

# Measuring the Leptonic CP Phase in Neutrino Oscillations with Non-Unitary Mixing

Pedro S. Pasquini<sup>1,2</sup>

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**NBIA PhD School: Neutrinos Underground & in the Heavens II**

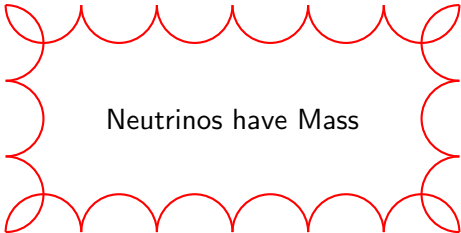
<sup>1</sup>Universidade Estadual de Campinas (Unicamp) - Brazil

<sup>2</sup>Instituto de Fisica Corpuscular (IFIC) - Spain

Fact<sup>5</sup>:

<sup>5</sup>Phys. Rev. Lett. **81**, 1158 (1998)

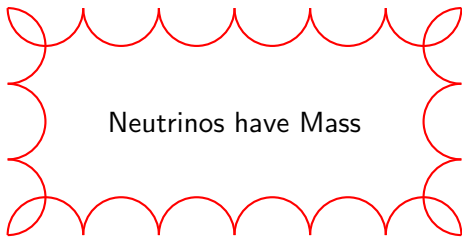
Fact<sup>5</sup>:



Neutrinos have Mass

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And they Oscillate!

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# Two basis! Mass and Flavor



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<http://lbne.fnal.gov/>

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There are two basis:

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Interaction (flavor) basis

$\nu_\alpha$ ,  $\alpha = e, \mu, \tau, 4, 5 \dots N$

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$$\nu_i, \quad i = 1, 2, 3, \dots N$$



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Mixing Matrix

$$\nu_\alpha = U_{\alpha i} \nu_i$$

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## $U$ mixing is unitary. But parts of it not!

If  $N > 3$  and  $M_h \gg E_{\text{exp}}$

$$U^{N \times N} = \begin{pmatrix} N & W \\ V & T \end{pmatrix}$$

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A red arrow points from the  $U^{N \times N}$  term to the word "Unitary". A blue arrow points from the  $N$  element in the top-left of the matrix to the word "Non-Unitary".

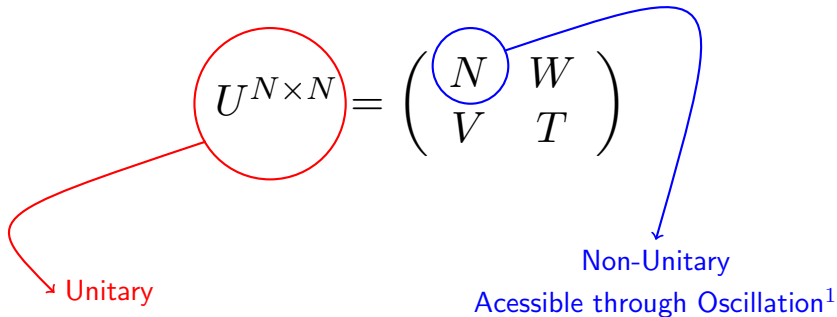
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Unitary

Non-Unitary  
Accessible through Oscillation<sup>1</sup>

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It can be shown that<sup>2</sup>:

$$N = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ \alpha_{21} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} \cdot U_{\text{PMNS}}$$

<sup>2</sup> F. J. Escrihuela et. al., Phys. Rev. D92, 053009 (2015)



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Only 3 ( $\alpha_{11}$ ,  $\alpha_{22}$  and  $\alpha_{21}$ ) are accessible through  $\nu_{e(\mu)} \rightarrow \nu_{\mu(e)}$

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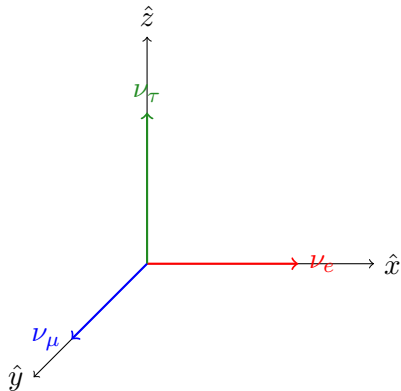


