

REVISITING THE LOWER BOUND ON FERMIONIC DM MASS FROM DSPHS

Fabrizio Nesti

Trieste University & INFN Trieste
(Ruđer Bošković Institute, Zagreb)

Phase space mass bound for fermionic dark matter from dwarf spheroidal galaxies

Chiara Di Paolo,^{1,*} Fabrizio Nesti,^{2,3,†} and Francesco L. Villante^{4,5,‡}

¹*SISSA/ISAS, Via Bonomea 265, 34136 Trieste, Italy*

²*Dipartimento di Fisica, Theoretical section, Università di Trieste, Strada Costiera 11, I-34151 Trieste, Italy*

³*Ruđer Bošković Institute, Division of Theoretical Physics, Bijenička cesta 54, 10000, Zagreb, Croatia*

⁴*Dipartimento di Scienze Fisiche e Chimiche, Università dell'Aquila, via Vetoio SNC, I-67100, L'Aquila, Italy*

⁵*INFN-LNGS, Via G. Acitelli 22, 67100, Assergi (L'Aquila), Italy*

We reconsider the lower bound on the mass of a fermionic dark matter (DM) candidate resulting from the existence of known small Dwarf Spheroidal galaxies, in the hypothesis that their DM halo is constituted by degenerate fermions, with phase-space density limited by the Pauli exclusion

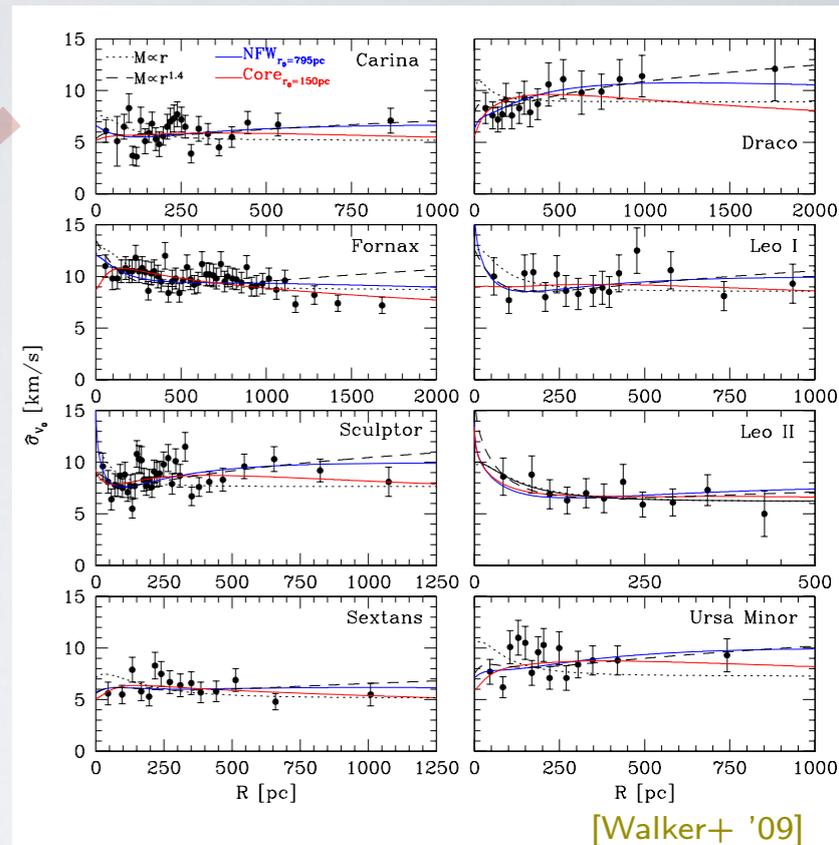
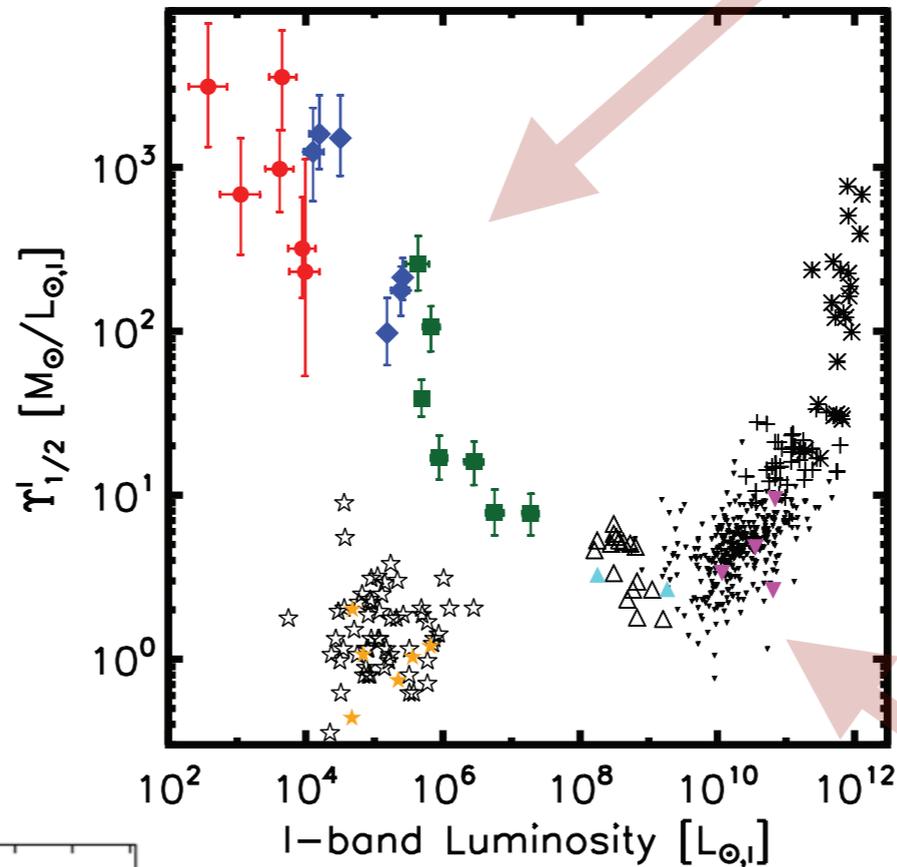
[arXiv:1704.06644]

Self-Interacting Dark Matter workshop — NBI, August 4th, 2017

REDUNDANT SLIDE

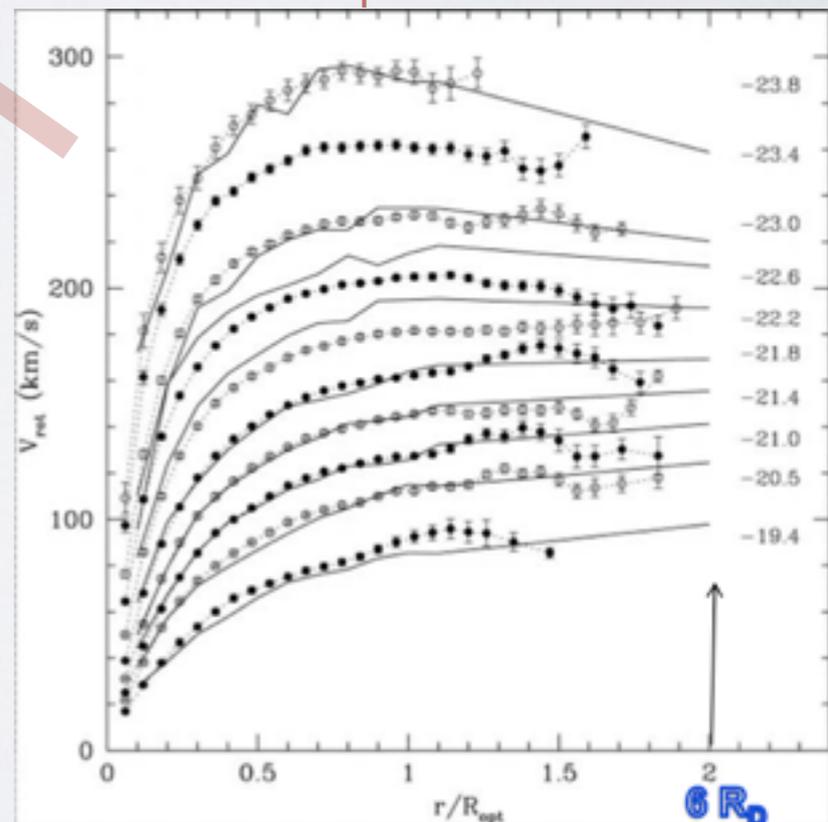
Dwarf Spheroidals

- Mass-to-Light ratio striking evidence of DM
- (Globular Clusters likely rule out modifications of gravity for DM)
- Cored profile preferred for small galaxies... ?



[Walker+ '09]

Spirals

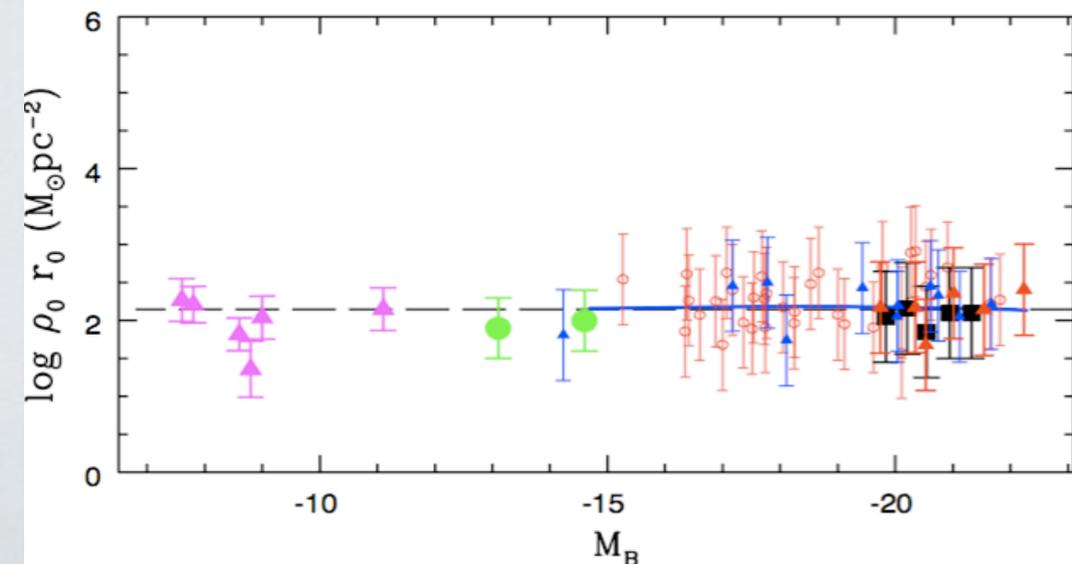


Fits with Burkert:

Constant surface density

$$\leftarrow \Sigma_0 = \rho_0 r_0 \simeq 120 M_{\odot}/pc^2$$

(over many magnitudes !?)



HYPOTHESIS OF DEGENERATE FERMIONS IN DARK MATTER HALOS

- Pauli exclusion can forbid a central density cusp
...can explain cored profiles

The largest density is observed in smallest systems, so
need to focus on the smallest dwarf galaxies

Dwarf galaxies, dark matter dominated, would be
quantum degenerate spheres of fermi particles (10^{70} of them)

The particle mass is bounded from below, *à la* Tremaine-Gunn

[Tremaine-Gunn '79, ... Gerhard-Spergel '92, ..., Chavanis+ '97, Bilić+ '99,
Boyarski+ '09..., Destri DeVega Sanchez '13; Domcke-Urbano '15]

AUTO GRAVITATING FERMION GAS

Spherical symmetry, isothermal. $\phi(r)$: average gravitational potential

Fermi Dirac Statistics:

$$\rho(r) = mn(r) = \frac{gm}{2\pi^2\hbar^3} \int_0^\infty p^2 dp f \left[\frac{p^2}{2m} - \mu(r) \right]$$

$$f_{FD}(E) = \frac{1}{1 + \exp(E/T_0)}$$

Poisson equation

$$\begin{cases} \frac{d\phi(r)}{dr} = G \frac{M(r)}{r^2} \\ \frac{dM(r)}{dr} = 4\pi r^2 \rho(r) \end{cases}$$

r -dependent chemical potential:

$$\mu(r) = \mu_0 - m\phi(r)$$

Thomas-Fermi Equation

$$\frac{d^2\mu}{dr^2} + \frac{2}{r} \frac{d\mu}{dr} = -4\pi Gm\rho(r) = -\frac{2gGm^2}{\pi\hbar^3} \int_0^\infty dp p^2 f \left[\frac{p^2}{2m} - \mu(r) \right]$$

$$\text{b.c.} \begin{cases} \frac{d\mu}{dr}(0) = 0 \\ \mu(0) \text{ free parameter: degeneracy at origin} \end{cases}$$

THOMAS FERMI - DIMENSIONLESS

$$r = l_0 \xi \quad , \quad \mu(r) = T_0 \nu(\xi) \quad y = p / \sqrt{2mT_0}$$

$$l_0 = \frac{\hbar}{\sqrt{8G}} \left(\frac{2}{g}\right)^{\frac{1}{3}} \left[\frac{9\pi I_2(\nu_0)}{m^8 \rho_0}\right]^{\frac{1}{6}} = R_0 \left(\frac{2 \text{ keV}}{m}\right)^{\frac{4}{3}} \left(\frac{2}{g}\right)^{\frac{1}{3}} \left[\frac{I_2(\nu_0) M_\odot}{\rho_0 \text{ pc}^3}\right]^{\frac{1}{6}} \quad R_0 = 7.425 \text{ pc}$$

$$\frac{d^2 \nu}{d\xi^2} + \frac{2}{\xi} \frac{d\nu}{d\xi} = -I_2(\nu) \quad I_2(\nu) = 3 \int_0^\infty y^2 dy \Psi(y^2 - \nu)$$

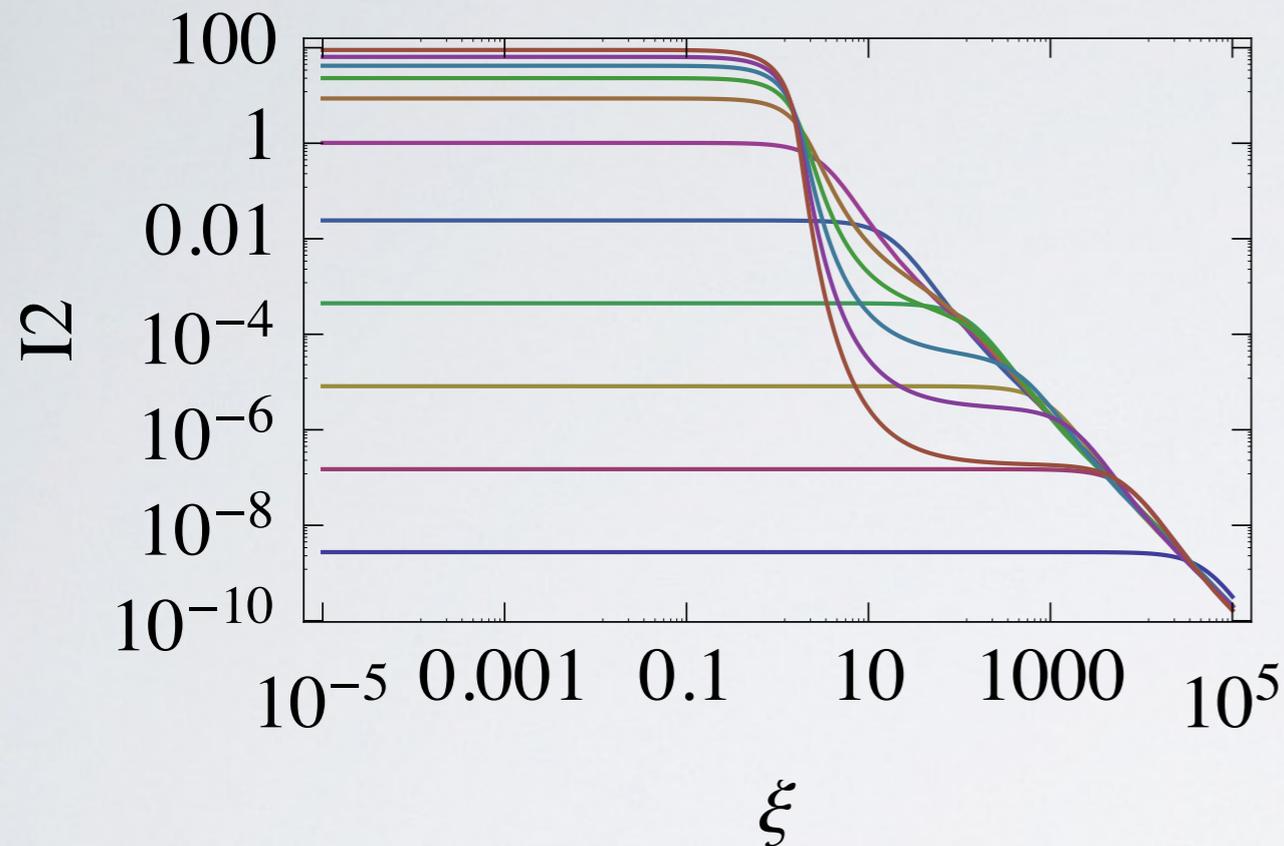
$$\text{b.c.} \quad \begin{cases} \nu'(0) = 0 \\ \nu_0 \text{ only one free parameter} \end{cases}$$

determines the dimensionless potential $\nu(\xi)$

...and all solutions are just rescalings.

