

Warm Dark Matter and Epoch of Reionization

Laura Lopez Honorez



partially based on [arXiv:1703.02302](https://arxiv.org/abs/1703.02302)
in collaboration with O. Mena, A. Moline, S. Palomares-Ruiz,
P. Villanueva Domingo & A. C. Vincent.

SIDM workshop - Copenhagen

Λ CDM problems?

Problems of Cold Dark Matter (CDM) on galactic and sub galactic scales

- **Missing satellite:** [Kyplin'99, Moore'99] CDM fails to reproduce abundance and properties of low mass galaxies $M < 5 \times 10^9 M_{\odot}$ [Zavala'09, Papastergis'11, Kyplin'11]
- **Core-Cusp problem:** [DeBlock'97, Oh'11, Walker'11] CDM inner density of Galaxies have cusp $\propto r^{-\alpha}$ with $\alpha \simeq 1$ [NFW'96 etc]
- **Too big to fail:** [Boylan'11, Papastergis'15] host of dwarf galaxies are too massive to account for the galactic rotation curves ($V_{rot}(r)$ too large)

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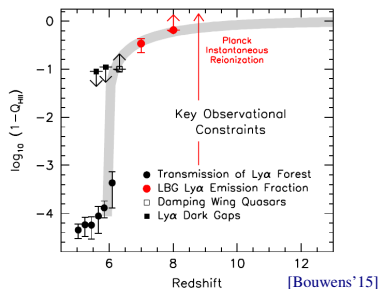
Solutions?

- within Λ CDM: baryonic physics (SN feedback, etc) see Pontzen's talk!
- Beyond Λ CDM \rightsquigarrow suppress structure formation at small scales:
 - **(S)IDM?** see [Boehm'00+, Cyr-Racine'12+, Bringman'12+, Buckley'14, etc] and also Yo, Valli, ... talk!
 - WDM?

Epoch of Reionization and WDM

IN THIS TALK:

- WDM free streaming
 \rightsquigarrow effect on EoR?
- constraints from $\text{Ly}\alpha$ emission, Gunn Peterson effect, and Planck optical depth

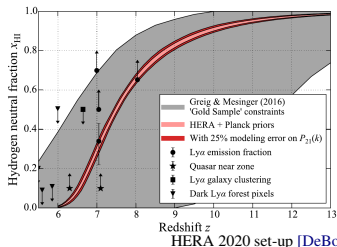
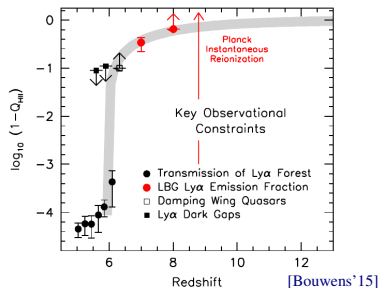


Epoch of Reionization and WDM

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Notice that understanding of EoR is expected to improve with (near) future cosmo probe \equiv 21cm signal



WDM description

WDM free-streaming: linear regime

At early time collisionless particles can stream out of overdense to underdense regions

- smooth out inhomogeneities for $\lambda < \lambda_{FS} = \int_0^{t_0} \frac{v}{a} dt$
 \rightsquigarrow particles relativistic at the time of decoupling can give substantial λ_{FS}

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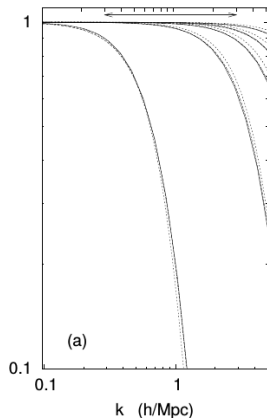
- Assuming thermal WDM [Viel'05]

$$\begin{aligned} T_{\text{WDM}}(k) &= (P_{\text{WDM}}(k)/P_{\text{CDM}}(k))^{1/2} \\ &= (1 + (\alpha k)^{2\nu})^{-5/\nu} \end{aligned}$$

with $\nu = 1.12$ and the breaking scale:

$$\alpha = 0.049 \left(\frac{\text{keV}}{m_X} \right)^{1.11} \left(\frac{\Omega_X}{0.25} \right)^{0.11} \left(\frac{h}{0.7} \right)^{1.22} \text{ Mpc}/h$$

\rightsquigarrow WDM suppress power at small scales (large k)

