

# Neutrino Theory and Phenomenology:

## Lecture I



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**The lectures are intended for a broad audience of students with competences in different fields in particle physics**

**The goal is to “get you (more) interested” in  $\nu$  physics, by moving from basic neutrino properties and phenomena to more advanced topics at the current frontier of the field.**

**Some exercises are also proposed on  $\nu$  oscill. probabilities. (see Tutorial pdf file). Others are contained in the slides.**

People interested in further reading can usefully browse the “Neutrino Unbound” website: [www.nu.to.infn.it](http://www.nu.to.infn.it) , or just email me for advice about specific topics: [eligio.lisi@ba.infn.it](mailto:eligio.lisi@ba.infn.it)

## Outline of lectures:

### Lecture I

Pedagogical intro + warm-up case study for oscillations

### Lecture II

Standard  $3\nu$  oscillations: evolution and current status

### Lecture III

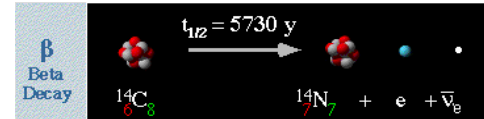
Neutrino absolute masses + open problems in  $\nu$  physics

**Feel free to stop me and ask questions at any time!**

# Pedagogical Introduction

# The neutrino will celebrate its 86<sup>th</sup> birthday in December!

This particle was invented in 1930 by Wolfgang Pauli as a “desperate remedy” to explain the continuous  $\beta$ -ray spectrum via a 3-body decay, e.g.,



*Original: Photocopy of Pauli 0393*  
Abschrift/15.12.56 PM

Offener Brief an die Gruppe der Radioaktiven bei der  
Gauvereins-Tagung zu Tübingen.

Abschrift  
Physikalisches Institut  
der Eidg. Technischen Hochschule  
Zürich

Zürich, 4. Des. 1930  
Gloriastrasse

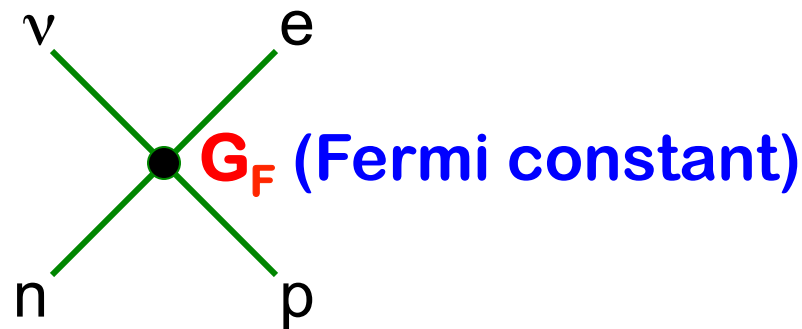
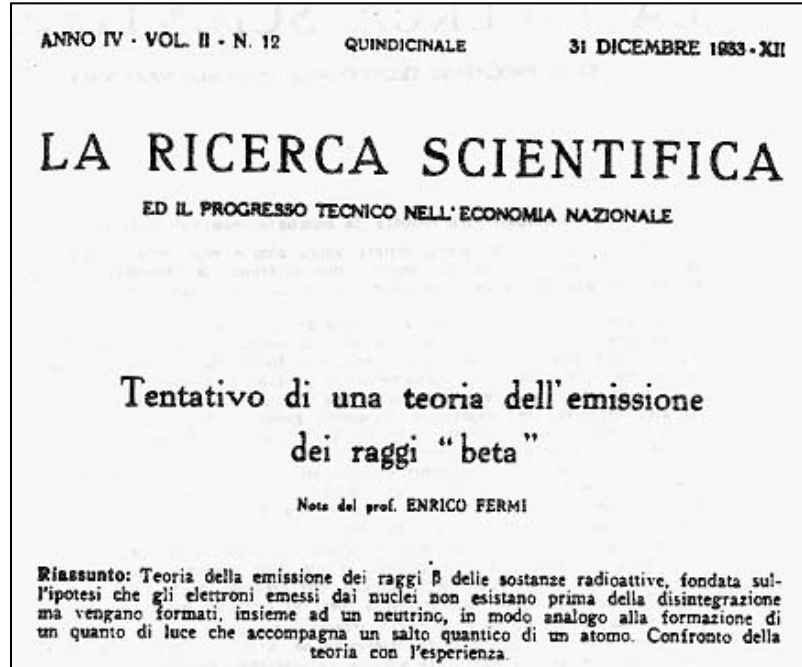
Liebe Radioaktive Damen und Herren,

Wie der Ueberbringer dieser Zeilen, den ich halbvollst  
ansuhren bitte, Ihnen des nÄheren auseinandersetzen wird, bin ich  
angesichts der "falschen" Statistik der N- und Li-6 Kerne, sowie  
des kontinuierlichen beta-Spektrums auf einen verweifelten Ausweg  
verfallen um den "Wechselst" (i) der Statistik und den Energiesatz  
zu retten. Nämlich die Möglichkeit, es könnten elektrisch neutrals  
Teilchen, die ich Neutronen nennen will, in den Kernen existieren,  
welche den Spin 1/2 haben und das Ausschliessungsprinzip befolgen und  
sich von Lichtquanten ausserdem noch dadurch unterscheiden, dass sie  
nicht mit Lichtgeschwindigkeit laufen. Die Masse der Neutronen  
wäre von derselben Grössenordnung wie die Elektronenmasse sein und  
jedenfalls nicht grösser als 0.01 Protonenmasse. Das kontinuierliche  
beta-Spektrum wäre dann verständlich unter der Annahme, dass beim  
beta-Zerfall mit dem Elektron jeweils noch ein Neutron emittiert  
wird, derart, dass die Summe der Energien von Neutron und Elektron  
konstant ist.



Kinematics: **spin 1/2**, **tiny mass**, **zero electric charge**

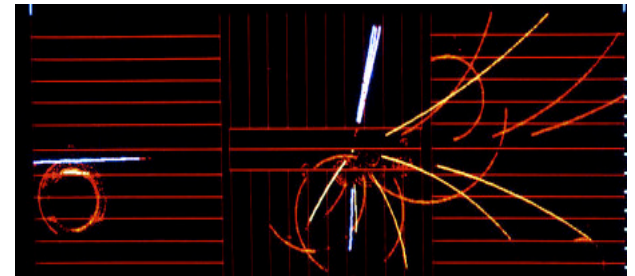
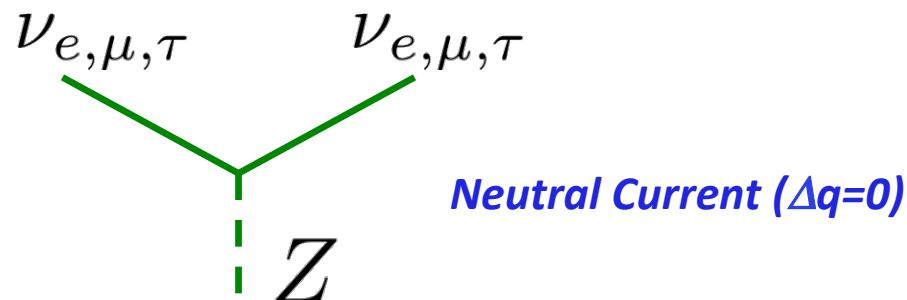
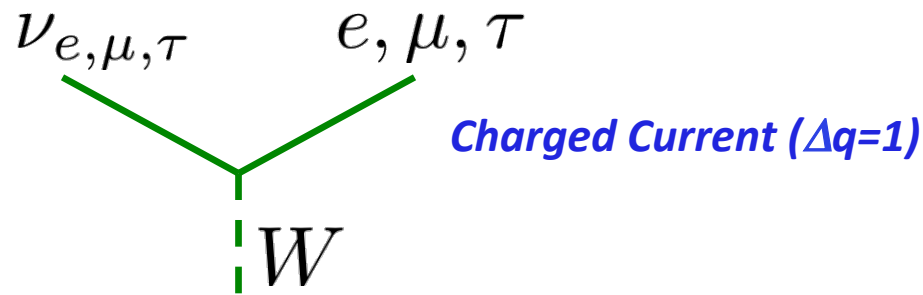
The name “neutrino” (=“little neutral one”, in Italian) was actually invented by Enrico Fermi, who first proposed in 1933-34 a theory for its **dynamics** (weak interactions)



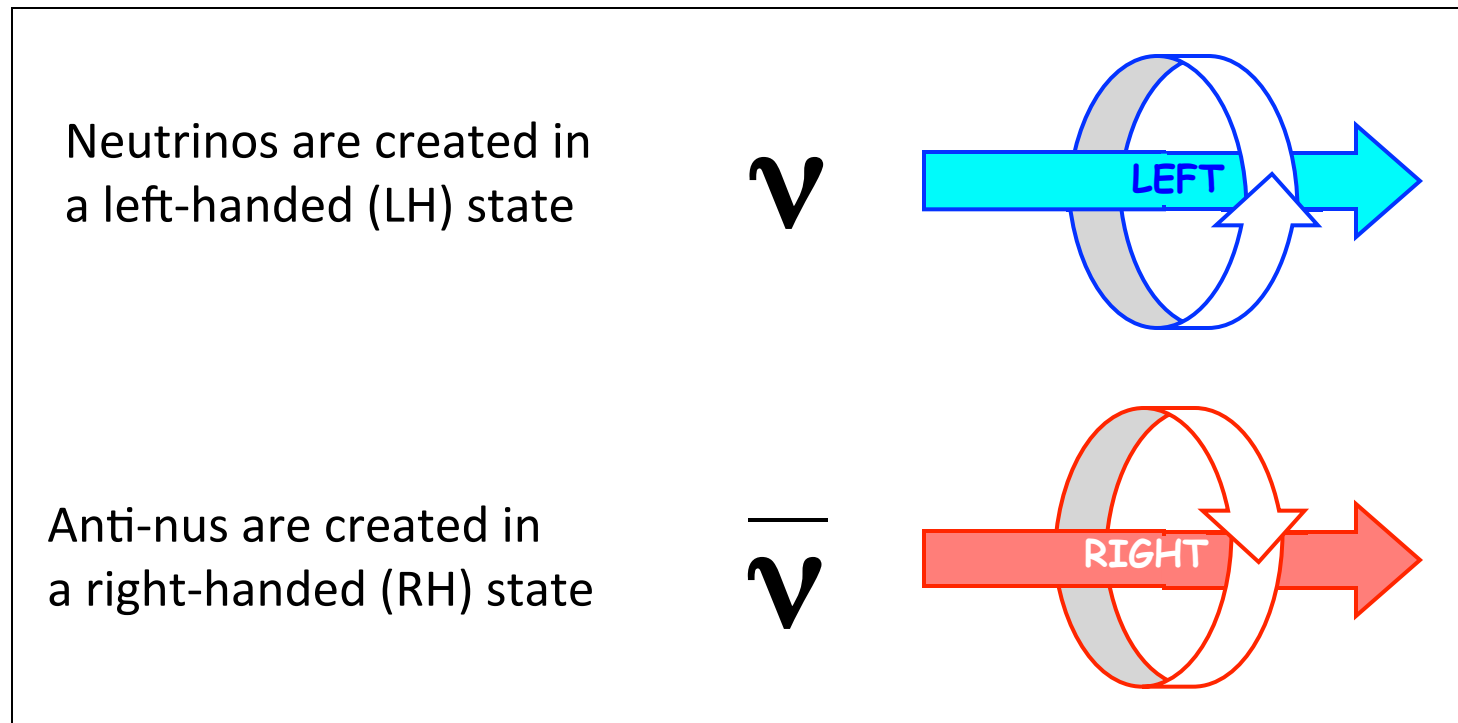
Many decades of research have revealed other properties of the **neutrino**. For instance, there are **3 different  $\nu$  “flavors”  $e \mu \tau$**

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix} \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix} \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix} \begin{matrix} \leftarrow q = 0 \\ \leftarrow q = -1 \end{matrix} \quad (\Delta q = 1)$$

and their Fermi interactions are mediated by a charged **vector boson  $W$** , with a neutral counterpart, the  **$Z$  boson**



Such interactions are chiral (= not mirror-symmetric):



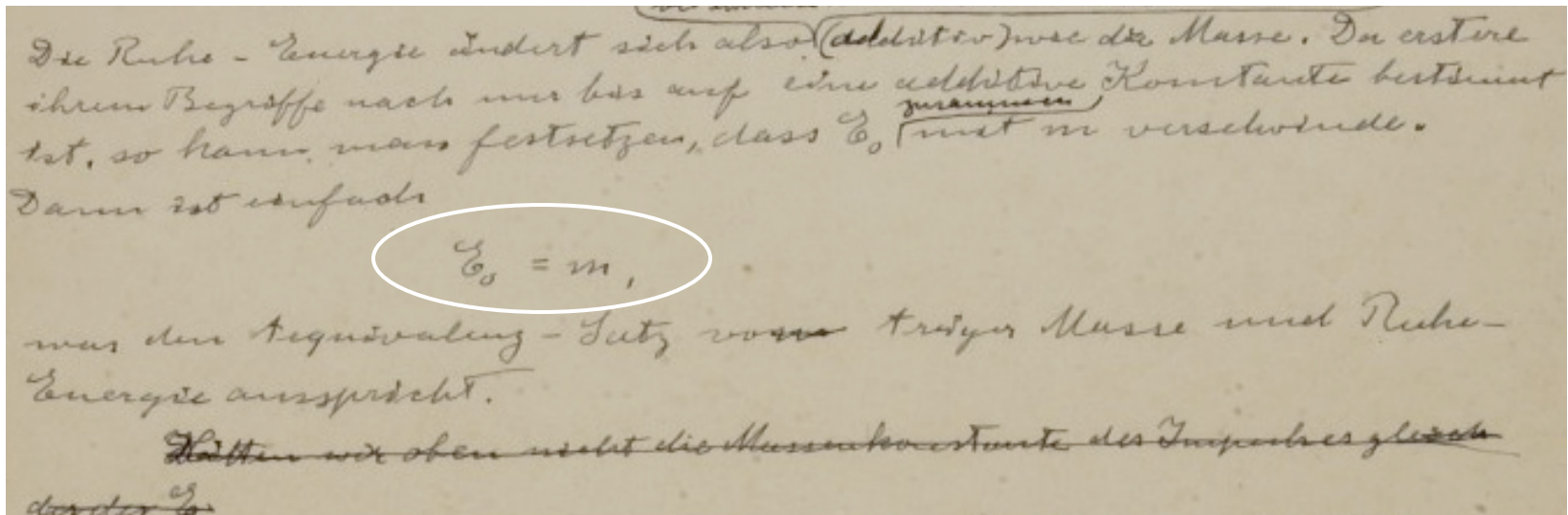
The handedness is a constant of motion only for massless neutrinos. It is “almost” constant –at  $O(m/E)$ - for ultrarelativistic  $\nu$  with mass  $m$ .