**In unitary: Probability add to 1**

# In non-unitary: Probability Don't add to 1

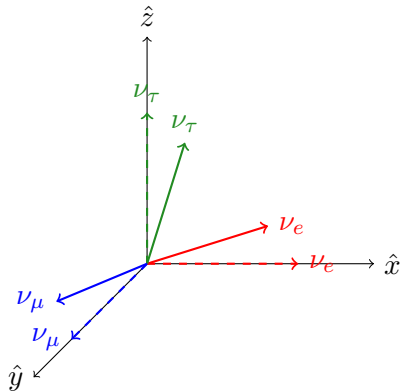
# Non-unitary basis is not Orthogonal!

Unitary



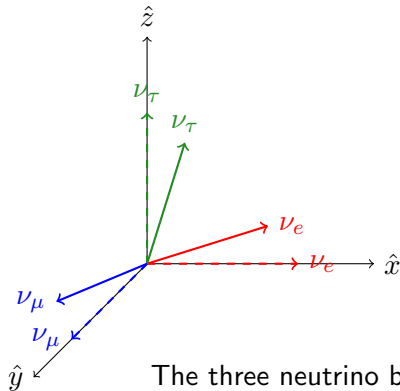
# Non-unitary basis is not Orthogonal!

Non- Unitary



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## Non- Unitary



The three neutrino basis is not orthogonal!

# New Phenomenon: 0-Distance and CP-phase

This means that you can have 0-distance 'oscillation' (transition):

<sup>3</sup> F. Ge, P. Pasquini, et. al., ARXIV:1605.01670



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$$(S_{\alpha\beta} = \langle \nu_\alpha^{\text{unitary}}(L) | \nu_\beta^{\text{unitary}}(L) \rangle)$$

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$P_{ee}(0) = 1$

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Complex parameter  
with a **new** CP phase ( $\phi$ )!

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Why do we care?



<sup>4</sup> Miranda, O. G., et. al., ARXIV:1604.05690

<sup>2</sup> F. J. Escrihuela et. al., Phys. Rev. D92, 053009 (2015)



Why do we care?

Non-unitary can lead to CP-phase ambiguity<sup>4</sup>!



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That's because  $|\alpha_{21}|$  can be as large as  $s^2 \sim 3\%$



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We can see that by two plots:

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$P_{\mu e}$  for different  $\delta_{CP}$  and  $\phi$ .



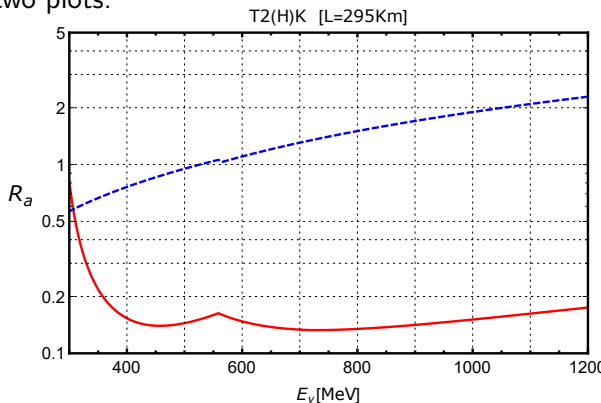
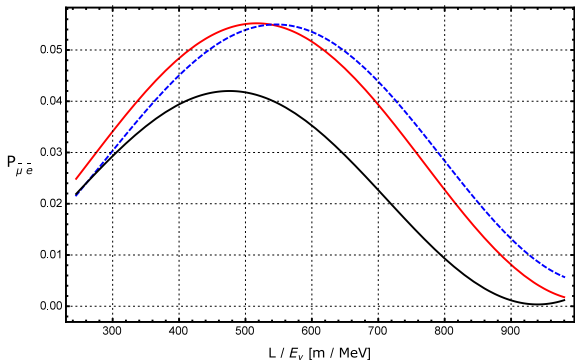
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$P_{\mu e}$  for different  $\delta_{CP}$  and  $\phi$ .