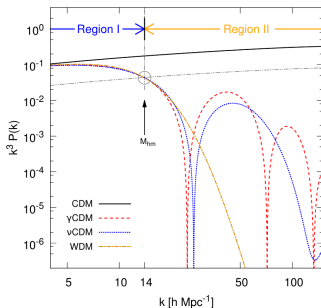


[Viel'05]

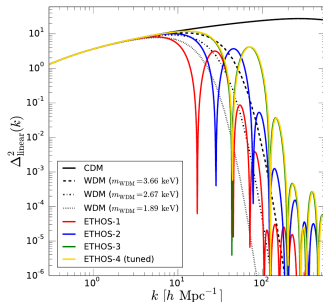
(S)IDM collisional Damping: linear regime

For dark matter interacting with (dark) relativistic degrees of freedom:

see also Zavala, Cyr-Racine, etc talks



[Schewtschenko'14]



[Vogelsberger'15]

Towards generalized fit to non-CDM (SIDM included)? [Murgia'17]

$$T(k) = (1 + (\alpha k)^\beta)^\gamma \rightarrow \text{might be useful enough to derive Ly}\alpha \text{ forest and MW satellite count constraints}$$

WDM: non linear regime

At low redshifts, DM perturbations in the non linear regime

↔ use **Press-Schechter (PS) formalism** [PS'74, Bond'91] to match N-body simu.:

$$\frac{dn(M, z)}{dM} = \frac{\rho_{m,0}}{M^2} \frac{d \ln \sigma^{-1}}{d \ln M} f(\sigma)$$

- $f(\sigma)$ represents the fraction of mass collapsed into halos.

For WDM we use Sheth & Tormen [ST'99+].

- $\sigma^2 = \sigma^2(P_{lin}(k), W(kR))$ is the variance of **linear** perturb. smoothed over the radius $R(\leftrightarrow M)$ using a window fn. W .

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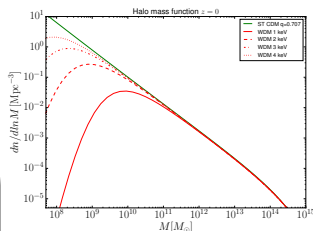
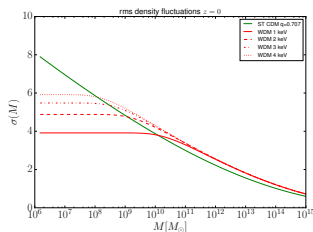
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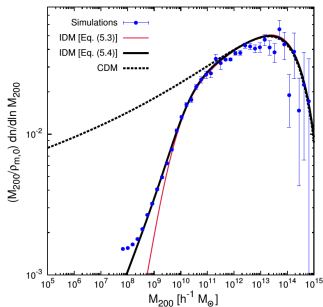
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- for WDM, $\sigma(M)$ cst. at low mass accounts for free-streaming effects [Benson'13, Schneider'13]

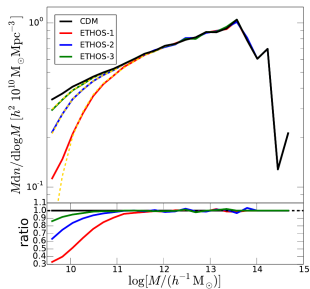
↪ **suppression of the halo mass function at low masses for WDM**



(S)IDM: non-linear regime



[Moline'16]



[VogelsBerger'15]

WDM solution to CDM problems?

- WDM can potentially provide partial solutions but strongly challenged by Ly α forest constr.
 $\rightsquigarrow m_X > 4.65$ keV (at 95%CL)

[Yèche 17] see also [Viel'13, Baur'15, Irsik 17]

all constraints from SDSS Ly- α QSO spectra BUT depends on T_{IGM} description!
 HiRes \rightsquigarrow good fit $m_X \simeq 2\text{-}3$ keV [Garzilli'13], max lik. $m_{\nu_s}^p \simeq 8$ keV [Baur'17]

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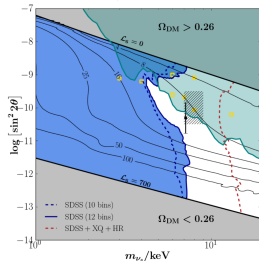
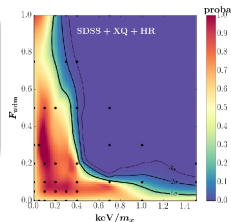
- Similar effects/constraints for Mixed DM, sterile neutrinos (non) resonantly produced, etc

