## Small (and large) scale structure beyond SIDM

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### **Beyond SIDM: Motivation**

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	1	1



Cherry et al., (2014)

### **Beyond SIDM: Motivation**

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	<b>√</b>	1
SIDM	×	1	1
SIDM + DR	<i>✓</i>	<i>√</i>	1



Cherry et al., (2014)

#### Beyond SIDM: small (and large) scales



- Dark Radiation Dark Matter
- Warm Dark Matter (Talk by Laura Lopez-Honorez)
- Fuzzy Dark Matter

(Talk by Luca Visinelli)

- Decaying Dark Matter
- Late Forming Dark Matter

#### Dark radiation - dark matter interactions



#### Timeline

Temperature	Process	Probe
$T_{\chi} \sim m_{\chi}$ / 25	DM freeze-out	DM relic abundance
T > 200 MeV	Dark sector decoupling	N <sub>eff</sub> BBN & CMB
$T_{\gamma} \sim 1 \text{ MeV}$	BBN & $v$ decoupling	
T <sub>Dark</sub> > 100 eV	DM kinetic decoupling*	CMB, Ly- $\alpha$ , Astrophys. obs.
T <sub>Dark</sub> < 100 eV	DR kinetic decoupling	СМВ
$T_{\gamma} \sim 1 \text{ eV}$	СМВ	
Structure formation	DM self-interactions	Astrophysical observations

\*= since H ~ T<sup>2</sup> during RDE, there is decoupling only if  $\tau^{-1}$  ~ T<sup>n</sup> with n>2, otherwise dark matter and dark radiation recouple at later times.

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Tulin et al., PRD (2013)

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#### Dark radiation

$$\xi(T) = \frac{T_{dark}}{T_{(\gamma)}}$$

$$g_{*S}(T) = g_{*S,vis}(T) + \sum_{i=bosons} g_{dark}(T)\xi^{3}(T) + \frac{7}{8} \sum_{i=fermions} g_{dark}(T)\xi^{3}(T)$$

$$s_{tot}(T) \propto g_{*S}(T)T^{3}$$

$$\xi^{3}(T_{BBN}) = \xi^{3}(T_{RH}) \frac{g_{*S,vis}(T_{BBN})}{g_{*S,vis}(T_{RH})} \frac{g_{dark}(T_{RH})}{g_{dark}(T_{BBN})}; \quad \xi(T_{RH}) = 1$$

$$\xi^{3}(T_{CMB}) = \xi^{3}(T_{BBN}) \left(\frac{4}{11}\right) \quad \text{For massless dark radiation and massive mediator}$$

$$\rho_{rad} \propto g_{*}T^{4}$$

$$\Delta N_{eff}(T_{BBN/CMB}) = \frac{\left(\sum_{i=bosons} g_{dark}(T) + \frac{7}{8} \sum_{i=fermions} g_{dark}(T)\right)}{2 \times 7/8} \frac{\xi^{4}(T_{BBN/CMB})}{(4/11)^{4/3}} \quad \begin{array}{c} \text{Equivalent neutrino number} \\ \rho_{rad} = \left[1 + \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} N_{eff}\right] \rho_{\gamma}, \quad N_{eff} = 3.046 + \Delta N_{eff} \end{array}$$

#### Dark radiation: constraints from BBN

Shortly after neutrino decoupling the weak interactions that kept neutrons and protons in statistical equilibrium freeze out.



 $\Delta N_{eff}(BBN) < 1 \ (95\% c.l.)$ 

#### Dark radiation: constraints from CMB



Background effects:

expansion rate

Perturbation effects (free-streaming):

- phase shift in  $\delta_{\gamma}$
- overall amplitude suppression (anisotropic stress)



$$N_{eff}(CMB) = 2.99 \pm 0.20 \ (68\% cl) \rightarrow \xi \le 0.5 \ (95\% cl)$$

The clustering of cold dark matter before baryon drag is described by the Meszaros

equation:  $\ddot{\delta}_{c}^{slow} + \frac{\dot{a}}{a}\dot{\delta}_{c}^{slow} = 4\pi G a^{2}\rho_{c}\delta_{c}^{slow}$  CDM is self-gravitating For photons:  $(1+R)\ddot{\delta}_{\gamma}^{fast} + \frac{\dot{a}}{a}\dot{\delta}_{\gamma}^{fast} + \frac{1}{3}k^{2}R\delta_{\gamma}^{fast} = 0 \Rightarrow$  CMB primary anisotropies



$$\dot{\delta}_{DM} + \theta_{DM} - 3\dot{\phi} = 0$$
$$\dot{\theta}_{DM} - k^2 c_D^2 \delta_{DM} + H \theta_{DM} - k^2 \psi = 0$$