The ratio  $R$  between the contributions of  $\delta_{CP}$  and  $\phi$  to  $P_{\mu e}$



We can see that by two plots:



$P_{\mu\bar{e}}$ :  $\delta_{CP} = 0$  and  $\alpha_{21} = 0$ ,  $\delta_{CP} = 3\pi/2$  and  $\alpha_{21} = 0$ ,  $\delta_{CP} = 0$  and  $\alpha_{21} = 0.02$

$R_a$ :  $\alpha = 2.5\%$  and  $R$ :  $c_\phi$  and  $s_\phi$  and  $c_{\phi+\delta}$  and  $s_{\phi+\delta}$  contributions.

From: <sup>3</sup> F. Ge, P. Pasquini, et. al., ARXIV:1605.01670



# T2(H)K experiment is awesome!

What about in Experimental Setup?

From: <sup>5</sup> Abe, K. and others, PTEP **2015**, no. 4, 043C01 (2015)



# T2(H)K experiment is awesome!

What about in Experimental Setup?

one of T2K and T2HK goal is to measure  $\delta_{CP}$

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# T2(H)K experiment is awesome!

What about in Experimental Setup?

one of T2K and T2HK goal is to measure  $\delta_{CP}$

The experiment consists of neutrinos flux from pion decay at Tokay

From: <sup>5</sup> Abe, K. and others, PTEP **2015**, no. 4, 043C01 (2015)





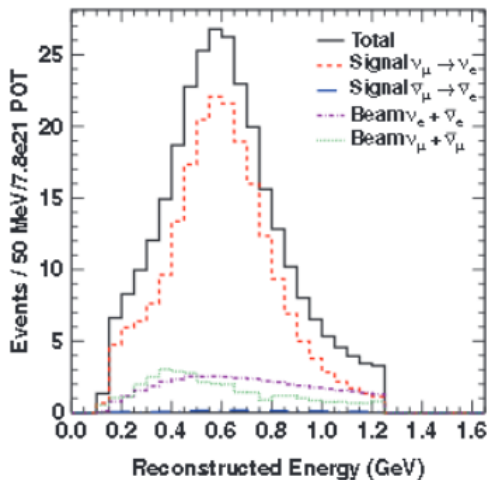








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The detector:

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The detector:

Super(Hyper)-K: a Huge water cherenkov detector at Kamioka

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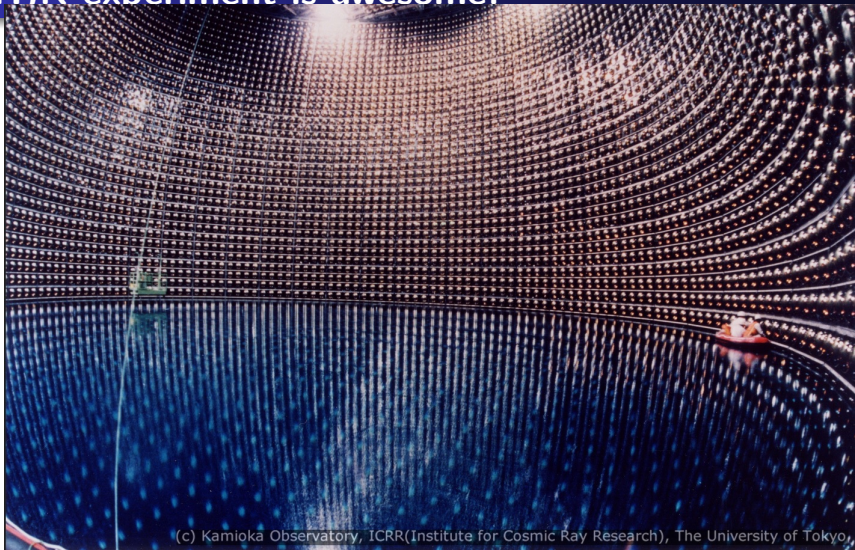
Super(Hyper)-K: a Huge water cherenkov detector at Kamioka