Some Ly- α forest constraints [Baur 17] :

$m_X > 3.2$ keV for $F_{w\text{dm}} > 80\%$ (at 95%CL)

$m_{\nu_s}^{\text{TP}} > 3.5$ keV (3σ)

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WDM and reionization

WDM imprint on Reionization

similar to [Sitwell'14, Bose'16] and for different approach [Yue'12, Barkana'01, Somerville'03, Yoshida'03, Schultz'14, Dayal '14+, Rudakovskiy'16]

- Ionization level at $z \sim z_{reio}$:

$$\bar{x}_i \approx \zeta_{UV} f_{coll} \text{ with } f_{coll} = f_{coll}(> M_{vir}^{\min}) = \int_{M_{vir}^{\min}} \frac{M}{\rho_{m,0}} \frac{dn}{dM} dM .$$

- Optical depth to reionization:

$$\tau = \sigma_T \int \bar{x}_i n_b dl \text{ and Planck: } \tau = 0.055 \pm 0.009 \text{ [Aghanim'16]}$$

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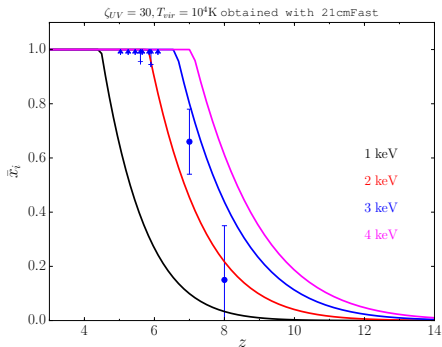
$$\tau = \sigma_T \int \bar{x}_i n_b dl \text{ and Planck: } \tau = 0.055 \pm 0.009 \text{ [Aghanim'16]}$$

Within our framework:

low m_χ suppress structure formation
at small scales

↪ reduces \bar{x}_i

↪ **WDM can delay reionization**



Astro parameters and Reionization

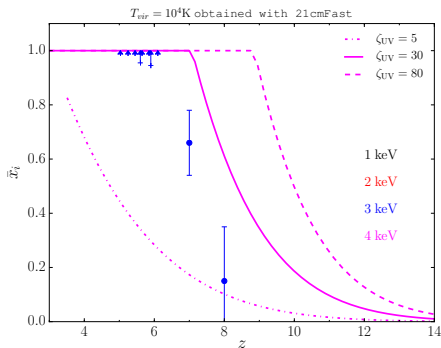
- Ionization efficiency:

$$\zeta_{UV} \propto f_{esc} N_{\gamma} / b f_{\star}$$

Regions ionized when

$$\zeta_{UV} f_{coll} > 1$$

↪ lower ζ_{UV} has similar effect
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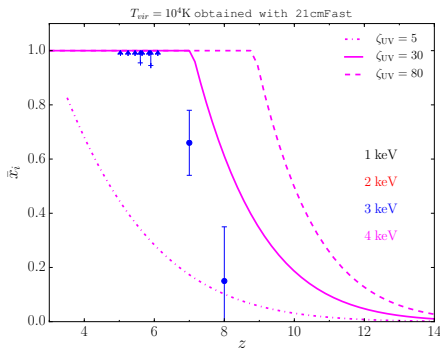
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- Threshold for halos hosting star-forming galaxies:

$$f_{coll}(> M_{vir}^{min}) = \int_{M_{vir}^{min}} \frac{M}{\rho_{m,0}} \frac{dn}{dM} dM$$

$$M_{vir}^{min}(z) \simeq 10^8 \left(\frac{T_{vir}^{min}}{2 \times 10^4 \text{ K}} \right)^{3/2} \left(\frac{1+z}{10} \right)^{-3/2} M_{\odot} \rightsquigarrow \text{larger } T_{vir}^{min} \text{ delays the reionization}$$