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$$\dot{\delta}_{DM} + \theta_{DM} - 3\dot{\phi} = 0$$
  
$$\dot{\theta}_{DM} - k^2 c_D^2 \delta_{DM} + H \theta_{DM} - k^2 \psi = \Gamma_{DM} (\theta_{DM} - \theta_{DR})$$

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equation:  $\ddot{\delta}_{c}^{slow} + \frac{\dot{a}}{a}\dot{\delta}_{c}^{slow} = 4\pi Ga^{2}\rho_{c}\delta_{c}^{slow}$  CDM is self-gravitating

For photons:  $(1+R)\ddot{\delta}_{\gamma}^{fast} + \frac{\dot{a}}{a}\dot{\delta}_{\gamma}^{fast} + \frac{1}{3}k^2R\delta_{\gamma}^{fast} = 0 \Rightarrow \text{CMB primary anisotropies}$ 







Relative change wrt  $\Lambda$ CDM+ $\Delta$ N<sub>eff</sub> (same bkg.)

 Scale dependent phase shift and amplitude suppression

If during MDE DM is still coupled: relative suppression of the odd (compression) peaks.

See also: Atomic DM *Cyr-Racine et al., PRD (2013) Cyr-Racine et al., PRD (2014)* 

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#### Kinetic decoupling: bounds from Ly-lpha

Talk by T. Binder

$$\Gamma_{DM} = H \longrightarrow T_{kd}(m_{\chi}, m_{\phi}, g_{\chi}, g_{\nu}, \xi)$$

The mass of the smallest proto-halos corresponds to the mass enclosed in the Hubble horizon at the time of kinetic decoupling.





0.2

0.0

0.005 0.010

 $\sigma_8$ 

0.500

1

0.050 0.100

k ( $Mpc^{-1}$ )





- $\tau_{DM}^{-1} \sim T^2$  Non-Abelian DM Buen-Abad et al., PRD (2015)
- τ<sub>DM</sub><sup>-1</sup>~T<sup>4</sup> ~massless mediator const. cross section *Wilkinson et al., JCAP (2014)*
- τ<sub>DM</sub><sup>-1</sup>~T<sup>6</sup> massive mediator
   Van den Aarssen et al., PRL (2012)





#### Coupling to active neutrinos



#### Constraints on DM- $\nu$



#### Active neutrino self-interactions



#### Constraints on active $\nu$ SI



Z, W, and kaon decays, and electron neutrino scattering.

#### Astrophysical constraints

#### Kolb & Turner, PRD (1987)

#### Supernova 1987A and the secret interactions of neutrinos

Edward W. Kolb

Osservatorio Astronomico di Roma, via del Parco Mellini 84, 00136 Rome, Italy and NASA/Fermilab Astrophysics Center, Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois 60510 and Department of Astronomy and Astrophysics, The University of Chicago, Chicago, Illinois 60637

#### Michael S. Turner

NASA/Fermilab Astrophysics Center, Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois 60510 and Department of Astronomy and Astrophysics, The University of Chicago, Chicago, Illinois 60637 and Department of Physics and the Enrico Fermi Institute, The University of Chicago, Chicago, Illinois 60637 (Received 13 July 1987)

By using SN1987A as a "source" of neutrinos with energy ~10 MeV we place limits on the couplings of neutrinos with cosmic background particles. Specifically, we find that the Majoron-electron-neutrino coupling must be less than about  $10^{-3}$ ; if neutrinos couple to a massless vector particle, its dimensionless coupling must be less than about  $10^{-3}$ ; and if neutrinos couple with strength g to a massive boson of mass M, then g/M must be less than 12 MeV<sup>-1</sup>.

#### Massive mediator: g/M < 12 MeV<sup>-1</sup>

#### Constraints on active vSI

Cosmological constraints CMB



## Constraints on active vSI summary



Dark matter coupling to active neutrinos is strongly constrained.