Size: 50 kton (560 kton) and Base Line: 295 km

From: <sup>5</sup> Abe, K. and others, PTEP **2015**, no. 4, 043C01 (2015)



# T2(H)K experiment is awesome!



(c) Kamioka Observatory, ICRR(Institute for Cosmic Ray Research), The University of Tokyo,

From: <sup>5</sup> Abe, K. and others, PTEP **2015**, no. 4, 043C01 (2015)



# T2K and T2HK cannot measure $\delta_{CP}$

T2K and T2HK says they can measure the  $\delta_{CP}$  :

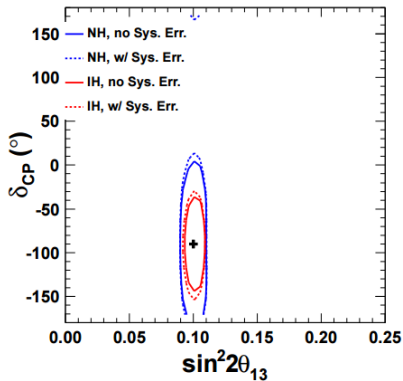
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# T2K and T2HK cannot measure $\delta_{CP}$

T2K a



$\delta_{CP}$  :

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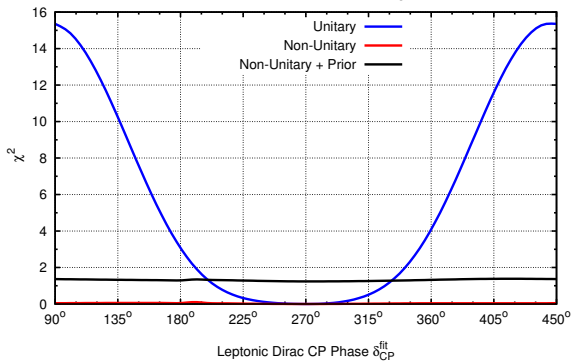
We performed the analysis on T2K and T2HK considering non-unitary:

From: <sup>5</sup> Abe, K. and others, PTEP **2015**, no. 4, 043C01 (2015)

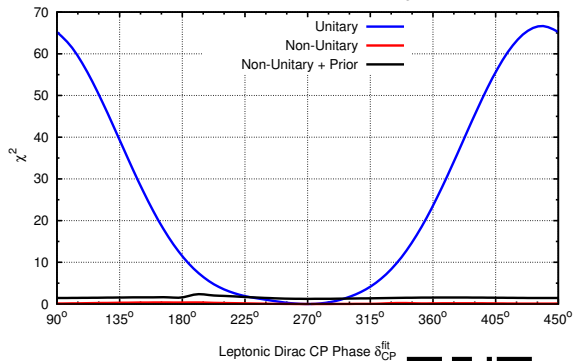


# T2K and T2HK cannot measure $\delta_{CP}$

The effect of including non-unitarity at T2K [  $\delta_{CP}^{\text{true}} = -90^\circ$ , NH ]



The effect of including non-unitarity at T2HK [  $\delta_{CP}^{\text{true}} = -90^\circ$ , NH ]



From: <sup>3</sup> F. Ge, P. Pasquini, et. al., ARXIV:1605.01670



Should we give up on T2(H)K  $\delta_{CP}$ ?

From: <sup>6</sup> J. Evslin et al., JHEP 02, 137 (2016)



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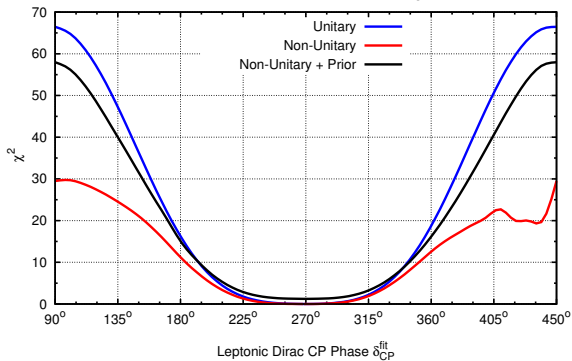
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So what happens to the  $\delta_{CP}$  sensibility?