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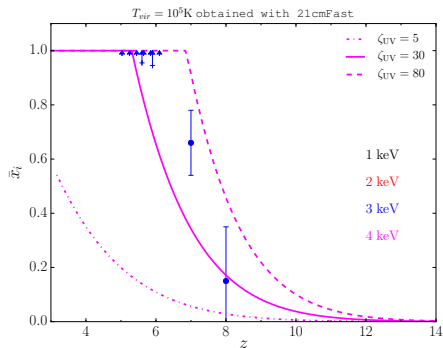
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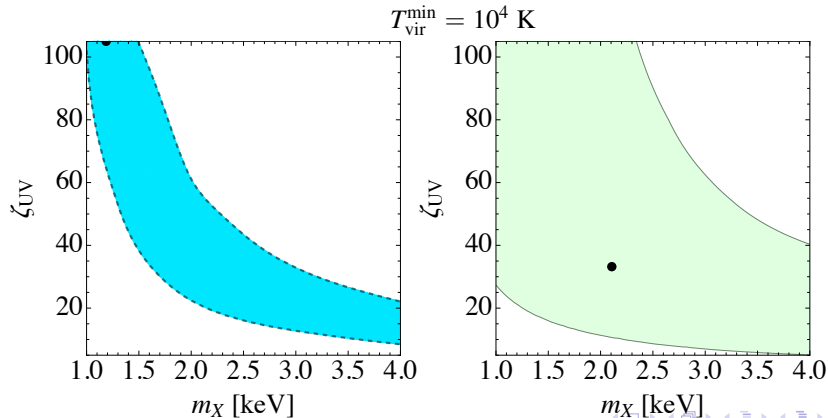


Important **degeneracies** between astro $\{\zeta_{UV}, T_{vir}^{min}\}$ and WDM effects

Degeneracies

Allowed regions at 90% CL for \bar{x}_i and τ data:

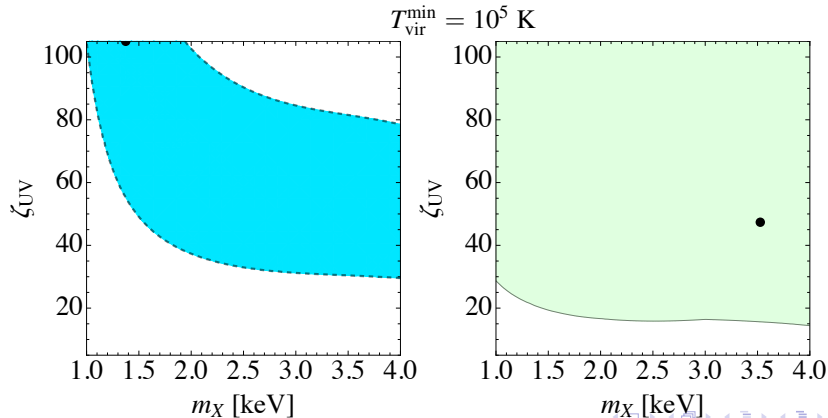
- One can compensate larger ζ_{UV} with smaller m_X



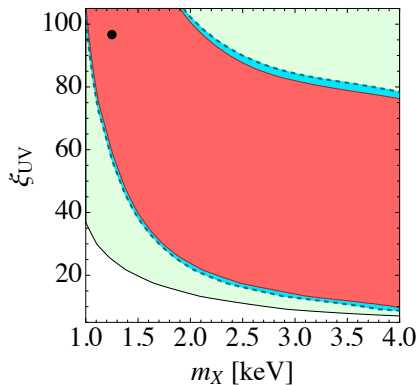
Degeneracies

Allowed regions at 90% CL for \bar{x}_i and τ data:

- One can compensate larger ζ_{UV} with smaller m_X
- Larger $T_{\text{vir}}^{\text{min}}$ shifts contours to larger ζ_{UV}