### Coupling to (eV) sterile neutrinos



Talk by J. Kersten

### The case for sterile neutrinos



Non-standard physics: partial thermalization of sterile neutrinos in the early Universe.

$$\Delta N_{eff} = \frac{\rho_{v,s}}{\rho_{v,m=0}^{thermal}} \left( \frac{P_{v,s} / \rho_{v,s}}{1/3} \right); \qquad \rho = \frac{g}{2\pi^2} \int dp E p^2 f(p)$$

- Lepton asymmetry Mirizzi et al., PRD (2012); Hannestad et al., JCAP (2012)
- Low reheating scenarios Lattanzi et al., PRD (2015)
- "Secret" sterile neutrino self-interactions <---</li>

### $\nu_{s}$ Secret Interactions

The sterile neutrino is coupled to a new light pseudoscalar (Majoron models)

 $L_{\rm int} \sim g_s \phi \overline{\nu}_s \gamma_5 \nu_s$ 

The phenomenological success of the model requires:



#### $\nu_{s}$ Secret Interactions

The sterile neutrino is coupled to a new light pseudoscalar (Majoron models)

$$L_{\rm int} \sim g_s \phi \overline{\nu}_s \gamma_5 \nu_s$$

Non-cosmological constraints:



 $etaeta g_{e}$  < 3 x 10<sup>-5</sup> Bernatowicz et al, PRL (1992)



SN energy loss  $g_e < 4 \times 10^{-7}$  $g_s < 10^{-5}$ Farzan, PRD (2003)

### Early Universe: flavour evolution

 $\rho(p,t) = \begin{pmatrix} \rho_{aa} & \rho_{as} \\ \rho_{sa} & \rho_{ss} \end{pmatrix} = \frac{f_0(p)}{2} \Big[ P_0(p,t) + \overline{\sigma} \times \overline{P}(p,t) \Big];$  $\frac{d\overline{P}}{dt} = \overline{V} \times \overline{P} - D\overline{P}_T + \frac{R}{f_0}\hat{z}$  $\overline{V} = \overline{V}_{vacuum} + \overline{V}_{medium} + \overline{V}_{s}$  $V_{vaccum} = \frac{\Delta m^2}{2 n}$  $V_{medium} \propto \frac{G_F}{M_e^2} n_a p T^4$  $D = \frac{1}{2}\Gamma$  damping  $R = \Gamma \left( f_0 - \frac{f_0}{2} (P_0 + P_z) \right) \quad \text{repopulation}$  $\Gamma_a \propto G_F^2 p T^4$ 

Stodolsky, PRD (1987)

$$V_{s}(p_{s}) = \frac{g_{s}^{2}}{8\pi^{2}p_{s}} \int p \, dp(f_{\phi} + f_{s}) \sim 10^{-1}g_{s}^{2}T_{s}$$
$$\Gamma_{s} = \frac{g_{s}^{4}}{4\pi T_{s}^{2}}n_{s}$$
$$V_{s} > V_{vacuum} \quad \text{until} \quad \frac{\Gamma_{a}}{H} > 1 \quad (\approx 1 \text{MeV})$$

# $\begin{array}{l} \mathsf{N}_{eff} \text{ at BBN} \\ \mathsf{BBN} \text{ bounds:} \\ \Delta \mathsf{N}_{eff} \leq 1 \ (95\% \ \text{c.l.}) \end{array} \xrightarrow[0.9]{0.8} \begin{array}{c} Archidiacono \ et \ al., \ PRD \ (2014) \\ \hline \mathsf{SBN} \ \mathsf{Sin}^2 \ 2\theta \ _s = 0.05 \\ m \ _s = 1 \ eV \end{array}$

When sterile neutrinos are produced, they will create non-thermal distortions in the sterile neutrino distribution, and the sterile neutrino spectrum end up being somewhat non-thermal.

 $m_s = 1 eV$ 0.7 0.6 ي م 2 0.5 0.4 0.3 0.2 0.1 LASAGNA code 0└── 10<sup>─6</sup> 10<sup>-5</sup> g<sub>s</sub> The transition between full thermalization and no thermalization occurs for coupling

 $10^{-6} < g_s < 10^{-5}$ 

## $N_{\rm eff}\,at\,CMB$

The  $v_s - \phi$  fluid becomes strongly interacting before neutrinos go non-relativistic around recombination.



#### $\Sigma m_{\!_{\rm V}} \, {\rm and} \, {\rm LSS}$

As soon as sterile neutrinos go non-relativistic, they start annihilating into pseudoscalars.



Archidiacono et al., JCAP (2015)

### $\Sigma m_{_{\rm V}} \, \text{and} \, \text{LSS}$

Sterile neutrinos disappear from the cosmic neutrino background. *Neutrinoless Universe, Beacom et al., PRL (2004)* 



If the mediator is a massive MeV vector boson, then the late time phenomenology is different.