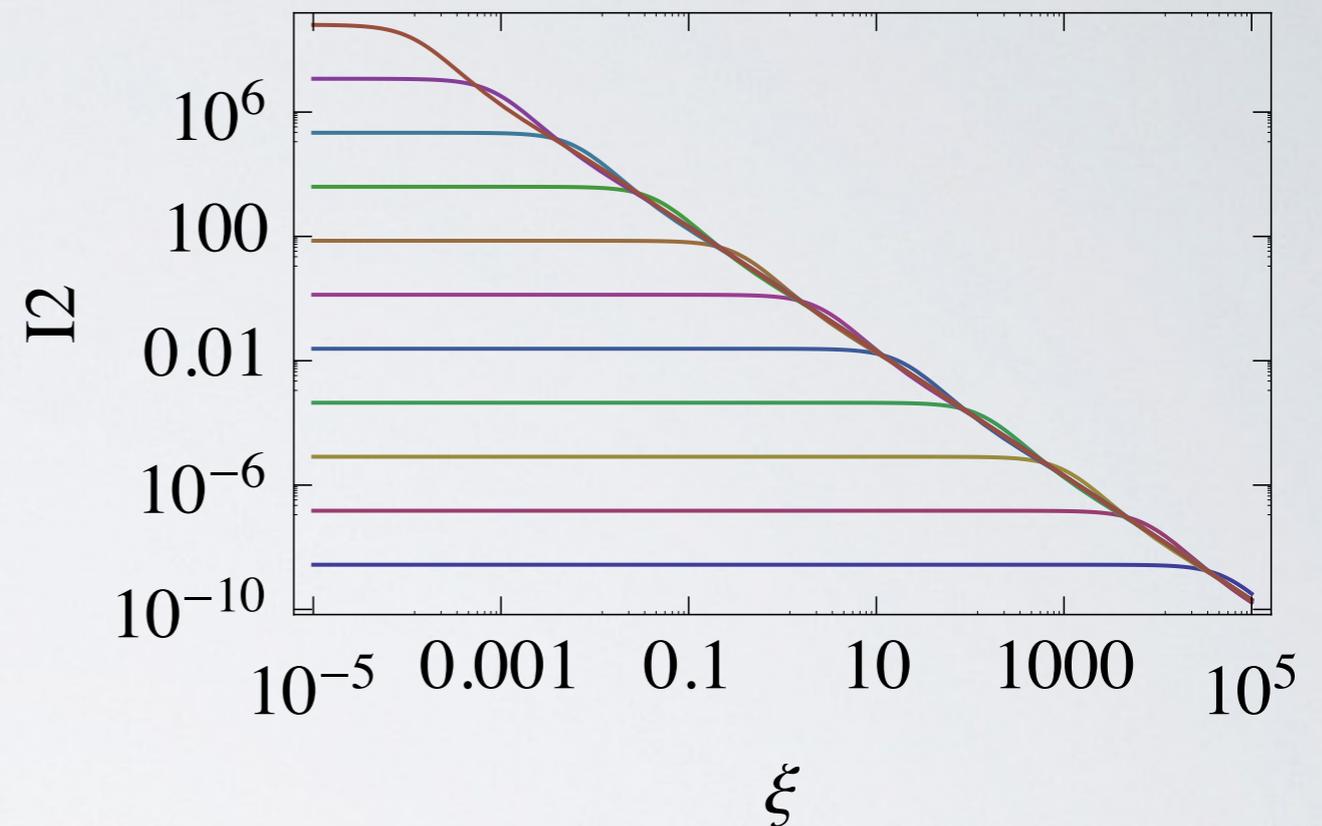
MASS DENSITY PROFILE $\rho(r) \sim I_2(\xi)$

Fermi-Dirac



core for high density

Maxwell-Boltzmann



cusp for high density

Fermi-Dirac



Double feature:
degenerate core plus **isothermal tail**

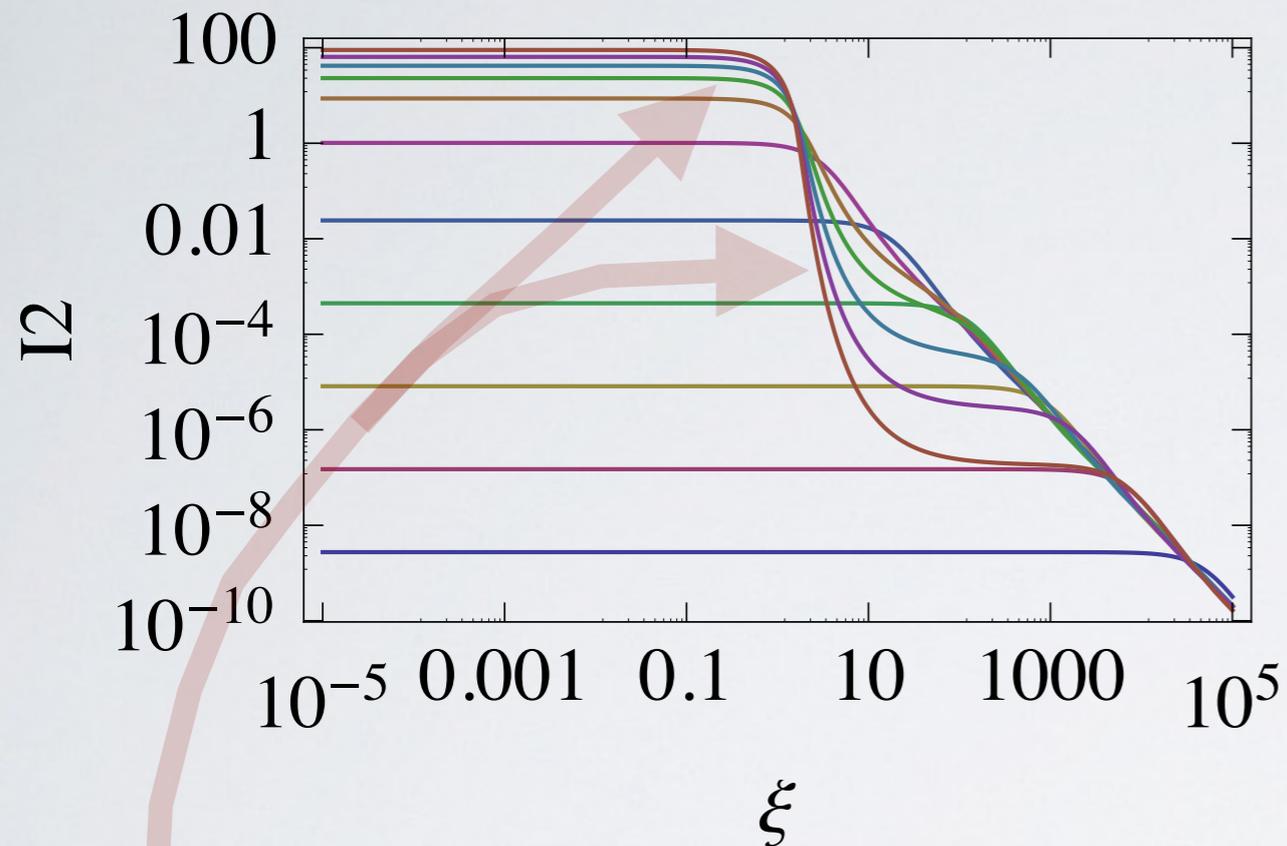
Max-Boltzmann



Classical isothermal halo

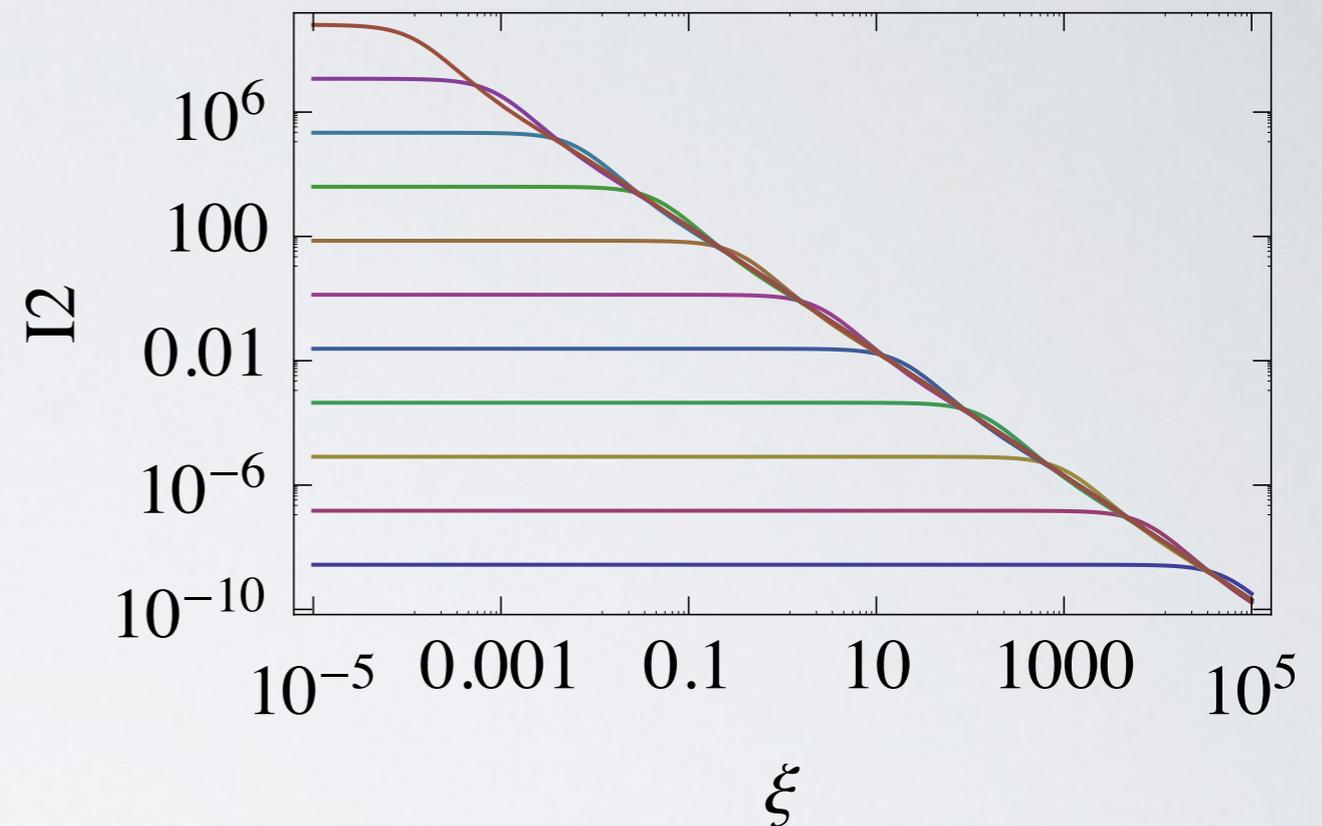
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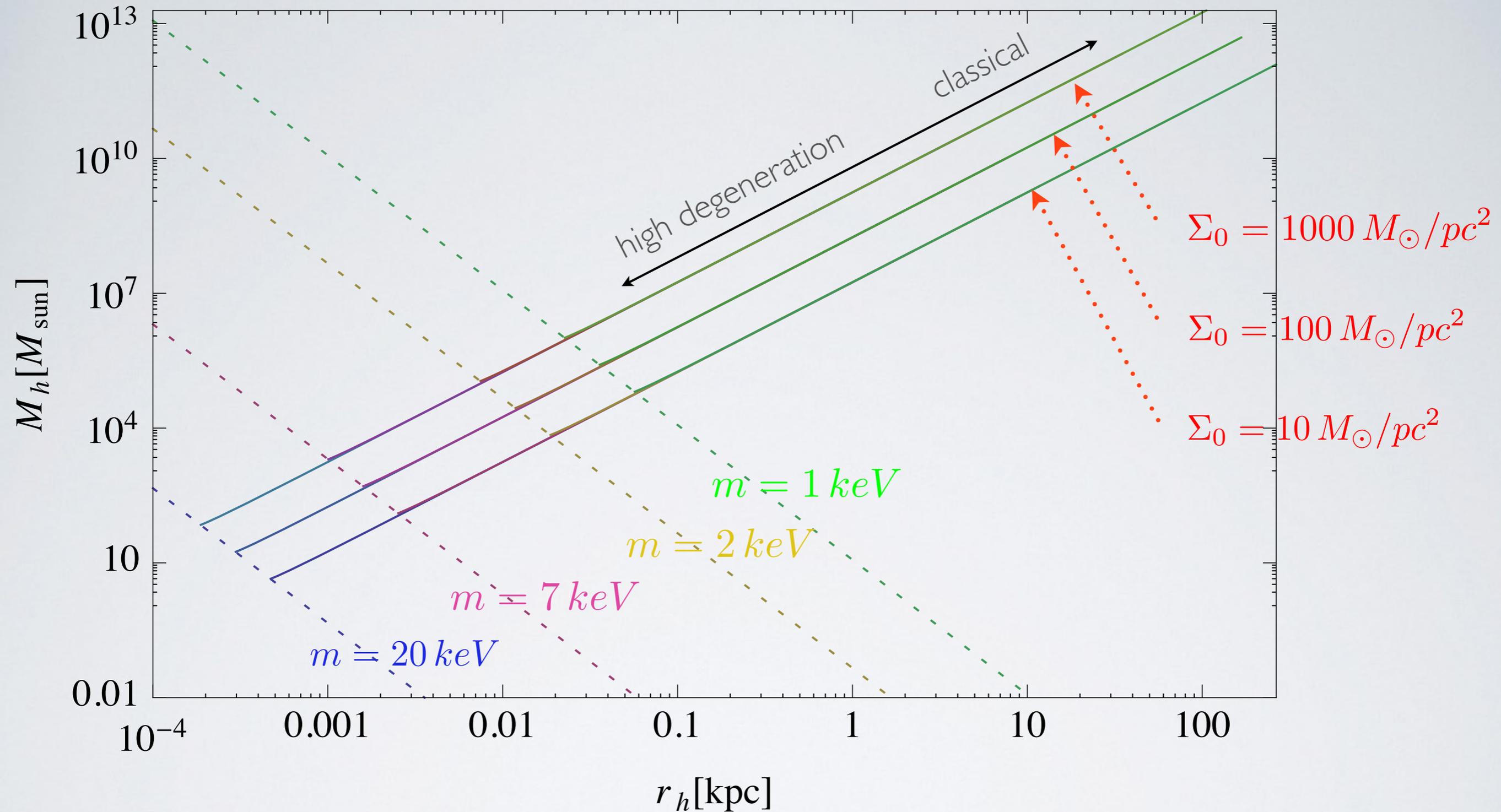
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▶ Double feature:
degenerate core plus isothermal tail

Max-Boltzmann

▶ Classical isothermal halo

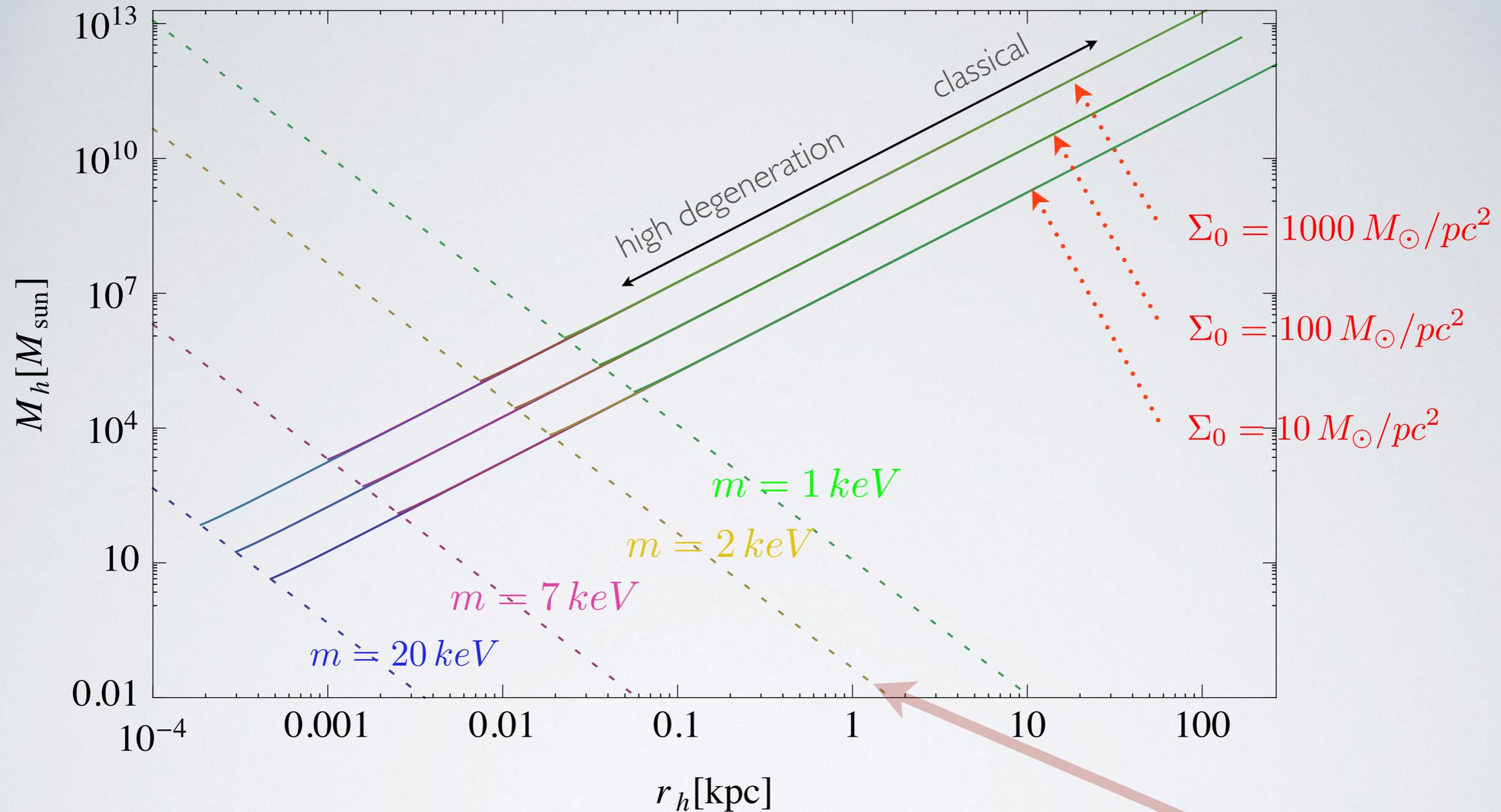


There are lower limits for degenerate:

$r_{h, \text{min}}$

$M_{h, \text{min}}$

...a minimal galaxy, for given mass m



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$r_{h, \text{min}}$ $M_{h, \text{min}}$

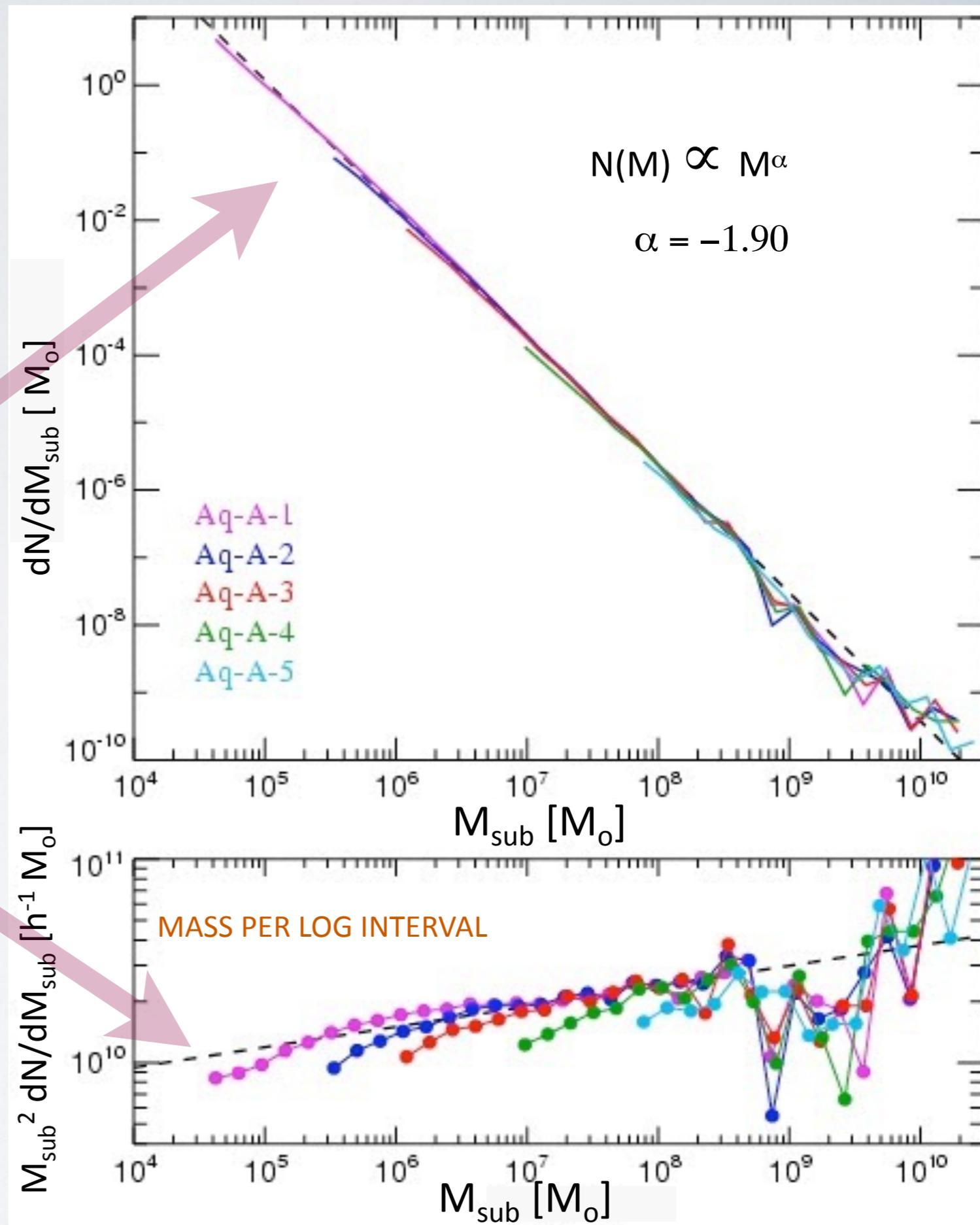
...a minimal galaxy, for given mass m

CUT THE SMALL-SCALE EXTRA SATELLITES OF CDM ?