Final contours

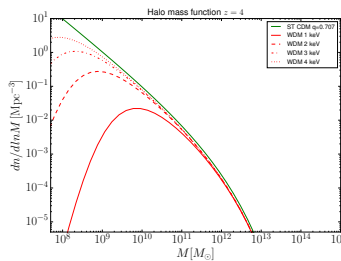


BUT constraints on T_{IGM} should provide a lower bound on m_X

Caveats

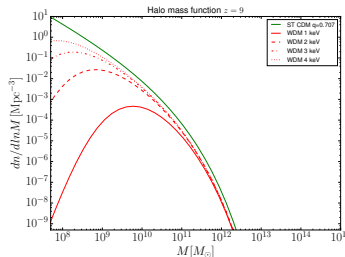
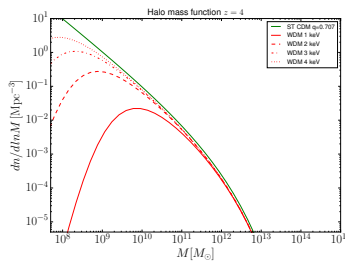
- **HMF considered validated until $z = 5$ only** see e.g. [Schneider'14] \rightsquigarrow needs Hydro-simu to larger z
- What about if $\zeta = \zeta_{UV}(z)$? \rightsquigarrow even $\zeta_{UV}(z)$ such that $x_i(z)^{WDM} = x_i(z)^{CDM}$ might be discriminated but needs good knowledge of ζ_{UV} using e.g. P_{21} [Sitwell'13]
- **SN feedback** \rightsquigarrow eject cold gas from galaxies, can inhibit ionizing γ production
see e.g. for WDM+SNfb [Bose'16]
- We assume $\zeta_{UV} \propto 1/(1 + n_{rec})$ BUT the lack of minihaloes in **WDM could suppress the average number of recombination/H atom** \rightsquigarrow some WDM could even get earlier reionization than CDM

see e.g. [Barkana'01, Somerville'03, Yoshida'03, Yue'12, Schultz'14, Dayal '14+, Rudakovskiy'16]

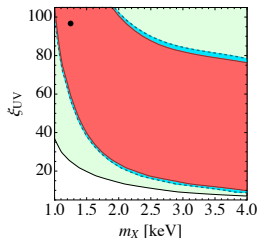


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Conclusion: WDM and EoR?



- Non-cold dark matter can suppress small scale structure formation
 \rightsquigarrow can delay reionization
- Parametrizing reionization as a function of a reduced set of parameters mainly ζ_{UV} , T_{vir}^{min} , m_X , we observed strong degeneracies to agree with the data \rightsquigarrow smaller $m_X \Leftrightarrow$ larger ζ_{UV} and smaller T_{vir} .

Within this framework the entire range of tested m_X is compatible with reionization and Planck data if one is allowed to consider ζ_{UV} up to 100.

Thank you for your attention

Backup

Top hat versus sharp k cutoff scale for γ CDM

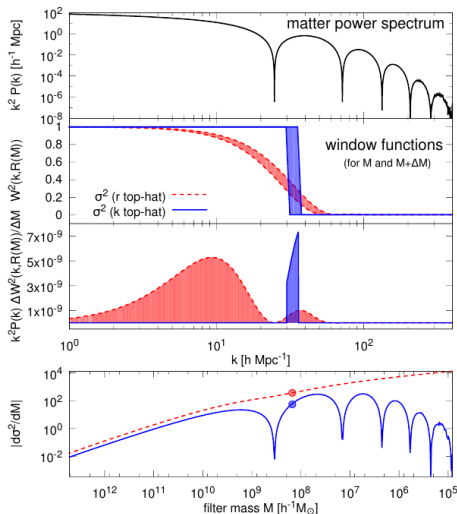


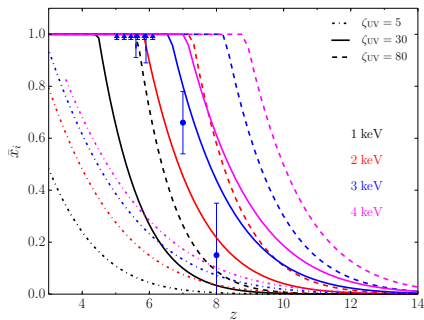
Figure 4. Real-space and k -space top-hat functions in Press-Schechter HMF predictions for γ CDM. The upper panel shows the matter power spectrum, while the second panel shows the Fourier transform of the two window functions (r top-hat and k top-hat). Each window function is evaluated for two filter masses, M and $M + \Delta M$. The difference between the two filter masses is highlighted by the shaded region in each case. The third panel shows the result of applying this differential filter to the matter distribution. Finally, the lower panel shows the integrated result for both window functions. The red and blue points are the results for the specific filter mass M used in the middle two panels.