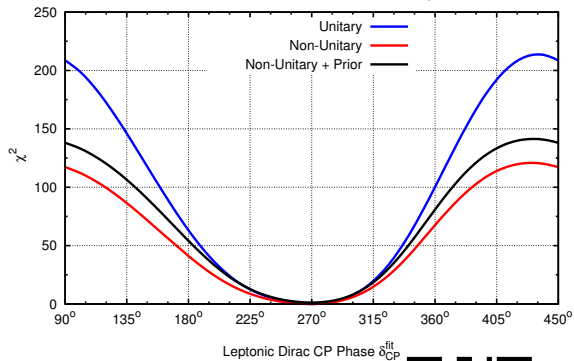


## Should we give up on T2(H)K $\delta_{CP}$ ?

The effect of including non-unitarity at T2K+ $\mu$ SK [  $\delta_{CP}^{\text{true}} = -90^\circ$ , NH ]



The effect of including non-unitarity at T2HK+ $\mu$ HK [  $\delta_{CP}^{\text{true}} = -90^\circ$ , NH ]



From: <sup>6</sup> J. Evslin et al., JHEP 02, 137 (2016)





Non-unitary can mimic  $\delta_{CP}$

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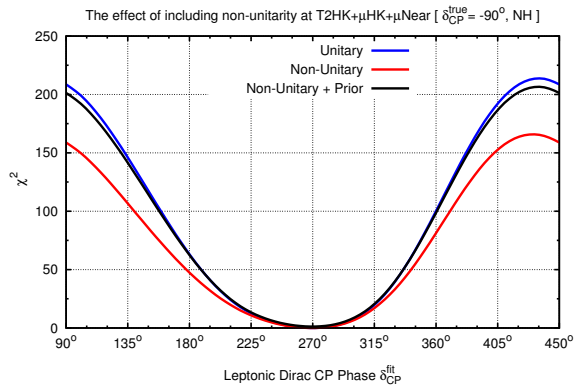
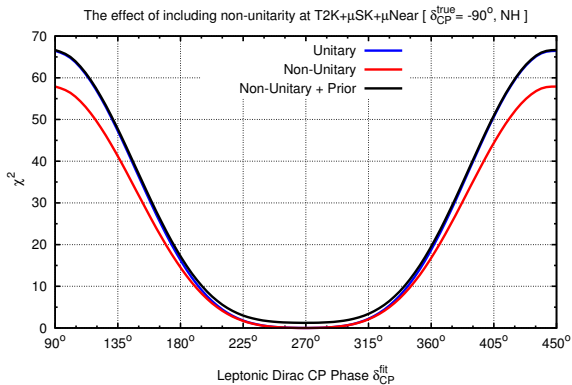
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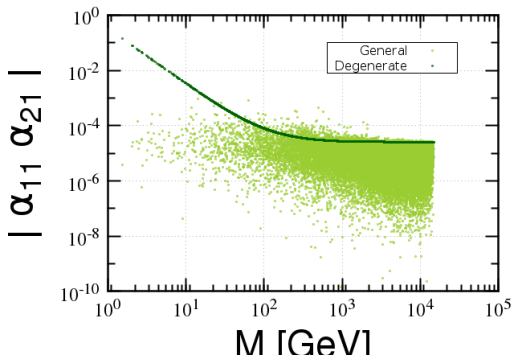
It is possible to recover T2(H)K sensitivity by coupling it to  $\mu$ DAR

Using a very near detector (20 m) to probe  $P_{\mu e}(0) = |\alpha_{21}|^2$





## Model Dependent Couplings



## DUNE Sensibility?