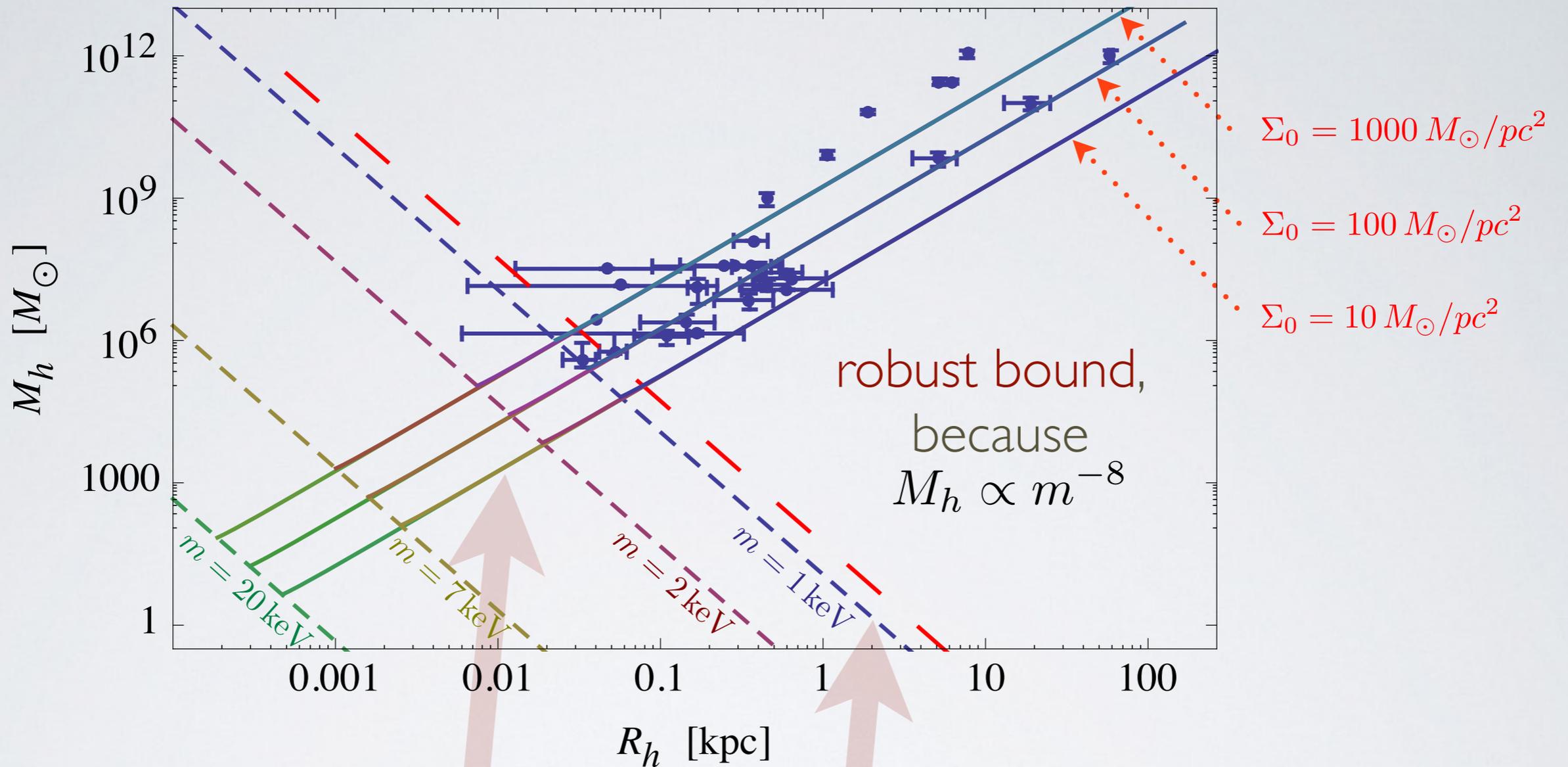
unseen low masses

Dramatic slope,
if extrapolated
to low masses

[Springel+ '08]



SO : LOWER+UPPER LIMIT ON m ?



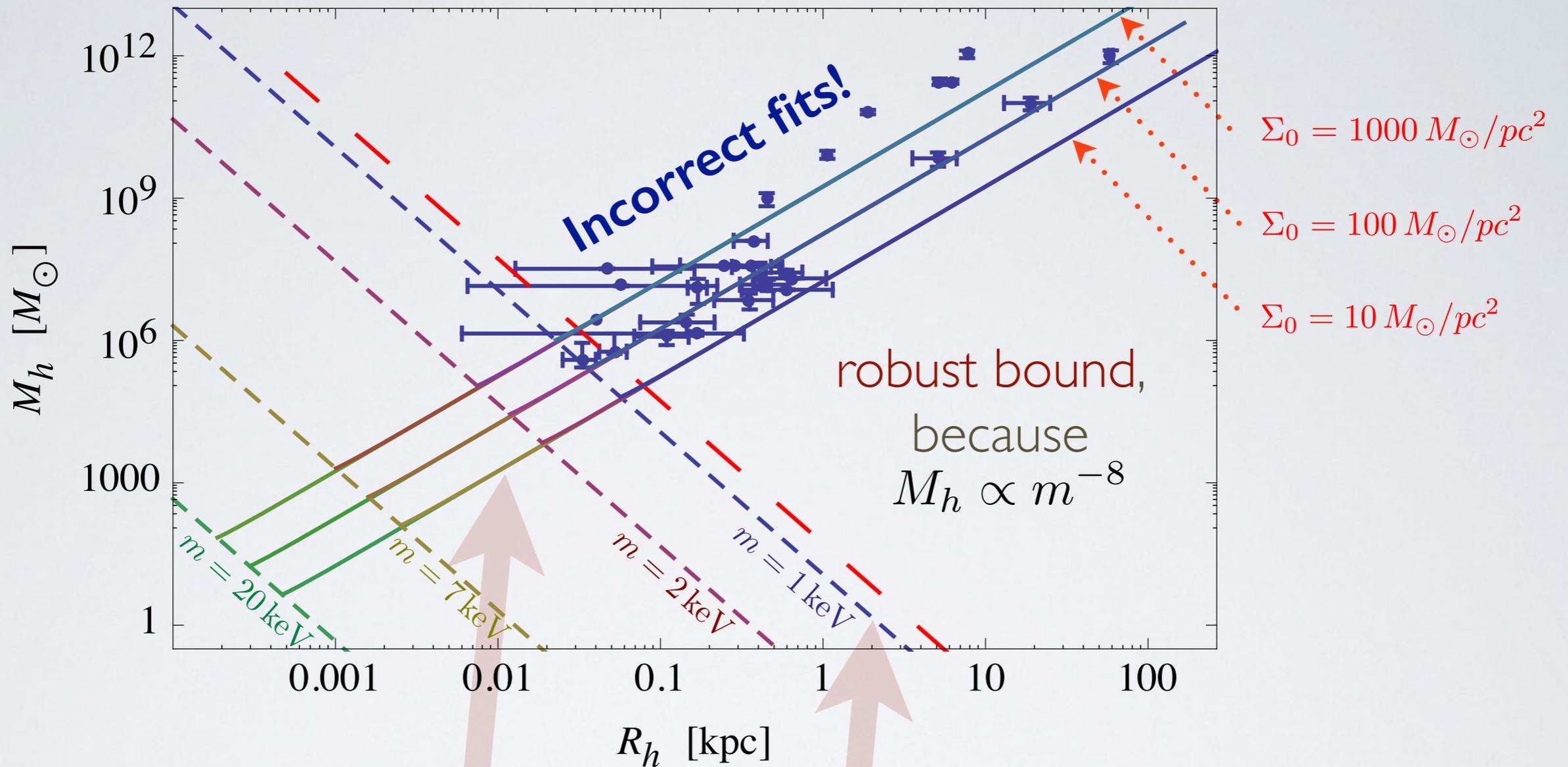
$$M_h \sim \frac{\hbar^6}{G^3 m^8} \frac{1}{r_h^3}$$

Degeneration limit (dashed) m fixed

$$M_h \sim \Sigma_0 r_h^2$$

and surface density (solid) Σ_0 fixed

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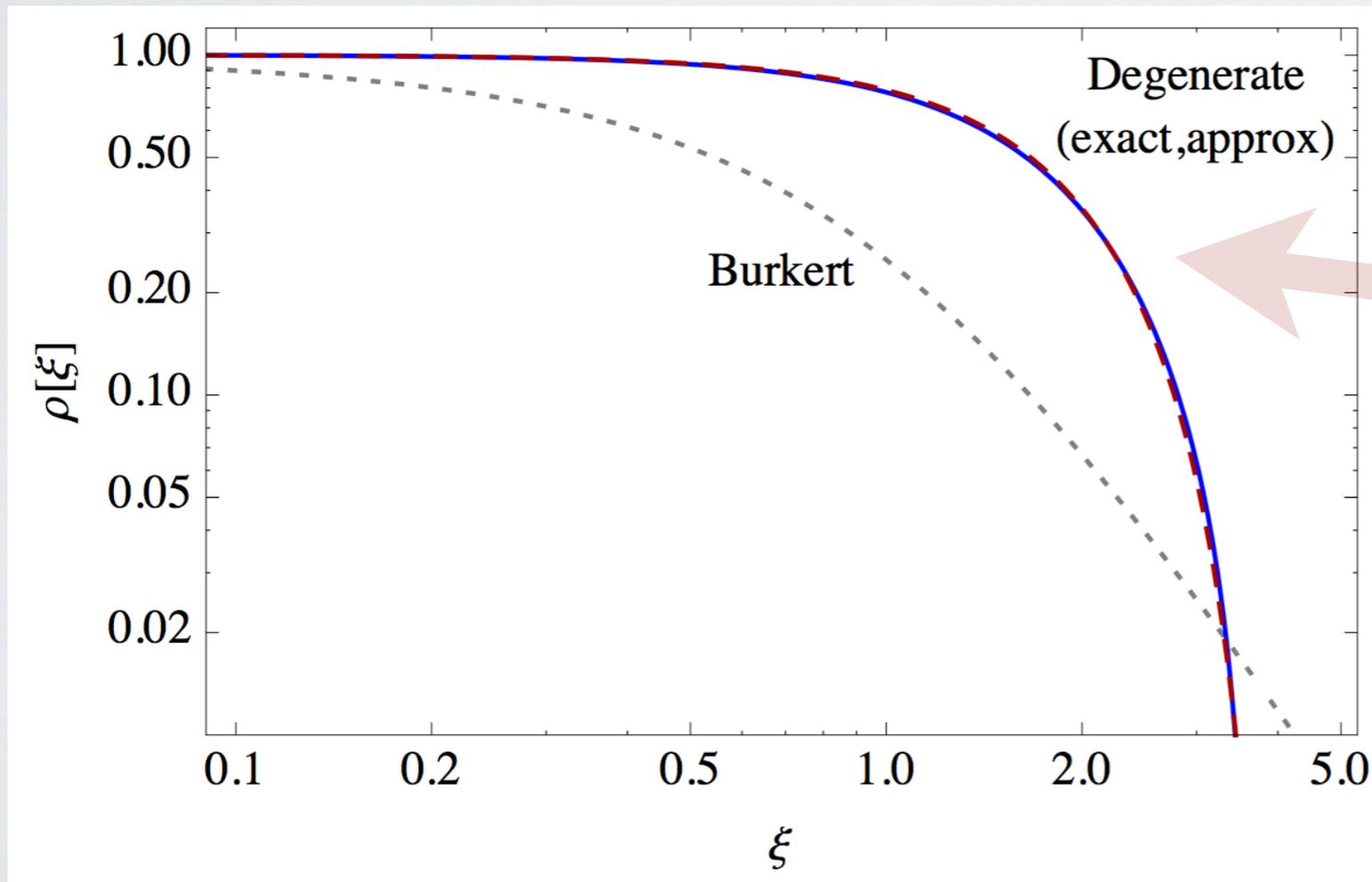
Degeneration limit (dashed) m fixed

$$M_h \sim \Sigma_0 r_h^2$$

and surface density (solid) Σ_0 fixed

SO, QUANTUM NATURE PREDICTS

- A minimum for total mass M_h and size R_h
- The shape of fully degenerate profile:



Lane-Emden solution.
we **approximate**
very well by

$$\rho(\xi) = \rho_0 \cos^3 \left[\frac{\pi}{8} \xi \right]$$

...can we test this profile?

NO: NONTRIVIAL PROBLEM ALREADY TO ESTIMATE THE HALO SIZE/MASS

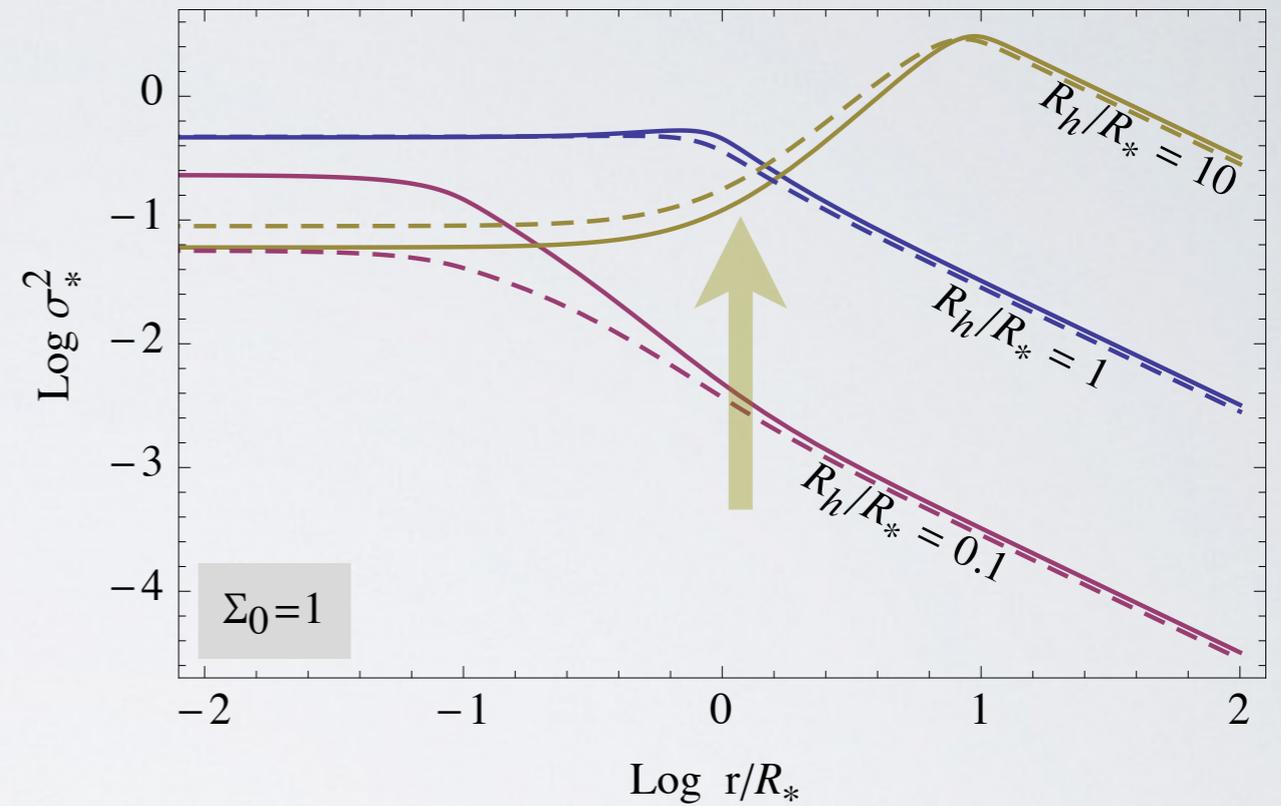
- **We observe the STAR velocity DISPERSION**
(line of sight only, σ_r)
- Jeans equation predicts it, from given mass model $M(r)$

$$\left(\frac{\partial}{\partial r} + \frac{2\beta}{r} \right) (n_* \sigma_r^2) = -n_* \frac{GM(r)}{r^2}$$

- *Stellar dispersion anisotropy β unknown* $\beta \equiv 1 - \sigma_{\perp}^2 / \sigma_r^2$
- *and it's hard to measure stars for small galaxies*

PREDICTED STAR VELOCITY DISPERSION WITH OR WITHOUT ANISOTROPY

- Small or large DM core R_h
too large cores excluded
by constant observed $\sigma_{*,r}^*$



