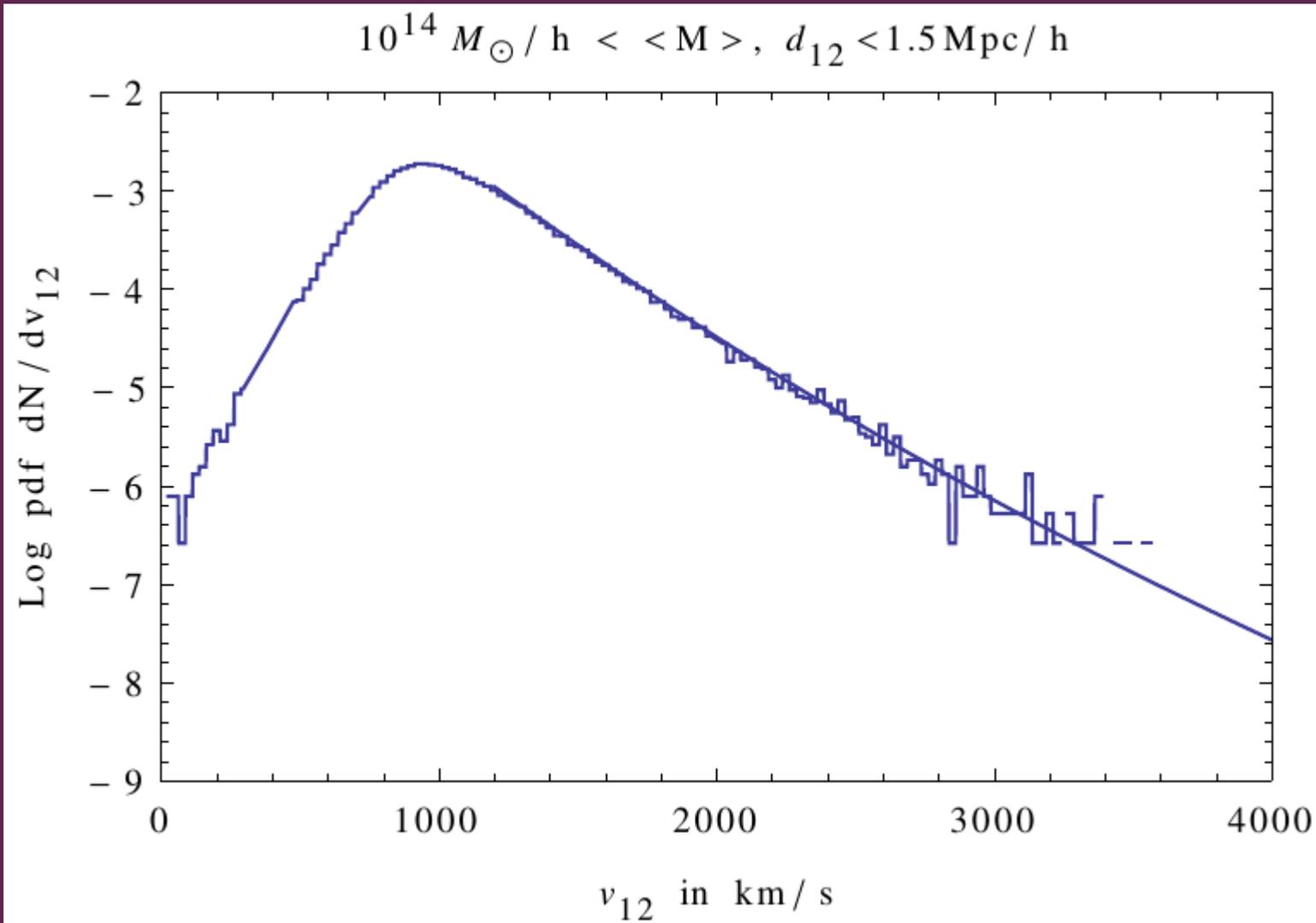
Probability of finding a bullet-like system in DS

(cuts of Watson et al.(2013))

Prelim.