We shall “forget” about neutrino handedness and spin for a while, until mass effects at  $O(m/E)$  will be reconsidered in Lecture III.



Most of the recent progress in  $\nu$  physics has actually been driven by another kind of effects, at  $O(m^2/E)$ : **neutrino flavor oscillations**

The starting point is a century-old equation ...



... namely, for  $p \neq 0$ : 
$$E = \sqrt{m^2 + p^2}$$

(in natural units)

Our ordinary experience takes place in the limit:  $p \ll m$

$$E \simeq m + \frac{p^2}{2m}$$

... while for neutrinos the proper limit is:  $p \gg m$

$$E \simeq p + \frac{m^2}{2p}$$

Energy difference between two neutrinos  $\nu_i$  e  $\nu_j$  with mass  $m_i$  e  $m_j$  in the same beam ( $p_i = p_j \simeq E$ ) :

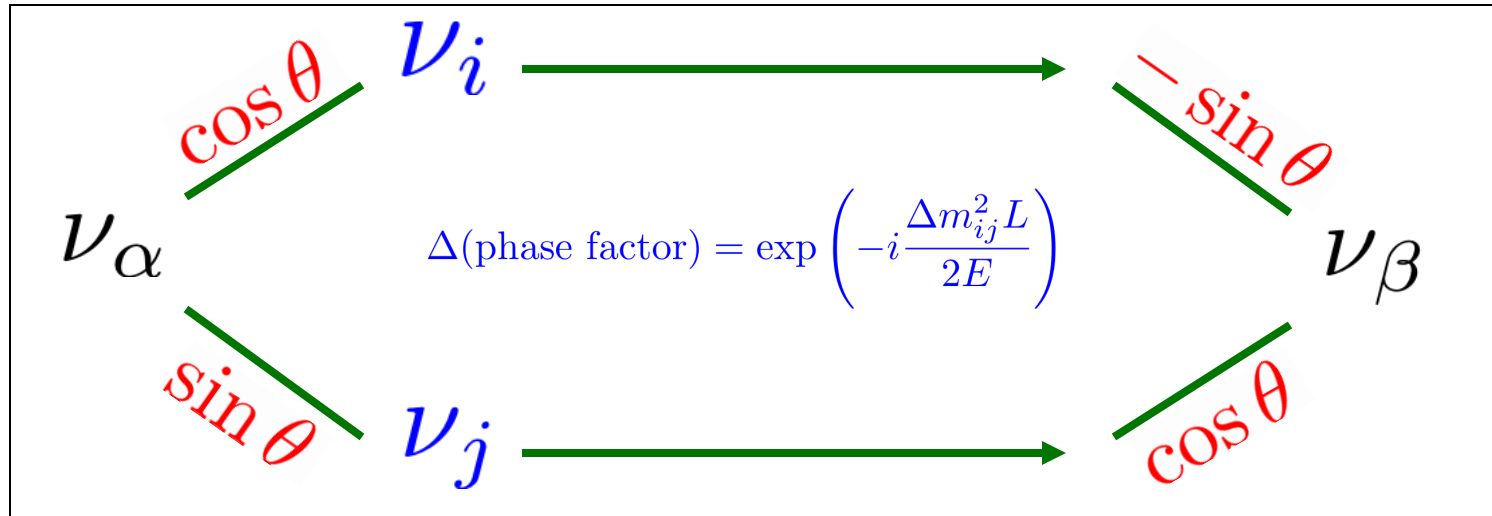
$$\Delta E \simeq \frac{\Delta m_{ij}^2}{2E}$$

**PMNS\***: neutrinos with definite mass ( $\nu_i$  and  $\nu_j$ ) might have NO definite flavor ( $\nu_\alpha$  e  $\nu_\beta$ ), e.g.,

$$\begin{pmatrix} \nu_\alpha \\ \nu_\beta \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_i \\ \nu_j \end{pmatrix}$$

\*Pontecorvo; Maki, Nakagawa & Sakata

## Analogy with a two-slit interference experiment in vacuum:



This is the simplest case (only 2 $\nu$  involved, no interactions with matter). It shows that, if neutrinos are massive and mixed (like quarks), then flavor is not a good quantum number during propagation.

Indeed, it changes (“oscillates”) significantly over a distance  $L$  ( $=x \approx \Delta t$ ) dictated by the uncertainty relation:

$$1 \sim \Delta E \Delta t \simeq \frac{m_i^2 - m_j^2}{2E} L$$

One can easily derive that a neutrino created with **flavor**  $\alpha$  can develop in vacuum a different **flavor**  $\beta$  with periodical oscillation probability in  $L/E$ :

$$P(\nu_\alpha \rightarrow \nu_\beta) = 4 \sin^2 \theta \cos^2 \theta \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) \quad (\text{B. Pontecorvo})$$

**Amplitude**

(vanishes for  $\theta=0$  or  $\pi/2$ ,  
is maximal for  $\theta=\pi/4$ )

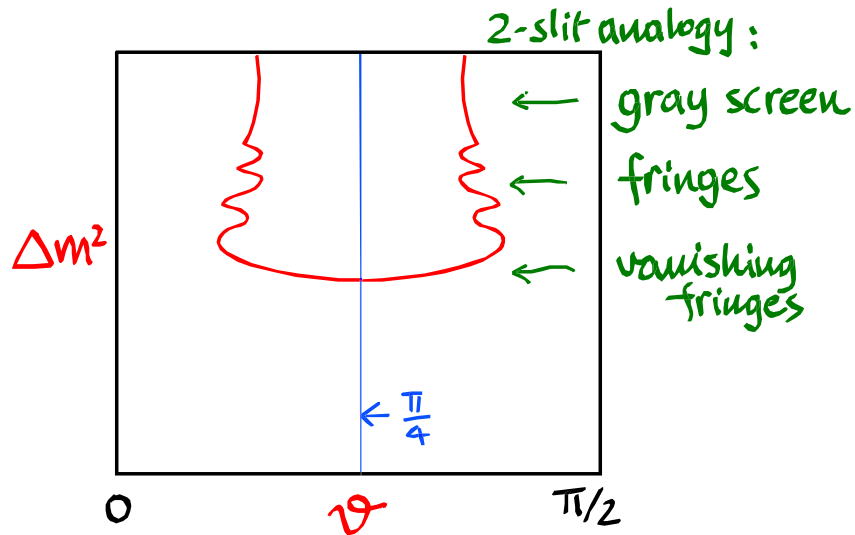
**Oscillation phase**

(vanishes for degenerate  
masses or small  $L/E$ )

Note 1 : This is the flavor “appearance” probability. The “disappearance” probability is the complement to 1.

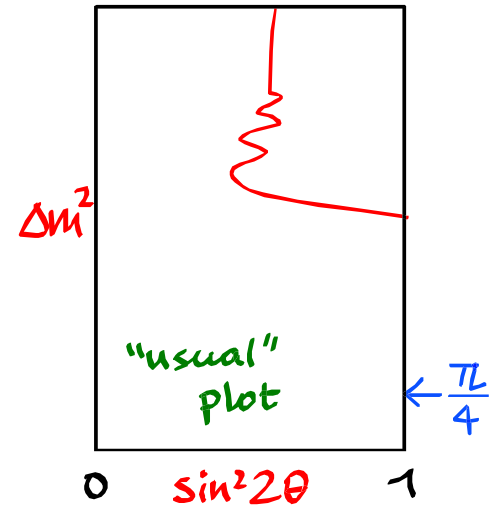
Note 2: The oscillation effect depends on the *difference* of (squared) masses, not on the *absolute masses themselves*.

# Typical iso- $\langle P_{\alpha\beta} \rangle$ contours



Octant symmetry:  $\theta \rightarrow \frac{\pi}{2} - \theta$  in  $P_{\mu\nu}$

If 2nd octant folded onto the 1st one:



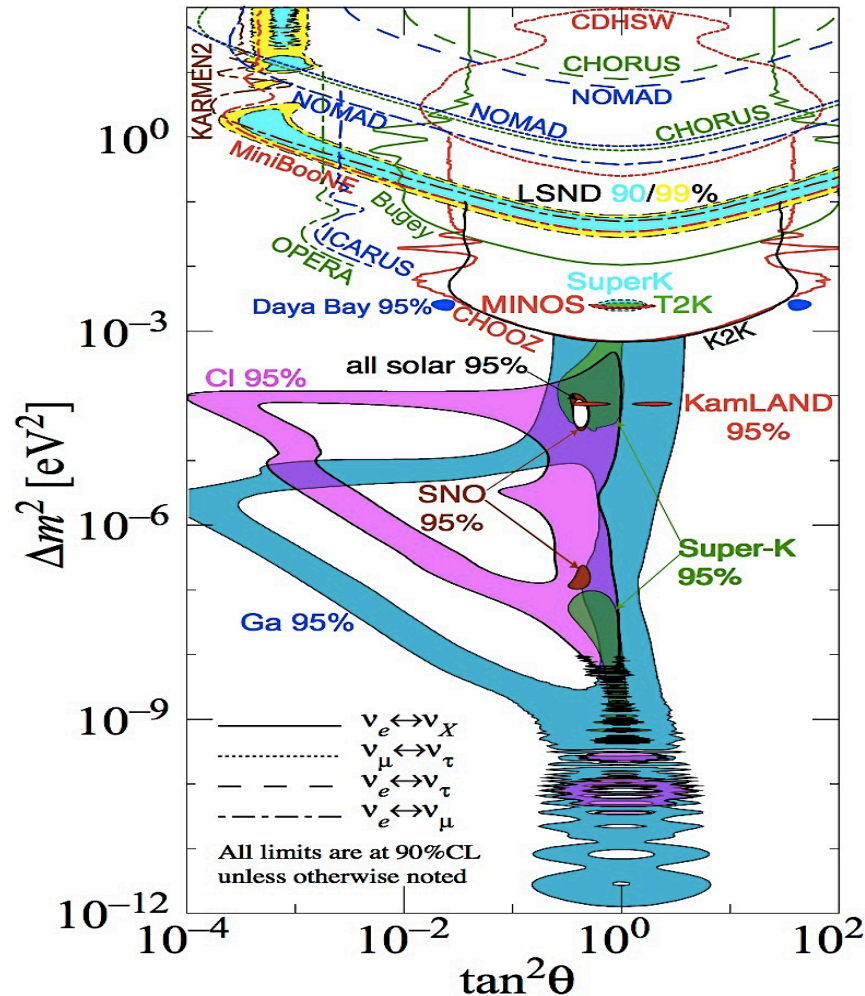
Basically obsolete

In general, better to use  
(preserve octant-symmetry)

$\log \tan^2 \theta$   
or  $\sin^2 \theta$

(Note: 2v Octant symmetry broken by 3v and/or matter effects)

# Octant (a)symmetric $2\nu$ contours from PDG Review:



But... patching  $2\nu$  approximations in different oscillation channels, in order to get a full  $3\nu$  picture, is no longer a useful approach:  
**better to go the other way around, from the full  $3\nu$  case to  $2\nu$  limits**

# The “standard” $3\nu$ oscillation framework

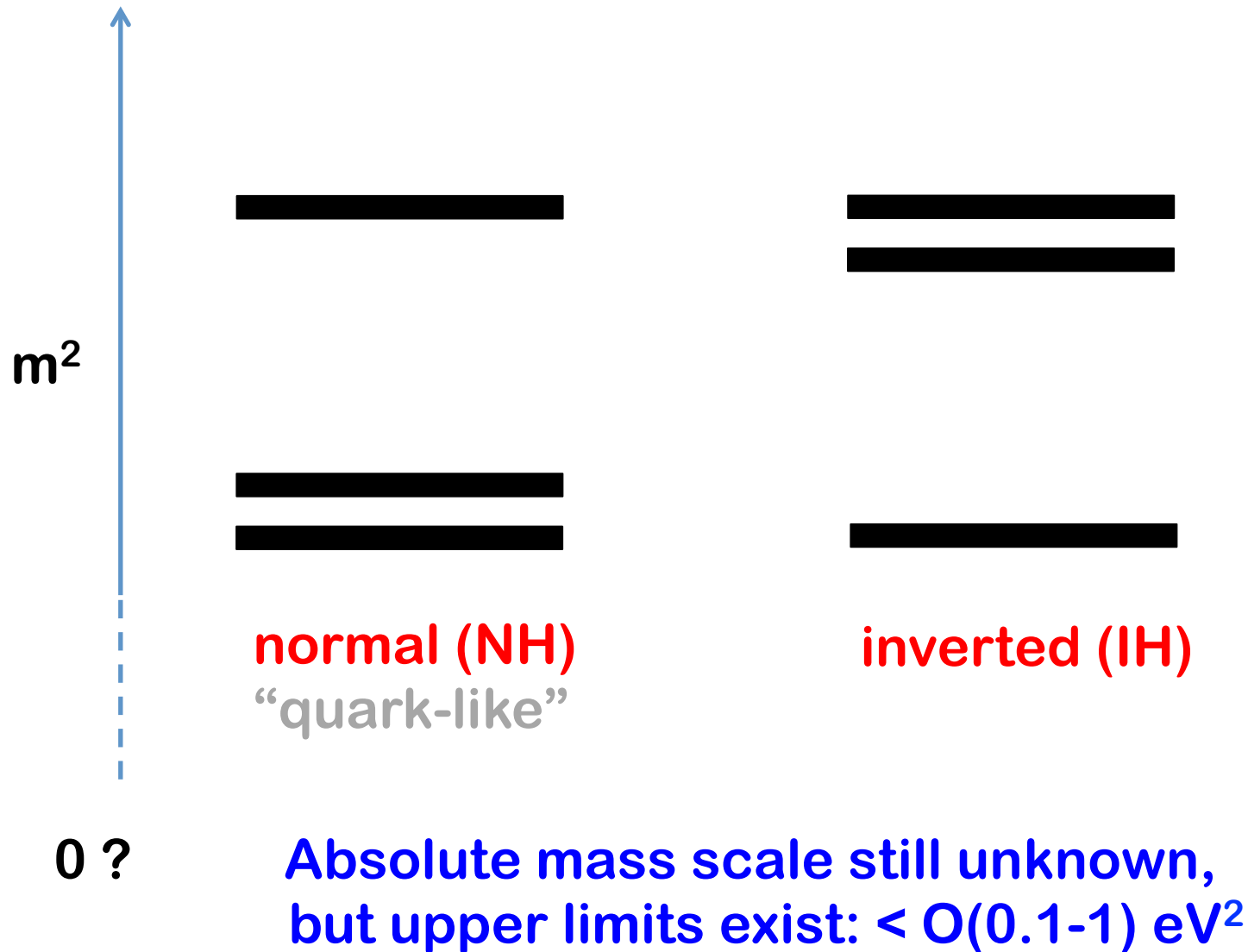
## Physics facts and mass notation:

- There are three mass states  $\nu_1, \nu_2, \nu_3$  with masses  $m_1, m_2, m_3$
- For ultrarelativistic  $\nu$  in vacuum,  $E = \sqrt{m_i^2 + p^2} \simeq p + \frac{m_i^2}{2p}$
- Neutrino oscillations probe the differences  $\Delta E \propto \Delta m_{ij}^2$
- 3 neutrinos  $\rightarrow$  two independent  $\Delta m_{ij}^2$ , say,  $\delta m^2$  and  $\Delta m^2$
- Experimentally, very different scales:  $\delta m^2 / \Delta m^2 \sim 1/30$   
Difficult to observe both! Current expts sensitive to a dominant one.

$$\delta m^2 \simeq 7.5 \times 10^{-5} \text{ eV}^2 \quad \leftarrow \text{“small” or “solar” splitting}$$

$$\Delta m^2 \simeq 2.5 \times 10^{-3} \text{ eV}^2 \quad \leftarrow \text{“large” or “atmospheric” splitting}$$

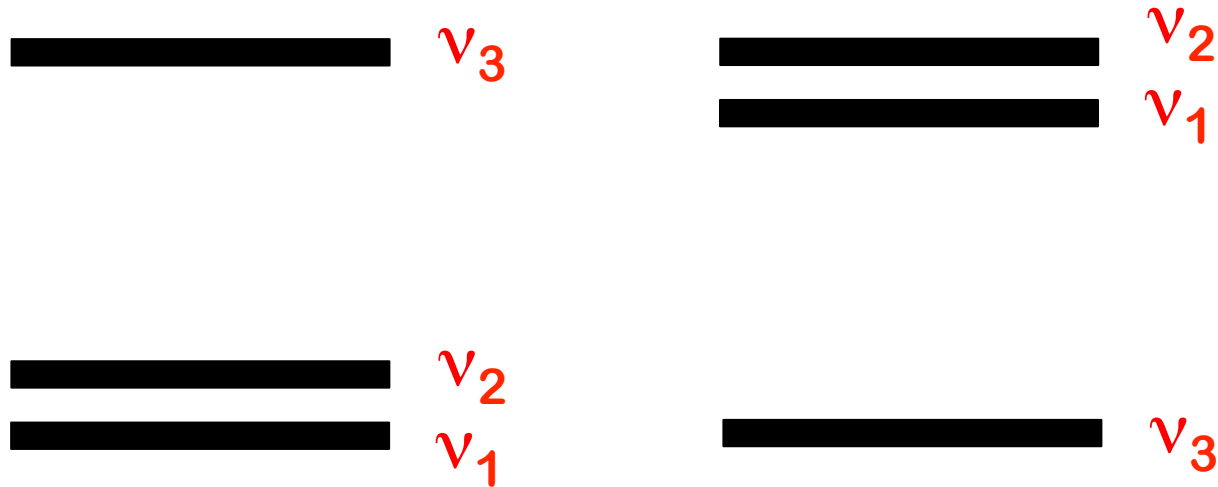
## Two possible mass orderings (hierarchies)





## PDG convention for $3\nu$ masses:

$(\nu_1, \nu_2)$  = “close” states, with  $m_2 > m_1$  in NH and IH  
 $\nu_3$  = “lone” state, with  $m_3 > m_{1,2}$  ( $< m_{1,2}$ ) in NH (IH)



**Our notation for splittings:** Define as independent ones

$$\delta m^2 = m_2^2 - m_1^2 > 0$$

$$\Delta m^2 = \frac{1}{2} (\Delta m_{31}^2 + \Delta m_{32}^2) > 0 \quad (\text{NH})$$
$$< 0 \quad (\text{IH})$$

## PDG convention for $3\nu$ mixing:

Three Euler rotations, one being complex

$$\nu_\alpha = U_{\alpha i} \nu_i \quad \begin{array}{l} \alpha = e, \mu, \tau \\ i = 1, 2, 3 \end{array}$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

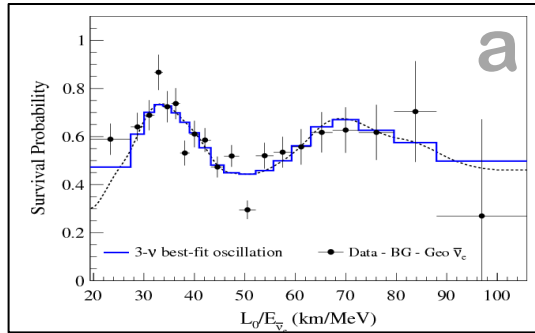
This ordering happens to be particularly useful for phenomenologically interesting limits

$$\begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{CP}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{CP}} & c_{23}c_{13} \end{bmatrix}$$

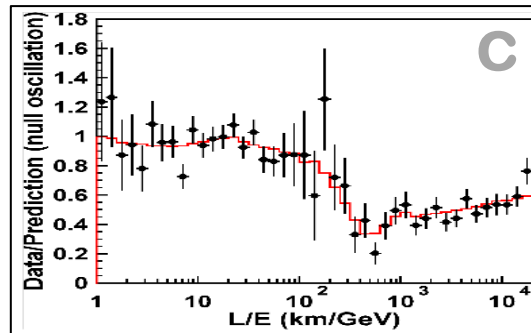
$$UU^\dagger = 1 \quad U \rightarrow U^* \text{ for } \bar{\nu} \quad c_{ij} = \cos \theta_{ij} \quad s_{ij} = \sin \theta_{ij}$$

# $3\nu$ can explain $\alpha \rightarrow \beta$ oscillations seen in vacuum and matter...

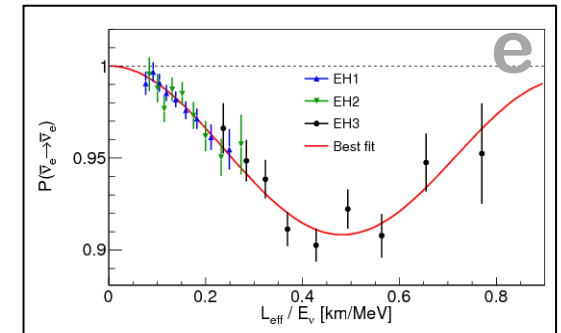
## $e \rightarrow e$



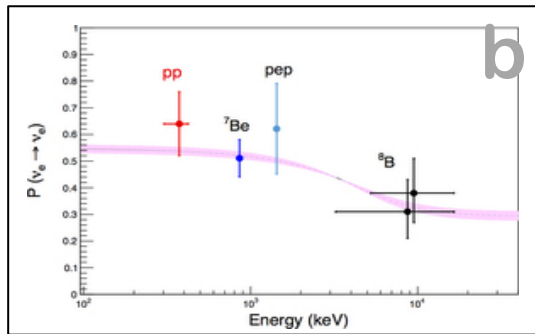
## $\mu \rightarrow \mu$



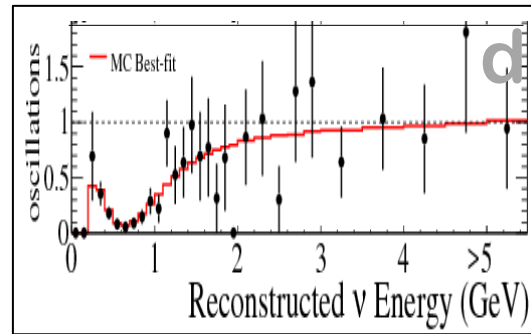
## $e \rightarrow e$



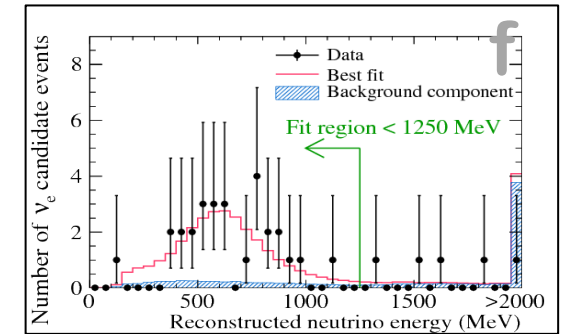
## $e \rightarrow e$



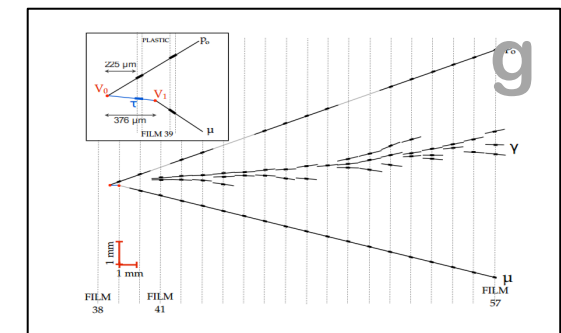
## $\mu \rightarrow \mu$



## $\mu \rightarrow e$



## $\mu \rightarrow \tau$

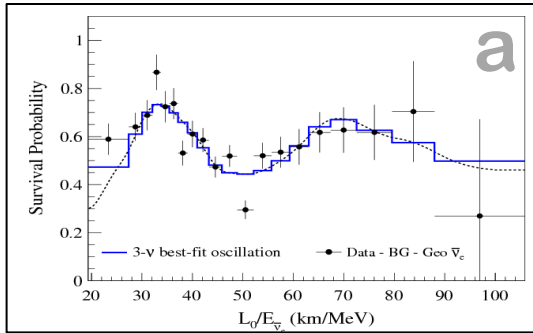


Data from various types of neutrino experiments: (a) solar, (b) long-baseline reactor, (c) atmospheric, (d) long-baseline accelerator, (e) short-baseline reactor, (f,g) long baseline accelerator (and, in part, atmospheric).

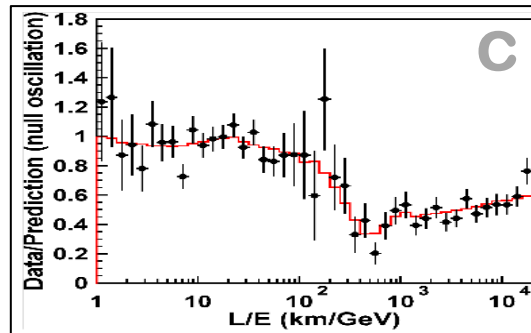
(a) KamLAND [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], DeepCore, MACRO, MINOS etc.; (d) T2K (plot), MINOS, K2K; (e) Daya Bay [plot], RENO, Double Chooz; (f) T2K [plot], MINOS, NOvA; (g) OPERA [plot], Super-K atmospheric.

...with dominant  $3\nu$  parameters:

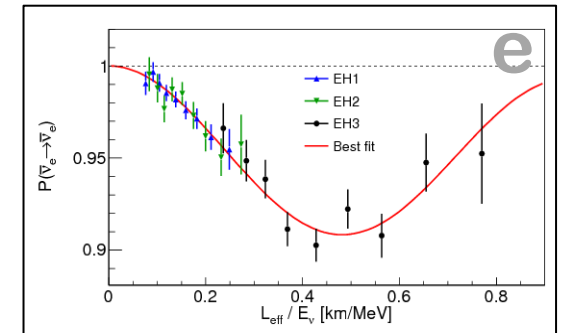
$e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ )



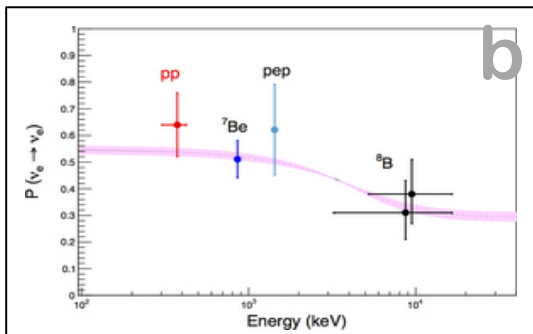
$\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ )



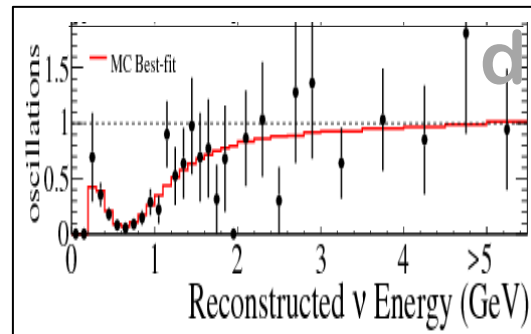
$e \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ )



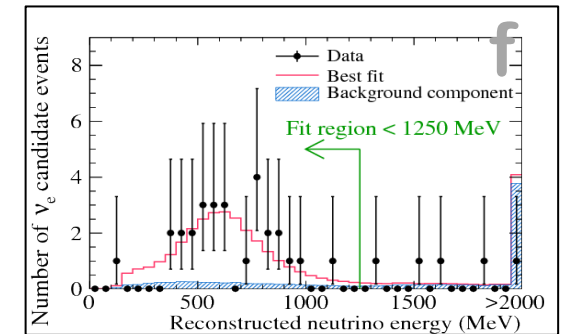
$e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ )



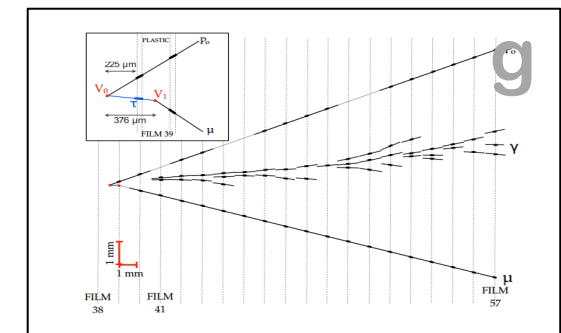
$\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ )



$\mu \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ ,  $\theta_{23}$ )



$\mu \rightarrow \tau$  ( $\Delta m^2$ ,  $\theta_{23}$ )