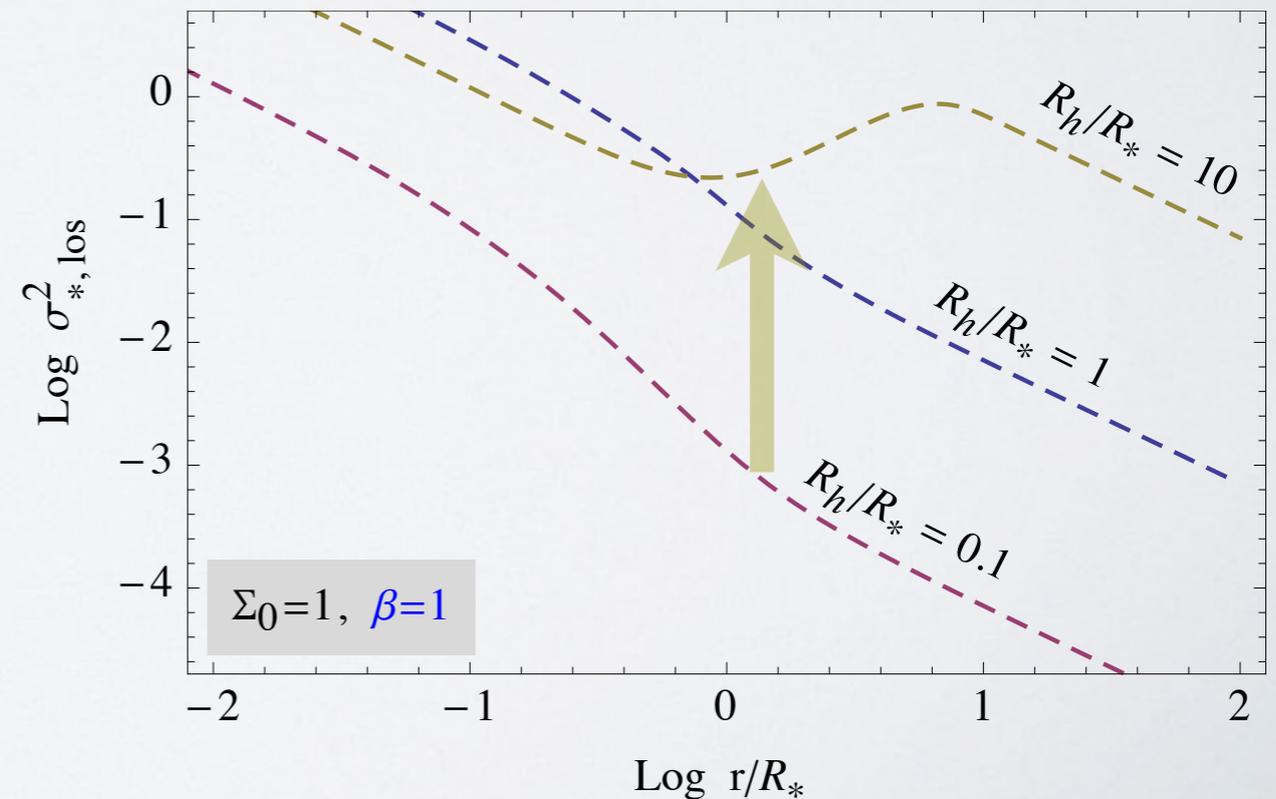
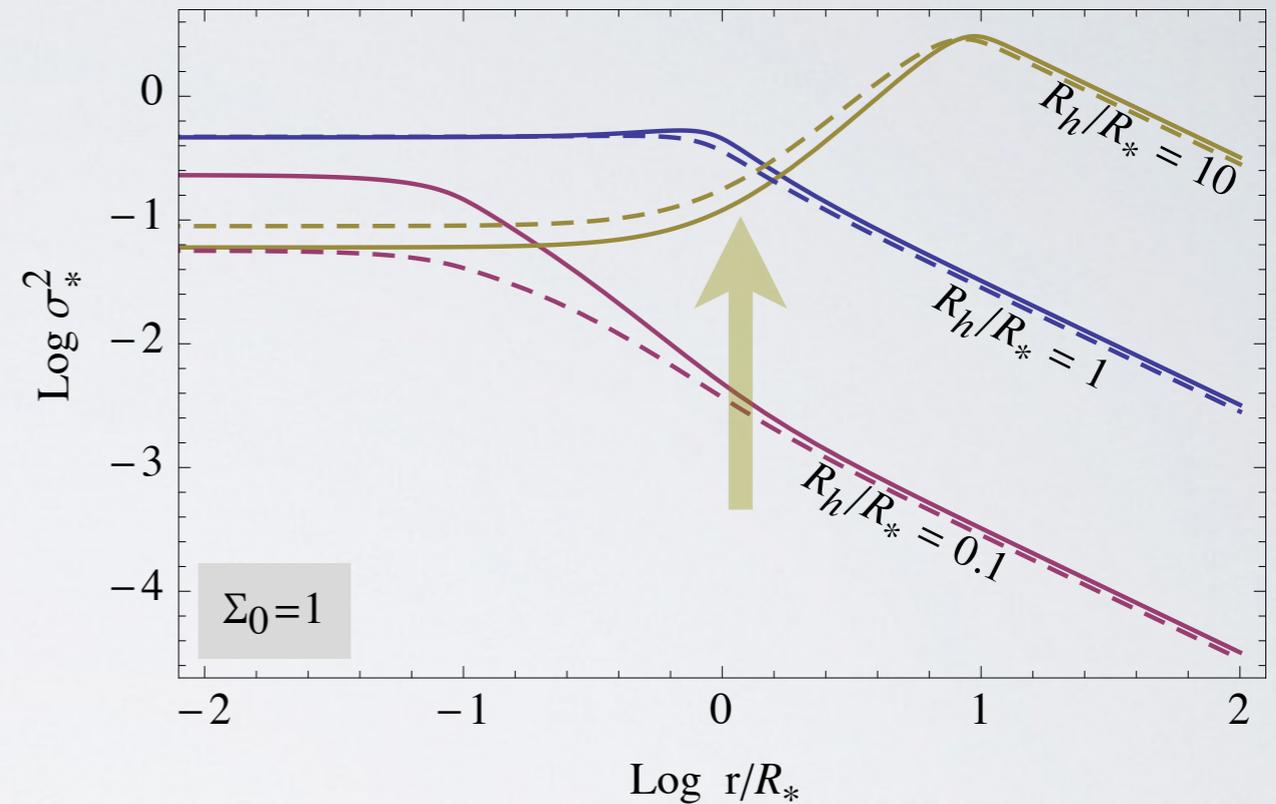
PREDICTED STAR VELOCITY DISPERSION WITH OR WITHOUT ANISOTROPY

- Small or large DM core R_h

too large cores excluded
by constant observed $\sigma_{*,r}$

- Effect of anisotropy, e.g. $\beta=1$

large core gives again
a flattish $\sigma_{*,r}$... !



TOTAL MASS LIMITED BY DYNAMICAL FRICTION

Satellites would have fallen in the MW halo...
...due to gravitational friction

[Chandrasekar formula, e.g. Binney Tremaine 2008 Read+ '06; Just '11, etc]

• Time:

$$t_{\text{fric}} = \frac{10^{10} \text{ y}}{\ln \Lambda} \left(\frac{D}{60 \text{ kpc}} \right)^2 \left(\frac{v}{220 \text{ km/s}} \right) \left(\frac{2 \cdot 10^{10} M_{\odot}}{M_{\text{h}}} \right)$$

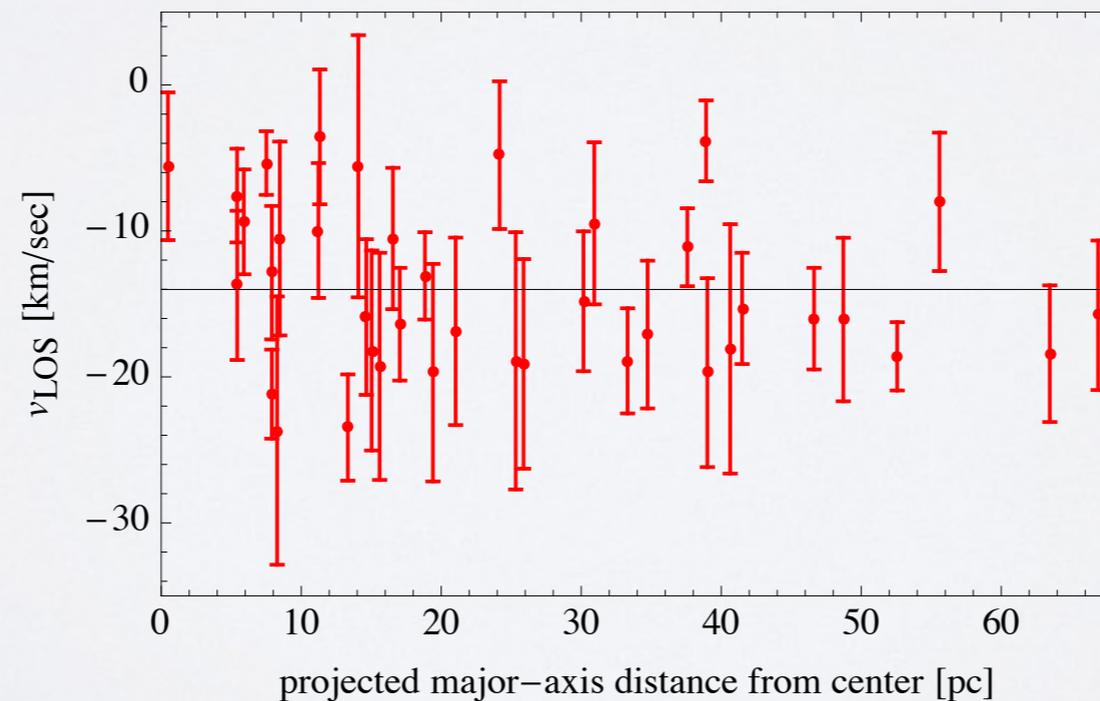
should be larger than the age of Galaxy $\sim 10^{10}$ y.

• Puts a limit on halo mass M_{h}

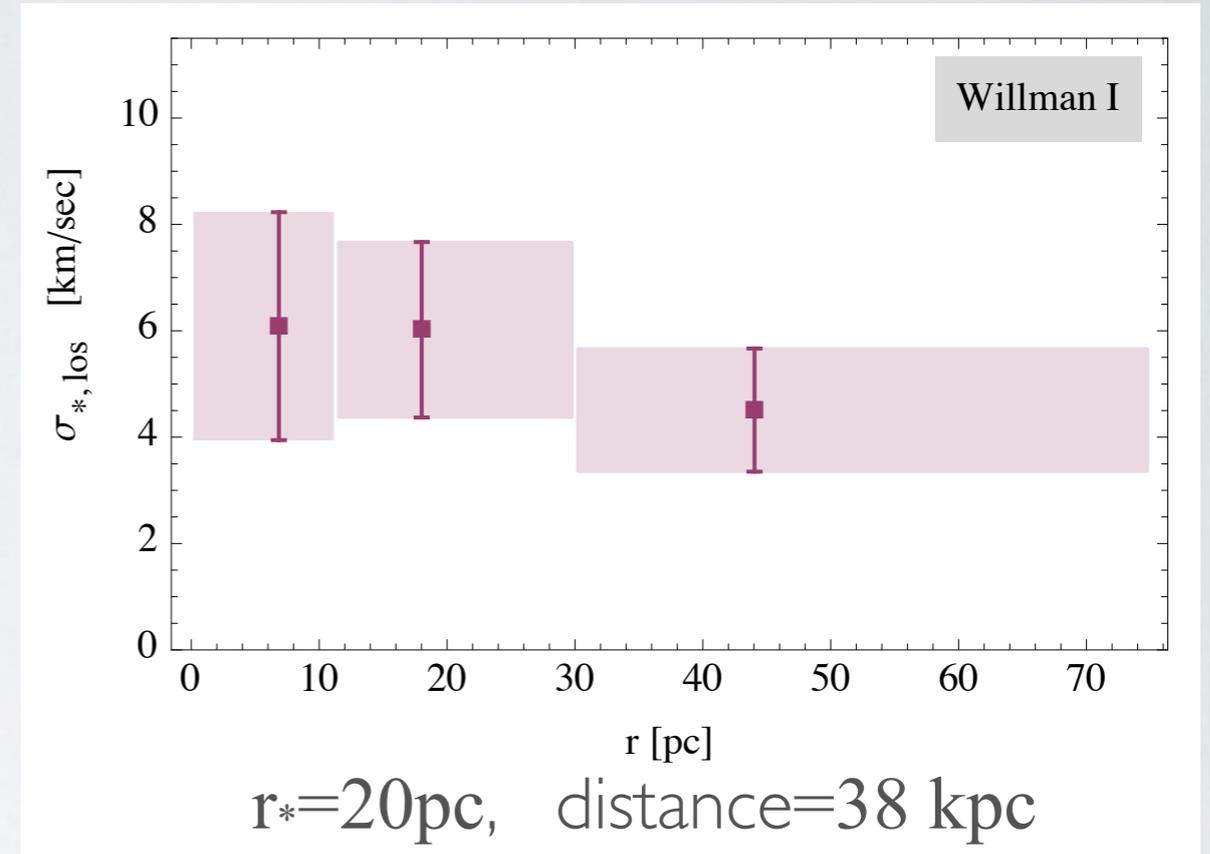
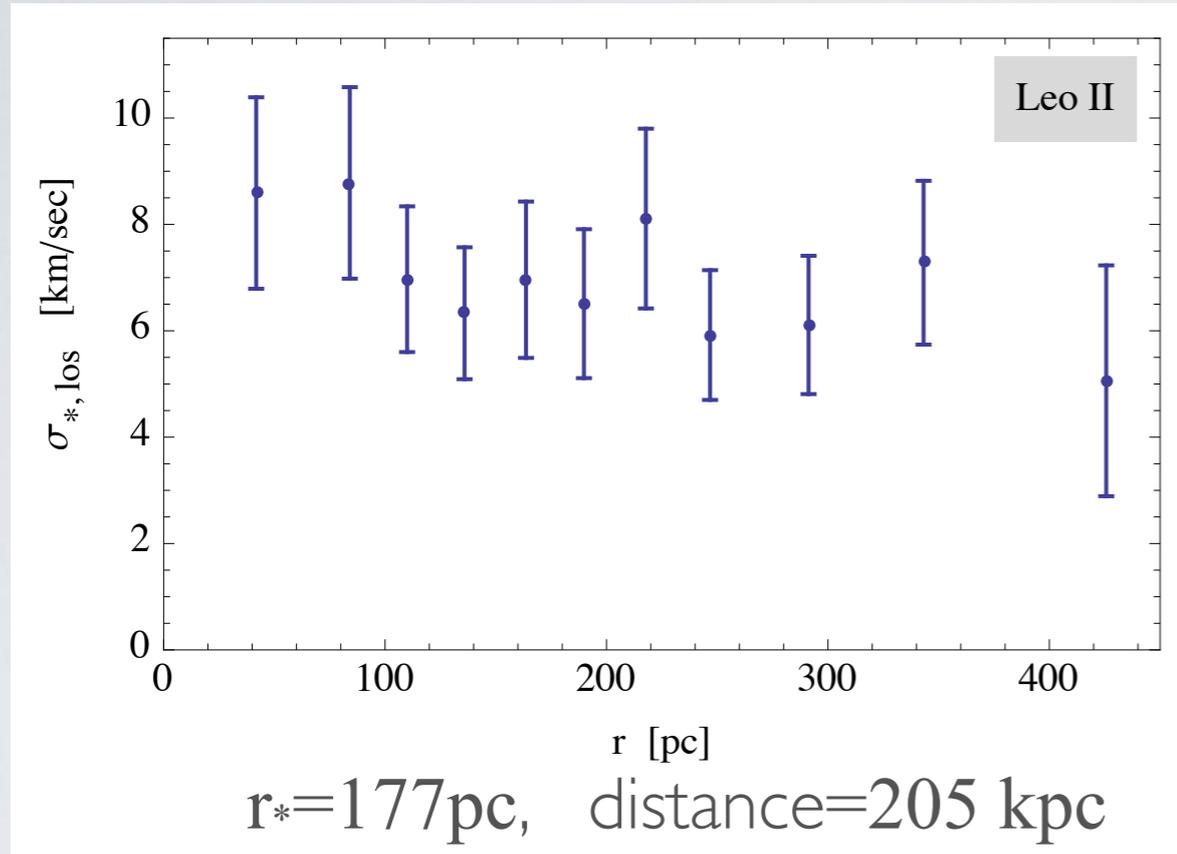
[Gerhard Spergel '92]

Are rising velocity dispersion profiles allowed?

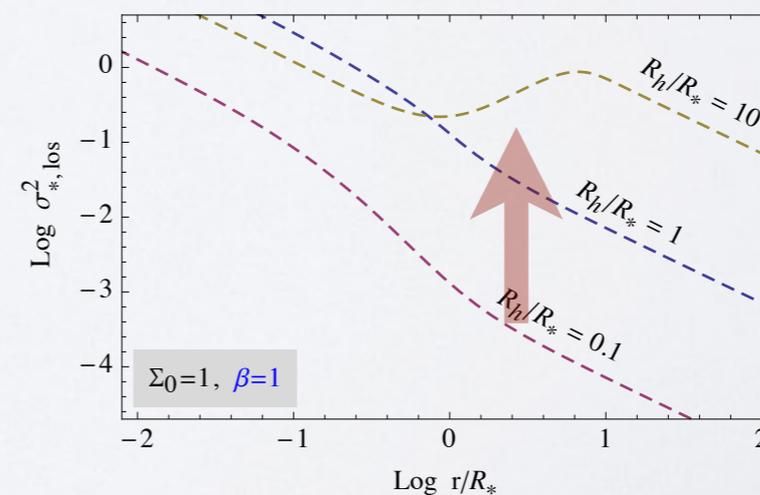
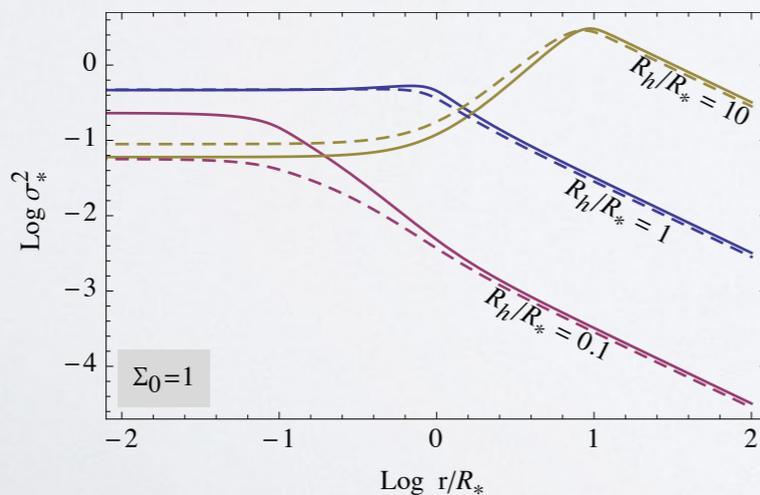
Compare with data



