

Atmospheric Neutrinos

Subir Sarkar (NBIA & Oxford)

NBIA PhD School: Neutrinos Underground & in the Heavens II, 1-5 August 2016, Copenhagen

Detection of naturally generated neutrinos



Discovery of atmospheric neutrinos: 1965



F. Reines, M. F. Crouch, T. L. Jenkins, W. R. Kropp, H. S. Gurr, and G. R. Smith

Case Institute of Technology, Cleveland, Ohio

and

J. P. F. Sellschop and B. Meyer

University of the Witwatersrand, Johannesburg, Republic of South Africa (Received 26 July 1965) Physical Review Letters **15** (1965) 429 - published 30th Aug 1965

Neutrino detector at the Kolar Gold Fields, India

FIGURE 18. A multiple neutrino event (event no

Discovery of atmospheric neutrino oscillations: 1998



Experiments using the atmospheric neutrino flux



The origin of cosmic rays

Extraordinary cosmic particle accelerators *somewhere*, but still **poorly identified** a century after the discovery of cosmic rays!

- Supernova remnants
- Active galactic nuclei ?
- Gamma ray bursts ?
- Radio galaxy jets ?
- Starburst galaxies ?

•

Cosmic ray interactions with matter and photons, near source or during propagation, produce neutrinos:

$$p + N \rightarrow X + \{\pi^+, \pi^-, \pi^0\}$$

$$\pi^0 \rightarrow \gamma + \gamma$$

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

Oscillations en-route to Earth can equibrate flavours so: v_e : v_{μ} : v_{τ} :: 1 : 1 : 1



Energies and rates of the cosmic-ray particles

Neutrino production through cosmic ray interactions

conventional $p, A + air \rightarrow \pi^{\pm}, \pi^{0}, K^{\pm}, K^{0}_{S,L}$

muons and muon neutrinos $\pi^{\pm}, K^{\pm} \to \mu^{\pm} \nu_{\mu}(\bar{\nu}_{\mu})$

electron neutrinos

$$K^{\pm}, K_L^0 \to [\pi^{\pm}, \pi^0] e^{\pm} \nu_e(\bar{\nu}_e)$$

prompt

$$p, A + \operatorname{air} \to D, \Lambda_{\mathrm{C}} \to \nu_{\mu}, \nu_{\mathrm{e}}, \mu$$

Subset of dominant	decay channels
--------------------	----------------

decay channel	branching ratio (BR)		
$\mu^- ightarrow e^- \bar{\nu}_e \nu_\mu$	100 %		
$\pi^+ o \mu^+ \nu_\mu$	99.9877 %		
$K^0_{e3}:K^0_L\to\pi^\pm e^\mp\nu_e$	40.55 %		
$K^0_{\mu3}:K^0_L\to\pi^\pm\mu^\mp\nu_\mu$	27.04 %		
$K^+ o \mu^+ \nu_\mu$	63.55 %		
$K_{e3}^+:K^+\to\pi^0 e^+\nu_e$	5.07 %		
$K^+_{\mu 3}: K^+ \to \pi^0 \mu^+ \nu_\mu$	3.353 %		
$D^+ \to \overline{K}^0 \mu^+ \nu_\mu$	9.2 %		
$D^0 \to K^- \mu^+ \nu_\mu$	3.3 %		

+ charge conjugates

http://pdg.lbl.gov

Prompt vs. conventional flux

The energy spectrum from semi-leptonic decay products depends on a hadronic
 'critical energy', below which the decay probability is > interaction probability:

$$\epsilon_h = \frac{m_h c^2 h_0}{c \tau_h \cos \theta} \qquad \qquad \begin{aligned} \epsilon_{\pi^{\pm}} &= 115 \ [GeV] \\ \epsilon_{K^{\pm}} &= 850 \ [GeV] \end{aligned}$$

 For pions & kaons, this critical energy is low (decay length is long) hence the leptonic energy spectrum is soft. For charmed mesons, the critical energy is high ... they decay promptly to highly energetic leptons:

$$\epsilon_{D^0} = 9.71 \times 10^7 \ [GeV]$$

$$\epsilon_{D^{\pm}} = 3.84 \times 10^7 \ [GeV]$$

$$\epsilon_{D_s^{\pm}} = 8.40 \times 10^7 \ [GeV]$$

$$\epsilon_{\Lambda_c} = 24.4 \times 10^7 \ [GeV]$$

The atmospheric neutrino flux from the decay of pions & kaons is the 'conventional flux,' whereas that from charm decay is called the 'prompt flux'