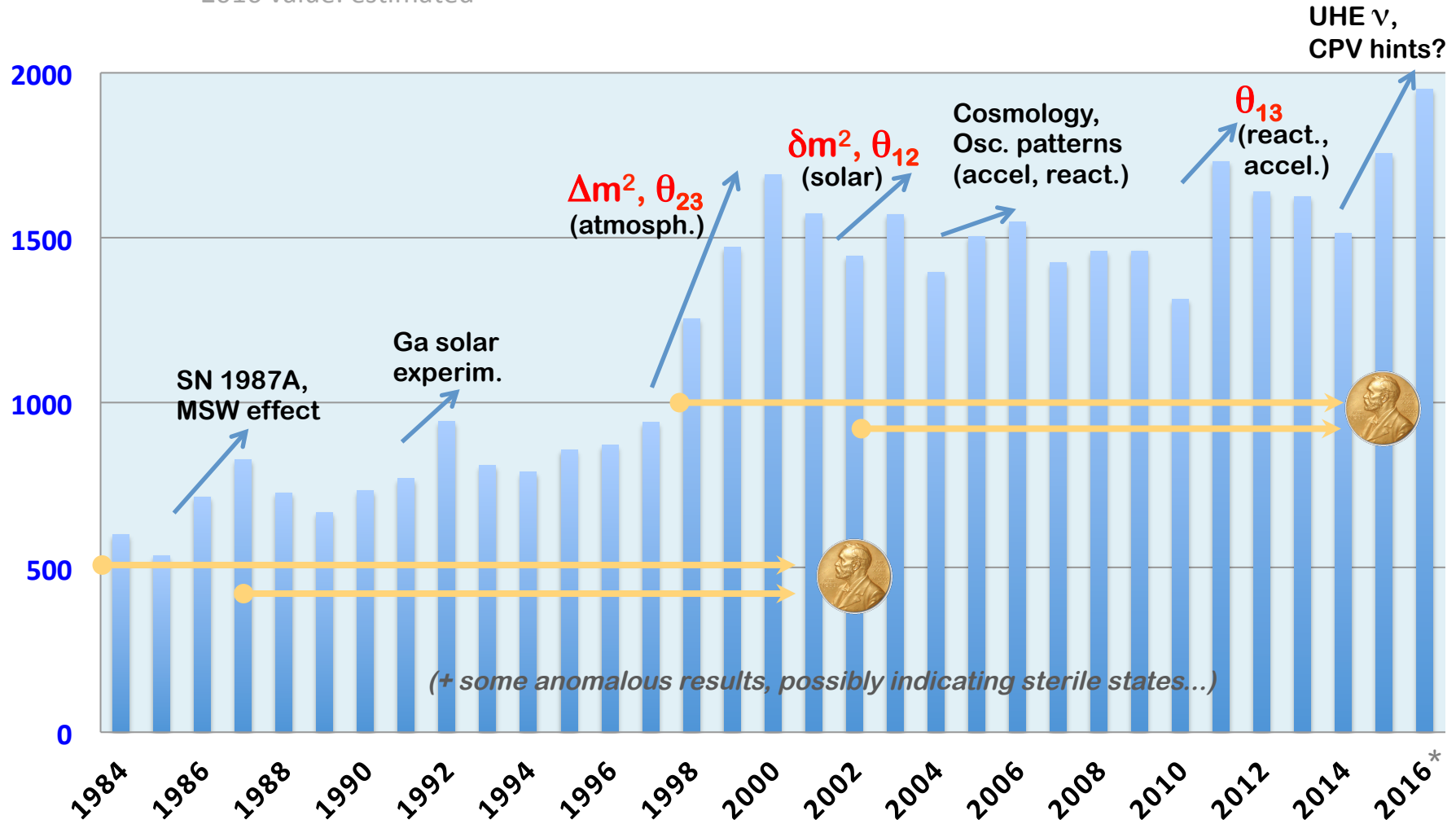


Established so far:

$\delta m^2$   $|\Delta m^2|$   $\theta_{12}$   $\theta_{23}$   $\theta_{13}$

# Preprints with #neutrino# in title (from InSPIres)

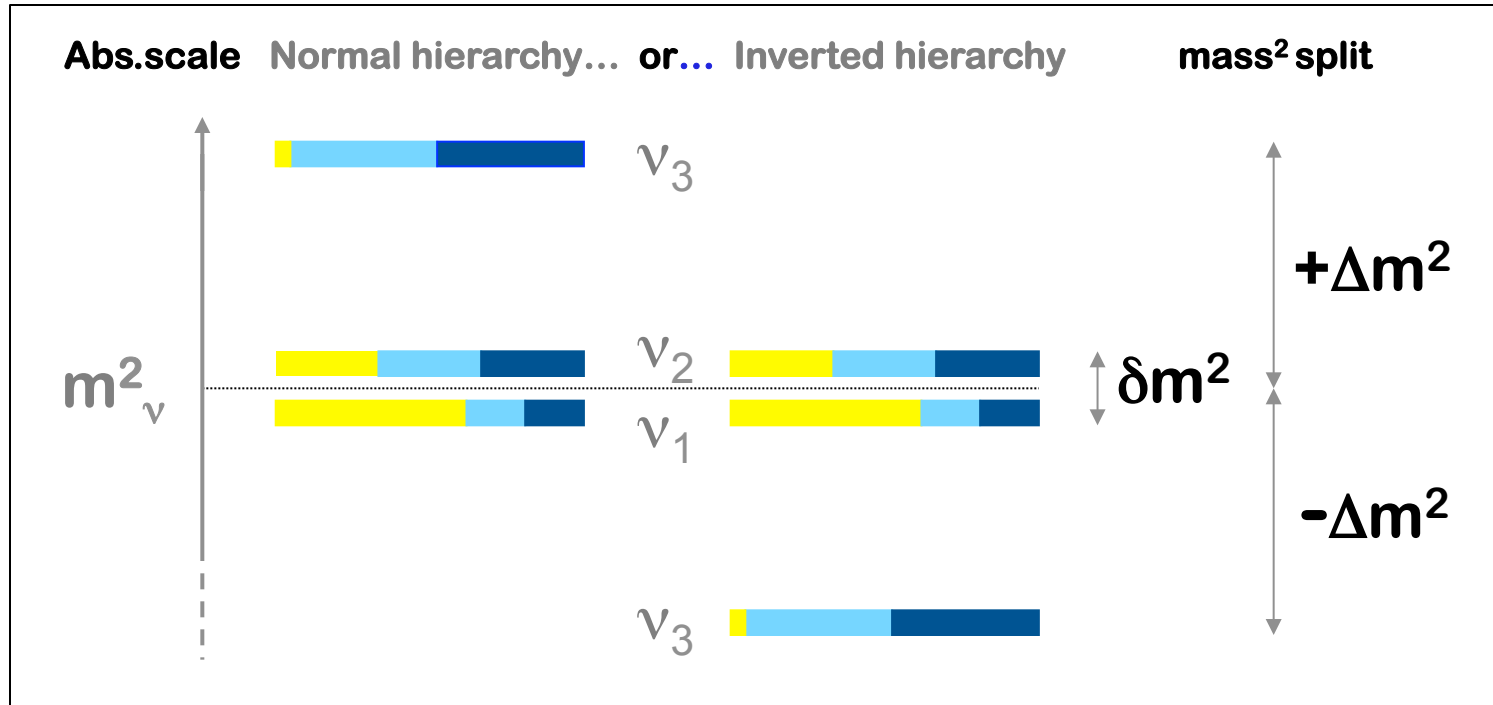
\*2016 value: estimated



... the future is yours!

# Present $3\nu$ knowledge in one slide (with 1-digit accuracy)

**e  $\mu$   $\tau$**



**We have seen:**

$$\begin{aligned} \delta m^2 &\sim 7 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02 \end{aligned}$$

**We would like to see:**

$\delta$  (CP)  
 $\text{sign}(\Delta m^2)$   
 octant( $\theta_{23}$ )  
 absolute mass scale  
 Dirac/Majorana nature

**+ Physics  
 beyond  $3\nu$ ?**

**(anomalies,  
 new states or  
 interactions)**

We shall now look into neutrino flavor evolution in more detail, both in vacuum and in matter.

The presence of two small parameters,

$$\delta m^2 / \Delta m^2 \sim 3 \times 10^{-2}$$

$$\sin^2 \theta_{13} \sim 2 \times 10^{-2}$$

will often simplify formalism & understanding.

# Neutrino flavor evolution

- It is  $m_i \ll E$  in almost all cases of phenomenological interest
- We can then set  $\beta = v/c \simeq 1$ ,  $\mathbf{x} \simeq \mathbf{t}$ ,  $\partial_{\mathbf{x}} \simeq \partial_t$
- Chirality flips LH $\rightarrow$ RH of amplitude  $O(m_i/E)$  can be ignored
- For propagation purposes, neutrinos akin to “scalar” states  $|\nu\rangle$
- State evolution governed by Hamiltonian:  $i \frac{d}{d\mathbf{x}} |\nu\rangle = \hat{H} |\nu\rangle$
- Formal solution (evolution operator):  $|\nu(\mathbf{x})\rangle = \hat{S}(\mathbf{x}, \mathbf{0}) |\nu(\mathbf{0})\rangle$
- $S_{\beta\alpha}$  components in flavor basis = amplitudes for  $\nu_{\alpha} \rightarrow \nu_{\beta}$
- Flavor evolution probabilities:  $P_{\alpha\beta} = P(\nu_{\alpha} \rightarrow \nu_{\beta}) = |S_{\beta\alpha}|^2$
- $\alpha=\beta$ : flavor disappearance channel,  $P_{\alpha\alpha} \leq 1$
- $\alpha \neq \beta$ : flavor appearance channel,  $P_{\alpha\beta} \geq 0$



# Three-neutrino flavor evolution in vacuum

The hamiltonian is exceedingly simple in the mass basis  $(\nu_1, \nu_2, \nu_3)^T$ :

$$\mathbf{H}_{\text{mass}} = \begin{pmatrix} E_1 & & \\ & E_2 & \\ & & E_3 \end{pmatrix} \simeq \mathbf{p} \begin{pmatrix} 1 & & \\ & 1 & \\ & & 1 \end{pmatrix} + \frac{1}{2E} \begin{pmatrix} m_1^2 & & \\ & m_2^2 & \\ & & m_3^2 \end{pmatrix}$$

*(and even simpler than that, since terms proportional to unity decouple)*

In flavor basis  $(\nu_e, \nu_\mu, \nu_\tau)^T$  it becomes nondiagonal ( $\rightarrow$  flavor not conserved):

$$\mathbf{H}_{\text{flavor}} = \mathbf{U} \mathbf{H}_{\text{mass}} \mathbf{U}^\dagger$$

Let us work out (tutorials) and discuss (slides)  
some implications of this simple hamiltonian  $\rightarrow$

## 3ν oscillations in vacuum: general case

Prove that

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i < j} \operatorname{Re} J_{\alpha\beta}^{ij} \sin^2 \left( \frac{\Delta m_{ij}^2 x}{4E} \right) - 2 \sum_{i < j} \operatorname{Im} J_{\alpha\beta}^{ij} \sin \left( \frac{\Delta m_{ij}^2 x}{2E} \right)$$

where

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

$$J_{\alpha\beta}^{ij} = U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j}$$

$$\frac{\Delta m_{ij}^2}{4E} = 1.267 \left( \frac{\Delta m_{ij}^2}{\text{eV}^2} \right) \left( \frac{x}{\text{m}} \right) \left( \frac{\text{MeV}}{E} \right)$$

← Jarlskog invariant

(See tutorials)

In general,  $P_{\alpha\beta}$  is not an observable...

$$\mathbf{R}_\beta \sim \int \Phi_\alpha \otimes \mathbf{P}_{\alpha\beta} \otimes \sigma_\beta \otimes \epsilon_\beta$$

Observable  
event rate

Source flux  
(production)

Propagation  
(flavor change)

Interaction  
and detection

→ need to take into account detailed phenomenology

Many open research problems for each of these ingredients, in all subfields of neutrino physics.

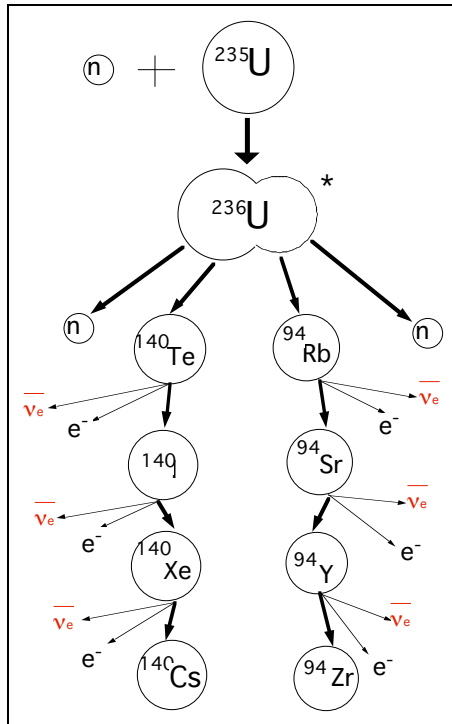
**Warm-up case study  
for oscillation phenomenology:**

**Short-baseline (SBL) reactors**

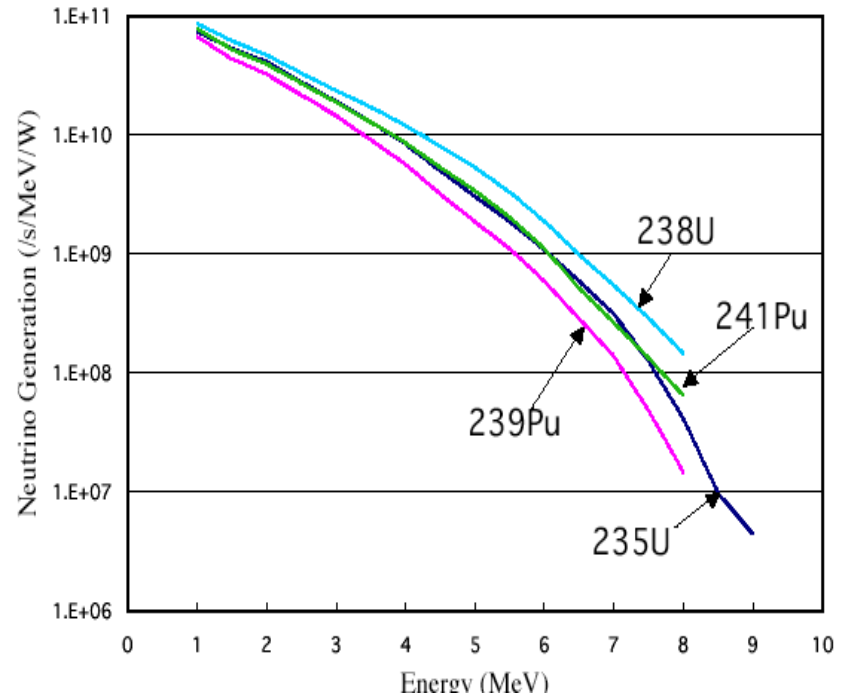
# Production

Reactors: Intense sources of anti- $\nu_e$  ( $\sim 6 \times 10^{20}$ /s/reactor)

Typically, 6 neutron decays to reach stable matter from fission:

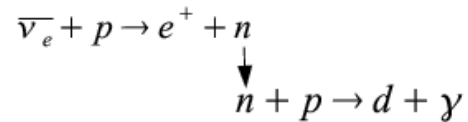


$\sim 200$  MeV per fission / 6 decays:  
Typical available neutrino energy  
 $E \sim$  few MeV



# Detection

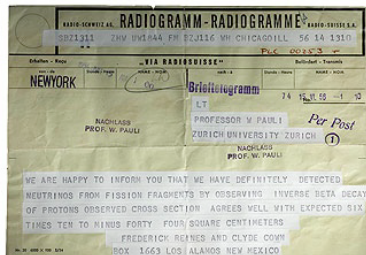
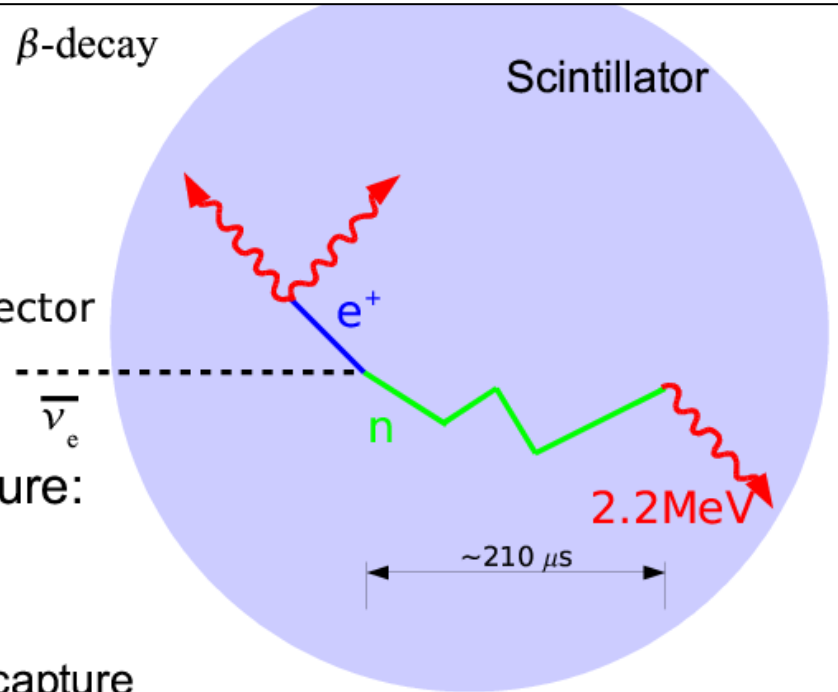
Reaction Process: inverse  $\beta$ -decay



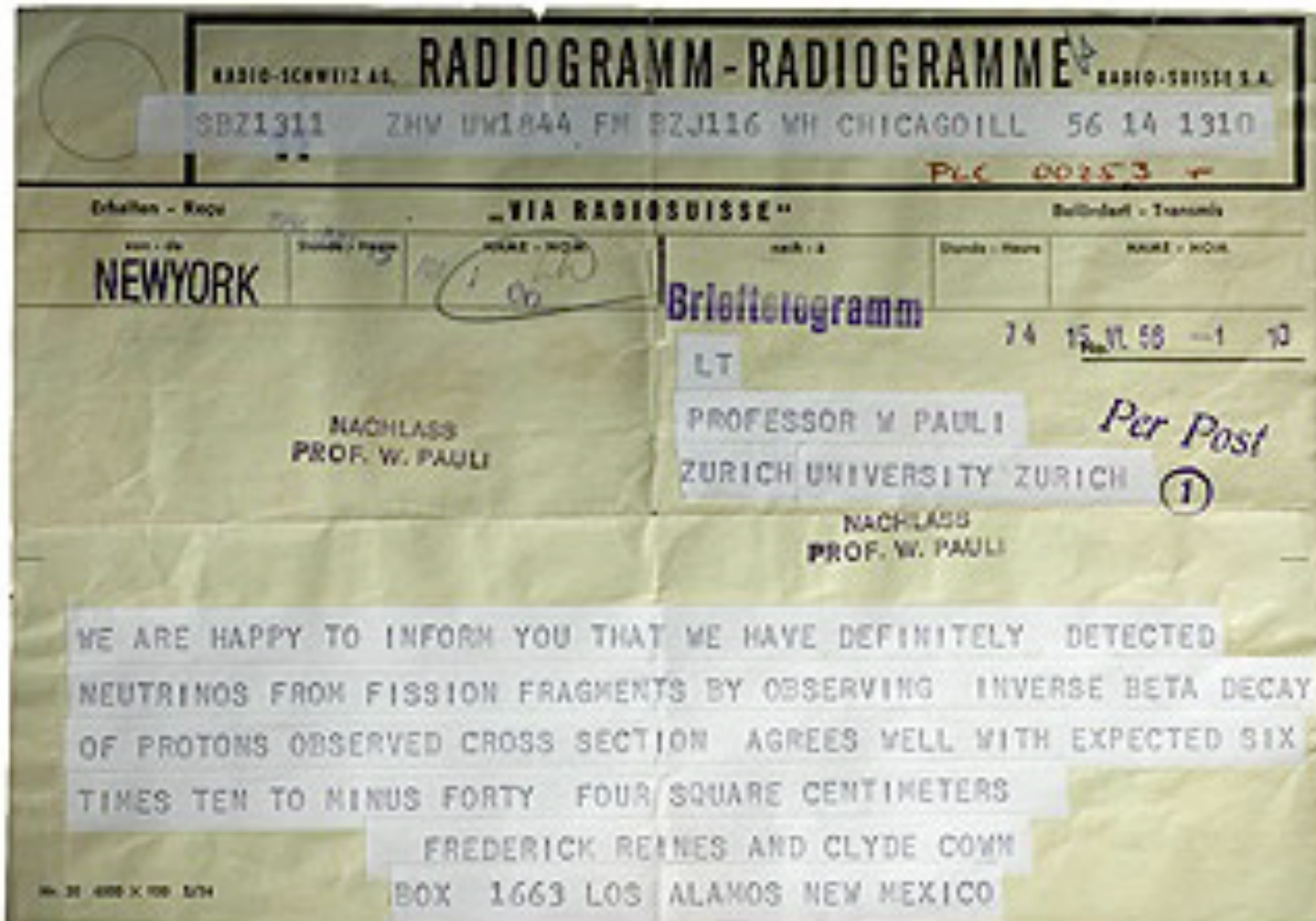
Scintillator is target and detector

- Distinct two-step signature:
  - prompt event: positron  
 $E_\nu \approx E_{e^+} + 0.8 \text{ MeV}$
  - delayed event: neutron capture  
after  $\sim 210 \mu\text{s}$ 
    - 2.2 MeV gamma

Delayed coincidence: good background rejection



← This reaction allowed experimental  $\bar{\nu}$  discovery in 1956 (Reines & Cowan)



*Reply by telegram:*

**"Thanks for message. Everything comes to him who knows how to wait. Pauli."**

# Propagation

## Exercise: $3\nu \rightarrow 2\nu$ reduction for SBL reactor expts.

Short-baseline reactor experiments look for  $\bar{\nu}_e$  oscillations at  $x = L \sim \mathcal{O}(1 \text{ km})$  and  $E \sim \text{few MeV}$ . At these energies, CC reactions in the final state can produce  $e^+$  but not  $\mu^+$  or  $\tau^+$ ; therefore, only  $P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$  is observable (disappearance) but not  $P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$  or  $P(\bar{\nu}_e \rightarrow \bar{\nu}_\tau)$  (appearance). Moreover, it is  $\delta m^2 L / 4E \ll 1$ , while  $\Delta m^2 L / 4E \sim \mathcal{O}(1)$ .

Prove that, in the limit  $\delta m^2 \approx 0$ , effective  $2\nu$  oscillations occur:

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \approx 1 - \underbrace{\sin^2 2\theta_{13}}_{\text{oscillation amplitude}} \underbrace{\sin^2\left(\frac{\Delta m^2 L}{4E}\right)}_{\text{oscillating factor}}$$

Try to get an intuitive understanding of the dependence on  $\theta_{13}$  only.



Solution - From the previous exercise (with  $U \rightarrow U^*$ ), the only nonzero oscillating terms for  $\alpha\beta = ee$  and  $\Delta m^2 = m_2^2 - m_1^2 \approx 0$  are multiplied by:  
 $J_{ee}^{13} = U_{e1}^* U_{e3} U_{e3}^* U_{e1} = |U_{e1}|^2 |U_{e3}|^2$  and  $J_{ee}^{23} = |U_{e2}|^2 |U_{e3}|^2$ . Then:  
 $\text{Im}(J_{ee}^{13}) = 0 = \text{Im}(J_{ee}^{23})$  and

$$\begin{aligned} P(\bar{\nu}_e \rightarrow \bar{\nu}_e) &= 1 - 4(|U_{e1}|^2 |U_{e3}|^2 + |U_{e2}|^2 |U_{e3}|^2) \sin^2\left(\frac{\Delta m^2 L}{4E}\right) \\ &= 1 - 4|U_{e3}|^2(1 - |U_{e3}|^2) \sin^2\left(\frac{\Delta m^2 L}{4E}\right) \quad \leftarrow |U_{e3}|^2 = s_{13}^2 \\ &= 1 - \sin^2 2\theta_{13} \sin^2\left(\frac{\Delta m^2 L}{4E}\right) \end{aligned}$$

Intuitively: two of the three mixing rotations have  $\sim$  no effect

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 2,3 \end{pmatrix} \begin{pmatrix} 1,3 \end{pmatrix} \begin{pmatrix} 1,2 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \quad \rightarrow \text{only } (1,3) \text{ physical}$$

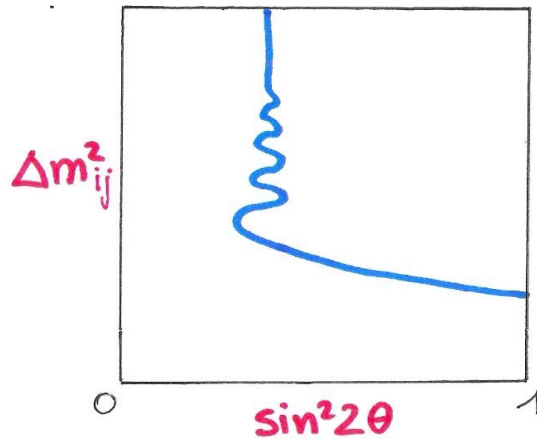
↑  
mixes unobservable flavors ( $\nu_\mu, \nu_\tau$ )
↑  
mixes  $\sim$  degenerate states ( $\nu_1, \nu_2$ )

Note that, in this case,  $\delta$  is unobservable, as well as  $\text{sign}(\pm \Delta m^2)$ , and  $P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = P(\nu_e \rightarrow \nu_e)$ .

# Generic experimental constraints in $2\nu$ approxim.

- Experiments measure some "averaged"  $P_{\alpha\beta} \simeq \sin^2 2\theta \left\langle \sin^2 \left( \frac{\Delta m_{ij}^2 x}{4E} \right) \right\rangle$

- Curve of iso- $P_{\alpha\beta}$ :

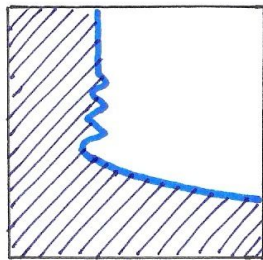


$\leftarrow \frac{\Delta m_{ij}^2 x}{4E} \gg 1, \langle \dots \rangle \sim \frac{1}{2}$ , fast oscillations

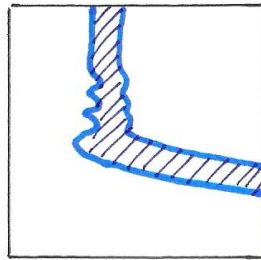
$\leftarrow \frac{\Delta m_{ij}^2 x}{4E} \sim \mathcal{O}(1)$

$\leftarrow \frac{\Delta m_{ij}^2 x}{4E} \ll 1$ , vanishing oscillations

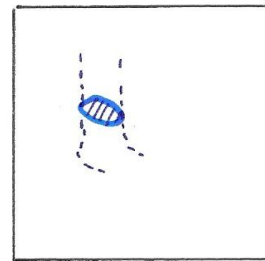
- Possible expt. constraints:



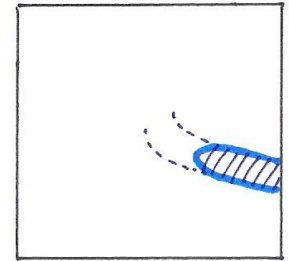
No signal



Signal



Precise signal at small mixing



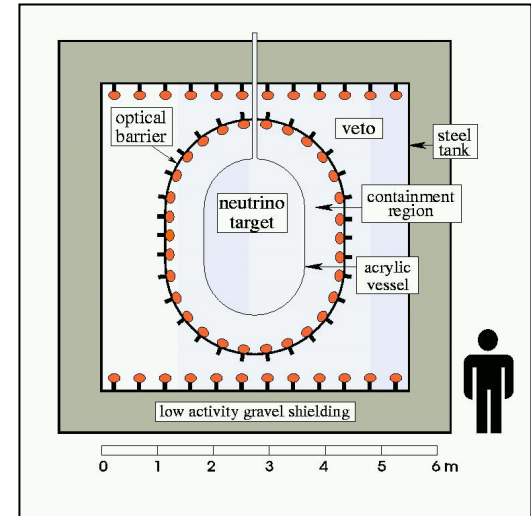
Precise signal at large mixing

(need  $\geq 2$  expts or spectral data in 1 expt)

# The short-baseline reactor experiment CHOOZ (1998+)



$L \sim 1 \text{ km} \rightarrow$



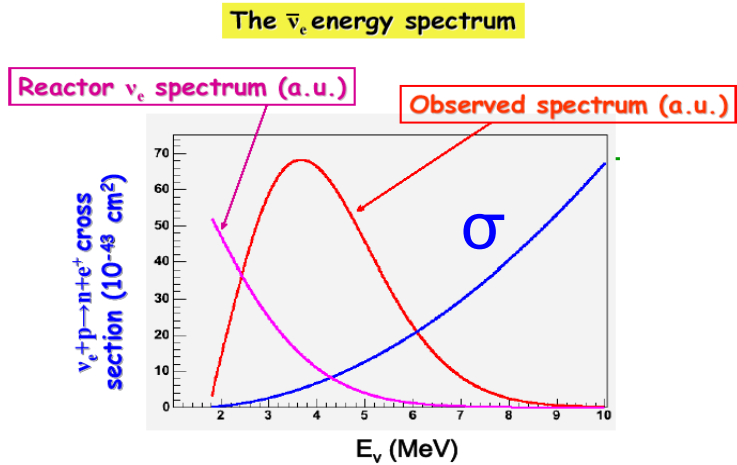
Probably (one of) the most cited **negative** results ever!