LEO II , WILLMAN I

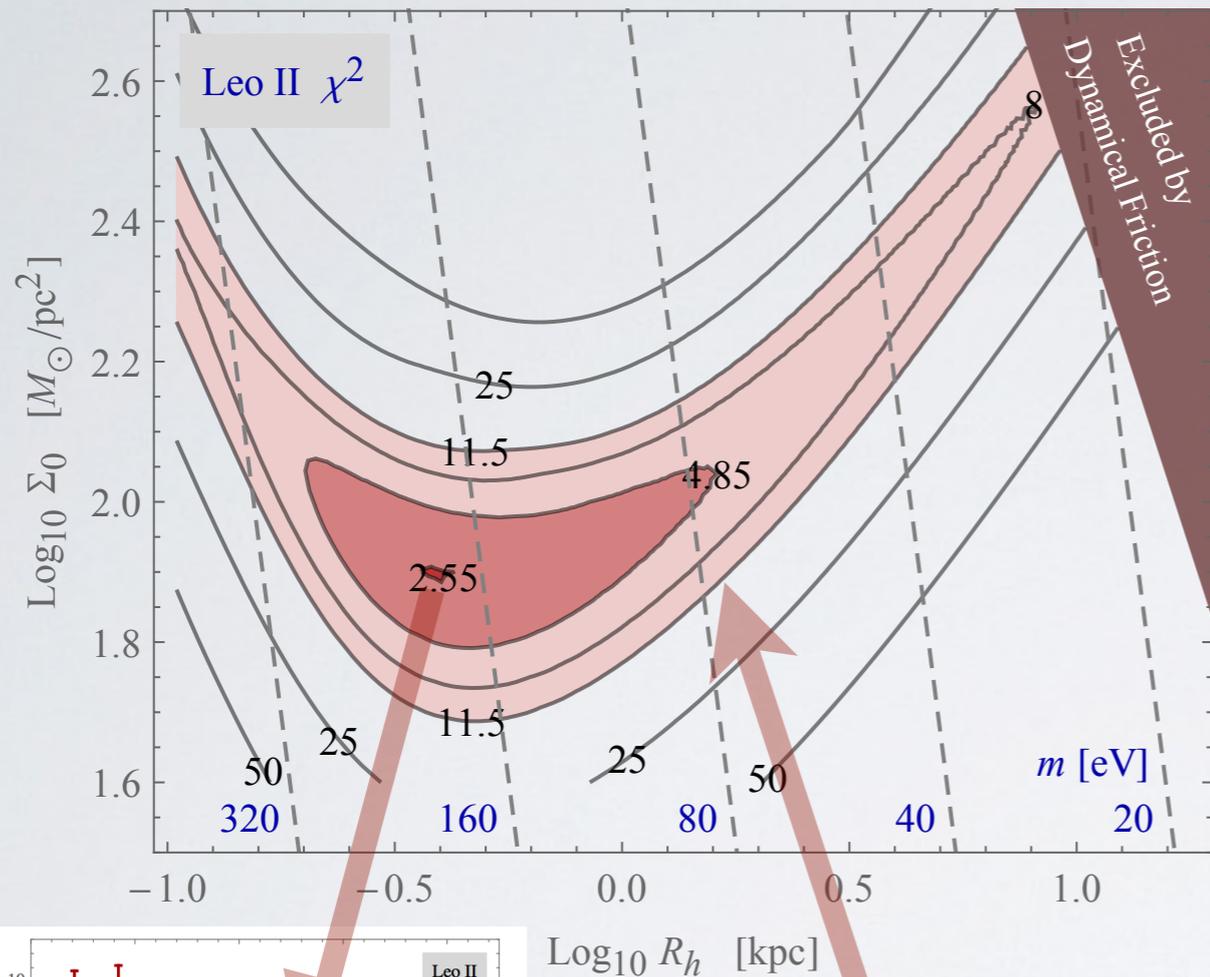


constrain R_h, M_h, m by fitting with predicted profiles



MARGINALIZING BETA β - LEO II

Exclusion by data is not Parameter estimation



1σ exclusion

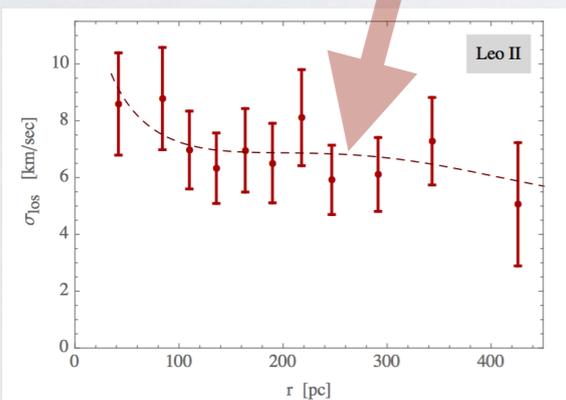
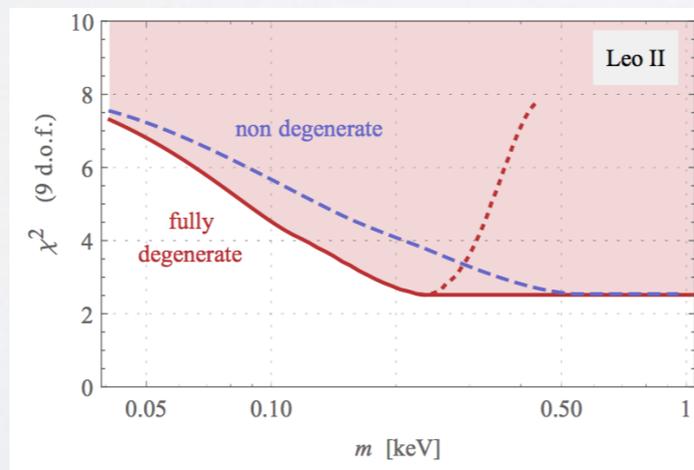
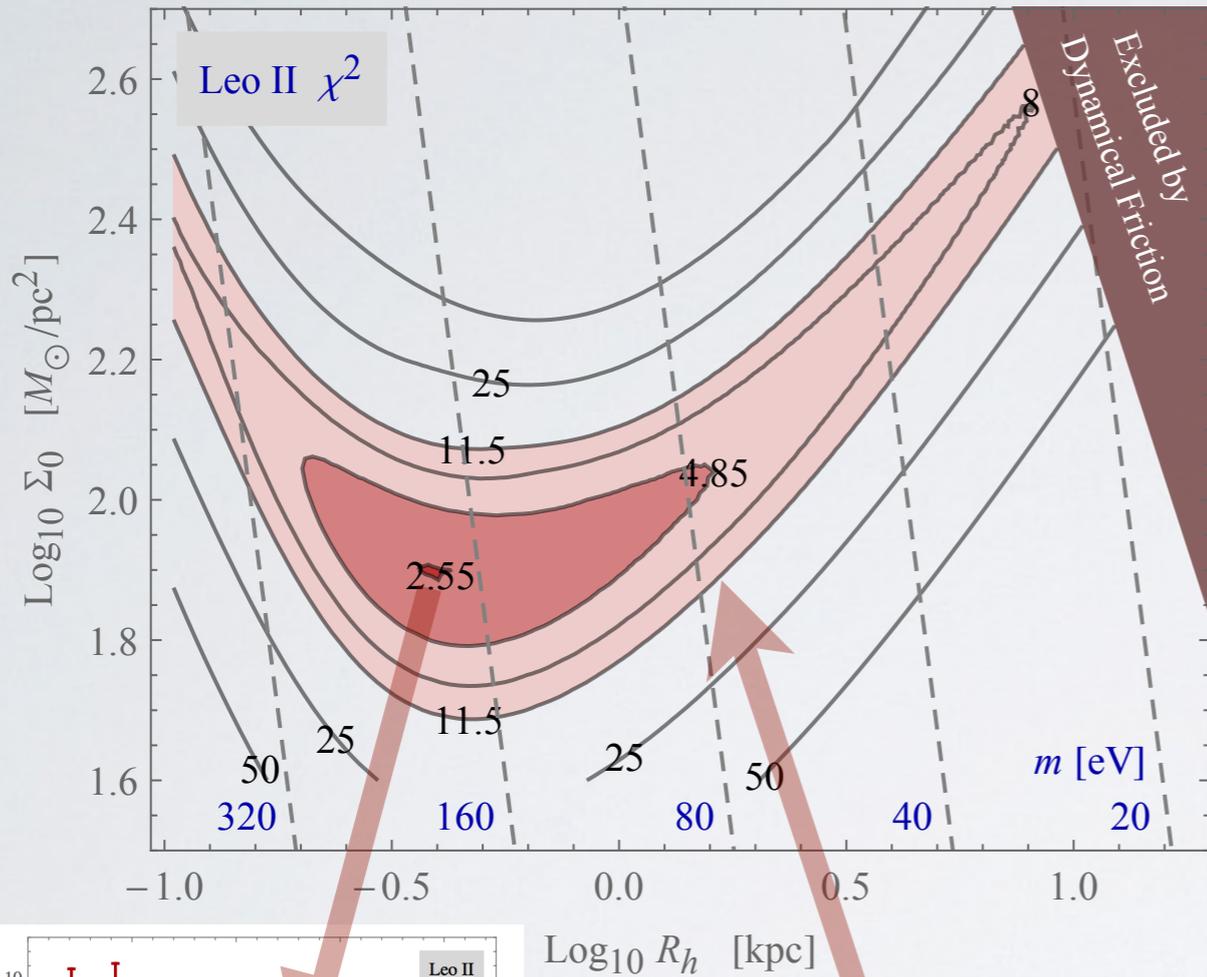


FIG. 4. Stellar line-of-sight velocity dispersions for Leo II. The dashed line represents the best fit, achieved for $\beta = 0.6$.



MARGINALIZING BETA β - LEO II

Exclusion by data is not Parameter estimation



due to $\beta \rightarrow 1$

No upper limit on R_h

No lower limit on m

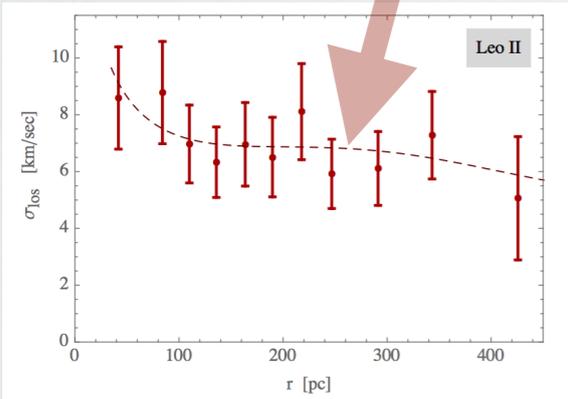
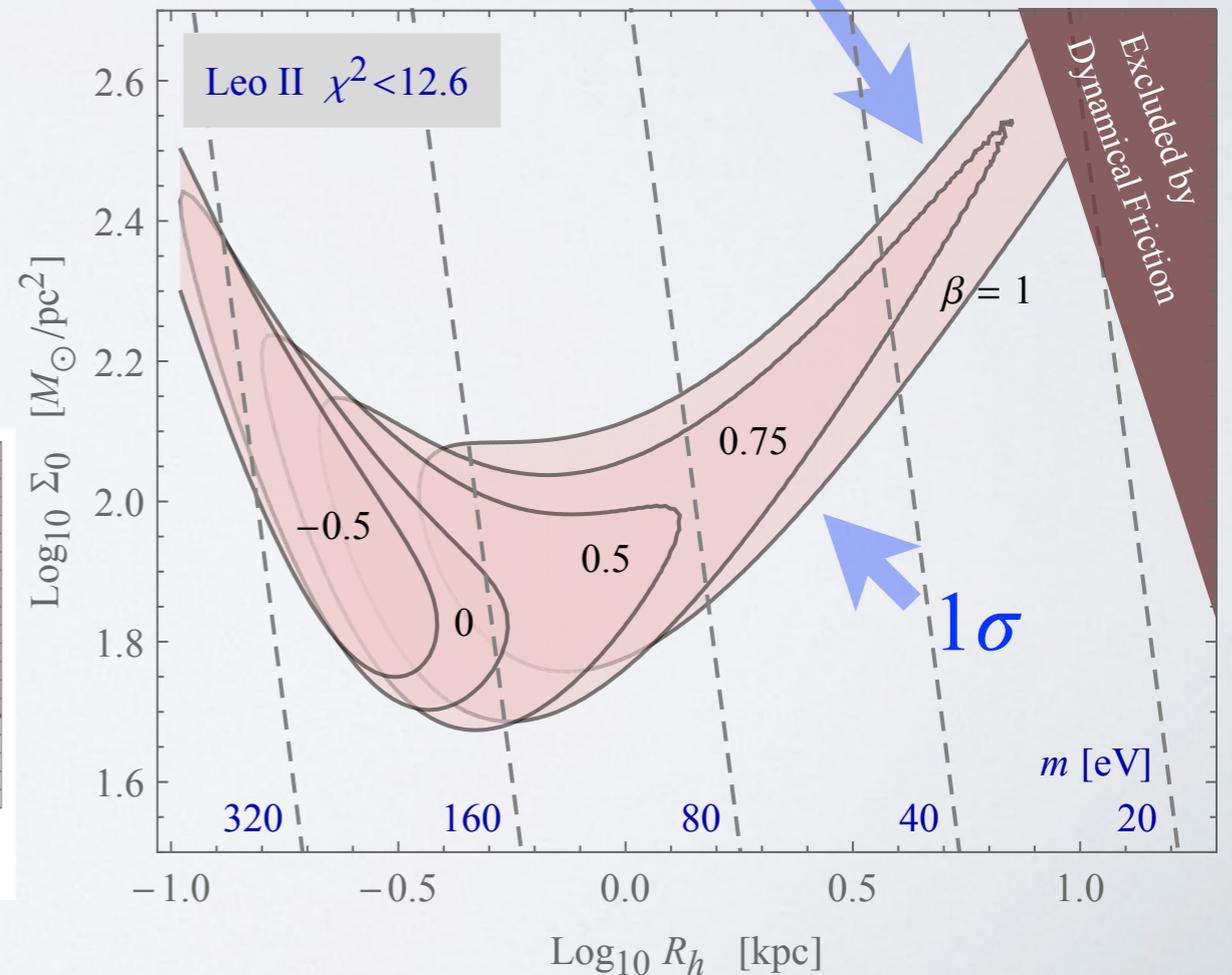
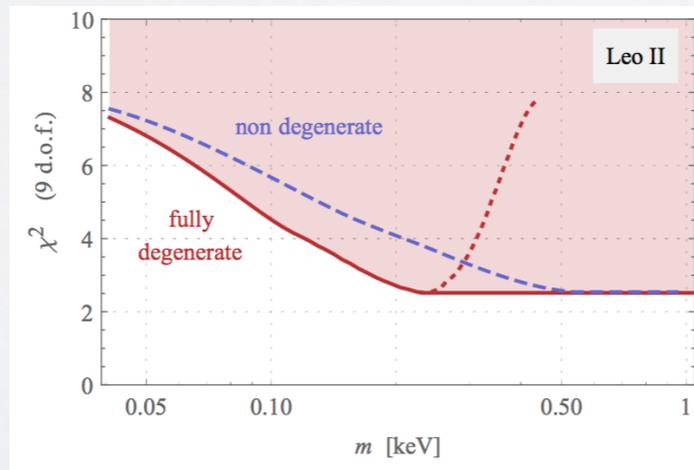


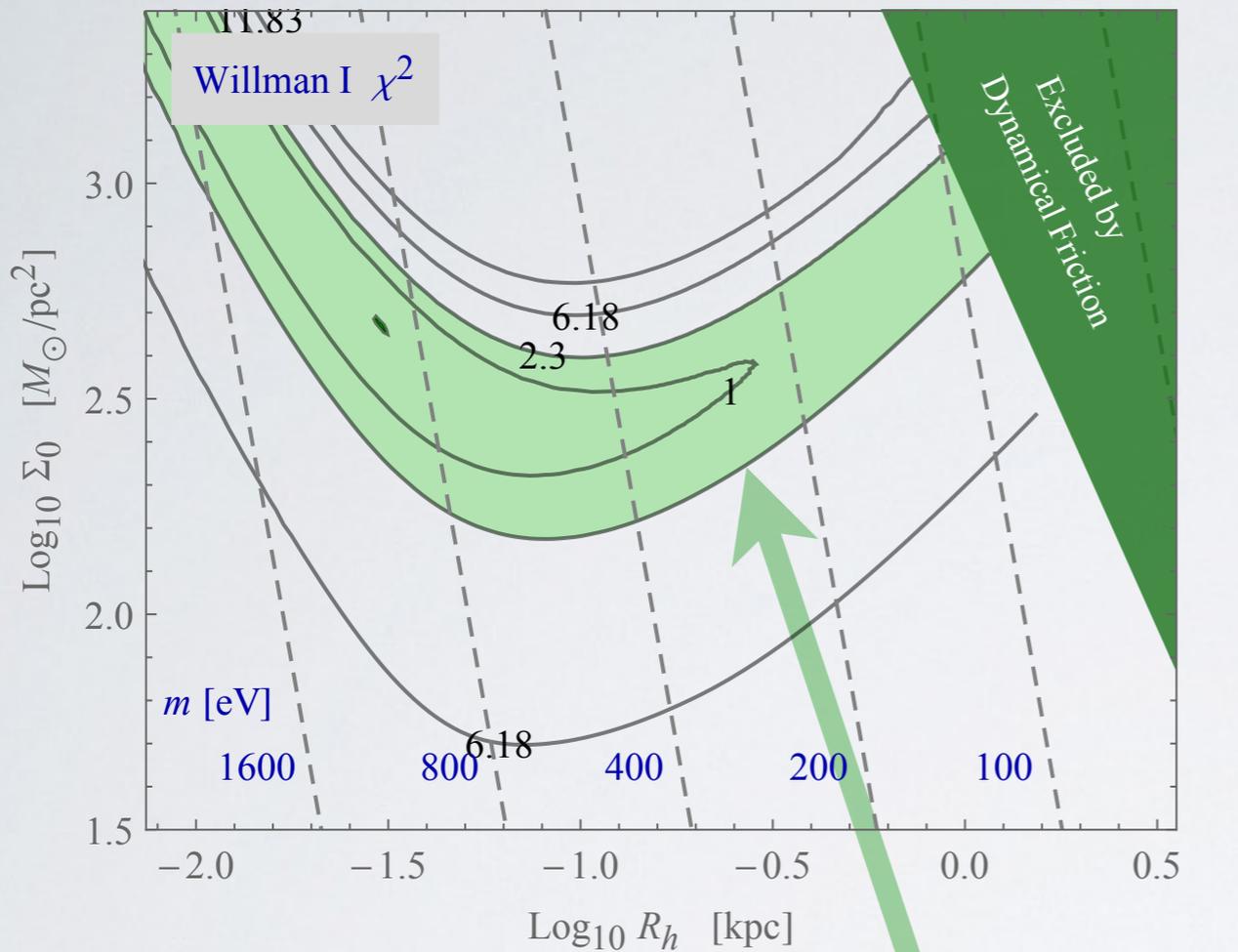
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1σ exclusion