Spectrum from π/K decay is measured to high energies



Monte Carlo calculation (e.g. http://www.icrr.u-tokyo.ac.jp/~mhonda/)

Atmospheric muon spectrum



Atmospheric muon neutrino spectrum



11

Atmospheric electron neutrino spectrum



Beating the atmospheric background



By using a veto for downgoing events, we remove the atmospheric neutrinos ... because we remove the muons coming from the *same* Cosmic Ray Air Shower

What's left is: PeV-EeV astrophysical neutrinos coming from above

NB: Doesn't work for upgoing, since the Earth absorbed the muons ... so Southern Sky (downgoing events) becomes the best channel.

'High energy starting events' (HESE) analysis



Discovery of high energy cosmic neutrinos

- * 2013: 662-day analysis, with 28 candidates in the energy range [50 TeV 2 PeV]. (4.1 σ excess over the expected atmospheric background).
- * 2014: 988-day analysis, with a total of 37 events with energy [30 TeV 2 PeV]
- (5.7 σ excess), no events in the energy range [400 TeV 1 PeV], spectral $\Gamma = -2.3 \pm 0.3$.
- * 2015: 1347-day analysis, with a total of 53 + 1 events, previous energy gap partially filled, (7 σ excess), spectral $\Gamma = -2.58 \pm 0.25$.



But where are the prompt neutrinos?

• The flux of prompt neutrinos is *harder* than that of conventional neutrinos, and was predicted to **dominate** the total atmospheric flux at energies above ~10⁵⁻⁶ GeV



 The conventional background is well understood as it has been calibrated against many observations ... uncertainties in charm production make the prompt flux less so but it is the most important background for the expected astrophysical flux! ¹⁶

Tension with ERS 'benchmark'

arXiv:astro-ph/1410.1749 arXiv:hep-ph/0806.0418



Recent data put an **upper limit** on the prompt flux above 1 TeV, which is *less* than ~1.06 x the benchmark ERS 2008 calculation (arXiv:1607.08006)

Even stronger limit of 0.54×ERS @ 90% C.L. from combined IC59 + IC79 + IC86 data (Sebastian Schonen, IPA 2015)

Need a better calculation of cosmic ray charm hadroproduction and decay

Theoretical calculations

- Volkova, Sov. J. Nucl. Phys. 12 (1980) 784
- Bugaev, Naumov, Sinegovksy, Zaslavskaya, Il Nuovo Cim. C 12 (1989) 41
- Lipari, Astropart. Phys. 1 (1993) 195
- Thunman, Ingelman, Gondolo (TIG), Astropart. Phys. 5 (1993) 309
- **Pasquali, Reno, Sarcevic** (PRS), Phys. Rev. D**59** (1999) 034020
- Gelmini, Gondolo, Varieschi (GGV1), Phys. Rev. D61 (2000) 036005
- Gelmini, Gondolo, Varieschi (GGV2), Phys. Rev. D61 (2000) 056011
- Martin, Ryskin, Stasto (MRS), Acta Phys. Polonica B34 (2003) 3273
- Enberg, Reno, Sarcevic (ERS), Phys. Rev. D78 (2008) 043005
- Bhattacharya, Enberg, Reno, Sarcevic, Stasto (BERSS), JHEP 06 (2015) 110
- Garzelli, Moch, Sigl (GMS), JHEP 10 (2015) 115
- Gauld, Rojo, Rottoli, Sarkar, Talbert (GRRST), JHEP 02 (2016) 130

Calculating the prompt flux of atmospheric neutrinos requires a synthesis of QCD, cosmic ray physics, and neutrino physics

Tracing a particle through the atmosphere

• The flux of particle j can be generically written as:

$$\frac{d\phi_j}{dX} = -\frac{\phi_j}{\lambda_j} - \frac{\phi_j}{\lambda_j^{dec}} + \sum S(k \to j)$$

Interaction decay production

• This depends on the '**slant depth**' X measuring the atmosphere traversed:

$$X(l,\theta) = \int_{l}^{\infty} \rho(H(l',\theta)dl' \qquad \qquad H(l,\theta) \simeq l\cos\theta + \frac{l^2}{2R_0}\sin^2\theta$$