Hannestad et al., PRL(2013); Bringmann et al., JCAP (2014); Mirizzi et al., PRD (2014); Chu, Dasgupta, Kopp, JCAP (2015)

### Galactic dynamics

Talk by Sebastian Wild No significant self-interaction expected from pseudoscalar exchange



The condition for having observable consequences on galactic dynamics is that the scattering time scale of DM self interactions is less than the age of the Universe.

Milky Way:

$$g_d \ge 6 \times 10^{-8} \left(\frac{m_{\chi}}{MeV}\right)^{9/4}$$

Bellazzini et al., PRD (2013) Ackerman et al., PRD (2009) It is just a lower bound It requires further investigation



Archidiacono et al., PRD (2014)

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	<i>✓</i>	1
SIDM + DR	1	1	1

DR = Sterile neutrinos

- Astrophysical observations
- SBL sterile neutrinos in cosmology (BBN, CMB & LSS)

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	1	1
SIDM + DR	1	1	1
WDM	1	×	1

Warm Dark Matter

Free-streaming length circa the size of a dwarf galaxy. Motivated by particle physics models of sterile neutrinos. Severely constrained by Ly- $\alpha$ .

> Viel et al., PRD (2013) Lovell et al., MNRAS (2014)

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	1	1
SIDM + DR	1	1	<i>✓</i>
WDM		×	1
DDM	1	×	1

#### **Decaying Dark Matter**

It is a natural way to generate a mixture of cold and warm dark matter that alters structure formation only in the late Universe, so it can evade constraints from Ly- $\alpha$  ( $\tau \sim H_0^{-1}$ ).

Wang et al., MNRAS (2014)

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	1	1
SIDM + DR	1	1	1
WDM	1	×	1
DDM	1	×	1
LFDM		×	1

#### Late Forming Dark Matter

Phase transition of a scalar field from radiation to matter (fuzzy dark matter is a form of LFDM). The earlier the phase transition, the smaller the power spectrum cutoff scale.

Agarwal et al., PRD (2015) Ultra Light Axions & Ly- $\alpha$ , Kobayashi et al., (2017)

	Missing satellites	Cusp vs. core	Too big to fail
Baryons	1	1	1
SIDM	×	<b>\</b>	1
SIDM + DR	1	1	1
WDM	1	×	1
DDM	1	×	1
LFDM	1	×	1
BSI	<i>✓</i>	1	×

Broken-Scale-Invariance inflationary model

The model predicts an excess of power wrt to  $\Lambda$ CDM before the cutoff; thus it is highly constrained by Ly- $\alpha$ .

Kamionkowski et al., PRL (2000)

#### Backup





Hou et al., PRD (2013)

#### Massive neutrinos & P(k)



Castorina et al., JCAP (2015)

#### Massive neutrinos & Halo profile



Brandbyge et al., JCAP (2010)

#### Massive neutrinos & HMF



#### CMB & annihilation cross section

$$\frac{dE}{dtdV}(z) = 2g\rho_{\rm crit}^2 c^2 \Omega_{\rm c}^2 (1+z)^6 p_{\rm ann}(z),$$

$$p_{\rm ann}(z) \equiv f(z) \frac{\langle \sigma v \rangle}{m_{\chi}},$$



#### **Flavour oscillations**

$$\sin^2 2\theta_m = \frac{\sin^2 2\theta_0}{\left(\cos 2\theta_0 + \frac{2E}{\Delta m^2} V_{\text{eff}}\right)^2 + \sin^2 2\theta_0}$$



#### **Collisional re-coupling**

$$\Gamma_{\text{coll}} = n_{\nu_s} \sigma \sim \begin{cases} n_{\nu_s} e_s^4 \frac{E^2}{M^4} & \text{for } T_s \ll M \\ n_{\nu_s} e_s^4 \frac{1}{E^2} & \text{for } T_s \gg M \end{cases} \qquad \Gamma_s \simeq \frac{1}{2} \sin^2 2\theta_m \times \frac{3}{4} n_{\nu_a}^{\text{SM}} \cdot \begin{cases} e_s^4 \frac{E^2}{M^4} & \text{for } T_s \ll M \\ e_s^4 \frac{1}{E^2} & \text{for } T_s \gg M \end{cases}$$



#### Neutrino PDF



Hannestad et al., PRL (2013)

#### DM-pseudoscalar

$$V(r) = -\frac{g_d^2}{m_\chi^2} \frac{e^{-m_\phi r}}{4\pi r^3} h(m_\phi r) \mathcal{S},$$

$$h(m_{\phi}, r) = 1 + m_{\phi}r + \frac{1}{3}(m_{\phi}r)^{2}$$

#### Sommerfeld & pseudoscalar