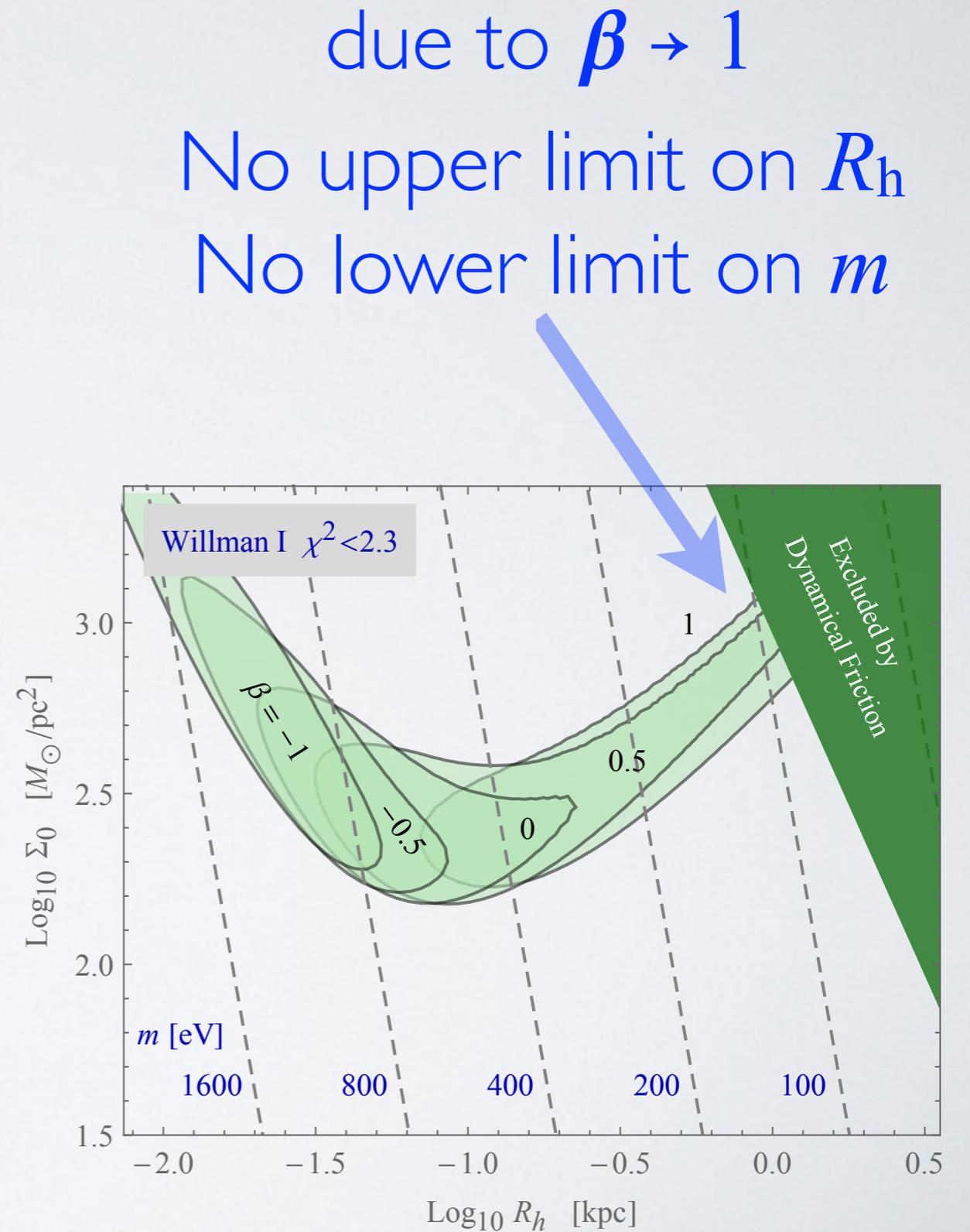


MARGINALIZING BETA β - WILLMAN I

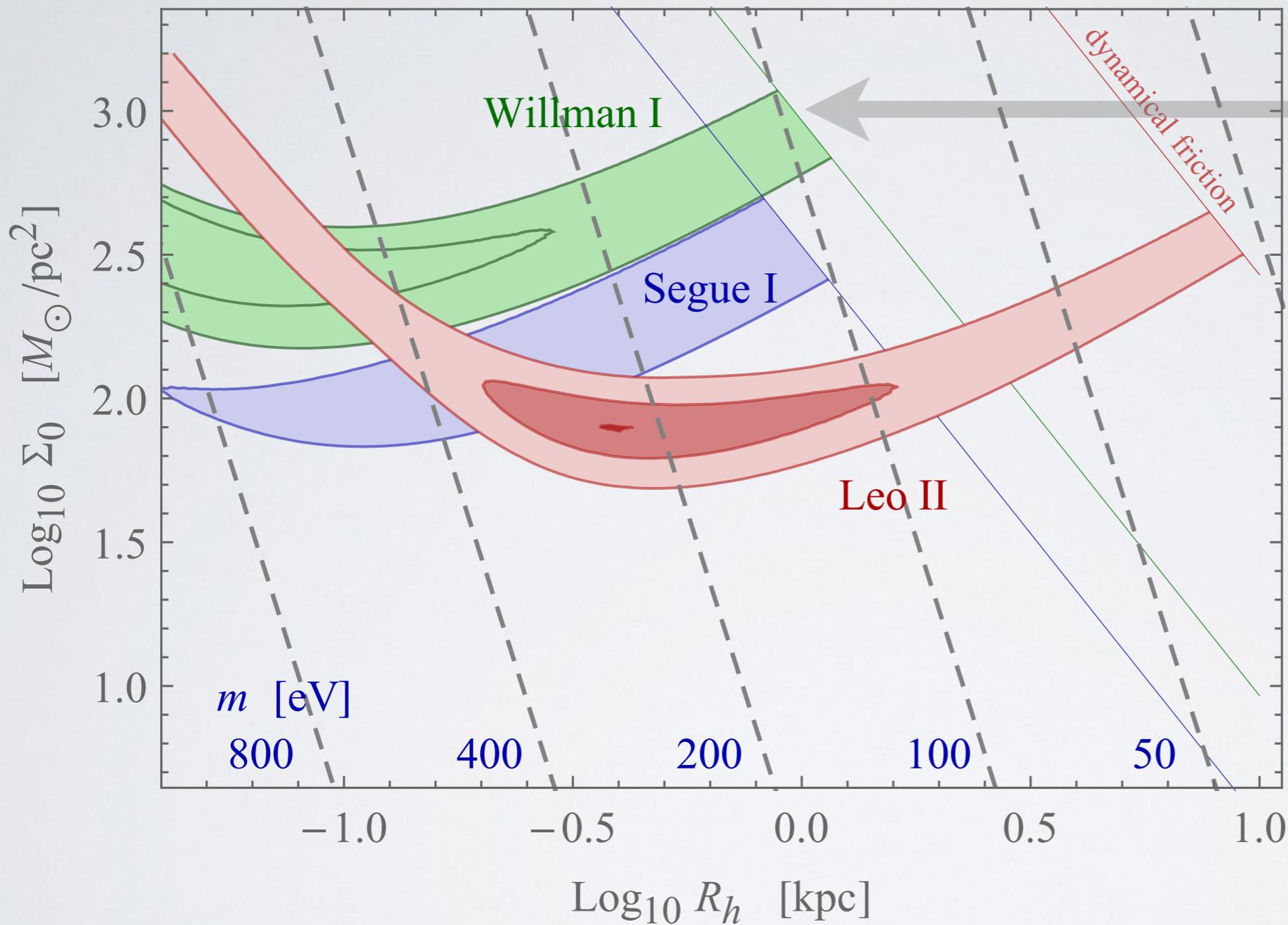
Exclusion by data



1σ exclusion



SO, BOUND ON DM MASS m



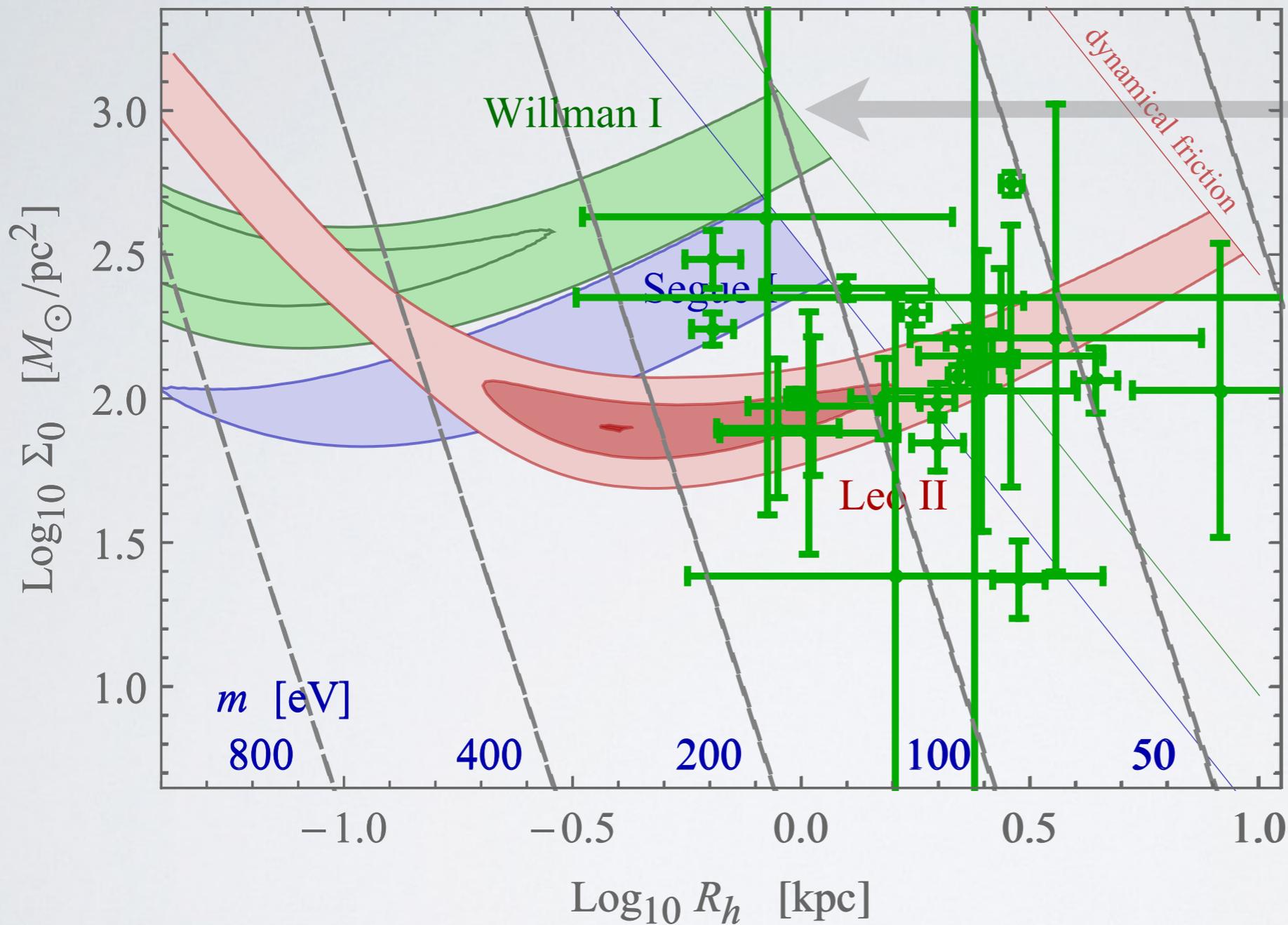
Tremaine Gunn
saved by
Dynamical Friction

...substantially
weakened to
 $m \gtrsim 100 \text{ eV}$

dSph
may be larger...

(even if one does not
want $\gtrsim \text{kpc}$ size)

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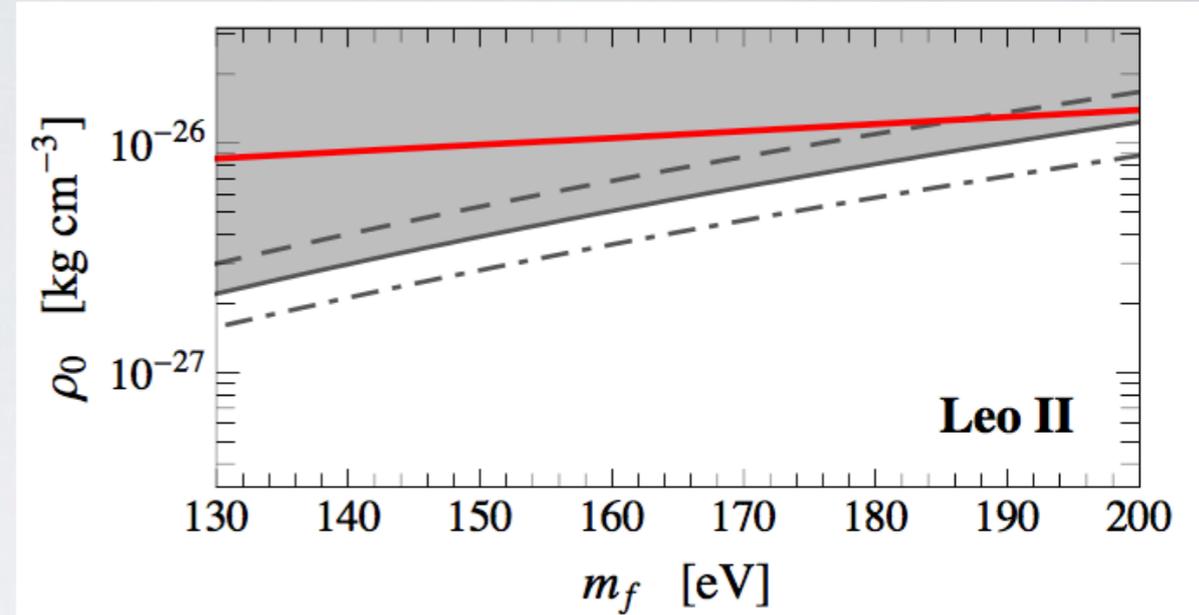
(even if one does not
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Nothing stronger from Dwarf Disk galaxies [Little Things '15 HI survey]

RECENT WORKS

[Domcke+ JCAP '15]

$m > 200 \text{ eV}$ from Leo II (?)

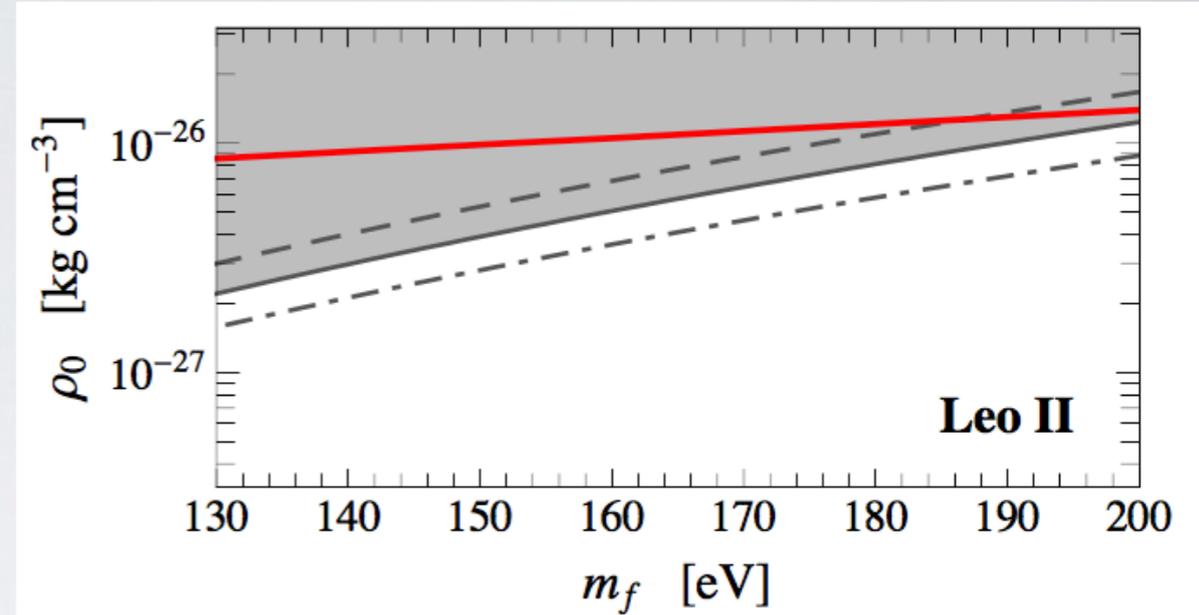


We plot the best-fit value for the central density ρ_0 as a function of the mass m_f , obtained marginalizing over the orbital anisotropy β . The value $m_f = 150 \text{ eV}$ is consistent with the bound $v_F \leq v_\infty^{\text{obs}}$ for all the analyzed dwarf spheroidal galaxy but Leo II. Note that this result

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[Randall+ MNRAS '17]

$m > 100 \text{ eV}$ from Fornax (?)

using multi-population

[Amorisco+ '12]

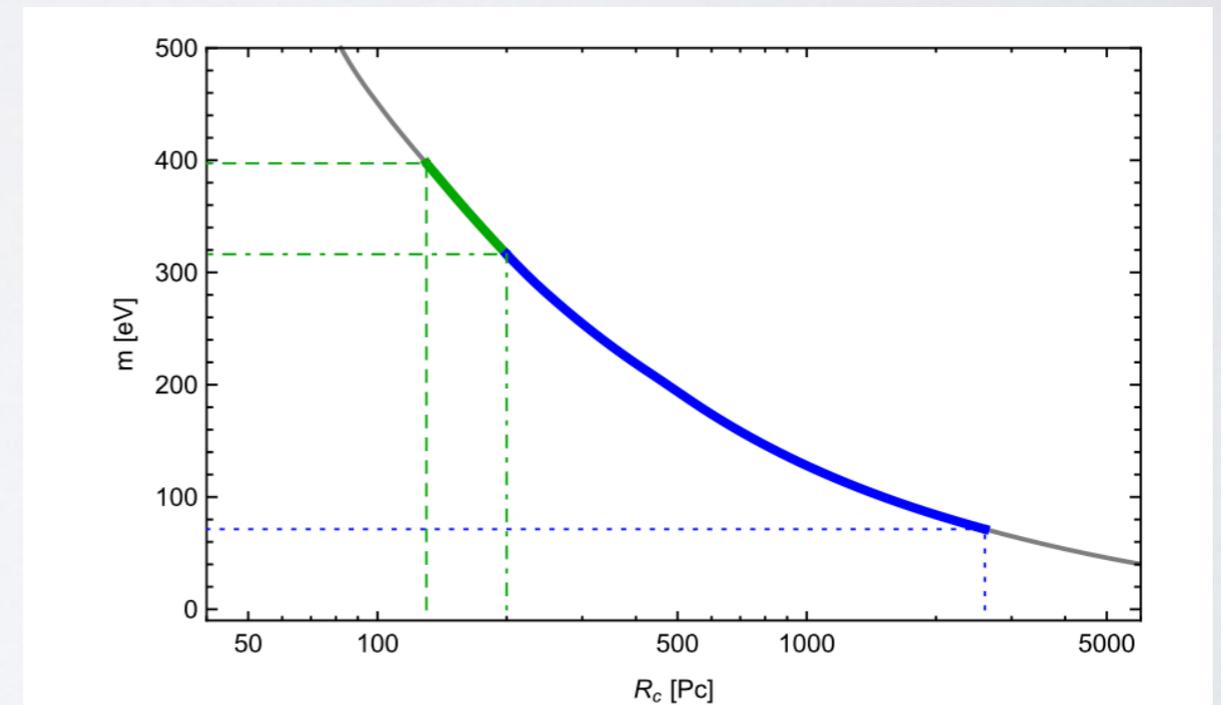


Figure 7. Applying the static solution of Section 2 to the Fornax dwarf galaxy, we show the necessary dark matter mass m as a function of the desired core radius R_c . The blue part of the curve indicates the preferred set of R_c from Walker & Penarrubia (2011). The green portion of the curve shows a weaker condition $R_c > 130 \text{ pc}$.