\rightsquigarrow with r -top hat filter (TH) a large number of un-suppressed small k scales contribute to $\sigma(M)$

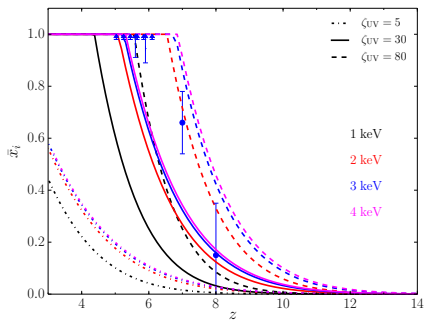
\rightsquigarrow not good to describe $\sigma(M)$ for suppressed $P(k)$ including WDM

WDM imprint on ionized fraction

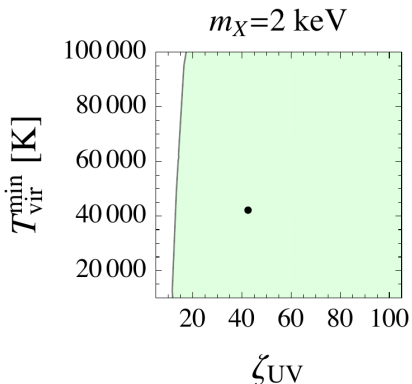
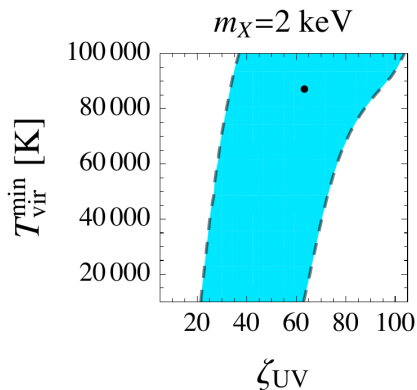
$$T_{vir}^{min} = 10^4 \text{K}$$



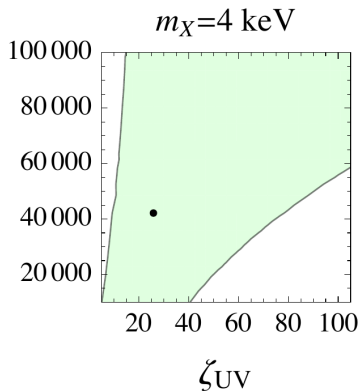
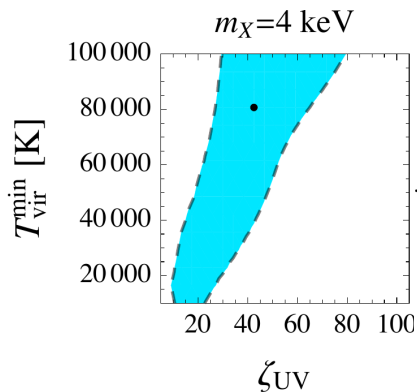
$$T_{vir}^{min} = 10^5 \text{K}$$



Fixed WDM mass and full contours

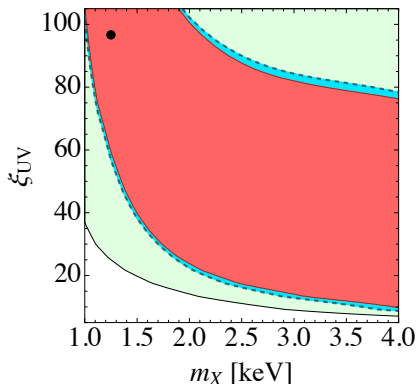


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Fixed WDM mass and full contours

- All together best fit at 1.25 keV, $\zeta_{UV} = 96.6$



BUT constraints on T_{IGM} should provide a lower bound on m_X

Characterization of the 21cm signal

The observed brightness of a patch of HI relative to the CMB at $\nu = \nu_0/(1+z)$ is associated to the differential brightness temperature δT_b :

$$\delta T_b(\nu) \simeq 27 x_{\text{HI}} (1 + \delta_b) \left(1 - \frac{T_{\text{CMB}}}{T_S}\right) \left(\frac{1}{1 + H^{-1} \partial v_r / \partial r}\right) \left(\frac{1+z}{10}\right)^{1/2} \left(\frac{0.15}{\Omega_m h^2}\right)^{1/2} \left(\frac{\Omega_b h^2}{0.023}\right) \text{ mK}$$