• Adopt a simple **isothermal model** of the atmosphere:

$$\rho(H) = \rho_0 e^{-\frac{H}{H_0}} \qquad \qquad \rho_0 = 2.03 \times 10^{-3} \ \left[\frac{g}{cm^3}\right] \\ H_0 = 6.4 \ [km]$$

• Such that sample values of X are:

$$X = 0 \begin{bmatrix} \frac{g}{cm^2} \end{bmatrix} (space) \qquad X = 1300 \begin{bmatrix} \frac{g}{cm^2} \end{bmatrix} (\theta = 0)$$
$$X = \infty \begin{bmatrix} \frac{g}{cm^2} \end{bmatrix} (ground) \qquad X = 36000 \begin{bmatrix} \frac{g}{cm^2} \end{bmatrix} (\theta = \frac{\pi}{2})$$

Cascade Formalism: Sources & Z-moments

$$S(k \to j) = \int_{E}^{\infty} \frac{\phi_k(E'_k)}{\lambda_k(E'_k)} \frac{dn(k \to j; E', E)}{dE} dE'$$

- Assuming factorisation in energy vs. depth in atmosphere , the S-moments simplify:
 - For particle **production**:

$$S(k \to j) = \frac{\phi_k}{\lambda_k} Z_{kj}$$

$$Z_{kh} = \int_{E}^{\infty} dE' \frac{\phi_k(E', X, \theta)}{\phi_k(E, X, \theta)} \frac{\lambda_k(E)}{\lambda_k(E')} \frac{dn(kA \to hY; E', E)}{dE}$$

$$\frac{dn(pA \to hY; E', E)}{dE} = \frac{1}{\sigma_{pA}(E')} \frac{d\sigma(pA \to hY; E', E)}{dE}$$

• For particle **decay**:

$$Z_{h\to l} = \int_{E}^{\infty} dE' \frac{\phi_h(E', X)}{\phi_h(E, X)} \frac{d_h(E)}{d_h(E')} \frac{dn(h \to lY; E', E)}{dE} \qquad \qquad \frac{dn(h \to lY; E', E)}{dE} = \frac{1}{\Gamma} \frac{d\Gamma}{dE}$$

Atmospheric Nucleon Flux

$$\frac{d\phi_N}{dX} = -\frac{\phi_N}{\lambda_N} + S(NA \to NY) = -\frac{\phi_N}{\lambda_N} + Z_{NN}\frac{\phi_N}{\lambda_N}$$

Assume a **factorisation** of fluxes $\longrightarrow \phi_k(E, X) = \phi_k(E)\phi_k(X)$

Define the **interaction** length $\longrightarrow \lambda_N(E) = \frac{A}{N_0 \sigma_{pA}(E)}$

Define the **attenuation** length

$$\Lambda_N = rac{\lambda_N}{(1-Z_{NN})}$$

$$\frac{d\phi_N}{dX} = \frac{\phi_N}{\lambda_N} \left(Z_{NN} - 1 \right) \rightarrow \frac{d\phi_N}{dX} + \frac{\phi_N}{\lambda_N} \left(1 - Z_{NN} \right) = 0$$

$$\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$$

$$\phi_N = \phi_N^0(E) \ e^{-\frac{X}{\Lambda_N}}$$
What is the primary nucleon flux?

Incident Cosmic Ray Fluxes: $\phi_N^0(E)$

 Cosmic ray spectrum constrained ~up to 10⁵ GeV by balloon and space expts, e.g. AMS and CREAM

 Higher energies rely on air shower arrays, e.g.
 Kascade, Auger & TA ... many uncertainties regarding CR composition



Does a 'Broken-Power-Law' (BPL) fit the data?

$$\phi_N^0(E) = \begin{cases} 1.7 \ E^{-2.7} & \text{for } E < 5 \times 10^6 \ GeV \\ 174 \ E^{-3} & \text{for } E > 5 \times 10^6 \ GeV \end{cases}$$

But cosmic rays are not just protons!