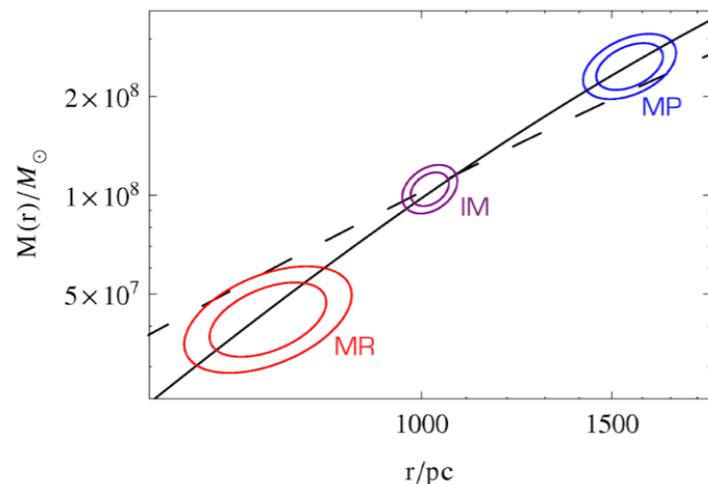
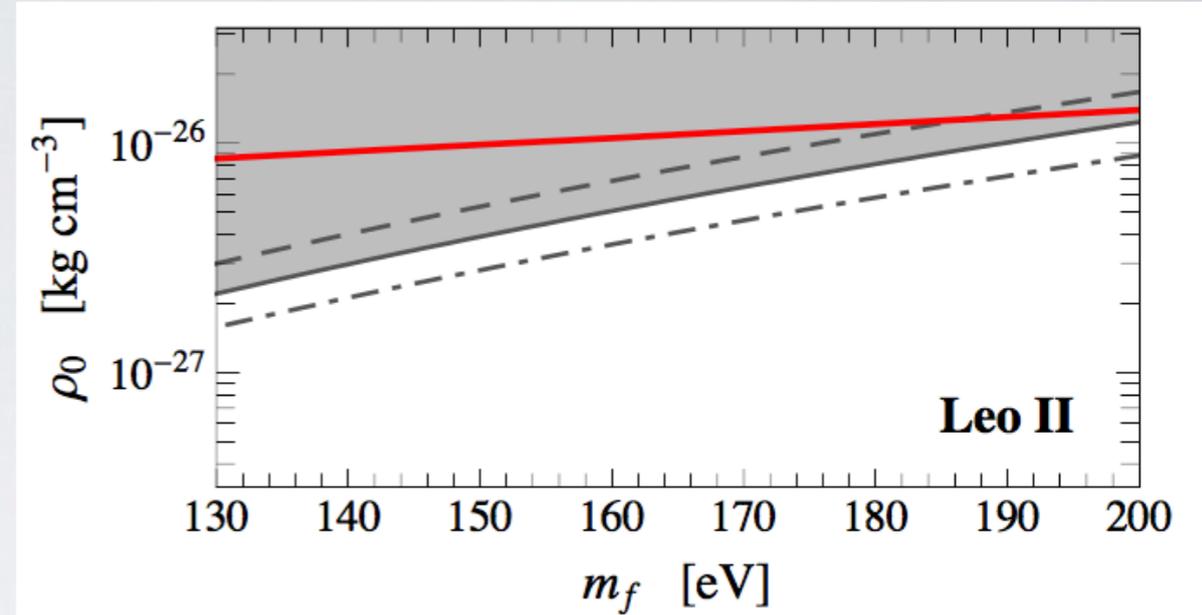


Figure 2. Left panel: estimates of the total enclosed mass $M(r)$ as obtained from the literature. Right panel: estimates of the total enclosed mass $M(r)$ as obtained from the literature.

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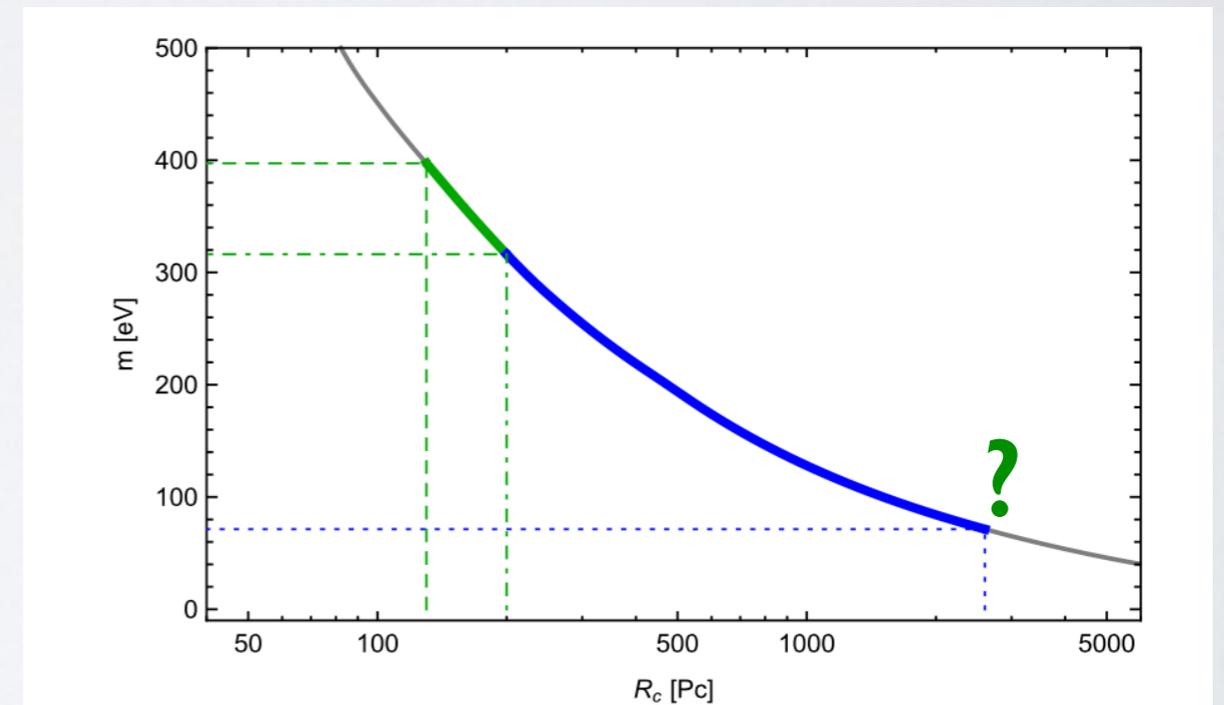
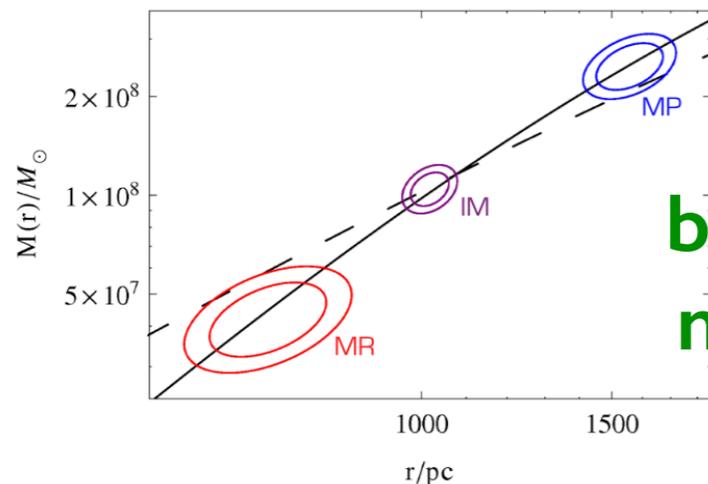


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but large cores
not excluded !

Figure 2. Left panel: estimates of the total enclosed mass $M(r)$ as obtained from the literature. Right panel: best-fit parameters for the dark matter halo.

E.G. SEARCHES FOR X-RAY LINES

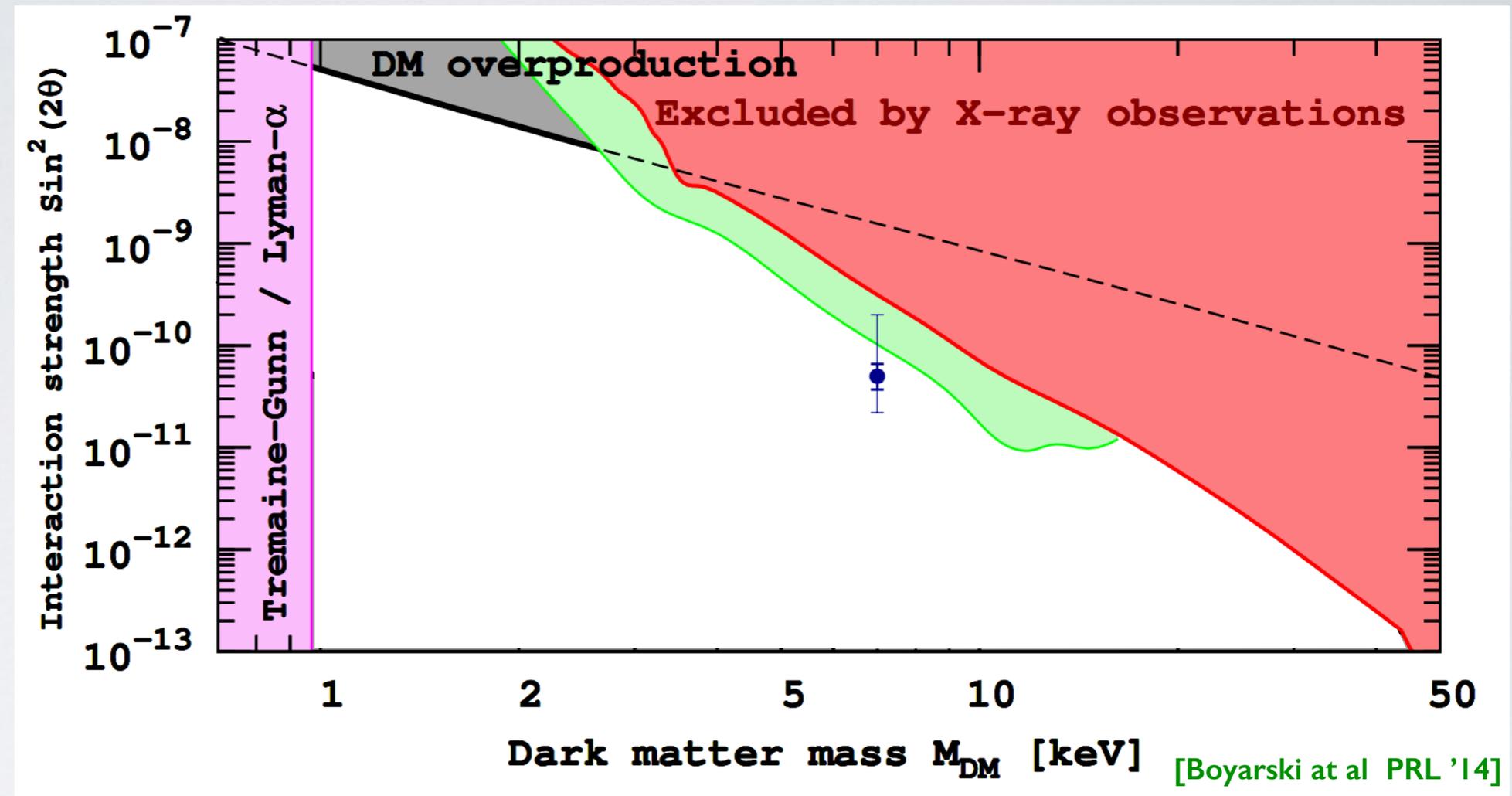
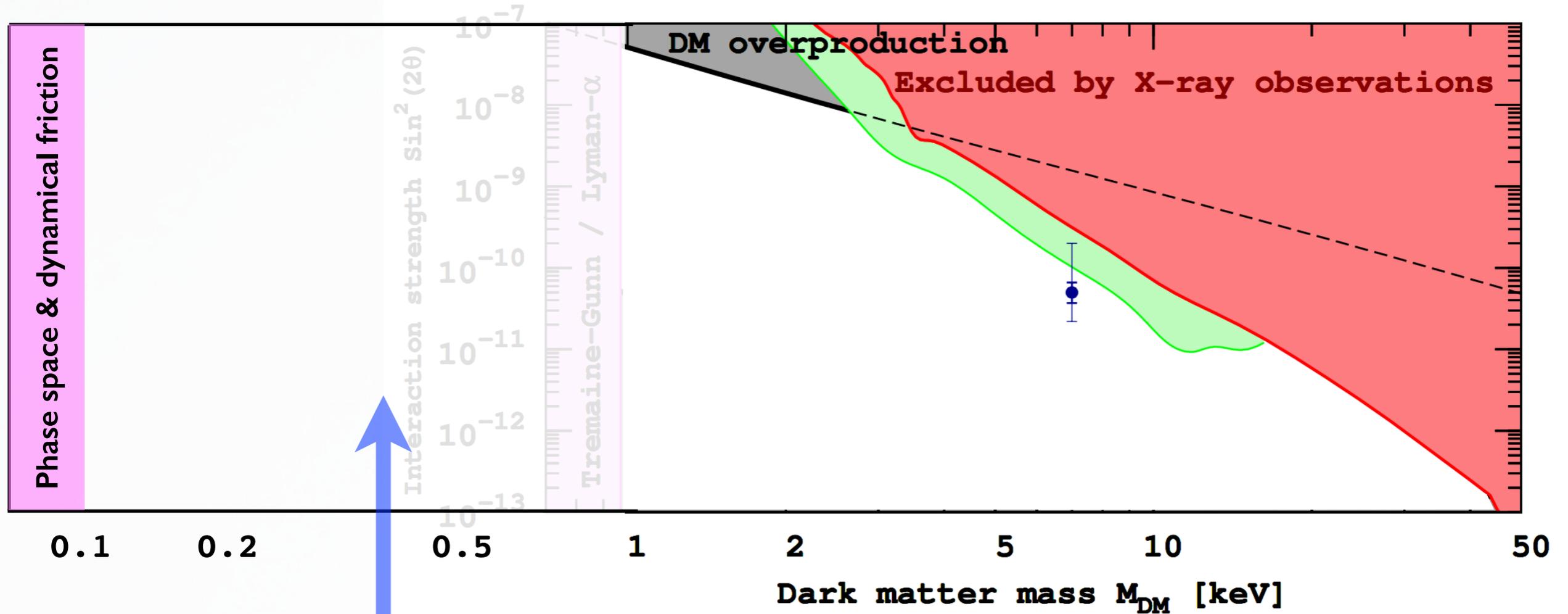


FIG. 4: Constraints on sterile neutrino DM within ν MSM [9]. Recent bounds from [16, 17] are shown in green. Similar to older bounds (marked by red) they are smoothed and divided by factor 2 to account for possible DM uncertainties in M31. In every point in the white region sterile neutrino constitute 100% of DM and their properties agree with the existing bounds. Within the gray regions too much (or not enough) DM would be produced in a minimal model like ν MSM. At masses below ~ 1 keV dwarf galaxies would not form [4, 48]. The blue point would correspond to the best-fit value from M31 if the line comes from DM decay. Thick errorbars are $\pm 1\sigma$ limits on the flux. Thin errorbars correspond to the uncertainty in the DM distribution in the center of M31.

E.G. SEARCHES FOR X-RAY LINES



more space
for sterile neutrinos

The Lyman-alpha bound $m > 1-7$ keV ...
...can be evaded if WDM is cold :) e.g.

- generated via decay

[Patraki-Kusenko '08]

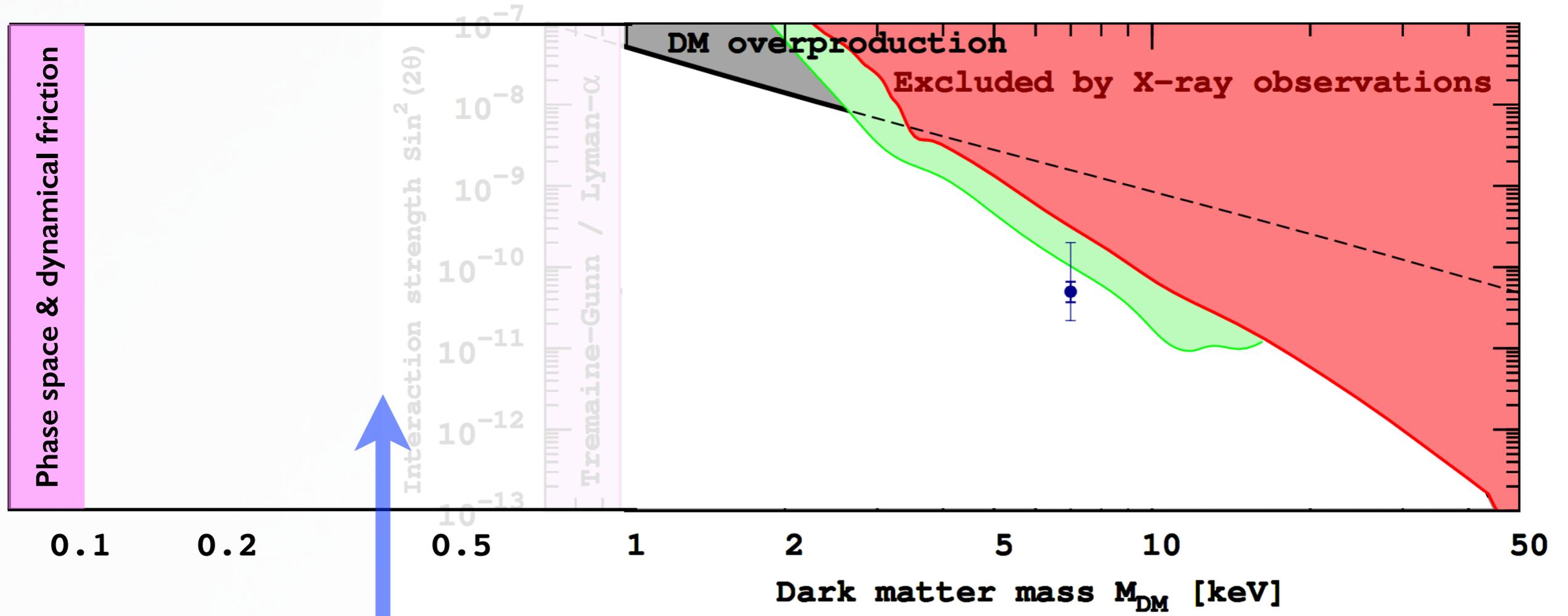
- w/ dilution

[Bezrukov+ '10]

[Nemevsek, Senjanovic, Zhang '12]

- ...