Fraction of neutral H

Spin temperature= excitation T of 21cm line

T_S characterises the relative occupancy of the 2 HI ground state energy levels:
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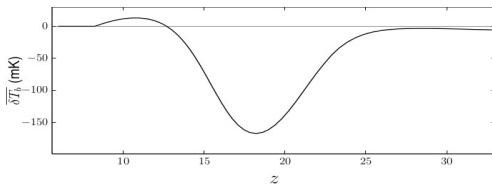
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- **Atomic collisions** with H, p or e^- (when IGM is dense, dark ages)
- **Scattering of Ly α photons** \equiv Wouthuysen-Field (WF) effect
 (once early radiation sources light on)
 \rightsquigarrow **IGM is seen in absorption or emission** compared to CMB
 i.e. when $T_K \neq T_{\text{CMB}}$ and some mechanism couples T_K to T_S

$$\delta T_b(\nu) \simeq 27 x_{\text{HI}} (1 + \delta_b) \left(1 - \frac{T_{\text{CMB}}}{T_S}\right) \left(\frac{1}{1 + H^{-1} \partial v_r / \partial r}\right) \left(\frac{1+z}{10}\right)^{1/2} \left(\frac{0.15}{\Omega_m h^2}\right)^{1/2} \left(\frac{\Omega_b h^2}{0.023}\right) \text{ mK}$$

Fraction of neutral H

Spin temperature= excitation T of 21cm line

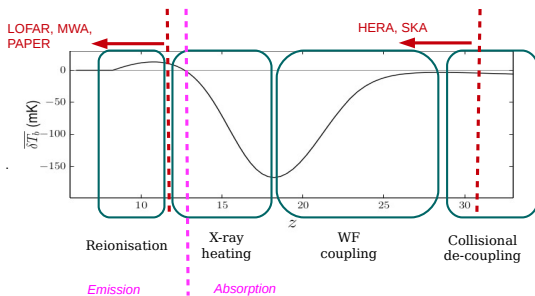


δT_b and Δ_{21} obtained using 21cm Fast [Mesinger'10]

$$\delta T_b(\nu) \simeq 27 x_{\text{HI}} (1 + \delta_b) \left(1 - \frac{T_{\text{CMB}}}{T_S}\right) \left(\frac{1}{1 + H^{-1} \partial v_r / \partial r}\right) \left(\frac{1+z}{10}\right)^{1/2} \left(\frac{0.15}{\Omega_m h^2}\right)^{1/2} \left(\frac{\Omega_b h^2}{0.023}\right) \text{mK}$$

Fraction of neutral H

Spin temperature= excitation T of 21cm line

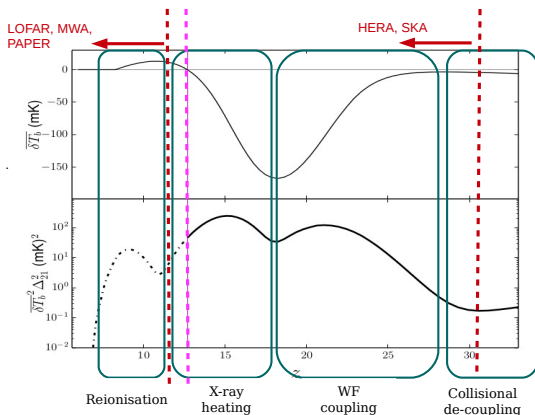


δT_b and Δ_{21} obtained using 21cm Fast [Mesinger'10]

$$\delta T_b(\nu) \simeq 27 x_{\text{HI}} (1 + \delta_b) \left(1 - \frac{T_{\text{CMB}}}{T_S}\right) \left(\frac{1}{1 + H^{-1} \partial v_r / \partial r}\right) \left(\frac{1+z}{10}\right)^{1/2} \left(\frac{0.15}{\Omega_m h^2}\right)^{1/2} \left(\frac{\Omega_b h^2}{0.023}\right) \text{mK}$$