The composition is not very well known at high energies hence empirical parameterisations must be used (guided by some 'theoretical' expectations and the energy spectrum shape)

arXiv:astro-ph/1111.6675 arXiv:astro-ph/1303.3565



Primary Energy, E [GeV]

Gaisser *et al*. fits:

 $\phi_N^0(E)$

$$\phi_i(E) = \Sigma_{j=1}^3 a_{i,j} E^{-\gamma_{i,j}} \times \exp\left[-\frac{E}{Z_i R_{c,j}}\right]$$

	р	He	CNO	Mg-Si	Fe
Pop. 1:	7860	3550	2200	1430	2120
$R_c = 4 \text{ PV}$	$1.66\ 1$	1.58	1.63	1.67	1.63
Pop. 2:	20	20	13.4	13.4	13.4
$R_c = 30 \text{ PV}$	1.4	1.4	1.4	1.4	1.4
Pop. 3:	1.7	1.7	1.14	1.14	1.14
$R_c = 2 \text{ EV}$	1.4	1.4	1.4	1.4	1.4
Pop. $3(*)$:	200	0.0	0.0	0.0	0.0
$R_c = 60 \text{ EV}$	1.6				

BPL vs. Gaisser parameterisations



• The effect of the new parameterisations is significant above ~10⁶ GeV ...

Atmospheric hadron flux

$$\frac{d\phi_h}{dX} = -\frac{\phi_h}{\rho d_h(E)} - \frac{\phi_h}{\lambda_h} + Z_{hh} \frac{\phi_h}{\lambda_h} + Z_{ph} \frac{\phi_p}{\lambda_p}$$

- In the low energy limit, the probability for hadron interaction is minimal, so we can
- neglect the interaction and regeneration terms:

$$\phi_h|_{low} = \frac{Z_{ph}}{\Lambda_p(1-Z_{pp})}\rho d_h\phi_p(E)e^{-\frac{X}{\Lambda_p}}$$

• At high energies the decay length becomes large, hence we **neglect the decay term**:

$$\phi_h|_{high} = \frac{Z_{ph}\phi_p(E)}{(1-Z_{pp})} \frac{\left(e^{-\frac{X}{\Lambda_h}} - e^{-\frac{X}{\Lambda_p}}\right)}{\left(1 - \frac{\Lambda_p}{\Lambda_h}\right)}$$

• These solutions then **feed into asymptotic solutions for the final leptonic flux** (note that the low-energy solution scales with an additional power of *E*):

$$\begin{array}{ll} high & \phi_h \propto \phi_p \\ low & \phi_h \propto E \phi_p \end{array}$$

Lepton flux @ detector

1.
$$\frac{d\phi_p}{dX} = -\frac{\phi_p}{\lambda_p} + Z_{pp}\frac{\phi_p}{\lambda_p}$$
2.
$$\frac{d\phi_h}{dX} = -\frac{\phi_h}{\rho d_h(E)} - \frac{\phi_h}{\lambda_h} + Z_{hh}\frac{\phi_h}{\lambda_h} + Z_{ph}\frac{\phi_p}{\lambda_p}$$
3.
$$\frac{d\phi_l}{dX} = \sum_h Z_{h \to l}\frac{\phi_h}{\rho d_h}$$
Full series of cascade equations, from incoming cosmic ray nucleons to final state leptons
$$\oint_{l|low} = \phi_p(E) Z_{h \to l}^{low} \frac{Z_{ph}}{(1 - Z_{pp})}$$

$$\oint_{l|high} = \frac{Z_{h \to l}\epsilon_h}{E} \frac{Z_{ph}\phi_p(E)}{(1 - Z_{pp})(1 - \frac{\Lambda_p}{\lambda_h})} \ln \frac{\Lambda_h}{\Lambda_p}$$

$$\oint_{l|low} = \int_h \frac{\phi_l^{low}\phi_l^{high}}{\phi_l^{low}} + \phi_l^{high}}$$

• Our final flux includes all (interpolated) contributions from charmed hadrons

The QCD input: *Z*_{ph}

$$Z_{ph} = \int_{E}^{\infty} dE' \frac{\phi_p(E')}{\phi_p(E)} \frac{A}{\sigma_{pA}(E)} \frac{d\sigma(pp \to c\bar{c}Y; E', E)}{dE}$$

- The **differential cross-section** can be calculated in a variety of formalisms, e.g. the ERS 'colour dipole model' which is *empirical* (but is the basis of the benchmark calculation)
- However, perturbative QCD (with DGLAP evolution) *can* describe charm production for the *entire* kinematical region of interest, hence can calculate with Next-to-Leading-Order QCD+Parton Shower Monte-Carlo event generators
- Boosting from CM to the rest frame of the (atmospheric) fixed target, one finds:

$$\sqrt{s} = 7 \ [TeV] \iff E_b = 2.6 \times 10^7 \ [GeV]$$

 Thus there is complementarity with LHC physics. We can predict the prompt neutrino flux at energies up to 10⁷ GeV ... at these energies, the charm production cross section is dominated by gluon fusion, hence we are sensitive to the behaviour of the gluon PDF (parton distribution function) at small-x

The (perturbative) QCD approach



... does a great job!