E.G. SEARCHES FOR X-RAY LINES



**more space
for sterile neutrinos**

(and btw how to search for them?)

**The Lyman-alpha bound $m > 1-7$ keV ...
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- generated via decay

[Patraki-Kusenko '08]

- w/ dilution

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- ...

That's all from data.

Then, a serious question is

Are degenerate fermionic galaxies physical?

PHASE SPACE DISTRIBUTIONS

[Navarro Eke Frenk '96]

- For classical models
(\sim maxwellian, intermediate momenta dominate)

- To be compared with
degenerate FD

Lower momenta, Denser:

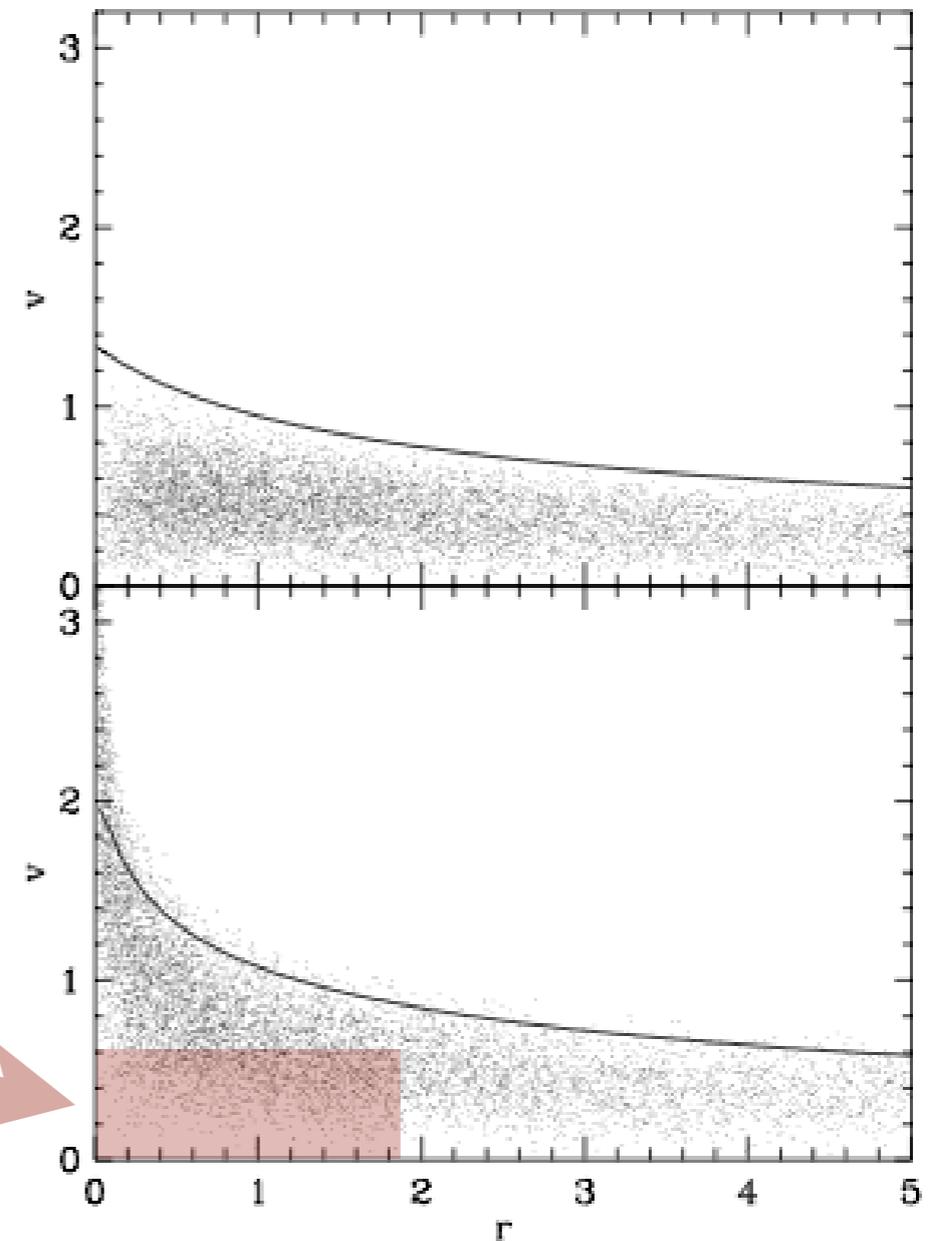
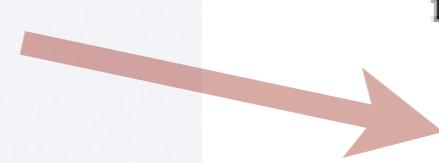


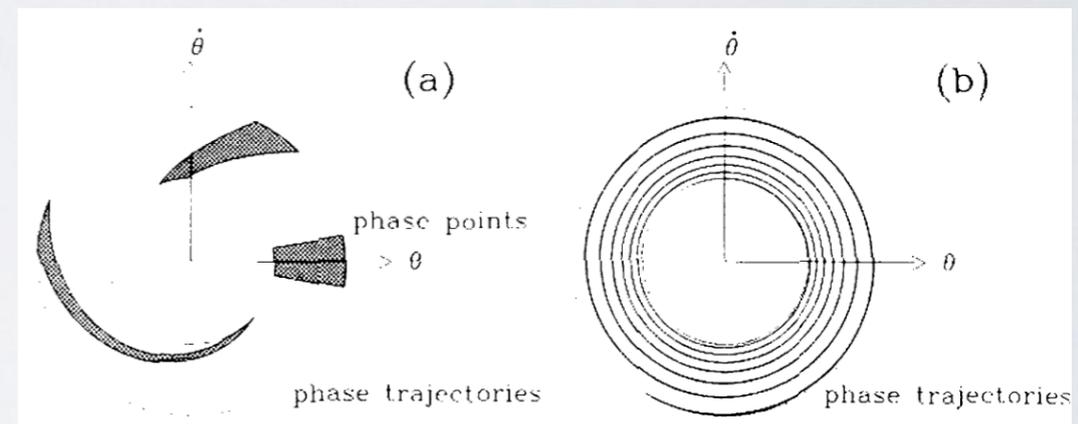
Figure 2. “Phase-space” distribution of halo particles before and after imposing the disk potential (upper and lower panel, respectively). The solid line in each panel shows the escape velocity

**Will the distribution collapse?
How?**

RELAXATION IN GALACTIC DYNAMICS

- **Encounters?** No - play a role only for few objects
($T = T_{\text{crossing}} 0.1 N / \log N$, here $N \sim 10^{70}$, very large)
Thus, we are *collisionless*

- **Phase mixing?** *Relaxation for ignorance.*
Not relevant to get degeneration
(phase space has to be fully filled)



- **Violent relaxation?**
changes energy per unit mass (i.e. independent of mass)
(collision independent - assumes motion in a changing potential)
- **In any case, would need interaction**
e.g. dissipation, to increase phase-space density (SIMD \rightarrow fermi cores?)

SO, CONCLUSIONS

- Quantum degenerate fermionic DM may avoid cusps in dwarfs
- Revisiting lower bound from existence of small galaxies:
Tremaine-Gunn + Dynamical Friction
 $m > 100\text{eV}$
challenging Direct Search
 - Missing satellite problem (helps SIDM?)
hint to upper bound $m < \text{few keV} ?$
- Smallest galaxies are the frontier - confrontation with data hard
dispersion anisotropy the main nuisance.
- Physics of fermionic galaxy formation the outstanding question

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Thanks!

OTHER DSPH

Using triaxial fits to dwarf spheroidal galaxies [Hayashi et al. 2016]

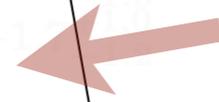
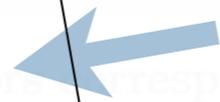
Table 1. Estimated lower bound on the fermionic DM mass m from a number of dwarf spheroidal galaxies, adopting the central densities as determined in Hayashi et al. (2016).

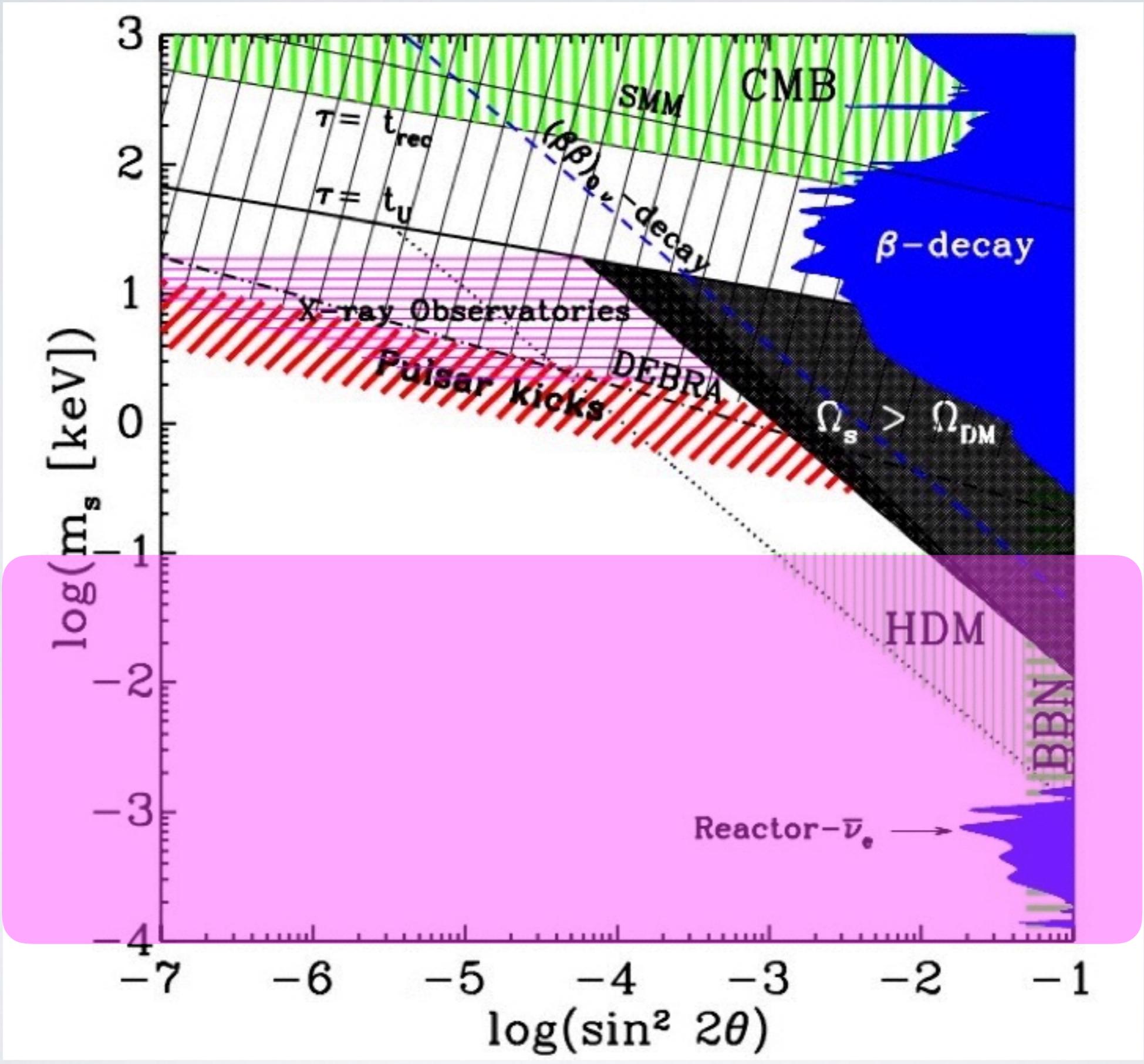
DSph	Log ρ_0 [M_\odot/pc^3]	d_0 [kpc]	lower bound on m
Triangulum II	0.3	30	127 eV
Segue 1	-0.4	32	100 eV
Leo T	-0.6	417	26 eV
Reticulum II	-0.8	32	89 eV
Ursa Major I	-0.8	106	49 eV
Coma Berenices	-0.8	44	76 eV
Sculptor	-0.8	86	54 eV
Fornax	-0.8	86	38 eV
Ursa Major II	-1.1	147	80 eV
Leo I	-1.2	32	27 eV
Canes Venatici II	-1.2	254	34 eV
Hercules	-1.3	151	37 eV
Pisces II	-1.4	132	30 eV
Leo IV	-1.4	180	30 eV
Leo II	-1.4	180	31 eV
Draco II	-1.5	158	25 eV
Sextans	-1.7	233	82 eV
Canes Venatici I	-1.7	20	38 eV
Carina	-1.9	86	22 eV
Bootes I	-2.	224	33 eV
Leo V	-2.2	106	39 eV
Draco	-2.2	66	22 eV
Hydra II	-2.4	178	33 eV
Segue 2	-2.6	76	22 eV
	-2.7	134	43 eV
	-3.1	35	
	-3.2		

Table 2. Parameter constraints for dwarf spheroidal galaxies.

Object	$-\beta_z$	α	i [deg]
Classical d			
Carina	$-1.0^{+0.4}_{-0.2}$		71^{+14}_{-15}
Fornax	$-0.2^{+0.1}_{-0.2}$		72^{+12}_{-15}
Sculptor	$-0.3^{+0.2}_{-0.3}$		68^{+16}_{-12}
Sextans	$-0.6^{+0.4}_{-0.5}$		72^{+13}_{-13}
Draco	$-1.0^{+0.2}_{-0.1}$		59^{+15}_{-7}
Leo I	$-1.2^{+0.6}_{-0.4}$		60^{+19}_{-14}
Leo II	$-1.0^{+0.5}_{-0.4}$		62^{+19}_{-17}
Ultra faint dwarf			
Segue 1	$-2.0^{+0.8}_{-0.6}$		73^{+11}_{-11}
Segue 2	$-1.4^{+1.0}_{-1.0}$		54^{+23}_{-16}
Boötes I	$-0.7^{+0.5}_{-0.6}$		77^{+9}_{-11}

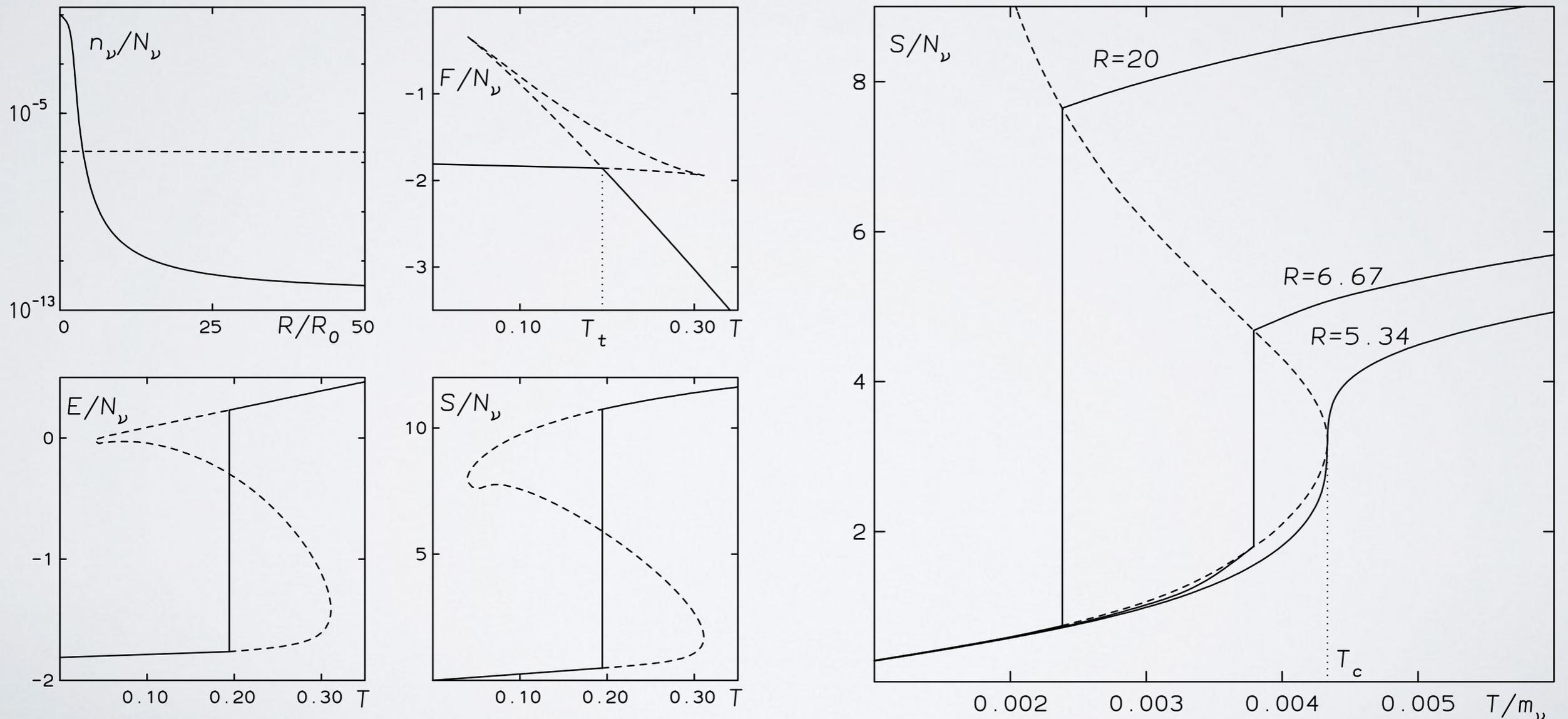
Adding dynamical friction bound





PHASE TRANSITION TO DEGENERATE?

possible, because gravity is attractive [Hertel Thirring '71]



[Bilić Viollier '98]

RELAXATION IN GALACTIC DYNAMICS

What about for fermions?

- Fermions interact only with near-fermi-surface states, so even reduced encounters? (and slow ones bounce off)
- Violent relaxation only possibility? (collisionless interaction)
But are timescales of Potential variation sufficiently long?
Still an open problem it seems [Chavanis '01-'03]
- BTW: violent relaxation leads to Fermi Dirac - like distribution, even for bosons... [Lynden-Bell '67]
(thus, we may say it's compatible)

SO IS IT ACTUALLY REALIZED?

Favourable (free)energy budget necessary for phase transition, not sufficient.

Self-gravitating systems like DM halos are **intrinsically non equilibrium...**

So what matter are the timescales... **Relaxation, thermalization, evaporation. ?**

- Fermionic jeans instability has lower k bound, degeneracy historically relevant
[Chavanis+ 1409xxxx]
- Ideal violent relaxation leads to core plus $1/r^2$ [Lynden Bell '67]
but incomplete violent relaxation can lead to large distance cutoff
as also evaporation
- Simulations of classical violent relaxation lead to core plus $1/r^4$
[Henon '64;van Albada+ '82; Roy+ '04; Joyce+'09]
due to thermalization + evaporation after core formation (but it appears to be slow?).

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Looking forward to quantum simulations?