Fraction of neutral H

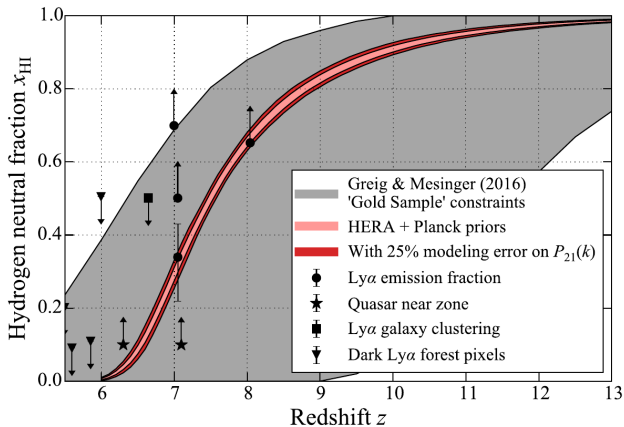
Spin temperature = excitation T of 21cm line



$$\langle \tilde{\delta}_{21}(\mathbf{k}, z) \tilde{\delta}_{21}^*(\mathbf{k}', z) \rangle \equiv (2\pi)^3 \delta^D(\mathbf{k} - \mathbf{k}') P_{21}(k, z) \quad \Delta_{21}^2(k, z) = \frac{k^3}{2\pi^2} P_{21}(k, z)$$

$$\tilde{\delta}_{21}(\mathbf{x}, z) = \delta T_b(\mathbf{x}, z) / \overline{\delta T_b}(z) - 1$$

δT_b and Δ_{21} obtained using 21cm Fast [Mesinger'10]

HERA reach on x_{HI} 

[De Boer'16]

Current constraints on EoR $\delta T_b^2 \Delta_{21}$

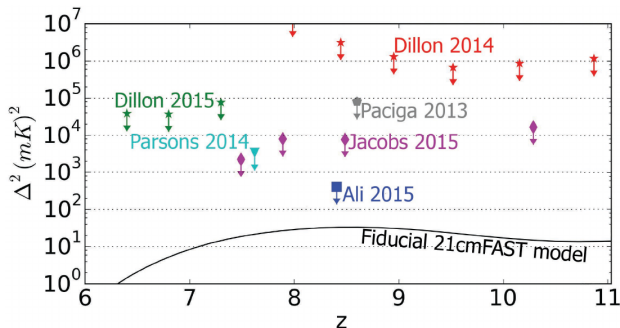


Figure 9. The current best published 2σ upper limits on the 21cm power spectrum, $\Delta^2(k)$, compared to a 21cmFAST-generated model at $k = 0.2 h \text{ Mpc}^{-1}$. Analysis is still underway on PAPER and MWA observations that approach their projected full sensitivities; HERA can deliver sub- mK^2 sensitivities.

[De Boer'16]

Current and future reach on $\delta T_b^2 \Delta_{21}$

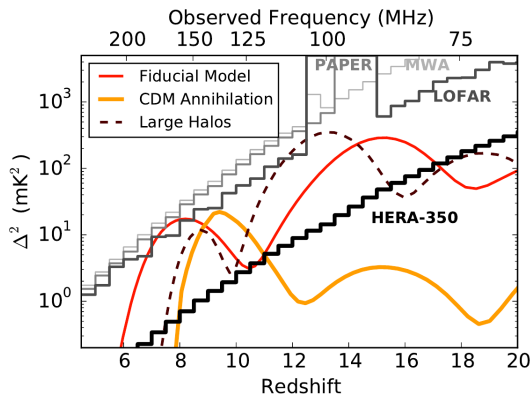


Figure 4. 1σ thermal noise errors on $\Delta^2(k)$, the 21 cm power spectrum, at $k=0.2 h \text{ Mpc}^{-1}$ (the dominant error at that k) with 1080 hours of integration (black) compared with various heating and reionization models (colored). Sensitiv-

[De Boer'16]

Resonant scattering of Ly α photons

Cause spin flip transitions

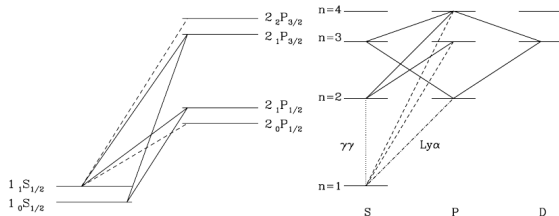


Figure 2. *Left panel:* Hyperfine structure of the hydrogen atom and the transitions relevant for the Wouthuysen-Field effect [24]. Solid line transitions allow spin flips, while dashed transitions are allowed but do not contribute to spin flips. *Right panel:* Illustration of how atomic cascades convert Ly n photons into Ly α photons.

[Pritchard'11]

title

This is really the end