... of understanding high energy collisions



 $\Lambda_{QCD} \sim 200 \,\mathrm{MeV}$

The QCD input: *Z*_{ph}



32

... can now confront with LHC data!



Cosmic ray interactions probe the very 'forward' region

The QCD input: *Z*_{ph}

* We used QCD in the standard collinear factorization formalism.

* So far this has been succesfully employed not only to explain ATLAS and CMS results (central pseudorapidities), but even many observables at LHCb (mid-forward pseudorapidities $2 < \eta < 5$).

* LHCf is able to investigate in very-forward rapidity regions (8.4 < η < ∞) the production of γ 's, π^{0} 's, neutrons and light neutral hadrons, no charmed charged particles :-(

* total cross-section for $c\bar{c}$ pair hadroproduction using NNLO QCD radiative corrections in pQCD.

* differential cross-section for $c\bar{c}$ pair hadroproduction not yet available at NNLO; use of a NLO QCD + Parton Shower + hadronization + decay approach.

* QCD parameters of computation and uncertainties due to the missing higher orders fixed by theory, i.e. by looking at the convergence of the perturbative series (LO/NLO/NNLO comparison).

Predicting total #-secn in perturbative QCD

 $\sigma(pp \rightarrow c\bar{c})$ at LO, NLO, NNLO QCD



exp data from fixed target exp + colliders (STAR, PHENIX, ALICE, ATLAS, LHCb).

$$E_{lab} = 10^{6} \text{ GeV} \sim E_{cm} = 1.37 \text{ TeV})$$

 $E_{lab} = 10^{8} \text{ GeV} \sim E_{cm} = 13.7 \text{ TeV})$
 $E_{lab} = 10^{10} \text{ GeV} \sim E_{cm} = 137 \text{ TeV})$



 We first validate our NLO predictions for forward charm production against recent LHCb data ... finding good agreement between the 3 calculation schemes

B ⁰ mesons,	2.0 < y < 2.5
------------------------	---------------

10 -----

arXiv: 1506.08025

Small-*x* Gluon NNPDF: LHCb constraints

- We utilise charm production data from LHCb to reduce the uncertainties in the small-x gluon PDF
- By implementing a **Bayesian reweighting technique**, the impact of the new data is estimated ... 75 data points added to NNPDF3.0 analysis
- The impact is negligible for x > 10⁻⁴, but substantial in the smaller-x region where data was previously unavailable. At x ~ 10⁻⁵, we achieve a 3x reduction in uncertainty
- We utilise these improved PDFs to make **predictions for 13 TeV** physics



Validation with LHC Run II data @13 TeV



Our new result: *Z*_{ph}

$$Z_{ph} = \int_{E}^{\infty} dE' \frac{\phi_p(E')}{\phi_p(E)} \frac{A}{\sigma_{pA}(E)} \frac{d\sigma(pp \to c\bar{c}Y; E', E)}{dE}$$

The differential cross-section is generated at various E' between 10³ and 10¹⁰ GeV with POWHEG+PYTHIA8, and incorporates our updated NNPDF3.0+LHCb ... Cross-checks made with aMC@NLO



Gauld, Rojo, Sarkar, Rotolli, Talbert, arXiv:1506.08025

Benchmark NNPDF3.0+LHCb data

 Predictions for prompt atmospheric neutrino flux adopting the broken power-law (BPL) as well as H3A and H3P cosmic-ray spectra



Scale, PDF, and charm mass uncertainty

Different cosmic ray spectrum parameterisations => **significant differences in the expected flux above ~100 TeV**

Consistency with previous calculations



Consistent with recent IceCube data



Conclusions

- The most important background for the detection of cosmic neutrinos is the (uncertain) flux of **prompt atmospheric neutrinos**
- This can be calculated in **perturbative QCD**, incorporating:
 - 1. State-of-the-art calculation of **charmed hadron production** in the **forward region**, validated against recent LHCb measurements
 - 2. A **small-***x* **gluon PDF** which is also constrained by LHCb data
- Current estimates are consistent with previous studies but provide a more reliable estimate of uncertainties and alleviate the tension between the previous empirical (ERS) calculation and IceCube data

The prompt flux should be seen *soon* (and provide a probe of low-*x* QCD)