First data: Phys. Lett. B 466, 415 (1999) >1700 cites

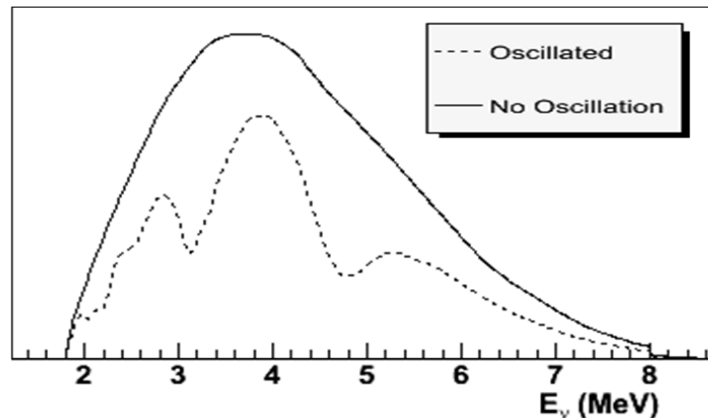
Final data: Eur. Phys. J. C 27, 331 (2003) >1200 cites

# CHOOZ reactor results (1998-2003)

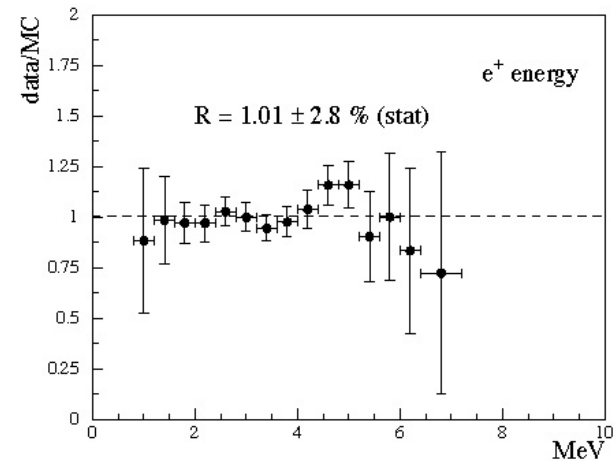
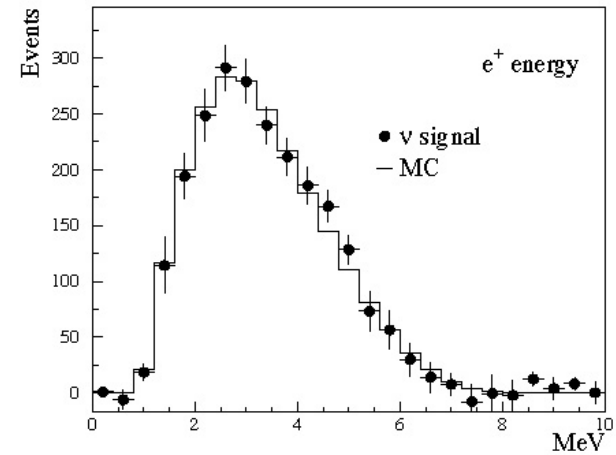
## Expected spectrum (no oscill.):



## With oscillations (qualitative):



## CHOOZ: no oscillations within few % error



# Interpretation

One mass scale dominance:

$$P_{ee} = 1 - \sin^2(2\theta_{13}) \sin^2(\Delta m^2 L / 4E_\nu)$$

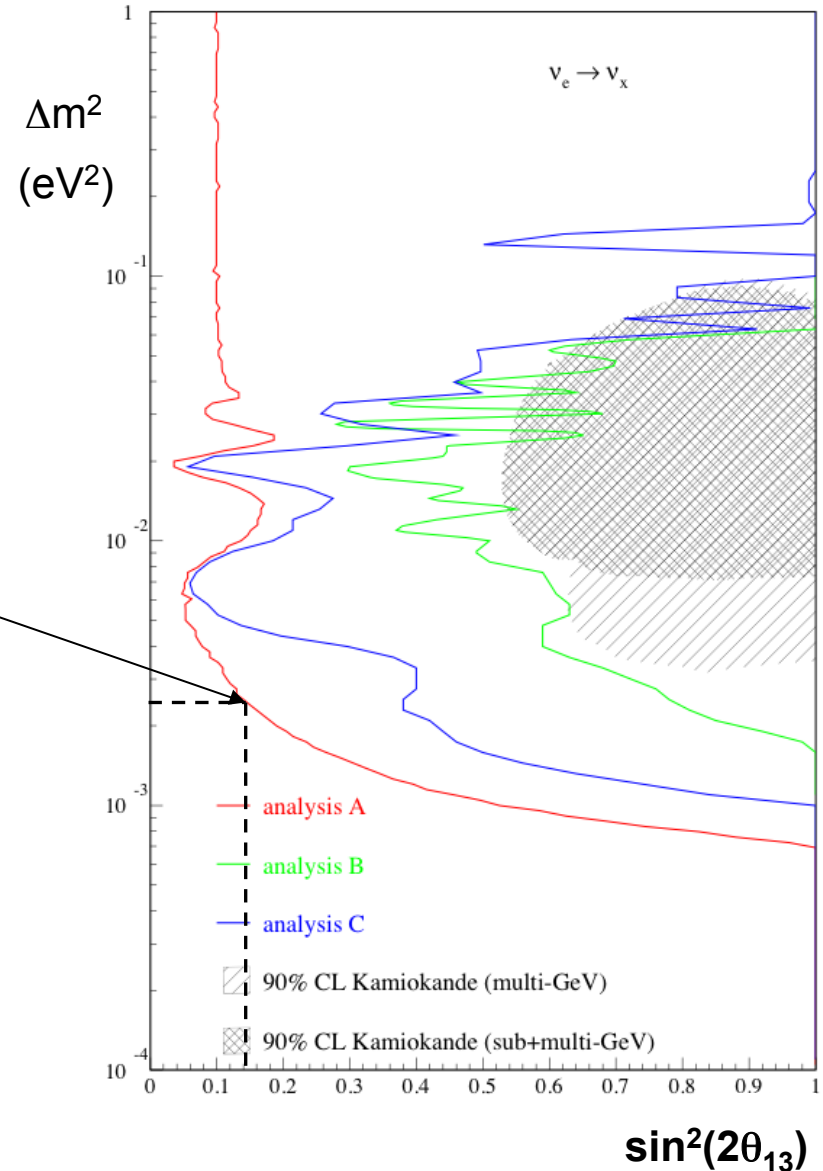
For any value of  $\Delta m^2$  in the range allowed by atmospheric data (next Lect.), get stringent **upper bound on  $\theta_{13}$**

$$\sin^2 \theta_{13} < \text{few \%} \\ (\text{depending on } \Delta m^2)$$

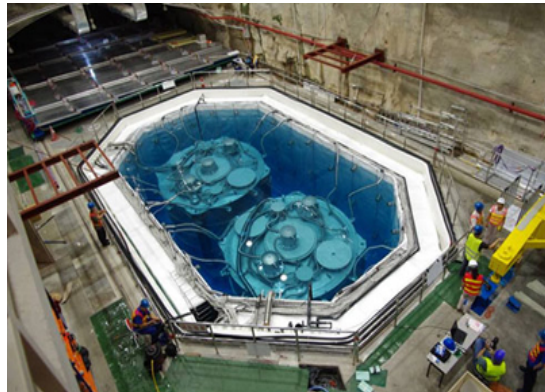
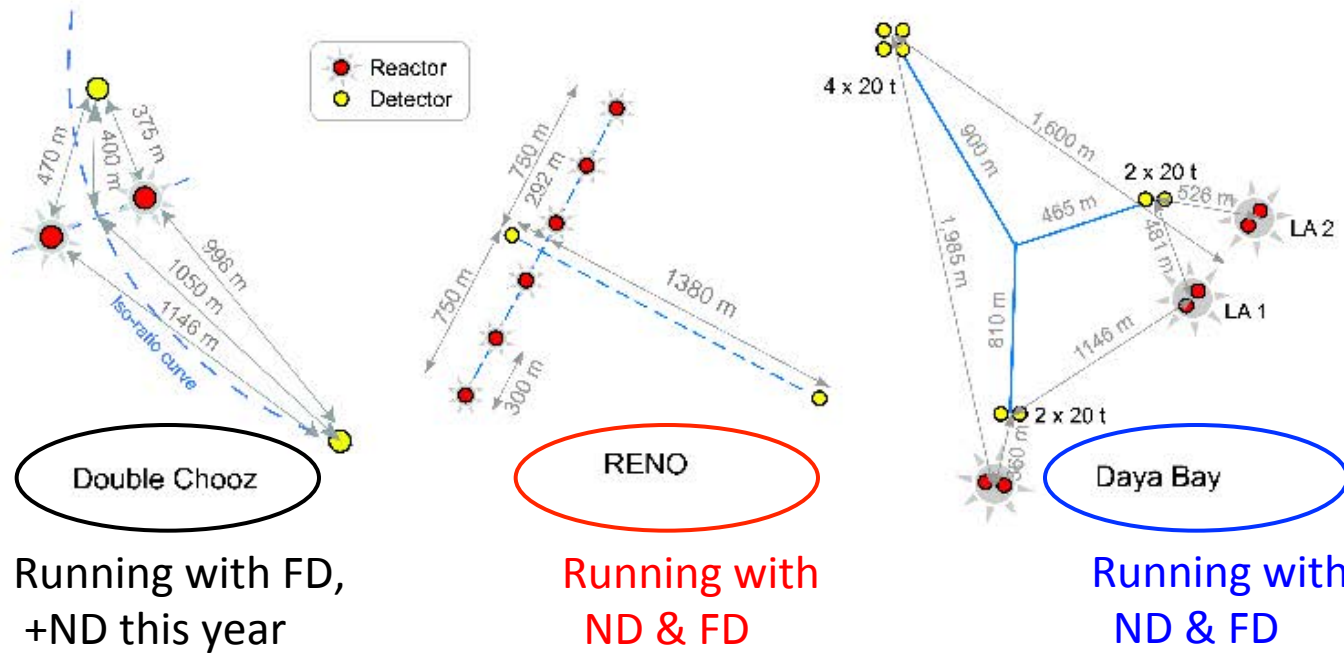
... Nobody could know at that time, but  $\theta_{13}$  was just behind the corner (less than a factor of two in sensitivity!)

In any case, it was clear that, to reach higher  $\theta_{13}$  sensitivity, need to use a second (close) detector to reduce systematics by far/near comparison →

## CHOOZ exclusion plot



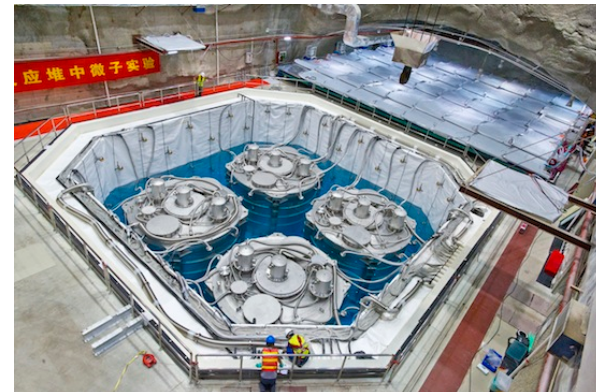
# Current SBL reactor expts with near & far detectors (ND & FD)



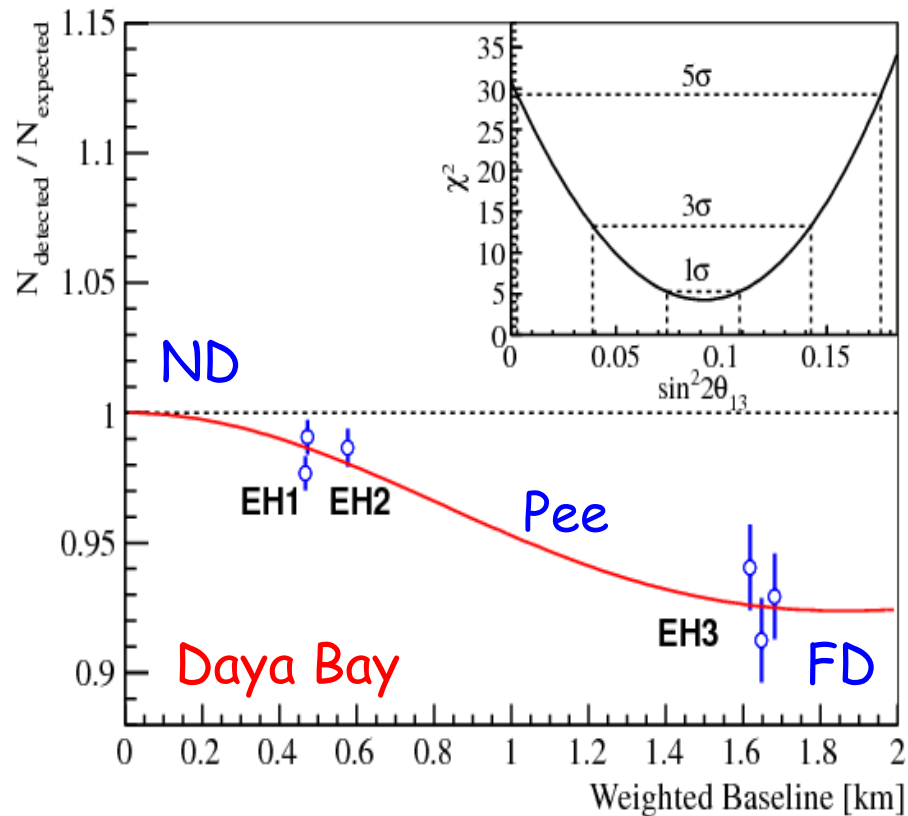
E.g, for  
Daya Bay:

← ND

FD →



# 2012: discovery of $\theta_{13} > 0$ ! ( $\sin^2\theta_{13} \sim 0.022$ at $\sim$ fixed $\Delta m^2$ )

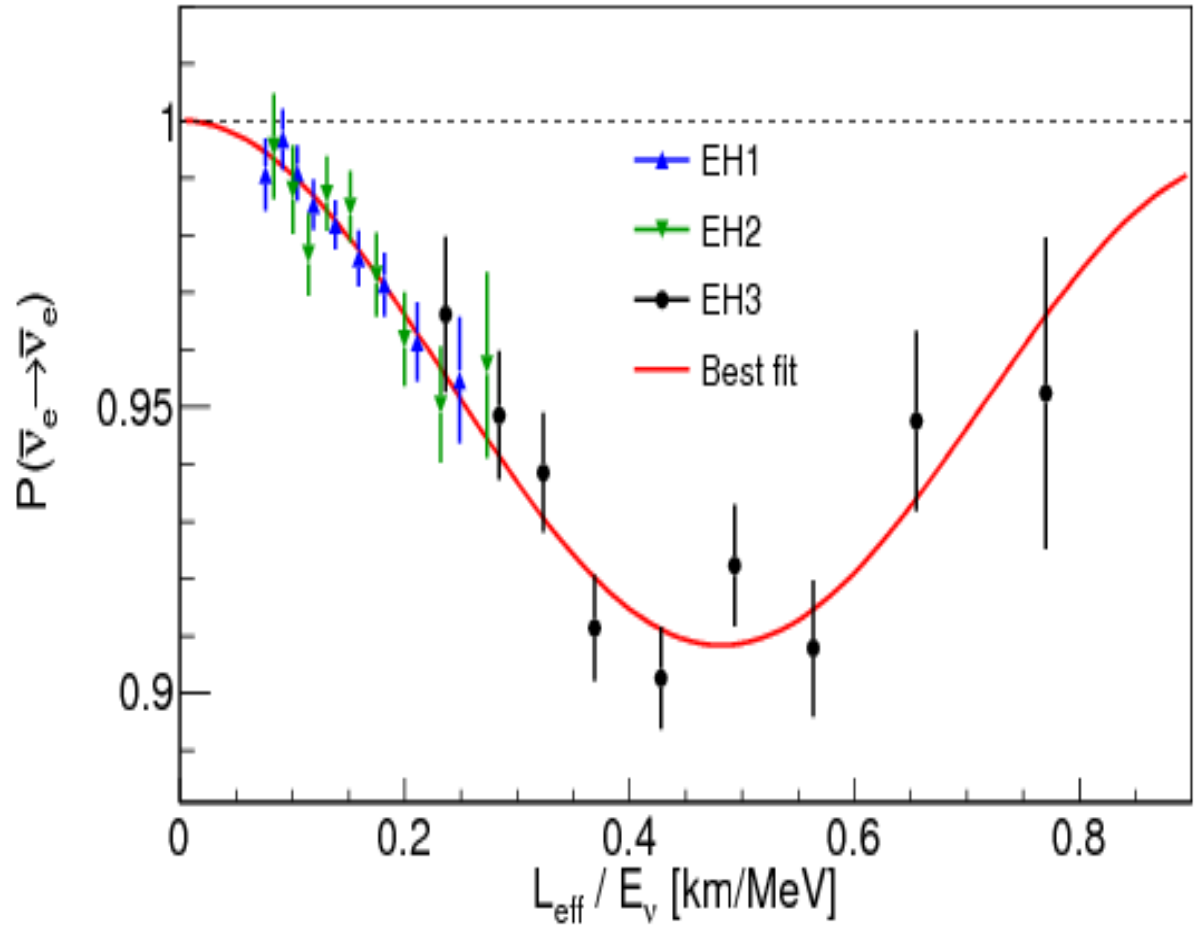
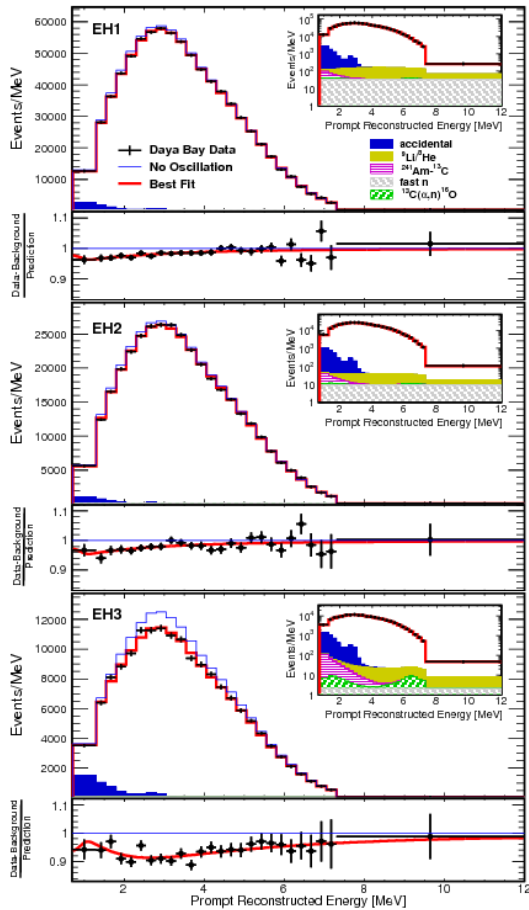


Daya Bay (& RENO): disappearance at FD w.r.t.  $\sim$ unoscillated at ND

Double Chooz results (FD only) were also consistent with Daya Bay & RENO.

Interestingly, approximate value of  $\theta_{13}$  was previously hinted from other data: weaker signals were also coming from other experiments before 2012 (see Lec. II).

2013: more data  $\rightarrow$  spectral analys.  $\rightarrow$   $\frac{1}{2}$  osc. cycle in L/E!



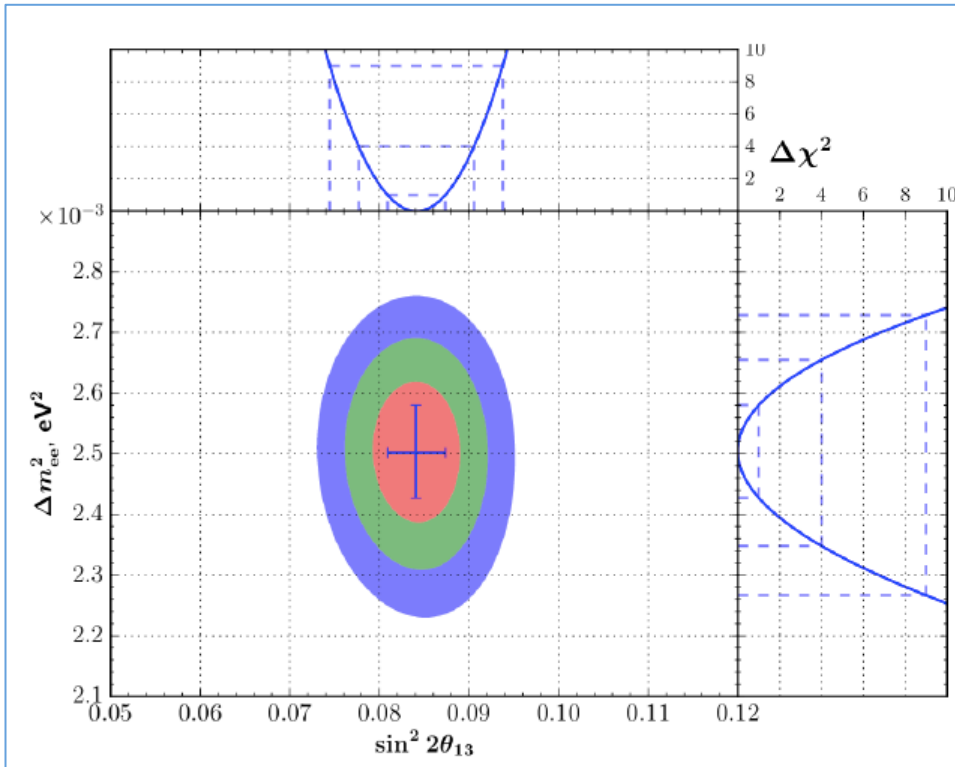
(Above: Daya Bay data.  $\frac{1}{2}$  cycle also observed in RENO, with less statistics)



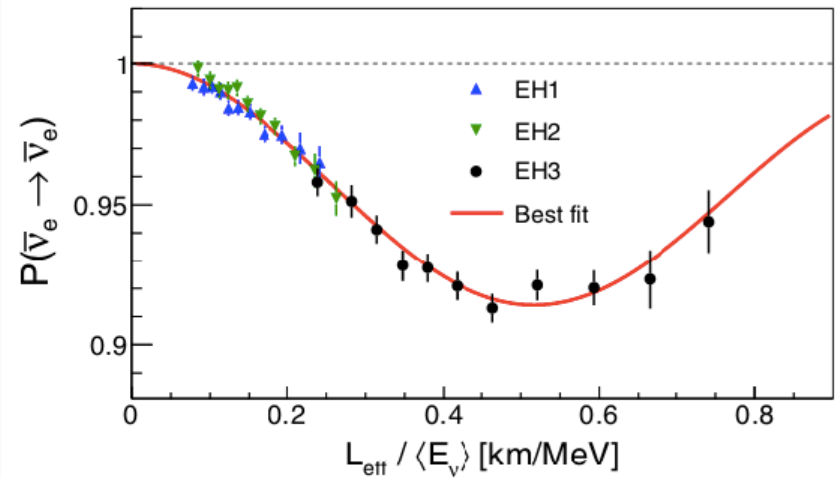
# Most recent Daya Bay results (Neutrino 2016, July, London)

(see also RENO and Double Chooz results at the same Conference)

Current accuracy requires to go beyond the  $2\nu$  approximation (see exercises in tutorial):  $\downarrow$



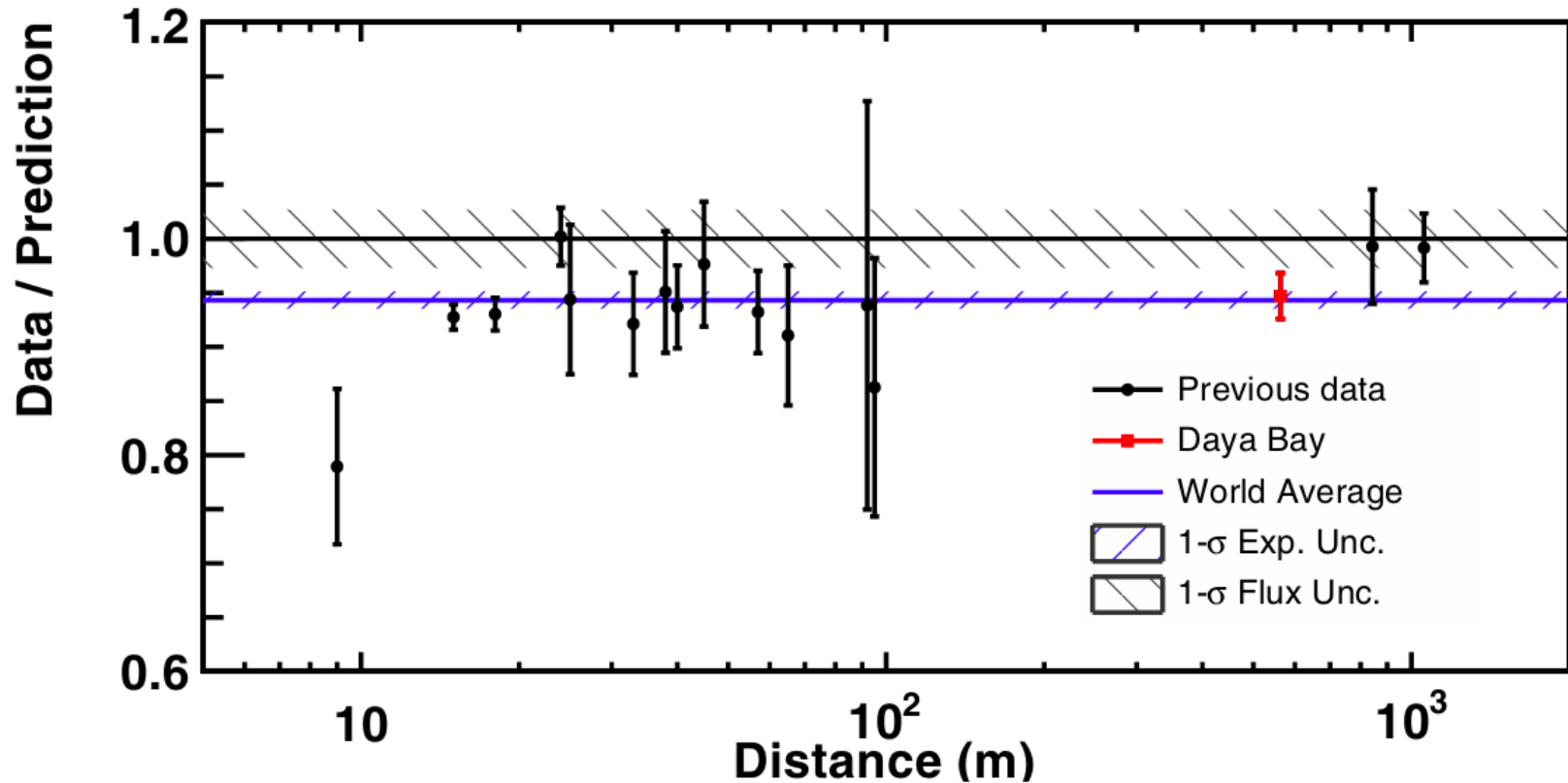
$$P = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{1.267 \Delta m_{21}^2 L}{E} - \sin^2 2\theta_{13} \sin^2 \frac{1.267 \Delta m_{ee}^2 L}{E}.$$



$\uparrow$  Precise measurement of both  $\Delta m^2$  (“mass”) and  $\theta_{13}$  (“mixing”) oscill. parameters in  $\nu_e \rightarrow \nu_e$  channel

$\uparrow$  Position of oscillation dip in L/E determines  $\Delta m^2$ , while depth fixes  $\theta_{13}$