Probability of finding a bullet-like system in DS

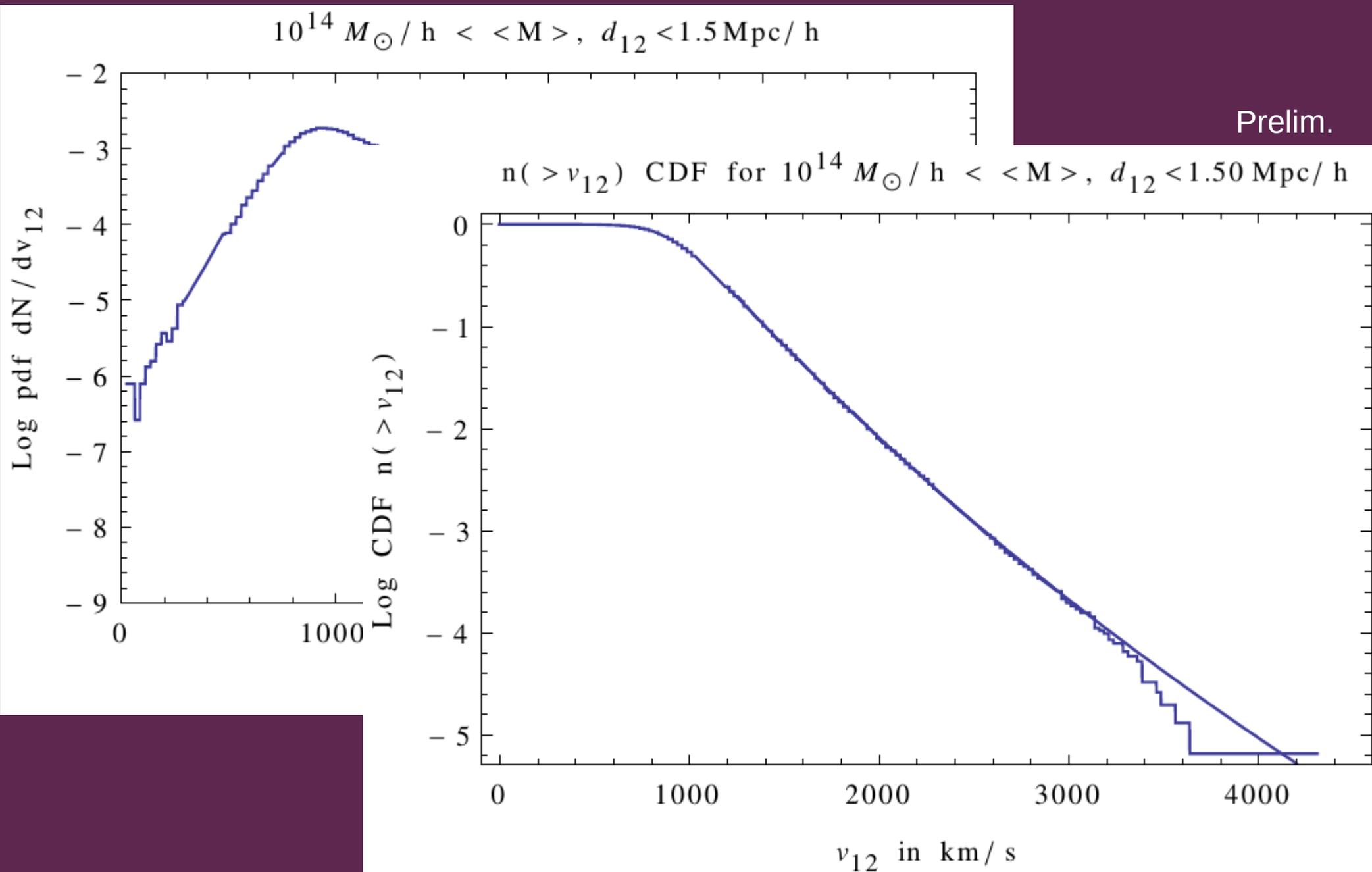
(cuts of Watson et al.(2013))



Prelim.

Probability of finding a bullet-like system in DS

(cuts of Watson et al.(2013))



Summary

Summary

- Bullet Cluster system offers an opportunity to check LCDM for consistency
- But only now the N-Body simulations have become big enough to start answering the question
- Probability low $\sim 10^{-4}$ but higher than in previous similar studies
- Effect of halofinder on the high-velocity tail needs to be resolved

Summary

- Bullet Cluster system offers an opportunity to check LCDM for consistency
- But only now the N-Body simulations have become big enough to start answering the question
- Probability low $\sim 10^{-4}$ but higher than in previous similar studies
- Effect of halofinder on the high-velocity tail needs to be resolved

Summary

- Bullet Cluster system offers an opportunity to check LCDM for consistency
- But only now the N-Body simulations have become big enough to start answering the question
- Probability low $\sim 10^{-4}$ but higher than in previous similar studies
- Effect of halofinder on the high-velocity tail needs to be resolved

Summary

- Bullet Cluster system offers an opportunity to check LCDM for consistency
- But only now the N-Body simulations have become big enough to start answering the question
- Probability low $\sim 10^{-4}$ but higher than in previous similar studies
- Effect of halofinder on the high-velocity tail needs to be resolved