## Some open problems in this field... (1)



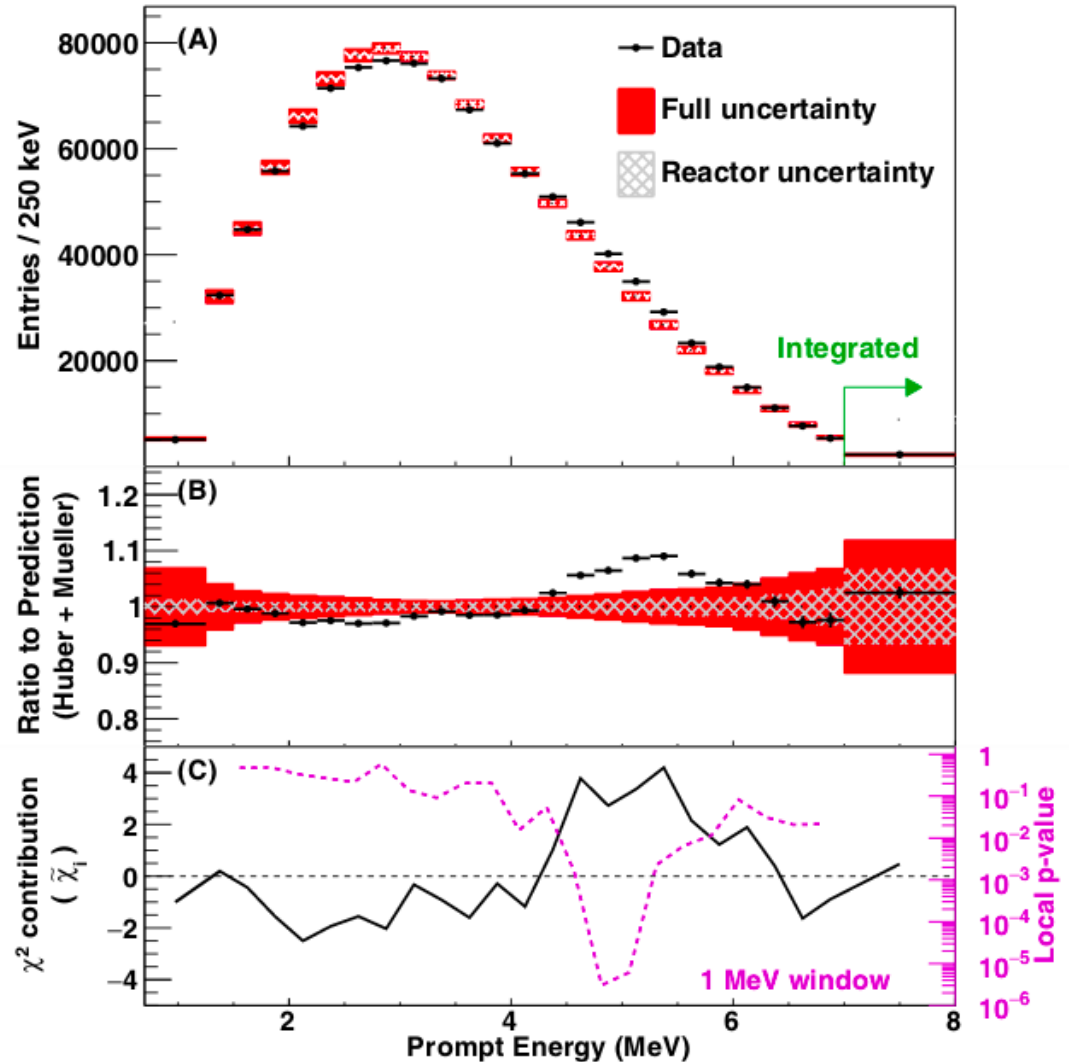
**Absolute flux normalization somewhat below expectations:**  
**overestimated flux, or fast disappearance into a new  $\nu$  state?**  
(“reactor  $\nu$  anomaly” and oscillations into “sterile neutrinos”)

## Some open problems in this field... (2)

Flux spectrum shape somewhat different from expectations: ~5 MeV “bump”

Incomplete nuclear physics description of decay chains?

(probably unrelated to oscillations, but affects systematics)

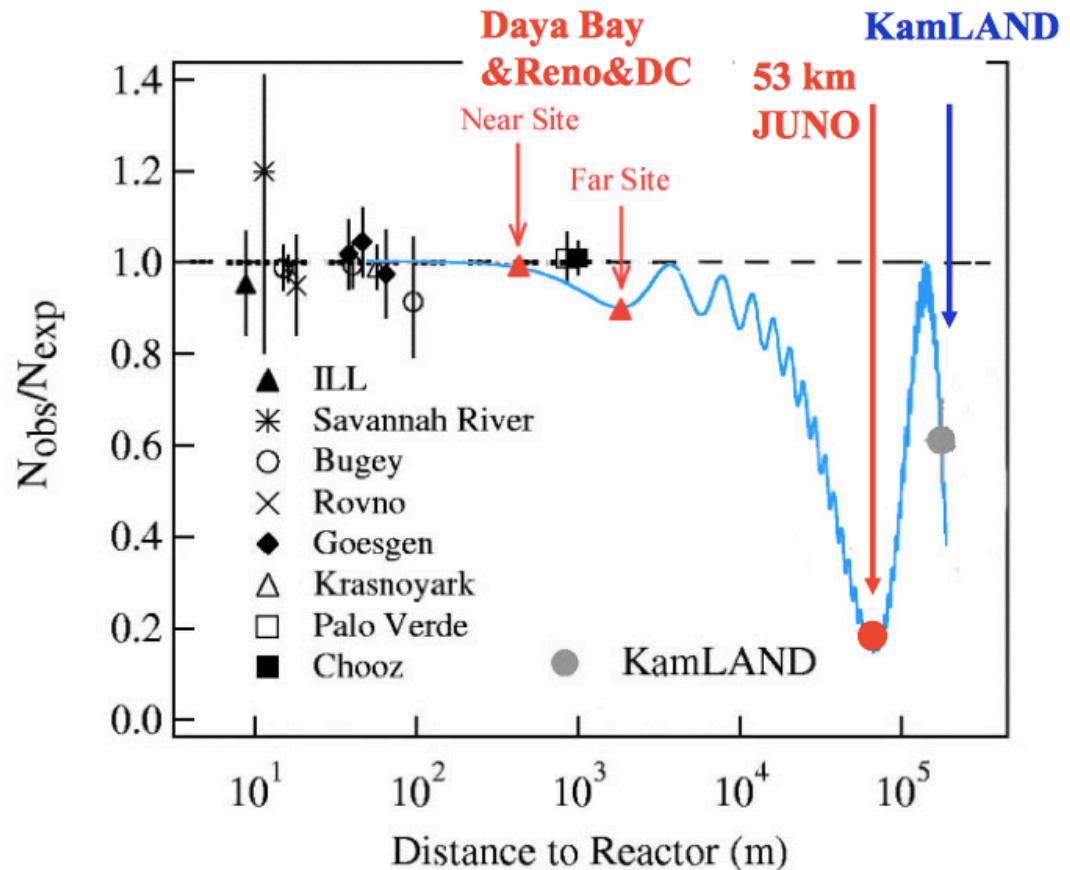


## Some open problems in this field... (3)

Can one reach the accuracy needed to observe also the oscillations driven by  $\delta m^2$ , as well as the interference between  $\delta m^2$  and  $\pm \Delta m^2 \rightarrow$  mass hierarchy effects?

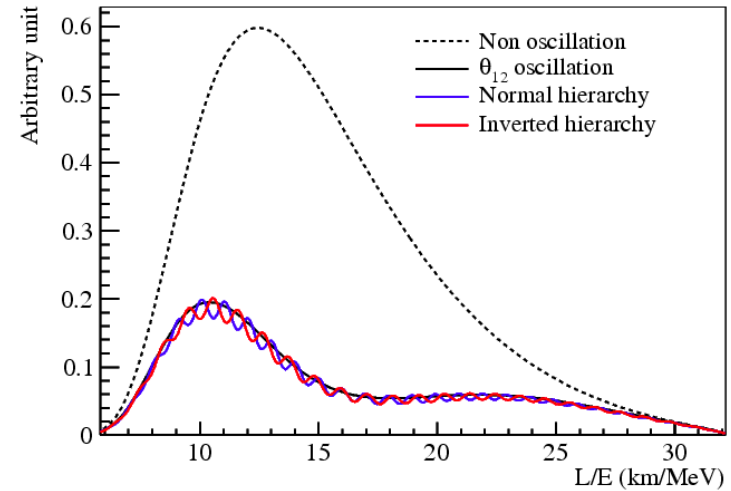
Not only a problem of accuracy but also of L/E  $\rightarrow$  **L~50 km** (“medium baselines”) needed to observe both oscillations at the same time within the reactor spectrum band width in energy

$\rightarrow$  JUNO, RENO-50



From JUNO proposal,  
arXiv:1507.05613v2, p. 36:

Hierarchy effects  $\rightarrow$  advancement  
or retardation of “phase”  $\pm\phi$  for the  
fast-oscillating component



JUNO is designed to resolve the neutrino MH using precision spectral measurements of reactor antineutrino oscillations. Before giving the quantitative calculation of the MH sensitivity, we shall briefly review the principle of this method. The electron antineutrino survival probability in vacuum can be written as [69, 79, 94]:

$$\begin{aligned}
 P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} &= 1 - \sin^2 2\theta_{13}(\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} \quad (2.1) \\
 &= 1 - \frac{1}{2} \sin^2 2\theta_{13} \left[ 1 - \sqrt{1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21}} \cos(2|\Delta_{ee}| \pm \phi) \right] - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21},
 \end{aligned}$$

where  $\Delta_{ij} \equiv \Delta m_{ij}^2 L / 4E$ , in which  $L$  is the baseline,  $E$  is the antineutrino energy,

$$\sin \phi = \frac{c_{12}^2 \sin(2s_{12}^2 \Delta_{21}) - s_{12}^2 \sin(2c_{12}^2 \Delta_{21})}{\sqrt{1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21}}}, \quad \cos \phi = \frac{c_{12}^2 \cos(2s_{12}^2 \Delta_{21}) + s_{12}^2 \cos(2c_{12}^2 \Delta_{21})}{\sqrt{1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21}}},$$

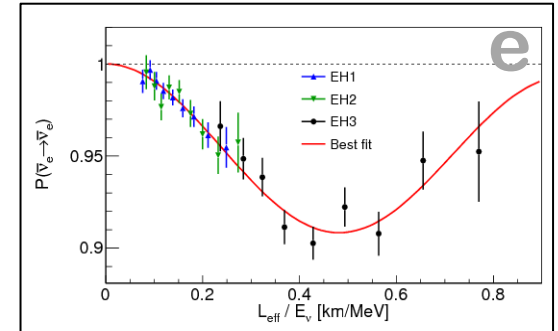
and [95, 96]

$$\Delta m_{ee}^2 = \cos^2 \theta_{12} \Delta m_{31}^2 + \sin^2 \theta_{12} \Delta m_{32}^2. \quad (2.2)$$

(see also tutorial). **Very challenging goal, at the frontier of the field!**

# Today's summary: Intro + ...

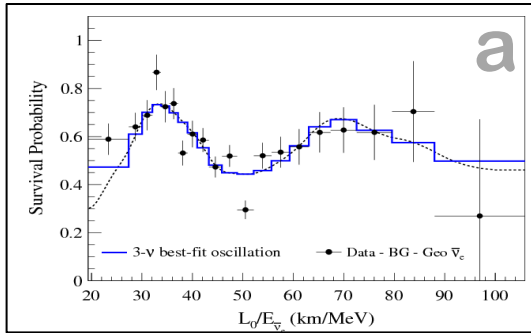
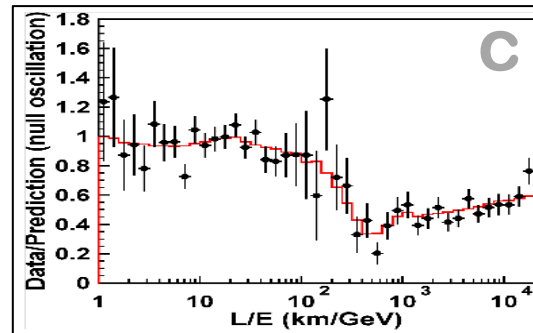
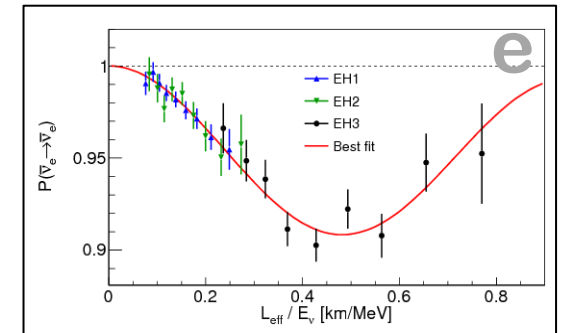
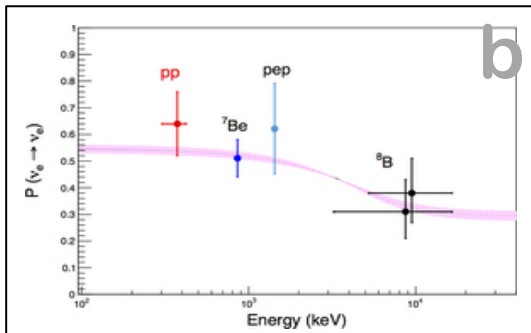
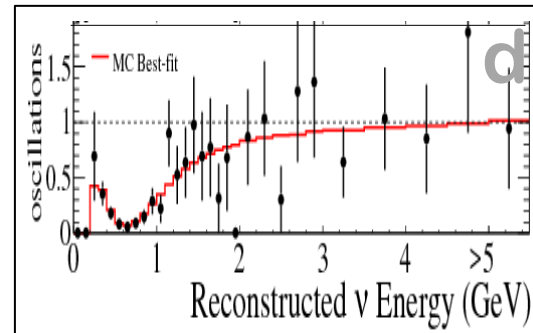
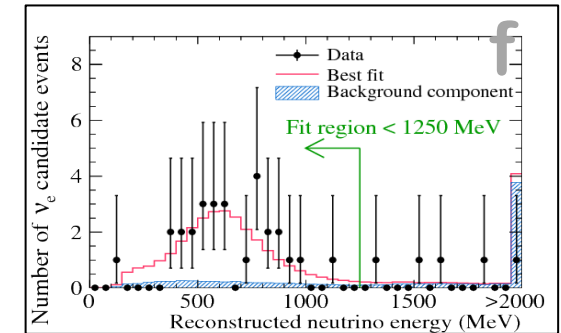
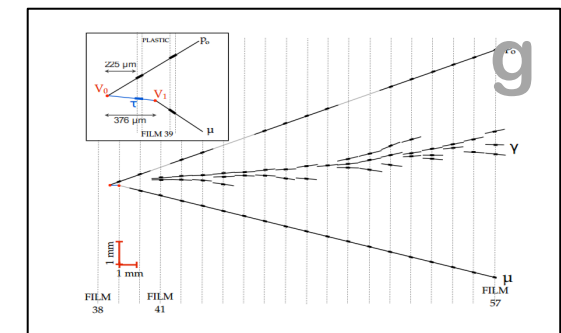
$e \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ )



$|\Delta m^2|$

$\theta_{13}$

## Next lecture:

 $e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ ) $\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ ) $e \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ ) $e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ ) $\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ ) $\mu \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ ,  $\theta_{23}$ ) $\mu \rightarrow \tau$  ( $\Delta m^2$ ,  $\theta_{23}$ )

$$\delta m^2 \quad |\Delta m^2| \quad \theta_{12} \quad \theta_{23} \quad \theta_{13}$$

+ 3ν unknowns:  $\text{sign}(\Delta m^2)$ ,  $\text{sign}(\theta_{23} - \pi/4)$ ,  $\delta$

**Thank you for your attention!**